

The statistical hadronization model and beauty hadrons: a case for partial equilibration of b-quarks?

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Outline

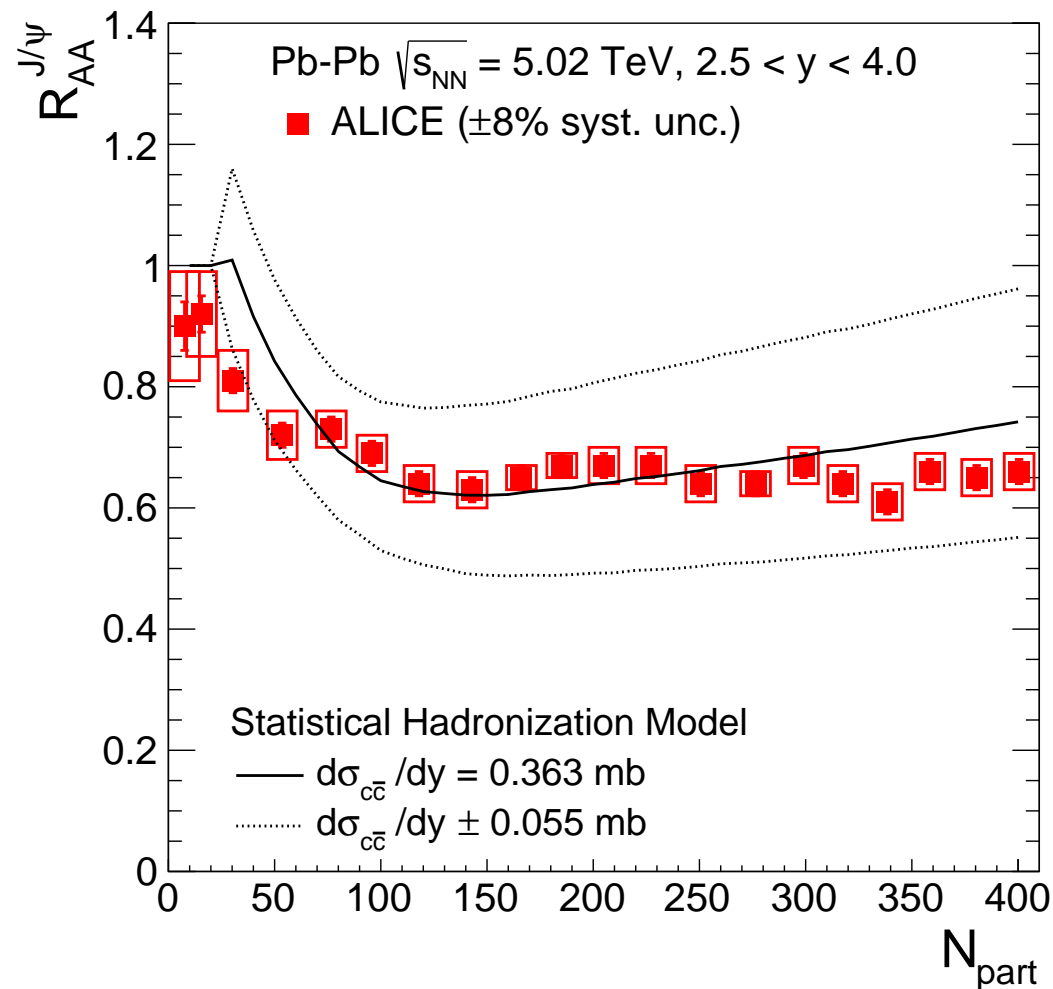
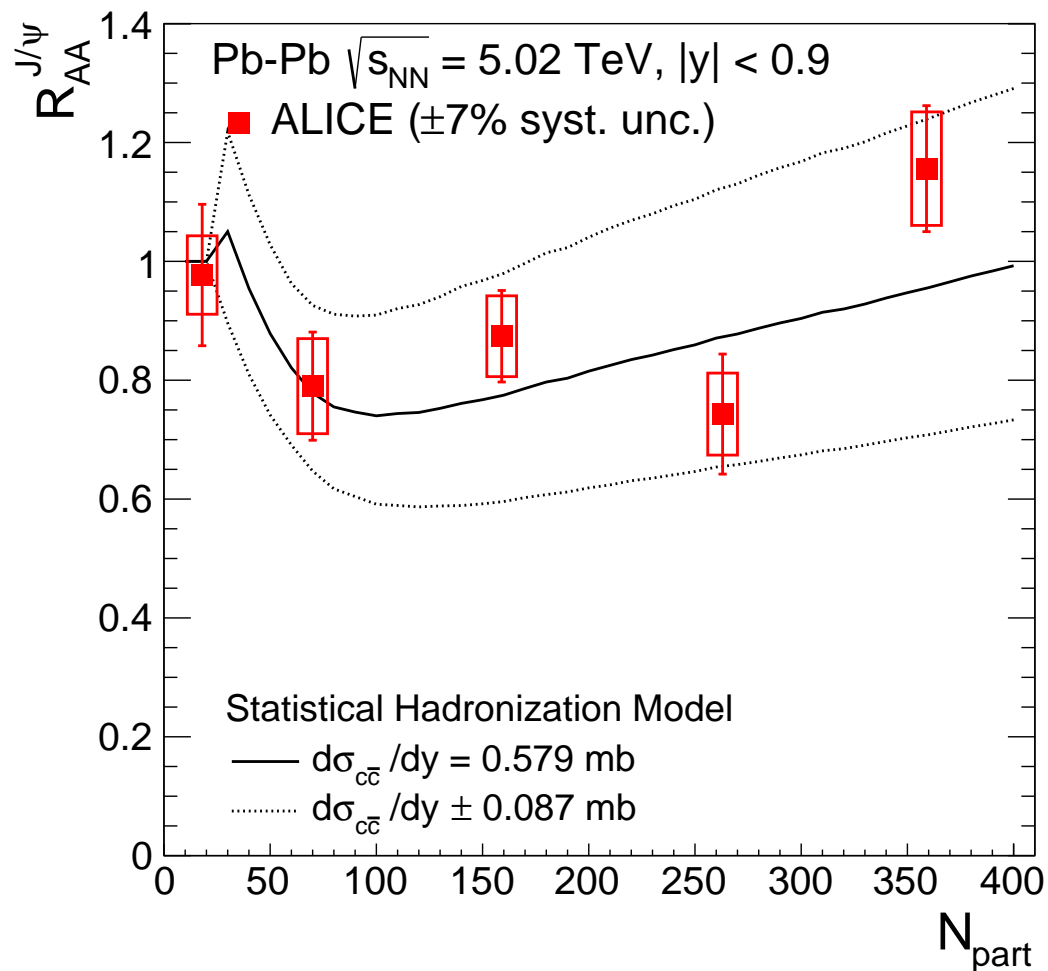
- Introduction: A brief look at charm
- The beauty model (and ingredients)
- Predictions and comparisons to data
- Summary (including the open questions)

The Statistical Hadronization Model for charm (SHMc)

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full thermalization of c quarks in QGP, hadronization at chemical freeze-out

