

Hastening Slowly from MSLRMs to

NMSGUT :
All ready to roll ?

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- Peroration
- SO(10) and MSGUT basics
- SO(10) Fitting Frenzy TO MSGUT Doom : Sumit Garg
- Saving the MSGUT : New Minimal Susy GUT Sumit Garg
- Threshold Corrections at M_G and M_X
- Rolling to be Ready : Searches for $m_f/\theta_f/\Gamma_B^{d=5}$ -viable fits

R PARITY and B-L

- SM : Gauge Invariance, Renormalizability \Rightarrow
 $B, L(\text{perturbative}) \Rightarrow B - L$ (Exact ,Unique Global U(1)).
- MSSM:Sfermions & Shiggs \Rightarrow
 $\mathcal{L}_{\Delta_{B,L} \neq 0} = [W]_{R_p} = [\mu' LH + \lambda LLe^c + \lambda' LQd^c + \lambda'' u^c d^c d^c]_F \Rightarrow$
catastrophic B, L violation $\Rightarrow \tau_p^{d=4} \sim \left(\frac{g M_S}{\lambda' M_X}\right)^4 \tau_p^{d=6} \Rightarrow$
 $\lambda'_{R} < 10^{-12}$
- $R_p : Z_2 : \text{Susy Particles odd}$: forbids B,L violating terms
 Mohapatra : (1986) : $R_p = (-1)^{3(B-L)+2S} = (-)^{2S} M_p \Rightarrow$
 $M_p \subset U(1)_{B-L} \subset G_{LR} \subset G_{PS} \subset SO(10)$
- Even B-L vevs(M_ν Compatible) $\Rightarrow R\sqrt{\sqrt{\quad}} \Rightarrow : \Rightarrow$
 LSP Stable : good as Dark Matter!!
 MSLRMs : CSA,Benakli,Senjanovic, Melfo(1995-8)

VIRTUES OF SO(10) UNIFICATION

- $\{Q_L, L_L, u_L^c, d_L^c, l_L^c\} \oplus \nu_L^c \equiv 16$: Tight and complete !

- Simple Tri-band FM Higgs Channel Spectrum

$$16 \otimes 16 = 10 \oplus 120 \oplus 126 \Rightarrow (10 + 120 + \overline{126}_H)$$

$$\overline{126} = (15, 2, 2) + \Delta_R(10, 1, 3) + \Delta_L(\overline{10}, 3, 1) + (6, 1, 1)$$

- $M_p \subset U(1)_{B-L} \subset G_{LR} \subset G_{PS} \subset SO(10) \oplus \langle \Delta_{L,R} \rangle \Rightarrow R_p$,
Stable LSP

- NATURAL HOME TO BOTH SEESAWS :

$$\vec{\Delta}_R(1, 3, -2), \vec{\Delta}_L(3, 1, 2) \subset \overline{126} \text{ PRESERVE } R_p !!:$$

$$M_{B-L} \sim \langle \vec{\Delta}_R \rangle_{SM=0} \Rightarrow M_{\nu^c} \Rightarrow M_{\nu}^I$$

$$\frac{v_W^2}{M_{B-L}} \sim \langle \vec{\Delta}_L \rangle_{Y=2, T_{3L}=-1} \Rightarrow M_{\nu}^{II}$$

TWO SCHOOLS OF SO(10)

Renormalizable SO(10)	NON-REN GUTS
<p style="color: blue;">Renormalizable couplings</p> <p style="color: green;">No ad-hoc symmetries</p> <p style="color: magenta;">Large(126,210,..) few (AS!)</p> <p style="color: cyan;"># Parameter minimal</p> <p style="color: purple;">No Higgs duplication</p> <p style="color: red;">$M_p \subset SO(10)$ gauged</p> <p style="color: blue;">Only B-L even vevs</p> <p style="color: magenta;">Higgs-Matter distinct</p> <p style="color: green;">a) $210 \oplus 126 \oplus \overline{126}$</p> <p style="color: blue;">b) $54 \oplus 45 \oplus 126 \oplus \overline{126}$</p>	<p style="color: blue;">Non Renorm. couplings</p> <p style="color: green;">Ad-hoc symmetries necessary</p> <p style="color: magenta;">Small (10,16,45,54) irreps (AF)</p> <p style="color: cyan;">Unlimited # parameters</p> <p style="color: purple;">Duplicates Higgs</p> <p style="color: red;">R_p broken or ungauged</p> <p style="color: blue;">“string motivated” Z_2</p> <p style="color: magenta;">Higgs-Matter mix</p> <p style="color: green;">$16_H^n \oplus 10 \oplus 45^m$ plethora</p>

