



# Two-Particle Correlations in Hadronic $e^+e^-$ Collisions at Belle and Their Implication

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on behalf of the Belle Collaboration

partial results in [arXiv:2201.01694](https://arxiv.org/abs/2201.01694)

accepted by PRL

new paper in preparation (to be submitted to JHEP)

Quark Matter 2022, Apr. 6



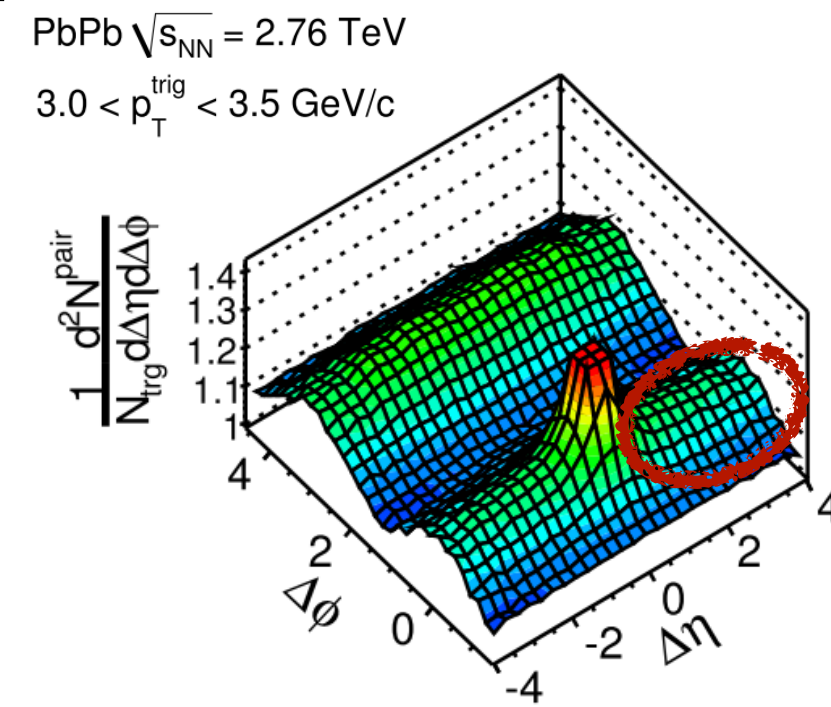
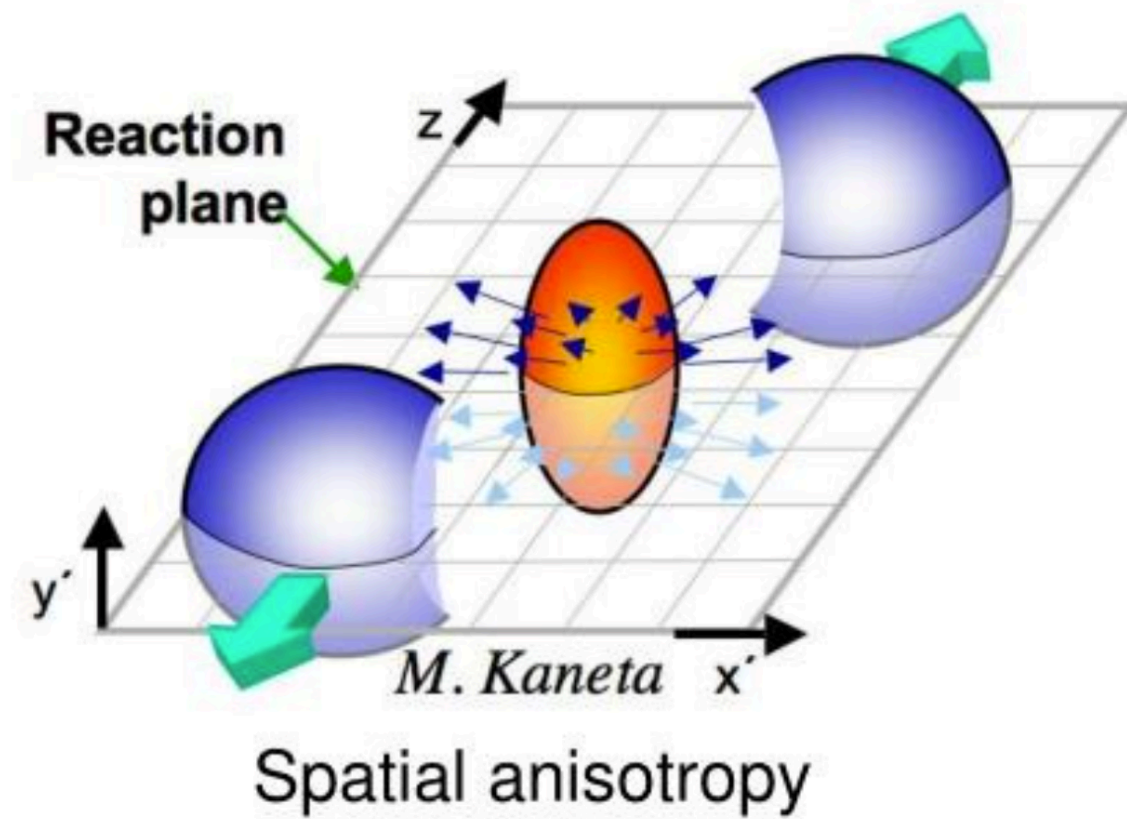
國立臺灣大學  
National Taiwan University



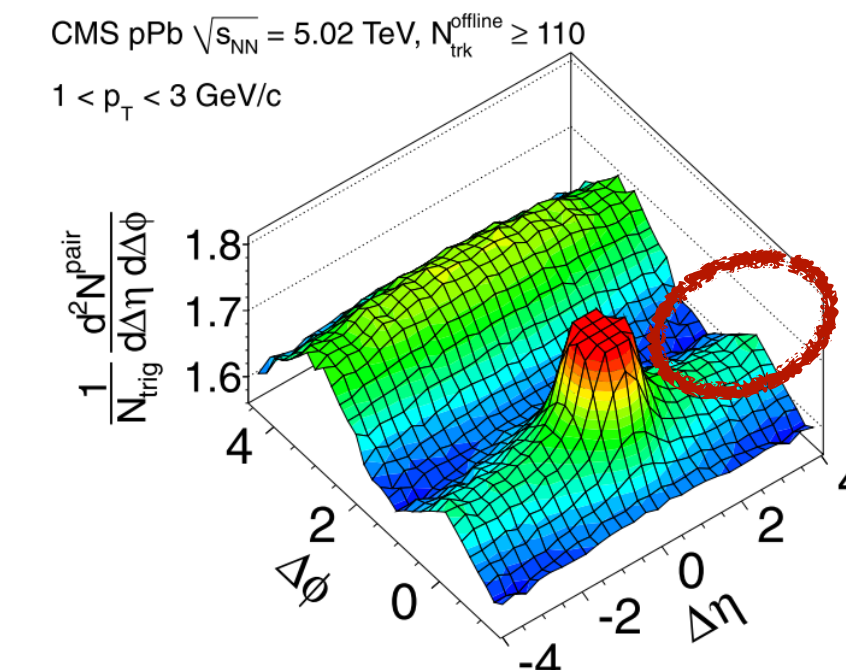
# Motivation

- Collectivity signal

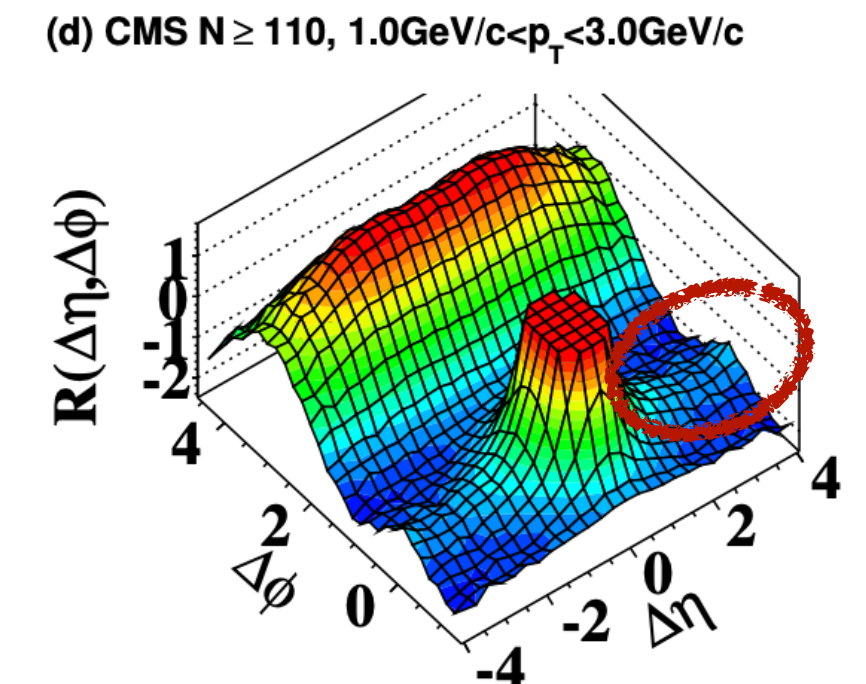
Two-particle correlation: soft probe for Quark-Gluon Plasma (QGP) in heavy ion collisions



**PbPb** [[Eur. Phys. J., C72](#)]

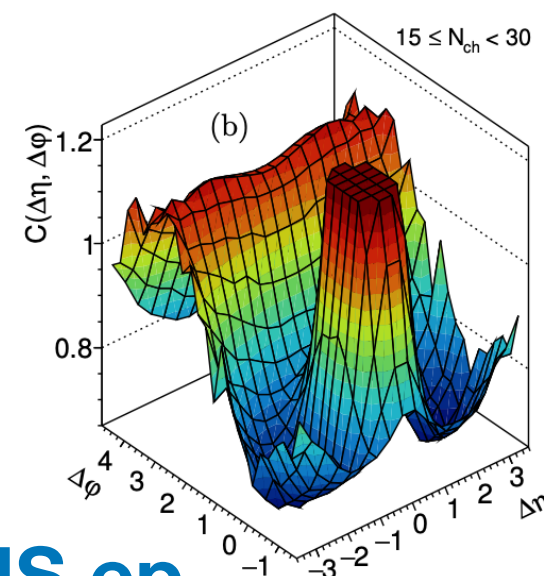


**pPb** [[Phys. Lett. B718 \(2013\) 795-814](#)]

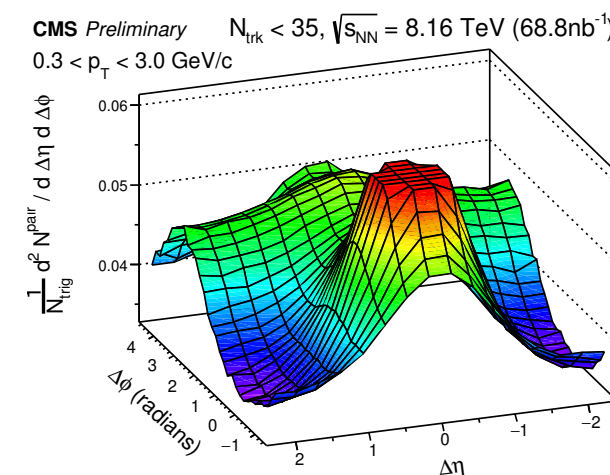


**pp** [[JHEP 1009 \(2010\) 091](#)]

- Minimal conditions for collectivity behavior [[nucl-th:1707.02307](#)]  
Smaller collision systems such as ep,  $e^+e^-$ ,  $\gamma p$ ,  $\gamma A$ , to the future EIC!



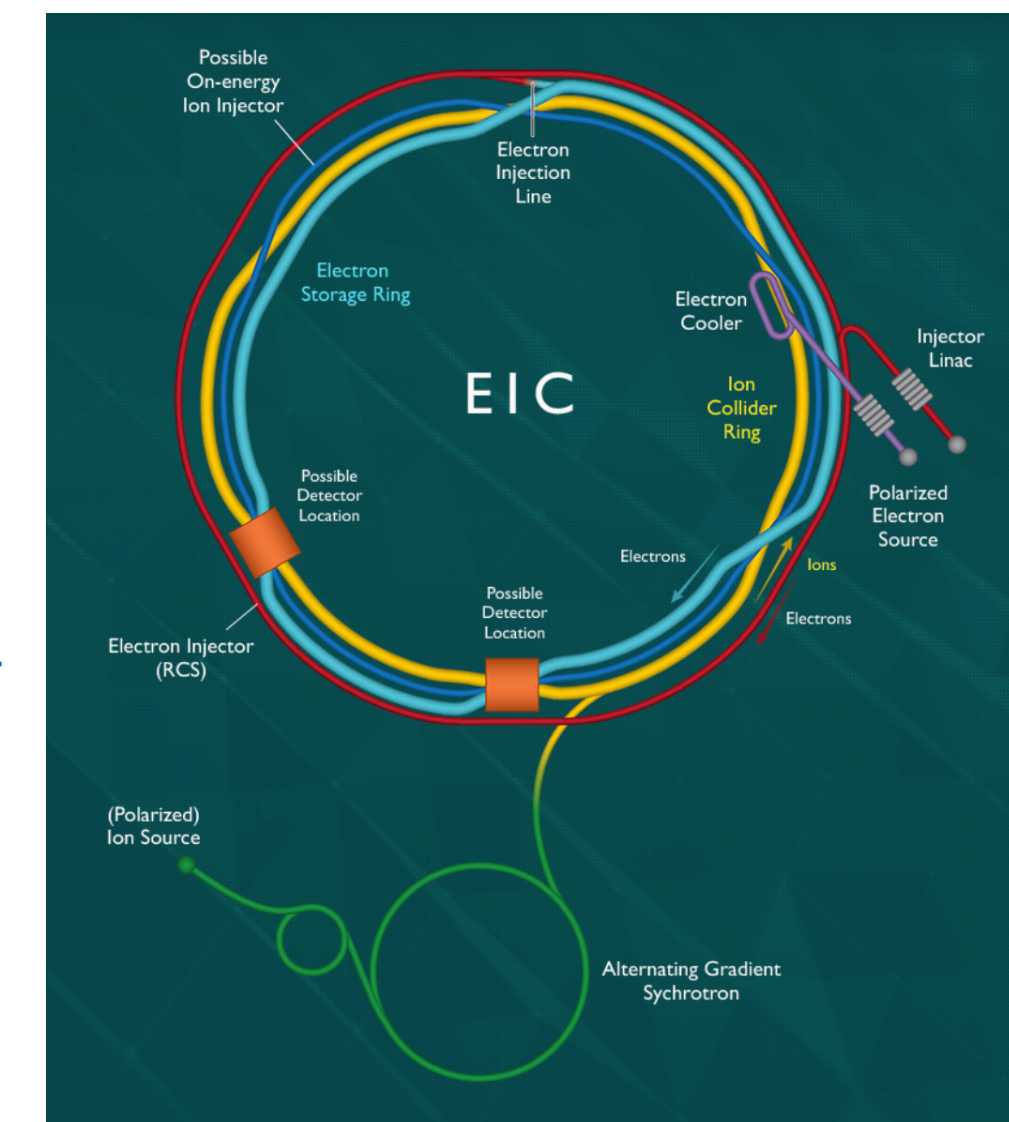
**ZEUS ep**  
[[JHEP 04 \(2020\) 070](#)]



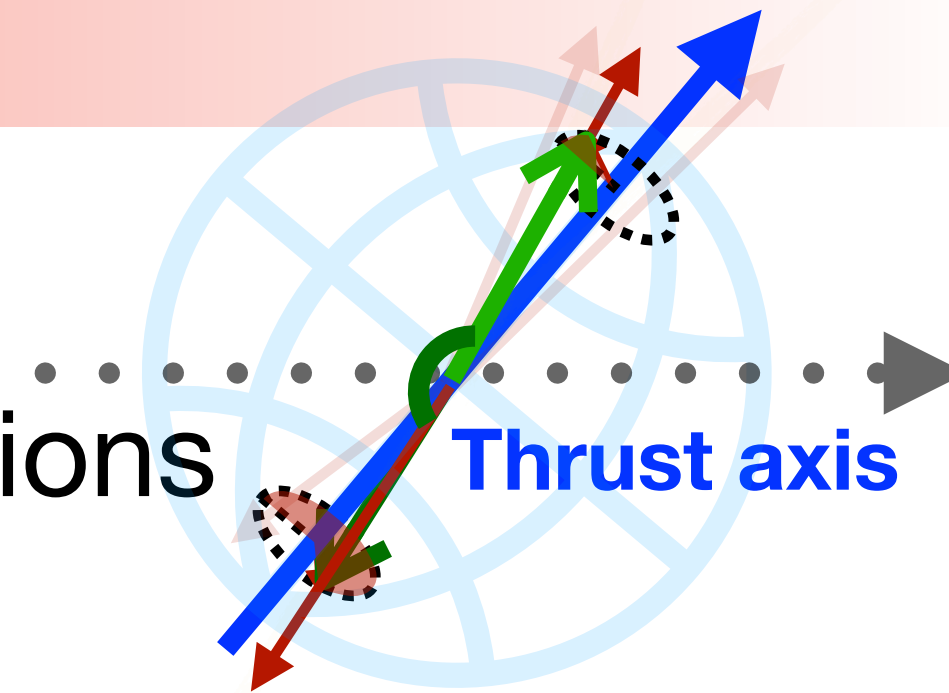
**CMS  $\gamma p$**   
[[CMS-PAS-HIN-18-008](#)]

**ALEPH  $e^+e^-$**  [[Phys. Rev. Lett. 123, 212002 \(2019\)](#)]

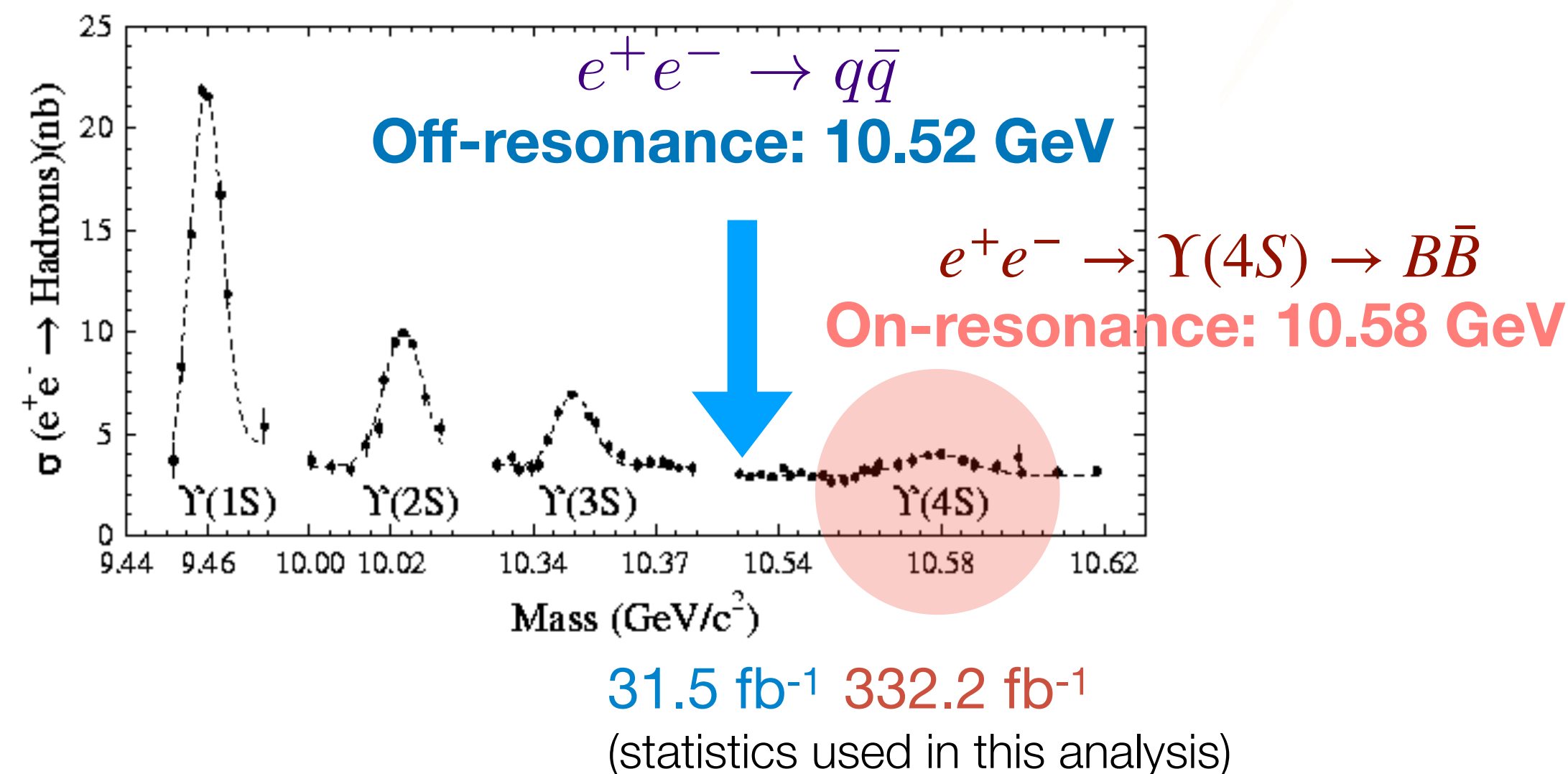
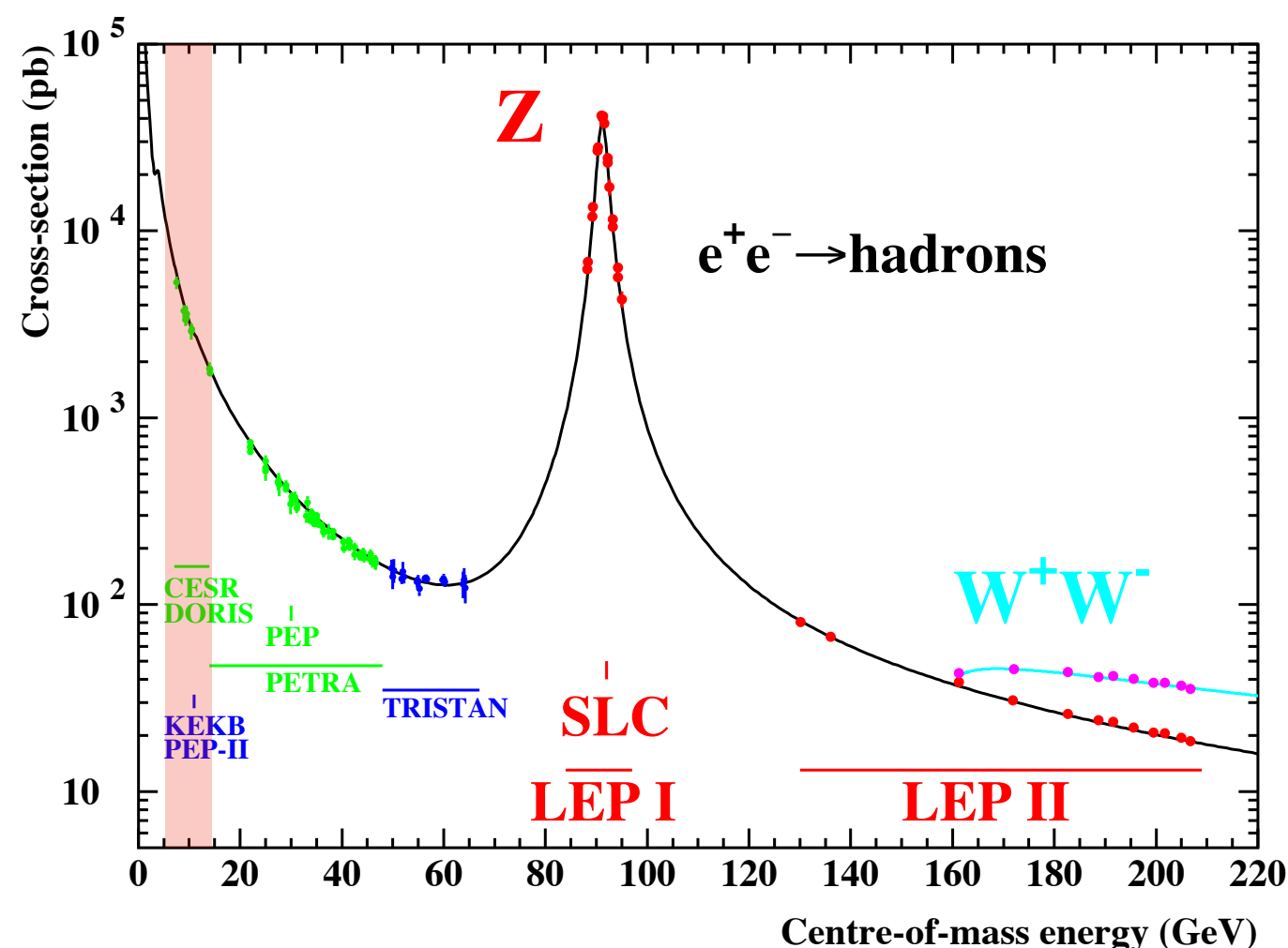
**ATLAS  $\gamma A$**  [[Phys. Rev. C. 104, 014903](#)]





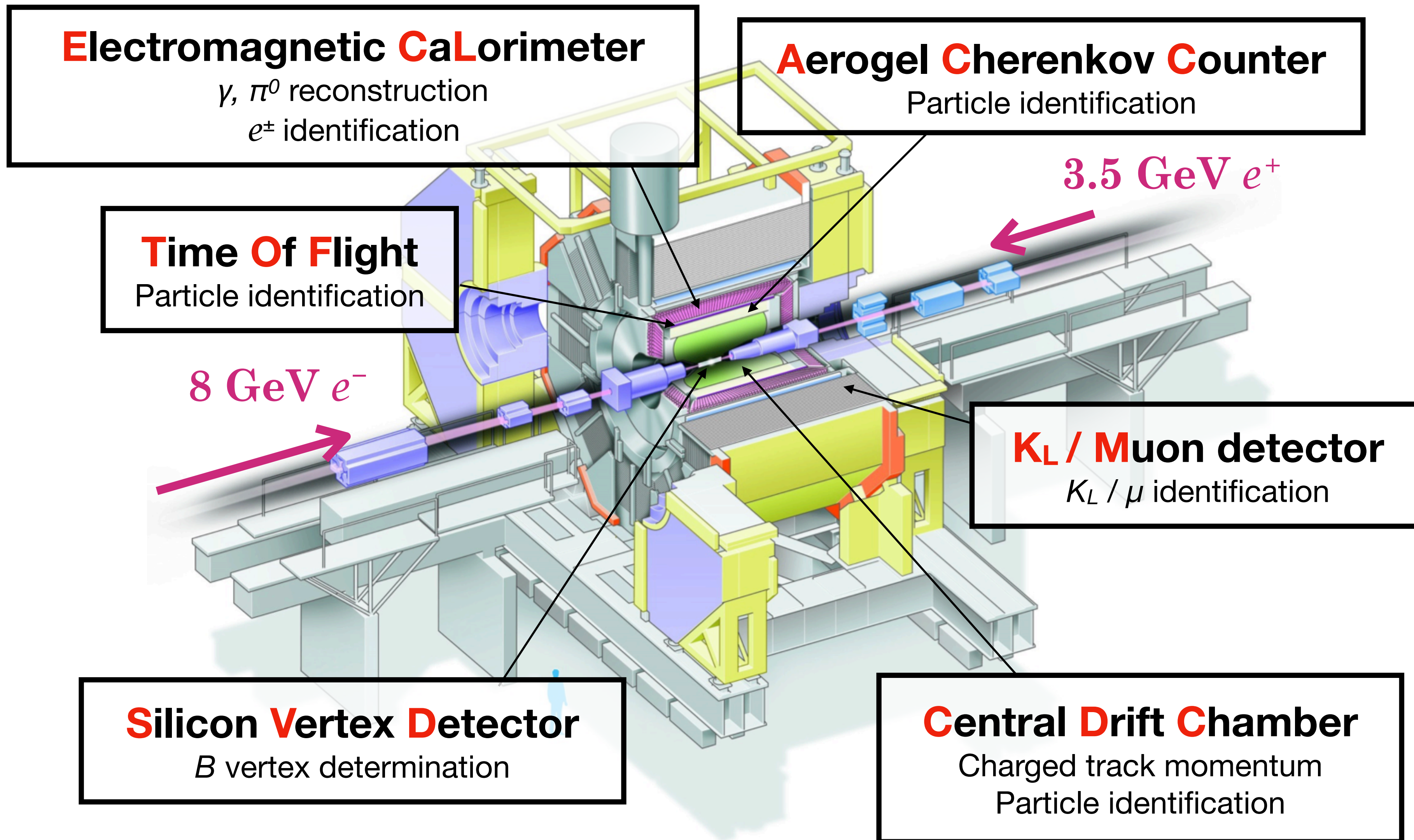


- Thrust-axis two-particle correlation:  
Search for medium expanding transverse to the out-going quark directions
- The first measurement at  $B$ -factory energy:



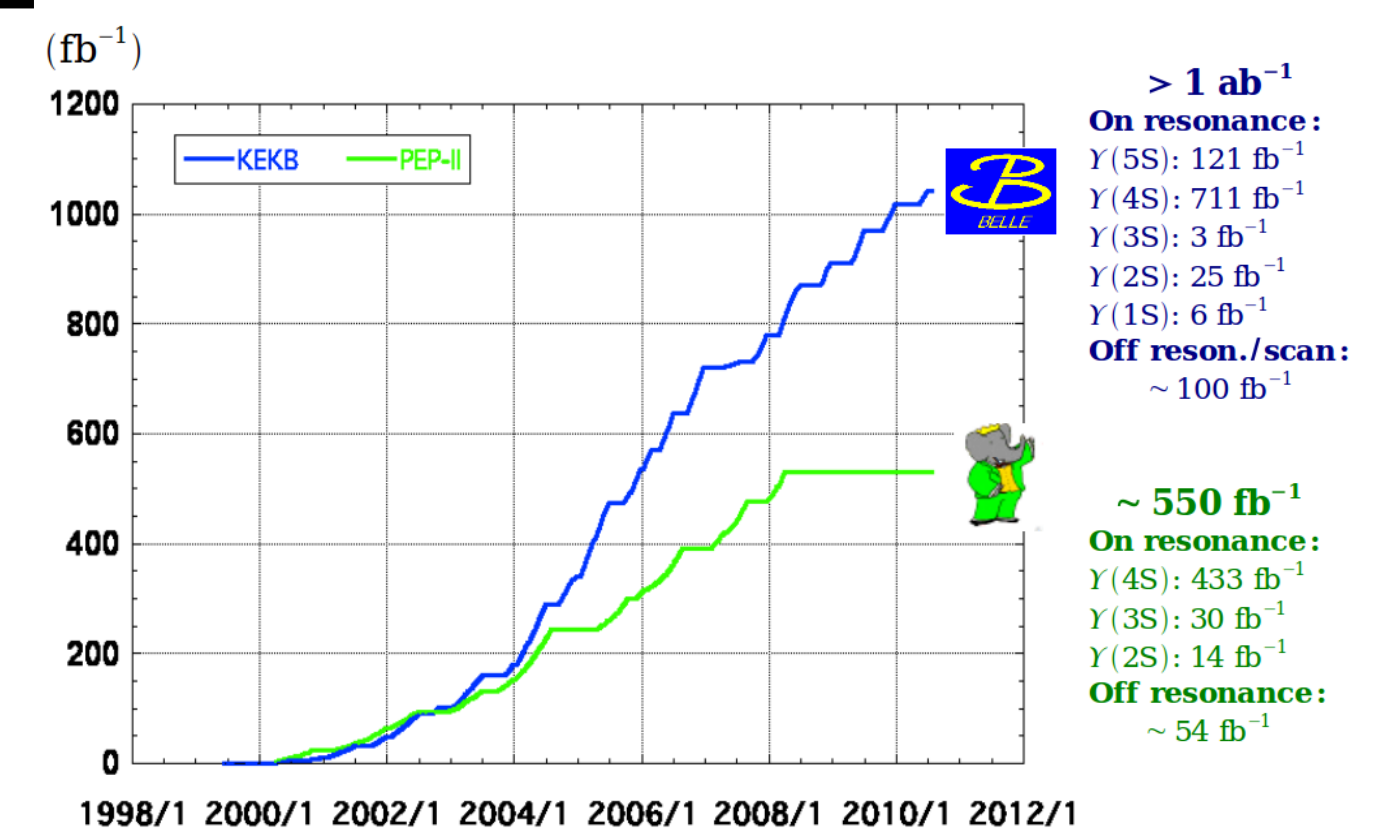
- The advantages:
  - Clean environment of  $e^+e^-$  system: turn-off any possible CGC effect
  - New inputs to the phenomenological fragmentation models at low collision energy
  - Newly-devised “thrust axis analysis” is sensitive to soft emissions





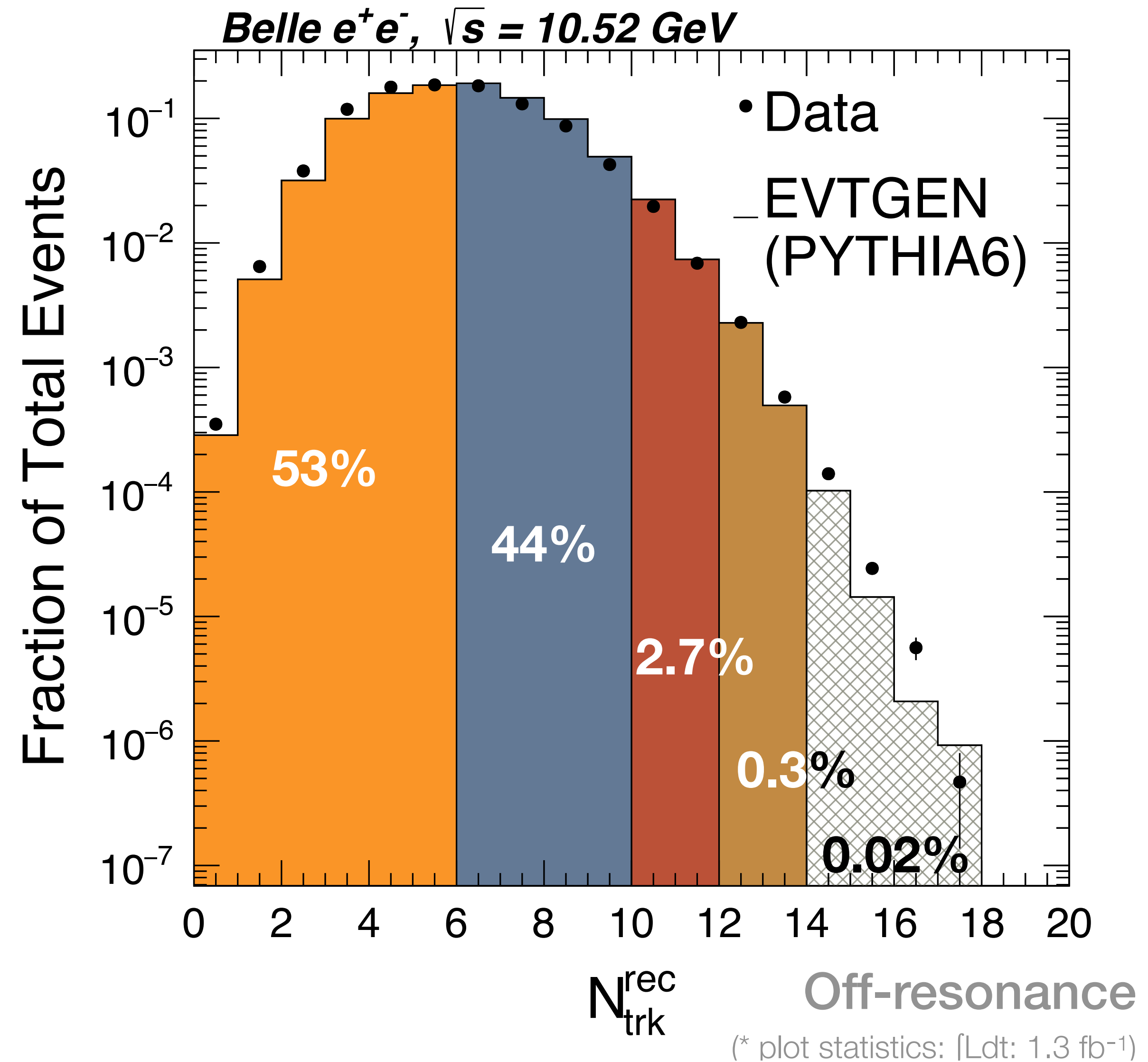
(KEK)

Boost to the CM frame for the correlation study!