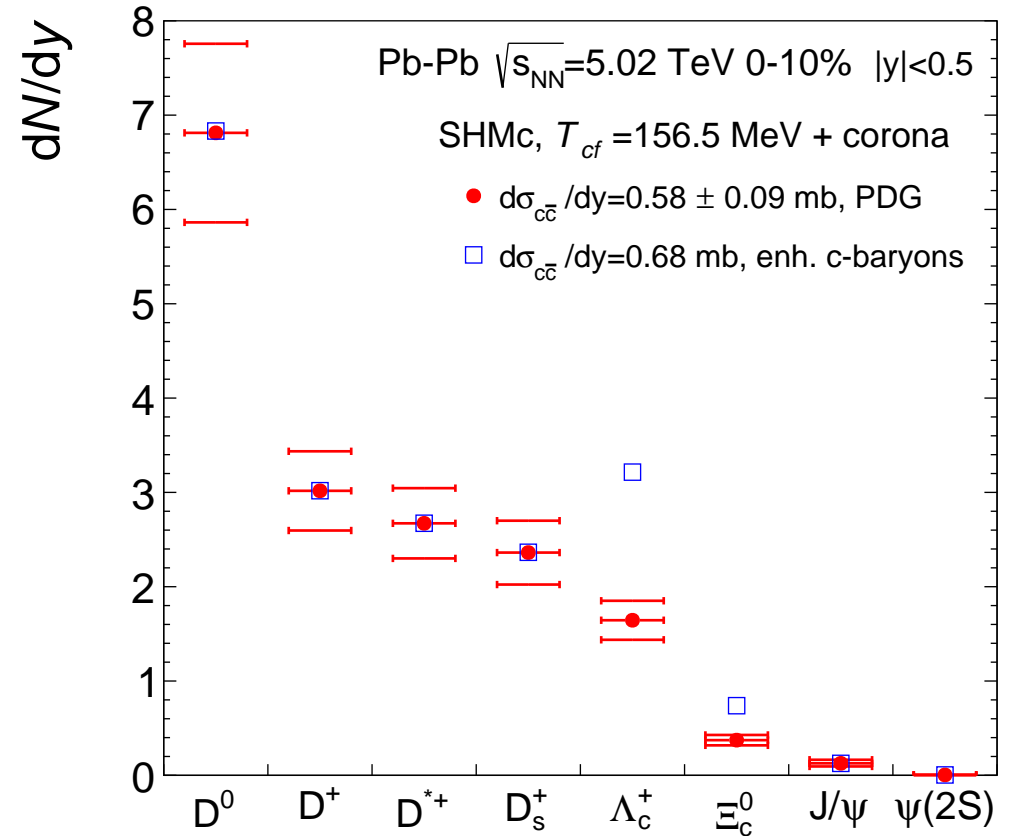
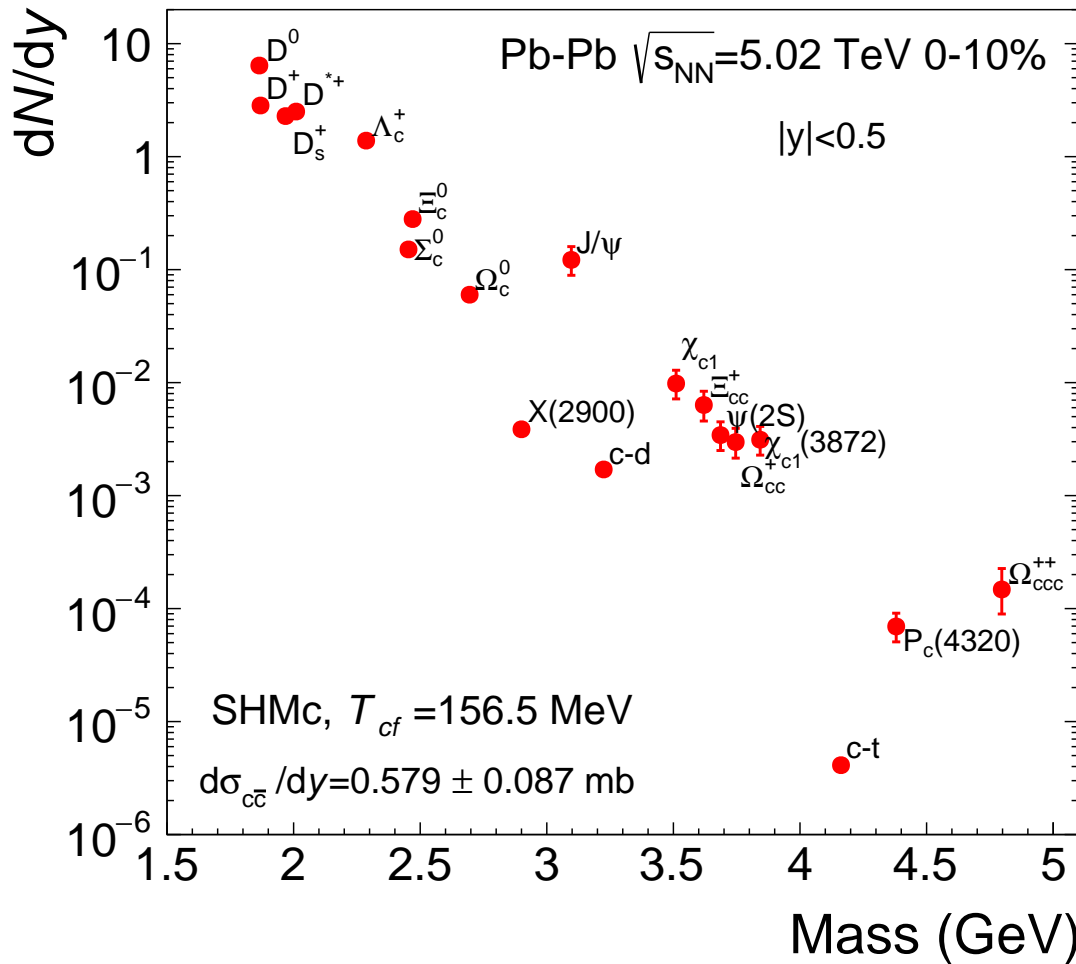


$d\sigma_{c\bar{c}}/dy$ via normalization to D^0 in Pb-Pb 0-10%, ALICE, [arXiv:2110.09420](https://arxiv.org/abs/2110.09420)

$dN/dy = 6.82 \pm 1.03$ (and assuming hadronization fractions in data as in SHMc)

SHMc: the charm zoo

The power of the model: predicting the full suite of charmed hadrons



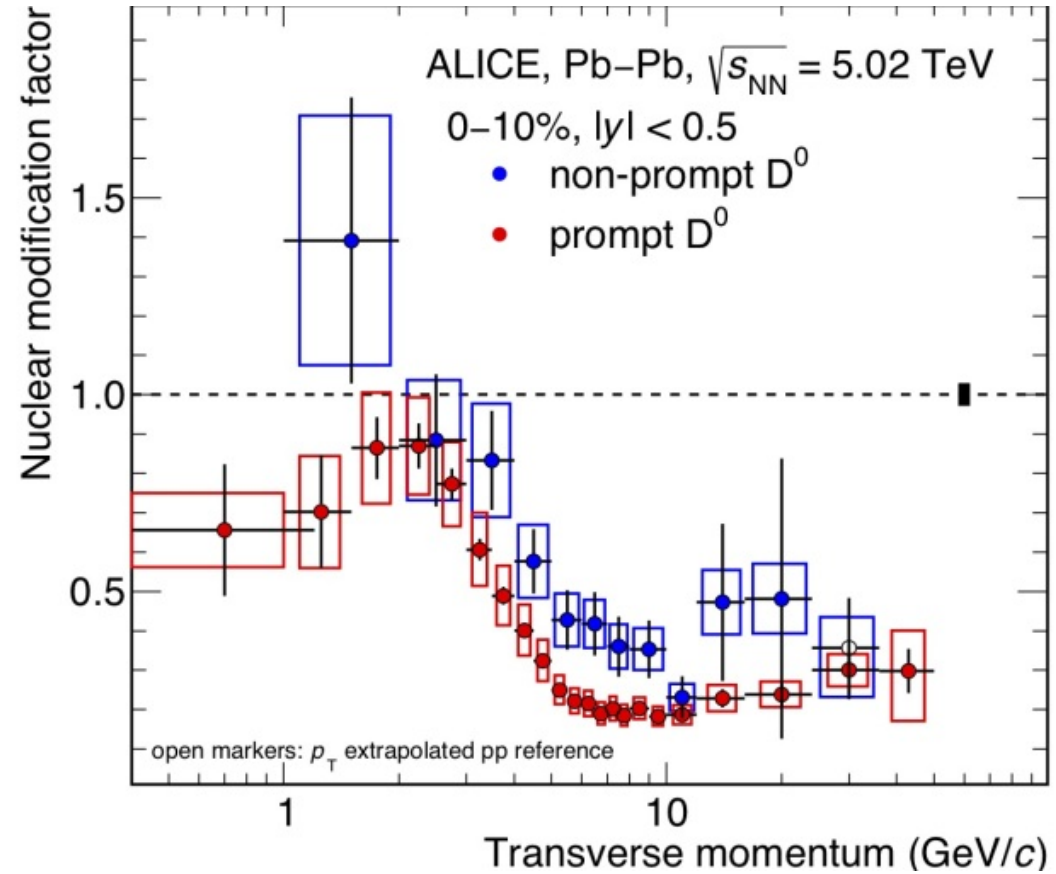
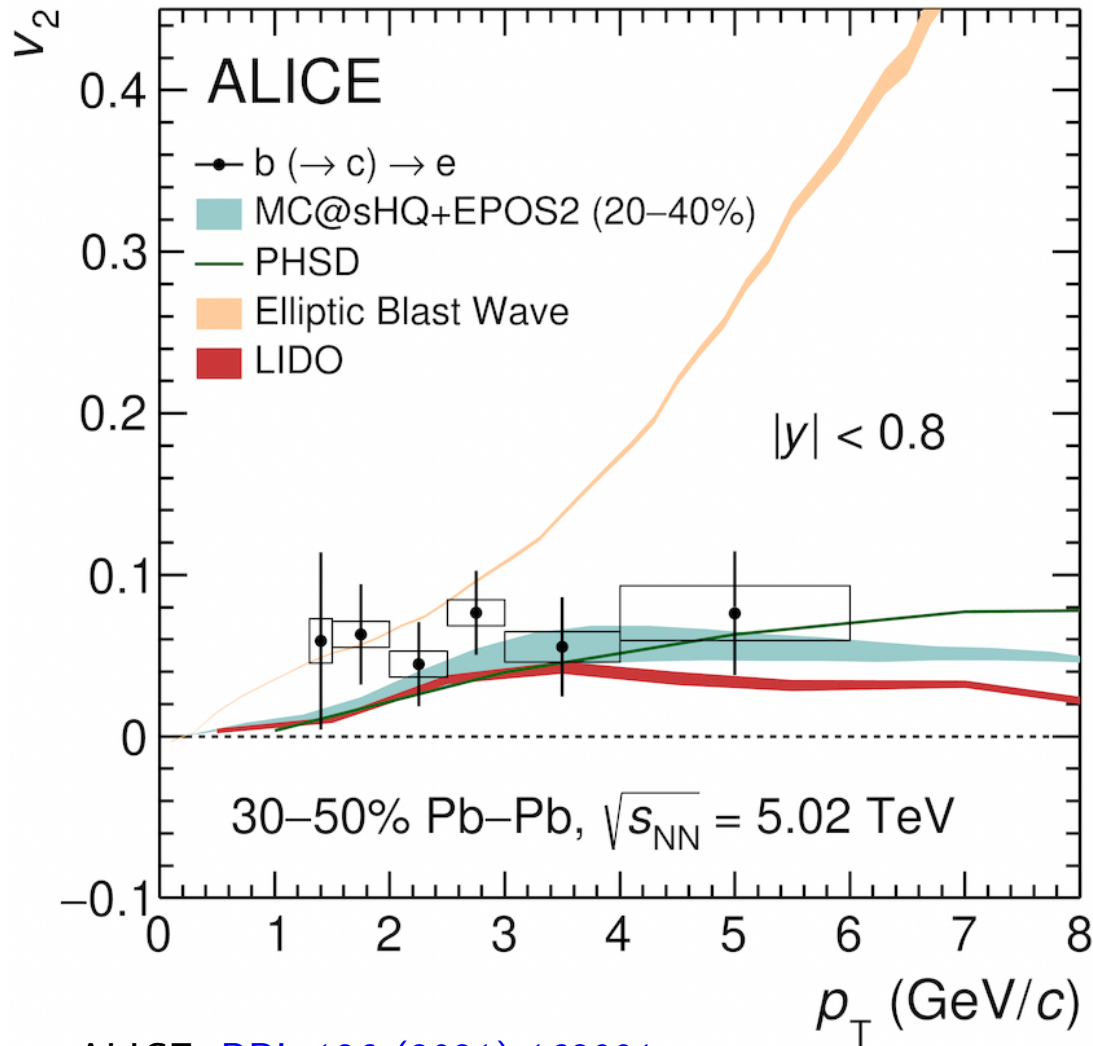
Comparison to data: talk by L. Vermunt, Friday, T11

