

WG 7 Summary

Mixing and CP Violation in the D system

Adam Davis and Cheng-Wei Chiang

26th of November, 2021

The Conveners



Only one internet gremlin
“Strange things happen in
full screen mode”



Thank you very much to the organizers and all the speakers!

[Source: Wikimedia Commons](#)

Disclaimer

This is an overview

All positive comments go directly to the speakers of the session

All negative go directly to us

Challenges in Charm System

- Charm quark scale (~ 1.3 GeV)
 - too light to have good heavy quark expansions
 - too heavy for chiral perturbation expansions
 - nonperturbative strong interaction coupling
 - many nearby hadronic resonances for rescattering effects
 - high precision calculations of Δm_D , $\Delta \Gamma_D$, strong phases, etc still theoretically challenging
- Resort to
 - flavor SU(3) symmetry (particularly strong phases)
 - Phenomenological assumptions (LD effects)
 - inclusion of symmetry breaking effects
 - higher-order calculations (particularly in mixing)
 - ...

Mixing and CPV in the D system

- Time-Dependent CP Asymmetry

$$A_{CP}(f(t)) = \frac{\Gamma(D^0 \rightarrow f(t)) - \Gamma(\bar{D}^0 \rightarrow f(t))}{\Gamma(D^0 \rightarrow f(t)) + \Gamma(\bar{D}^0 \rightarrow f(t))}$$

- Time-Integrated CP Asymmetry

$$A_{CP}(f) = a_{CP}^{dir}(f) + \frac{\langle t \rangle}{\tau} a_{CP}^{ind}(f)$$

- Short-distance contributions within SM predict CPA of $\lesssim \mathcal{O}(10^{-4})$
 ▣ long-distance rescattering effects to be included

Mixing and CPV in the D system

- Mass eigenstates \neq Flavour Eigenstates \rightarrow Mixing!

$$|D_{12}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle$$

- Redefine in terms of effective Hamiltonian

$$\hat{H} = \mathbf{M} - i\mathbf{\Gamma} \quad i\hbar \frac{d}{dt} \begin{pmatrix} |D^0(t)\rangle \\ |\bar{D}^0(t)\rangle \end{pmatrix} = \hat{H} \begin{pmatrix} |D^0(t)\rangle \\ |\bar{D}^0(t)\rangle \end{pmatrix}$$

$$x = \frac{\Delta M}{\Gamma}, y = \frac{\Delta\Gamma}{2\Gamma}$$

$$\frac{q}{p} = \left| \frac{q}{p} \right| e^{i\phi}$$

$$A_f = \langle f|H|D^0\rangle$$

$$\bar{A}_f = \langle f|H|\bar{D}^0\rangle$$

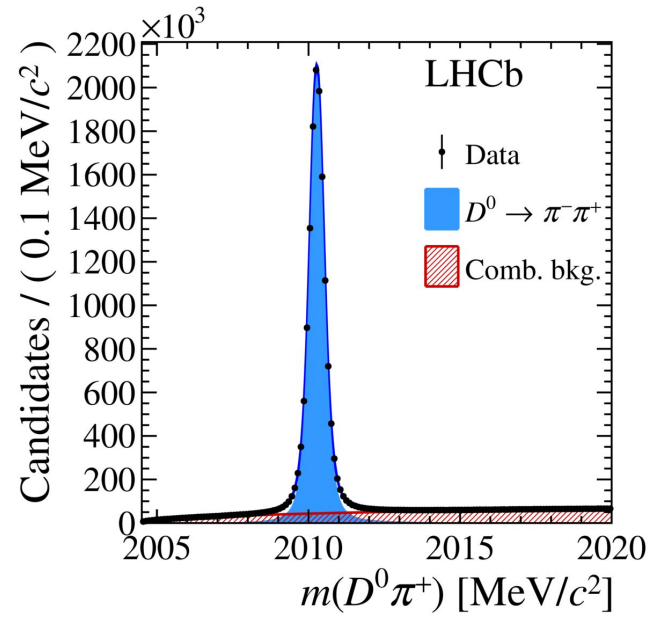
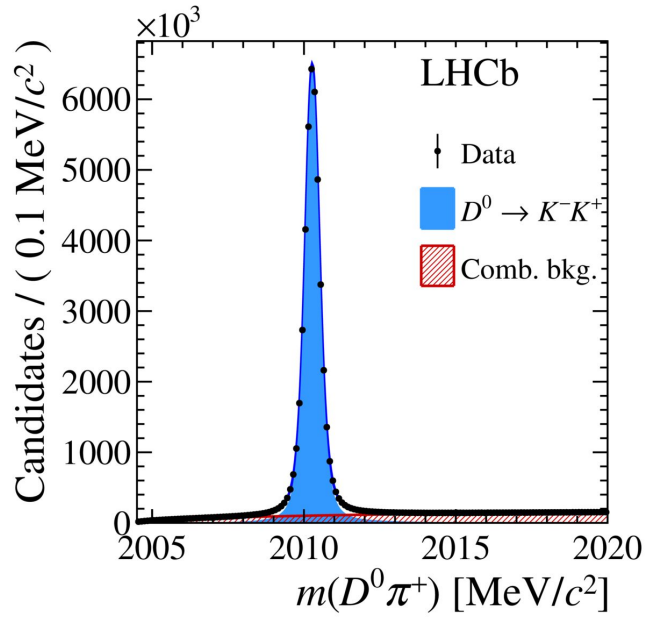
$$A_{\bar{f}} = \langle \bar{f}|H|D^0\rangle$$

$$\bar{A}_{\bar{f}} = \langle \bar{f}|H|\bar{D}^0\rangle$$

Direct CPV

Bonza!