Guts OF MSGUT

- **AM Higgs** : $\langle \mathbf{210}(\Phi_{ijkl}), \overline{\mathbf{126}}(\overline{\Sigma}_{ijklm}), \mathbf{126} \rangle \Rightarrow$
Susy SO(10) \longrightarrow MSSM

- **Superpotential**

$$\begin{aligned}
 W &= m \mathbf{210}^2 + \lambda \mathbf{210}^3 + M \mathbf{126} \cdot \overline{\mathbf{126}} + \eta \mathbf{210} \cdot \mathbf{126} \cdot \overline{\mathbf{126}} \\
 &+ 10 \cdot \mathbf{210}(\gamma \mathbf{126} + \bar{\gamma} \overline{\mathbf{126}}) \\
 &+ M_H \mathbf{10}^2 + h_{AB} \mathbf{16}_A \cdot \mathbf{16}_B + f'_{AB} \mathbf{16}_A \mathbf{16}_B
 \end{aligned}$$

Superpotential Parameters : **(25) Minimal !!** [ABMSV\(2003\)](#)

- **GUT scale VEVs** : $SO(10) \rightarrow MSSM$

$$\begin{aligned}
 \langle (15, 1, 1) \rangle_{\mathbf{210}} &: a & \langle (15, 1, 3) \rangle_{\mathbf{210}} &: \omega \\
 \langle (1, 1, 1) \rangle_{\mathbf{210}} &: p \\
 \langle (10, 1, 3) \rangle_{\overline{\mathbf{126}}} &: \bar{\sigma} & ; & \langle (\overline{\mathbf{10}}, 1, 3) \rangle_{\mathbf{126}} &: \sigma
 \end{aligned}$$

- D Terms, preserve SUSY : $|\sigma| = |\bar{\sigma}|$
- F Terms : **SSB completely analyzable !!** 4 eqns \Rightarrow **Cubic in**

$$x = -\lambda\omega/m : \xi = \frac{\lambda M}{\eta m}. \text{ (ABMSV 2003)}$$

$$8x^3 - 15x^2 + 14x - 3 = -\xi(1-x)^2$$

- Units : $\frac{m}{\lambda}$

$$\tilde{a} = \frac{(x^2+2x-1)}{(1-x)} \quad ; \quad \tilde{p} = \frac{x(5x^2-1)}{(1-x)^2} \quad ; \quad \tilde{\sigma}\tilde{\sigma} = \frac{2}{\eta} \frac{\lambda x(1-3x)(1+x^2)}{(1-x)^2}$$

- Chiral GUT scale spectra : 52 MSSM multiplet sets,

26 MSSM types : 18 unmixed , 8 mixed : 504 Fields

CSA, Girdhar(2003) ; Fukuyama, Ilakovac, Kikuchi, Mejanac,

Okada (2004), BMSV (2004), CSA Girdhar(2004)

Complete gauge, spinor couplings , Clebsches : CSA Girdhar

(2002) (2004) Spectra \Rightarrow RG including Threshold effects

etc. CSA, Girdhar (2004)