$$\frac{dN_{c\bar{c}}}{dy} = 13.8$$

Beauty quark thermalization?

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ALICE, [arXiv:2202.00815](https://arxiv.org/abs/2202.00815), ATLAS

definitely strong flow but clearly less strong than for charm (CMS, QM'22, HIN-21-003)
...and a strong coupling with the medium (less energy loss than charm, $p_T \simeq 10$ GeV/c)

SHM for beauty (SHMb): method and inputs

- Thermal model calculation (grand canonical) T, μ_B : $\rightarrow n_X^{th}$
- $N_{b\bar{b}}^{dir} = \frac{1}{2}g_b V (\sum_i n_{B_i}^{th} + n_{\Lambda_{b,i}}^{th}) + g_b^2 V (\sum_i n_{\Upsilon_i}^{th} + n_{\chi_{b,i}}^{th})$
- $N_{b\bar{b}} \ll 1 \rightarrow$ Canonical (J.Cleymans, K.Redlich, E.Suhonen, Z. Phys. C51 (1991) 137):

$$N_{b\bar{b}}^{dir} = \frac{1}{2}g_b N_{ob}^{th} \frac{I_1(g_b N_{ob}^{th})}{I_0(g_b N_{ob}^{th})} + g_b^2 N_{b\bar{b}}^{th} \rightarrow g_b \text{ (beauty fugacity)}$$

$$\text{Outcome: } N_B = g_b V n_B^{th} I_1/I_0 \quad N_\Upsilon = g_b^2 V n_\Upsilon^{th}$$

$$\text{Inputs: } T, \mu_B, \quad V_{\Delta y=1} (= (dN_{ch}^{exp}/dy)/n_{ch}^{th}), \quad N_{b\bar{b}}^{dir} \text{ (exp. and pQCD)}$$

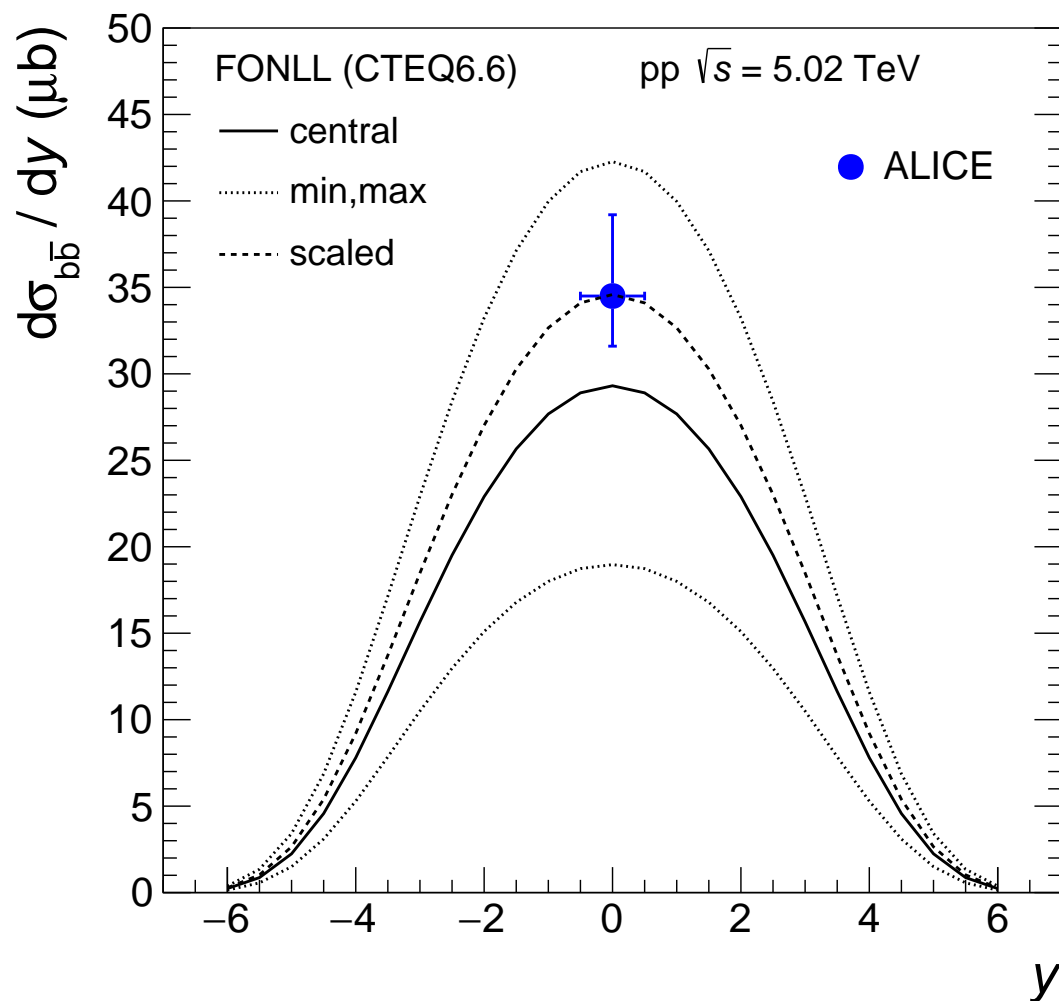
Assumed minimal volume for QGP: $V_{QGP}^{min} = 200 \text{ fm}^3$

