



New TeV-scale Seesaw with Vectorlike Mediators

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**2. Conventional Seesaw Models:
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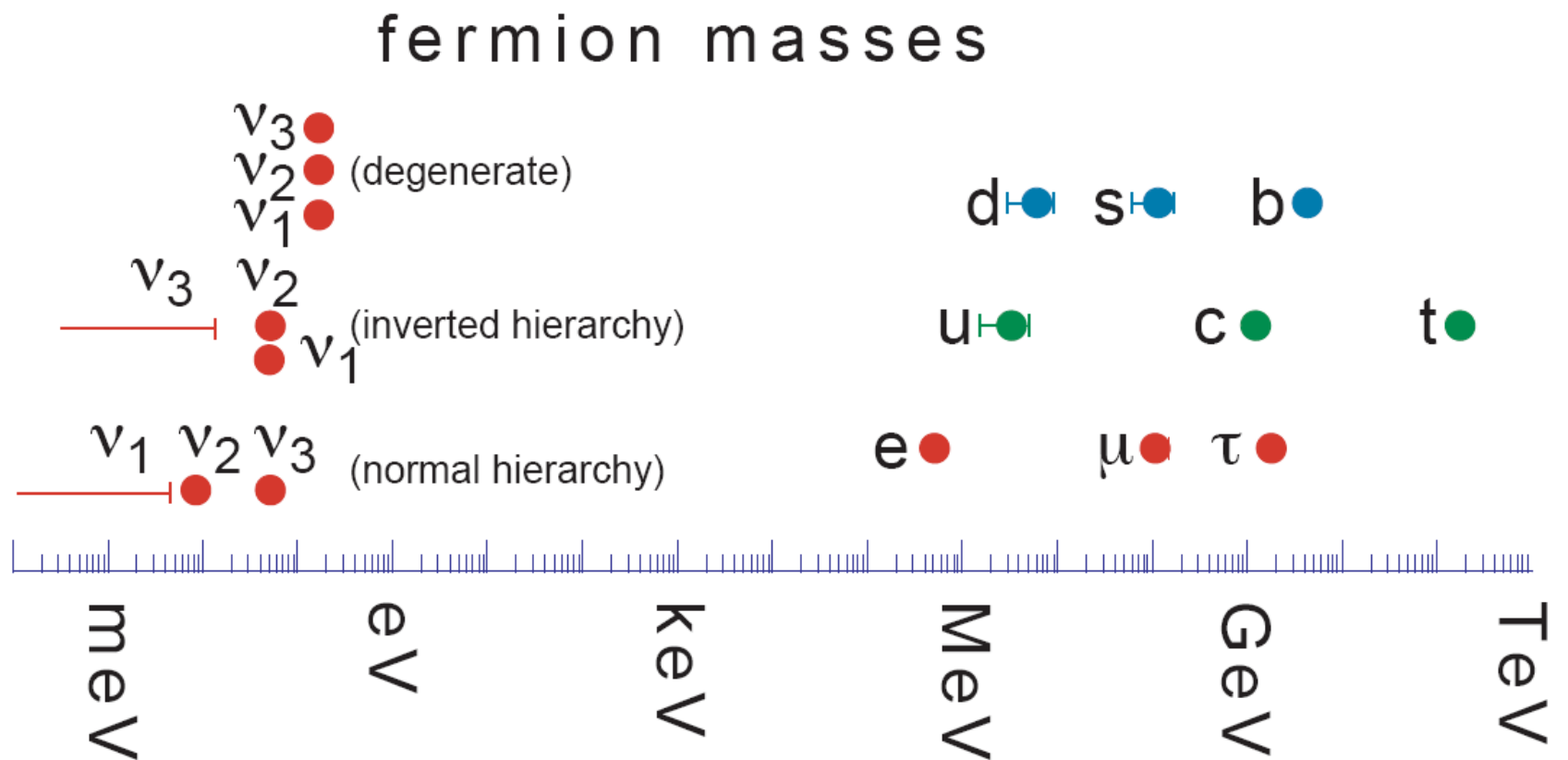
**Majorana Neutrinos with
TeV-scale Dirac Vectorlike mediators**



1. Prominent Landmarks in Addressing BSM Physics:

- **Heavyness of top**
- **Lightness of neutrinos**
- **Lightness of the SM Higgs**

The first two Landmarks: **Lightness of ν 's & Heavyness of top** (Fig. Murayama'08)





The 3rd Landmark: Lightness of the SM Higgs doublets - known as the Hierarchy Problem

- Introducing the top-partner T to cancel the largest contribution to Higgs mass quadratic divergence \rightarrow suggests
- Introducing such Seesaw Mediators which explain small neutrino masses without introducing extra Hierarchy Problem



Revealing new d.o.f. via QM loops:

- **c quark from K-Kbar box diagram**
- **t quark from B-Bbar box diagram**
- **Followed by proposals of extra T state:**

a recent revival of the latter box diagrams by Vysotsky [1], in the context of a simple extension of the standard model