- PYTHIA6-based Belle MC:
  - $q\bar{q}$  ( $q = u, d, c$  and  $s$ ) fragmentation
  - $\Upsilon(4S)$  decays (by EVTGEN)
- Also simulated:
  - Radiative Bhabha events
  - Low multiplicity  $e^+e^- \rightarrow l^+l^-$
  - Two-photon processes
- High statistics sample allows for probing the very stringent high-multiplicity class:
   
 $N_{\text{trk}}^{\text{rec}} \geq 14$  (**0.02%** of all events)



on-resonance see backup



Thrust axis is defined with the consideration of the missing momentum (MET):

$$T = \max_{\hat{n}} \frac{\sum_i |\vec{p}_i \cdot \hat{n}|}{\sum_i |\vec{p}_i|}$$

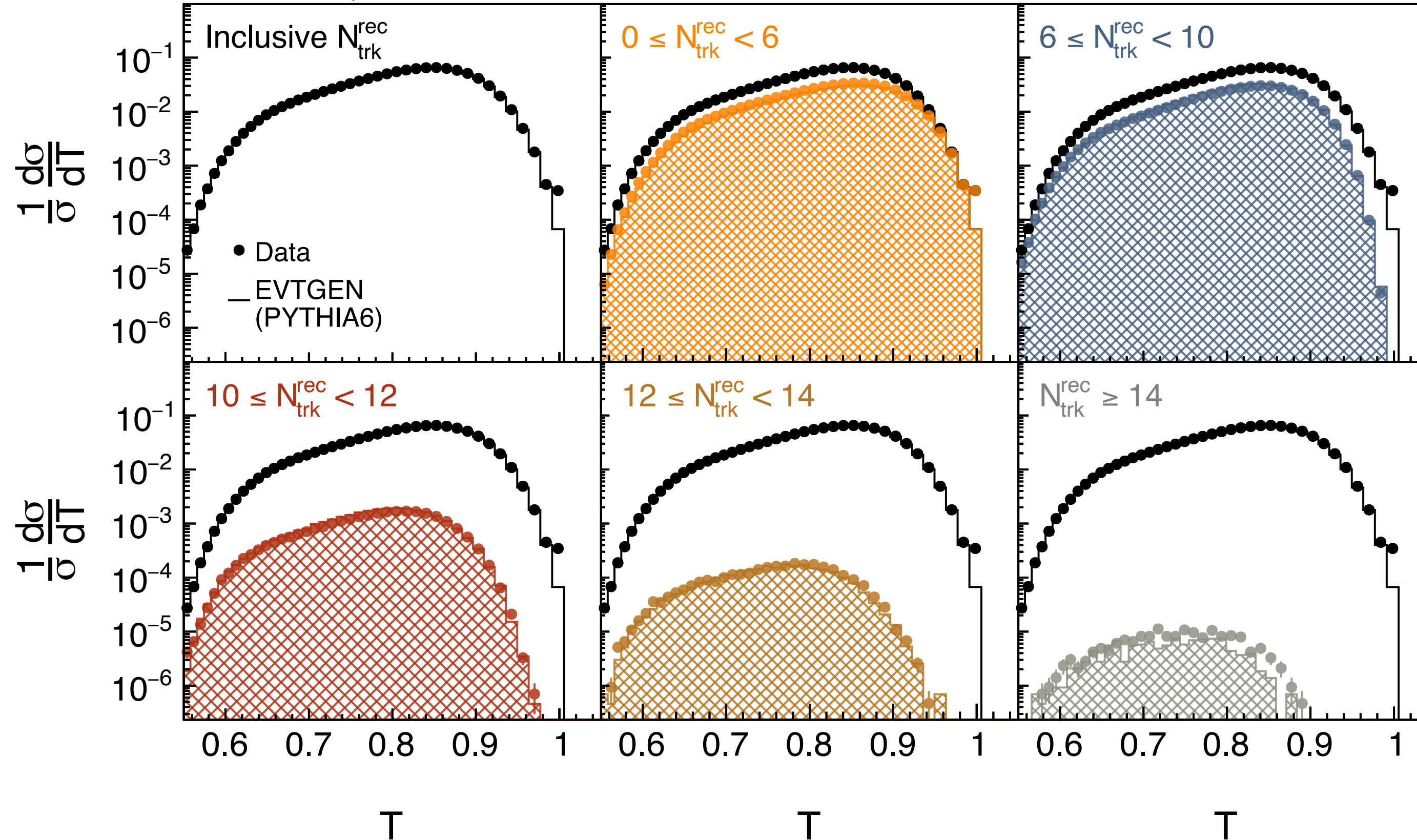
( $i \in$  charged, neutral particles and MET)

$$\vec{p}_{\text{MET}} = - \sum_{\text{neu,chg}} \vec{p}$$

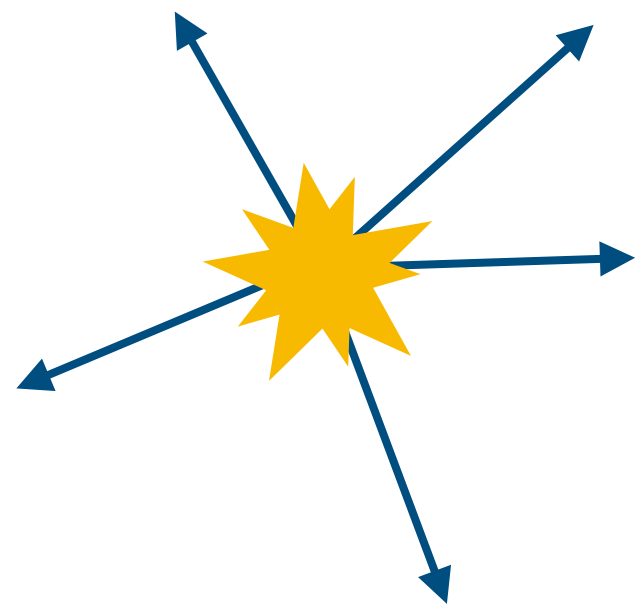
Off-resonance

(\* plot statistics:  $\int \text{Ldt: } 1.3 \text{ fb}^{-1}$ )

Belle  $e^+e^-$ ,  $\sqrt{s} = 10.52 \text{ GeV}$



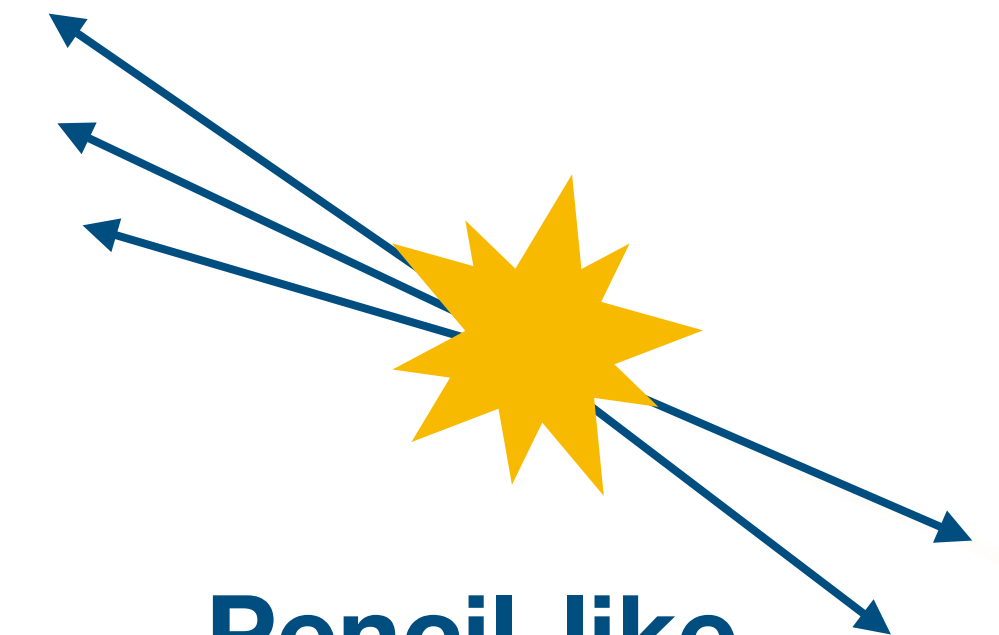
$T$  closes to 0.5



Spherical

ex:  $B$ -decay

$T$  closes to 1



Pencil-like

ex:  $q\bar{q}$  fragmentation

on-resonance see backup



## BELLE

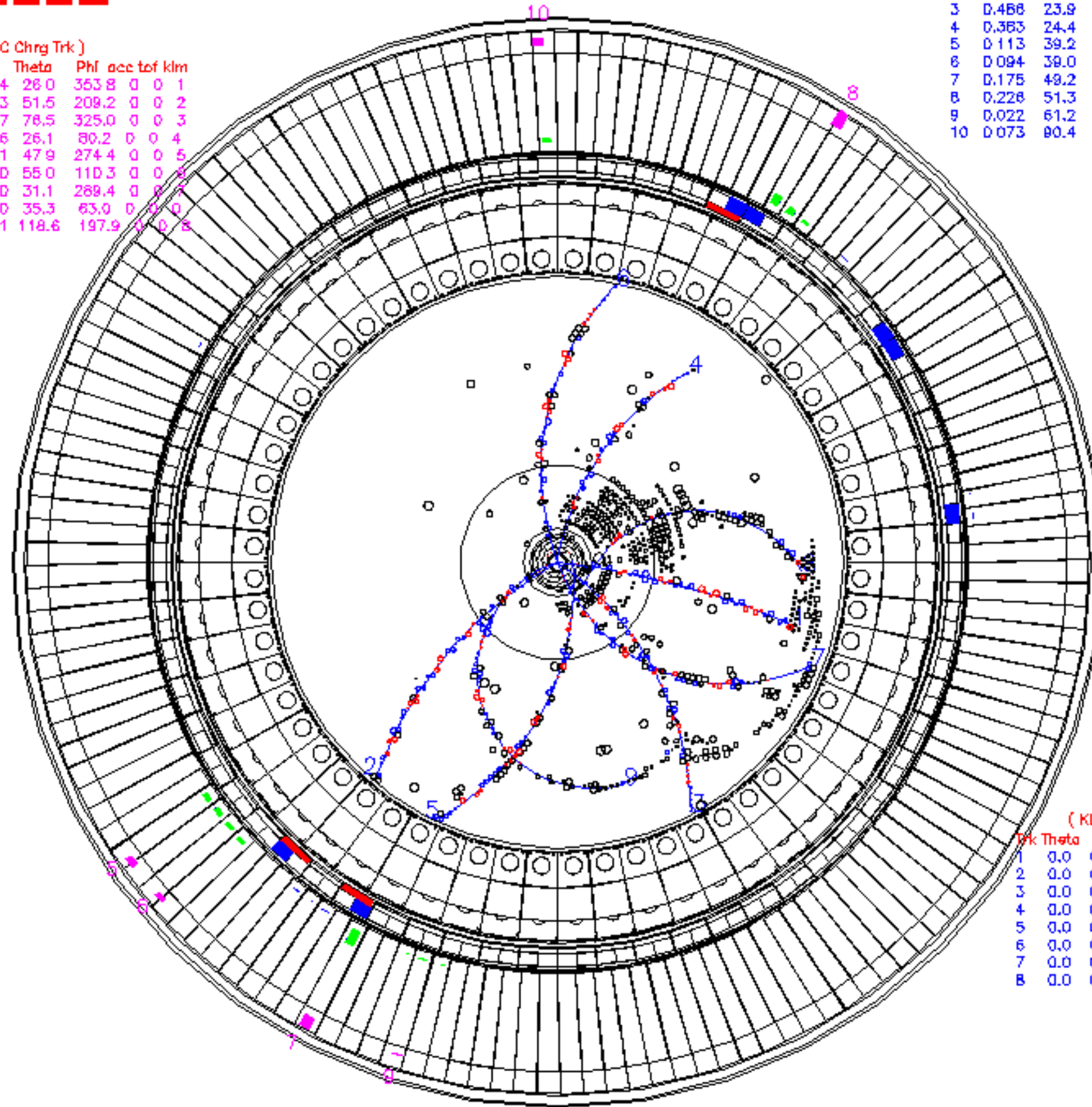
Exp 3 Run 34 Farm 3 Event 118  
 Eher 8.00 Eler 3.50 Date/TIME Tue Jun 1 22z12z01 1999  
 TrgID 0 DetVer 0 MagID 0 BField 1.50 DspVer 2.01

(CDC Chrg Trk)

Trk	ch	Ptot	Theta	Phi	acc	tof	klm
1	+	2.364	26.0	353.8	0	0	1
2	-	0.683	51.5	209.2	0	0	2
3	+	0.437	76.5	325.0	0	0	3
4	+	0.826	26.1	80.2	0	0	4
5	+	0.491	47.9	274.4	0	0	5
6	+	0.440	55.0	110.3	0	0	6
7	-	0.480	31.1	289.4	0	0	7
8	+	0.290	35.3	63.0	0	0	8
9	-	0.181	118.6	197.9	0	0	9

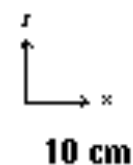
(ECL)

Trk	E	Theta	Phi	match	elld
1	0.147	20.3	337.3	0	0
2	0.039	22.8	34.8	2	0
3	0.468	23.9	44.2	1	0
4	0.363	24.4	352.2	1	0
5	0.113	39.2	215.1	2	0
6	0.094	39.0	220.1	1	0
7	0.175	49.2	241.4	1	0
8	0.228	51.3	57.5	1	0
9	0.022	61.2	252.0	0	0
10	0.073	90.4	92.1	0	0



(KLM)

Trk	Theta	Phi	Muld	Match
1	0.0	0.0	0	1
2	0.0	0.0	0	2
3	0.0	0.0	0	3
4	0.0	0.0	0	4
5	0.0	0.0	0	5
6	0.0	0.0	0	6
7	0.0	0.0	0	7
8	0.0	0.0	0	8

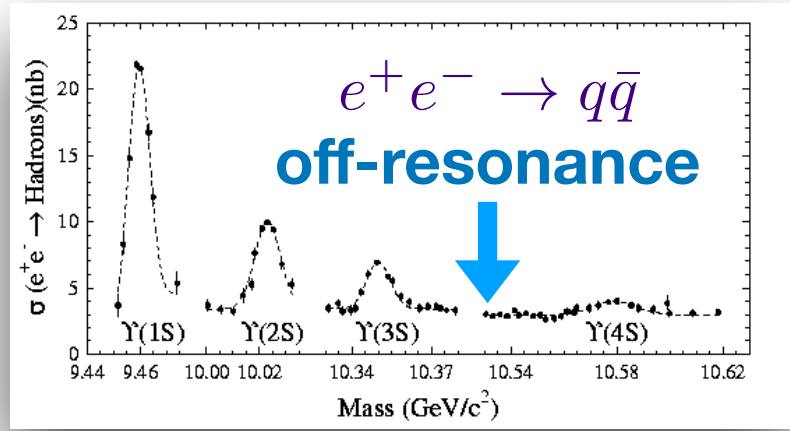


gdl-in =z  
 ftdl-out=z  
 gdl-out =z

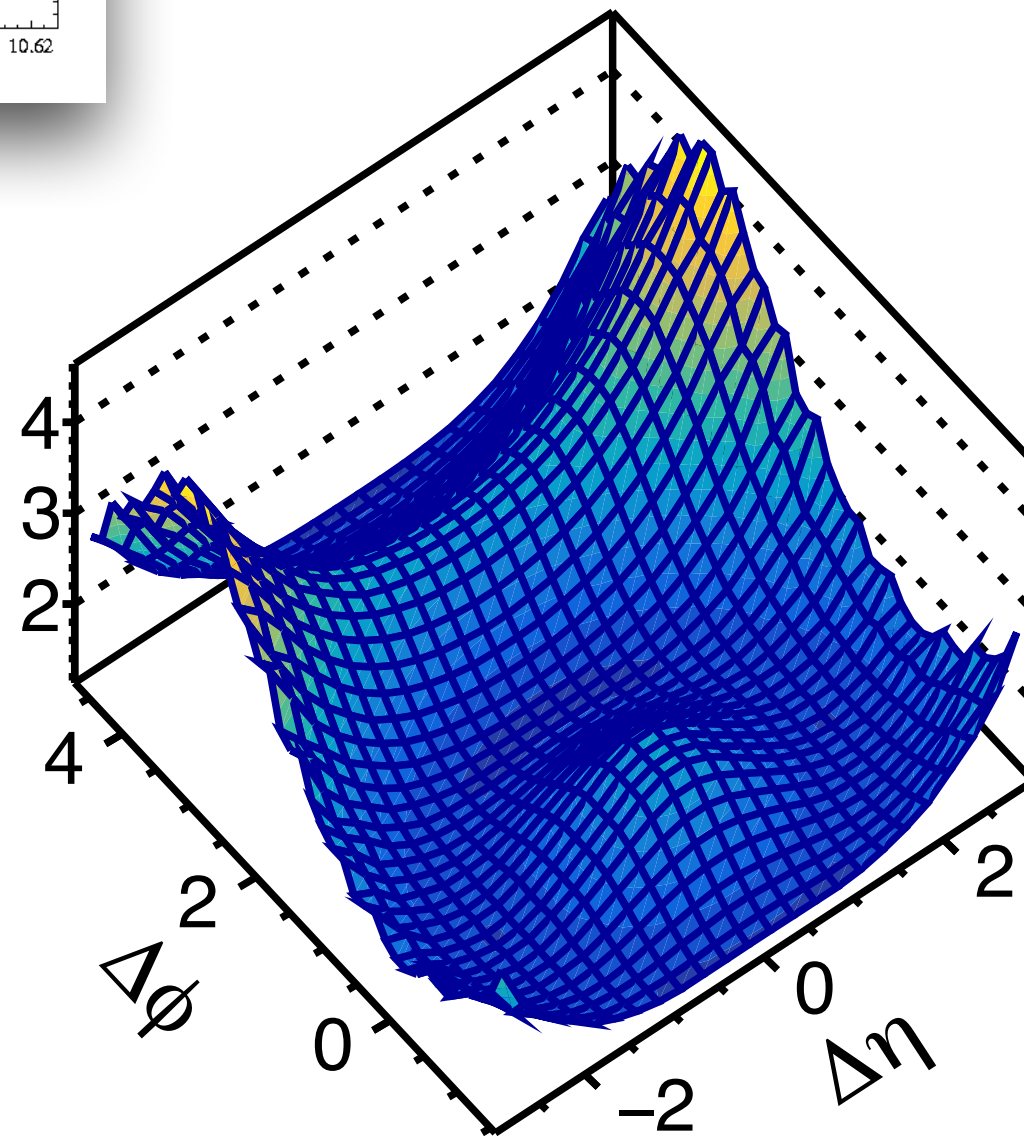
Belle has rather spherical events!



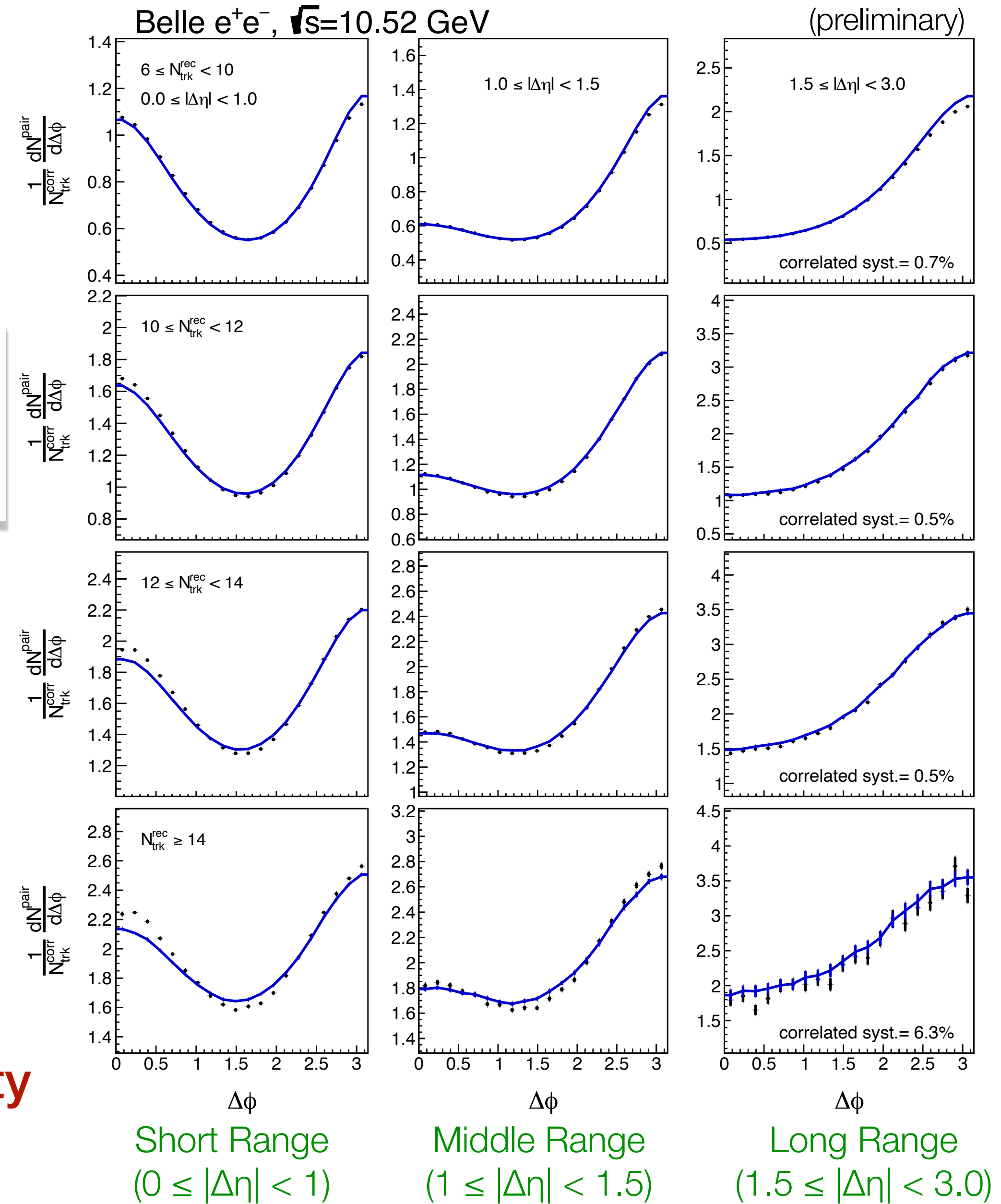
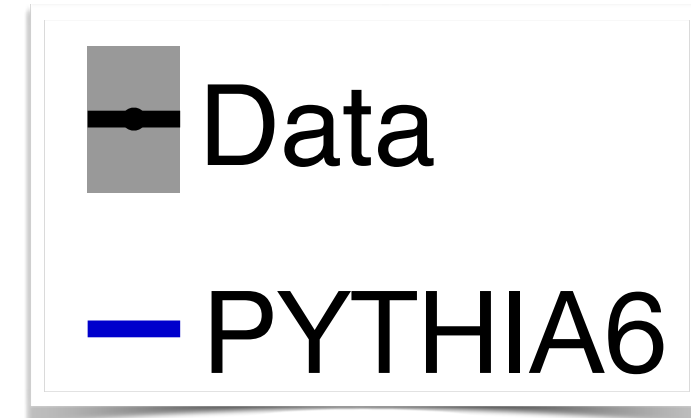
- Reasonable data and MC agreements
- Intriguing discrepancies in high-multiplicity events from short to the middle range



$$\frac{1}{N_{\text{trk}}^{\text{corr}}} \frac{d^2 N^{\text{pair}}}{d\Delta\eta d\Delta\phi}$$



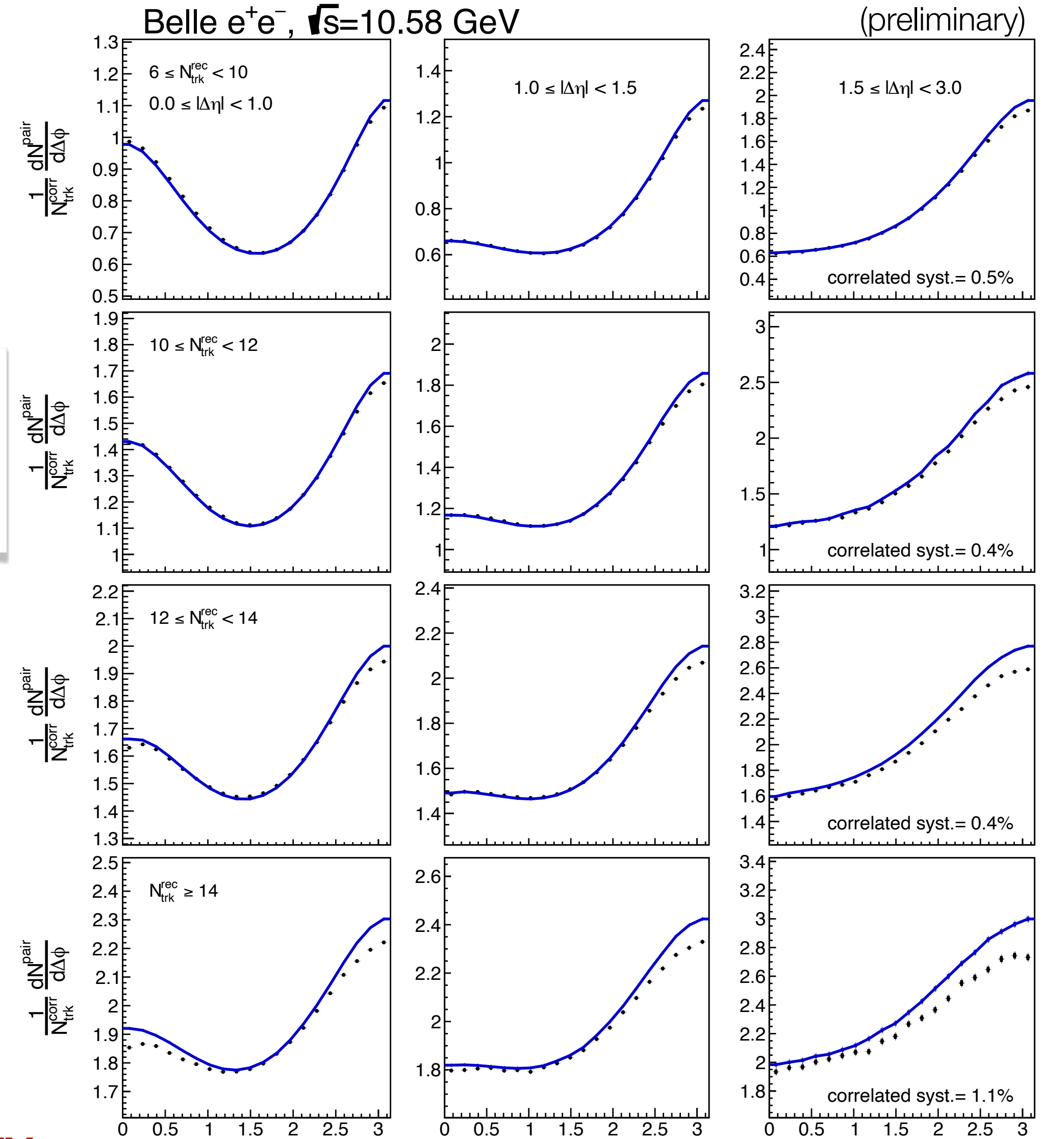
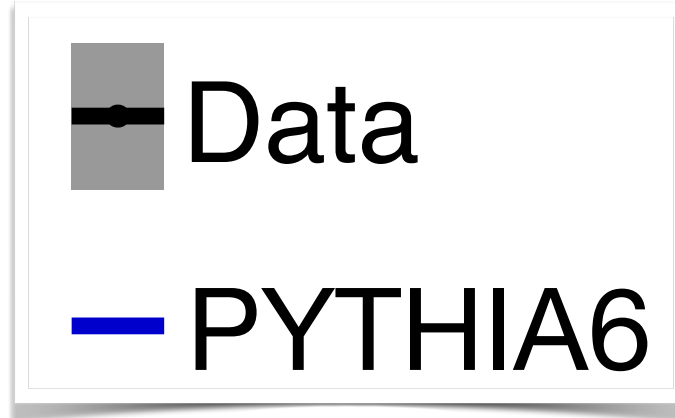
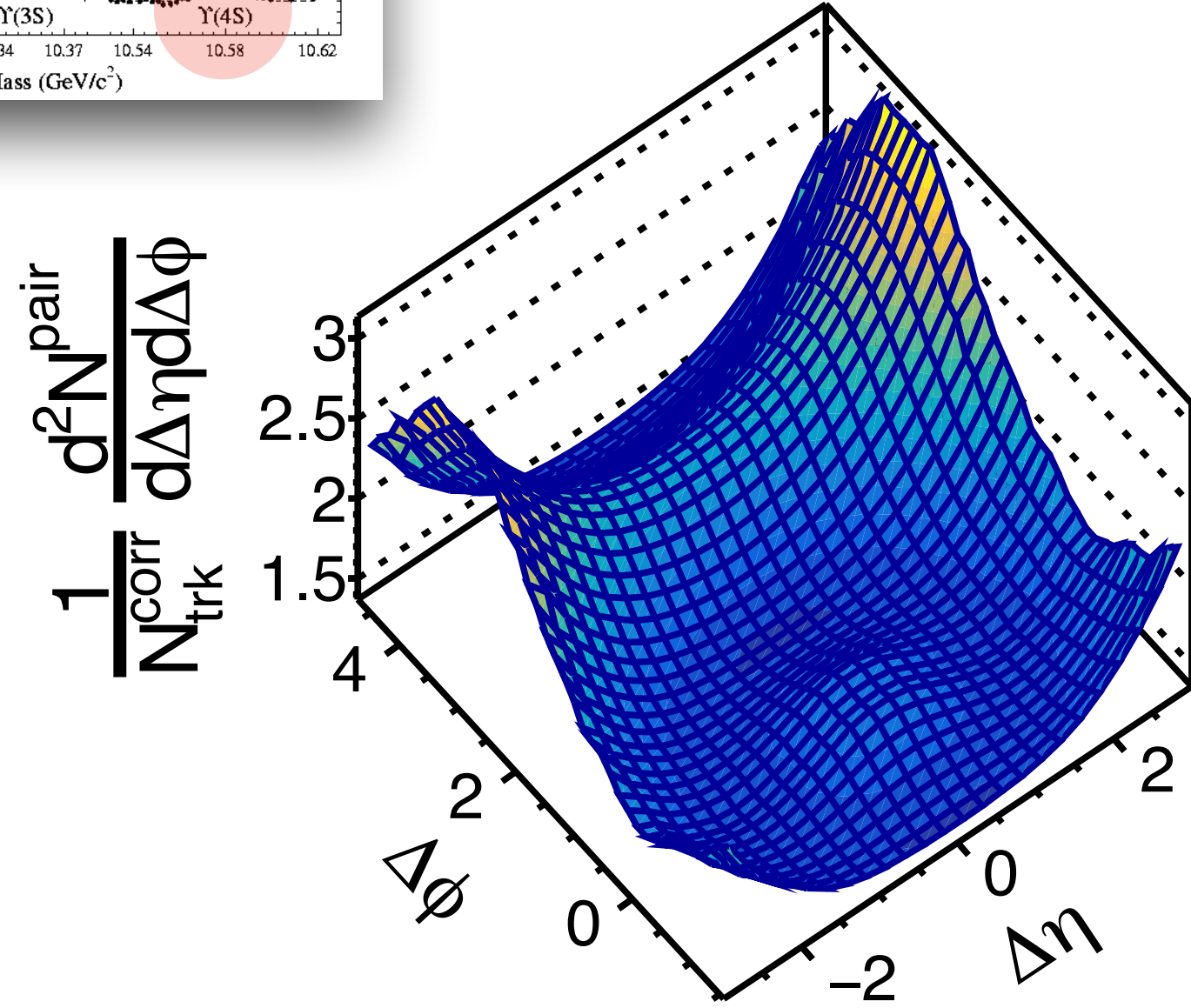
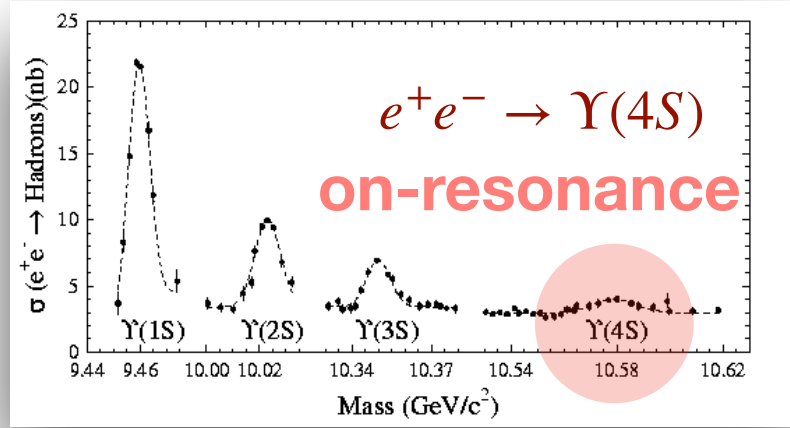
$$12 \leq N_{\text{trk}}^{\text{rec}} < 14$$