The beauty production cross section $d\sigma_{b\bar{b}}/dy$

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ALICE, [JHEP 05 \(2021\) 220](#): $\frac{d\sigma_{b\bar{b}}}{dy} = 34.5 \pm 2.4(stat)_{-2.9}^{+4.7}(tot.syst)\mu b$



[FONLL](#), Cacciari et al., [JHEP 1210 \(2012\)](#)

scaling for $y=2.5-4$

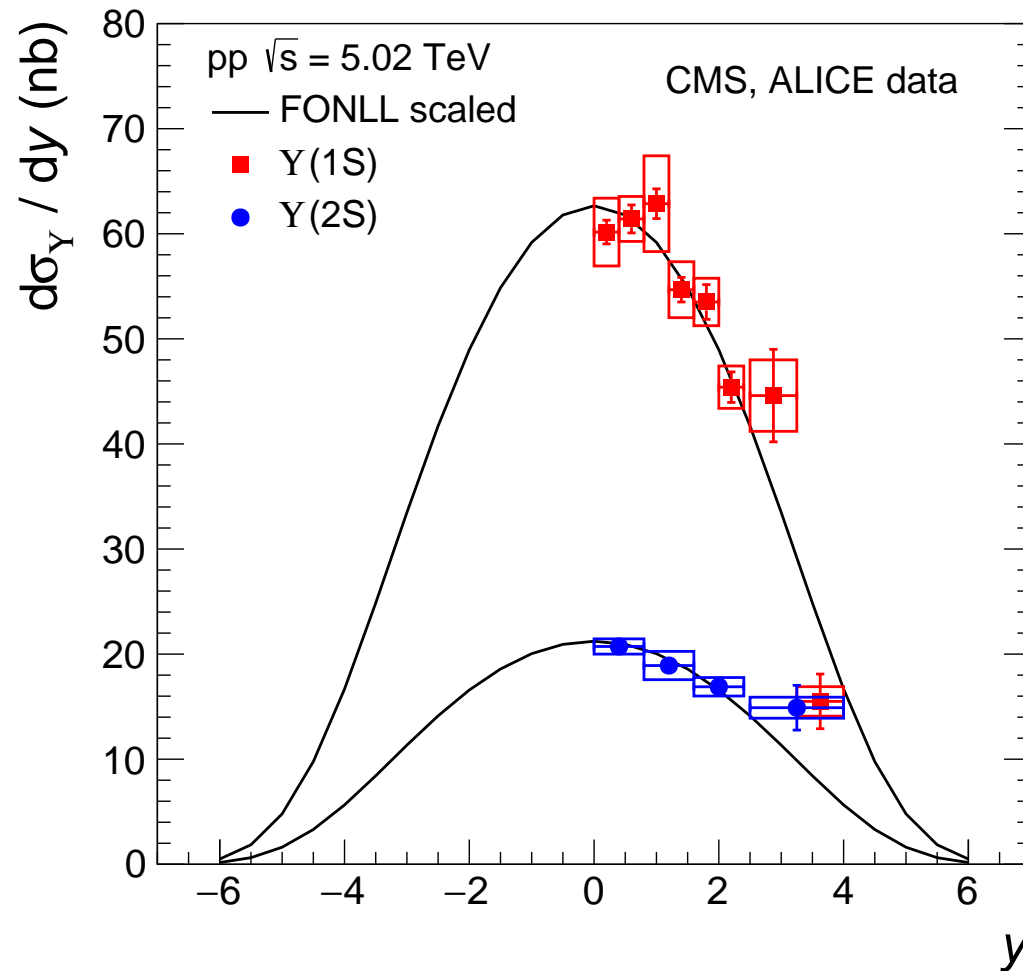
Shadowing: 0.7, independent on y

$$y = 0 : \frac{dN_{b\bar{b}}}{dy} = 0.57$$

$\pm 20\%$ total uncertainty

All produced anew ...no Υ state survives in QGP (extreme for $\Upsilon(1S)$?)

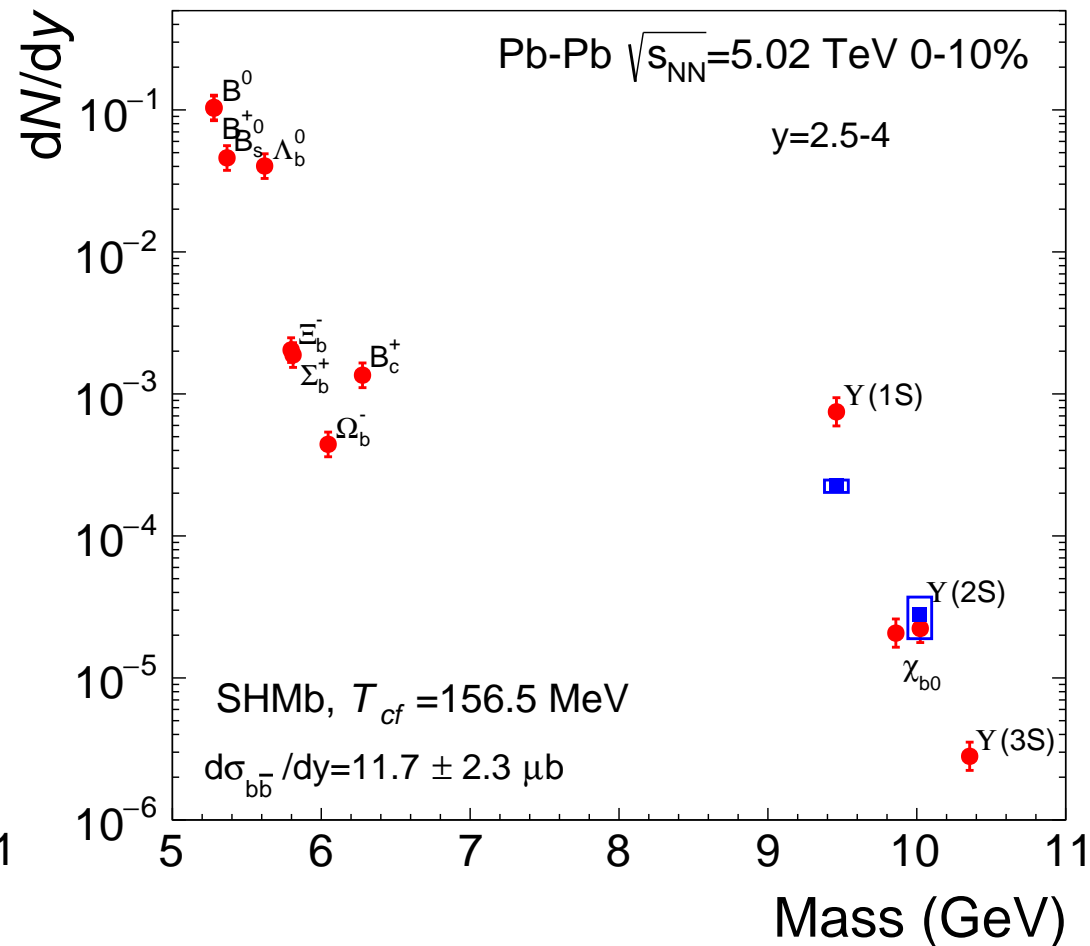
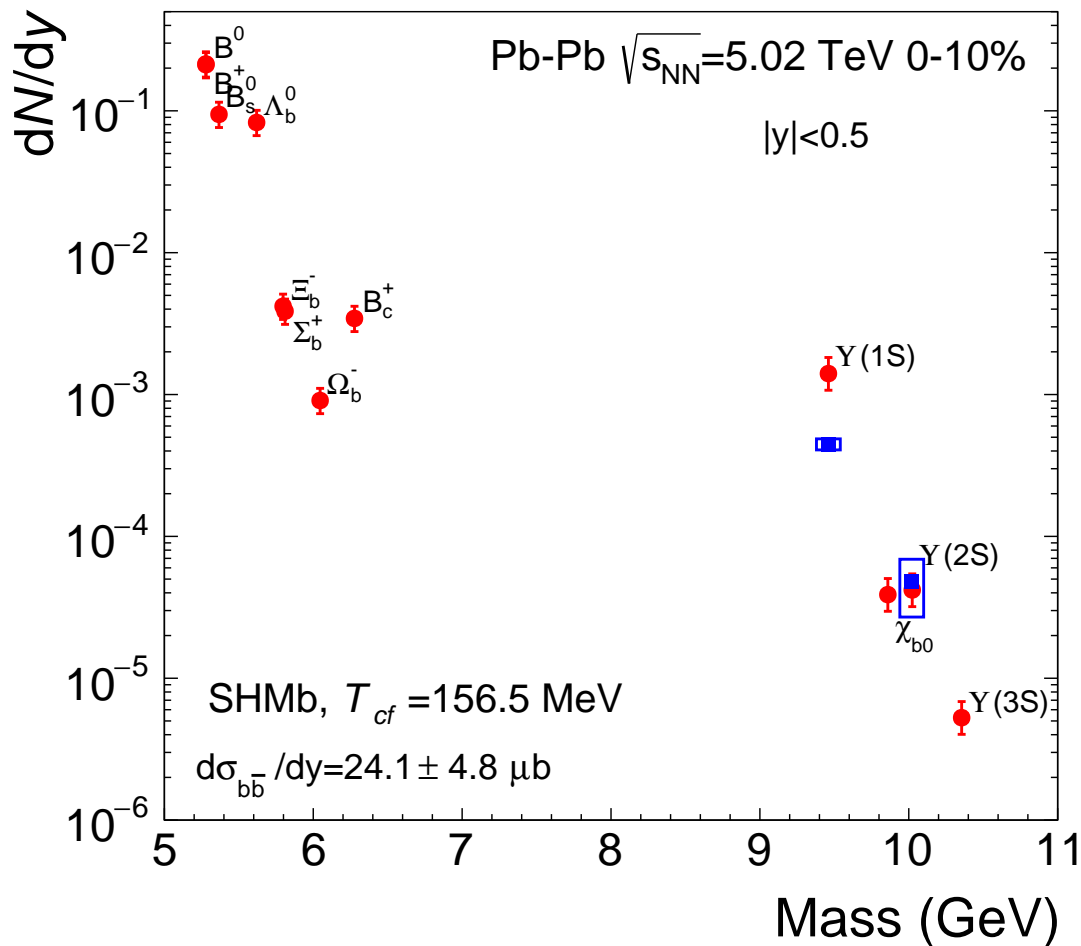
Core(SHMb)-corona with pp data input CMS, [PLB 790 \(2019\) 270](#), ALICE, [arXiv:2109.15240](#)