PARAMETER COUNTING & MINIMALITY

- Minimality: All desire and most claim it ! : Grounds : a) Renorm/Non renorm. (b) Fewer Representations (c) Size of Irreps (AS/AF)(d) Parameter Counting (e) Number of ad-hoc symmetries (f) Higgs channel sparseness/completeness
- MSGUT: Renormalizable, has few irreps AND only one of each, no ad-hoc symmetries, but is AS (but $\Delta_X > 1.5$!!) and Higgs channel incomplete
- COUNTING : $m_{210}, M_{126}, M_H : 3 \times 2 = 6$;
 $\lambda, \eta, \gamma, \bar{\gamma} : 4 \times 2 = 8$; $y_{10} \oplus y_{\overline{126}} : 2 \times 2 \times 6 = 24$;
 $Sum = 38$ LESS (4 (Rephasing) + 9 (SO(10)-U(3) flavour)
equals 25 superpotential parameters, two more (M_H) fixed by Doublet fine TUNING = 23 real parameters
- PARAMETER COUNTING MINIMAL !! : COMPETITORS (SU(5)NONREN ETC) : > 40 PARAMETERS

MSSM_{eff} : Light Doublets

- Doublet Mass matrix CSA, Girdhar (2003) : **10, $\overline{126}$, 126, 210**

$$\mathcal{H} = \begin{pmatrix} -M_H & +\bar{\gamma}\sqrt{3}(\omega - a) & -\gamma\sqrt{3}(\omega + a) & -\bar{\gamma}\bar{\sigma} \\ -\bar{\gamma}\sqrt{3}(\omega + a) & 0 & -(2M + 4\eta(a + \omega)) & 0 \\ \gamma\sqrt{3}(\omega - a) & -(2M + 4\eta(a - \omega)) & 0 & -2\eta\bar{\sigma}\sqrt{3} \\ -\sigma\gamma & -2\eta\sigma\sqrt{3} & 0 & -2m + 6\lambda(\omega - a) \end{pmatrix}$$

- $\bar{U}^T \mathcal{H} U = Dg(m_H^{(1)}, m_H^{(2)}, \dots)$; $h^{(i)} = U_{ij} H^{(j)}$; $\bar{h}^{(i)} = \bar{U}_{ij} \bar{H}^{(j)}$

- **Fine Tune M_H (INEVITABLY COMPLEX!) \Leftarrow**

$$Det \mathcal{H} = 0 \Rightarrow \text{Light Doublets } H^{(1)}, \bar{H}^{(1)} \Rightarrow E \ll M_X$$

$$h^{(i)} \rightarrow \alpha_i H^{(1)} \quad ; \quad \alpha_i = U_{i1}; \quad \bar{h}^{(i)} \rightarrow \bar{\alpha}_i \bar{H}^{(1)} \quad ; \quad \bar{\alpha}_i = \bar{U}_{i1}$$

$$\mathcal{H} \alpha = 0 \quad ; \quad \bar{\alpha}^T \mathcal{H} = 0 \quad \Rightarrow \alpha, \bar{\alpha}.$$

(ABMSV(2003), BMSV(2004), NMSGUT CSA, Garg(2006))

FERMION YUKAWAS IN SO(10)

- **Data for GUT To Explain :**

Measured(17) : $m_{q,l}, \theta_i^{CKM}, \delta^{CKM}, \Delta m_\nu^2, \theta_{12,23}^{PMNS}$

Bounded: $\theta_{13}^{PMNS} < .1$

- **Awaited (4) :** $M_\nu, \delta^{PMNS}, \alpha_{1,2}^{PMNS}$

- Yukawa couplings : $h = h^T, f = f^T, g = -g^T$

$W = \mathbf{16}_A \times \mathbf{16}_B \cdot (h_{AB}\mathbf{10} + f_{AB}\overline{\mathbf{126}} + g_{AB}\mathbf{120})$

- MSGUT(AM+CKN 1983)/**GENERIC : BABU**

MOHAPATRA(1992) : USE ONLY $\mathbf{10} + \overline{\mathbf{126}}$

- **MSGUT SPECIFIC** formulae need 16×16 clebsches

CSA, Girdhar(2004,5), **NULL EIGENVECTORS OF \mathcal{H} CSA,**

Bajc, Melfo, Senjanovic, Vissani ; CSA, Girdhar(2005)

$$y^u = (\hat{h} + \hat{f})$$

$$y^\nu = (\hat{h} - 3\hat{f})$$

$$y^d = (r_1\hat{h} + r_2\hat{f})$$

$$y^l = (r_1 \hat{h} - 3r_2 \hat{f})$$

- Weinberg Operator Coefficients :

$$\begin{aligned} \kappa_\nu^I &= vr_4 \hat{n} \\ \kappa_\nu^{II} &= 2vr_3 \hat{f} \\ \hat{n} &= (\hat{h} - 3\hat{f}) \hat{f}^{-1} (\hat{h} - 3\hat{f}) \end{aligned}$$