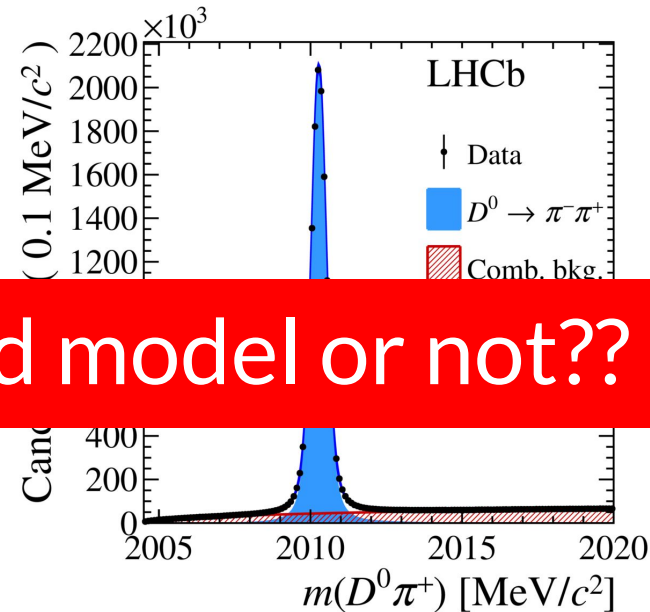
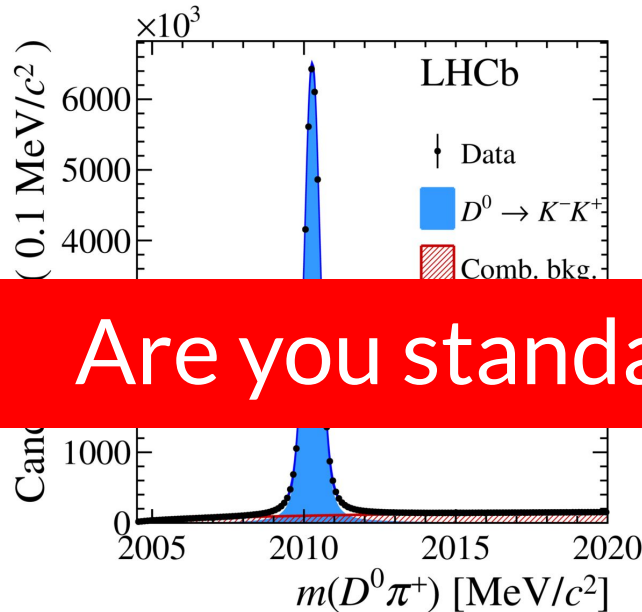
Andrea Contu



$$\Delta A_{CP} = A_{CP}(KK) - A_{CP}(\pi\pi) = (-15.4 \pm 2.9) \times 10^{-4}$$

Bonza!

Andrea Contu



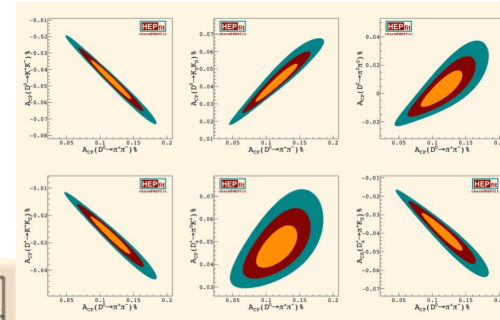
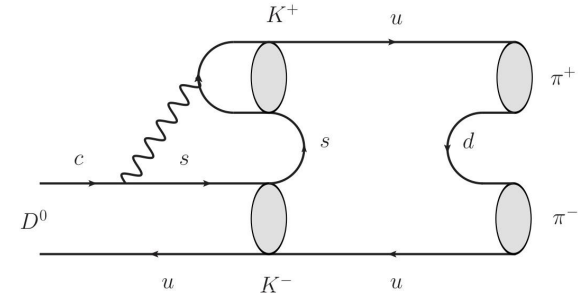
Are you standard model or not??

$$\Delta A_{CP} = A_{CP}(KK) - A_{CP}(\pi\pi) = (-15.4 \pm 2.9) \times 10^{-4}$$

Progress on Theory

- Topological amplitude analysis ([Hai-Yang Cheng](#))
 - include $SU(3)_F$ breaking effects from CF to SCS/DCS modes
 - include SD penguin amplitudes using QCDF (rescattering effects)
 - invoke LD rescattering to penguin-exchange amplitude
 - Also look into VP decays and identify six golden modes to test theory
 - Analogous to the PP case, predict CPA difference:

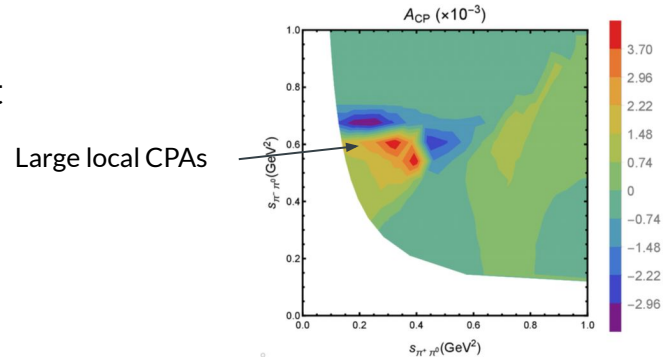
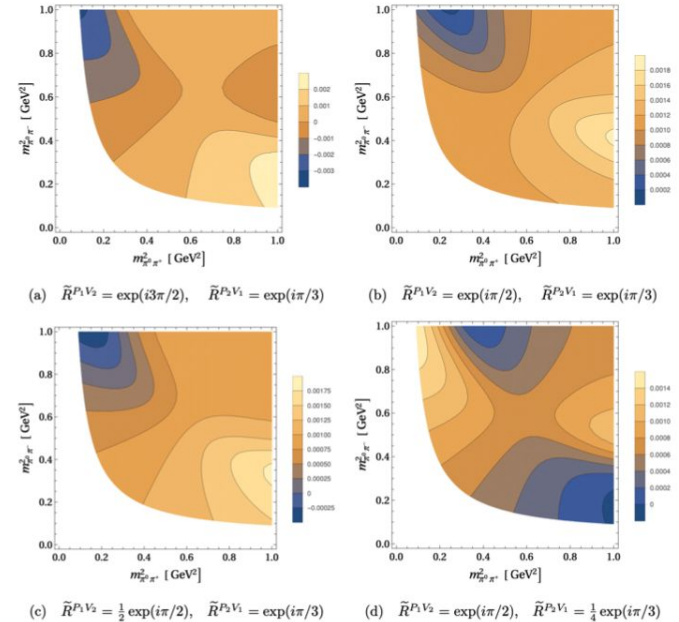
$$a_{CP}(K^+K^{*-}) - a_{CP}(\pi^+\rho^-) = (-1.61 \pm 0.33) \times 10^{-3}$$
 - Dalitz analysis of local CPAs in 3-body D decays can provide more info
- Also account for $SU(3)_F$ breaking with final state interactions and shifts to amplitudes - fits to BFs allow for predictions of DCPV ([Ayan Paul](#))
- Correlations stem from rescattering



$A_{CP}(D^0)$	$(\mu \pm \sigma) (\%)$		$A_{CP}(D_{(s)}^+)$	$(\mu \pm \sigma) (\%)$	
	$\delta_i \rightarrow -ve$	$\delta_i \rightarrow +ve$		$\delta_i \rightarrow -ve$	$\delta_i \rightarrow +ve$
$D^0 \rightarrow \pi^+\pi^-$	0.117 ± 0.020	0.118 ± 0.020	$D^+ \rightarrow K^+K_S$	-0.028 ± 0.005	-0.026 ± 0.005
$D^0 \rightarrow \pi^0\pi^0$	0.004 ± 0.009	0.079 ± 0.010	$D_s^+ \rightarrow \pi^+K_S$	-0.040 ± 0.007	-0.036 ± 0.007
$D^0 \rightarrow K^+K^-$	-0.047 ± 0.008	-0.046 ± 0.008	$D_s^+ \rightarrow \pi^0K^+$	0.048 ± 0.006	-0.003 ± 0.004
$D^0 \rightarrow K_S K_S$	0.043 ± 0.007	0.038 ± 0.007			

Progress on Theory (2)

- Look further into testing O(1) rescattering effects using $\Delta U=0$ with $D^0 \rightarrow V^\pm P^\mp \rightarrow P^\pm P^0 P^\mp$ (Avital Dery)
- Assumptions: Production/Detection asymmetry constant across Dalitz Plot
- 7 parameters to describe $D^0 \rightarrow \rho^\pm \pi^\mp \rightarrow \pi^+ \pi^- \pi^0$, 7 points on Dalitz plot enough
- Additional analogue to DACP using $K^* \pi$ and $\rho^\pm \pi^\mp$? Pseudo 2-body decays have exact U-spin correspondence, but 3-body final states are not related by full $d \leftrightarrow s$ interchange
- Effects of finite width of ρ^\pm included (Hai-Yang Cheng)
- How to associate meaningfully two points on different Dalitz plots?
- Discussion focused on what's reasonable for experimental measurements

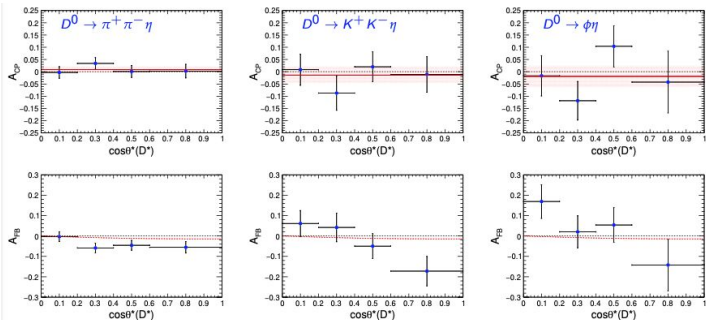


Experimental Pushes

Belle
Long-Ke Li

$$A_{CP} = \frac{A_{\text{corr}}(\cos\theta^*) + A_{\text{corr}}(-\cos\theta^*)}{2}$$

$$A_{\text{FB}} = \frac{A_{\text{corr}}(\cos\theta^*) - A_{\text{corr}}(-\cos\theta^*)}{2}$$



$$A_{CP}(D^0 \rightarrow \pi^+ \pi^- \eta) = [0.9 \pm 1.2 (\text{stat}) \pm 0.5 (\text{syst})]\%$$

$$A_{CP}(D^0 \rightarrow K^+ K^- \eta) = [-1.4 \pm 3.3 (\text{stat}) \pm 1.1 (\text{syst})]\%$$

$$A_{CP}(D^0 \rightarrow \phi \eta) = [-1.9 \pm 4.4 (\text{stat}) \pm 0.6 (\text{syst})]\%$$