High-multiplicity

arXiv:2201.01694  
accepted by PRL

- Larger discrepancies are observed btw data and PYTHIA6 in the near-side ( $\Delta\phi \approx 0$ ) and away-side ( $\Delta\phi \approx \pi$ ) peak values



paper in preparation

$$12 \leq N_{\text{trk}}^{\text{rec}} < 14$$

High-multiplicity

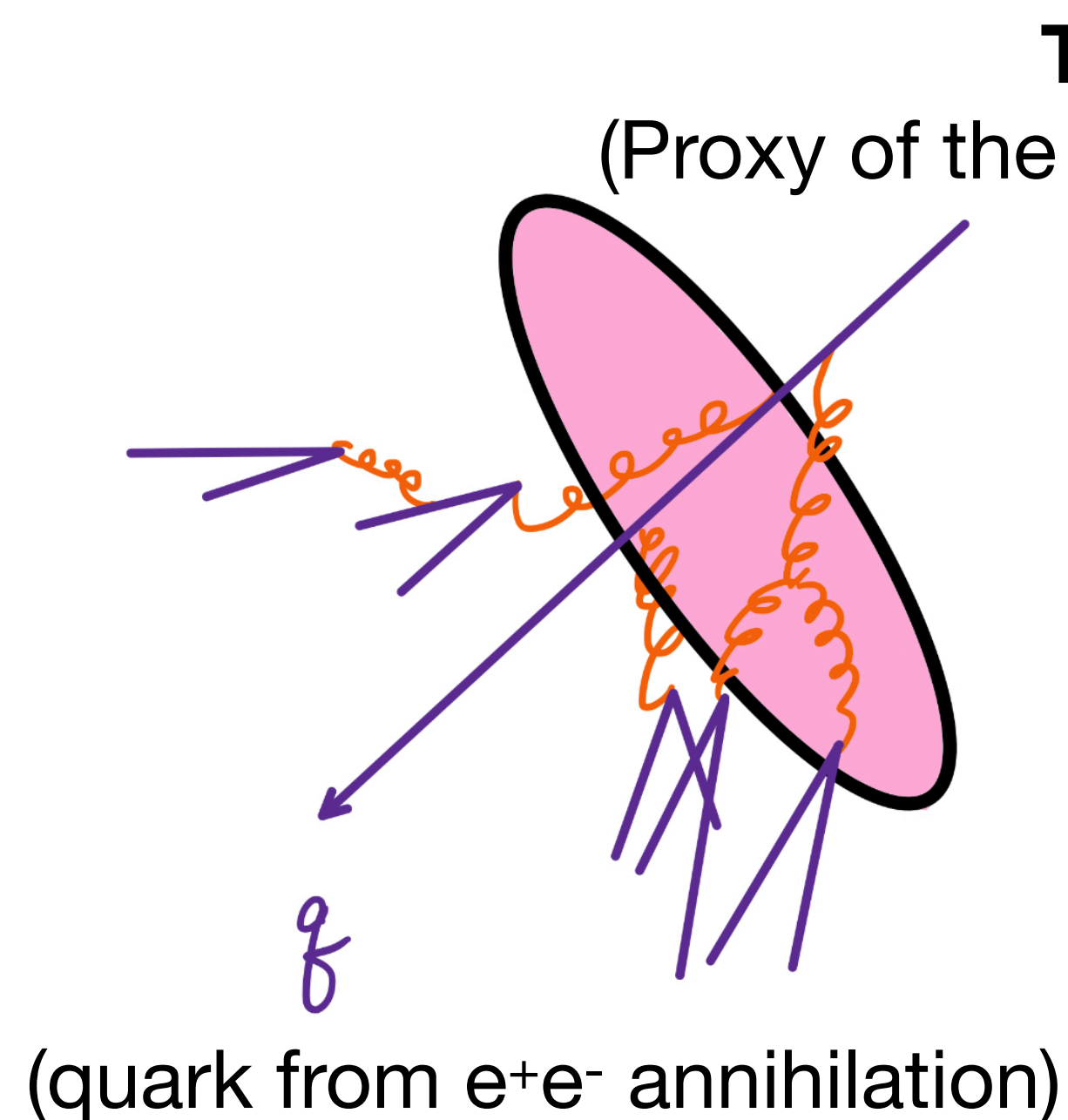
Short Range  
( $0 \leq |\Delta\eta| < 1$ )

Middle Range  
( $1 \leq |\Delta\eta| < 1.5$ )

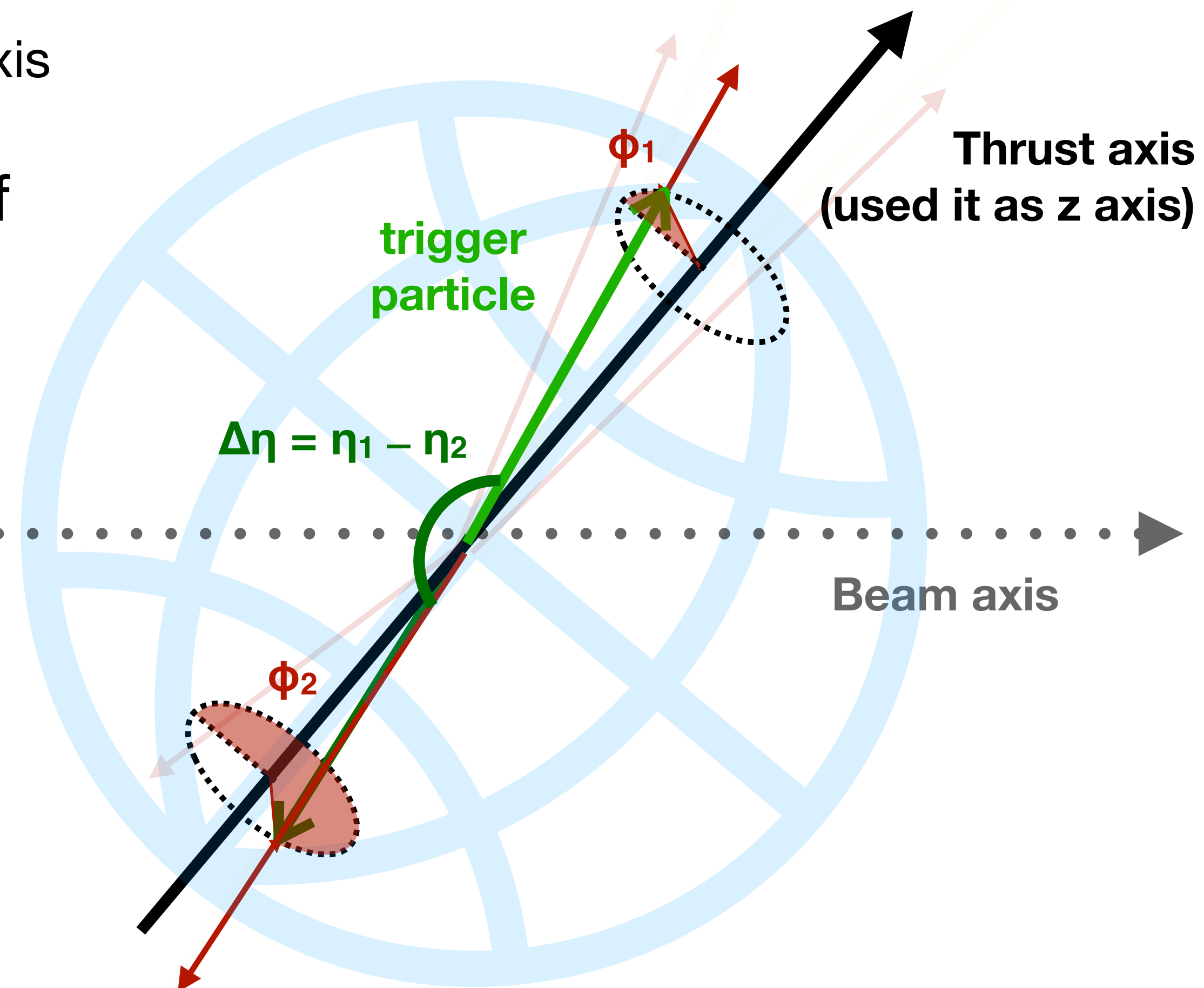
Long Range  
( $1.5 \leq |\Delta\eta| < 3.0$ )



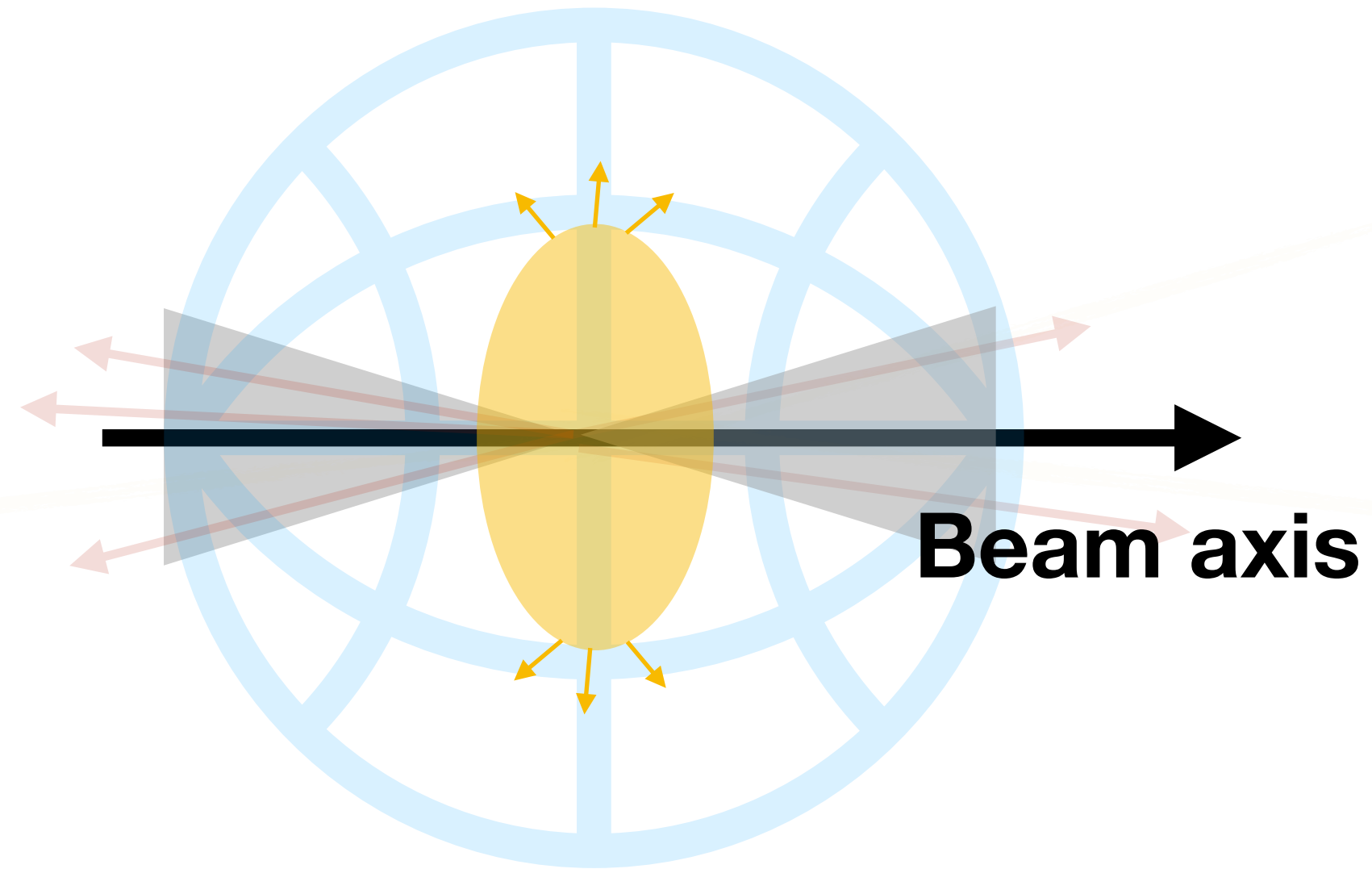
- New reference z axis: event thrust axis  
particles  $(p_T, \eta, \phi)$  are re-calculated with respect to thrust axis
- Similar to heavy-ion collisions study, the role of beam remnant is replaced by outgoing quarks



If high energy quarks can form some medium, looking from the thrust axis is sensitive to the azimuthal anisotropy of this "imaginary medium."



ALEPH  
 $e^+e^-$ : *Phys. Rev. Lett.*  
123, 212002 (2019)

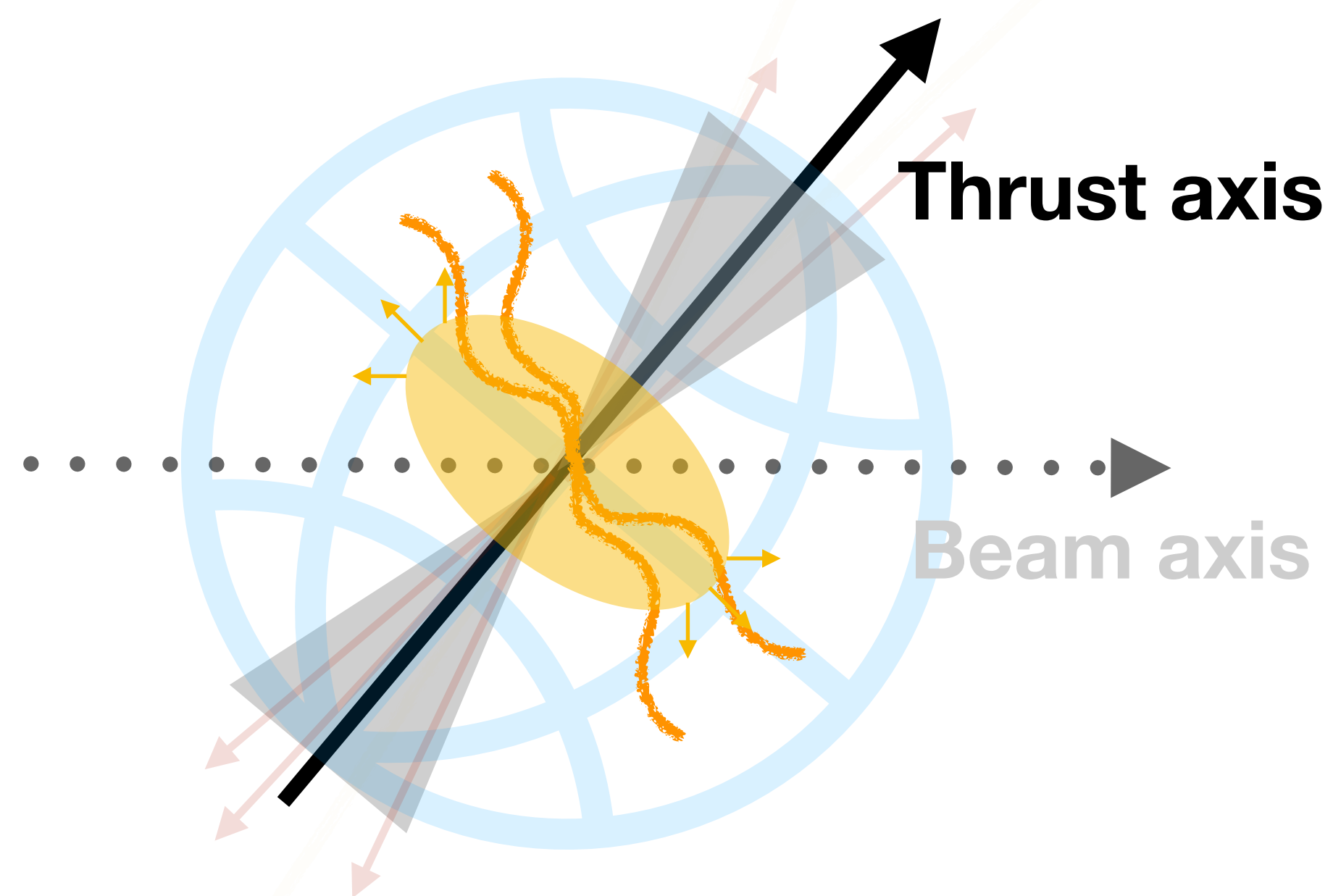
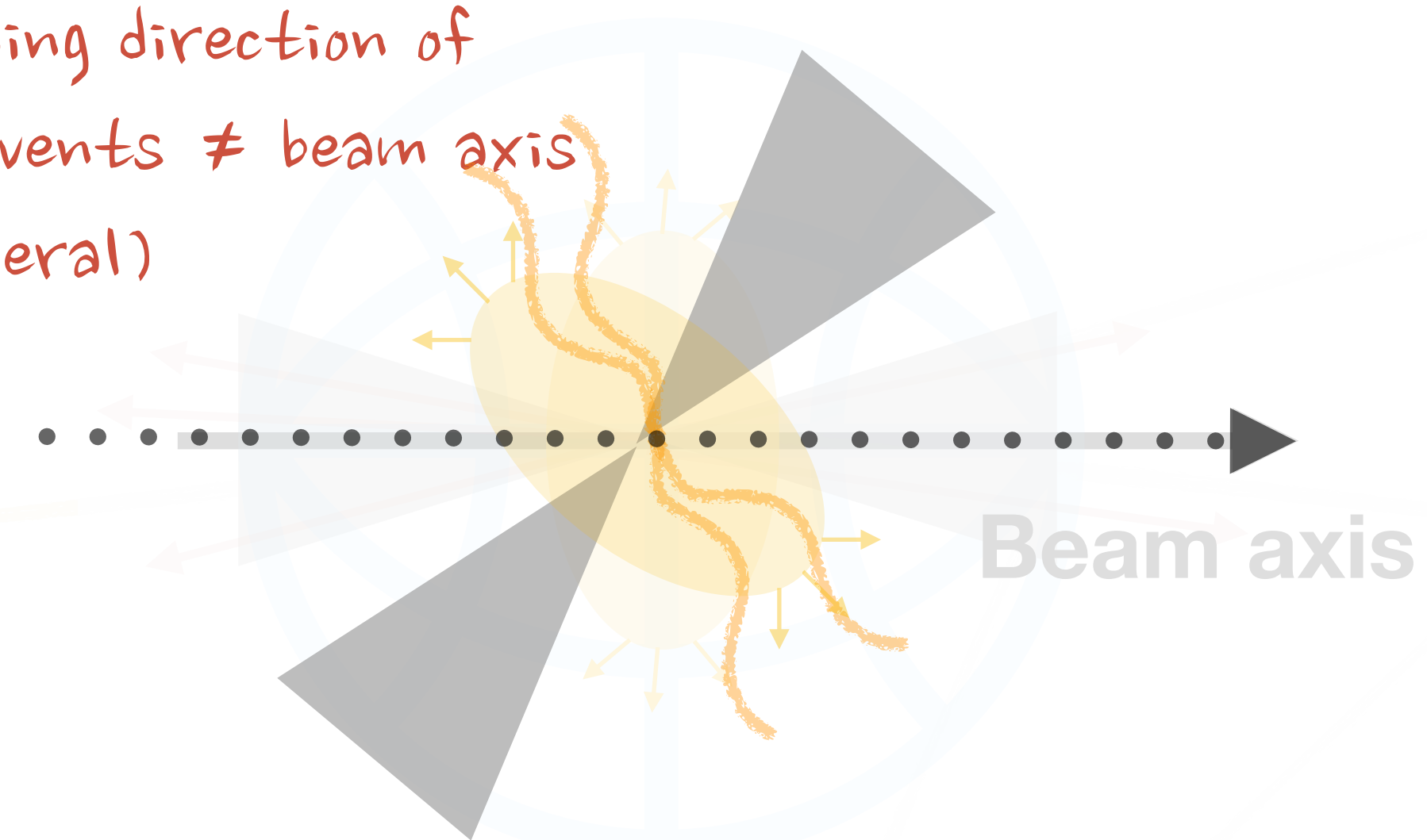


The **mid rapidity region** is where a correlation function sensitive to:

- Beam axis analysis: hydrodynamic expansion of possible QGP medium in HI collisions



Out-going direction of  
 $e^+e^-$  events  $\neq$  beam axis  
 (in general)

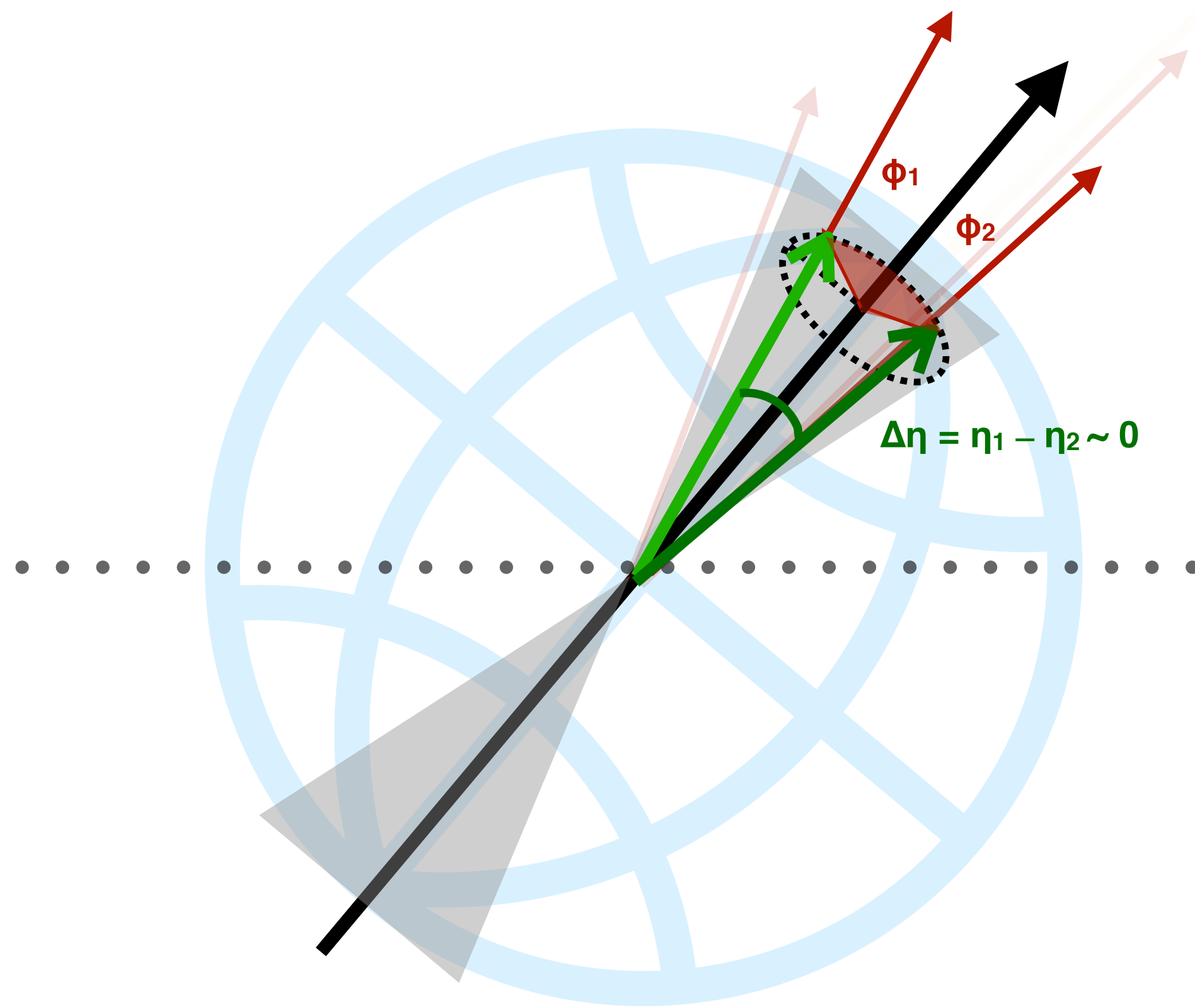


The **mid rapidity region** is where a correlation function sensitive to:

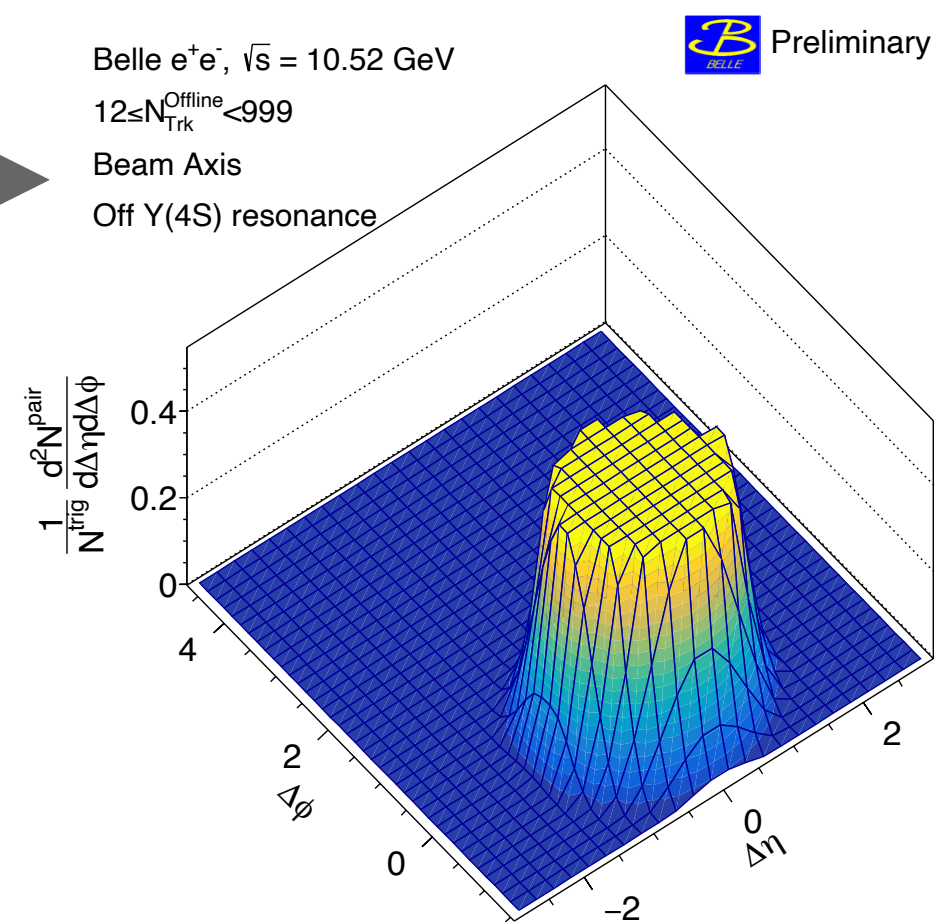
- Beam axis analysis:  
hydrodynamic expansion of possible QGP medium in HI collisions
- Thrust axis analysis:  
soft emissions or QGP in  $e^+e^-$  annihilation

# How to understand correlation function in thrust axis coordinate?

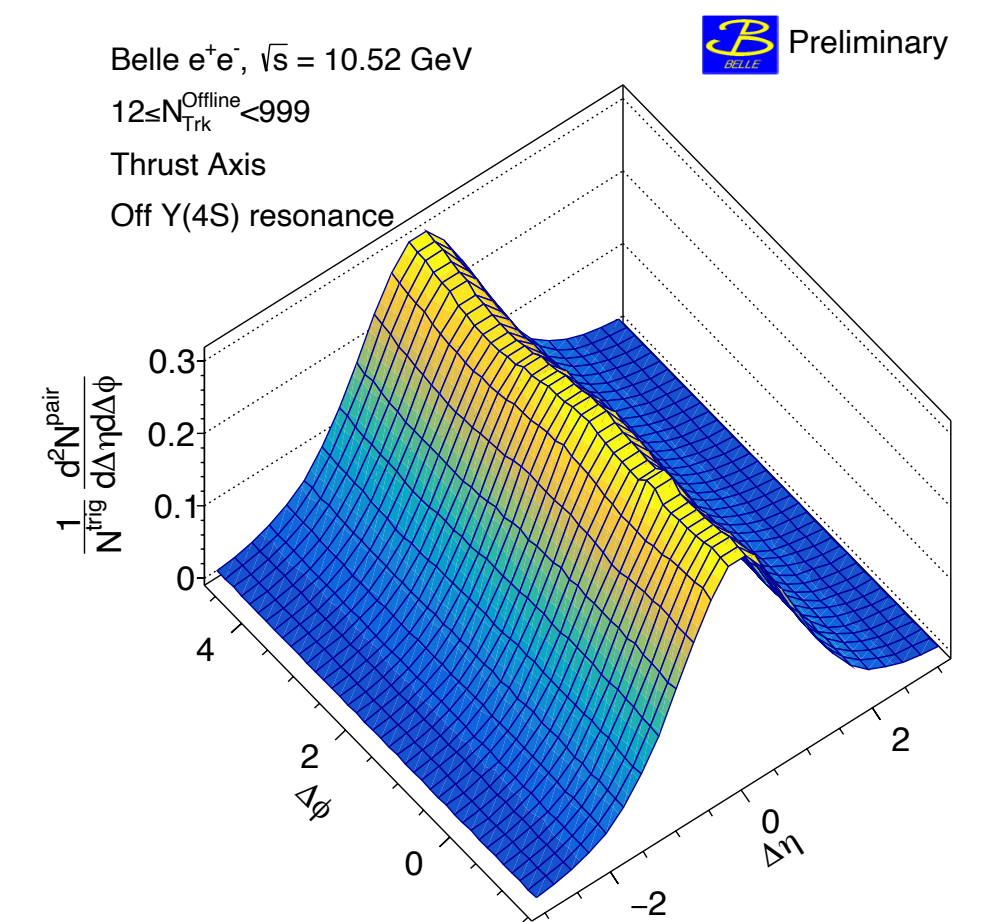
- Intra-jet correlation of on-axis jets is diluted!