[1] M. I. Vysotsky, Phys. Lett. B **644**, 352 (2007).

generalized to FC rare decays for relatively heavy T: I.P. & B.Radovčić, PRD78, 015014 ('08)

The SM Lagrangian extended by top-partner: weak (t', T') st's

$$\mathcal{L}_{BSM} = -M\bar{T}'_L T'_R + \left[\mu_R \bar{T}'_L t'_R + \frac{\mu_L}{v/\sqrt{2}} (\bar{t}', \bar{b}')_L \Phi^c T'_R \right] + h.c.$$

- The Dirac mass term M
- The (t', T') mixing by two terms

μ_R and the μ_L term

The “Dirac seesaw” - by diagonalizing the mass matrix

$$M_{t-T} = \overline{(t'_L t'_R T'_L T'_R)} \begin{pmatrix} 0 & m_t & 0 & \mu_L \\ m_t & 0 & \mu_R & 0 \\ 0 & \mu_R & 0 & -M \\ \mu_L & 0 & -M & 0 \end{pmatrix} \begin{pmatrix} t'_L \\ t'_R \\ T'_L \\ T'_R \end{pmatrix}$$

- explains the heaviness of top quark:

by putting $m_t = 0$, top quark gets all its mass $\sim \mu_L \mu_R / M$ from the mixing with heavy T

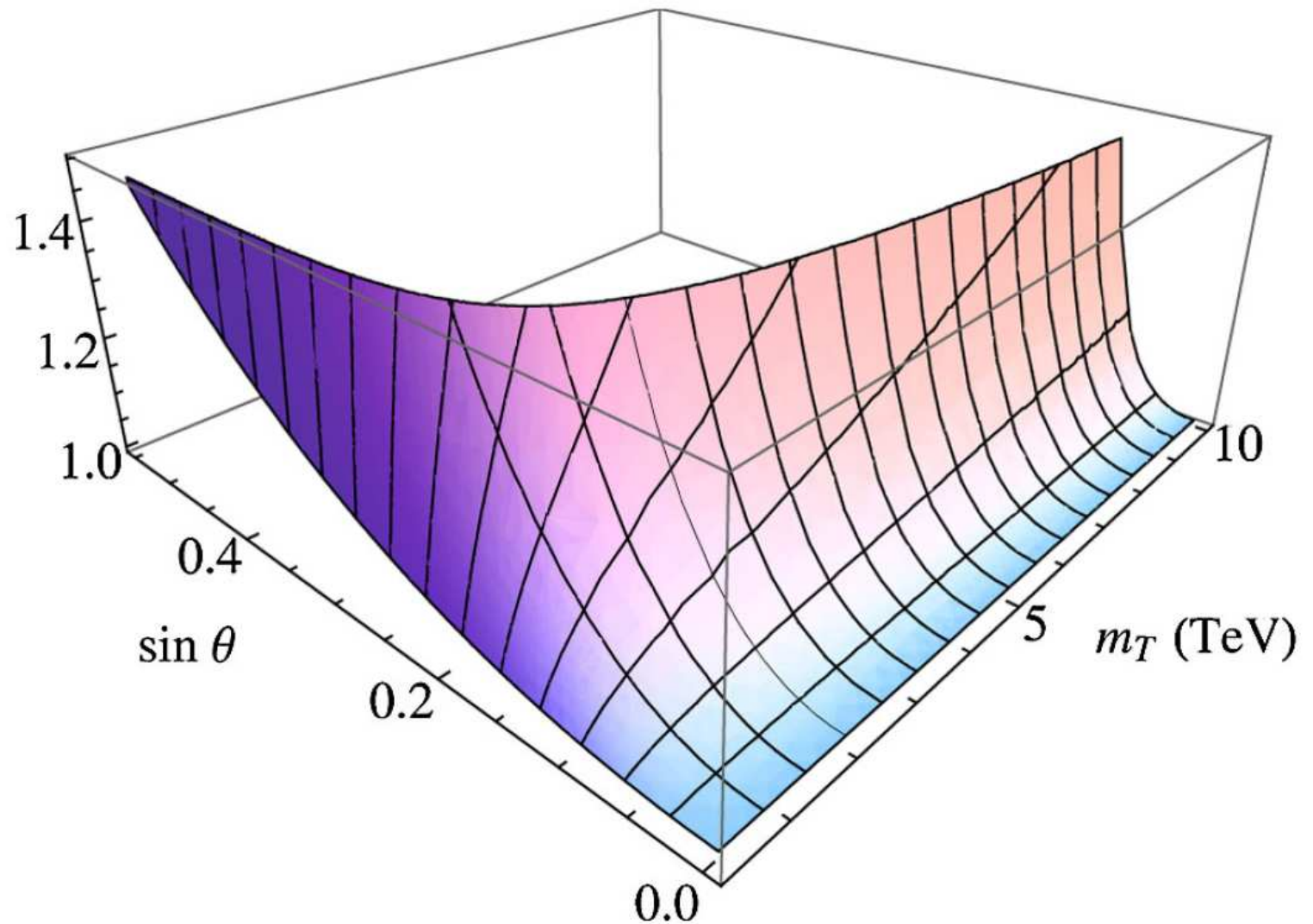


Assumption that T' mixes only with t'