Decay mode	A_{raw}	A_{CP}
$D_s^+ \rightarrow K^+ \pi^0$	0.115 ± 0.045	$0.064 \pm 0.044 \pm 0.011$
$D_s^+ \rightarrow K^+ \eta \gamma \gamma$	0.046 ± 0.027	$0.040 \pm 0.027 \pm 0.005$
$D_s^+ \rightarrow K^+ \eta 3\pi$	-0.011 ± 0.033	$-0.008 \pm 0.034 \pm 0.008$
$D_s^+ \rightarrow K^+ \eta$	—	$0.021 \pm 0.021 \pm 0.004$
$D_s^+ \rightarrow \pi^+ \eta \gamma \gamma$	0.007 ± 0.004	$0.002 \pm 0.004 \pm 0.003$
$D_s^+ \rightarrow \pi^+ \eta 3\pi$	0.008 ± 0.006	$0.002 \pm 0.006 \pm 0.003$
$D_s^+ \rightarrow \pi^+ \eta$	—	$0.002 \pm 0.003 \pm 0.003$
$D_s^+ \rightarrow \phi \pi^+$	0.002 ± 0.001	—

LHCb
Andrea Contu

$$A_{CP}(D^+ \rightarrow \pi^+ \pi^0) = (-1.3 \pm 0.9 \pm 0.6)\%$$

$$A_{CP}(D^+ \rightarrow K^+ \pi^0) = (-3.2 \pm 4.7 \pm 2.1)\%$$

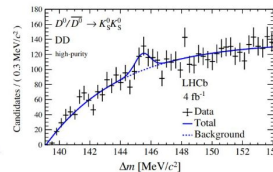
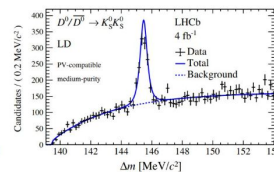
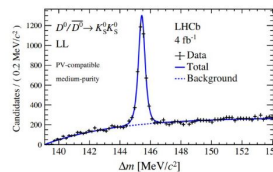
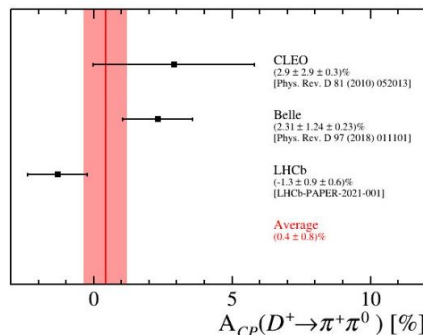
$$A_{CP}(D^+ \rightarrow \pi^+ \eta) = (-0.2 \pm 0.8 \pm 0.4)\%$$

$$A_{CP}(D^+ \rightarrow K^+ \eta) = (-6 \pm 10 \pm 4)\%$$

$$A_{CP}(D_s^+ \rightarrow K^+ \pi^0) = (-0.8 \pm 3.9 \pm 1.2)\%$$

$$A_{CP}(D_s^+ \rightarrow \pi^+ \eta) = (0.8 \pm 0.7 \pm 0.5)\%$$

$$A_{CP}(D_s^+ \rightarrow K^+ \eta) = (0.9 \pm 3.7 \pm 1.1)\%$$



$$A_{CP}(D^0 \rightarrow K_S^0 K_S^0) = (-3.1 \pm 1.2 (\text{stat.}) \pm 0.4 (\text{syst.}) \pm 0.2 (A_{CP}(D^0 \rightarrow KK))\%$$

First
Measurements

BESIII

Jim Libby

- Surprises happen e.g. doubly Cabibbo suppressed branching fraction for $D^+ \rightarrow K^+ \pi^+ \pi^- \pi^0$ [PRL 125 (2020) 14180]

$$B(D^+ \rightarrow K^+ \pi^+ \pi^- \pi^0) = (6.28 \pm 0.52) \times \tan^4 \theta_c \times B(D^+ \rightarrow K^- \pi^+ \pi^+ \pi^0)$$

- $A_{CP} = -0.04 \pm 0.06 (\text{stat}) \pm 0.01 (\text{syst})$

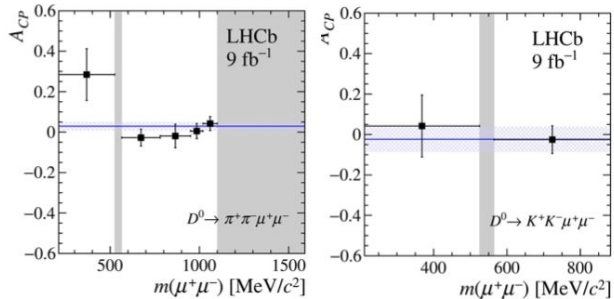
14 BF's of 3- & 4-body D decays with η in final state
→ no significant ACP, precision 1-5%

Push to Rare Decays

Marcel Golz

- Devise null tests in non-resonance regions to constrain WC's from EFT approach
- E.g. A_{FB} vs q^2 of $D_s \rightarrow K \mu \mu$
- E.g. Lepton non-universality possibly at $O(1 - 100)$
- Plenty of opportunities in mesonic/baryonic modes