- Babu and Mohapatra (1992): $\mathbf{10} \oplus \overline{\mathbf{126}} \Leftrightarrow m_{q,l} \Rightarrow$
Predictive in the Neutrino Sector ?! : failure (1992,93,94..)
- Matsuda, Koide , Fukuyama, Nishiura (2002): Type I, large θ^{PMNS} , **GENERIC**fit. CP violation!(complex couplings)

Type II: BM -BSV FITTING FRENZY

- Bajc, Senjanovic, Vissani (2003) Large PMNS mixing angle
 $b - \tau$ unification connection

$$M_\nu^{II} \sim f \langle \Delta_L \rangle \sim (M_d - M_l) \sim m_\tau \begin{pmatrix} \epsilon^2 & \epsilon^2 \\ \epsilon^2 & \frac{(m_b - m_\tau)}{m_\tau} \end{pmatrix} \Rightarrow$$

$$\text{MSSM} : m_b \simeq m_\tau (M_X) (\text{all simple GUTs}) \Rightarrow \theta_{23}^{PMNS} \simeq 1$$

- Goh Mohapatra Ng : Type II : 3 generations, Real/Complex :
Good **GENERIC** Fits except $\delta^{CKM} > \frac{\pi}{2}$.
- Bertolini, Malinsky (2004)(Type II, $\oplus 120$) ; Babu Macesanu
(2005)(I+II) **Good Angle and Ratio GENERIC !!**
- Datta Mimura, Mohapatra(2004/5) **120**, $\langle CP \rangle$, Type II: **and**
GENERIC fits excellent. $d = 5, \Delta B \neq 0$ control by
cancellations

MSGUT DOOM(2005)

- Type I ,Type II GENERIC fits : freedom to choose r_1, r_2, r_3, r_4 assumed. M_ν scale, Relative strength of Type I / Type II assumed. **NOT JUSTIFIED IN MSGUT !**
- **IN MSGUT MAGNITUDE AND RELATIVE STRENGTH OF SEESAW MASSES FIXED !! FIT FULLY SPECIFIED : IS IT VIABLE ??**
- **Does it Work ?** : **NO !!** CSA , CSA,Garg (2005). SCISSORS : $\langle \Delta_L(3, 1, 2) \rangle \sim v_W^2 / M_\Delta \Rightarrow$ too small : Type I \ll Type II.
BUT Type I itself too small because ;
 $f_{22}(126) \sim h_2 2(10) \ll h_{33}$ used for Georgi-Jarlskog
2-generation charged fermion improvement and thus M_{ν^c} is too large !

NMSGUT : FM-Higgs Completion

- $10 \oplus \overline{126}$ FM Higgs irreps \Rightarrow Type I , Type II Seesaw failure :
 $\oplus 120$ -plet : **THIRD FM CHANNEL !** \Rightarrow **VIABLE** y_f, κ_ν ???
- **120** Yukawa : $g_{AB} = -g_{BA}$: **Novel Fitting Properties.**
- **NEW SCENARIO** : $h \oplus g \gg f \Rightarrow (m_{q,l}, \theta_q^i, \delta_c)$.
- **120** $\supset (15, 2, 2) \oplus (1, 2, 2) \Rightarrow$ **2 new doublet pairs** ($M_H 6 \times 6$,
 $M_T 7 \times 7$)
- $f \ll h, g \Rightarrow$ **Type I boosted !!** ($\hat{n} \sim \hat{f}^{-1}$) !
- $f < 10^{-4} \Rightarrow M_X \gg M_{\nu^c} \sim < 10^{12} GeV$: Characteristic
feature !! Well adapted for Leptogenesis !