SHMb: the beauty zoo (0-10%)

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$$g_b = 1.05 \cdot 10^9$$

$$B_c : 3.44 \cdot 10^{-3}$$

$$g_b = 0.86 \cdot 10^9$$

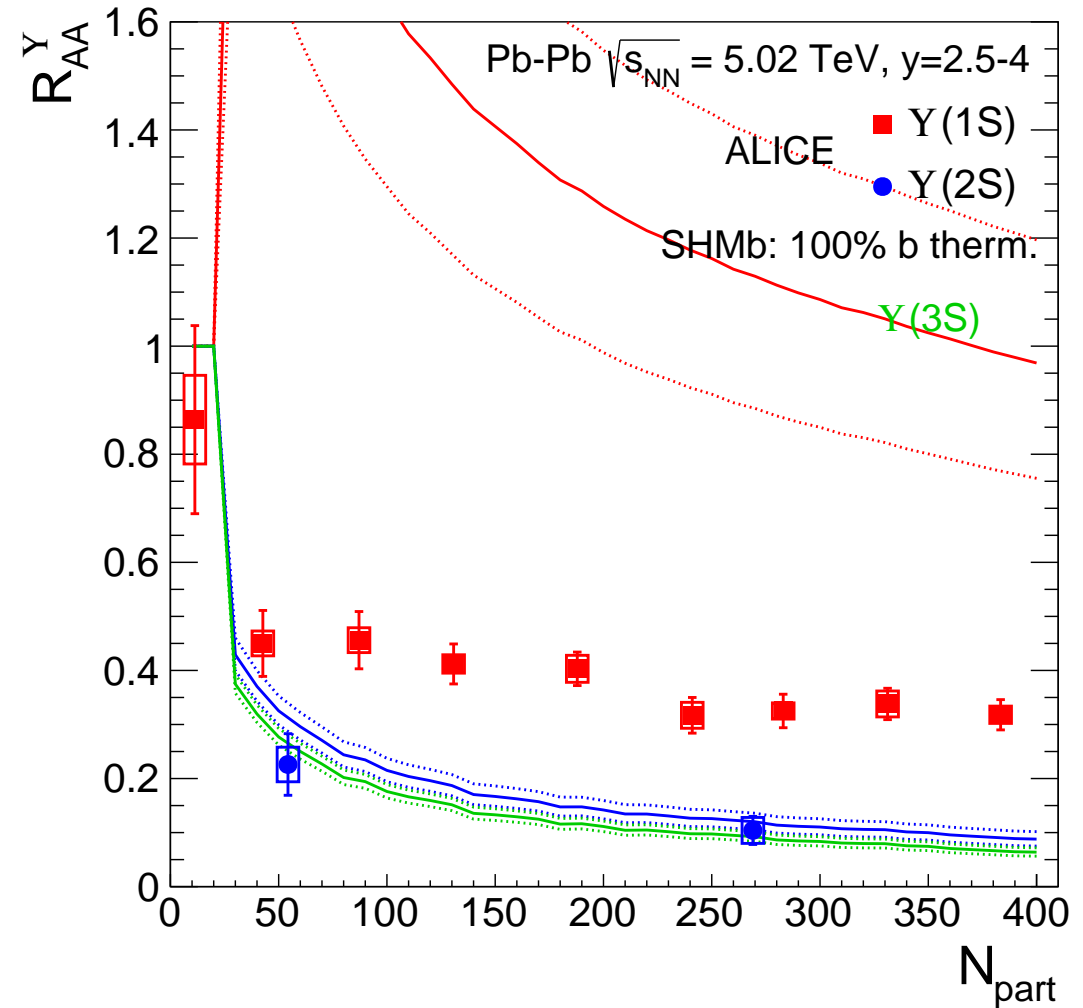
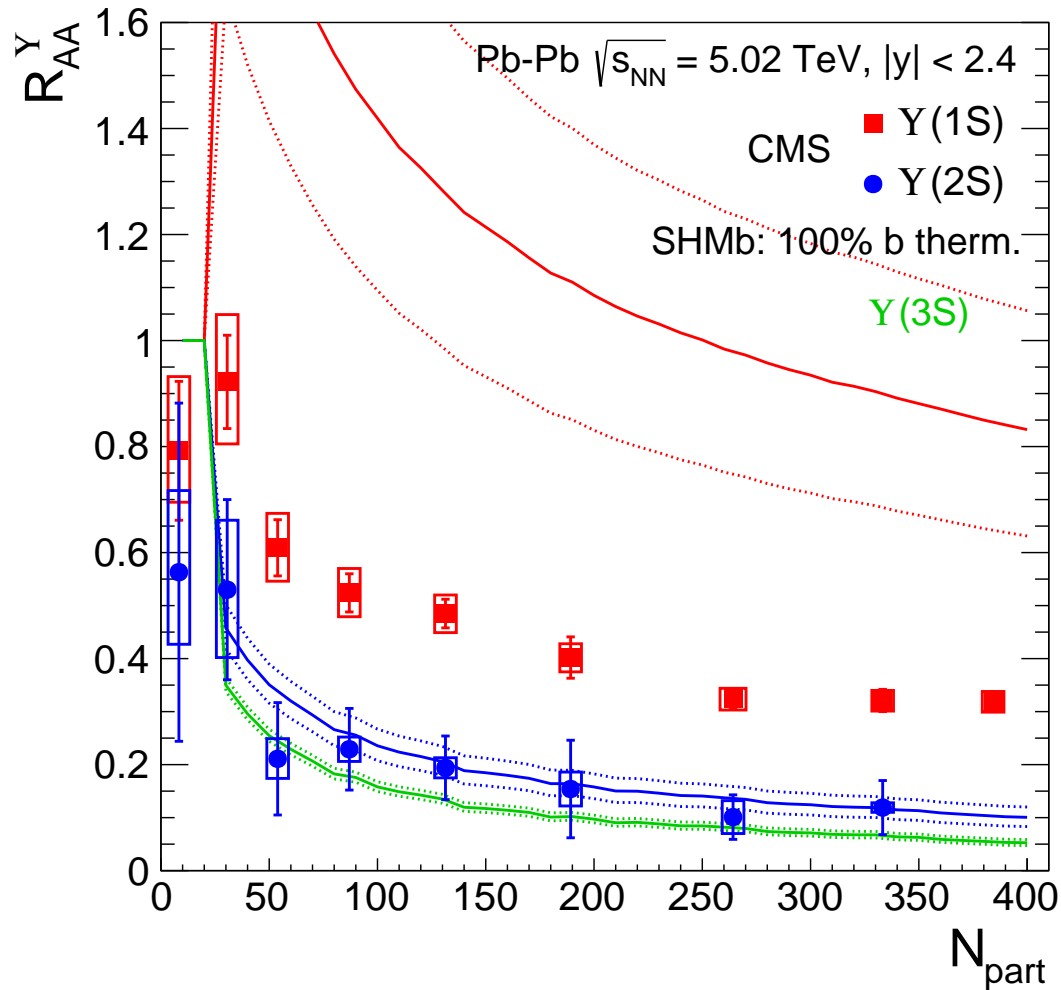
$$B_c : 1.36 \cdot 10^{-3}$$