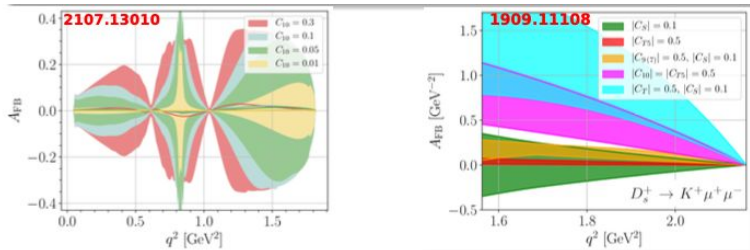
Andrea Contu + D. Brundu in WG 3



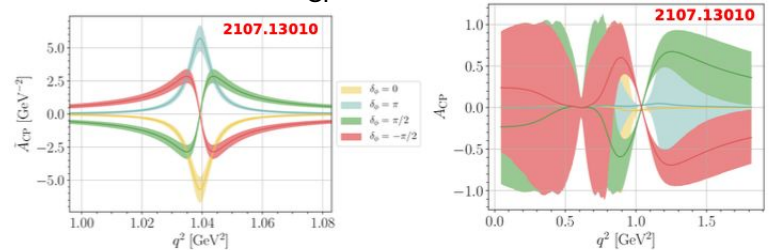
$m(\mu^+\mu^-)$ [MeV/c ²]	A_{CP} [%]
--	--------------

$D^0 \rightarrow \pi^+\pi^-\mu^+\mu^-$	
< 525	$28 \pm 13 \pm 1$
525–565	–
565–780	$-2.7 \pm 4.1 \pm 0.4$
780–950	$-1.9 \pm 5.8 \pm 0.4$
950–1020	$0.5 \pm 3.7 \pm 0.4$
1020–1100	$4.2 \pm 3.4 \pm 0.4$
> 1100	–
Full range	$2.9 \pm 2.1 \pm 0.4$

$D^0 \rightarrow K^+K^-\mu^+\mu^-$	
< 525	$4 \pm 15 \pm 1$
525–565	–
> 565	$-2.5 \pm 6.8 \pm 0.6$
Full range	$-2.3 \pm 6.3 \pm 0.6$



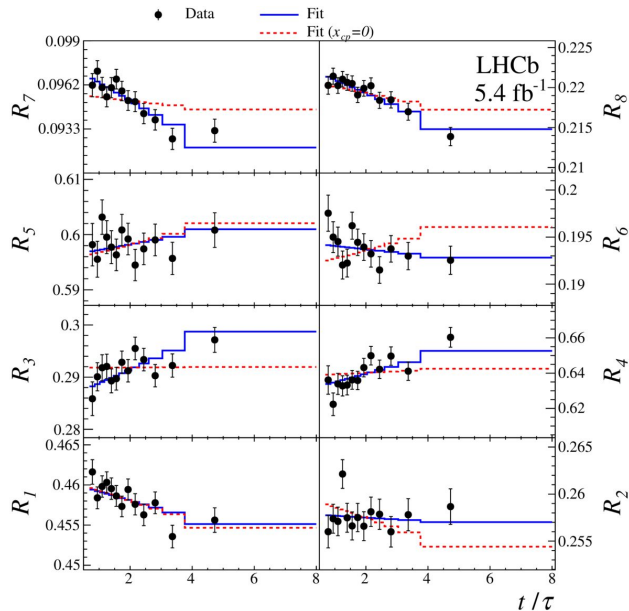
- Leverage ϕ region to control strong phases for A_{CP} vs q^2



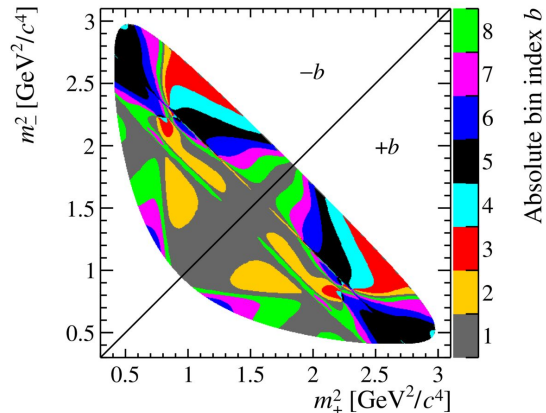
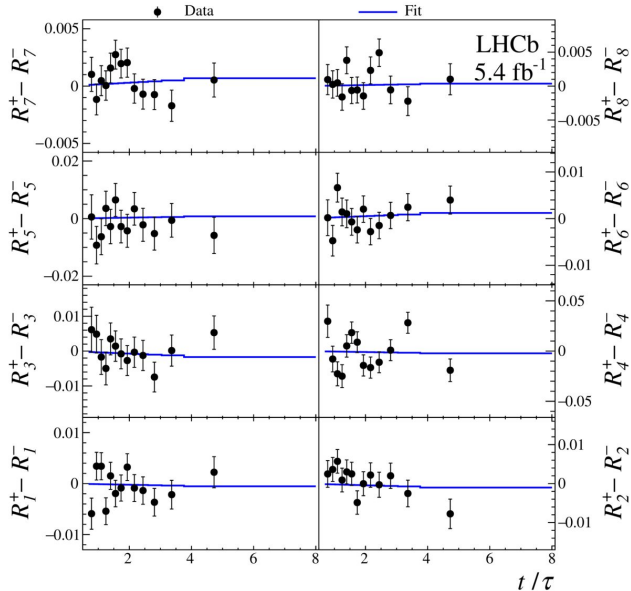
“Turn a bug into a feature”

Mixing and Indirect CPV

Bonza!