Guts of NMSGUT

- Decomposition **120**-plet w.r.t $SU(4) \times SU(2)_L \times SU(2)_R$

$$\begin{aligned}
 O_{ijk}(120) &= O_{\mu\nu}^{(s)}(10, 1, 1) + \overline{O}_{(s)}^{\mu\nu}(\overline{10}, 1, 1) + O_{\nu\alpha\dot{\alpha}}{}^{\mu}(15, 2, 2) \\
 &+ O_{\mu\nu\dot{\alpha}\dot{\beta}}^{(a)}(6, 1, 3) + O_{\mu\nu}^{(a)}{}_{\alpha\beta}(6, 3, 1) + O_{\alpha\dot{\alpha}}(1, 2, 2)
 \end{aligned}$$

- **AM SSB unmodified, 26 MSSM multiplet types same.**

$$\begin{aligned}
 W_{120} &= M_O 120 \cdot 120 + k 10 \cdot 120 \cdot 210 + \rho 120 \cdot 120 \cdot 210 \\
 &+ \zeta 120 \cdot 126 \cdot 210 + \bar{\zeta} 120 \cdot \overline{126} \cdot 210 + g_{[AB]} 16_A \cdot 16_B \cdot 120
 \end{aligned}$$

- Parameter Counting : Complex Case

$$M_O, k, \rho, \zeta, \bar{\zeta}, g_{AB} : (1 + 1 + 1 + 2 + 3) \times 2 - 1 = 15 \oplus 24 \text{ (old)} = 39$$

(Minimal No Longer ?)

- **Pangloss approach** : Spontaneous CP violation only ? \Rightarrow All Superpot couplings Real (but M_H cannot be !!), CP violation phases from vevs (\Rightarrow *Complex x!!*)

$$OLD : m, M, M_H, \lambda, \eta, \gamma, \bar{\gamma}, h_{AB}, f_{AB} : 7 + 3 + 6 = 16$$

$$NEW : M_O, k, \rho, \zeta, \bar{\zeta}, g_{AB} : 5 + 3 = 8$$

$$TOTAL : 24 \text{ *I.E one less than MSGUT!*}$$

- **Honest Renormalizable-SO(10)** : No ad-hoc CP Z_2 , Keep all gauge allowed couplings. Fine tuning requires complex M_H anyway !! 15 extra phases \Rightarrow 38 couplings in all. Still competitive. Moreover is Structurally minimal and FM-Higgs complete. Effect of phases on fitting flexibility is marginal(LKG)

- 6×6 DOUBLET MASS MATRIX CSA TIWANA;
CSA,GARG(2005,6)

$$\begin{pmatrix} -M_H & \bar{\gamma}\sqrt{3}(\omega - a) & -\gamma\sqrt{3}(\omega + a) & -\bar{\gamma}\bar{\sigma} & kp & -\sqrt{3}ik\omega \\ -\bar{\gamma}\sqrt{3}(\omega + a) & 0 & -(2M + 4\eta(a + \omega)) & 0 & -\sqrt{3}\bar{\zeta}\omega & i(p + 2\omega)\bar{\zeta} \\ \gamma\sqrt{3}(\omega - a) & -(2M + 4\eta(a - \omega)) & 0 & -2\eta\bar{\sigma}\sqrt{3} & \sqrt{3}\zeta\omega & -i(p - 2\omega)\zeta \\ -\sigma\gamma & -2\eta\sigma\sqrt{3} & 0 & -2m + 6\lambda(\omega - a) & \zeta\sigma & \sqrt{3}i\zeta\sigma \\ pk & \sqrt{3}\bar{\zeta}\omega & -\sqrt{3}\omega\zeta & \bar{\zeta}\bar{\sigma} & -m_0 & \frac{\rho}{\sqrt{3}}i\omega \\ \sqrt{3}ik\omega & i(p - 2\omega)\bar{\zeta} & -i(p + 2\omega)\zeta & -\sqrt{3}i\bar{\zeta}\bar{\sigma} & -\frac{\rho}{\sqrt{3}}i\omega & -m_0 - \frac{2\rho}{3}a \end{pmatrix}$$

