

Progress in Theory on Rare Decays

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Flavor in the Standard Model and Beyond

$$\begin{aligned}\mathcal{L}_{\text{SM}} \sim & \Lambda^4 + \Lambda^2 H^2 + \lambda H^4 \\ & + \bar{\Psi} \not{D} \Psi + (D_\mu H)^2 + (F_{\mu\nu})^2 + F_{\mu\nu} \tilde{F}^{\mu\nu} \\ & + Y H \bar{\Psi} \Psi\end{aligned}$$

Flavor in the Standard Model and Beyond

The diagram illustrates the Standard Model Lagrangian \mathcal{L}_{SM} and its associated theoretical problems. The Lagrangian is given by:

$$\mathcal{L}_{\text{SM}} \sim \Lambda^4 + \Lambda^2 H^2 + \lambda H^4 + \bar{\Psi} \not{D} \Psi + (D_\mu H)^2 + (F_{\mu\nu})^2 + F_{\mu\nu} \tilde{F}^{\mu\nu} + Y H \bar{\Psi} \Psi$$

Callouts identify the following problems:

- CC problem**: Callout pointing to the Λ^4 term.
- Hierarchy problem**: Callout pointing to the $\Lambda^2 H^2$ term.
- Vacuum stability?**: Callout pointing to the λH^4 term.
- Strong CP problem**: Callout pointing to the $F_{\mu\nu} \tilde{F}^{\mu\nu}$ term.
- SM flavor puzzle**: Callout pointing to the $Y H \bar{\Psi} \Psi$ term.

Flavor in the Standard Model and Beyond

CC problem

Hierarchy problem

Vacuum stability?

Strong CP problem

$$\mathcal{L}_{\text{SM}} \sim \Lambda^4 + \Lambda^2 H^2 + \lambda H^4$$
$$+ \bar{\Psi} \not{D} \Psi + (D_\mu H)^2 + (F_{\mu\nu})^2 + F_{\mu\nu} \tilde{F}^{\mu\nu}$$

$+ Y H \bar{\Psi} \Psi$

$$+ \frac{1}{\Lambda} (LH)^2 + \frac{1}{\Lambda^2} \sum_i \mathcal{O}_i^{\text{dim6}} + \dots$$

SM flavor puzzle

Neutrino masses

Flavorful new physics?

Flavor in the Standard Model and Beyond

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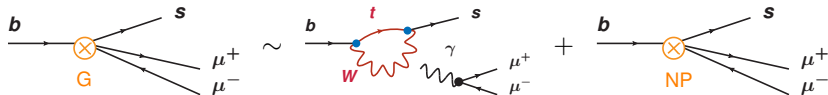
Callouts and their corresponding terms:

- CC problem**: Points to the Λ^4 term.
- Hierarchy problem**: Points to the $\Lambda^2 H^2$ term.
- Vacuum stability?**: Points to the λH^4 term.
- Strong CP problem**: Points to the $F_{\mu\nu} \tilde{F}^{\mu\nu}$ term.
- SM flavor puzzle**: Points to the $Y H \bar{\Psi} \Psi$ term.
- Neutrino masses**: Points to the $\frac{1}{\Lambda} (LH)^2$ term.
- Flavorful new physics?**: Points to the $\frac{1}{\Lambda^2} \sum_i \mathcal{O}_i^{\text{dim}6}$ term.

Q1: What is the origin of the hierarchies in the SM sources of flavor violation?

Q2: Are there other sources of flavor violation beyond the SM?

New Physics in FCNC Decays



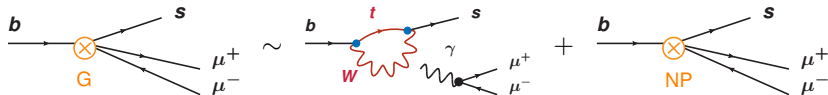
$$G \sim \frac{1}{16\pi^2} \frac{g^4}{m_W^2} \frac{m_t^2}{m_W^2} V_{tb} V_{ts}^* + \frac{C_{NP}}{\Lambda_{NP}^2}$$

measure
precisely

calculate precisely
the SM contribution

get information on
NP coupling and scale

New Physics in FCNC Decays



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“Anomalies” in rare decays could establish
a new scale in particle physics