Collinear leading intra-jet correlation dilutes along  $\Delta\phi$



leading intra-jet correlation viewed @ beam coordinate



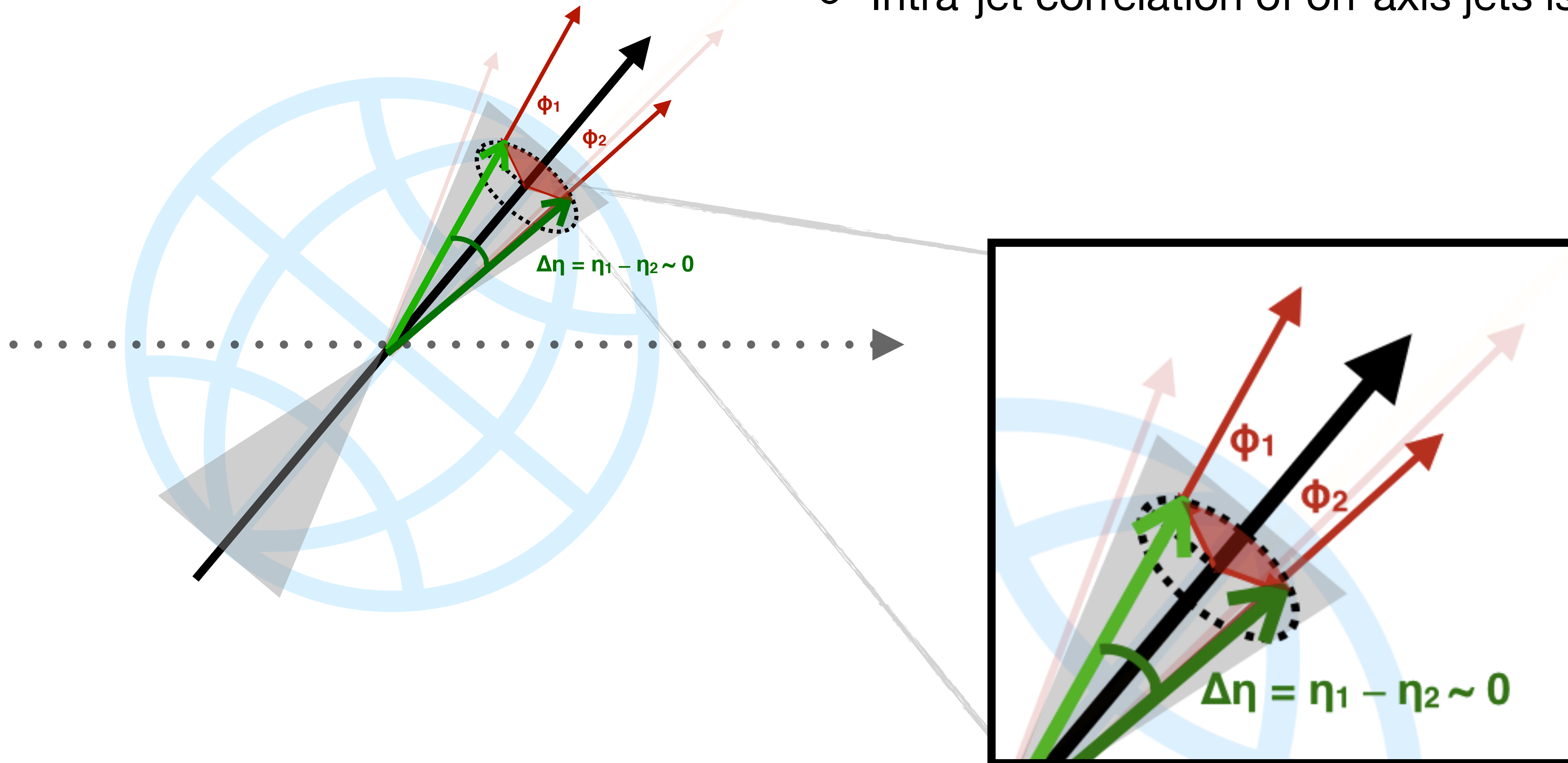
leading intra-jet correlation viewed @ thrust coordinate





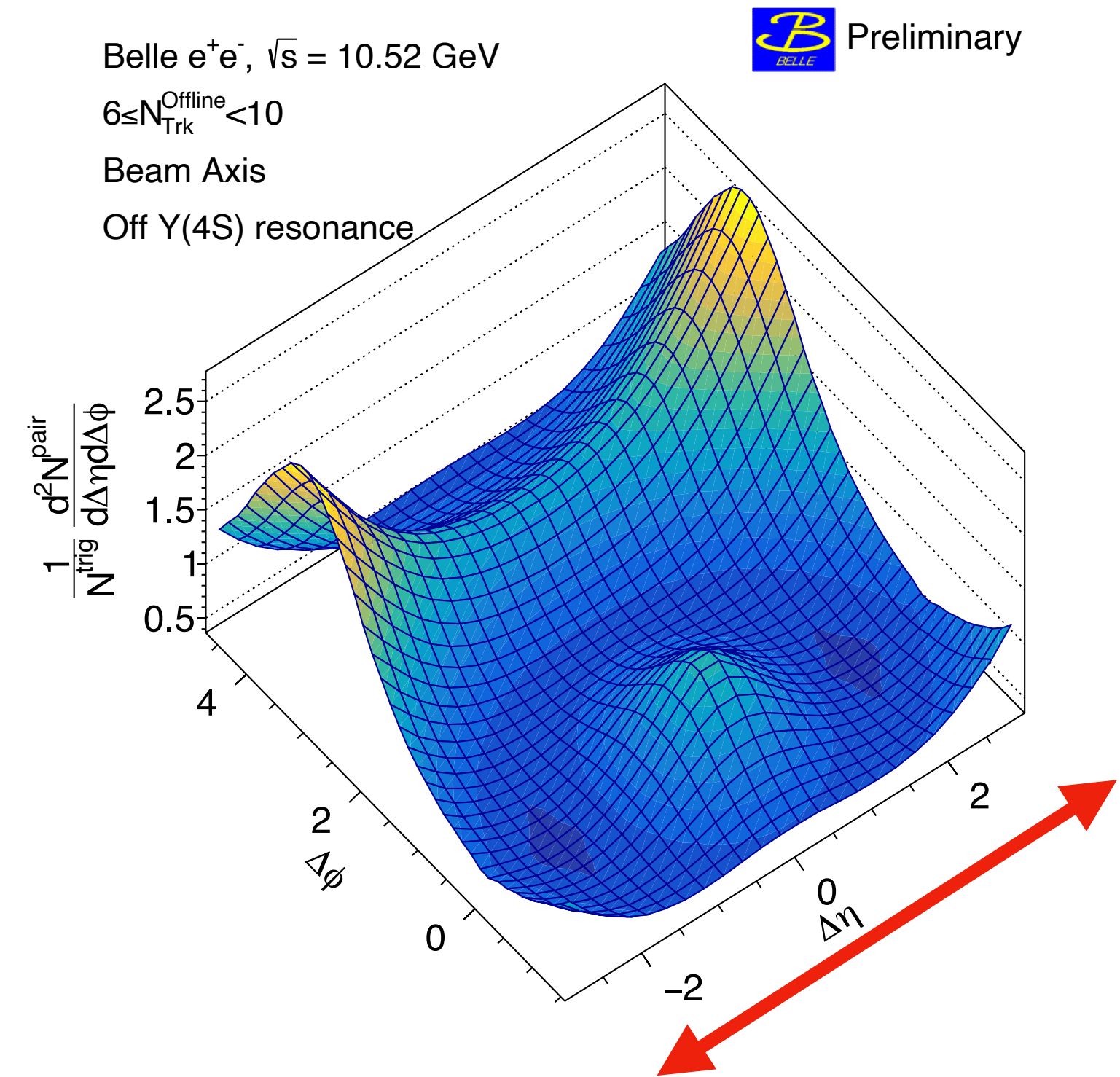
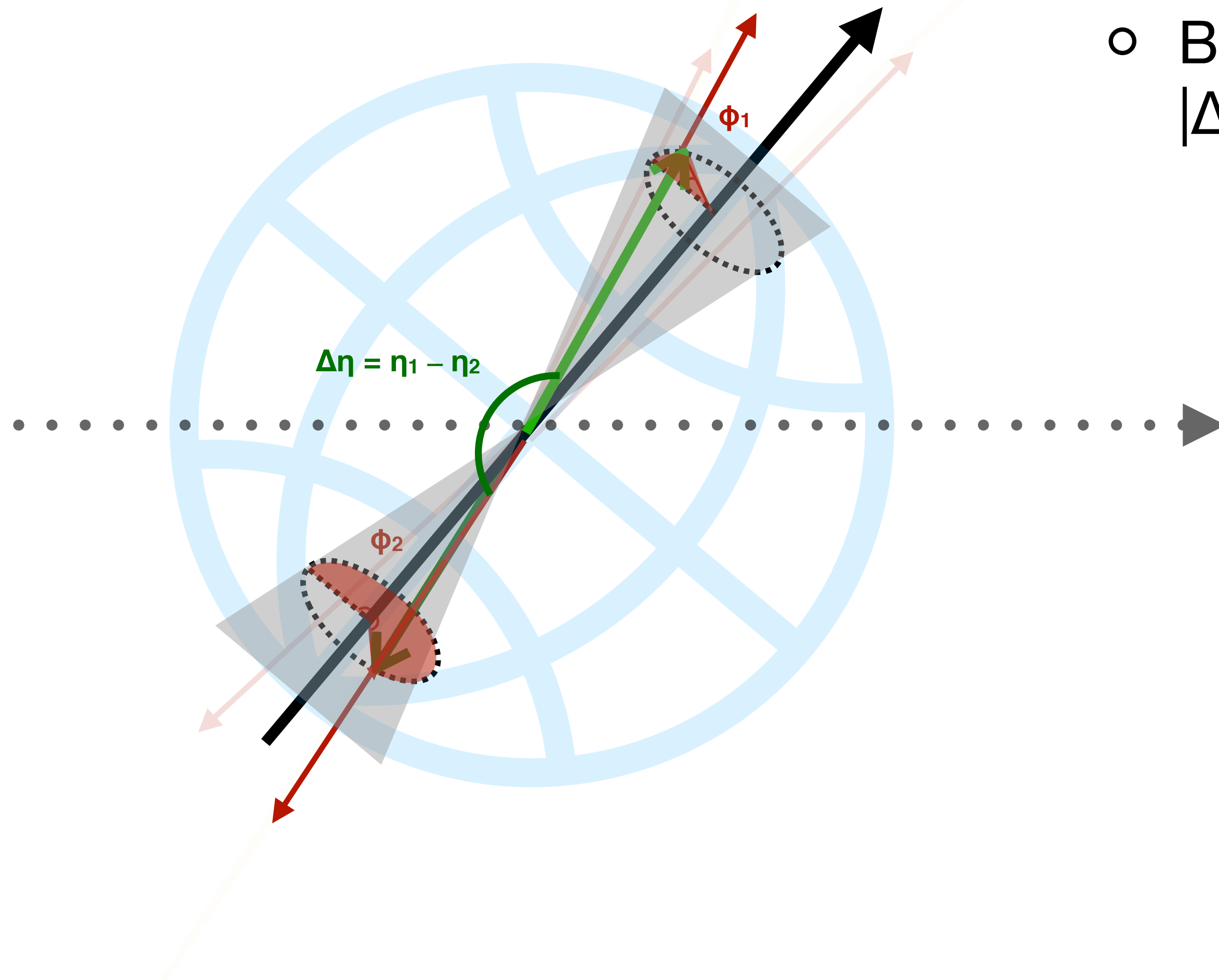
## A weakened jet correlation

- Intra-jet correlation of on-axis jets is diluted!



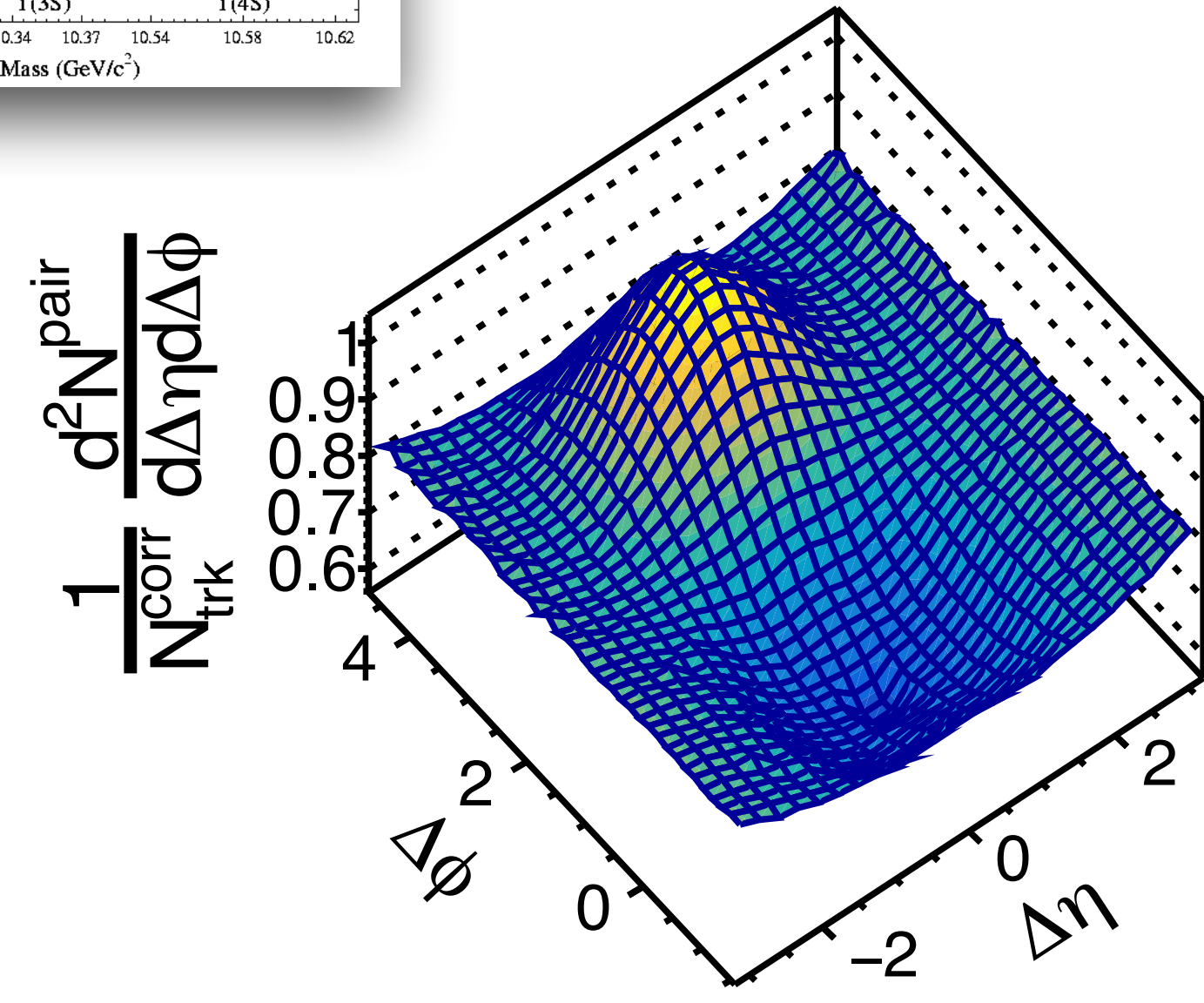
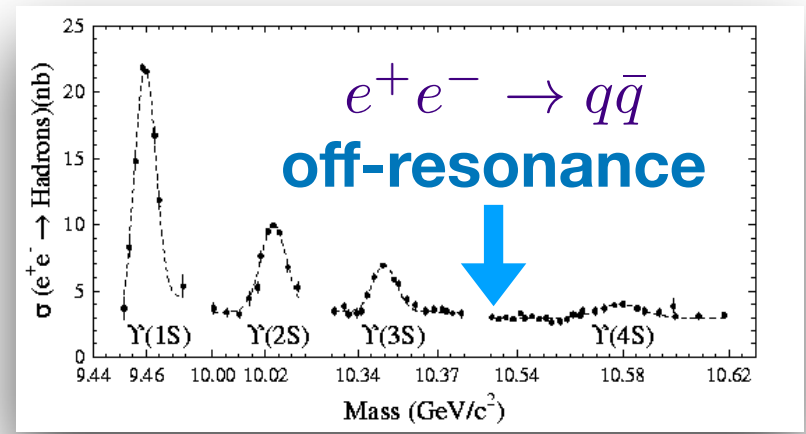
# A weakened jet correlation

- Intra-jet correlation of on-axis jets is diluted!
- Back-to-back-jet correlation is excluded at finite  $|\Delta\eta|$  region of interest

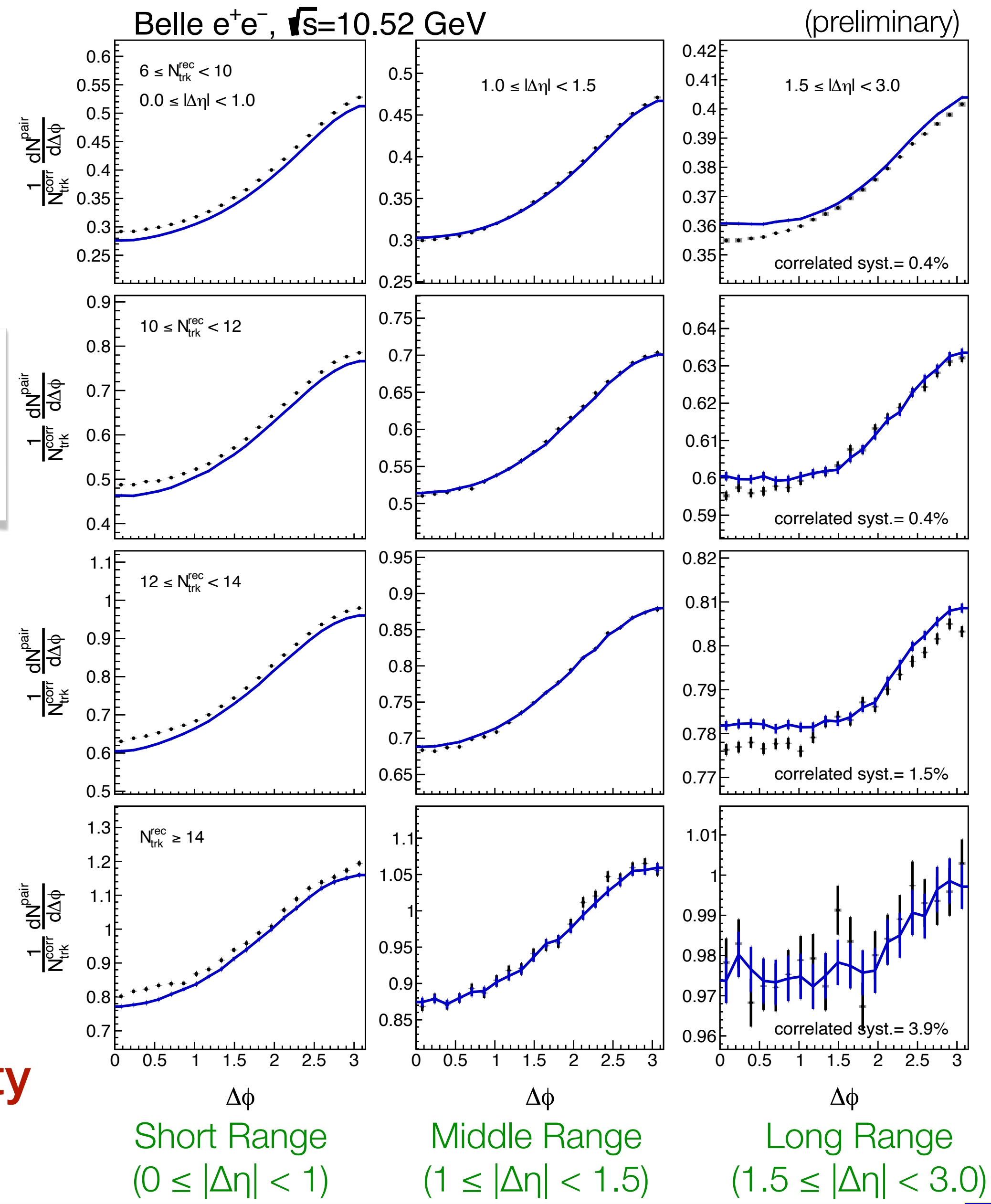
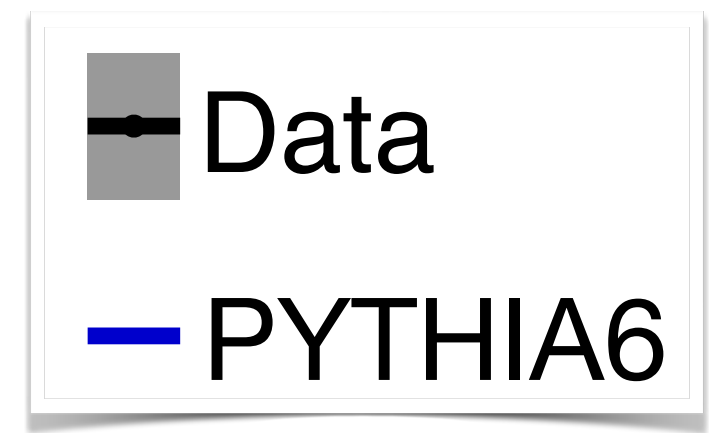




- Sizable origin-peak is lacking
- Qualitatively good agreement in correlation function shape btw data and MC



$$12 \leq N_{\text{trk}}^{\text{rec}} < 14$$

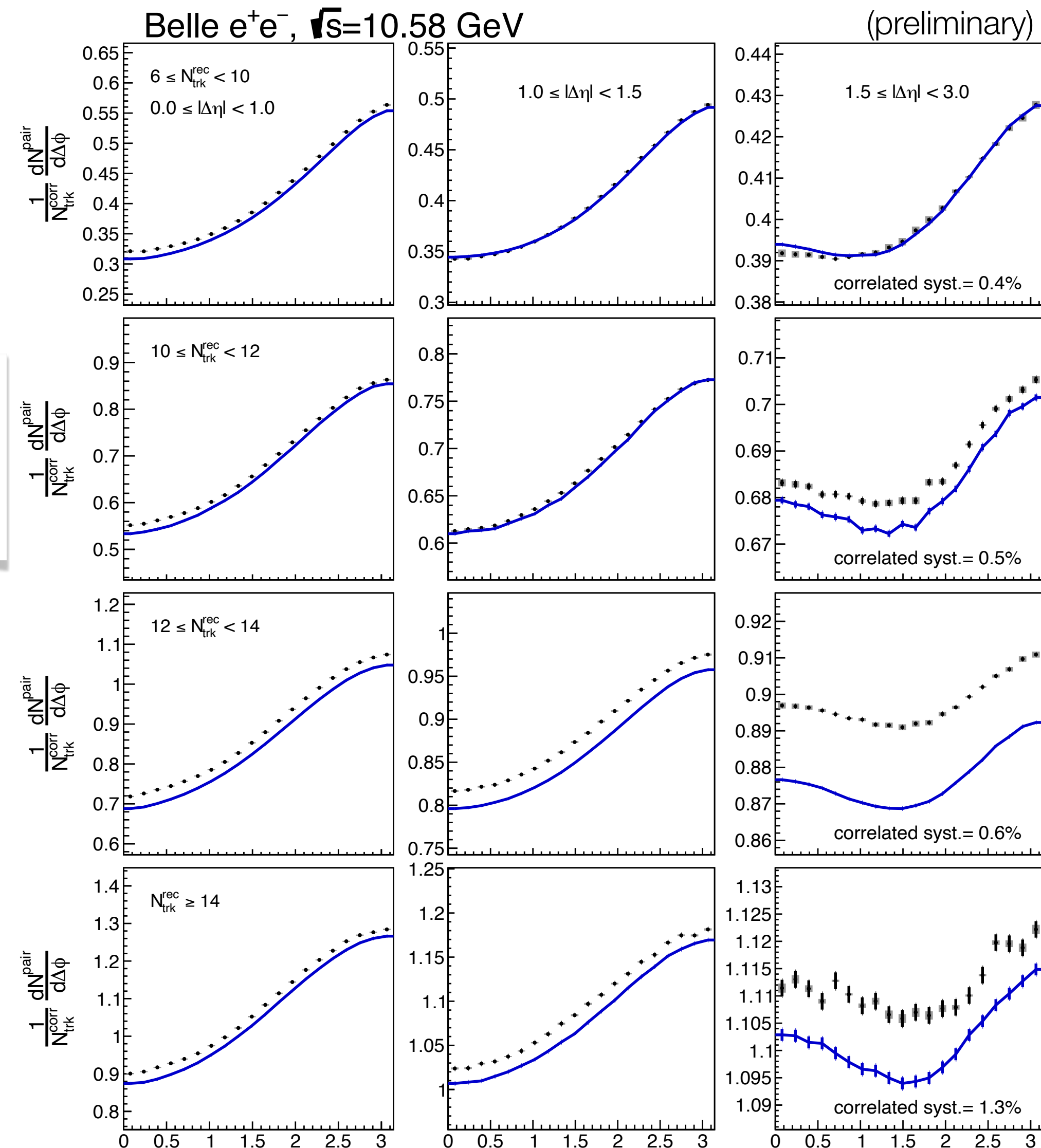
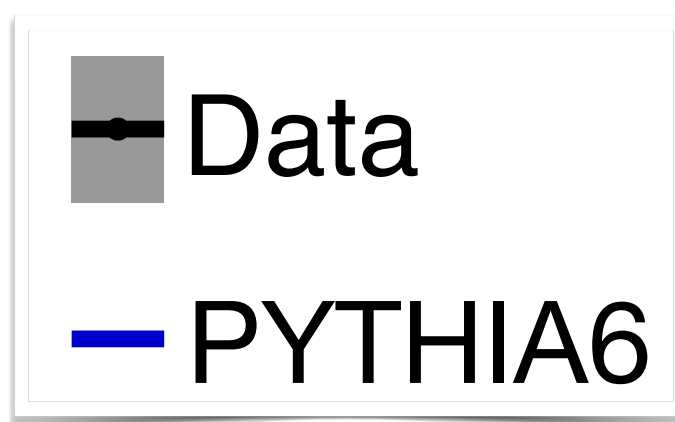


High-multiplicity

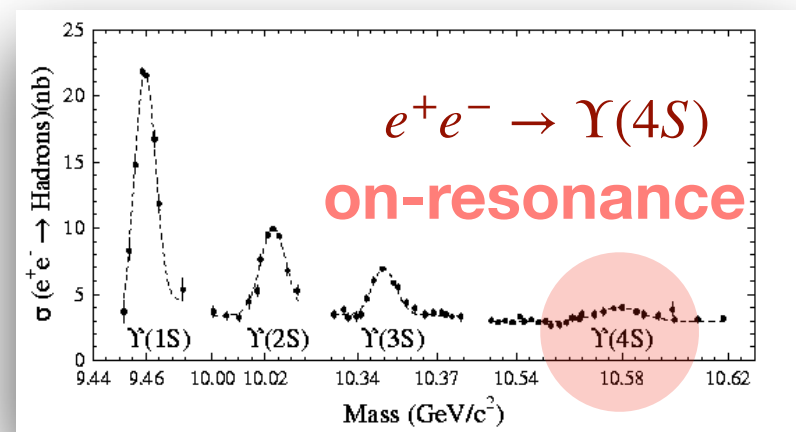
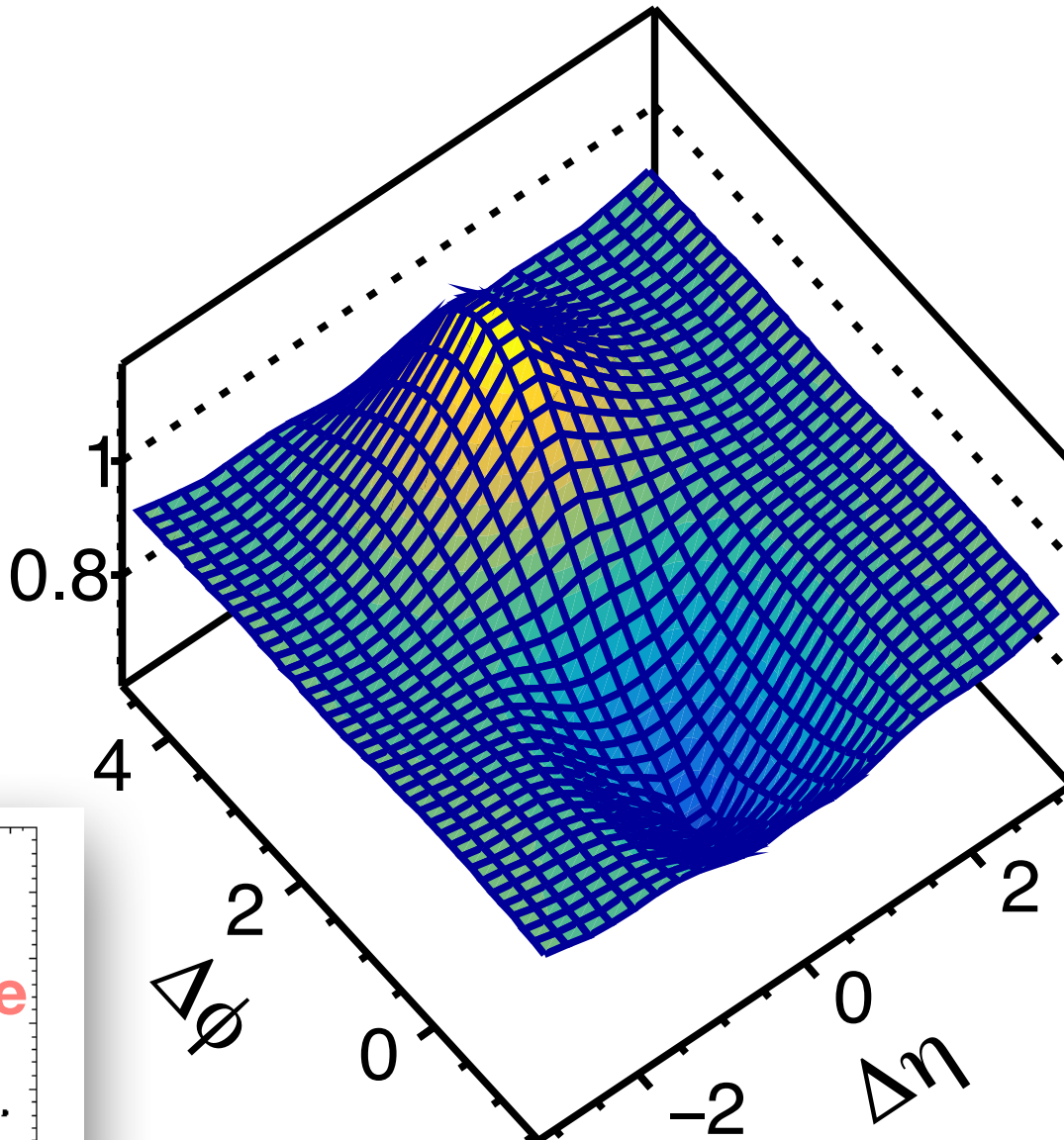
arXiv:2201.01694  
accepted by PRL



- Enhanced long-range near-side correlation, but does NOT resemble to typical ridge structure
- Similar enhancement seen in MC
- Up to 5% larger discrepancy seen in the correlation magnitude in the long-range region



$$\frac{1}{N_{\text{trk}}^{\text{corr}}} \frac{d^2 N^{\text{pair}}}{d\Delta\eta d\Delta\phi}$$



paper in preparation

$$12 \leq N_{\text{trk}}^{\text{rec}} < 14$$

High-multiplicity

Short Range ( $0 \leq |\Delta\eta| < 1$ ) Middle Range ( $1 \leq |\Delta\eta| < 1.5$ ) Long Range ( $1.5 \leq |\Delta\eta| < 3.0$ )

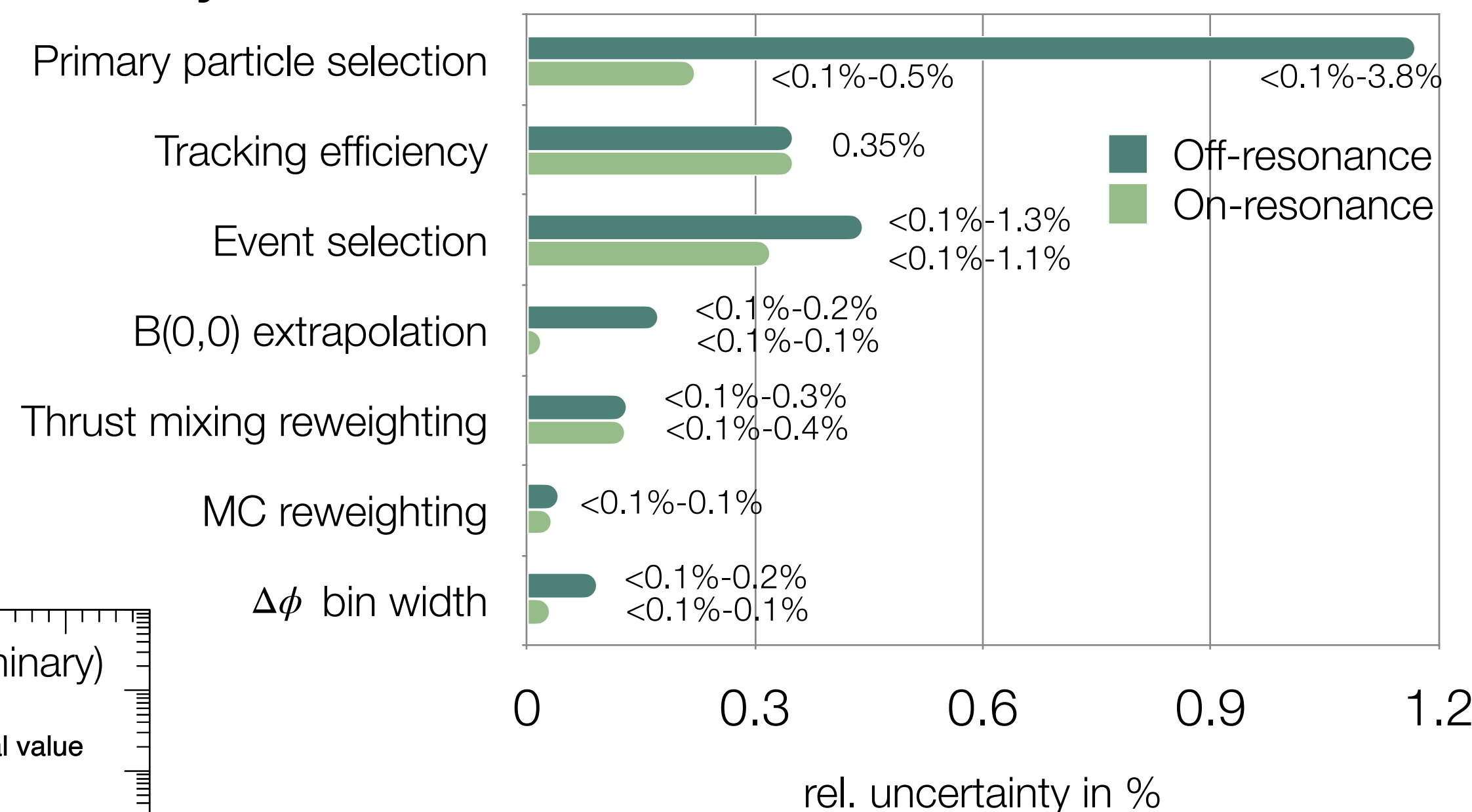




- Selections are the dominant systematics sources
- Beam axis analysis:  $>5\sigma$  exclusion of ridge signal