Blue: Υ data (CMS, ALICE): calc. based on R_{AA} and pp (would be nice to include in publications dN/dy)

R_{AA} , 100% $b\bar{b}$ thermalized

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CMS, [PRL 120 \(2018\) 142301](#)

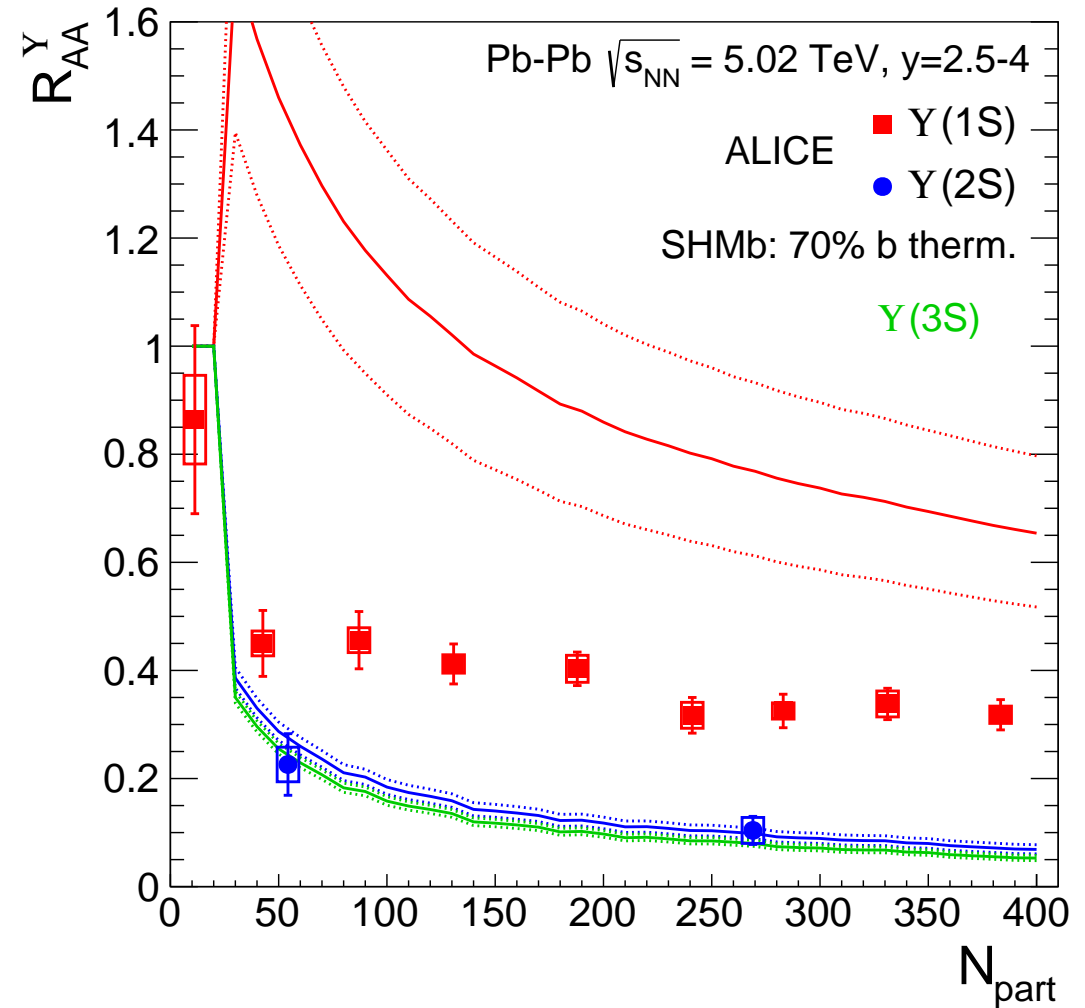
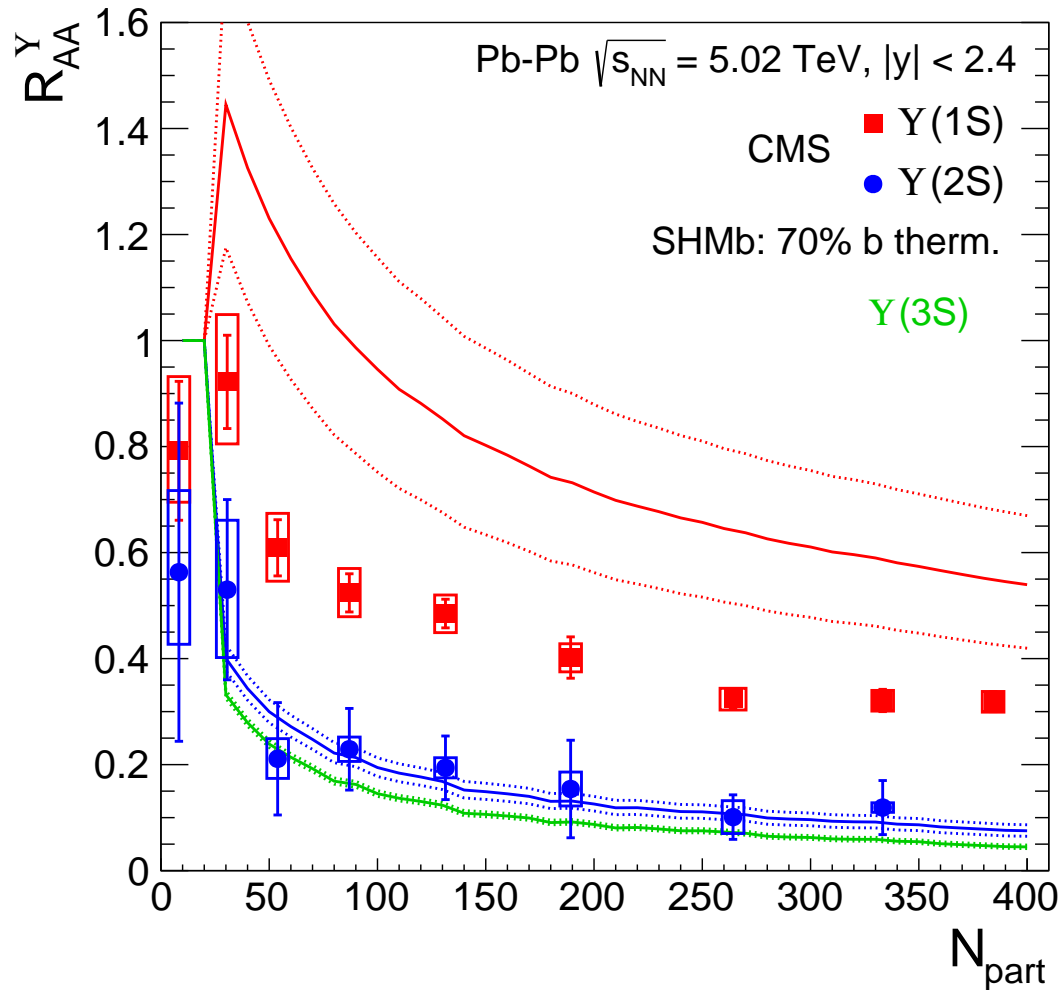
ALICE, [PLB 822 \(2021\) 136579](#)