A Wealth of Rare $b \rightarrow s$ Decays

radiative decays

$$B \rightarrow X_s \gamma$$

$$B \rightarrow K^* \gamma$$

$$B_s \rightarrow \phi \gamma$$

leptonic decays

$$B_s \rightarrow \ell^+ \ell^-$$

baryon decays

$$\Lambda_b \rightarrow \Lambda \ell^+ \ell^-$$

neutrino final states

$$B \rightarrow K \nu \bar{\nu}$$

$$B \rightarrow K^* \nu \bar{\nu}$$

semileptonic decays

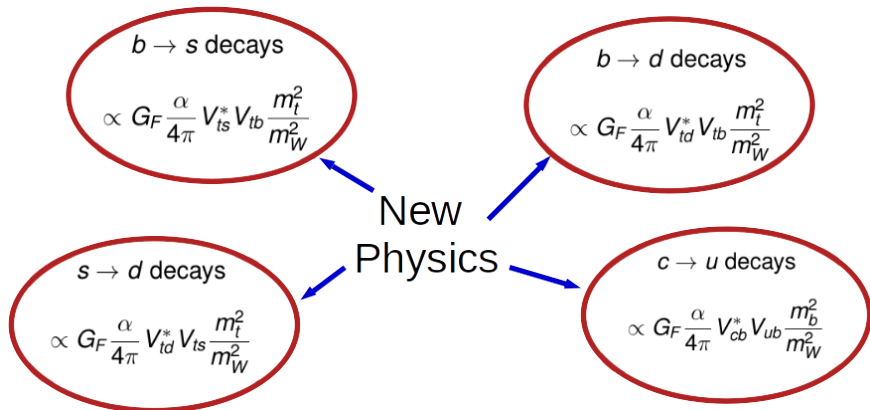
$$B \rightarrow X_s \ell^+ \ell^-$$

$$B \rightarrow K \ell^+ \ell^-$$

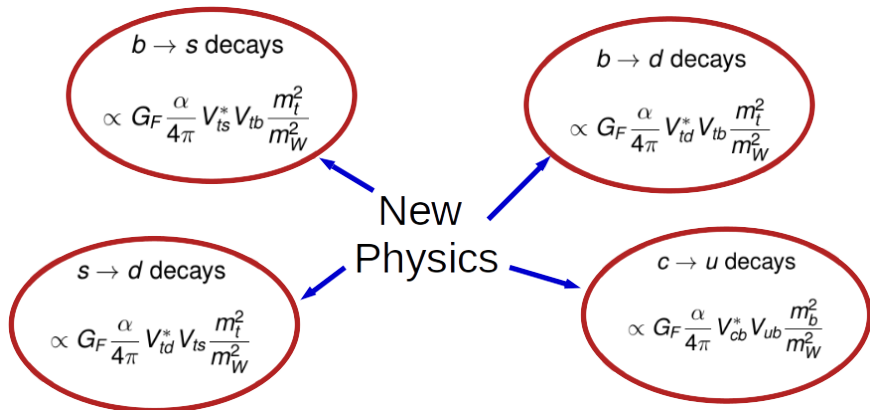
$$B \rightarrow K^* \ell^+ \ell^-$$

$$B_s \rightarrow \phi \ell^+ \ell^-$$

Complementarity of Rare Decays



Complementarity of Rare Decays



Q3: Are there hierarchies in the new physics sources of flavor violation?
If yes, what is their origin?

$$B_s \rightarrow \mu^+ \mu^-$$

amplitude \sim Wilson coefficient \times decay constant

amplitude \sim Wilson coefficient \times decay constant

- Decay constant is known from lattice QCD with sub-percent precision!

$$f_{B_s} = (230.3 \pm 1.3) \text{ MeV} \quad \text{FLAG review 2021, 2111.09849}$$

amplitude \sim Wilson coefficient \times decay constant

- Decay constant is known from lattice QCD with sub-percent precision!

$$f_{B_s} = (230.3 \pm 1.3) \text{ MeV} \quad \text{FLAG review 2021, 2111.09849}$$

- Precision of the SM prediction is limited by the CKM element V_{cb}

$$\text{BR}(B_s \rightarrow \mu^+ \mu^-) = (3.66 \pm 0.14) \times 10^{-9} \quad \text{Beneke, Bobeth, Szafron 1908.07011}$$

- Note: the above SM prediction uses the inclusive value for $|V_{cb}|_{\text{incl.}} \simeq 42 \times 10^{-3}$. Using instead the exclusive value, the branching ratio is lower by $\sim 10\%$ (e.g. Bobeth, Buras 2104.09521)
- A precision measurement of $\text{BR}(B_s \rightarrow \mu^+ \mu^-)$ could be used to give a precise value for V_{cb} (assuming the absence of new physics...)

The Effective $B_s \rightarrow \mu^+ \mu^-$ Lifetime

- The sizeable width difference of the B_s mesons gives the opportunity to test new physics in a complementary way through measurements of the **effective lifetime** (De Bruyn et al. 1204.1737)

$$\tau_{\text{eff}} = \frac{\int_0^\infty dt t \langle \Gamma(B_s(t) \rightarrow \mu^+ \mu^-) \rangle}{\int_0^\infty dt \langle \Gamma(B_s(t) \rightarrow \mu^+ \mu^-) \rangle} = \frac{\tau_{B_s}}{1 - y_s^2} \left(\frac{1 + 2\mathcal{A}_{\Delta\Gamma}^{\mu\mu} y_s + y_s^2}{1 + \mathcal{A}_{\Delta\Gamma}^{\mu\mu} y_s} \right)$$

$$\text{with } y_s = \frac{\Delta\Gamma_s}{2\Gamma_s} = 0.068 \pm 0.004 \quad \text{HFLAV}$$

- In the SM, $\mathcal{A}_{\Delta\Gamma}^{\mu\mu} = 1$, but in the presence of new physics it can take any value $-1 < \mathcal{A}_{\Delta\Gamma}^{\mu\mu} < 1$

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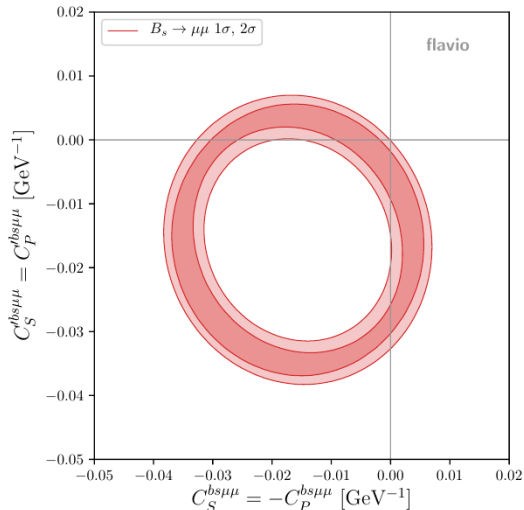
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- In the SM, $\mathcal{A}_{\Delta\Gamma}^{\mu\mu} = 1$, but in the presence of new physics it can take any value $-1 < \mathcal{A}_{\Delta\Gamma}^{\mu\mu} < 1$
- **Want precision measurement of τ_{eff} to access $\mathcal{A}_{\Delta\Gamma}^{\mu\mu}$**

$$\tau_{\text{eff}} = (2.07 \pm 0.29 \pm 0.03) \text{ ps} \quad \text{LHCb 2108.09284}$$

$$\tau_{\text{eff}} = (1.70_{-0.44}^{+0.61}) \text{ ps} \quad \text{CMS 1910.12127}$$