- DIAGONALIZE \mathcal{H} after $Det\mathcal{H} = 0 \Rightarrow, H, \bar{H} \Rightarrow M_H \text{ FIXED!!}$
LIGHT. R-L Eigenvectors $\Rightarrow \alpha_i, \bar{\alpha}_i$
- Yukawa couplings (CSA,Girdhar(2004),CSA,Garg(2006))

$$\hat{y}^u = (\check{h} + \check{f} + \check{g}) \quad ; \quad r_1 = \frac{\bar{\alpha}_1}{\alpha_1} \quad ; \quad r_2 = \frac{\bar{\alpha}_2}{\alpha_2}$$

$$\hat{y}^\nu = (\check{h} - 3\check{f} + (r_5 - 3)\check{g}) \quad ; \quad r_5 = \frac{4i\sqrt{3}\alpha_5}{\alpha_6 + i\sqrt{3}\alpha_5}$$

$$\hat{y}^d = (r_1\check{h} + r_2\check{f} + r_6\check{g}); \quad r_6 = \frac{\bar{\alpha}_6 + i\sqrt{3}\bar{\alpha}_5}{\alpha_6 + i\sqrt{3}\alpha_5}$$

$$\hat{y}^l = (r_1\check{h} - 3r_2\check{f} + (\bar{r}_5 - 3r_6)\check{g}); \quad \bar{r}_5 = \frac{4i\sqrt{3}\bar{\alpha}_5}{\alpha_6 + i\sqrt{3}\alpha_5}$$

$$\check{g} = 2ig\sqrt{\frac{2}{3}}(\alpha_6 + i\sqrt{3}\alpha_5) \quad ; \quad \check{h} = 2\sqrt{2}h\alpha_1 \quad ; \quad \check{f} = -4\sqrt{\frac{2}{3}}if\alpha_2$$

- **New Baryon Decay Channels** : $P[3, 3, \pm\frac{2}{3}]$, $K([3, 1, \pm\frac{8}{3}] \subset 120$
- **Viable m_f , CKM , Δm_ν^2 , PMNS ?? : No! : GJ FAILURE**
IMPLIES $y_{d,s}$ come out too small. Numerical analysis confirms
otherwise excellent fits unable to raise $y_{d,s}$. BUT just for
 $T_3 = -1/2$ quarks there are significant

Threshold Corrections at M_S

- $\tan \beta \sim m_t/m_b \sim 40 - 60$ generic in SO(10) GUTs. Single **10** $t - b - \tau$ unification allows $\tan \beta \sim 50 - 60 \sim m_t/m_b$ only.
- $m_b \simeq m_\tau$ expected in simple single FM Higgs GUTs. Also in SO(10) with negligible $\overline{126}$ yukawas.
- **LARGE SUSY THRESHOLD CORRECTIONS** to $m_{T_3=-.5}^{quark}$ **AT LARGE** $\tan \beta$ (α_s (gluino) and ($A_t y_t^2$ loops for 3d gen)) !!! Carena, Olechowski, Pokorski and Wagner(1994); Hall Ratzzi and Sarid(1994)
- **FITTING FRENZY IGNORED effect OF THRESHOLD CORRECTIONS IN B-TAU-TOP- ν_τ UNIFICATION !!**

Large THRESHOLD CORRECTIONS to y_f at M_S

- Threshold corrections in unbroken limit Freitas et al
($\epsilon_i = \epsilon_i^G + \epsilon_i^B + \epsilon_i^W + \epsilon^y \delta_{ib}$):

$$\frac{y_i^{GUT}(M_S) \cos \beta}{y_i^{SM}(M_S)} = \frac{1}{1 + \epsilon_i(m_{\tilde{f}}, M_i \mu, A_t) \tan \beta}$$

Dominant corrections for quarks:

$$\epsilon_i^G = -\frac{2\alpha_S}{3\pi} \frac{\mu}{M_3} H_2(u_{\tilde{Q}_i}, u_{\tilde{d}_i}) \quad \epsilon^y = -\frac{y_t^2}{16\pi^2} \frac{A_t}{\mu} H_2(v_{\tilde{Q}_3}, v_{\tilde{u}_3})$$

