

Recent theoretical developments for top-quark production

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Top quark **heaviest** known elementary particle

Yukawa coupling $\lambda_t \sim 1 \Rightarrow$ link to EW symmetry breaking:

- top-loop corrections to $M_H \Rightarrow$ hierarchy problem

$$\text{---} \circ \text{---} \Rightarrow \delta M_H = -\frac{\lambda_t^2}{8\pi^2} \Lambda_{UV}^2 + \dots$$

\Rightarrow top-partners in BSM models (stop in MSSM, T in Little-Higgs...)

Top established at Tevatron:

plethora of measurements (Γ_t , spin correlations, charge asymmetry...)

room for new physics (V_{tb} , FCNC tcZ -couplings, heavy resonances in $t\bar{t}$...)

Top quark **precision** physics:

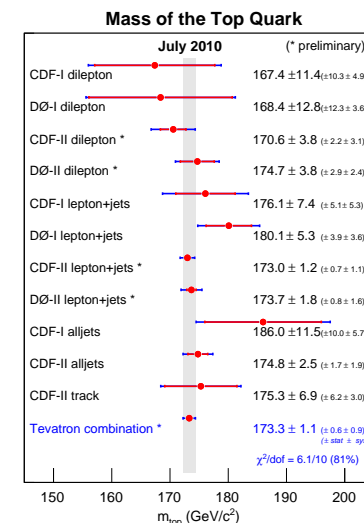
$$\Delta\sigma_{t\bar{t}}/\sigma_{tt} \sim 7\% \quad , \quad \Delta m_t/m_t < 1\%$$

\Rightarrow Challenge for theory! (Focus of this talk)

Large LHC cross section $\sigma_{t\bar{t}}(14\text{TeV}) \approx 900 \text{ pb}$

+ Plenty of tops to study

- Background for other processes



Top-pair production

QCD production, two LO subprocesses:

$$q\bar{q} \rightarrow t\bar{t} : \begin{cases} 90\% \\ 20 - 10\% \end{cases} , \quad gg \rightarrow t\bar{t} \begin{cases} 10\% \\ 80 - 90\% \end{cases} \quad \begin{matrix} \text{Tevatron} \\ \text{LHC7 - 14} \end{matrix}$$

(NLO QCD corrections

(Nason, Dawson Ellis 88, Beenakker et.al. 89/91, ...)

EW corrections

(Bernreuther/Fuecker/Si; Kühn/Scharf/Uwer, 05/06)

Parton shower matching

(Frixione/Nason/Webber 03, Frixione/Nason/Ridolfi 07))

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Single top production

EW production $\sim V_{tb}$, LO Production channels

$$q\bar{q}' \xrightarrow{W^+} t\bar{b} \begin{cases} 0.54\text{pb} \\ 7.8\text{pb} \end{cases} \quad b\bar{q}' \rightarrow t\bar{q}' \begin{cases} 1.15\text{pb} \\ 150\text{pb} \end{cases} \quad gb \rightarrow W^- t \begin{cases} 0.14\text{pb} & \text{TeV} \\ 44\text{pb} & \text{LHC14} \end{cases}$$

(NLO QCD

(Smith/Willenbrock 96; Giele et.al. 96; Stelzer et.al. 97...)

EW corrections

(Beccaria et.al. 06)

Parton shower matching

(Frixione et.al. 05; Alioli et.al. 09; Re 10))

Hadron collider cross sections from **QCD factorization**

(Collins, Soper, Sterman)

$$\sigma_{NN'}(s) = \sum_{pp'} \int dx_1 dx_2 f_{N/p}(x_1, \mu_f) f_{N'/p'}(x_2, \mu_f) \hat{\sigma}_{pp'}(sx_1x_2, \mu_f)$$

- $\hat{\sigma}_{pp'}$: **partonic cross section**: compute in perturbation theory
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PDF uncertainties for top:

(e.g. Guffanti/Rojo arXiv:1008.4671 [hep-ph])