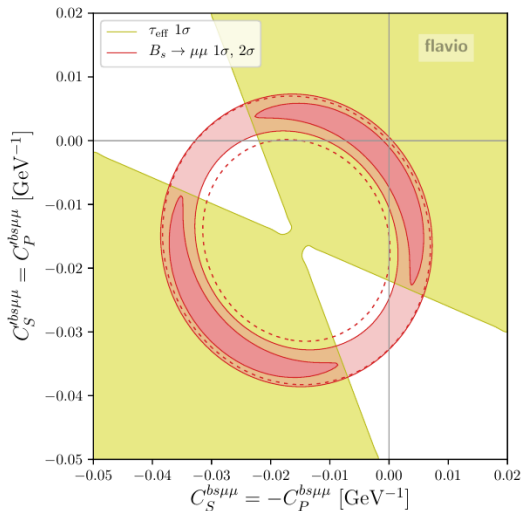
Sensitivity to New Physics



WA, Stangl 2103.13370

- scalar new physics is **strongly constrained**. (certain leptoquarks, or additional Higgs bosons from the MSSM)
- branching ratio data alone leaves **degeneracy** in the allowed parameter space

Sensitivity to New Physics

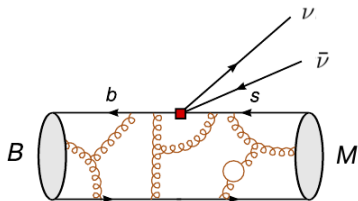


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- scalar new physics is **strongly constrained**. (certain leptoquarks, or additional Higgs bosons from the MSSM)
- branching ratio data alone leaves **degeneracy** in the allowed parameter space
- latest results on the **effective lifetime** already start having impact (despite the sizable uncertainties)

$$B \rightarrow K^{(*)} \nu \bar{\nu}$$

amplitudes \sim Wilson coefficients \times form factors



- form factors from
 - lattice QCD (high q^2)
 - light-cone sum rules (low q^2)
 - combined fits available
(Bharucha, Straub, Zwicky 1503.05534;
Gubernari, Kokulu, van Dyk 1811.00983)
- typical uncertainties $\lesssim 10\%$

$$\text{BR}(B^+ \rightarrow K^+ \nu \bar{\nu}) = (4.23 \pm 0.56) \times 10^{-6} \quad \text{Bause et al. 2109.01675}$$

$$\text{BR}(B^0 \rightarrow K^{*0} \nu \bar{\nu}) = (8.24 \pm 0.99) \times 10^{-6} \quad \text{Bause et al. 2109.01675}$$

Sensitivity to New Physics

SM rates of $B \rightarrow K^{(*)}\nu\bar{\nu}$ can be observed at Belle II

(first limit on $B \rightarrow K\nu\bar{\nu}$ from Belle II: 2104.12624)

Observables	Belle 0.71 ab^{-1} (0.12 ab^{-1})	Belle II 5 ab^{-1}	Belle II 50 ab^{-1}
$\text{Br}(B^+ \rightarrow K^+\nu\bar{\nu})$	$< 450\%$	30%	11%
$\text{Br}(B^0 \rightarrow K^{*0}\nu\bar{\nu})$	$< 180\%$	26%	9.6%
$\text{Br}(B^+ \rightarrow K^{*+}\nu\bar{\nu})$	$< 420\%$	25%	9.3%

(Belle II Physics Book 1808.10567)

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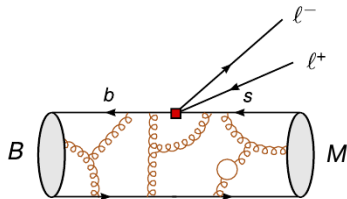
Role of $b \rightarrow s\nu\bar{\nu}$ in probing New Physics

- ▶ modification of $b \rightarrow s\nu\bar{\nu}$ rates by **heavy new physics**, e.g. leptoquarks, Z' , ... (e.g. Browder et al. 2107.01080; Bause et al. 2109.01675)
- ▶ neutrino flavor is summed over in the measurement \rightarrow indirect sensitivity to new physics in $b \rightarrow s\tau\tau$ because of $SU(2)_L$
- ▶ new invisible decay modes into **light dark sector particles** $b \rightarrow sX$, $b \rightarrow sX_1X_2$, ... (e.g. Hostert et al. 2005.07102; Felkl et al. 2111.04327)

$$B \rightarrow K^{(*)} l^+ l^-$$

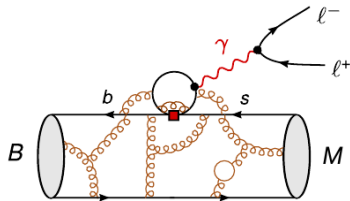
$$B_s \rightarrow \phi l^+ l^-$$

amplitudes \sim Wilson coefficients \times form factors



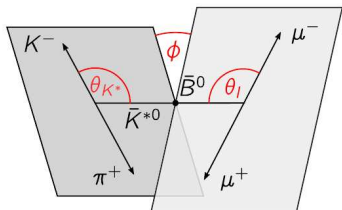
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- typical uncertainties $\lesssim 10\%$

amplitudes \sim **Wilson coefficients** \times **form factors**
+ **non-local terms** (aka “charm loops”)



- various model approaches:
 - **sum of resonances**
(Blake et al. 1709.03921)
 - **polynomial fit to data**
(Ciuchini et al. 1512.07157)
 - **LCSR estimates** (Khodjamirian et al. 1006.4945; Gubernari et al. 2011.09813)
 - **analytic function fit to data**
(Bobeth et al. arXiv:1707.07305; Gubernari et al. 2011.09813)
- dominant uncertainty ($\sim 10\%$)