Clearly, full beauty thermalization seems not realized in nature

R_{AA} , 70% $b\bar{b}$ thermalized

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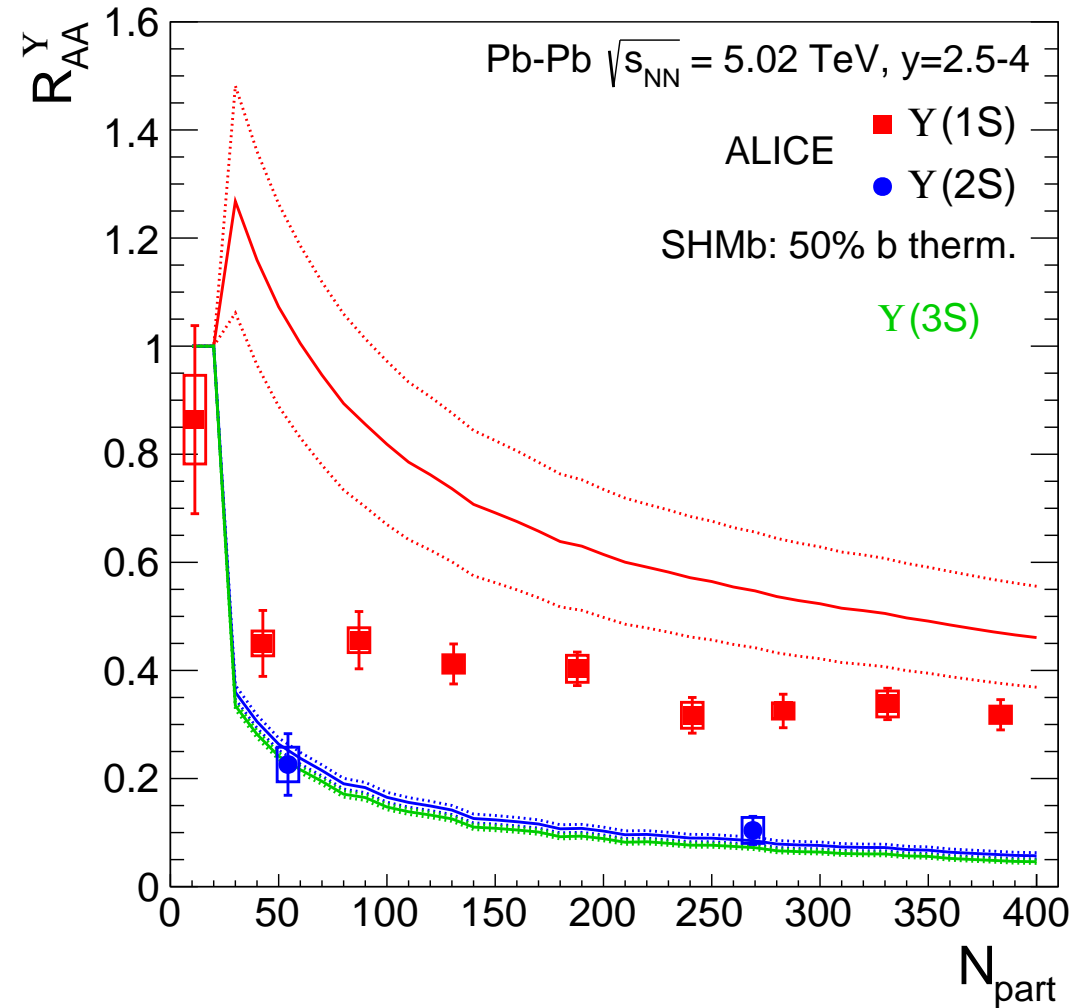
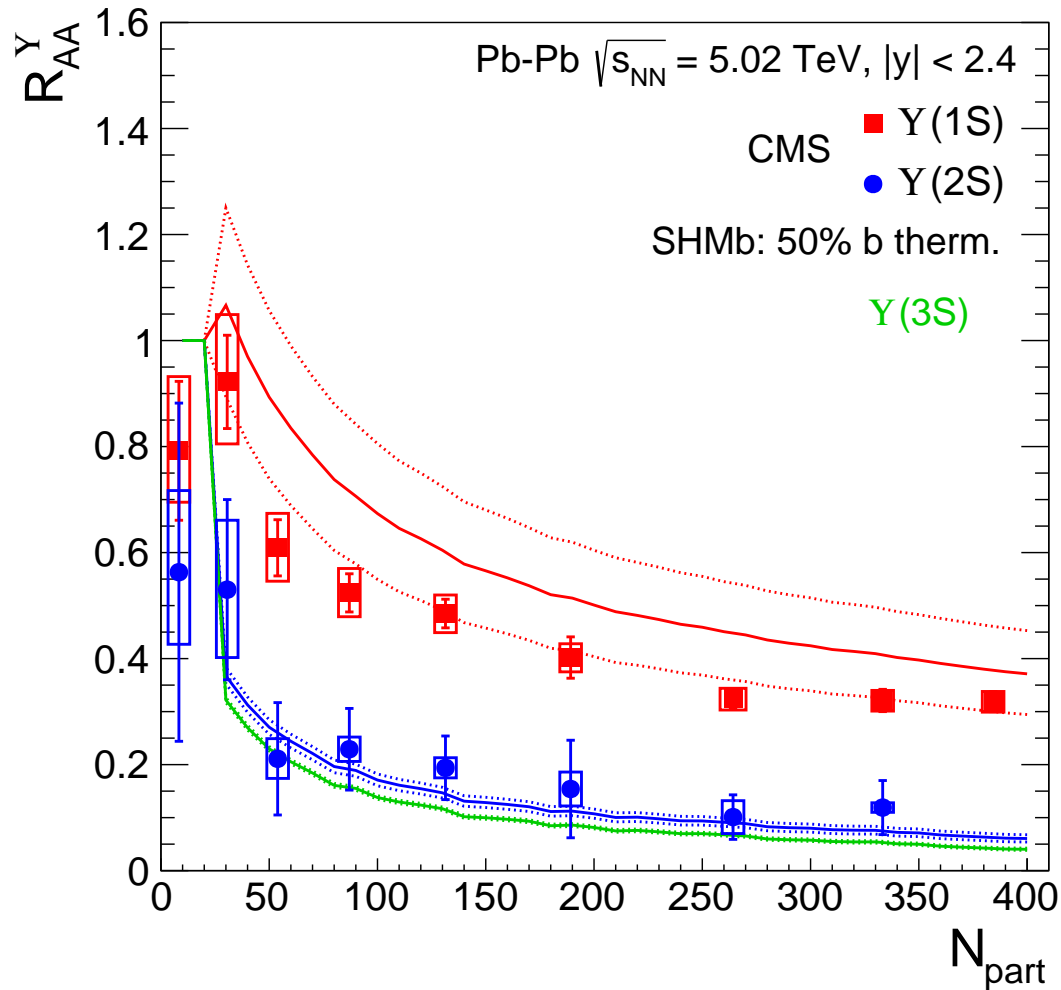
CMS, PRL 120 (2018) 142301