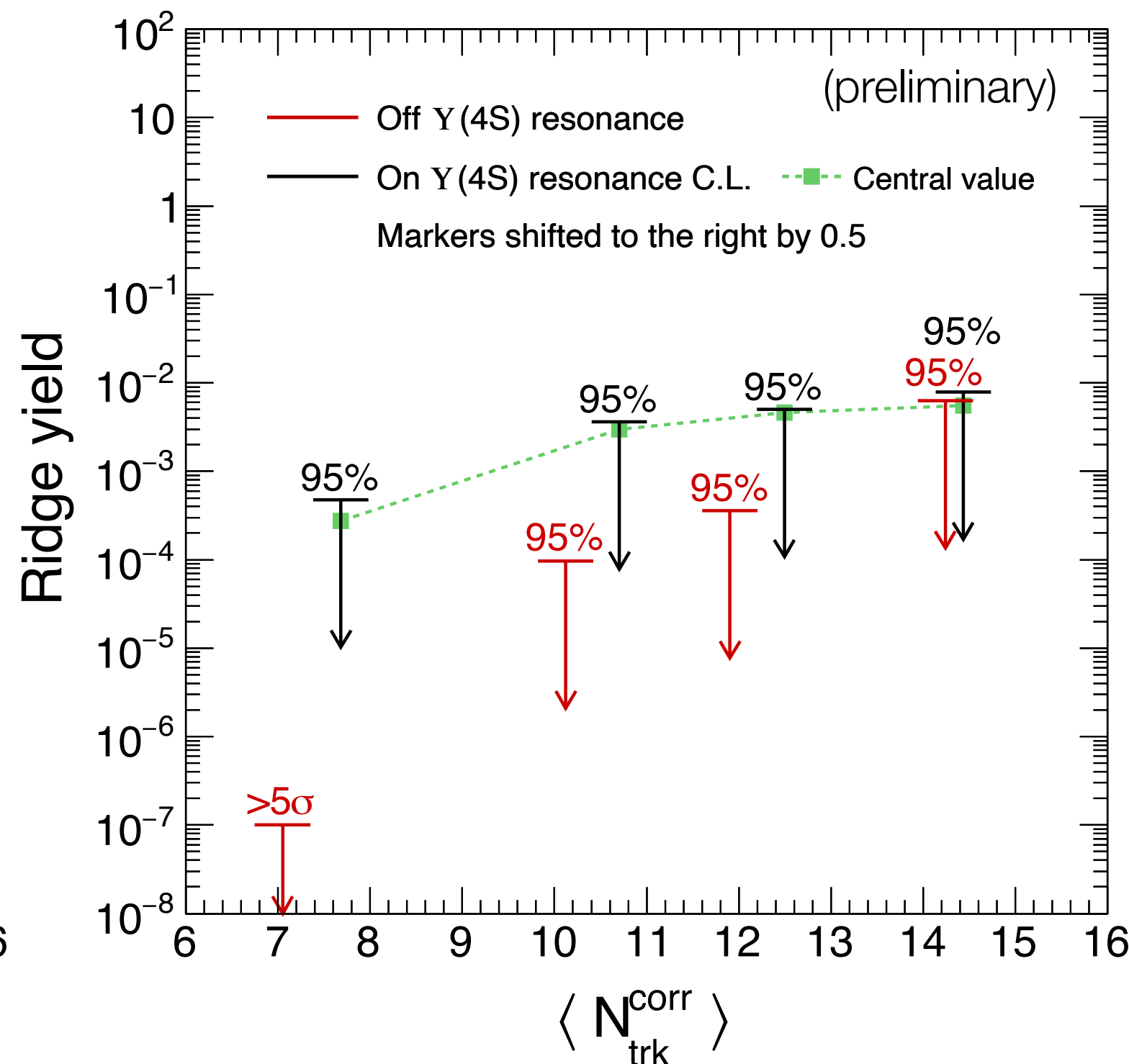
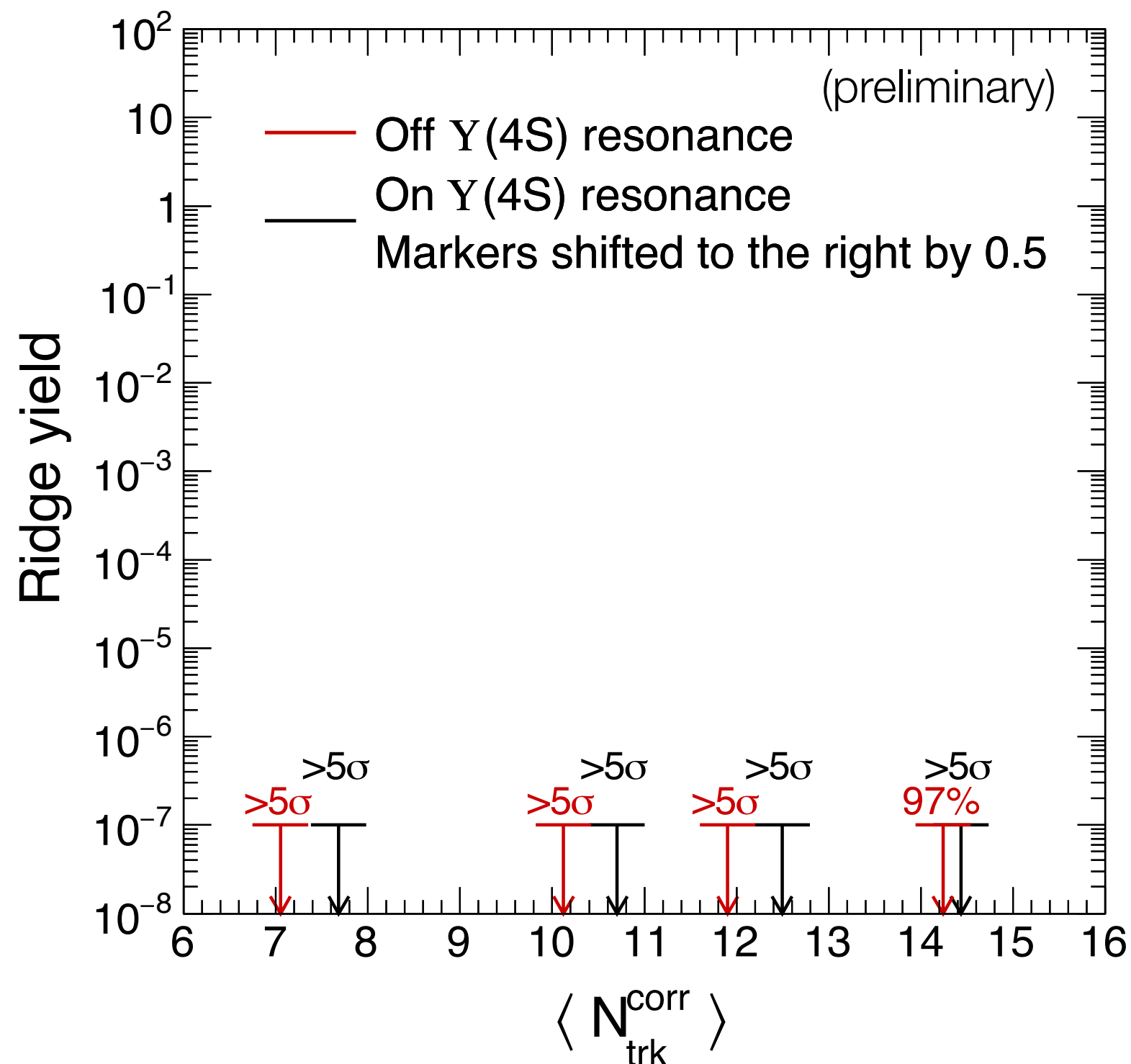
### Systematics

### Thrust axis



### Beam axis

### Thrust axis



- Thrust axis analysis:
  - Off-resonance: no significant ridge signal, but C.L. in high-multiplicity bins are limited by statistics
  - On-resonance: low-scale long-range near-side enhancement

Low-multiplicity



High-multiplicity

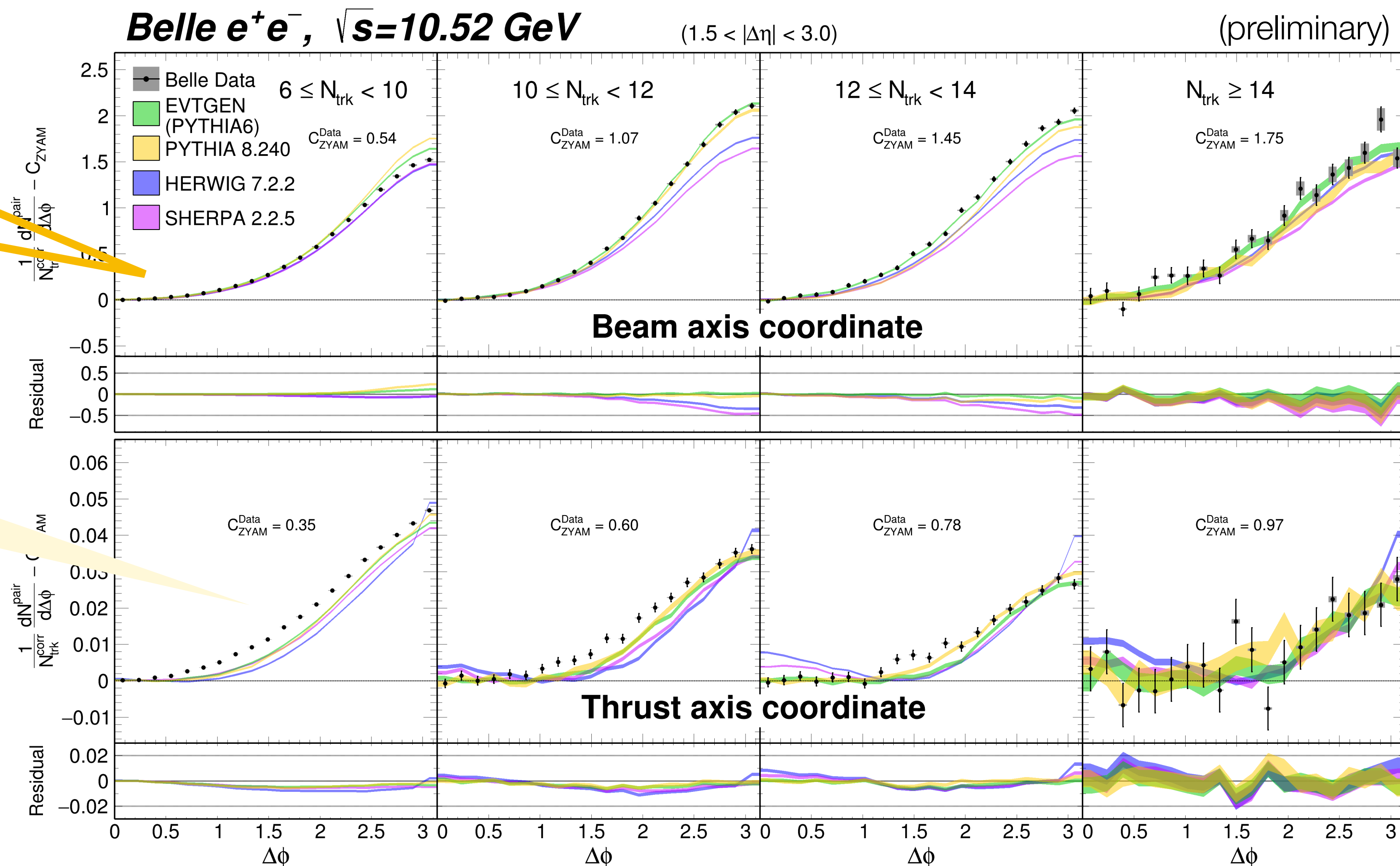
○ MCs consistent with data in near side

○ Discrepancies in the away-side magnitude

Differences in data & MC correlation shapes

○ PYTHIA6 agrees better with data than HERWIG & SHERPA

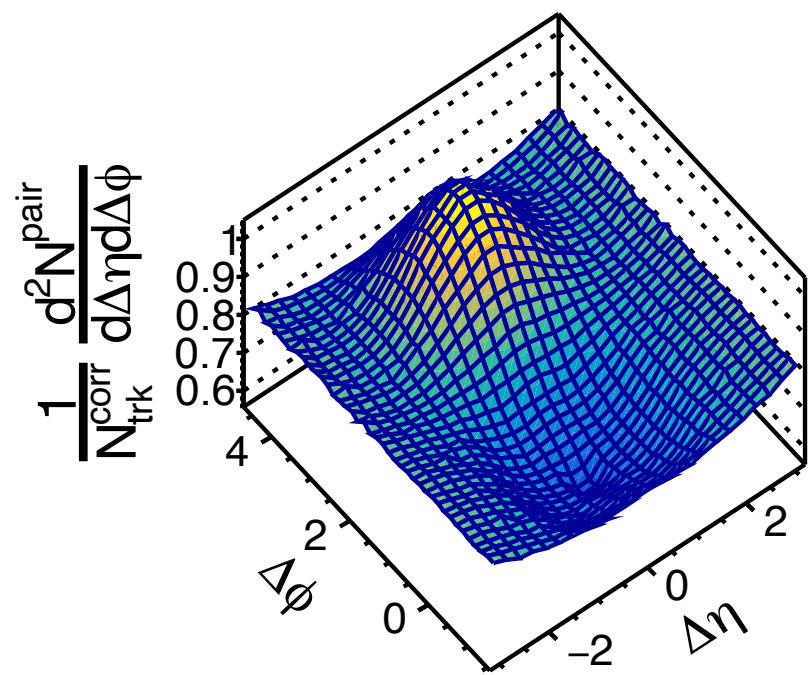
○ PYTHIA8 has similar behavior as PYTHIA6



on-resonance see backup

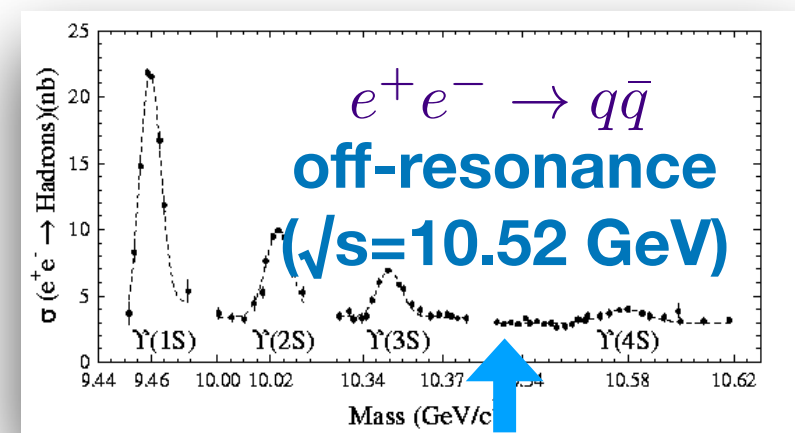


# Lack of origin-peak jet correlation



- Sharp origin-peak correlation is recovered as  $\sqrt{s}$  goes high
- Thrust-axis analysis: from null to significant intra-jet correlation!

\* Demonstrated with  $6 \leq N_{\text{trk}} < 10$   
 This phenomenon is seen in all multiplicity ranges



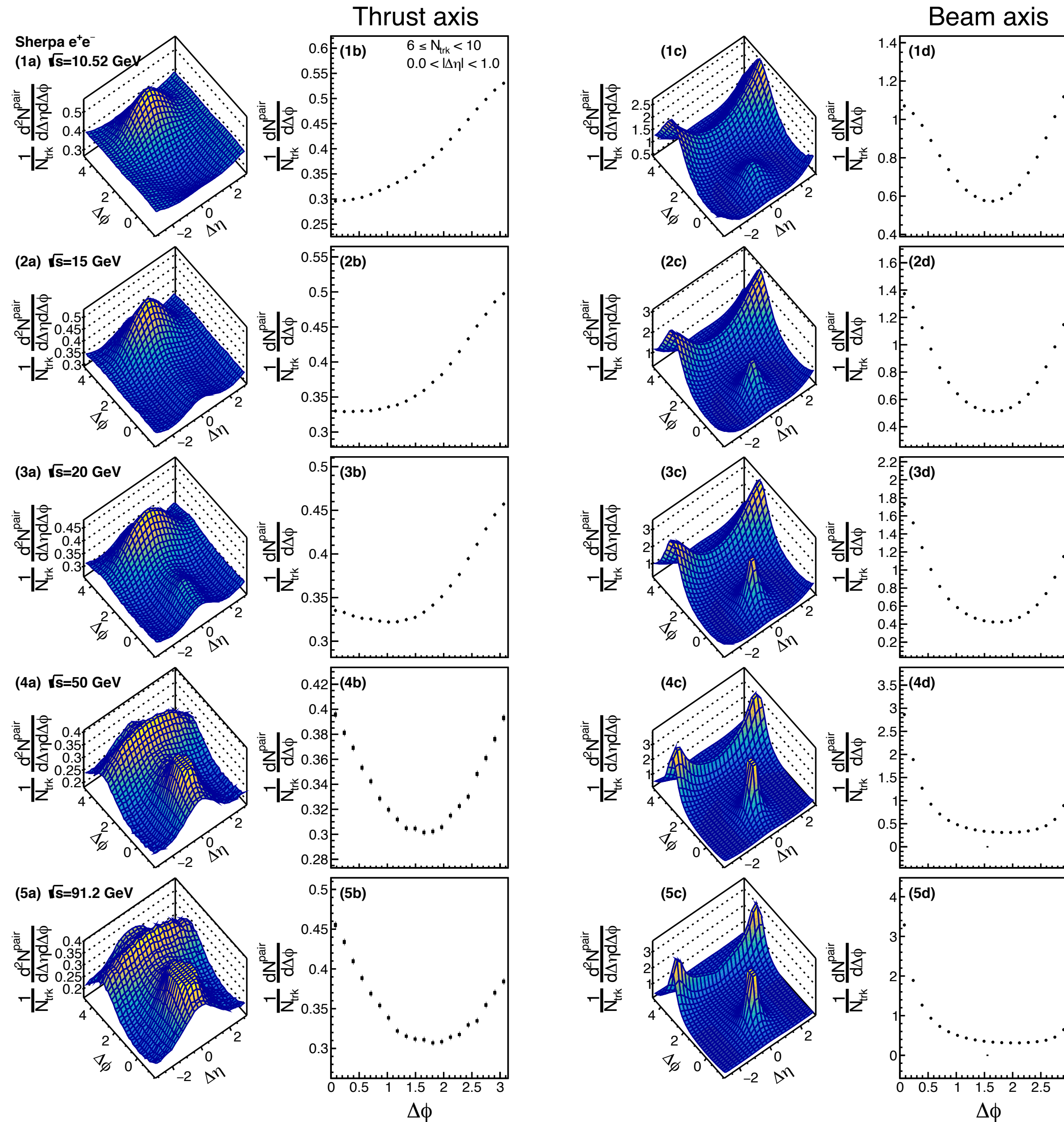
$\sqrt{s} = 15 \text{ GeV}$

$\sqrt{s} = 20 \text{ GeV}$

$\sqrt{s} = 50 \text{ GeV}$

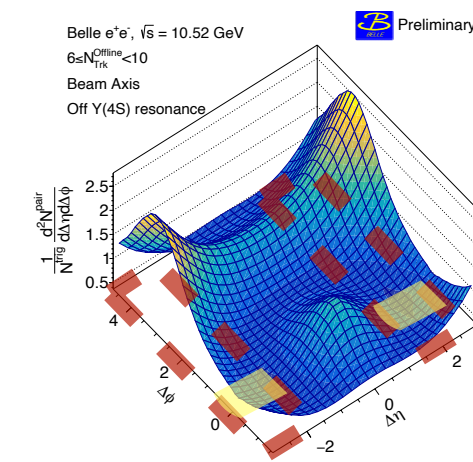
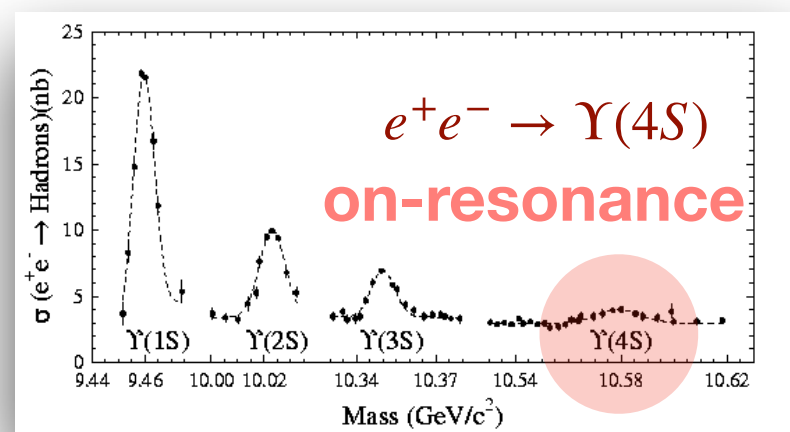
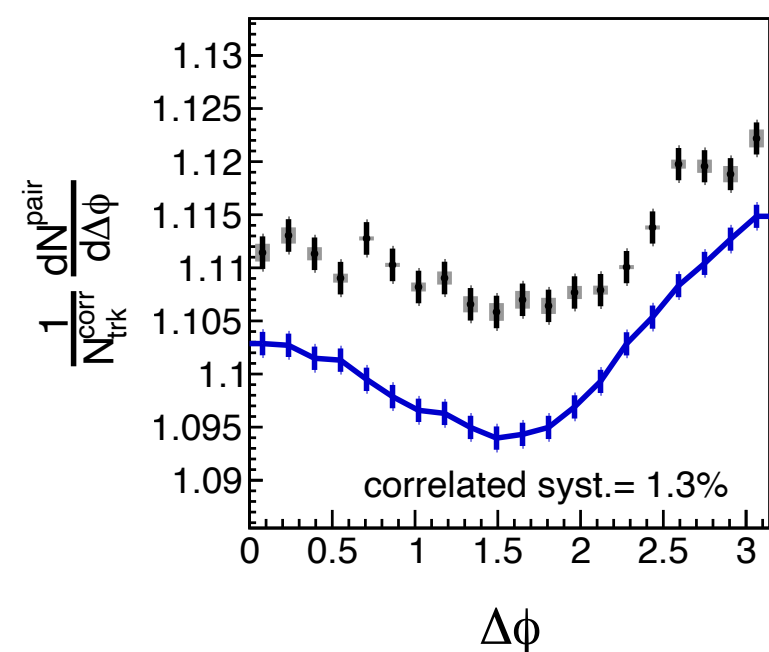
$\sqrt{s} = 91.2 \text{ GeV}$   
 (LEP1 energy)

Larger origin peak correlation is found

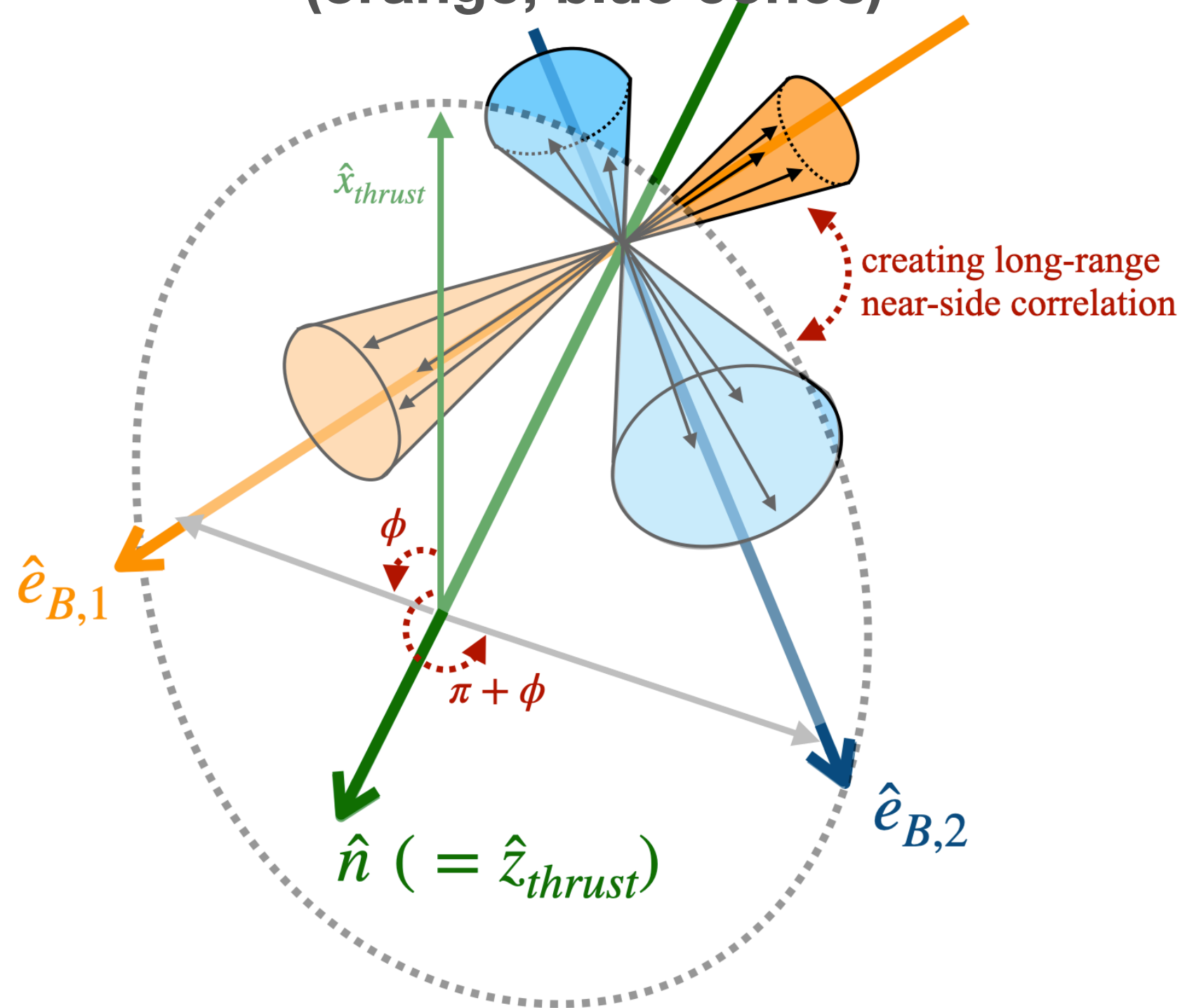




# Long-range near-side enhancement in on-resonance sample



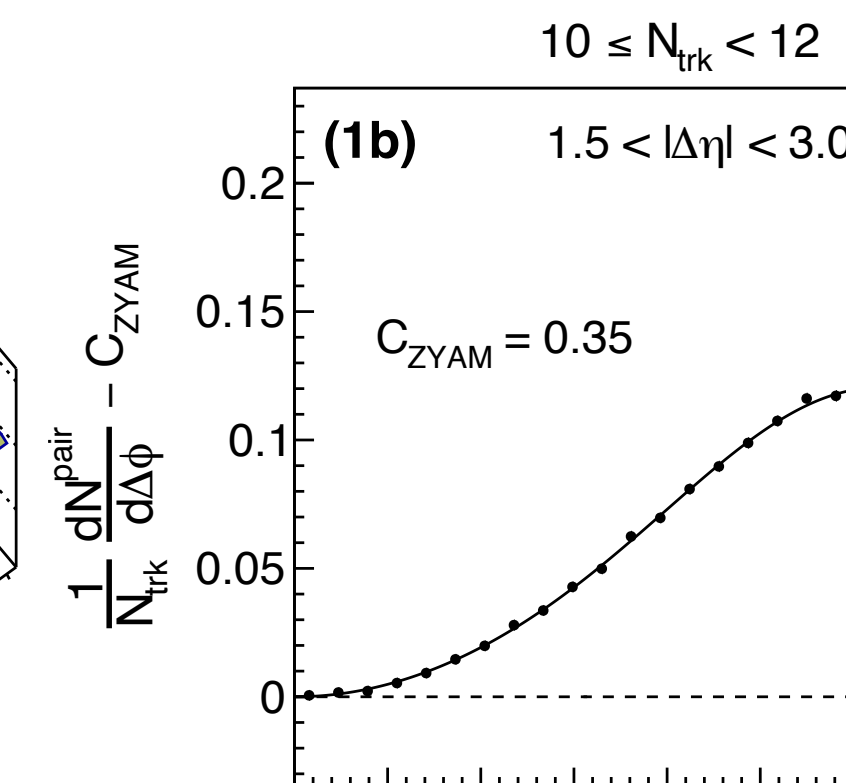
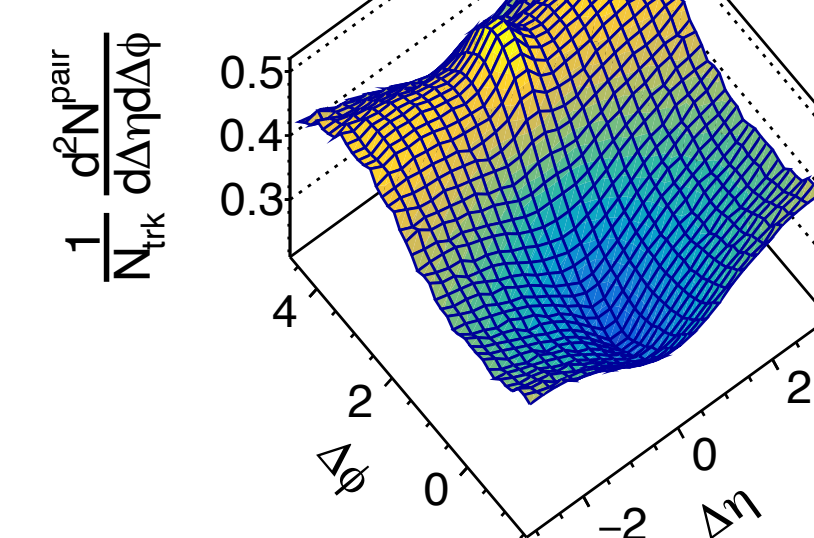
Schematic plot for  $\Upsilon(4S) \rightarrow B\bar{B}$  (orange, blue cones)



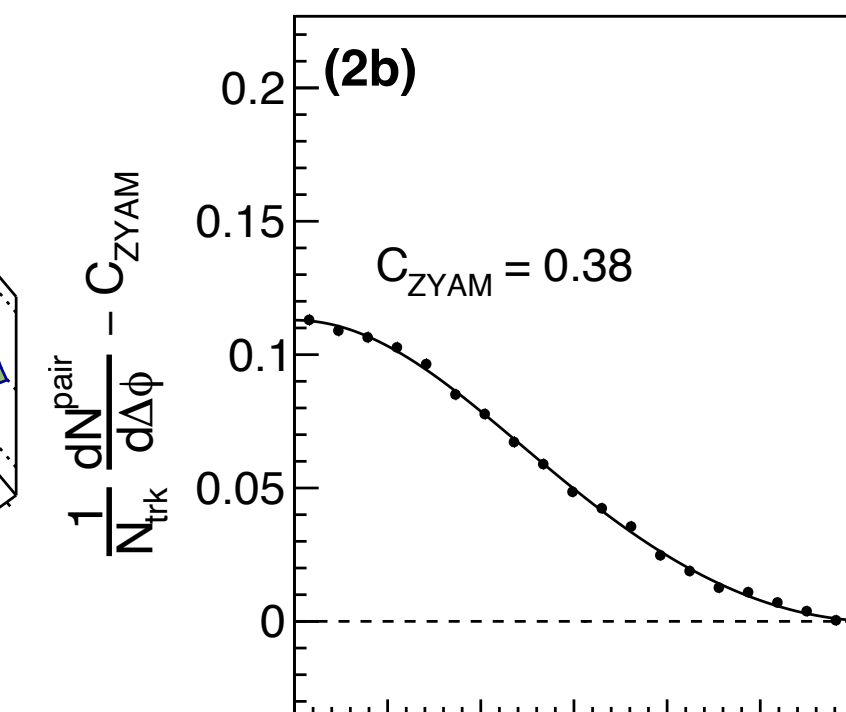
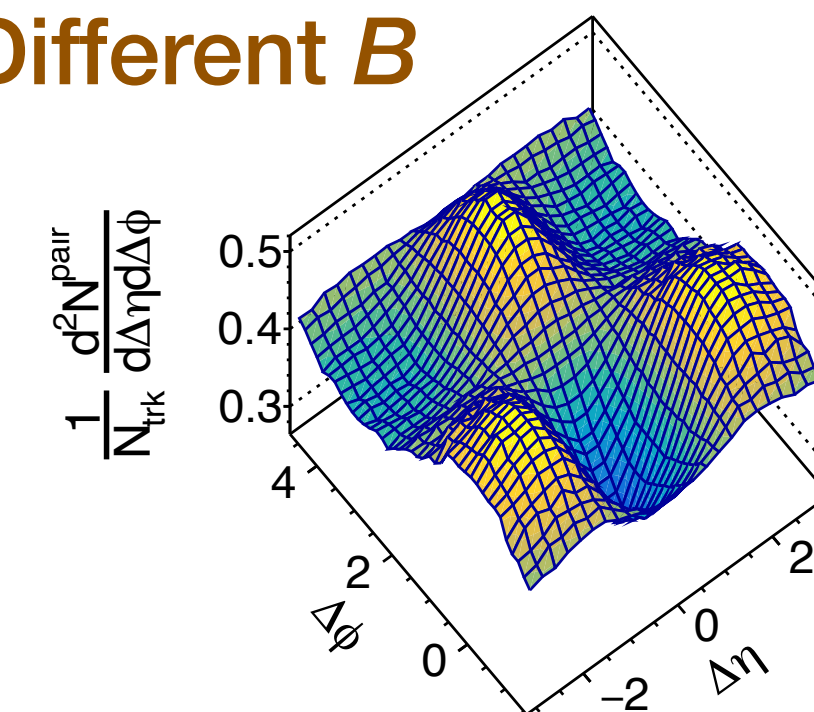
- Two  $B$ -meson decays: special event topology thrust axis alignment
- Toy sample pairing uncorrelated  $B$ 's from different events shows similar enhancement!