Angular Distributions



$$\frac{1}{\frac{d}{dq^2}(\Gamma + \bar{\Gamma})} \frac{d^4(\Gamma + \bar{\Gamma})}{dq^2 d\vec{\Omega}} =$$

$$\begin{aligned}
 &= \frac{3}{4}(1 - F_L) \sin^2 \theta_{K^*} + F_L \cos^2 \theta_{K^*} \\
 &+ \frac{1}{4}(1 - F_L) \sin^2 \theta_{K^*} \cos 2\theta_\ell - F_L \cos^2 \theta_{K^*} \cos 2\theta_\ell \\
 &+ \mathbf{S}_3 \sin^2 \theta_{K^*} \sin^2 \theta_\ell \cos 2\phi + \mathbf{S}_4 \sin 2\theta_{K^*} \sin 2\theta_\ell \cos \phi + \mathbf{S}_5 \sin 2\theta_{K^*} \sin \theta_\ell \cos \phi \\
 &+ \frac{4}{3} \mathbf{A}_{\text{FB}} \sin^2 \theta_{K^*} \cos \theta_\ell + \mathbf{S}_7 \sin 2\theta_{K^*} \sin \theta_\ell \sin \phi \\
 &+ \mathbf{S}_8 \sin 2\theta_{K^*} \sin 2\theta_\ell \sin \phi + \mathbf{S}_9 \sin^2 \theta_{K^*} \sin^2 \theta_\ell \sin 2\phi
 \end{aligned}$$

angular observables have (somewhat) **reduced theory uncertainties**

Distinguishing New Physics from Hadronic Effects

(heavy) New Physics

Hadronic Contributions

described by local
four fermion operator

a non-local and
non-perturbative effect

Distinguishing New Physics from Hadronic Effects

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Distinguishing New Physics from Hadronic Effects

(heavy) New Physics

described by local
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might be CP violating

might violate lepton flavor universality

Hadronic Contributions

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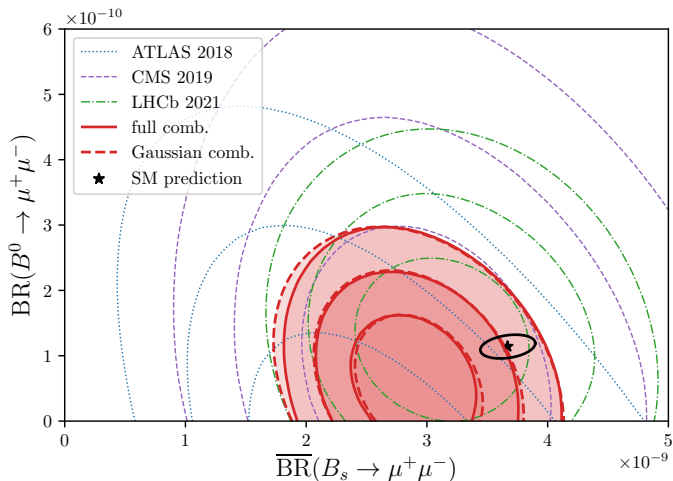
CP conserving

lepton flavor universal

Overview of the Flavor Anomalies

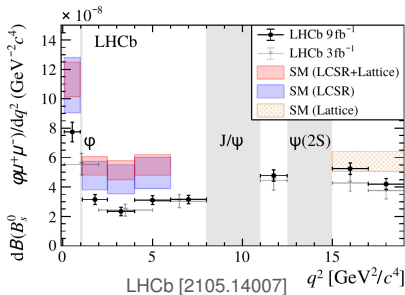
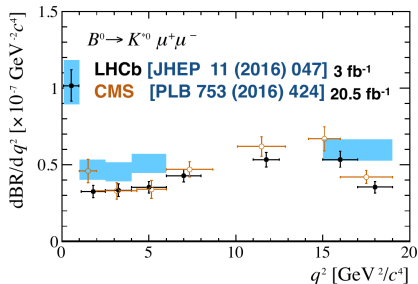
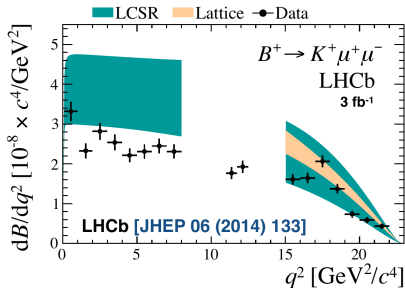
The $B_s \rightarrow \mu^+ \mu^-$ Branching Ratio

WA, Stangl 2103.13370; combination of LHCb 2108.09284, CMS 1910.12127, ATLAS 1812.03017



$\sim 2\sigma$ tension between SM and experiment

$b \rightarrow s\mu\mu$ Branching Ratios



Experimental results for

$$\text{BR}(B \rightarrow K\mu\mu)$$

$$\text{BR}(B \rightarrow K^*\mu\mu)$$

$$\text{BR}(B_s \rightarrow \phi\mu\mu)$$

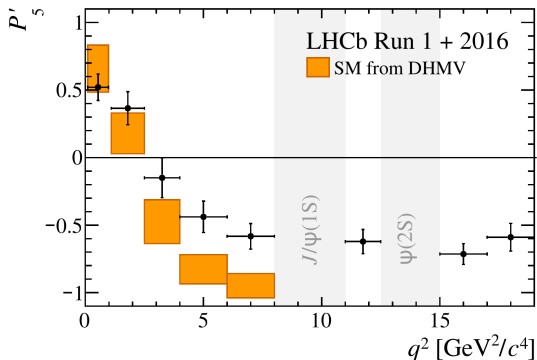
are consistently low
across many q^2 bins

($\sim 2\sigma - 3\sigma$)