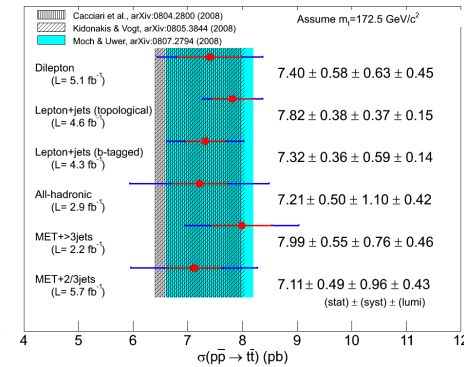
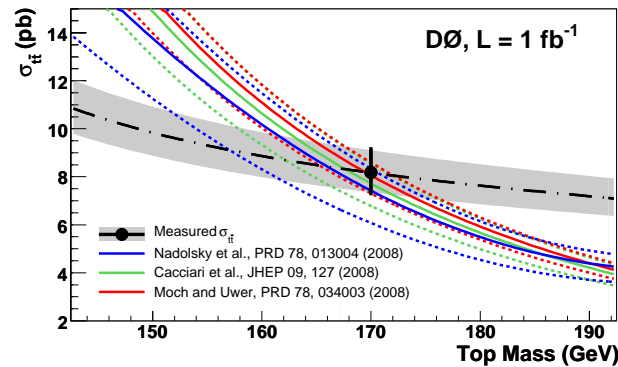
	CTEQ6.6	MSTW2008	NNPDF2.0	ABKM09	HERAPDF1.0
$\sigma_{t\bar{t}}^{\text{NLO}}(7\text{TeV})[pb]$	147.7 ± 6.4	159.0 ± 4.7	160.0 ± 5.9	131.9 ± 4.8	136.4 ± 4.7

- Different α_s values
- Differences in gluon pdf at large x (impact of Tevatron jet-data)

Experimental knowledge of $t\bar{t}$ cross section:

Tevatron: $\Delta\sigma_{t\bar{t}} = 6.8\%$; LHC Goal: $\Delta\sigma_{t\bar{t}} \approx 5\%$

Sensitivity to m_t , gluon PDFs, ...

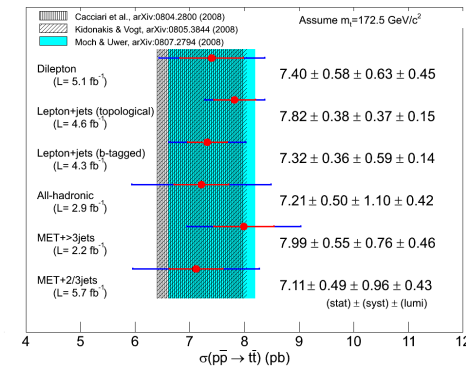
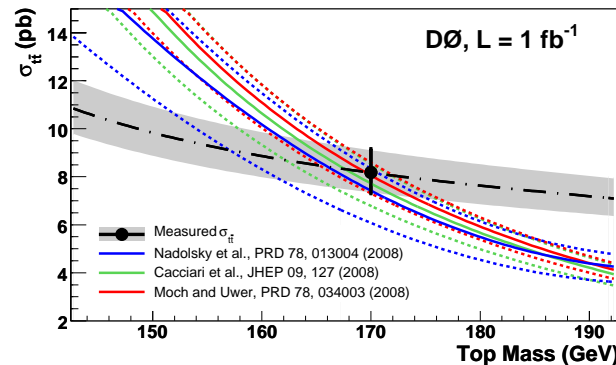


Theory status: NLO + higher-order soft gluons $\Rightarrow \Delta\sigma_{t\bar{t}} \approx 10\%$

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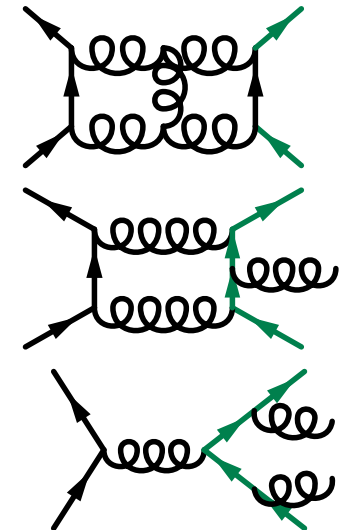
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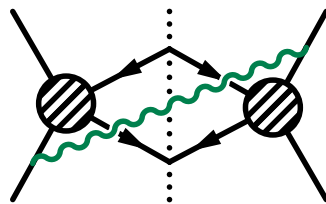
Building blocks for NNLO:

- **two-loop** $t\bar{t}$, ($m_t \rightarrow 0$: Czakon/Mitov/Moch 07;
 $q\bar{q}$: Czakon 08; Bonciani et.al. 08/09)
- **one-loop** $t\bar{t} + j$ (Dittmaier/Uwer/Weinzierl 07)
 $t\bar{t}$ squared
(Körner et.al. 05-09, Anastasiou/Mert-Aybert 08)
- **tree** $t\bar{t} + jj$ (IR subtraction: Czakon 10)

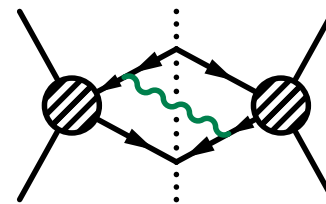


NLO corrections to σ_{tot} **enhanced** for $\beta = \sqrt{1 - 4m_t^2/\hat{s}} \rightarrow 0$

Soft corrections: (Resummation in Mellin space: Sterman 87; Catani, Trentadue 89, Kidonakis, Sterman 97, Bonciani et.al. 98, ...)

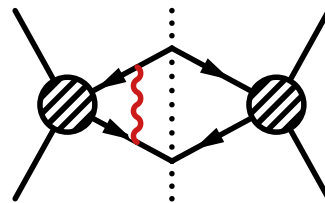


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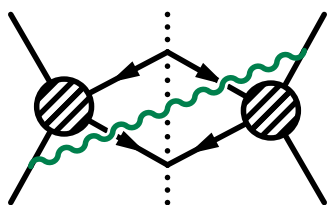
Coulomb gluon corrections (Fadin, Khoze 87; Peskin, Strassler 90, NRQCD, ...)



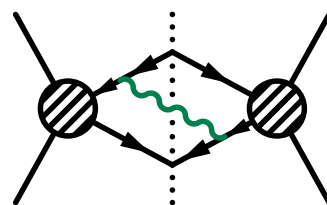
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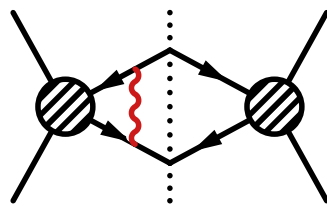


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Counting of threshold corrections:

$$\hat{\sigma}_{pp'} \propto \sigma^{(0)} \exp \left[\underbrace{\ln \beta g_0(\alpha_s \ln \beta)}_{\text{(LL)}} + \underbrace{g_1(\alpha_s \ln \beta)}_{\text{(NLL)}} + \underbrace{\alpha_s g_2(\alpha_s \ln \beta)}_{\text{(NNLL)}} + \dots \right] \\ \times \sum_{k=0} \left(\frac{\alpha_s}{\beta} \right)^k \times \{1 \text{ (LL, NLL)}; \alpha_s, \beta \text{ (NNLL)}; \dots\},$$

Application of β -summation to $t\bar{t}$

- NLL summation of $\ln\beta$ terms (Bonciani et.al. 98)
- Development of NNLL resummations:
 - 2-loop soft anomalous dimension (Becher/Neubert; Kidonakis; Mitov/Sterman/Sung; Beneke/Falgari/CS; Ferroglia et.al. 09)
 - soft/Coulomb factorization (Beneke, Falgari, CS 09/10)

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- NNLO_{approx} (also implemented in HATHOR, Aliev et.al. 10)
 - α_s^2 expansion of NNLL (Moch, Uwer (Langenfeld) 08/09)
 - + all potential corrections (Beneke, Czakon, Falgari, Mitov CS, 09)

$$\text{e.g. } \sigma_{q\bar{q}}^{(2)} = \frac{3.61}{\beta^2} + \frac{1}{\beta} \left(-140.4 \ln \beta^2 + 32.1 \ln \beta + 3.95 \right) \\ + 910.2 \ln \beta^4 - 1315.5 \ln \beta^3 + 592.3 \ln \beta^2 + 528.6 \ln \beta + C_{q\bar{q}}^{(2)}$$

- Combined $\ln \beta$, β^{-1} NNLL summation

(Beneke, Falgari, Klein, CS, in progress)

Resummation for other observables:

- Pair invariant mass cross sections (Kidonakis, Sterman 97)

$$\frac{d\sigma(t\bar{t})}{dM_{t\bar{t}}} \Rightarrow \left[\frac{\log^n(1-z)}{1-z} \right]_+, \quad z = \frac{M_{t\bar{t}}^2}{\hat{s}}$$