- Generalizes the SM3 CKM to a 4x3 non-unitary matrix
- Modifies the NC couplings
- Leads to the very predictive 2-parameter model:

$T' - t'$ mixing angle θ , and the mass $m_{T'}$

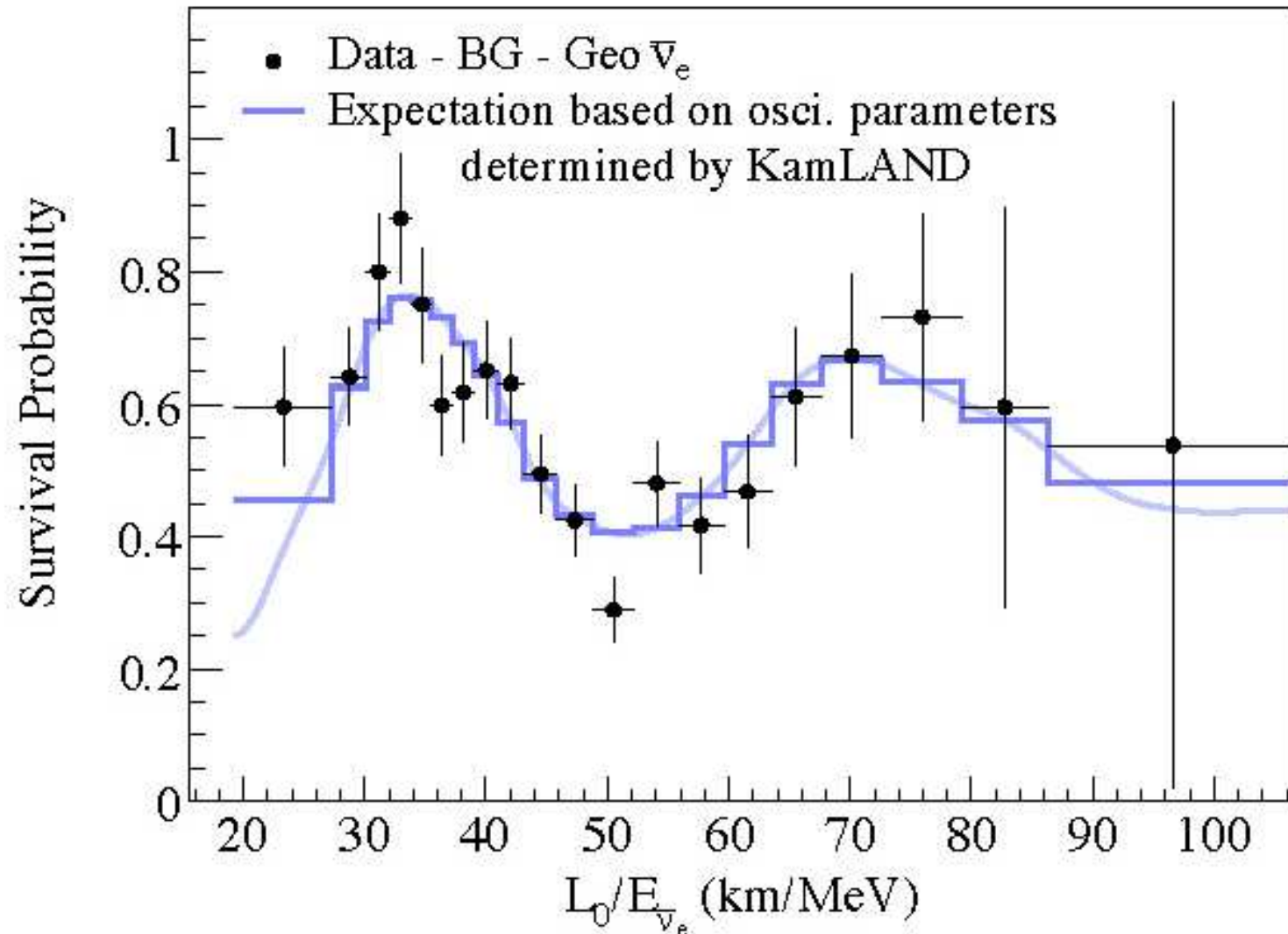
Possible ~50% enhancement of $B \rightarrow \mu\mu$ w.r.t. the SM prediction @ LHC