Belle  $e^+e^-$ ,  $\sqrt{s} = 10.58 \text{ GeV}$

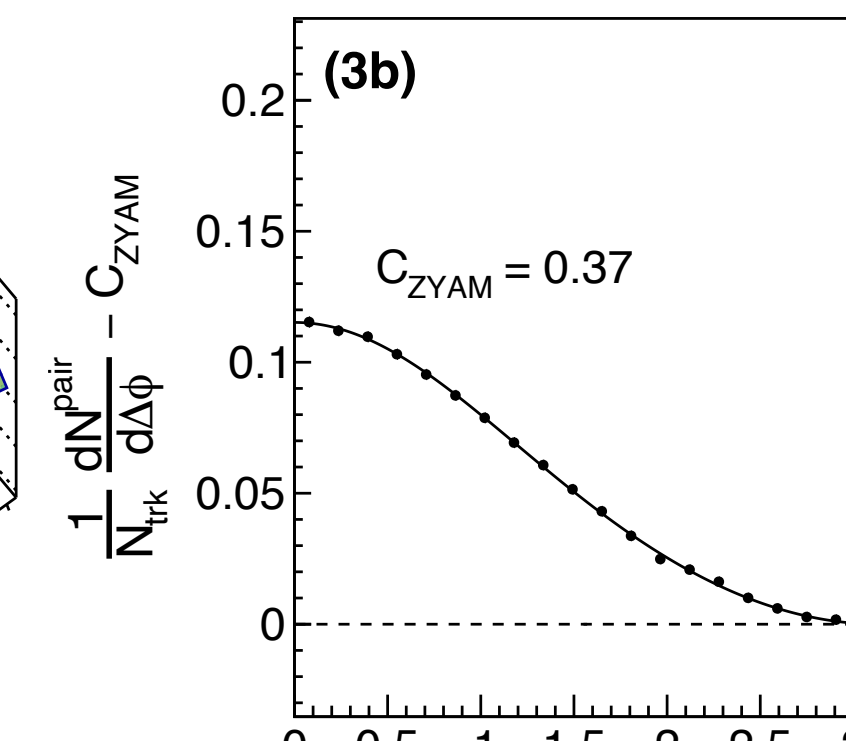
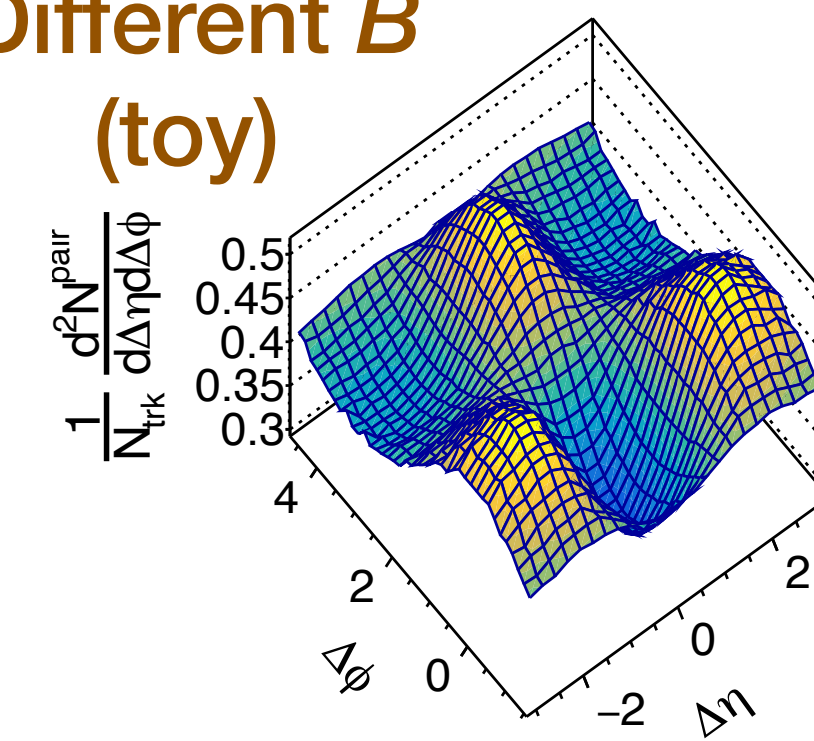
Same  $B$



Different  $B$

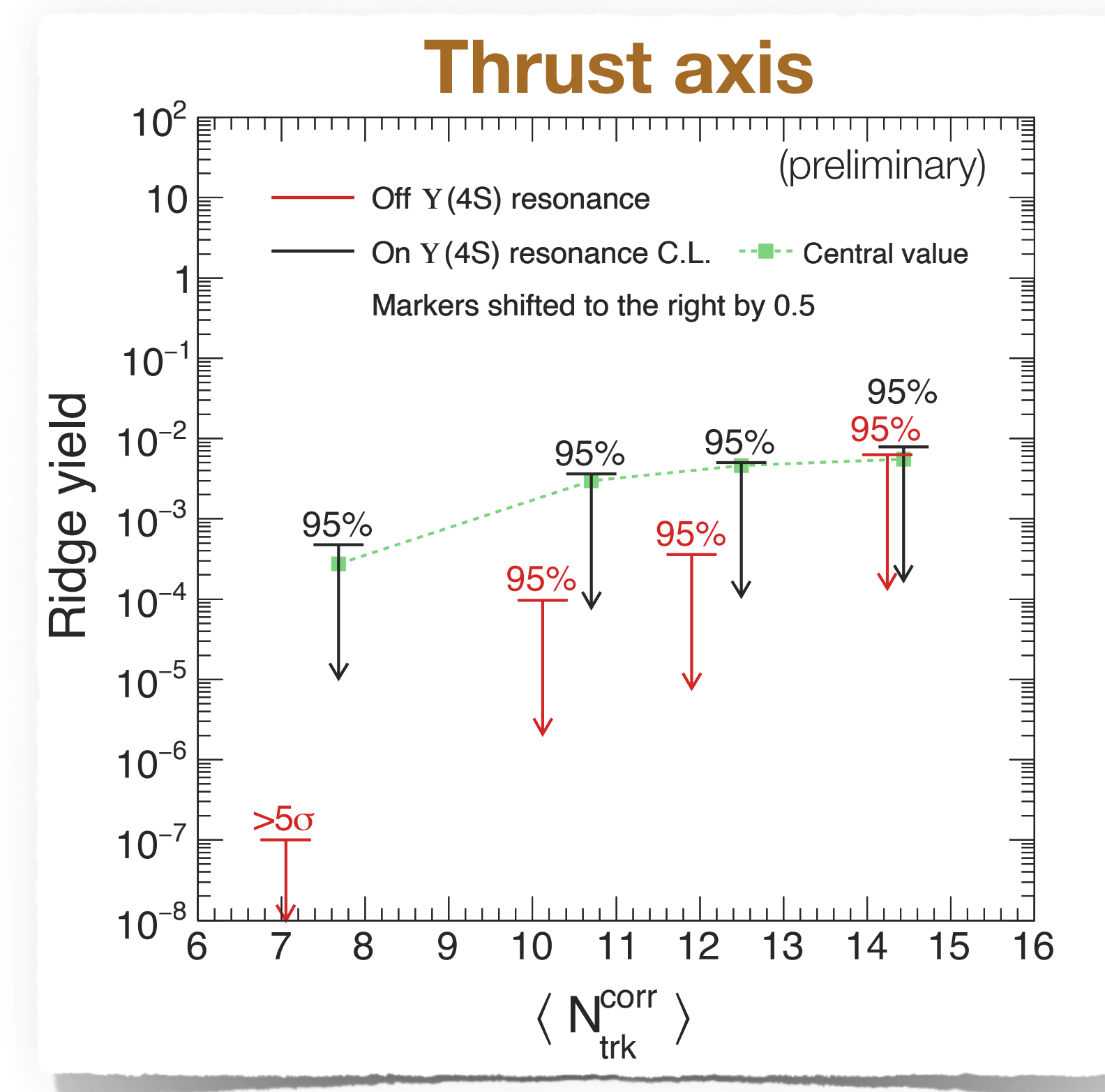


Different  $B$  (toy)





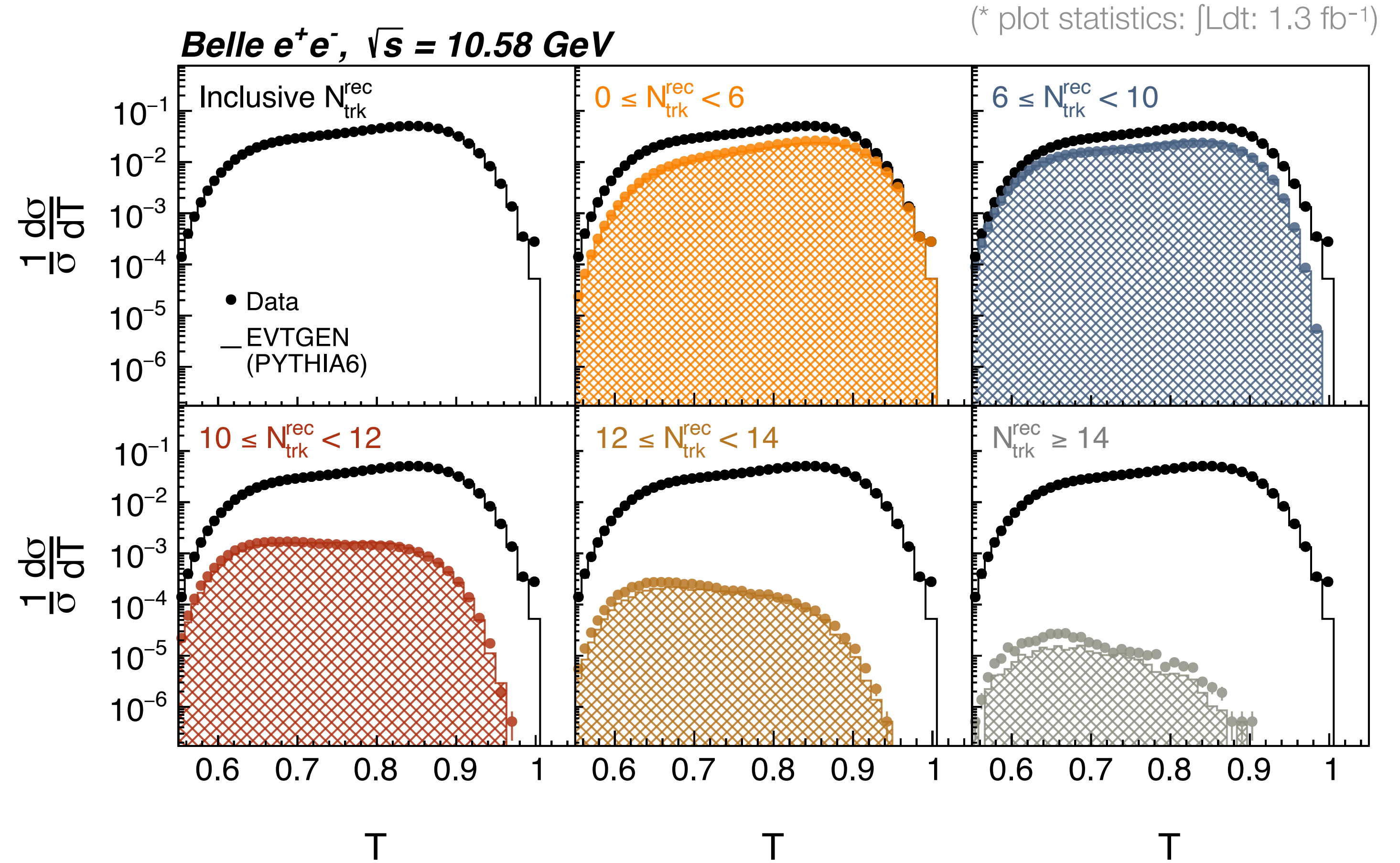
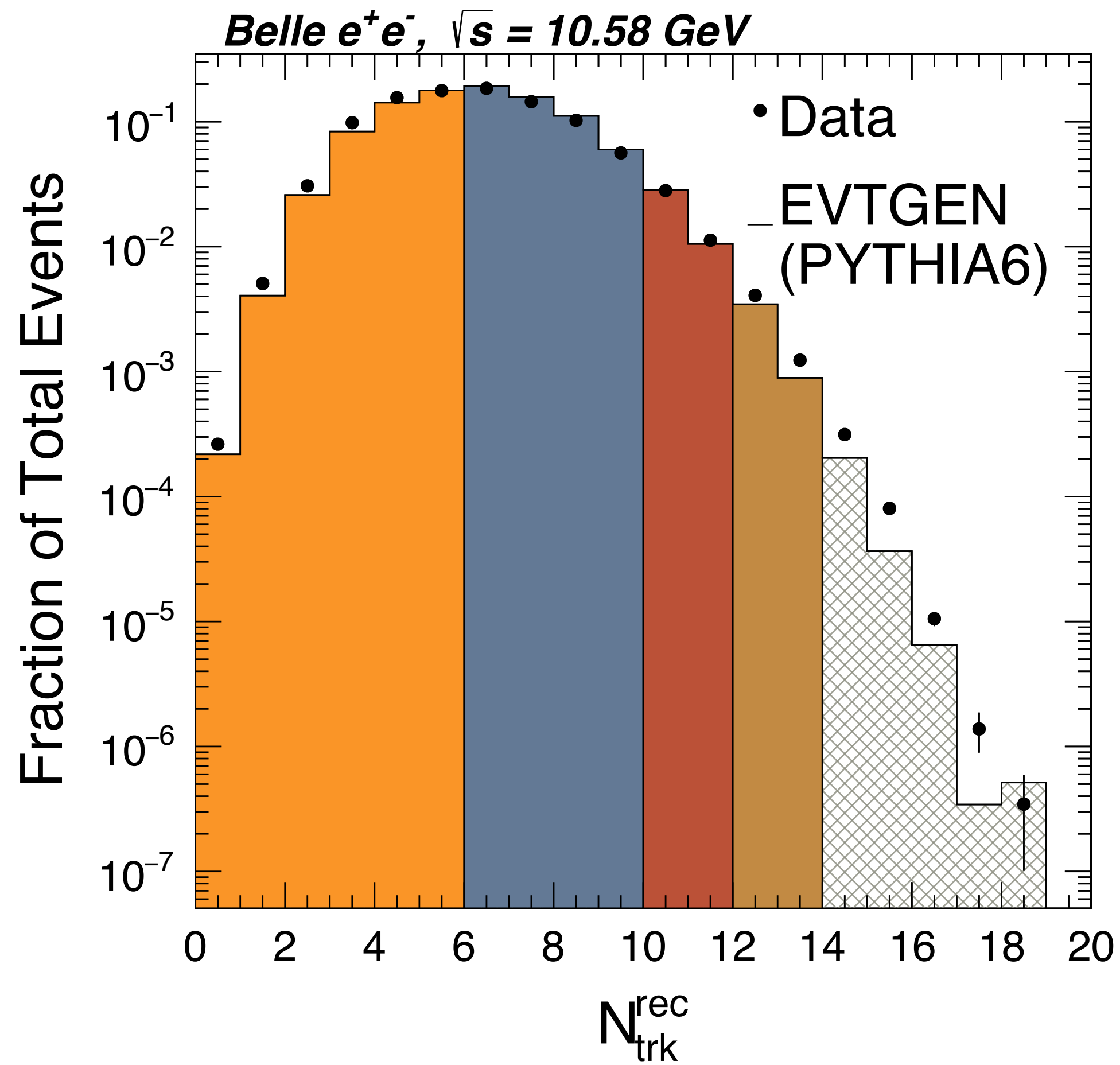
- First results of two-particle correlations measured in both beam axis and thrust axis coordinates at Belle
- Beam axis analysis, strong exclusion of ridge signals
- Thrust axis analysis:
  - Off-resonance: no significant ridge signal, origin-peak jet correlation scales with collision energy
  - On-resonance: low-scale long-range near-side enhancement due to special decay topology of  $\Upsilon(4S) \rightarrow B\bar{B}$  system, observed also on MC
- PYTHIA is in better agreement with data than SHERPA & HERWIG



# Backup



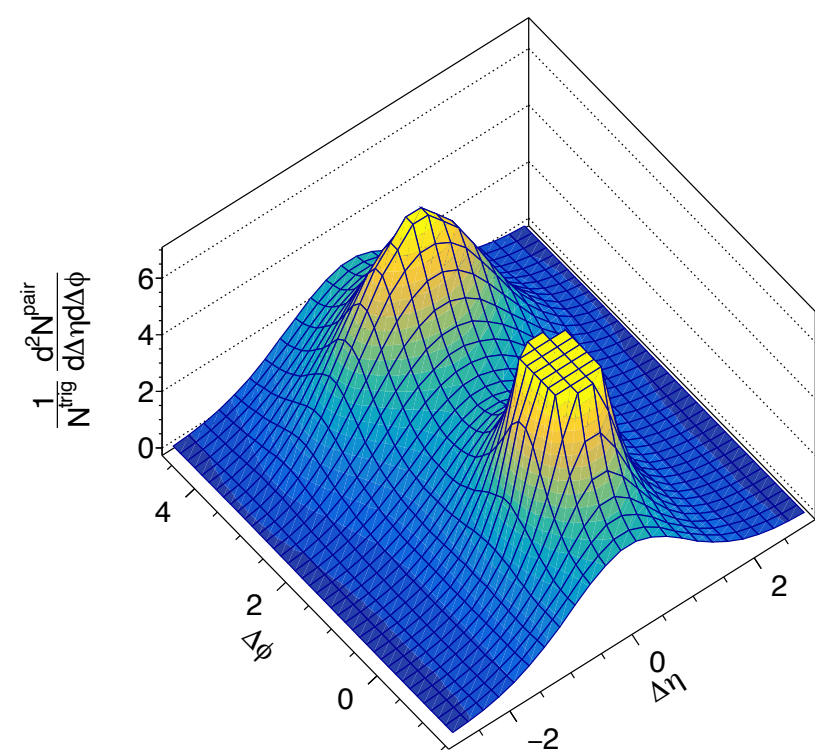
Charged particles	
Primary tracks	<ul style="list-style-type: none"> <li>• [reconstructed] the distance in the transverse plane of the decay vertex from the primary vertex <math>&lt; 1</math> cm</li> <li>• [MC-truth] decay promptly or from particles with proper lifetime <math>\tau \leq 1</math> cm/<math>c</math></li> </ul>
Acceptance	$17^\circ \leq \theta \leq 150^\circ$
High quality tracks	$p_T \geq 0.2$ GeV
Impact parameter	$ \Delta r  < 2,  \Delta z  < 5$
Duplicate track removal	veto the softer track of a low-momentum pair ( $p_T < 0.4$ GeV) travelling with a small open angle $\delta$ : <ol style="list-style-type: none"> <li>1. same-sign charges with <math>\cos \delta &gt; 0.95</math></li> <li>2. opposite-sign charges with <math>\cos \delta &lt; -0.95</math></li> </ol>
Photon conversion veto	veto track pairs which can form common vertices ( $V^0$ objects) with <ol style="list-style-type: none"> <li>1. <math>z</math> distance between two tracks <math>&lt; 10</math> cm</li> <li>2. reconstructed <math>V^0</math>'s mass <math>&lt; 0.25</math> GeV</li> <li>3. decay-vertex radius <math>&gt; 1.5</math> cm</li> </ol>
Neutral particles (for thrust calculation)	
Cluster selection	No direct track-matching and tracks matched at cluster edges
Acceptance	$17^\circ \leq \theta \leq 150^\circ$
Energy cut	Forward endcap: $E < 0.10$ GeV Backward endcap: $E < 0.15$ GeV Barrel: $E < 0.05$ GeV





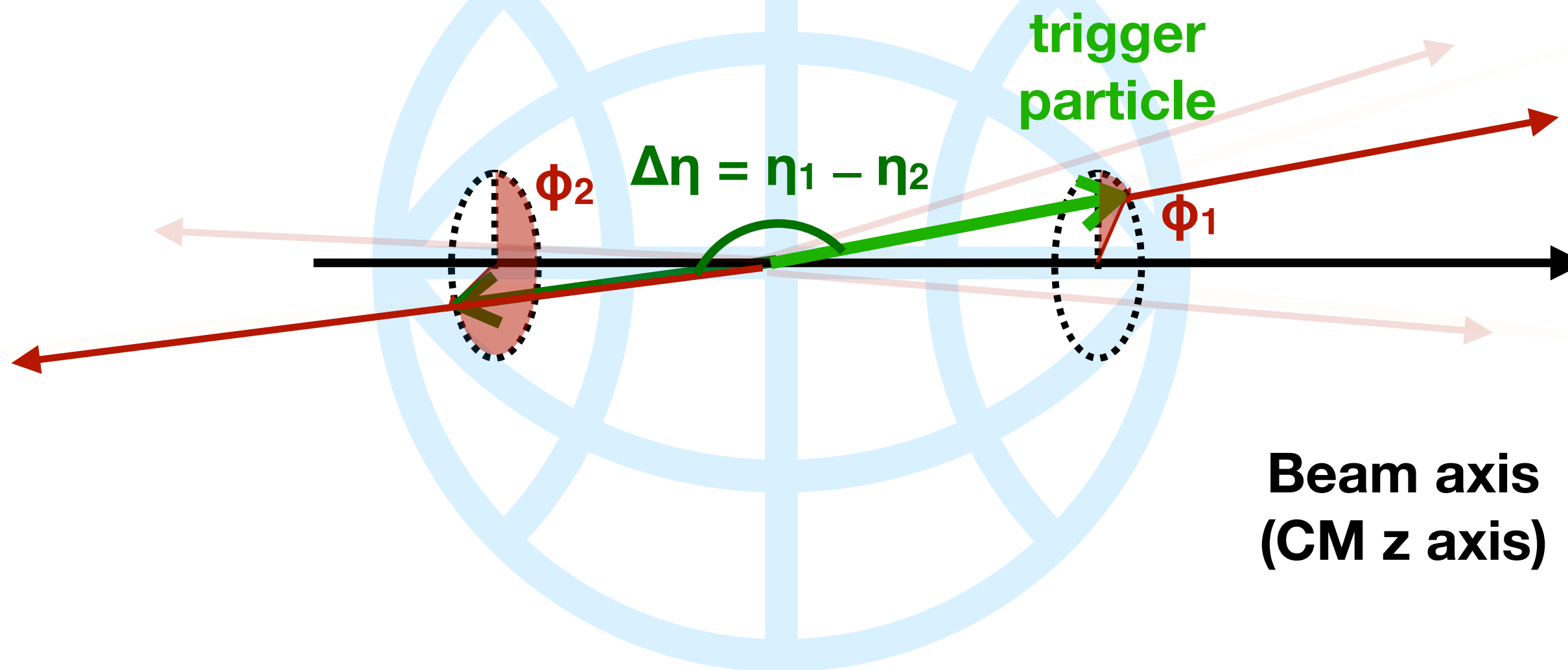
## Signal

(raw correlation function)



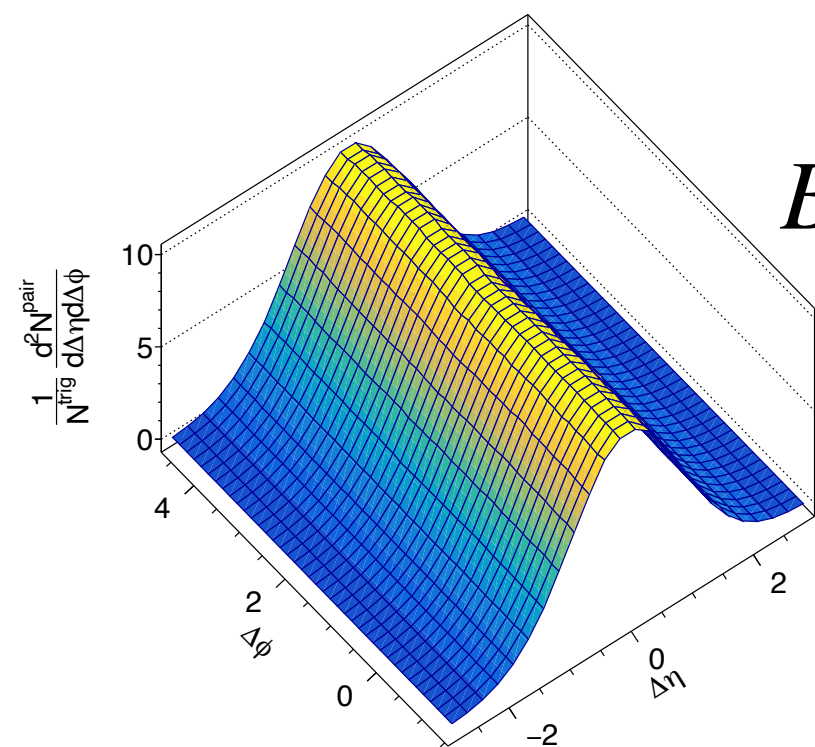
$$S(\Delta\eta, \Delta\phi) = \frac{1}{N_{\text{trk}}^{\text{corr}}} \frac{d^2 N^{\text{same}}}{d\Delta\eta d\Delta\phi}$$

Track pairs' angular difference in  $\eta$  (pseudorapidity),  $\phi$  (azimuthal angle)



## Background

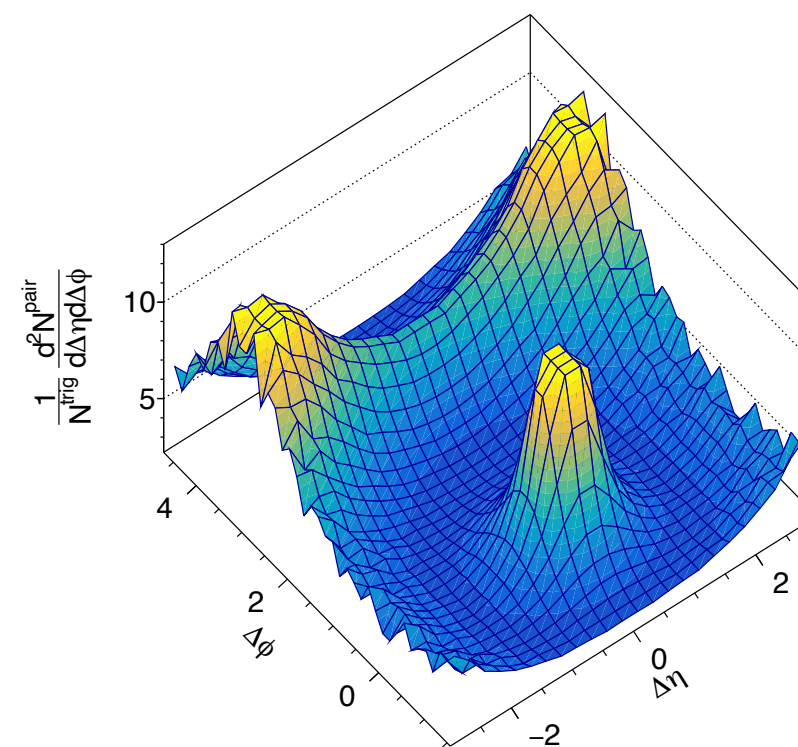
(accounting for baseline of random pairing)



$$B(\Delta\eta, \Delta\phi) = \frac{1}{N_{\text{trk}}^{\text{corr}}} \frac{d^2 N^{\text{mix}}}{d\Delta\eta d\Delta\phi}$$

## Two-particle correlation function

(per-trigger-particle associated yield)



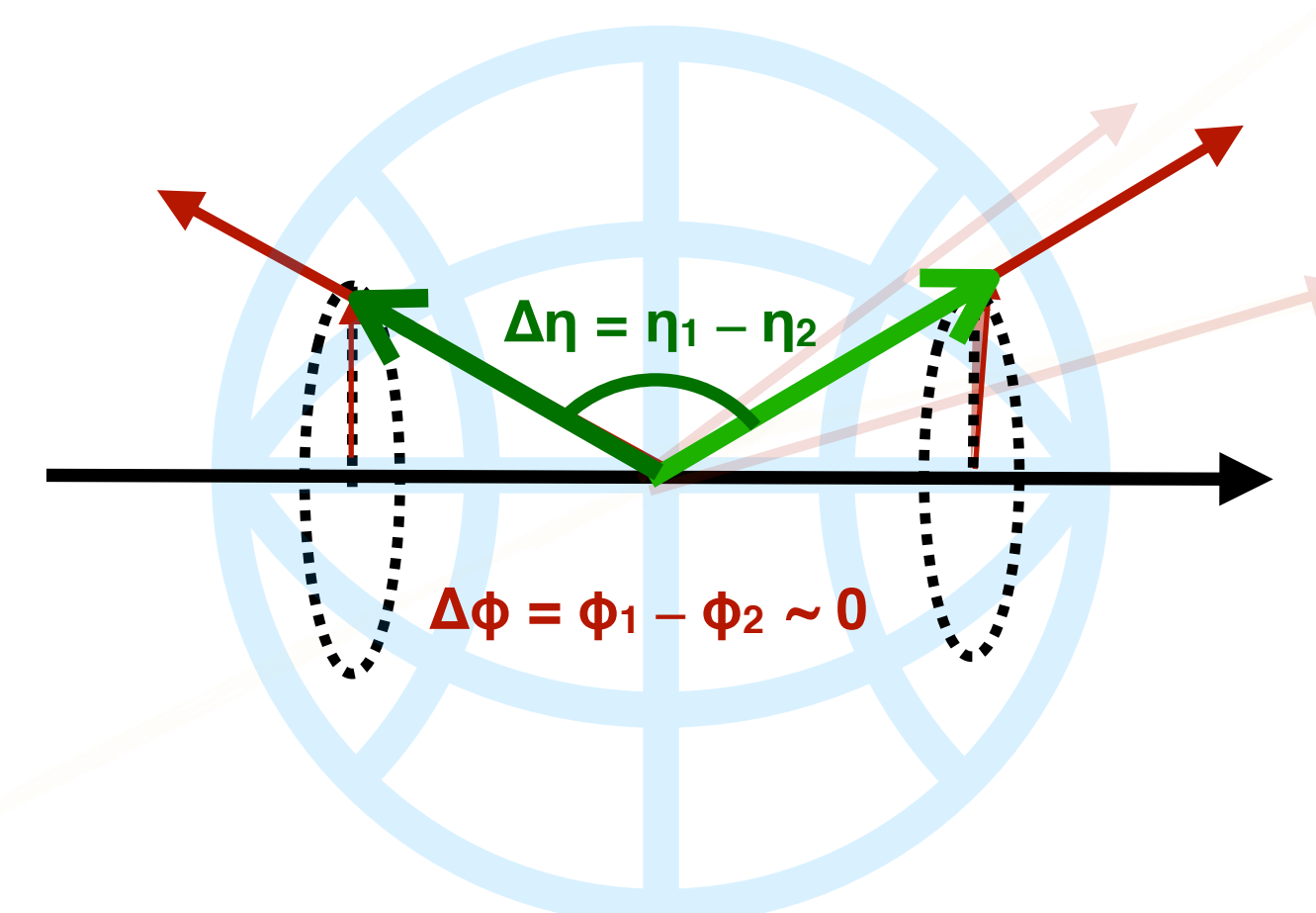
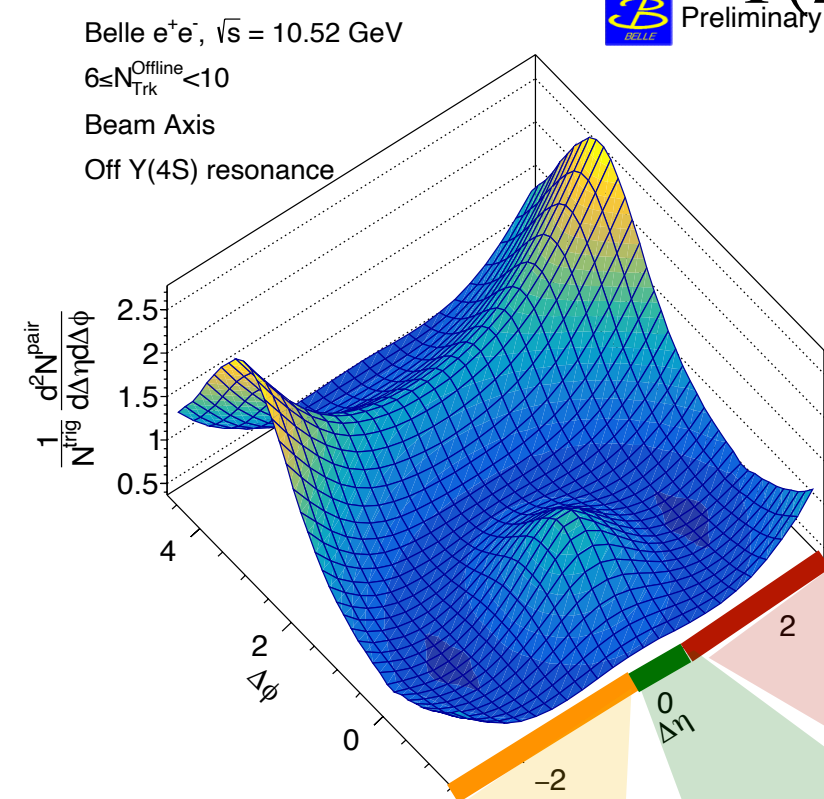
$$\frac{1}{N_{\text{trk}}^{\text{corr}}} \frac{d^2 N^{\text{pair}}}{d\Delta\eta d\Delta\phi} = B(0,0) \times \frac{S(\Delta\eta, \Delta\phi)}{B(\Delta\eta, \Delta\phi)}$$