- One particle inclusive cross sections: (Laenen, Oderda, Sterman 98)

$$\frac{d\sigma(t+X)}{ds_4} \Rightarrow \left[\frac{\log^n(s_4/m^2)}{s_4} \right], \quad s_4 = p_X^2 - m_t^2$$

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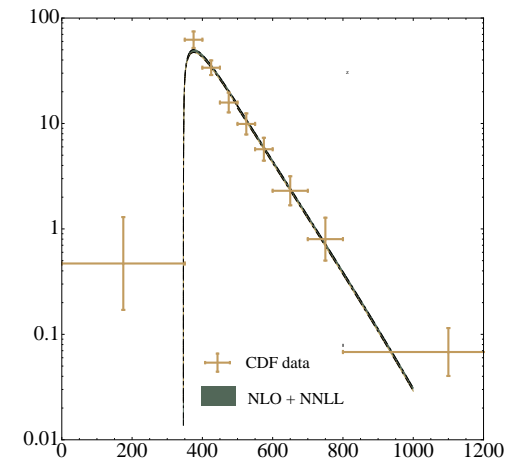
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Applications to top-pairs:

- $\mathcal{O}(\alpha_s^2)$ expansion (Kidonakis et.al. 01/03, Ahrens et.al. 09, Kidonakis 10)
- NNLL $M_{t\bar{t}}$ distribution (Ahrens et.al. 10)

Single Top:

- $\mathcal{O}(\alpha_s^2)$ expansion (Kidonakis 06-10)
- NNLL resummation (Zhu et.al. 10)



(Ahrens et.al. 10)

$\sigma_{t\bar{t}}$ (pb)	Tevatron	LHC7	LHC10	LHC14
NLO	$6.50^{+0.32+0.33}_{-0.70-0.24}$	150^{+18+8}_{-19-8}	380^{+44+17}_{-46-17}	842^{+97+30}_{-97-32}
NNLO _{approx} (β)	$7.13^{+0.00+0.36}_{-0.33-0.26}$	162^{+3+9}_{-3-9}	407^{+11+17}_{-5-18}	895^{+29+31}_{-7-33}
NNLO _{approx} (β) + NNLL (Beneke, Falgari, Klein, CS in progress)	$7.14^{+0.13+0.36}_{-0.19-0.26}$	162^{+4+9}_{-2-9}	407^{+14+17}_{-4-18}	896^{+36+31}_{-7-33}
NLO + NNLL ($M_{t\bar{t}}$) (Ahrens et.al. 10)	$6.48^{+0.17+0.32}_{-0.21-0.25}$	146^{+7+8}_{-7-8}	368^{+20+19}_{-14-15}	813^{+50+30}_{-36-35}
NNLO _{approx} (s_4) ($m_t=173$; Kidonakis 10)	$7.08^{+0.00+0.36}_{-0.24-0.27}$	163^{+7+9}_{-5-9}	415^{+17+18}_{-21-19}	920^{+50+33}_{-39-35}

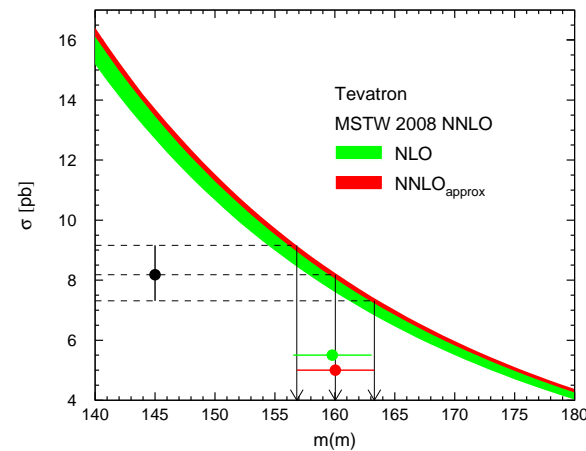
($m_t = 173.1$ GeV, $\mu_f = m_t$, MSTW08NNLO)

Application: (Moch, Langenfeld, Uwer 09)