- Loop function $H_2 < 0 \Rightarrow$ lowering $y_{d,s}^{SGUT} \Rightarrow \mu, -A_t \gg M_{\tilde{f}}$
with cancellation for y_b FITTING GIVES THIRD GEN
SFERMIONS HEAVIER THAN FIRST TWO
GENERATIONS ! DISTINCT CLASS OF SPECTRA ! LHC
- Corrections available only in diagonal approximation.
Numerical fit requires non degenerate sfermion families at M_X
as well as splitting in A_0 values for families !

LARGE THRESHOLD CORRECTIONS to y_f at M_X !

- Negligible ?? BUT $120 \times .1^2 \sim 1 \Rightarrow$ large wavefunction renormalization !

Threshold correction to a Yukawa coupling matrix then has the form (Wright 1994)

$$Y_f = Y_f + \Delta_{\bar{f}}^T \cdot Y_f + \Delta_f \cdot Y_f + \Delta_{H^\pm} \cdot Y_f \quad (1)$$

$$W = \frac{1}{6} \sum_{ijk} Y_{ijk} \Phi^i \Phi^j \Phi^k \Rightarrow,$$

$$\Delta_i^j = \frac{1}{32\pi^2} \left(-2g_{10}^2 \sum_{k,A} F_1(m_A^2, m_k^2) T_{ik}^A T_{kj}^A + \frac{1}{2} \sum_{kl} Y_{ikl} Y_{jkl}^* F_1(m_k^2, m_l^2) \right) \quad (2)$$

F_1 : Passarino-Veltman function

$$F_{12}(M_A, M_B, \mu) = \frac{1}{(M_A^2 - M_B^2)} \left(M_A^2 \ln \frac{M_A^2}{\mu^2} - \ln \frac{M_B^2}{\mu^2} \right) - 1 \quad (3)$$

- Large effect on Yukawa couplings! Make possible fits with $A_A^0 = A_0$ and $m_1^0 = m_2^0 \neq m_3^0$ is only non-universal soft

breaking.

d = 5 NUCLEON DECAY

- FAMILIAR $\bar{t}[\bar{3}, 1, -\frac{2}{3}] \oplus t[3, 1, \frac{2}{3}] \oplus$ NOVEL
 $P[3, 3, \pm\frac{2}{3}], K[3, 1, \pm\frac{8}{3}]$ MULTIPLY TYPES CONTRIBUTE
 TO BARYON VIOLATION IN SO(10)
 BABU,PATI,WILCZEK(2000);CSA,GIRDHAR,GARG(2004,2006)

$$W_{eff}^{\Delta B \neq 0} = -\hat{L}_{ABCD}(\frac{1}{2}\epsilon\hat{Q}_A\hat{Q}_B\hat{Q}_C\hat{L}_D) - \hat{R}_{ABCD}(\epsilon\bar{e}_A\bar{u}_B\bar{u}_C\bar{d}_D)$$

where the coefficients are

$$\begin{aligned} \hat{L}_{ABCD} &= \mathcal{S}_1^1 \tilde{h}_{AB} \tilde{h}_{CD} + \mathcal{S}_1^2 \tilde{h}_{AB} \tilde{f}_{CD} + \mathcal{S}_2^1 \tilde{f}_{AB} \tilde{h}_{CD} + \mathcal{S}_2^2 \tilde{f}_{AB} \tilde{f}_{CD} \\ &- \mathcal{S}_1^6 \tilde{h}_{AB} \tilde{g}_{CD} - \mathcal{S}_2^6 \tilde{f}_{AB} \tilde{g}_{CD} + \sqrt{2}(\mathcal{P}^{-1})_2^1 \tilde{g}_{AC} \tilde{f}_{BD} \\ &- (\mathcal{P}^{-1})_2^2 \tilde{g}_{AC} \tilde{g}_{BD} \end{aligned}$$