2. New States entering into gauge invariant Yukawa terms



Neutrino Masses beyond doubt - KamLAND evidence of ν -masses

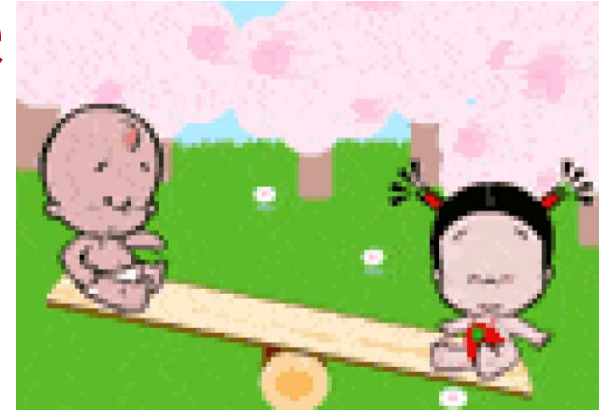




New d.o.f. and Yukawa terms explaining Neutrino Masses:

- **Light sterile neutrinos –
lacking motivation?**
- **Heavy Majorana neutrinos –
conventional fermionic seesaws**
- **Vectorlike Dirac fermions –
beyond Type I & III seesaw**

The seesaw picture
-ascribes the lightness of
 ν 's to the existence of
some heavy-scale d.o.f.



Type-I: SM + 3 right-handed Majorana ν 's (Minkowski 77; Yanagida 79; Glashow 79; Gell-Mann, Ramond, Slanski 79; Mohapatra, Senjanovic 79)

Type-II: SM + 1 Higgs triplet (Magg, Wetterich 80; Schechter, Valle 80; Lazarides et al 80; Mohapatra, Senjanovic 80; Gelmini, Roncadelli 80)

Type-III: SM + 3 triplet fermions (Foot, Lew, He, Joshi 89)

Other variations or combinations (e.g., **type-I + type-II** in SO(10) GUT)

Conventional Seesaw Mediators

Type I

— three heavy right-handed neutrinos

$$N_R \sim (1, 1, 0)$$

Type II

— one heavy Higgs triplet $\Delta \equiv \begin{pmatrix} \Delta^- & -\sqrt{2} \Delta^0 \\ \sqrt{2} \Delta^{--} & -\Delta^- \end{pmatrix}$

$$\Delta \sim (1, 3, -2)$$

Type III

— three heavy triplet fermions $\Sigma = \begin{pmatrix} \Sigma^0/\sqrt{2} & \Sigma^+ \\ \Sigma^- & -\Sigma^0/\sqrt{2} \end{pmatrix}$

$$\Sigma \sim (1, 3, 0)$$

Higher States are not isolated

Fermion 5-plet in conjunction with scalar 4-plet

$$\Sigma \sim (1, 5, 0)$$

$$\Phi \sim (1, 4, -1)$$

Conventional “isolated” tree-level seesaw mediators

Type I — three heavy right-handed neutrinos

$$- \mathcal{L}_{\text{lepton}} = \bar{l}_L Y_l H E_R + \bar{l}_L Y_\nu \tilde{H} N_R + \frac{1}{2} \overline{N_R^c} M_R N_R + \text{h.c.}$$

Type II — one heavy Higgs triplet $\Delta \equiv \begin{pmatrix} \Delta^- & -\sqrt{2} \Delta^0 \\ \sqrt{2} \Delta^{--} & -\Delta^- \end{pmatrix}$

$$- \mathcal{L}_{\text{lepton}} = \bar{l}_L Y_l H E_R + \frac{1}{2} \bar{l}_L Y_\Delta \Delta i\sigma_2 l_L^c - \lambda_\Delta M_\Delta H^T i\sigma_2 \Delta H + \text{h.c.}$$

Type III — three heavy triplet fermions $\Sigma = \begin{pmatrix} \Sigma^0/\sqrt{2} & \Sigma^+ \\ \Sigma^- & -\Sigma^0/\sqrt{2} \end{pmatrix}$

$$- \mathcal{L}_{\text{lepton}} = \bar{l}_L Y_l H E_R + \bar{l}_L \sqrt{2} Y_\Sigma \Sigma^c \tilde{H} + \frac{1}{2} \text{Tr} (\overline{\Sigma} M_\Sigma \Sigma^c) + \text{h.c.}$$

Integrating out heavy d.o.f. gives

$$\frac{\mathcal{L}_{d=5}}{\Lambda} = \begin{cases} \frac{1}{2} (Y_\nu M_R^{-1} Y_\nu^T)_{\alpha\beta} \overline{l}_{\alpha L} \tilde{H} \tilde{H}^T l_{\beta L}^c + \text{h.c.} & \text{(Type I) ,} \\ -\frac{\lambda_\Delta}{M_\Delta} (Y_\Delta)_{\alpha\beta} \overline{l}_{\alpha L} \tilde{H} \tilde{H}^T l_{\beta L}^c + \text{h.c.} & \text{(Type II) ,} \\ \frac{1}{2} (Y_\Sigma M_\Sigma^{-1} Y_\Sigma^T)_{\alpha\beta} \overline{l}_{\alpha L} \tilde{H} \tilde{H}^T l_{\beta L}^c + \text{h.c.} & \text{(Type III)} \end{cases}$$