Comparison to Tevatron data:

$$m_t(\overline{MS}) = 160.0^{+3.3}_{-3.2} \text{ GeV}$$

$$\Rightarrow m_t(\text{pole}) = 168.9^{+3.5}_{-3.4} \text{ GeV}$$



Top quark **unstable**: $t \rightarrow bW^+ \rightarrow bff'$

Narrow-width approximation (NWA):

$$\frac{i}{p^2 - m_t^2 + im_t\Gamma_t} \Rightarrow \frac{2\pi}{2\Gamma_t m_t} \delta(p^2 - m_t^2)$$

$$\sigma_{pp' \rightarrow b\bar{b}4f} \Rightarrow \sigma_{pp' \rightarrow t\bar{t}} \times \frac{\Gamma_{t \rightarrow bf_1 f_2}}{\Gamma_t} \frac{\Gamma_{\bar{t} \rightarrow \bar{b}f_3 f_4}}{\Gamma_t}$$

expect finite width corrections $\mathcal{O}(\Gamma_t/m_t) \sim 1\%$

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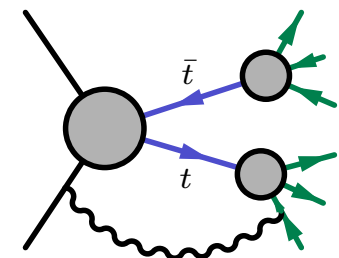
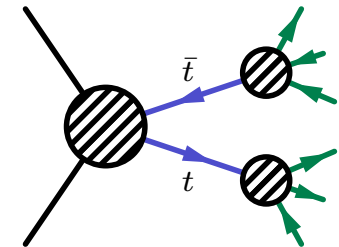
Radiative corrections:

(Double) pole approximation

- **Factorizable** corrections to production/decay
- **Nonfactorizable** corrections

(Cancellations for σ_{tot} : Melnikov, Yakovlev; Fadin et.al. 93)

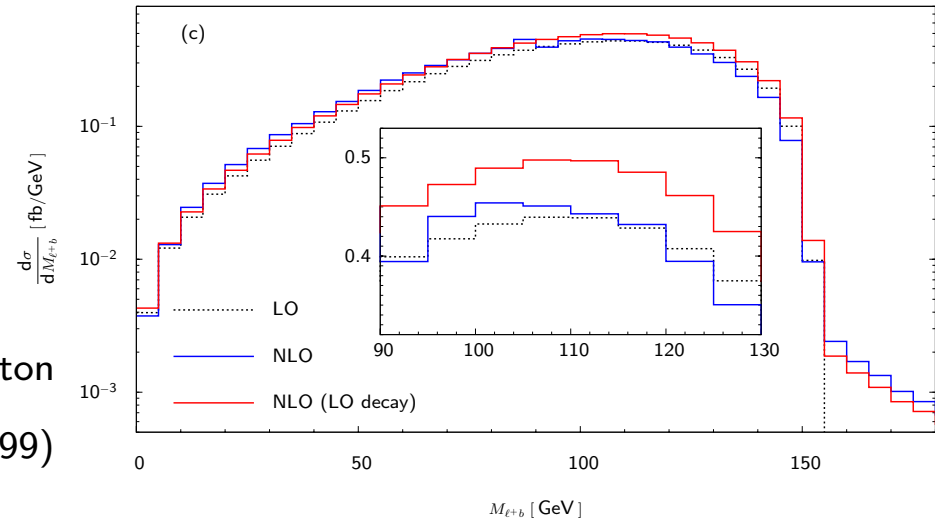
(For $e^-e^+ \rightarrow W^-W^+ \rightarrow 4f$ see Berends et. al. 98; Denner et.al. 99, Jadach et.al 99, Beneke et.al 07/08)



Top pairs

- Factorizable corrections, spin correlations, NWA
(Bernreuther et.al. 04/10, Melnikov/Schulze 09)
- Nonfact. corrections (parton level: Beenakker, Berends, Chapovsky 99)