$\mathcal{S} = \mathcal{T}^{-1}$; $W = \bar{t}^i \mathcal{T}_i^j t_j + \dots$ similarly R_{ABCD} (also involves K^{-1})

- $L_{ABCD}, R_{ABCD}(M_X)$ GOOD ESTIMATORS FOR

$L_{ABCD}, R_{ABCD}(M_S)$ WE USE WITH SFERMION FITS AND
MIXING ASSUMPTIONS TO ESTIMATE DECAY RATE
WITHIN SEARCH ALGORITHM

NUMERICAL SEARCH FOR COMPLETE GUT PARAMETERS

PRECISION SM m_f AT $Q = M_Z$

\Rightarrow MSSM +threshold corrections $\Rightarrow y_f$ at fixed $v, \tan \beta$

\Downarrow

2 loop MSSM \Downarrow FLOW

$M_X = 10^{16.3}$ GeV, DOWNHILL SIMPLEX, ANTUSCH ERRORS

Unification Constraints, Fit all but $y_{b,d,s}$ accurately

2 loop MSSM soft + hard $M_X \Downarrow M_Z$ RG FLOW

with achieved yukawas \Downarrow and random soft SUGRA

LARGE $\tan \beta$ Corrections \Rightarrow FITS Across M_Z to SM Precision

Data \Rightarrow Optimal SUGRA SOFT SUSY

USE SPHENO FOR FULL \Downarrow MSSM ONE LOOP EFFECTS

2 loop MSSM RG FLOW TO M_X

\Downarrow

ITERATE !

Fitting Features

- “Solutions” with $\chi^2 < .1$ for 18 fermion quadratic data fitted.
- $h_{AB} \sim 10^{-7} - 10^{-2}$; $g_{AB} \sim 10^{-2} - 10^{-4}$; $f_{AB} \sim 10^{-7} - 10^{-4}$
- $M_X \sim 10^{17.8} - 10^{19} GeV, \Delta\alpha_3(M_Z) \sim -.01, \alpha_G \sim .1, Max(L_{ABCD}, R_{ABCD}) < 10^{-21} GeV^2$
- Third sgeneration much heavier, μ , A_0 large and of opposite signs (M_i positive) $M_{\frac{1}{2}}(M_X) = 200.000000000, A^0(M_X) = -7061.56862128, (m_{\tilde{f}}^2)_{1/2} = 1.169457E6, (m_{\tilde{f}}^2)_3 = 5.40168346545E7, m_{H_1^2} = 9.52660735743E6, m_{H_2^2} = -5.45339726387E6$
- $|(y_b - y_\tau)/(y_s - y_\mu)| = 1.0 \pm .05$ Expected on Real Core view !!
- freedom of gaugino phases and mu signs unexploited.
- $d = 5$ Baryon decay rates calculated using complete fit data (Lucas Raby, Goto Nihei) $< 10^{32} yr^{-1}$.

Conclusions

- M_S, M_X threshold corrections to fermion yukawas calculated (M_X due to 120 novel).
- SM data fitted in NMSGUT BY DOWNHILL SIMPLEX SEARCHES in 38 dimensional Superpot parameter space plus 5 soft parameters at M_X
- SO(10) NMSGUT MAY WELL BE COMPATIBLE WITH ALL FM DATA and Baryon decay Constraints
- M_S THRESHOLD CORRECTIONS CONSTRAIN SUGRA SOFT PARAMETERS, THIRD GEN HEAVY, large trilinears A_0 !
- SMALL $\overline{126}$ COUPLINGS VITAL TO SUCCESSFUL NEUTRINO MASS AND ANGLE FIT : DOOR OPEN TO PERTURBATIVE UNDERSTANDING OF HIERARCHY
- UNIFICATION SCALE GENERICALLY RAISED TO NEAR PLANCK SCALE : ASTRONG PROBLEM POSTPONED:

so(10) GRAVITY CONNECTION ?

- D=5 NUCLEON DECAY CONSTRAINTS ON SFERMION SPECTRA marginally satisfied : AWAIT SUPERPARTNER DISCOVERY
- NMSGUT VULNERABLE TO FALSIFICATION AT LHC