The P'_5 Anomaly

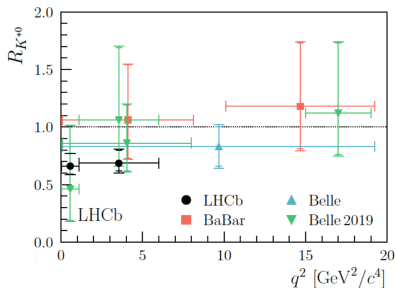
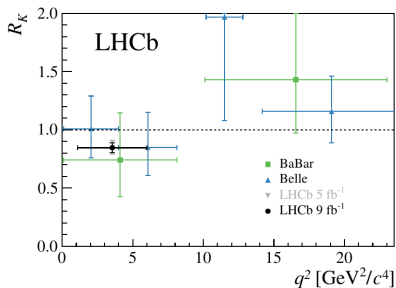
$$P'_5 = \frac{S_5}{\sqrt{F_L(1-F_L)}}$$

LHCb 2003.04831



$\sim 2\sigma - 3\sigma$ anomaly persists in the latest update of $B^0 \rightarrow K^{*0} \mu^+ \mu^-$.
(Anomaly also seen in $B^\pm \rightarrow K^{*\pm} \mu^+ \mu^-$ LHCb 2012.13241)

Evidence for Lepton Flavor Universality Violation



$$R_{K^{(*)}} = \frac{BR(B \rightarrow K^{(*)} \mu \mu)}{BR(B \rightarrow K^{(*)} e e)} \stackrel{\text{SM}}{\simeq} 1$$

$$R_{K^+}^{[1,6]} = 0.846_{-0.039-0.012}^{+0.042+0.013} \quad (3.1\sigma)$$

$$R_{K^{*0}}^{[0.045,1.1]} = 0.66_{-0.07}^{+0.11} \pm 0.03 \quad (\sim 2.5\sigma)$$

$$R_{K^{*0}}^{[1.1,6]} = 0.69_{-0.07}^{+0.11} \pm 0.05 \quad (\sim 2.5\sigma)$$

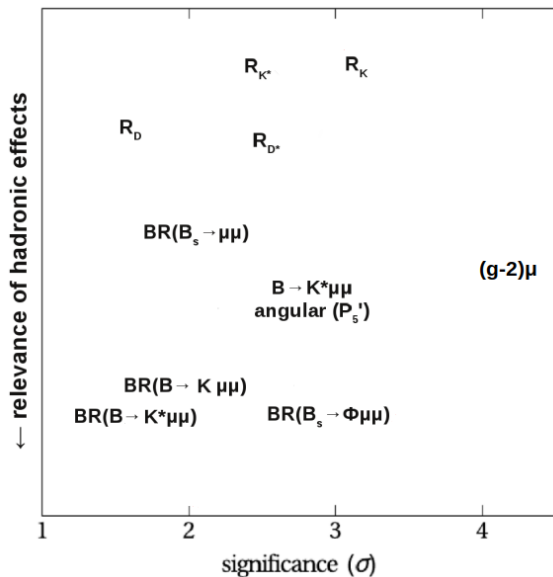
$$R_{K_S}^{[1.1,6]} = 0.66_{-0.14-0.04}^{+0.20+0.02} \quad (\sim 1.5\sigma)$$

$$R_{K^{*+}}^{[0.045,6]} = 0.70_{-0.13-0.04}^{+0.18+0.03} \quad (\sim 1.5\sigma)$$

$$R_{\rho K}^{[0.1,6]} = 0.86_{-0.11}^{+0.14} \pm 0.05 \quad (\sim 1\sigma)$$

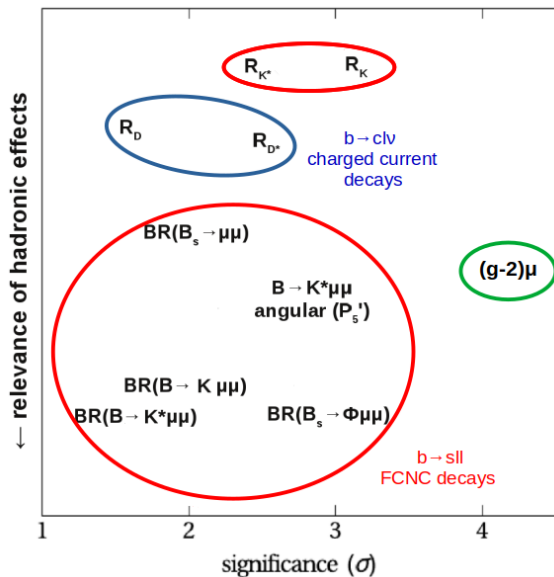
LHCb 2103.11769, LHCb 1705.05802, 1912.08139, 2110.09501; also Belle 1904.02440, 1908.01848

Flavor Anomalies in 2021



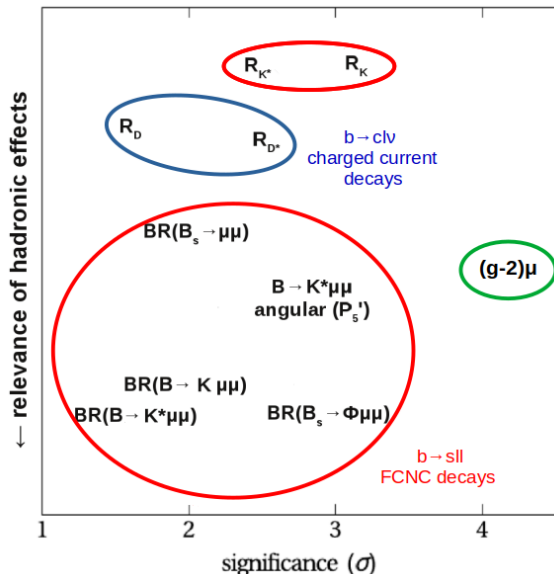
(inspired by
Zoltan Ligeti)

Flavor Anomalies in 2021



(inspired by
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Flavor Anomalies in 2021



plus several others:

- inclusive vs. exclusive V_{cb} ?
- inclusive vs. exclusive V_{ub} ?
- first row CKM unitarity?
- ...