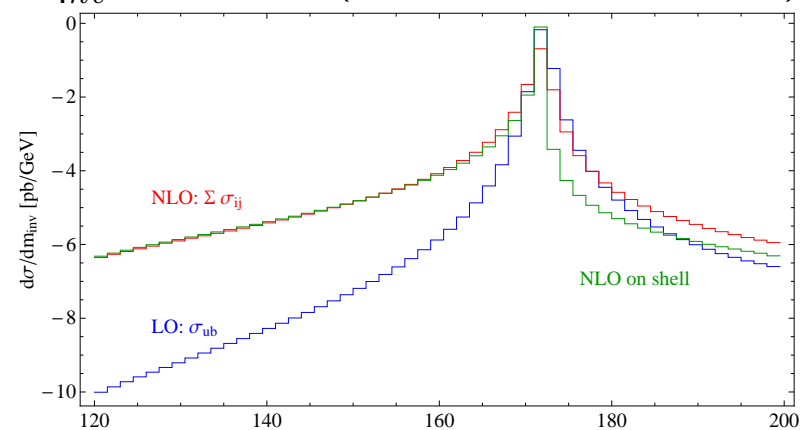
$M_{\ell+b}$: (Melnikov/Schulze 09)



Single top

- Factorizable corrections, NWA
(Campbell/Ellis/Tramontano 04, spin-correll.: Cao et.al. 04/05)
- Nonfactorizable corrections
(Falgari, Mellor, Signer 10)

m_{inv} : (Falgari, Mellor, Signer 10)



Higgs production:

$$H \rightarrow W^+W^-, Hqq \rightarrow W^+W^-qq$$

- Background from $t\bar{t}$, $t\bar{t} + \text{jets}$
- NWA underestimates $t\bar{t}$ background
(Kauer/Zepfenfeld 01)

Associated $t\bar{t}H$ production:

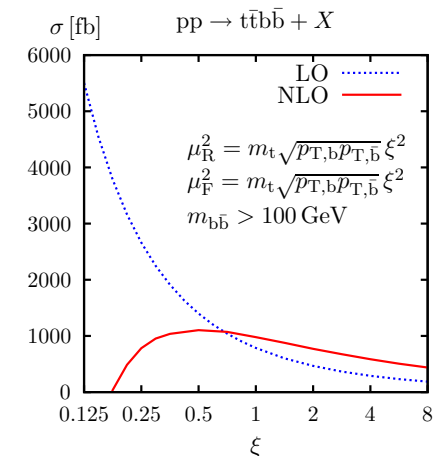
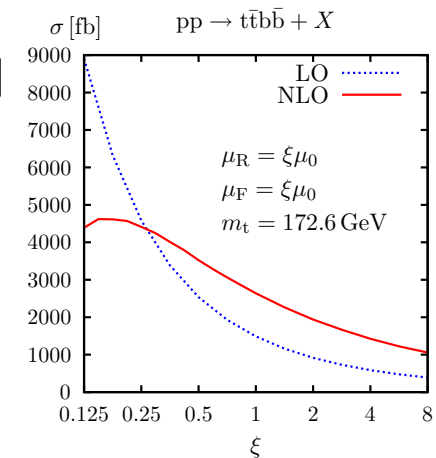
- $t\bar{t}b\bar{b}$, $t\bar{t} + \text{jets}$ background

Recent NLO-multileg progress:

- $t\bar{t}j$ (Dittmaier/Uwer/Weinzierl 07);
- $t\bar{t}b\bar{b}$ (Bredenstein et.al. 08-10);
- $t\bar{t}jj$ (Bevilacqua et.al. 10)
- (1-loop amp $b\bar{b}W^+W^-$: v.Hameren et.al. 09)

Complicated **multiscale** processes:

scale choice?



(Bredenstein et.al. 10)

(Selected) recent theory activities for production cross sections

- Total $t\bar{t}$ cross section: towards NNLO, NNLL resummation
- Corrections to top-production \otimes decay:
NLO+spin correlations, nonfactorizable corrections
- Top as background: $t\bar{t} + j$, $t\bar{t} + jj$ at NLO

Not discussed

(\Rightarrow TOP2010 proceedings)

- top-mass definitions

(see e.g. Hoang/Stewart arXiv:0808.0222 [hep-ph]; Corcella arXiv:1008.4498 [hep-ph])

- Charge asymmetry (BSM e.g. Ferrario/Rodrigo arXiv:1007.4328 [hep-ph];
higher order SM: Almeida/Sterman/Vogelsang 08; Ahrens et.al.; Bernreuther/Si 10)

- Spin correlations (Mahlon arXiv:1007.1716 [hep-ph])

- Top and BSM ($t\bar{t}t\bar{t}$ final states in strong EWSB, light $Q = 5/3$ top partners, . . .)