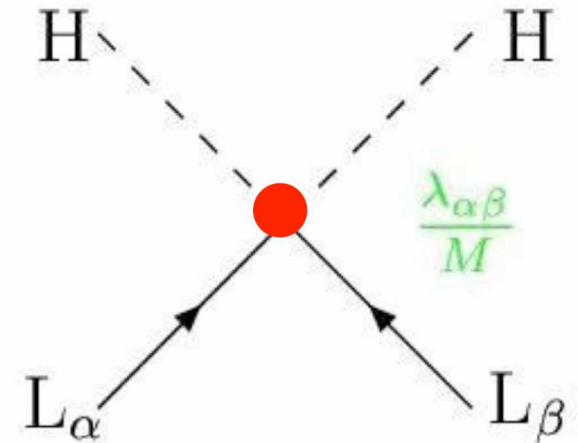
**SSB results in
Majorana mass term
for active neutrinos**

$$-\mathcal{L}_{\text{mass}} = \frac{1}{2} \overline{\nu}_L M_\nu \nu_L^c + \text{h.c.} \quad M_\nu = \begin{cases} -\frac{1}{2} Y_\nu \frac{v^2}{M_R} Y_\nu^T & \text{(Type I) ,} \\ \lambda_\Delta Y_\Delta \frac{v^2}{M_\Delta} & \text{(Type II) ,} \\ -\frac{1}{2} Y_\Sigma \frac{v^2}{M_\Sigma} Y_\Sigma^T & \text{(Type III)} \end{cases}$$

Dim 5 Weinberg's op. $\sim LLHH$

Dimension 5 operator:

$$\lambda/M \underbrace{(L L H H)}_{O^{d=5}} \rightarrow \lambda v^2/M (v v)$$



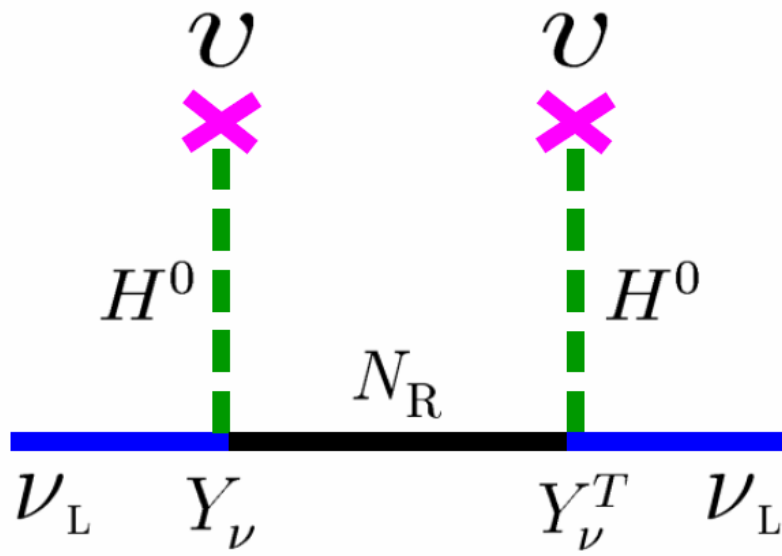
It's unique \rightarrow very special role of ν masses:
lowest-order effect of higher energy physics

This mass term **violates lepton number (B-L)**
 \rightarrow **Majorana** neutrinos

$O^{d=5}$ *is common to all models of Majorana ν s*

GUT-scale fermion mediators in Type I & III seesaw – and possible low scale mission of adjoint fermionic 24 of SU(5)

Bajc & Senjanović, JHEP 0708, 014 (2007)

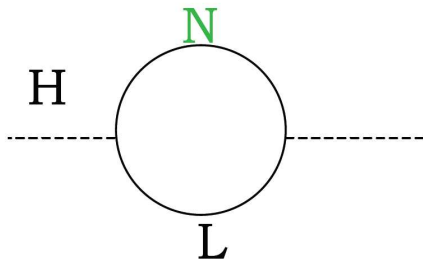


$$M_\nu \approx -v^2 Y_\nu \frac{1}{M_R} Y_\nu^T$$

$$M_\nu \approx M_D M_R^{-1} M_D^T$$

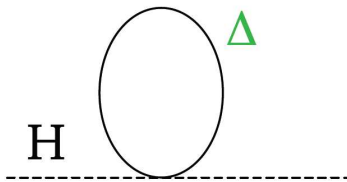
0.01 eV
100 GeV
10¹⁵ GeV

TeV-seesaw scale is suggested by EW hierarchy problem



$$\delta m_H^2 = -\frac{Y_N^\dagger Y_N}{16\pi^2} \left[2\Lambda^2 + 2M_N^2 \log \frac{M_N^2}{\Lambda^2} \right]$$