Two-particle correlation function  
(per-trigger-particle associated yield)

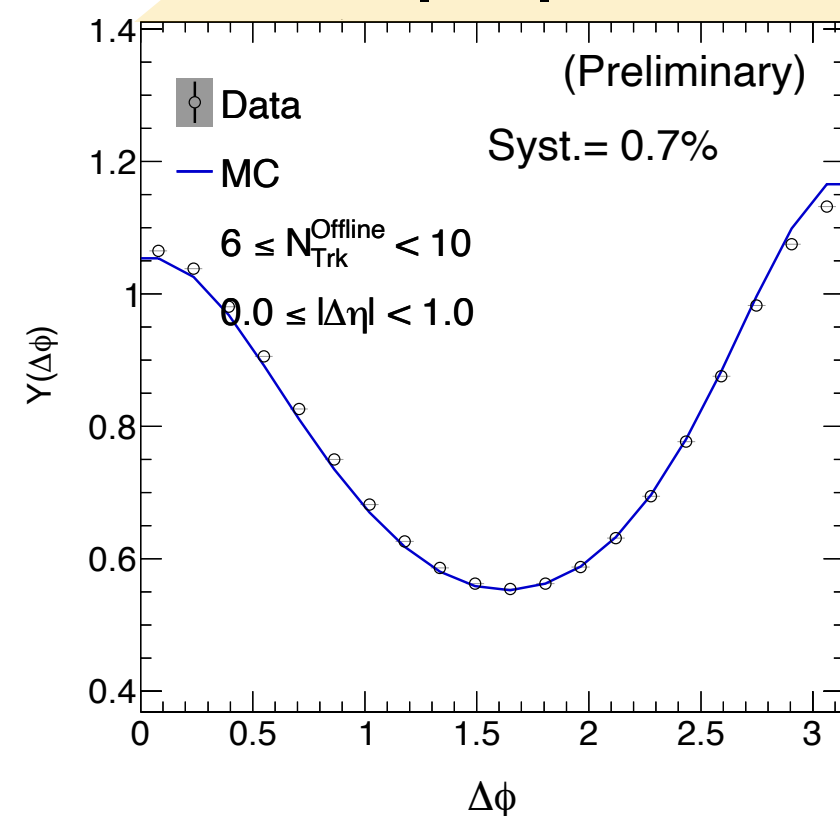
$$\frac{1}{N_{\text{trig}}} \frac{d^2 N^{\text{pair}}}{d\Delta\eta d\Delta\phi}$$

Associated yield vs.  $\Delta\phi$

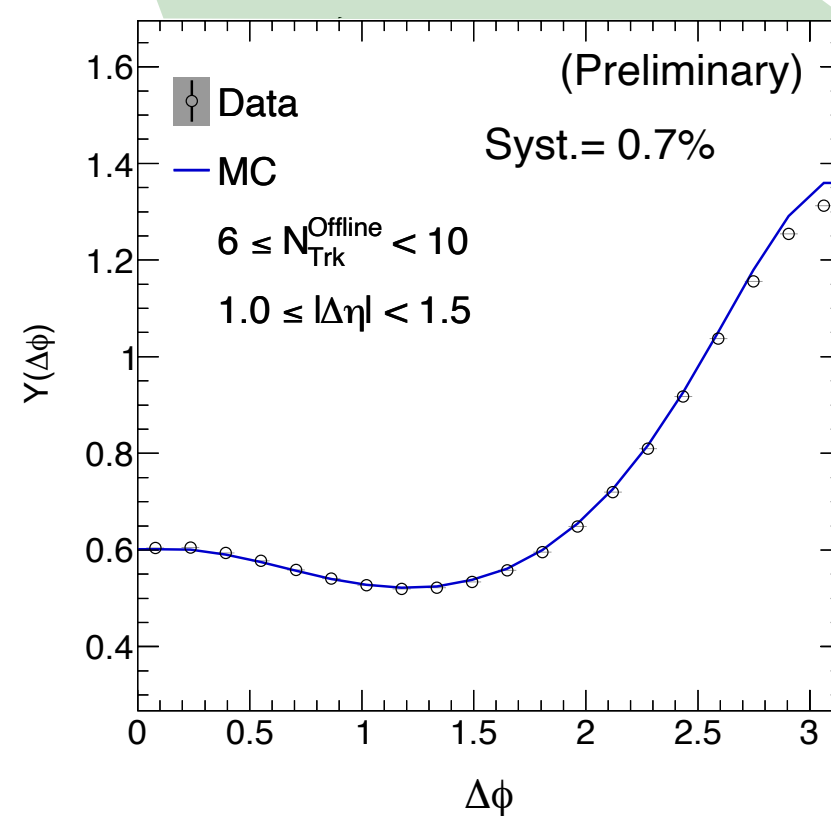
$$Y(\Delta\phi) = \frac{1}{N_{\text{trig}}} \frac{dN^{\text{pair}}}{d\Delta\phi} = \frac{1}{\Delta\eta_{\text{max}} - \Delta\eta_{\text{min}}} \int_{\Delta\eta_{\text{min}}}^{\Delta\eta_{\text{max}}} \frac{1}{N_{\text{trig}}} \frac{d^2 N^{\text{pair}}}{d\Delta\eta d\Delta\phi} d\Delta\eta$$



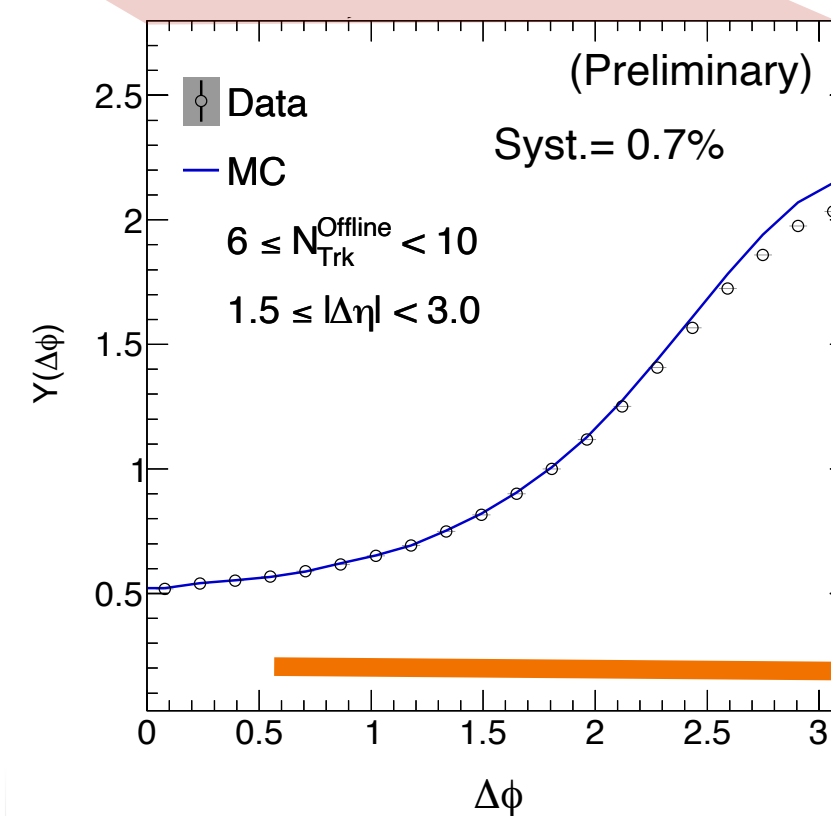
**Short Range**  
( $0 \leq |\Delta\eta| < 1$ )



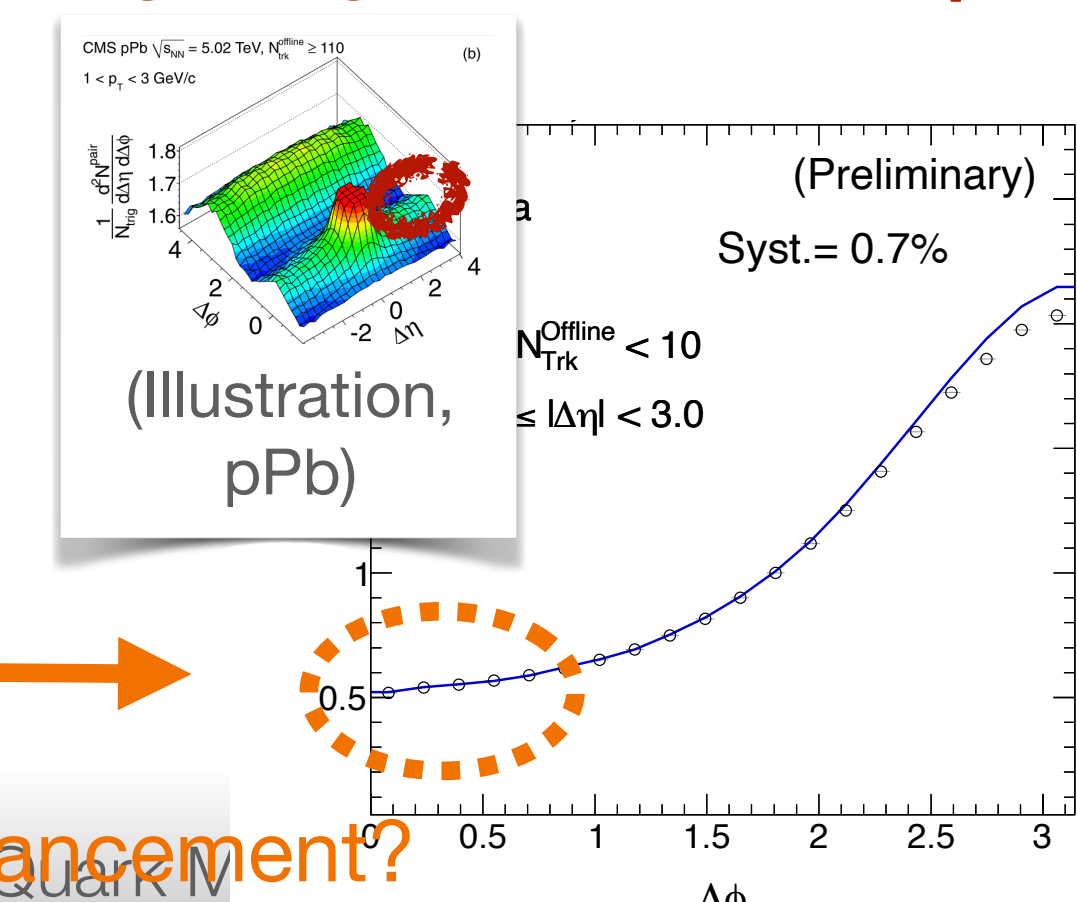
**Middle Range**  
( $1 \leq |\Delta\eta| < 1.5$ )



**Long Range**  
( $1.5 \leq |\Delta\eta| < 3.0$ )



**Ridge Signal**  
(long-range, near-side ( $\Delta\phi \sim 0$ ))



special enhancement?

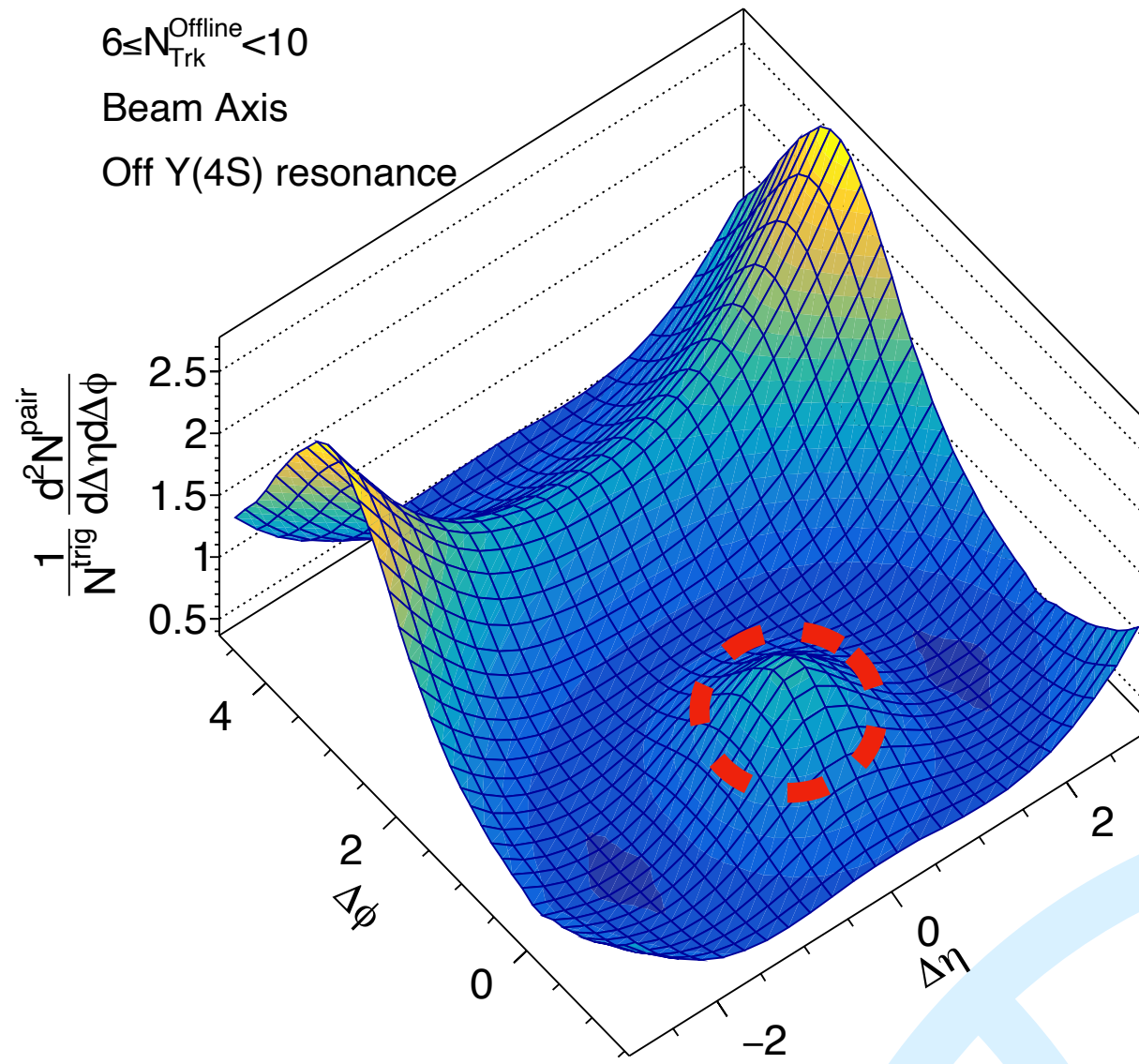


## Two-particle correlation function (per-trigger-particle associated yield)

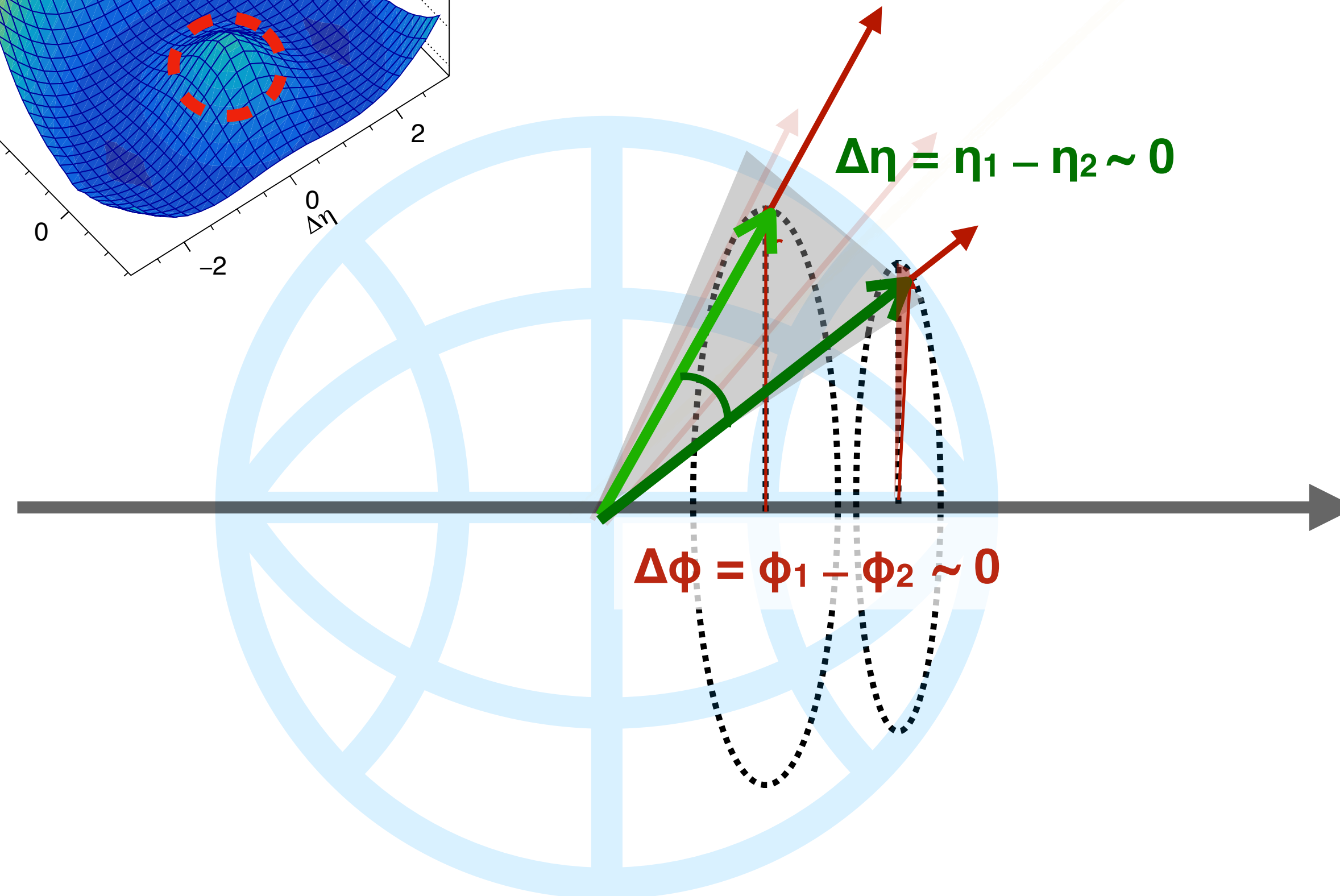
$$\frac{1}{N_{\text{trig}}} \frac{d^2 N^{\text{pair}}}{d\Delta\eta d\Delta\phi}$$

Belle  $e^+e^-$ ,  $\sqrt{s} = 10.52$  GeV  
 $6 \leq N_{\text{Trk}}^{\text{Offline}} < 10$   
 Beam Axis  
 Off  $Y(4S)$  resonance

 Preliminary



## Origin-peak intra-jet correlations @ near side $(\Delta\eta, \Delta\phi) \sim (0,0)$

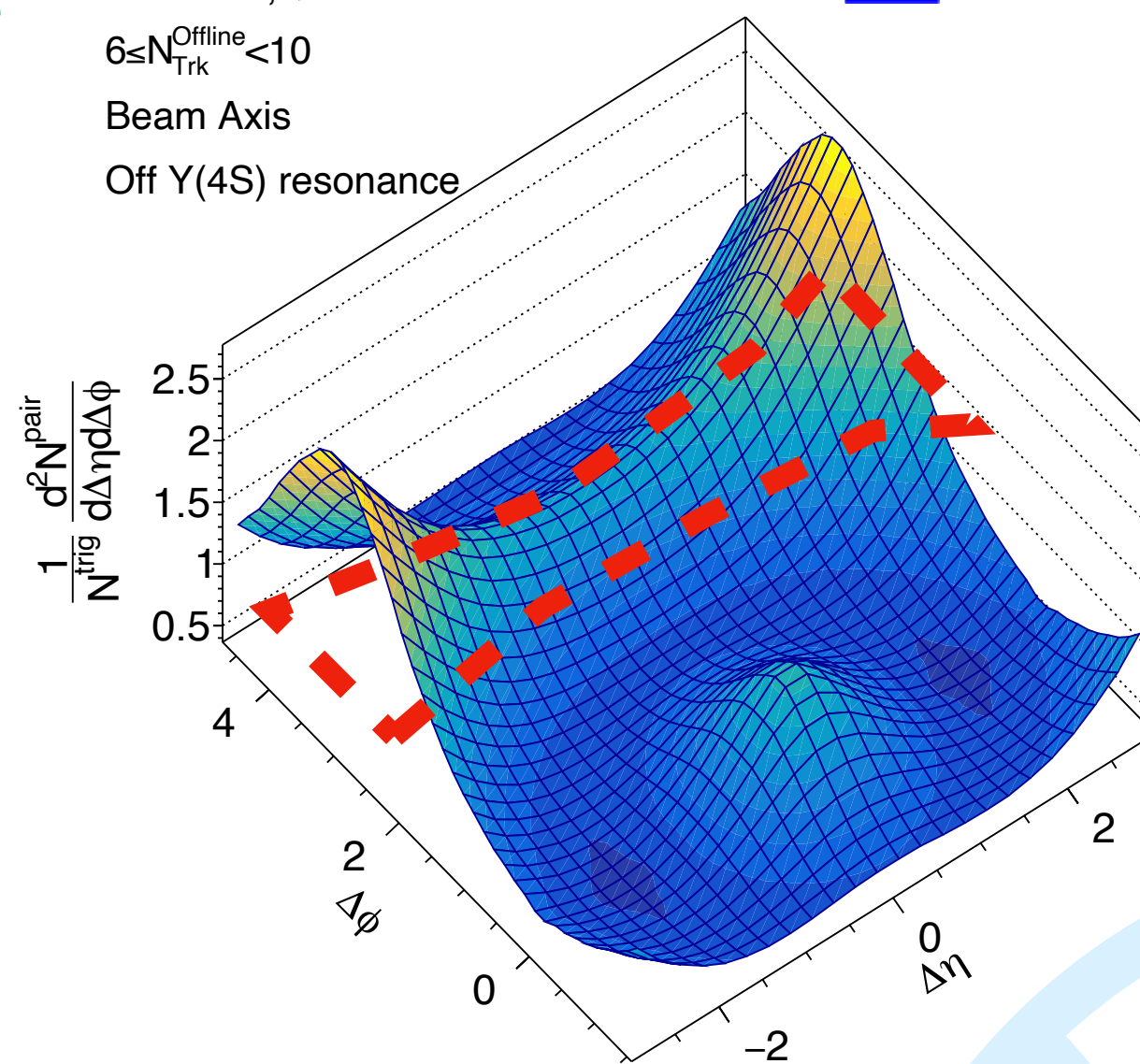


**Two-particle correlation function**  
(per-trigger-particle associated yield)

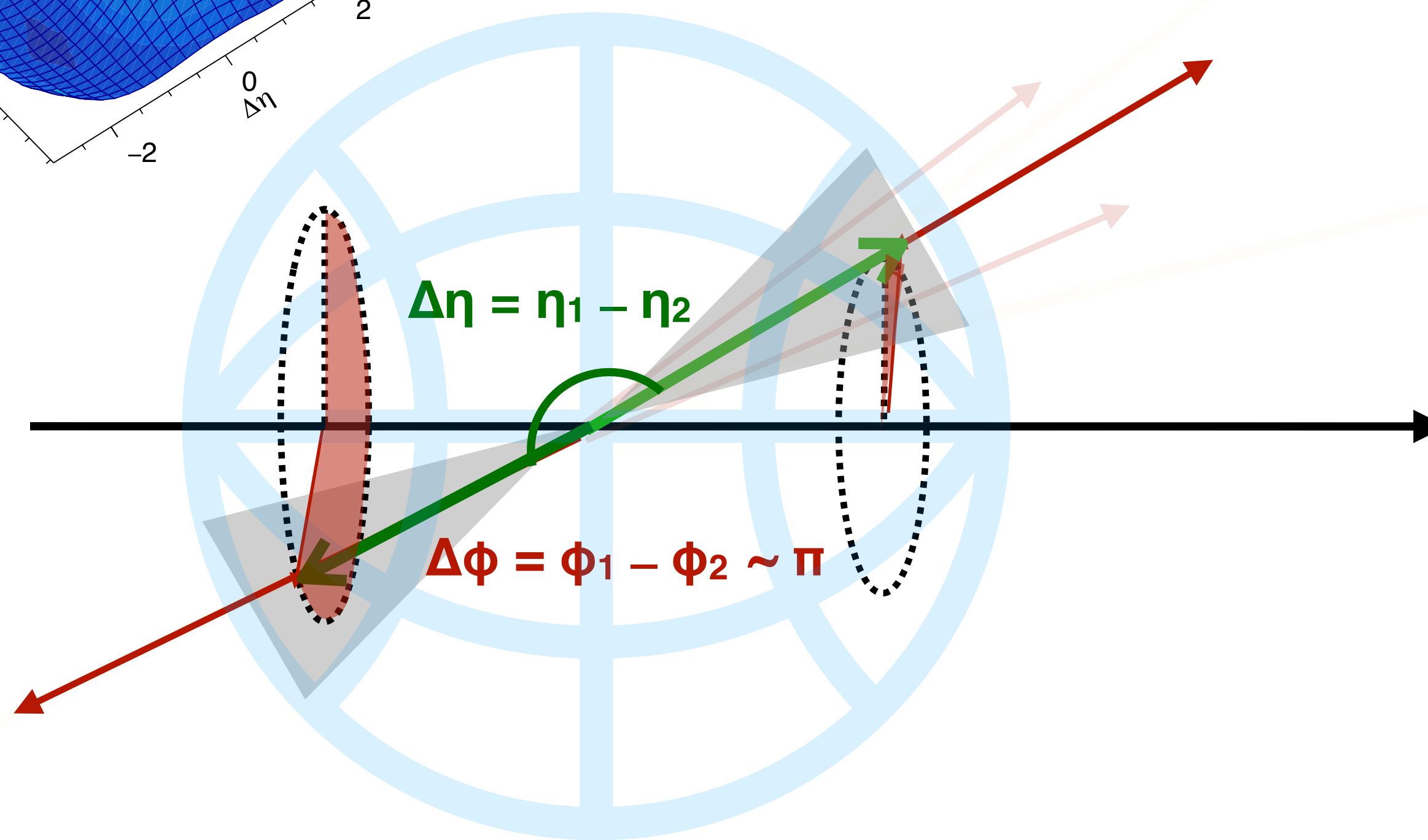
$$\frac{1}{N_{\text{trig}}} \frac{d^2 N^{\text{pair}}}{d\Delta\eta d\Delta\phi}$$

Belle  $e^+e^-$ ,  $\sqrt{s} = 10.52$  GeV  
 $6 \leq N_{\text{Trk}}^{\text{Offline}} < 10$   
 Beam Axis  
 Off  $Y(4S)$  resonance

 Preliminary



**Back-to-back jet correlations**  
@ away side ( $\Delta\phi \sim \pi$ )



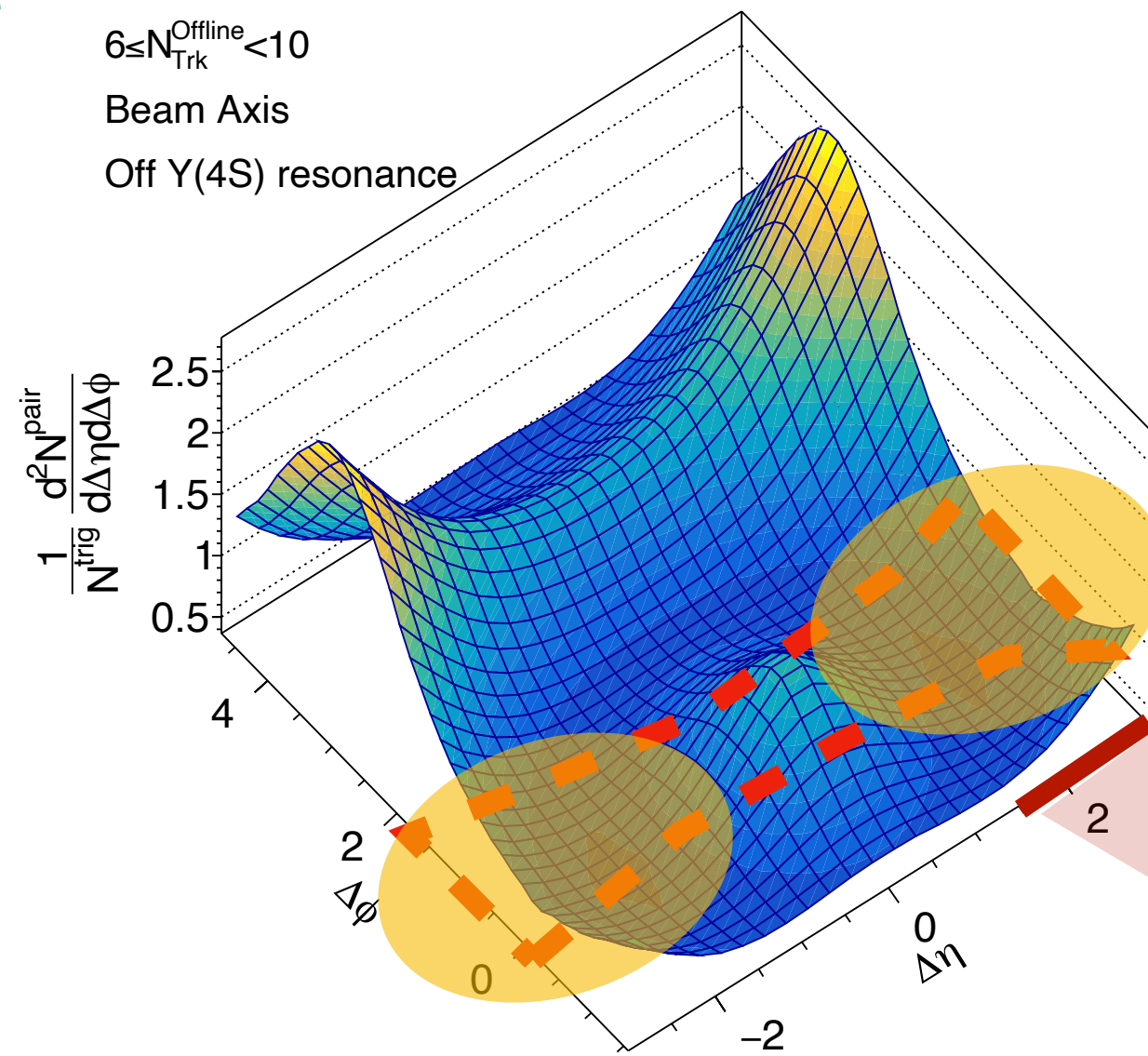


## Two-particle correlation function (per-trigger-particle associated yield)

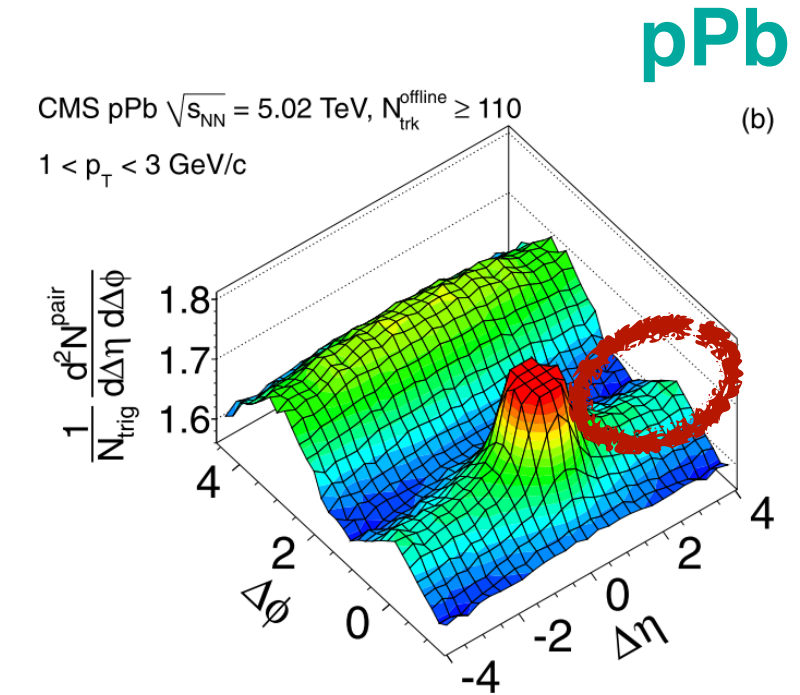
$$\frac{1}{N_{\text{trig}}} \frac{d^2 N^{\text{pair}}}{d\Delta\eta d\Delta\phi}$$