Daniel Červenkov



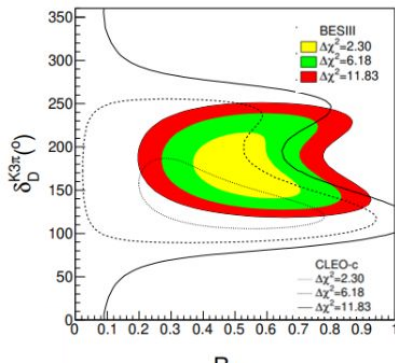
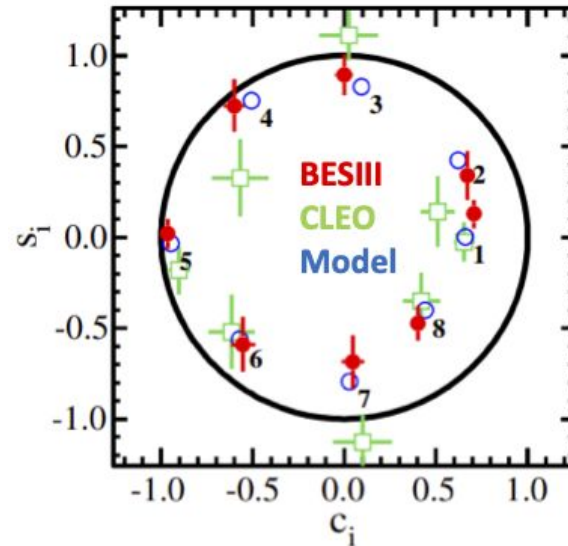
$$\Delta x = (-0.27 \pm 0.18(\text{stat}) \pm 0.01(\text{syst})) \times 10^{-3} \quad x_{CP} = (3.97 \pm 0.46(\text{stat}) \pm 0.29(\text{syst})) \times 10^{-3}$$

$$\Delta y = (0.20 \pm 0.36(\text{stat}) \pm 0.13(\text{syst})) \times 10^{-3} \quad y_{CP} = (4.59 \pm 1.20(\text{stat}) \pm 0.85(\text{syst})) \times 10^{-3}$$

$$R_{bj}^\pm \approx \frac{r_b + \sqrt{r_b} \text{Re}[X_b^*(z_{CP} \pm \Delta z)] \langle t \rangle_j + \frac{1}{4} [|z_{CP} \pm \Delta z|^2 + r_b \text{Re}(z_{CP}^2 - \Delta z^2)] \langle t^2 \rangle_j}{1 + \sqrt{r_b} \text{Re}[X_b(z_{CP} \pm \Delta z)] \langle t \rangle_j + \frac{1}{4} [\text{Re}(z_{CP}^2 - \Delta z^2) + r_b |z_{CP} \pm \Delta z|^2] \langle t^2 \rangle_j} \quad z_{CP} = -y_{CP} - ix_{CP}, \Delta z = -\Delta y - i\Delta x$$

Exploit Synergies

- One vital input to Ks $\pi\pi$ bin flip is strong phase differences c_i and s_i
- Also crucial for extraction of γ/ϕ_3
- Discussion point - What binning is the best? Current binning is driven by γ/ϕ_3 , are there better binnings? As Statistically limited, there is no limitation on the BESIII side
- Other measurements as well
 - coherence factors in $K3\pi$ and $K\pi\pi^0$
 - $\delta_{K\pi}$
 - Other modes to look at?



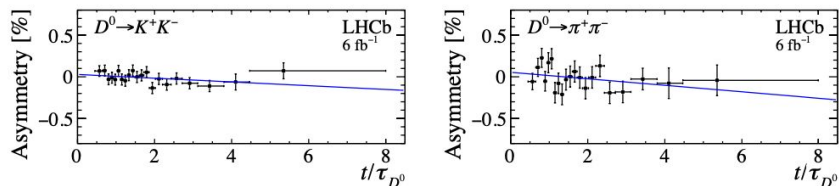
	c_i	s_i
1	$0.708 \pm 0.020 \pm 0.009$	$0.128 \pm 0.076 \pm 0.017$
2	$0.671 \pm 0.035 \pm 0.016$	$0.341 \pm 0.134 \pm 0.015$
3	$0.001 \pm 0.047 \pm 0.019$	$0.893 \pm 0.112 \pm 0.020$
4	$-0.602 \pm 0.053 \pm 0.017$	$0.723 \pm 0.143 \pm 0.022$
5	$-0.965 \pm 0.019 \pm 0.013$	$0.020 \pm 0.081 \pm 0.009$
6	$-0.554 \pm 0.062 \pm 0.024$	$-0.589 \pm 0.147 \pm 0.031$
7	$0.046 \pm 0.057 \pm 0.023$	$-0.686 \pm 0.143 \pm 0.028$
8	$0.403 \pm 0.036 \pm 0.017$	$-0.474 \pm 0.091 \pm 0.027$

More experimental results!

LHCb

Daniel Červenkov

$$\Delta Y_{K^+K^-} = (-2.3 \pm 1.5 \pm 0.3) \times 10^{-4} \quad \Delta Y_{\pi^+\pi^-} = (-4.0 \pm 2.8 \pm 0.4) \times 10^{-4}$$



- LHCb continues to exploit their large sample of Charm
- Belle II has made new precision measurements of the D^0/D^+ lifetime \rightarrow TDCPV measurements ready, only awaiting integration of luminosity