(inspired by
Zoltan Ligeti)

What Could It Be?

$B_s \rightarrow \mu\mu$
rate

semileptonic
rates

angular
observables

LFU
ratios

$(g-2)_\mu$

What Could It Be?

	$B_s \rightarrow \mu\mu$ rate	semileptonic rates	angular observables	LFU ratios	$(g-2)_\mu$
experimental issues?	?	?	?	?	?

What Could It Be?

	$B_s \rightarrow \mu\mu$ rate	semileptonic rates	angular observables	LFU ratios	$(g-2)_\mu$
experimental issues?	?	?	?	?	?
statistical fluctuations?	✓	✓	✓	✓	✗

What Could It Be?

	$B_s \rightarrow \mu\mu$ rate	semileptonic rates	angular observables	LFU ratios	$(g-2)_\mu$
experimental issues?	?	?	?	?	?
statistical fluctuations?	✓	✓	✓	✓	✗
parametric uncertainties?	✓	✓	✗	✗	✗

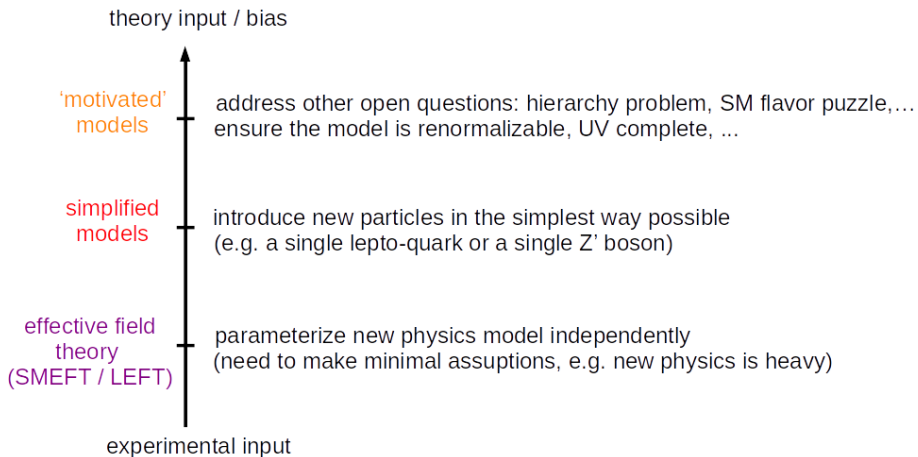
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experimental issues?	?	?	?	?	?
statistical fluctuations?	✓	✓	✓	✓	✗
parametric uncertainties?	✓	✓	✗	✗	✗
underestimated hadronic effects?	✗	✓	✓	✗	✓

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experimental issues?	?	?	?	?	?
statistical fluctuations?	✓	✓	✓	✓	✗
parametric uncertainties?	✓	✓	✗	✗	✗
underestimated hadronic effects?	✗	✓	✓	✗	✓
New Physics?	✓	✓	✓	✓	✓

Bottom-Up Approach to the Flavor Anomalies



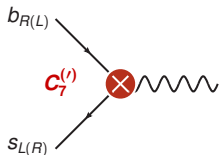
(inspired by Marco Nardecchia)

Implications for New Physics

Model Independent New Physics Analysis

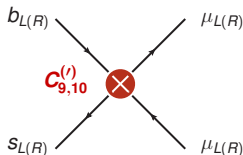
$$\mathcal{H}_{\text{eff}}^{b \rightarrow s} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{e^2}{16\pi^2} \sum_i (C_i \mathcal{O}_i + C'_i \mathcal{O}'_i)$$

magnetic dipole operators



$$C_7^{(i)} (\bar{s} \sigma_{\mu\nu} P_{R(L)} b) F^{\mu\nu}$$

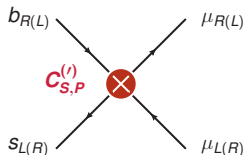
semileptonic operators



$$C_9^{(i)} (\bar{s} \gamma_\mu P_{L(R)} b) (\bar{\mu} \gamma^\mu \mu)$$

$$C_{10}^{(i)} (\bar{s} \gamma_\mu P_{L(R)} b) (\bar{\mu} \gamma^\mu \gamma_5 \mu)$$

scalar operators



$$C_S^{(i)} (\bar{s} P_{R(L)} b) (\bar{\mu} P_{L(R)} \mu)$$

neglecting tensor operators and additional scalar operators

(they are dimension 8 in SMEFT: Alonso, Grinstein, Martin Camalich 1407.7044)

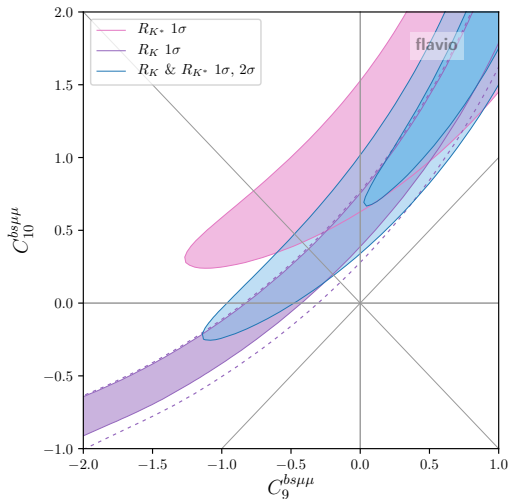
Complementary Sensitivity

	C_7, C'_7	C_9, C'_9	C_{10}, C'_{10}	C_S, C'_S
$B \rightarrow (X_s, K^*)\gamma$	★			
$B_s \rightarrow \phi\gamma$	★			
$B \rightarrow (X_s, K, K^*)\ell^+\ell^-$	★	★	★	★
$B_s \rightarrow \phi\ell^+\ell^-$	★	★	★	★
$\Lambda_b \rightarrow \Lambda\ell^+\ell^-$	★	★	★	★
$B_s \rightarrow \ell^+\ell^-$			★	★
$B \rightarrow (K, K^*)\nu\bar{\nu}^*$		★	★	

(* SU(2) invariance implies that the neutrino modes are sensitive to $C_9 - C_{10}$ and $C'_9 - C'_{10}$.