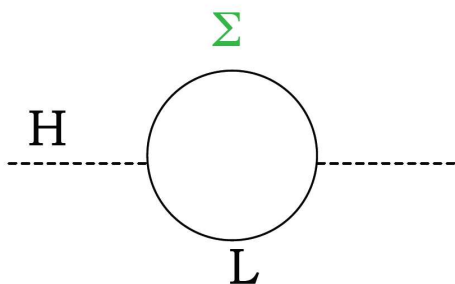
(Vissani)



$$\delta m_H^2 = -3 \frac{\lambda_3}{16\pi^2} \left[\Lambda^2 + M_\Delta^2 \left(\log \frac{M_\Delta^2}{\Lambda^2} - 1 \right) \right]$$

$$- \frac{\mu_\Delta^2}{2\pi^2} \log \left(\left| \frac{M_\Delta^2 - \Lambda^2}{M_\Delta^2} \right| \right)$$

(Abada, Biggio, Bonnet, Hambye, M.B.G.)



$$\delta m_H^2 = -3 \frac{Y_\Sigma^\dagger Y_\Sigma}{16\pi^2} \left[2\Lambda^2 + 2M_\Sigma^2 \log \frac{M_\Sigma^2}{\Lambda^2} \right]$$

Lowering seesaw scale by going to dim>5 operators:

$$\mathcal{O}^5 = \mathcal{O}_W = LLHH$$

$$\mathcal{O}^7 = (LLHH)(H^\dagger H)$$

$$\mathcal{O}^9 = (LLHH)(H^\dagger H)(H^\dagger H)$$

⋮

$$m_\nu \sim v \left(\frac{v}{\Lambda_{\text{NP}}} \right)^{d-4}$$

F. Bonnet, D. Hernandez, T. Ota and W. Winter, JHEP **0910**:076,2009 [0907.3143 [hep-ph]];

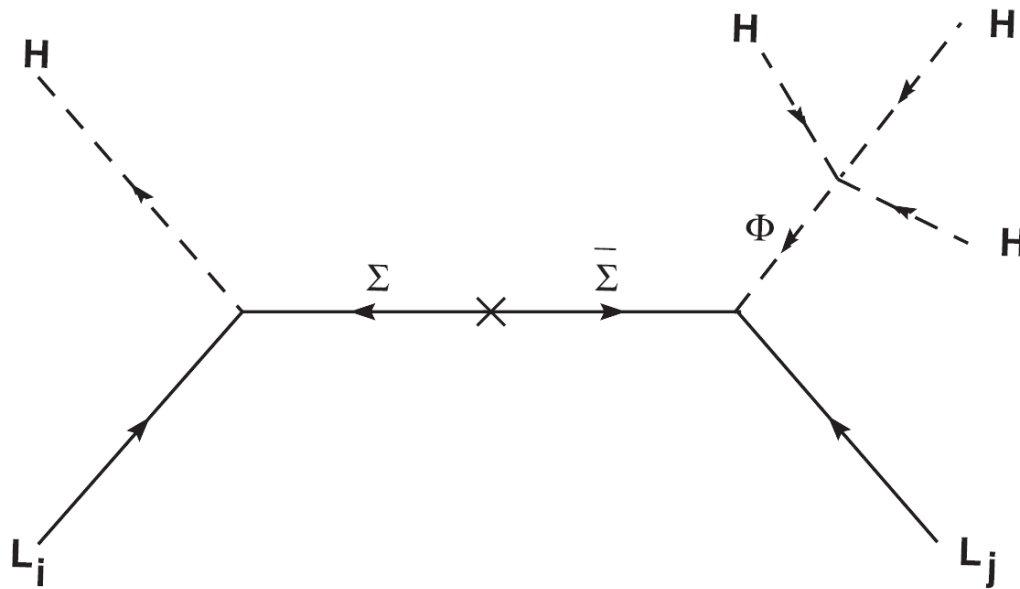
- NP scale 1-10 TeV with d=9 is enough for sub-eV neutrino mass
- Operators are studied for singlet, doublet and triplet mediators



3. Tree-level Seesaw diagrams giving $\dim > 5$ Operators

- Lowering seesaw scale by multiple seesaw
E. Ma, PRL86 ('01) 2502
- further elaborated by
W.Grimus, L.Lavoura, B.Radovčić, PLB 674 ('09) 117;
- Dim 7 Operator Babu et al'09, PRD 80,071702(R)
- Dim 9 Operator I.P. and B.Radovčić, PLB 687 ('10) 338

Dim-7 op. \sim LLHH(H † H) Babu et al.



$$m_\nu \sim v^4 / M^3$$

$$\mathcal{L}_{\nu\text{-mass}} = Y_i L_i H^* \Sigma + \bar{Y}_i L_i \Phi \bar{\Sigma} + M_\Sigma \Sigma \bar{\Sigma} + \text{H.c.}$$

$$\Sigma = (\Sigma^{++}, \Sigma^+, \Sigma^0) \text{ and } \bar{\Sigma} = (\bar{\Sigma}^0, \Sigma^-, \Sigma^{--})$$

- **Vectorlike fermions** transforming as $(1, 3, 2) + (1, 3, -2)$
- **Scalar 4-plet** $(\Phi^{+++}, \Phi^{++}, \Phi^+, \Phi^0)$ (with $Y = 3$)