Belle  $e^+e^-$ ,  $\sqrt{s} = 10.52$  GeV  
 $6 \leq N_{\text{Trk}}^{\text{Offline}} < 10$   
 Beam Axis  
 Off Y(4S) resonance

 Preliminary

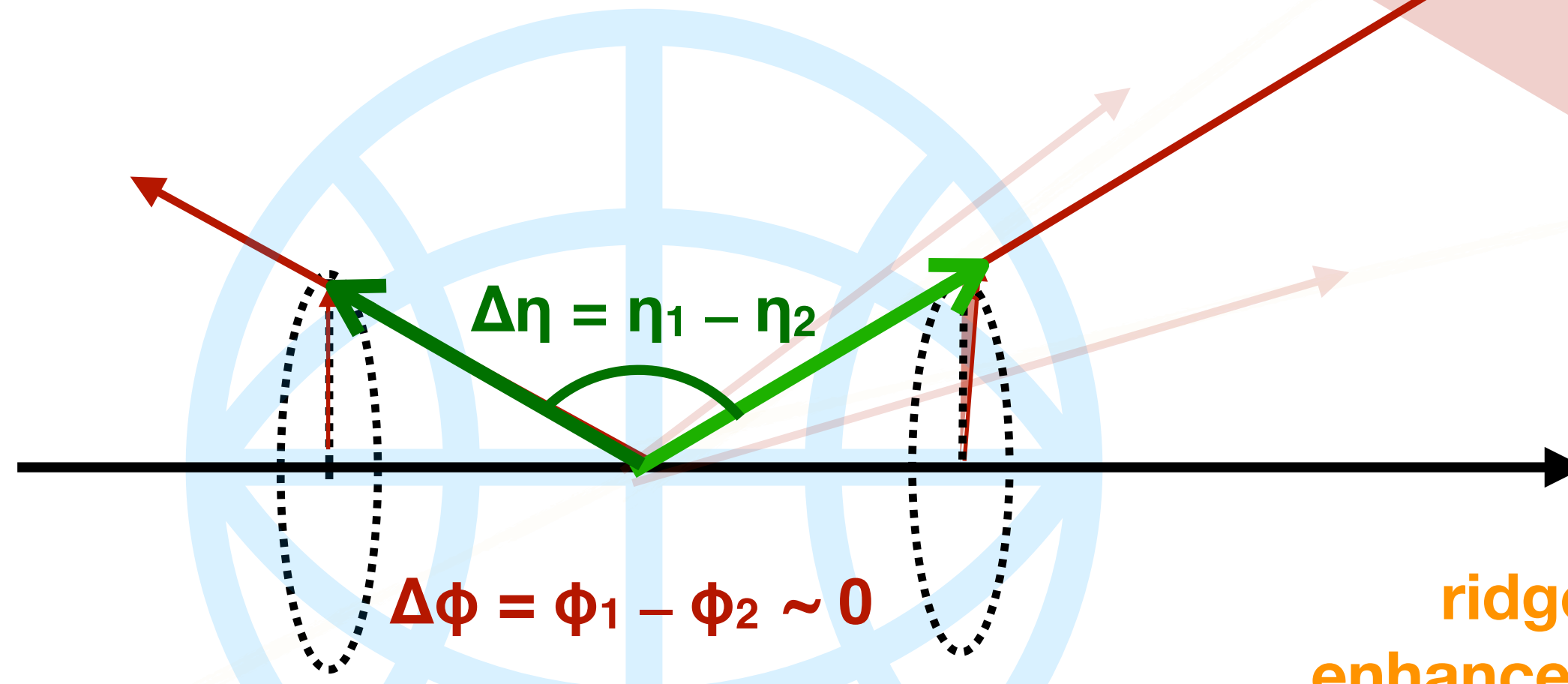


## Ridge correlations @ long range, near side

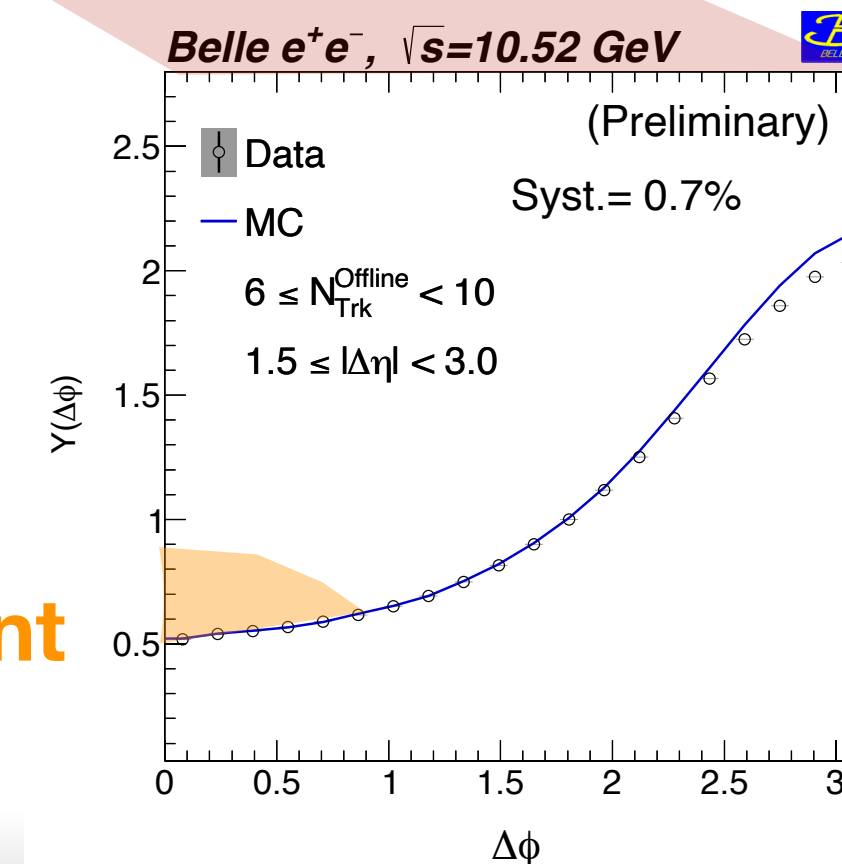


pA: [Phys. Lett. B718 \(2013\) 795-814](#)

long range  
( $1.5 \leq |\Delta\eta| < 3.0$ )



ridge  
enhancement



## Selections

### 1. Primary particle selection

Vary the primary particle definition between the proper lifetime cut  $\tau < 1 \text{ cm}/c$  and the vertex cut  $V_r < 1 \text{ cm}$

### 2. Tracking efficiency

Universal 0.35% uncertainty quoted for high  $p_T$  ( $> 200 \text{ MeV}/c$ ) tracks

### 3. Event selection

Vary the energy sum in ECL from  $> 0.18 \sqrt{s}$  to  $> 0.23 \sqrt{s}$

## Histogramming imperfection

### 4. B(0,0) extrapolation and long-range correlation scaling

Corrections of bin-size effect on the B(0,0) scaling factor and the magnitude of the long-range correlations are applied. Uncertainties of the correction factors are considered as sources of systematics

### 5. $\Delta\phi$ bin width

## Reweighting

Accessing by reweighting factors with the alternative parametrization

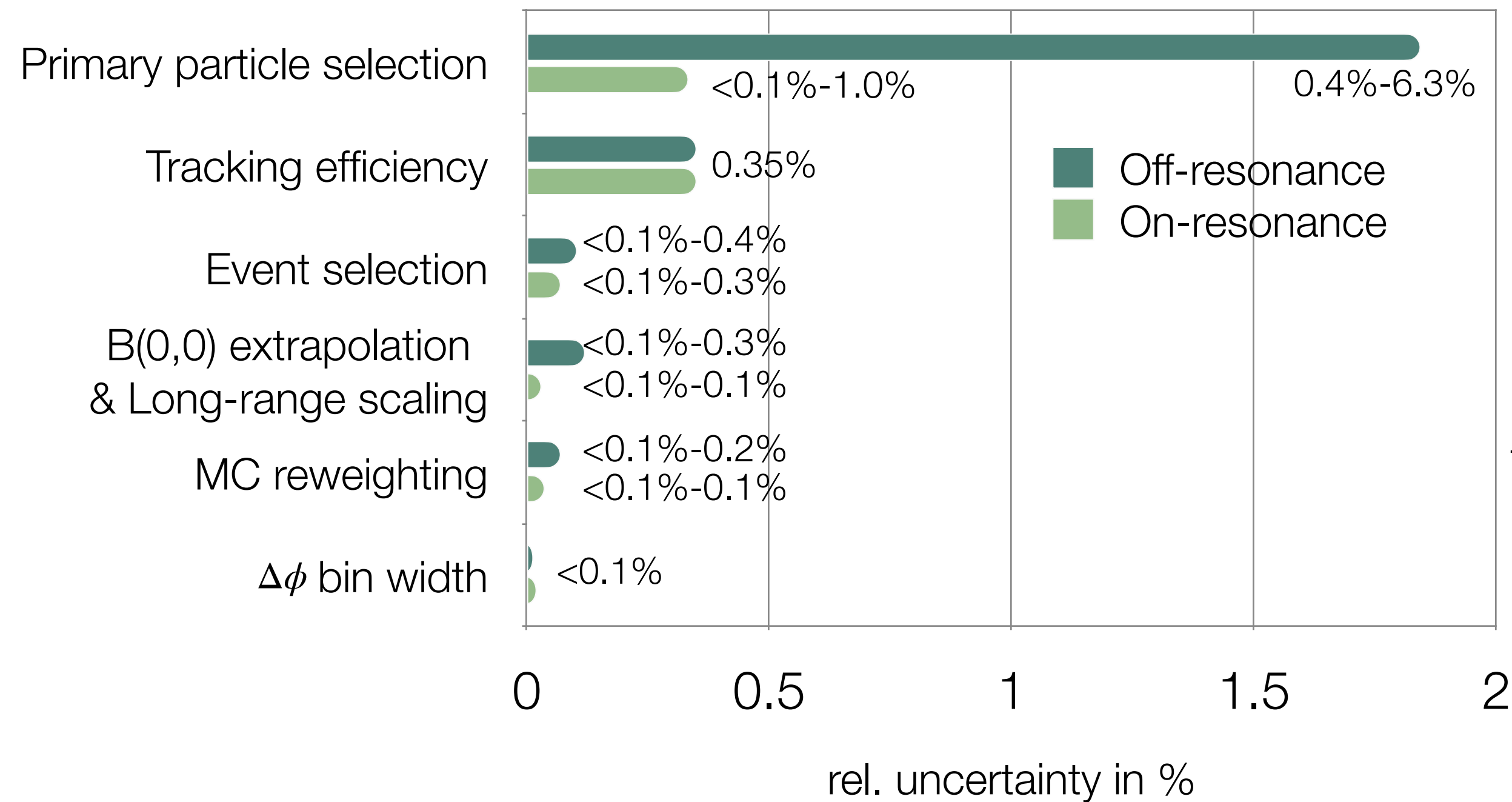
### 6. MC reweighting

### 7. Thrust mixing reweighting

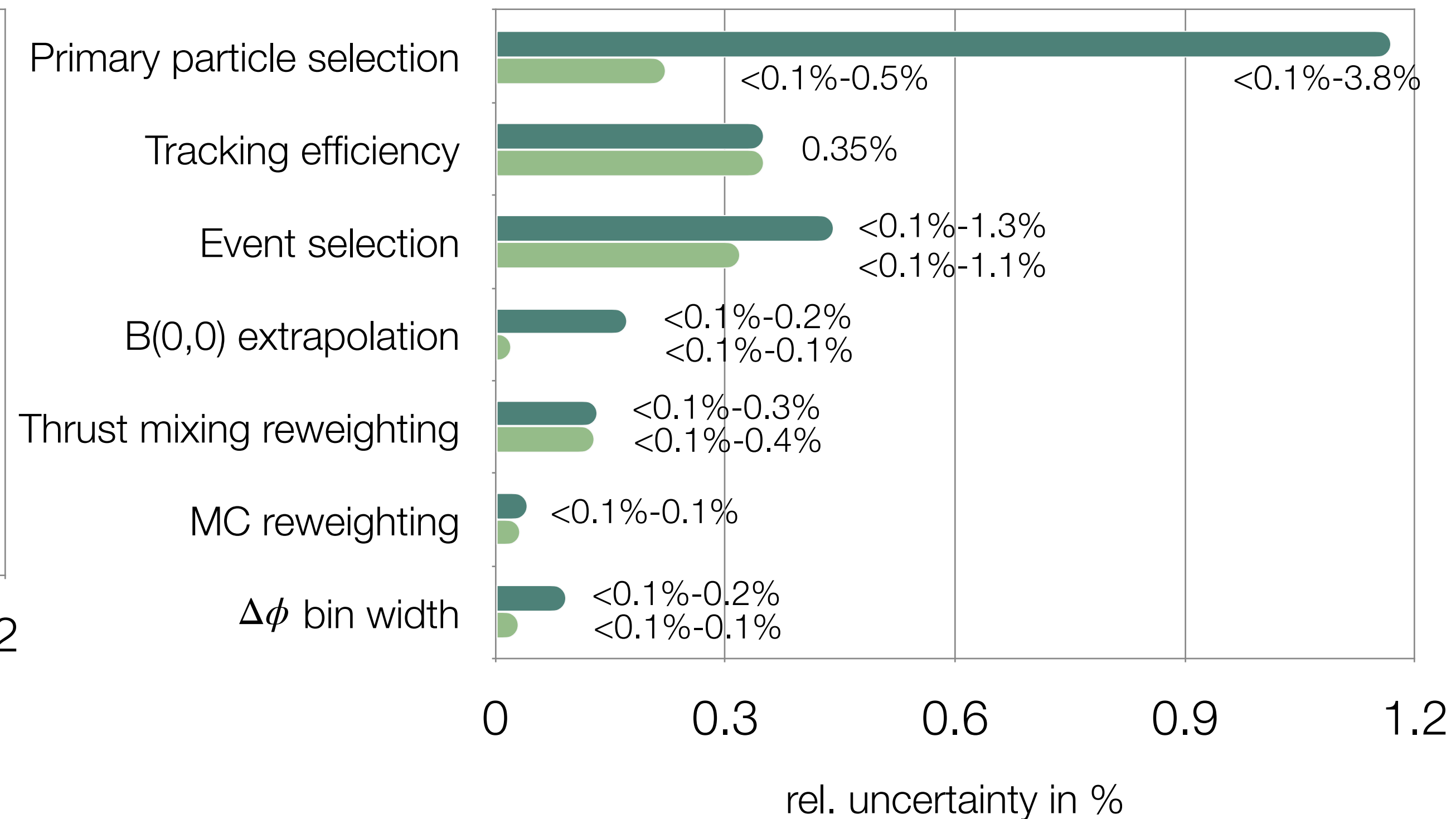


- Selections (primary particle, tracking, and event selections) are the dominant systematics sources
- Others are comparably small:  $O(10^{-4})$  up to 0.5%

## Beam axis analysis



## Thrust axis analysis



- ZYAM method (zero yield at minimum) is applied to calculate “ridge yield”

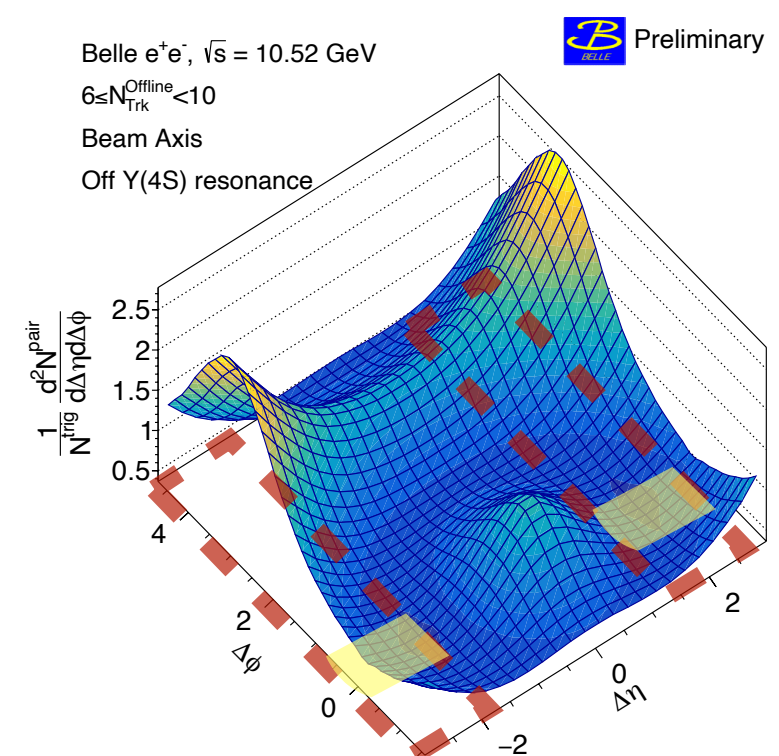
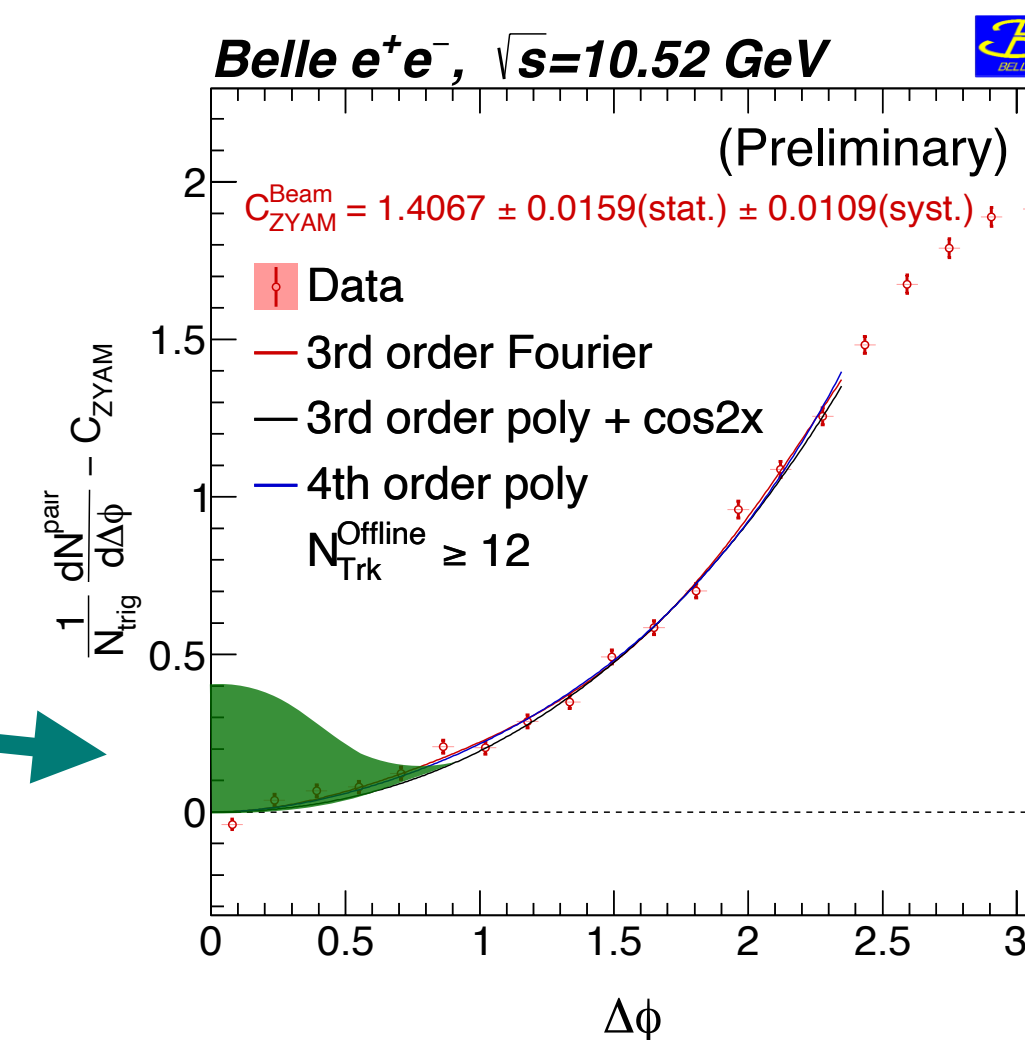
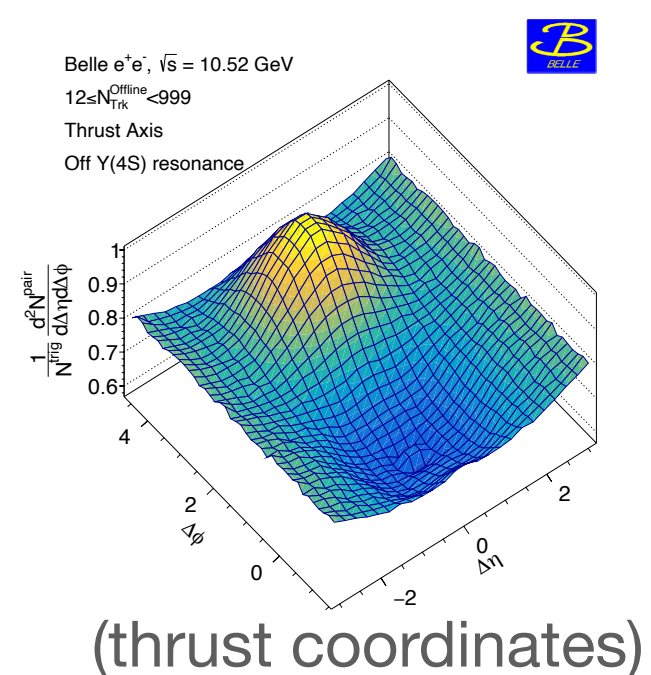
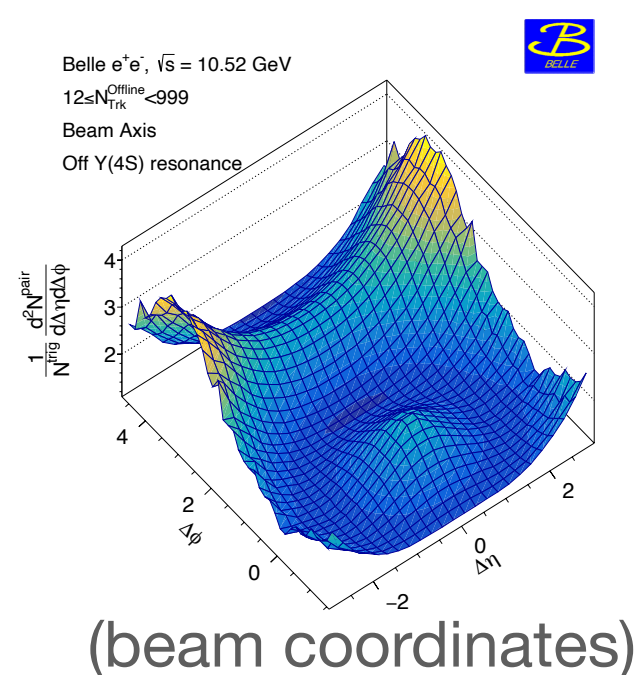


illustration of an enhanced ridge signal



- No significant ridge signals are observed in both beam, thrust axis coordinates
- Upper limits of ridge yield by the bootstrap method reported



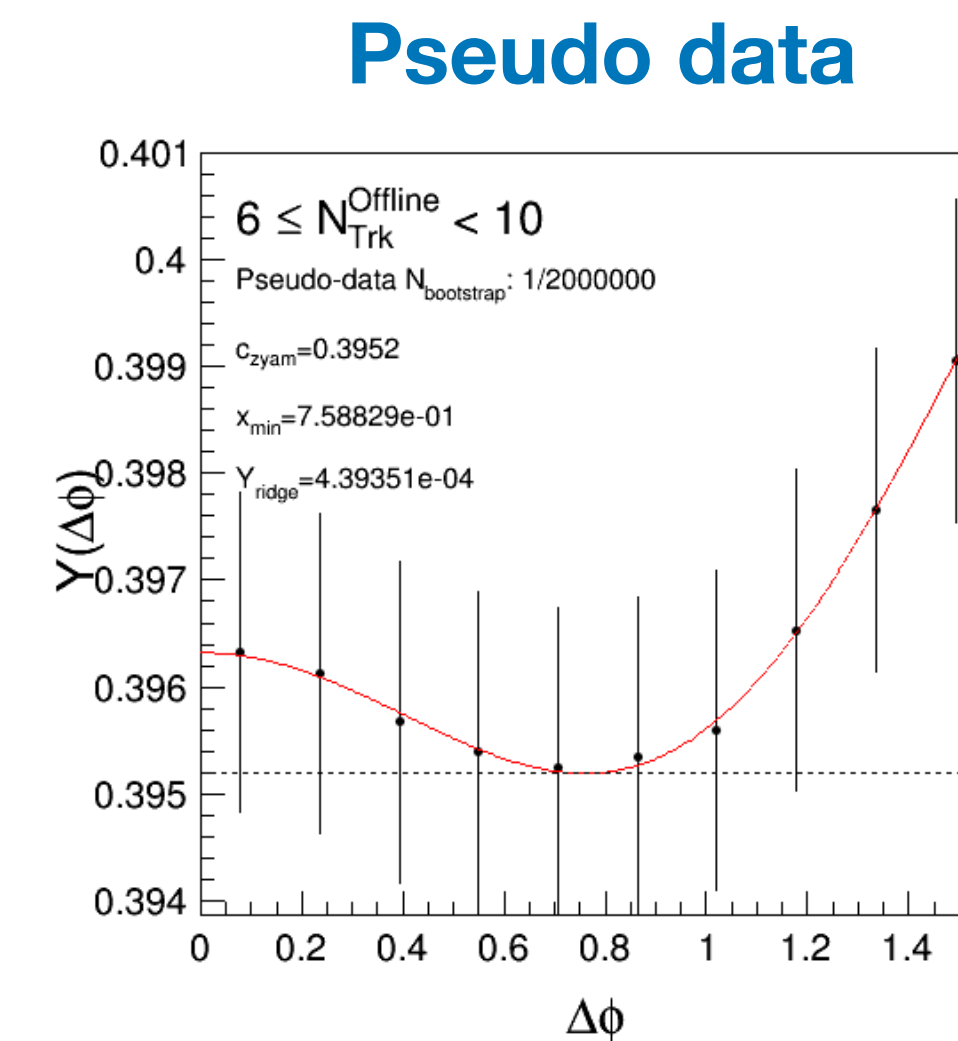
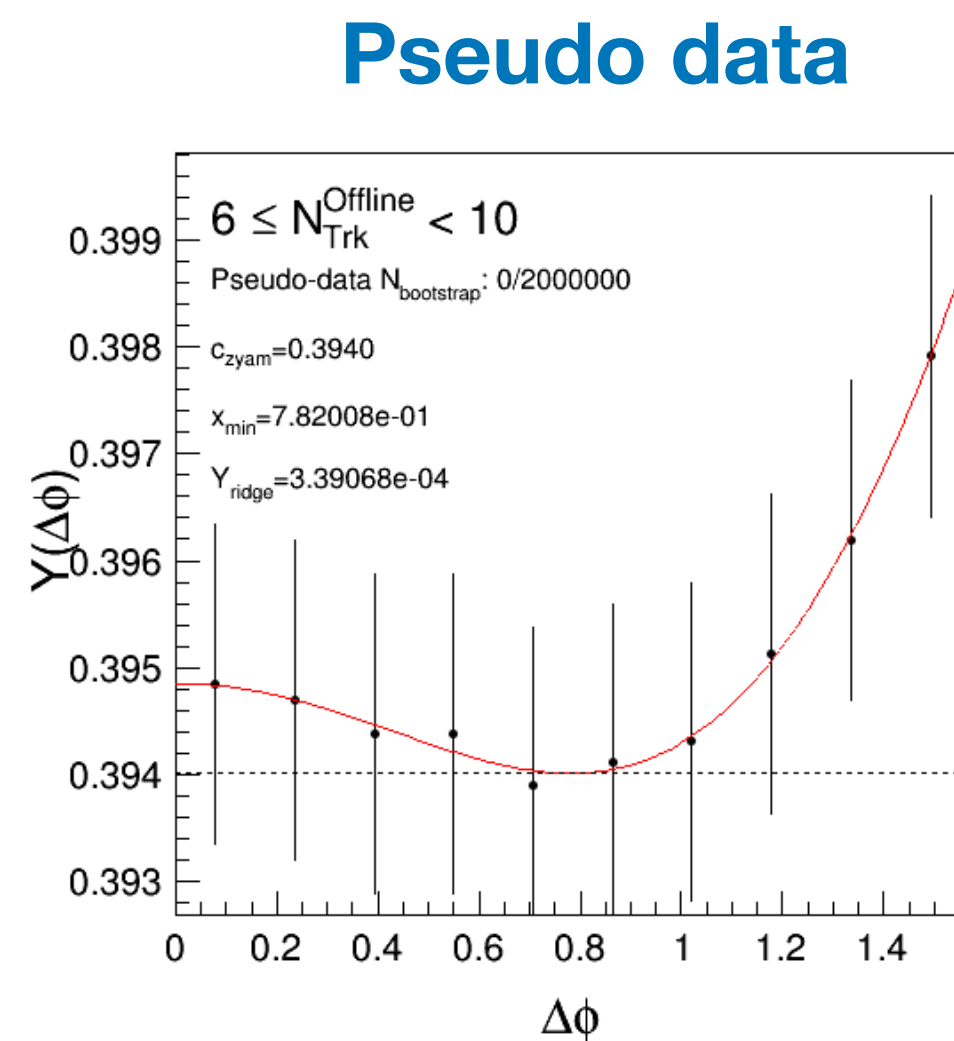
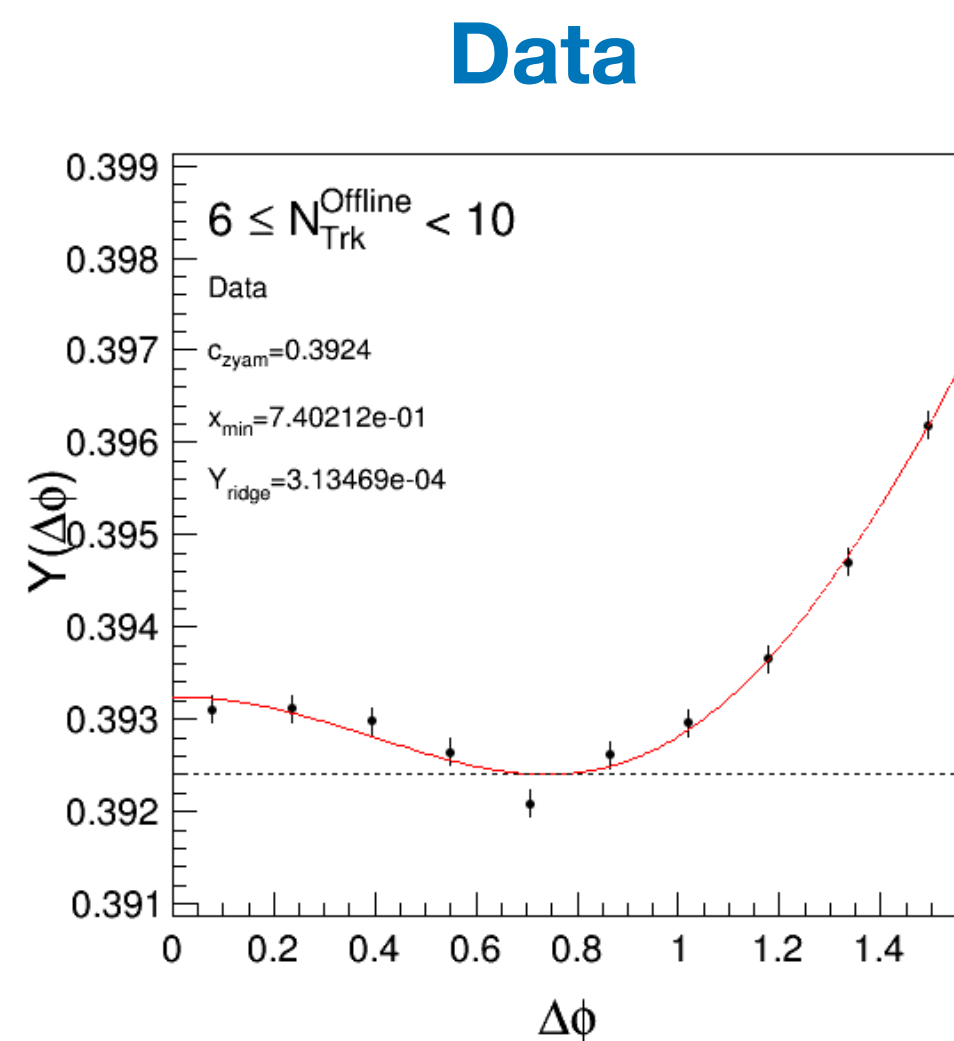
ZYAM  
[Phys.Rev. C72 \(2005\) 011902](#)

bootstrap: [bootstrap](#)



## Bootstrap method

- Fit the long-range yield distribution  $Y(\Delta\phi)$ .
- Vary the functional distribution by statistical and systematic uncertainties to construct a pseudo data.
- Refit the distribution with the same function and get a new ridge yield from this smeared distribution.
- Total 2M pseudo data are constructed.



Ref: [[bootstrap](#)]

**Belle  $e^+e^-$ ,  $\sqrt{s}=10.58$  GeV**

$(1.5 < |\Delta\eta| < 3.0)$