Measurements sum over all neutrino flavors)

Fits of Pairs of Wilson Coefficients



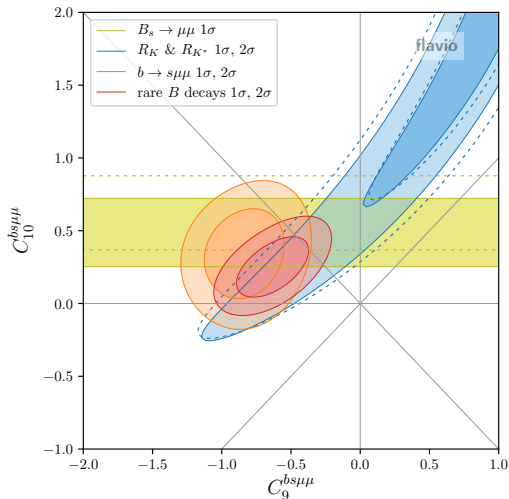
$$C_9^{bs\mu\mu} (\bar{s}\gamma_\alpha P_L b) (\bar{\mu}\gamma^\alpha \mu)$$

$$C_{10}^{bs\mu\mu} (\bar{s}\gamma_\alpha P_L b) (\bar{\mu}\gamma^\alpha \gamma_5 \mu)$$

- LFU ratios prefer non-standard C_{10} , but large degeneracy

WA, Stangl 2103.13370

Fits of Pairs of Wilson Coefficients



WA, Stangl 2103.13370

$$C_9^{bs\mu\mu}(\bar{s}\gamma_\alpha P_L b)(\bar{\mu}\gamma^\alpha \mu)$$

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- LFU ratios prefer non-standard C_{10} , but large degeneracy
- $B_s \rightarrow \mu^+ \mu^-$ branching ratio shows slight preference for non-standard C_{10}
- $b \rightarrow s\mu\mu$ observables prefer non-standard C_9
- best fit point

$$C_9^{bs\mu\mu} \simeq -0.63$$

$$C_{10}^{bs\mu\mu} \simeq +0.25$$

Comparison of Global Fits

(B. Capdevilla, M. Fedele, S. Neshatpour, P. Stangl @ Flavour Anomaly Workshop, CERN, Oct. 20 2021)

- ▶ **ACDMN** (M. Algueró, B. Capdevila, S. Descotes-Genon, J. Matias, M. Novoa-Brunet)
Statistical framework: χ^2 -fit, based on private code arXiv:2104.08921
- ▶ **AS** (W. Altmannshofer, P. Stangl)
Statistical framework: χ^2 -fit, based on public code `flavio` arXiv:2103.13370
- ▶ **CFFPSV** (M. Ciuchini, M. Fedele, E. Franco, A. Paul, L. Silvestrini, M. Valli)
Statistical framework: Bayesian MCMC fit, based on public code `HEPfit` arXiv:2011.01212
- ▶ **HMMN** (T. Hurth, F. Mahmoudi, D. Martínez-Santos, S. Neshatpour)
Statistical framework: χ^2 -fit, based on public code `SuperIso` arXiv:2104.10058

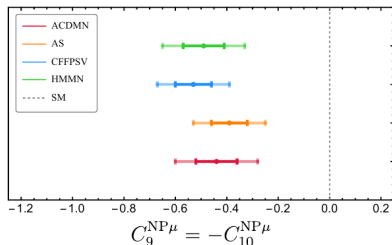
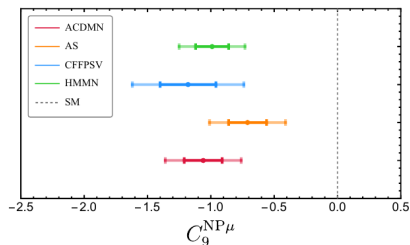
See also similar fits by other groups:

Geng et al., arXiv:2103.12738, Alok et al., arXiv:1903.09617, Datta et al., arXiv:1903.10086, Kowalska et al., arXiv:1903.10932, D'Amico et al., arXiv:1704.05438, Hiller et al., arXiv:1704.05444, ...

- Global fits have reached a high level of sophistication. Are done by many groups with different statistical approaches, different treatment of theory uncertainties, different selection of observables, ...

Fits of One Single Wilson Coefficient

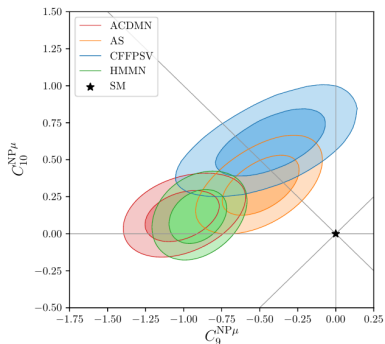
(B. Capdevilla, M. Fedele, S. Neshatpour, P. Stangl @ Flavour Anomaly Workshop, CERN, Oct. 20 2021)



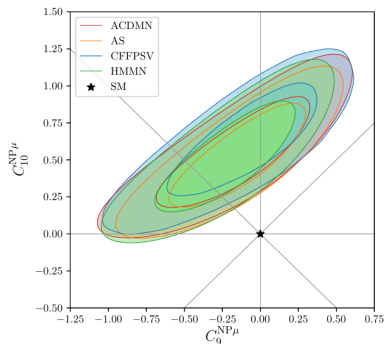
- small differences among the groups due to different approaches, but overall **remarkable agreement**
- NP scenarios are preferred over SM with pulls $> 5\sigma$
- Warning: pull \neq global significance.
- Global significance $\simeq 4.3\sigma$ determined in Isidori et al. arXiv:2104.05631