Novel Tree-level Seesaw Model

based on vectorlike Dirac fermion 5-plet Σ
($I=2$, $Y=2$) mediators

$$\Sigma_L = (\Sigma_L^{+++}, \Sigma_L^{++}, \Sigma_L^+, \Sigma_L^0, \Sigma_L^-)$$

$$\Sigma_R = (\Sigma_R^{+++}, \Sigma_R^{++}, \Sigma_R^+, \Sigma_R^0, \Sigma_R^-)$$

both transforming as $(1, 5, 2)$

- In conjunction with isospin 3/2 scalar fields $\bar{\Phi}_1$ and $\bar{\Phi}_2$:

$$\bar{\Phi}_1 = (\bar{\Phi}_1^0, \bar{\Phi}_1^-, \bar{\Phi}_1^{--}, \bar{\Phi}_1^{---}) \quad \bar{\Phi}_2 = (\bar{\Phi}_2^+, \bar{\Phi}_2^0, \bar{\Phi}_2^-, \bar{\Phi}_2^{--})$$

transforming as $(1, 4, -3)$ and $(1, 4, -1)$, respectively.



SMG 3x2x1 symmetric terms

Dirac mass term of our seesaw mediator:

$$\mathcal{L}_M = - M_\Sigma \bar{\Sigma}_L \Sigma_R + \text{H.c.}$$

Yukawa term with LNC & LNV parts

$$\mathcal{L}_Y = Y_1 \bar{l}_L \Sigma_R \Phi_1 + Y_2 \bar{\Sigma}_L (l_L)^c \Phi_2^* + \text{H.c.}$$



Dirac seesaw by diagonalizing the mass matrix

$$\begin{pmatrix} \bar{\nu}_L & \overline{\Sigma_L^0} & \overline{(\Sigma_R^0)^c} \end{pmatrix} \begin{pmatrix} 0 & m_2 & m_1 \\ m_2 & 0 & M_\Sigma \\ m_1 & M_\Sigma & 0 \end{pmatrix} \begin{pmatrix} (\nu_L)^c \\ (\Sigma_L^0)^c \\ \Sigma_R^0 \end{pmatrix}$$

- representing the mixing between neutral components of the SM lepton doublet and the Σ 5-plets

Mass eigenvalues:

- Two nearly degenerate Heavy states

$$m_{\nu_H} \sim M_\Sigma$$

- Light Majorana neutrinos

$$m_\nu \sim \frac{m_1 m_2}{M_\Sigma} \sim \frac{Y_1 Y_2 v_{\Phi_1} v_{\Phi_2}}{M_\Sigma}$$

From the EW precision: $\rho = 1.0004_{-0.0004}^{+0.0008}$

$$\rho \simeq 1 - 6v_{\Phi_1}^2/v^2 + 6v_{\Phi_2}^2/v^2$$

an upper bound on v_{Φ_1} and v_{Φ_2} of a few GeV.

EWSB in usual way from Higgs doublet

$$\mu_H^2 < 0$$

$$V(H, \Phi_1, \Phi_2)$$

$$\begin{aligned} &\sim \mu_H^2 H^\dagger H + \mu_{\Phi_1}^2 \Phi_1^\dagger \Phi_1 + \mu_{\Phi_2}^2 \Phi_2^\dagger \Phi_2 + \lambda_H (H^\dagger H)^2 \\ &+ \{ \lambda_1 \Phi_1^* H^* H^* H^* + \text{H.c.} \} + \{ \lambda_2 \Phi_2^* H H^* H^* + \text{H.c.} \} \\ &+ \{ \lambda_3 \Phi_1^* \Phi_2 H^* H^* + \text{H.c.} \} . \end{aligned}$$

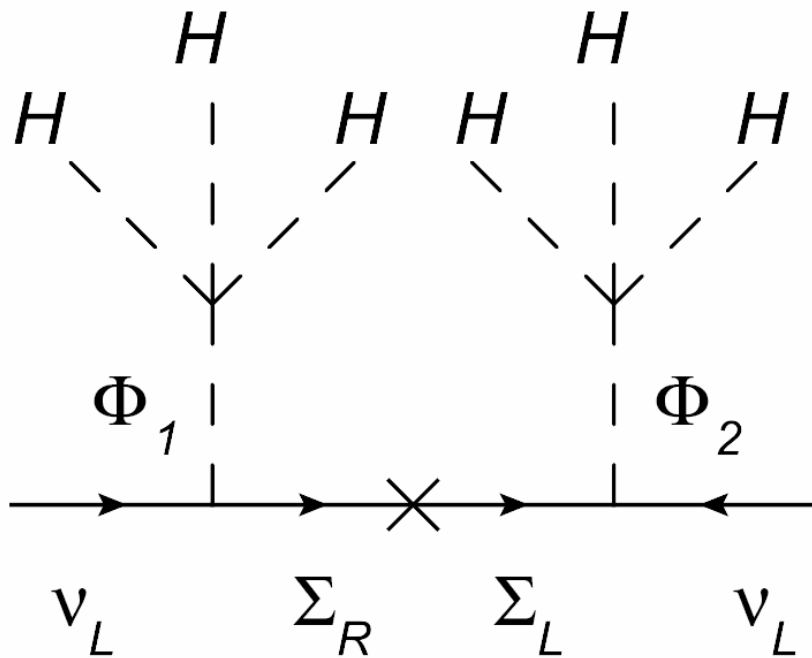
- **Induced vev for Φ_1 and Φ_2 , scalars with**