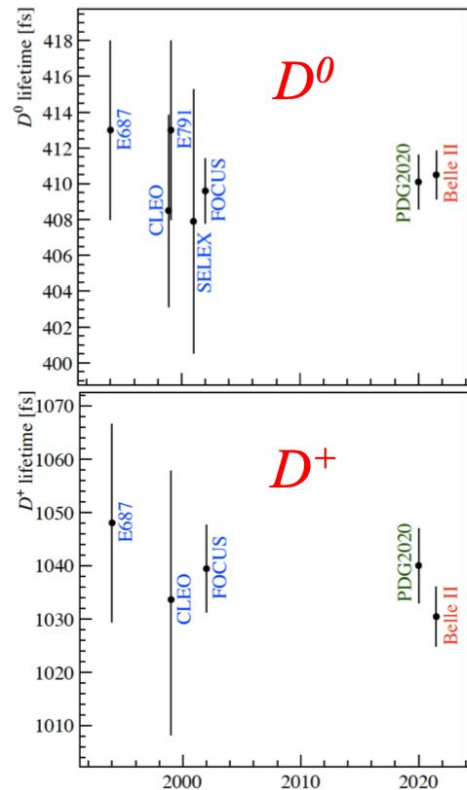
$$\tau(D^0) = 410.5 \pm 1.1 \pm 0.8 \text{ fs}$$

$$\tau(D^+) = 1030.4 \pm 4.7 \pm 3.1 \text{ fs}$$

$$\tau(D^+)/\tau(D^0) = 2.510 \pm 0.015$$

(accounted for correlated systematic uncertainties)

Belle II
Soeren Prell



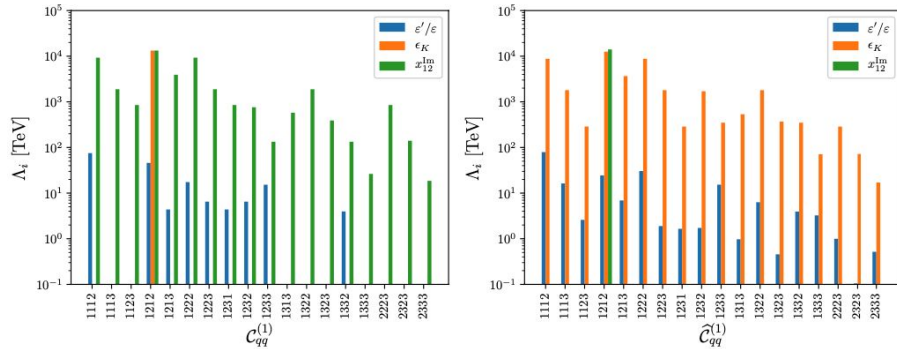
Year

A Bigger Picture

Pushes on Theory

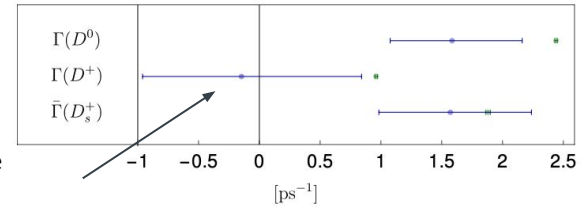
Maria Laura Piscopo

Use HQE to explore charm lifetimes and hence Γ_{12}

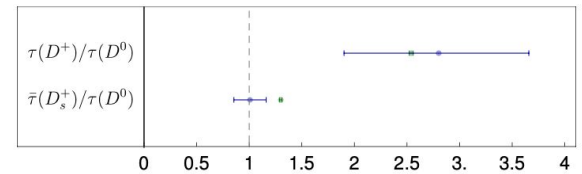


Jason Aebischer

- Concentrate on M_{12} in this work
- Use SMEFT to evaluate bounds on new physics contributions
- Master formula in WET (2 loop QCD running)/SMEFT (1 loop SMEFT-WET matching) done
- Leads to mixing between up/down bases - should consider simultaneously



Need to include higher-dim operators



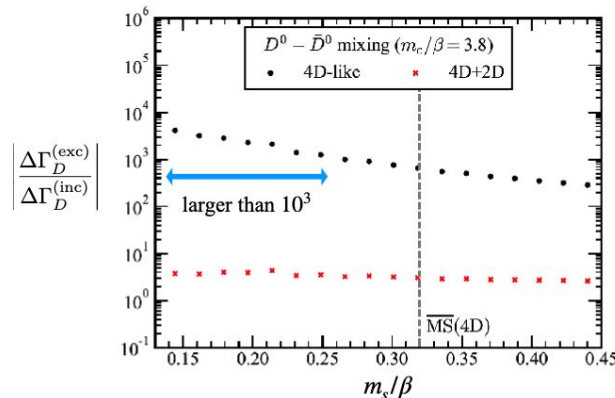
• experimental value • HQE prediction *

- HQE Fails for charm mixing, but OK for lifetimes?
- Need further inclusive $D \rightarrow X \text{ ell nu}$ measurements to help constrain
- N²LO-QCD corrections at $d=6$, Higher power corrections coming
- Long discussion on negative lifetime prediction which is not present in ratios

Pushes on Theory (2)

Hiroyuki Umeeda

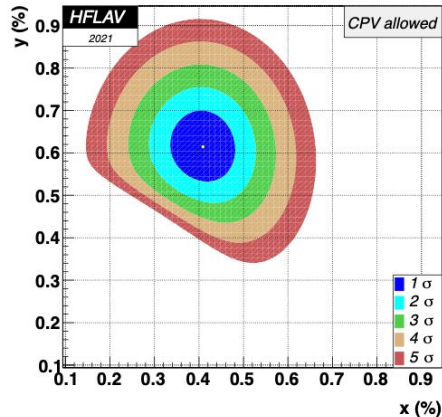
- Exclusive approach to Γ_{12} generally unsatisfactory and relying on data inputs
- Investigate Quark-Hadron duality violation in 't Hooft's model using a resonance-based method
- $\Delta\Gamma_D$ enhanced by more than $O(10^3)$ confirmed for the range of $0.14 < m_s/\beta < 0.25$, if the phase space function is given by 4D-like one.
- Analogous calculation of Δm_D still missing



$$m_c = m_c^{\overline{\text{MS}},4\text{D}}$$

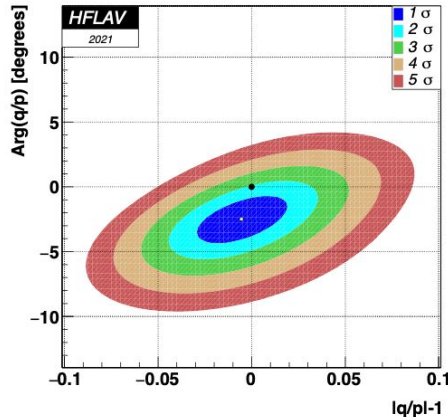
{ points: based only on the 4D-like phase space
 { crosses: based on the 4D-like phase space + 2D-specific one