Fits of Pairs of Wilson Coefficients

(B. Capdevilla, M. Fedele, S. Neshatpour, P. Stangl @ Flavour Anomaly Workshop, CERN, Oct. 20 2021)



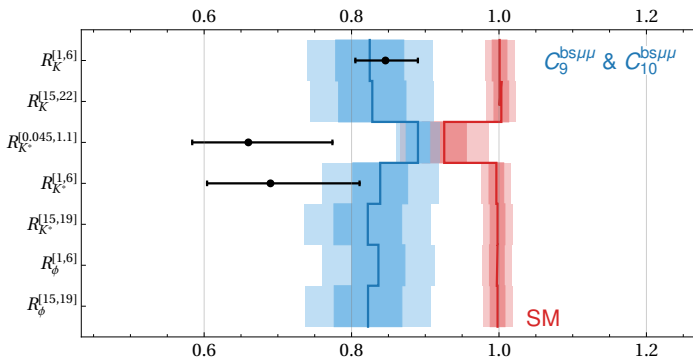
global fit



fit to LFU observables + $B_s \rightarrow \mu\mu$

- Perfect agreement if only theoretically clean observables are used.

Predictions for Other LFU Ratios



WA, Stangl 2103.13370

LFU ratios of branching fractions are all predicted to show a similar deviation from the SM

$$R_K \simeq R_{K^*} \simeq R_\phi \simeq 0.8$$

Implications for the New Physics Scale

unitarity bound $\frac{4\pi}{\Lambda_{\text{NP}}^2} (\bar{s}\gamma_\nu P_L b)(\bar{\mu}\gamma^\nu \mu)$ $\Lambda_{\text{NP}} \simeq 120 \text{ TeV} \times (C_9^{\text{NP}})^{-1/2}$

generic tree $\frac{1}{\Lambda_{\text{NP}}^2} (\bar{s}\gamma_\nu P_L b)(\bar{\mu}\gamma^\nu \mu)$ $\Lambda_{\text{NP}} \simeq 35 \text{ TeV} \times (C_9^{\text{NP}})^{-1/2}$

MFV tree $\frac{1}{\Lambda_{\text{NP}}^2} V_{tb} V_{ts}^* (\bar{s}\gamma_\nu P_L b)(\bar{\mu}\gamma^\nu \mu)$ $\Lambda_{\text{NP}} \simeq 7 \text{ TeV} \times (C_9^{\text{NP}})^{-1/2}$

generic loop $\frac{1}{\Lambda_{\text{NP}}^2} \frac{1}{16\pi^2} (\bar{s}\gamma_\nu P_L b)(\bar{\mu}\gamma^\nu \mu)$ $\Lambda_{\text{NP}} \simeq 3 \text{ TeV} \times (C_9^{\text{NP}})^{-1/2}$

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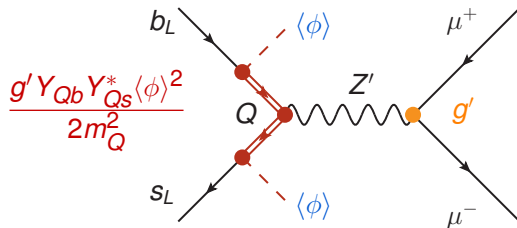
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→ Targets for Colliders!

My Favorite Model for R_K and R_{K^*}

Z' based on gauging $L_\mu - L_\tau$ (He, Joshi, Lew, Volkas PRD 43, 22-24)
with effective flavor violating couplings to quarks

WA, Gori, Pospelov, Yavin 1403.1269; WA, Yavin 1508.07009

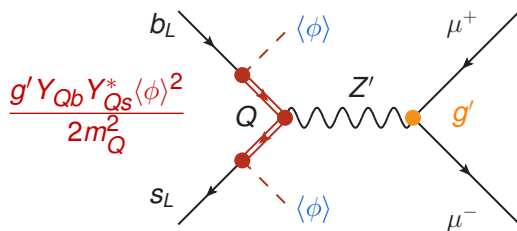


Q : heavy vectorlike fermions with mass $\sim 1 - 10$ TeV
 ϕ : scalar that breaks $L_\mu - L_\tau$

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predicted Lepton
Universality Violation!

Q : heavy vectorlike fermions with mass $\sim 1 - 10$ TeV
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Probing the Z' Parameter Space

WA, Gori, Martin-Albo, Sousa, Wallbank 1902.06765

Neutrino Tridents

B_s mixing

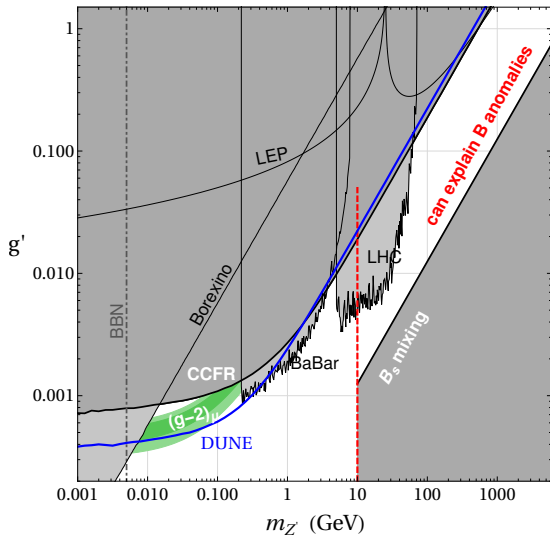
$(g-2)_\mu$

νe scattering

$Z \rightarrow \ell\ell$

$Z \rightarrow 4\mu$

$e^+e^- \rightarrow 4\mu$



I look forward
to an exciting workshop!