$$\mu_{\Phi_1}^2, \mu_{\Phi_2}^2 > 0$$

$$v_{\Phi_1} \simeq -\lambda_1 \frac{v^3}{\mu_{\Phi_1}^2}, \quad v_{\Phi_2} \simeq -\lambda_2 \frac{v^3}{\mu_{\Phi_2}^2}$$

Dim-9 \sim LLHH(H † H)(H † H)

tree-level op. by integrating out heavy d.o.f.



$$m_\nu \sim \frac{Y_1 Y_2 \lambda_1 \lambda_2 v^6}{M_\Sigma \mu_{\Phi_1}^2 \mu_{\Phi_2}^2}$$

$$\sim v^6 / M^5$$

- **Light Majorana neutrino naturally in sub-eV range with TeV-scale heavy d.o.f.**



Operators of dim 7 and 5 are generated at loop level from dim 9 op.
- smaller than dim 9 tree level if

$$\Lambda_{NP} < 4\pi v \simeq 2 \text{ TeV}$$

- **The operator of dim 5 generated at loop level from λ_3 term is smaller than dim 9 tree level if**

$$\Lambda_{NP} < \sqrt{4\pi} v \simeq 620 \text{ GeV}$$

The scale splitting Dim 5 loop & dim 9 tree-level contributions

For simplicity, $\mu_\Phi = M_\Sigma = \Lambda_{NP}$

the values $v = 174$ GeV and $m_\nu \sim 0.1$ eV

& moderate $Y \sim Y' \sim \lambda_2 \sim 10^{-2}$ result in

$\Lambda_{NP} \simeq 580$ GeV and $v_{\Phi_1} \simeq 80$ MeV and $v_{\Phi_2} \simeq 60$ MeV.

- There is a part of the parameter space where tree-level dim 9 operator dominates over loop generated dim 5 and dim 7 contributions!



Drell-Yan fusion production

- **Via CC associated production of pairs**
- **Via NC direct pair production - NEW**

$$(\Sigma^{+++}, \overline{\Sigma^{+++}}), (\Sigma^{++}, \overline{\Sigma^{++}})$$

$$(\Sigma^{+}, \overline{\Sigma^{0}}), (\Sigma^{0}, \overline{\Sigma^{-}})$$

$$\underline{(\Sigma^{0}, \overline{\Sigma^{0}})}$$



Small mass splittings within a multiplet ...

$$M_Q - M_0 \simeq Q(Q + Y / \cos \theta_W) \Delta M$$

$$\Delta M = \alpha_2 M_W \sin^2 \frac{\theta_W}{2} = (166 \pm 1) \text{MeV}.$$

- .. suppresses the cascade Σ decays

Signatures from LNC & LNV decays

$$\Sigma^{+++} \rightarrow W^+W^+l^+ \quad \Sigma^{++} \rightarrow W^+l^+$$

$$\Sigma^+ \rightarrow W^+\nu, Zl^+, H^0l^+$$

$$\Sigma^- \rightarrow W^-\nu, Zl^-, H^0l^-$$

$$\Sigma^0 \rightarrow W^\pm l^\mp, Z\nu, H^0\nu$$

- **Two types of decays with same sign dileptons and the jets as a signature**

$$q\bar{q}' \rightarrow W^* \rightarrow \Sigma^+\overline{\Sigma^0} \rightarrow l^+Zl^+W^- \rightarrow l^+l^+jj,$$

$$q\bar{q} \rightarrow Z^* \rightarrow \Sigma^0\overline{\Sigma^0} \rightarrow l^\pm W^\mp l^\pm W^\mp \rightarrow l^\pm l^\pm jj$$



Testability of New Vectorlike Matter in the reach of LHC

- i) By testing the seesaw type - try to infer on new d.o.f. realized in Nature; States too heavy to be produced may be revealed through virtual loop effects**
- ii) New vectorlike leptonic 5-plet as a link between collider phenomenology and the origin of neutrino masses**

Conclusions:

FALSE

- We are introducing a falsifiable dim 9 tree-level seesaw model: corresponds to testable parameter space (accessible to the LHC)
- Drell-Yan produced 5-plet fermion Σ states decay with characteristic same sign dileptons and jet signature
- Singly charged & neutral Σ states have small mixing ($\sim 10^{-6}$) and fast decay ($\sim 10^{-13}$ s)
- Non-discovery of sub-TeV Σ 's at the LHC leaves us with radiative (loop-induced) neutrino mass