Global Fits



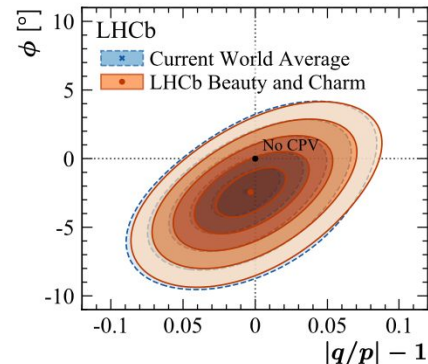
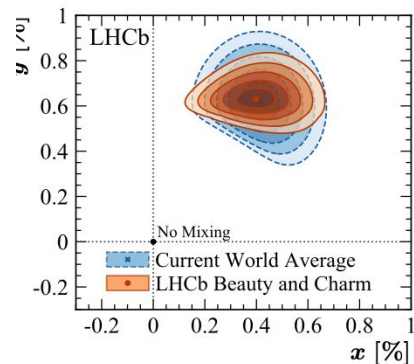
No mixing point $(x,y) = (0,0)$:
 $\Delta\chi^2 = 2099$, excluded at $\gg 11.5\sigma$

HFLAV Alan Schwartz

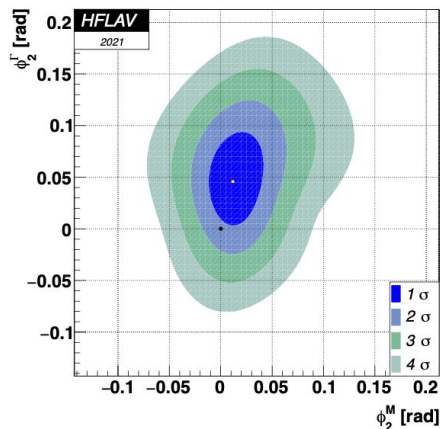


No CPV point $(|q/p|, \phi) = (1,0)$:
 $\Delta\chi^2 = 5.633$, excluded at 1.6σ

LHCb Daniel Červenkov



Using new description from Kagan/Silvestrini, fit separately for absorptive and dispersive phases



- Is the future to fit B+D simultaneously for ultimate precision? What about K?

Summary of the Summary

Charm is even more charming than before

Direct CPV established
 $x > 0 @ > 8 \sigma$

There are many new results in the pipeline on both theory and experimental side

Barely touched on baryons in this workshop

Watch this space

Backup

Parameter	No <i>CPV</i>	No direct <i>CPV</i> in DCS decays	<i>CPV</i> -allowed	<i>CPV</i> -allowed 95% CL Interval	
x (%)	$0.44^{+0.13}_{-0.15}$	0.409 ± 0.048	$0.409^{+0.048}_{-0.049}$	[0.313, 0.503]	
y (%)	0.63 ± 0.07	$0.603^{+0.057}_{-0.056}$	$0.615^{+0.056}_{-0.055}$	[0.509, 0.725]	
$\delta_{K\pi}$ ($^\circ$)	$8.9^{+8.9}_{-9.8}$	$5.5^{+8.3}_{-9.9}$	$7.2^{+7.9}_{-9.2}$	[-12.6, 21.8]	
R_D (%)	0.344 ± 0.002	0.343 ± 0.002	0.343 ± 0.002	[0.340, 0.347]	
A_D (%)	—	—	-0.70 ± 0.36	[-1.40, 0.00]	
$ q/p $	—	1.005 ± 0.007	0.995 ± 0.016	[0.96, 1.03]	$\phi_2^M = (0.7 \pm 1.0)^\circ$
ϕ ($^\circ$)	—	$-0.18^{+0.28}_{-0.29}$	-2.5 ± 1.2	[-4.91, -0.19]	$\phi_2^\Gamma = (2.6 \pm 1.7)^\circ$
$\delta_{K\pi\pi}$ ($^\circ$)	$21.8^{+23.5}_{-23.9}$	$22.3^{+21.9}_{-23.0}$	$23.0^{+21.8}_{-22.9}$	[-22.6, 64.9]	
A_π (%)	—	0.027 ± 0.137	0.045 ± 0.137	[-0.22, 0.31]	
A_K (%)	—	-0.133 ± 0.136	-0.113 ± 0.137	[-0.38, 0.15]	
x_{12} (%)	—	0.409 ± 0.048		[0.314, 0.503]	
y_{12} (%)	—	$0.603^{+0.057}_{-0.056}$		[0.495, 0.715]	
ϕ_{12} ($^\circ$)	—	$0.58^{+0.91}_{-0.90}$		[-1.20, 2.42]	
$\chi^2/\text{d.o.f.}$	$98.68/52 = 1.90$	$66.27/53 = 1.25$	$63.64/51 = 1.25$		