ALICE, PLB 822 (2021) 136579

R_{AA} , 50% $b\bar{b}$ thermalized

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CMS, PRL 120 (2018) 142301

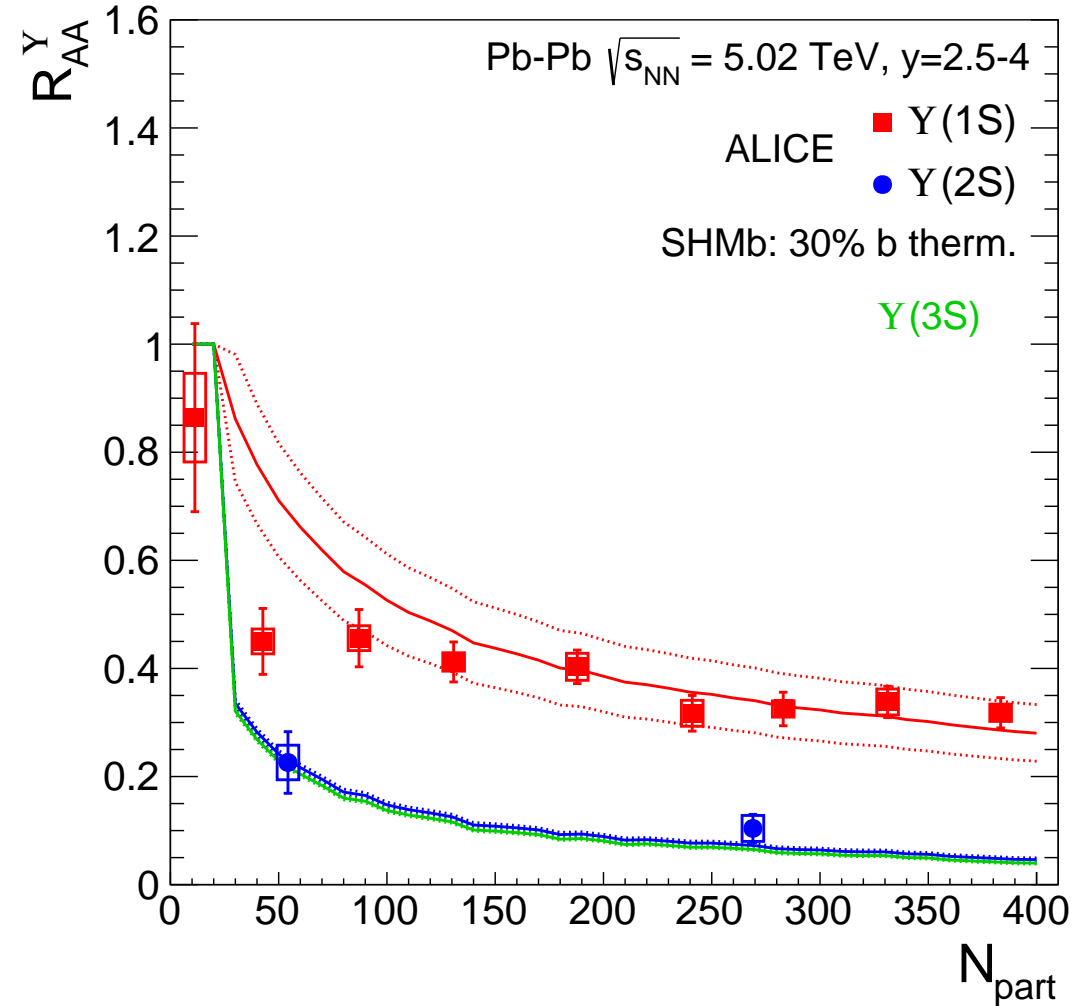
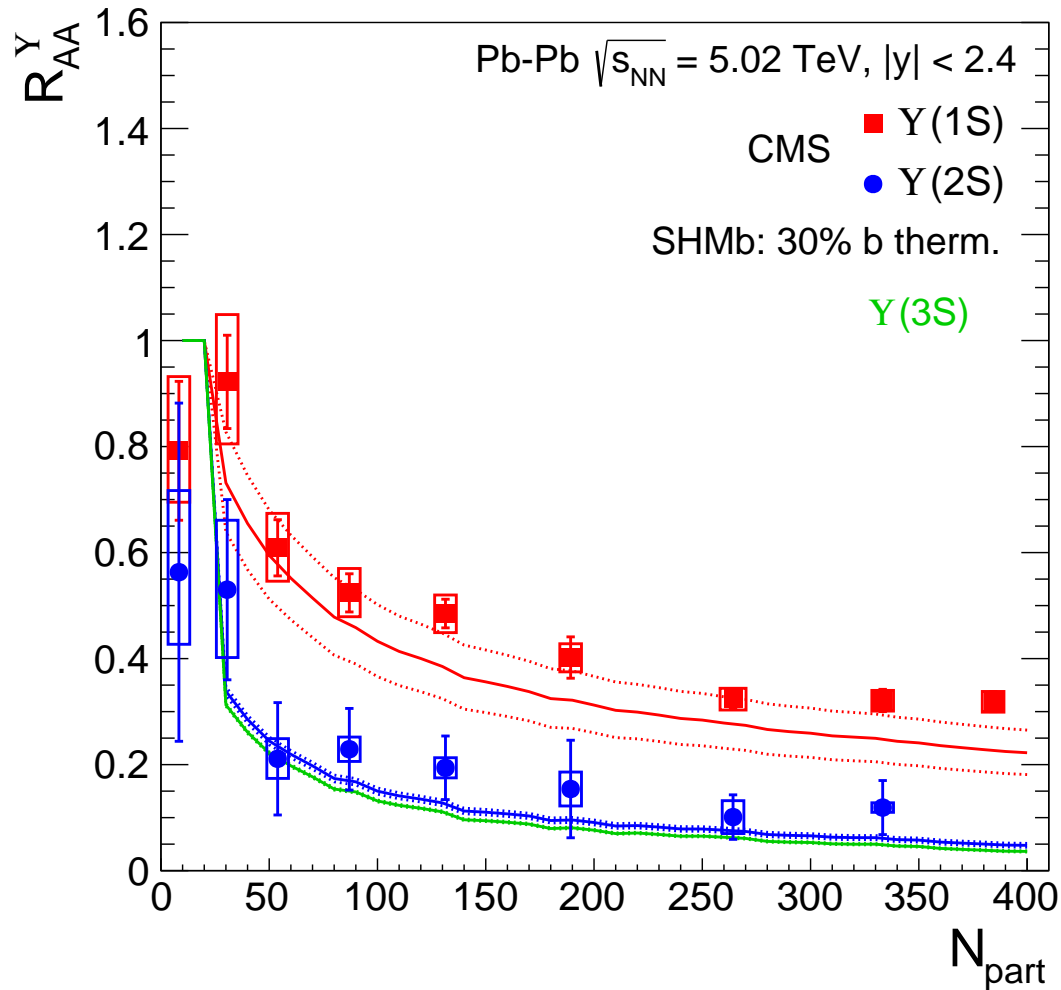
ALICE, PLB 822 (2021) 136579

What does non-thermalized beauty produce? (no room for it in SHMb)

R_{AA} , 30% $b\bar{b}$ thermalized

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CMS, PRL 120 (2018) 142301

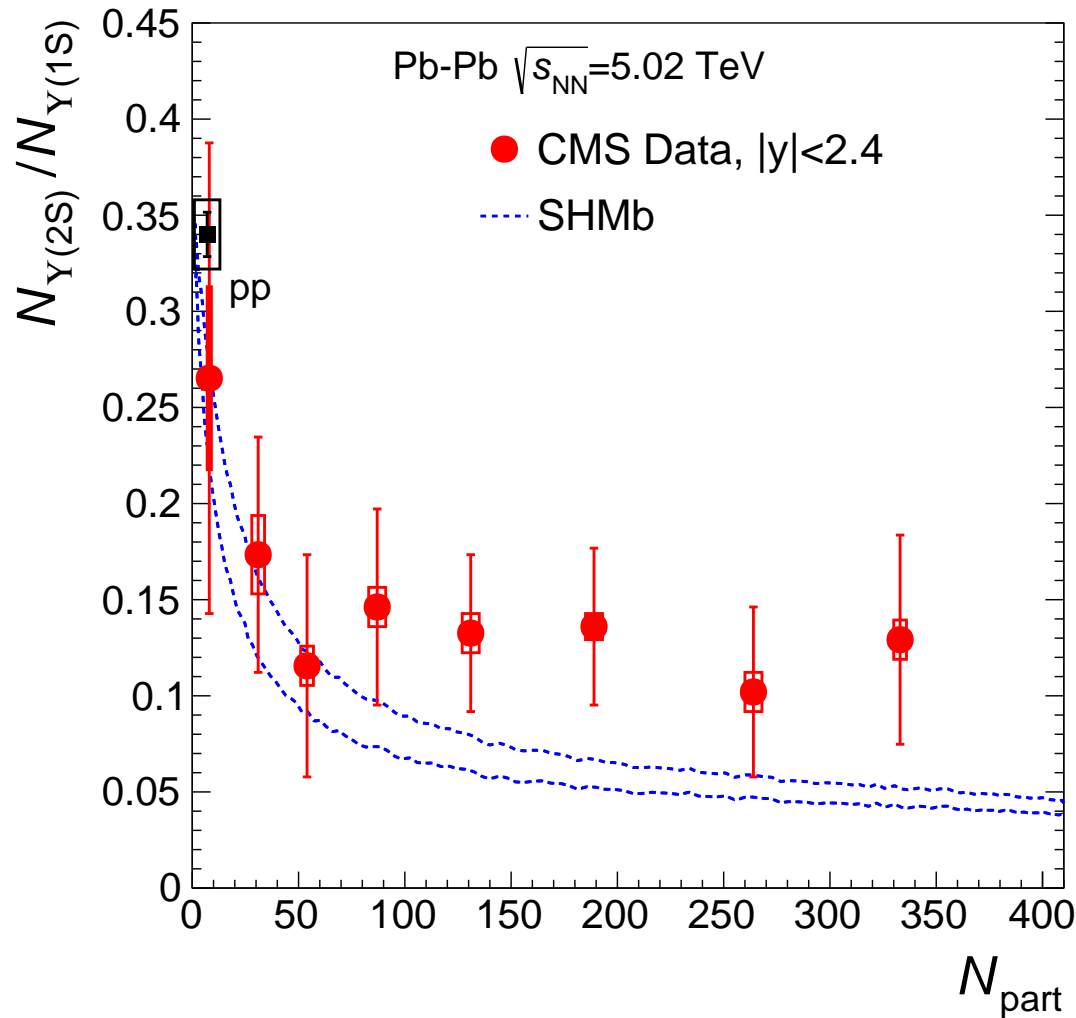
ALICE, PLB 822 (2021) 136579

What does non-thermalized beauty produce? (no room for it in SHMb)

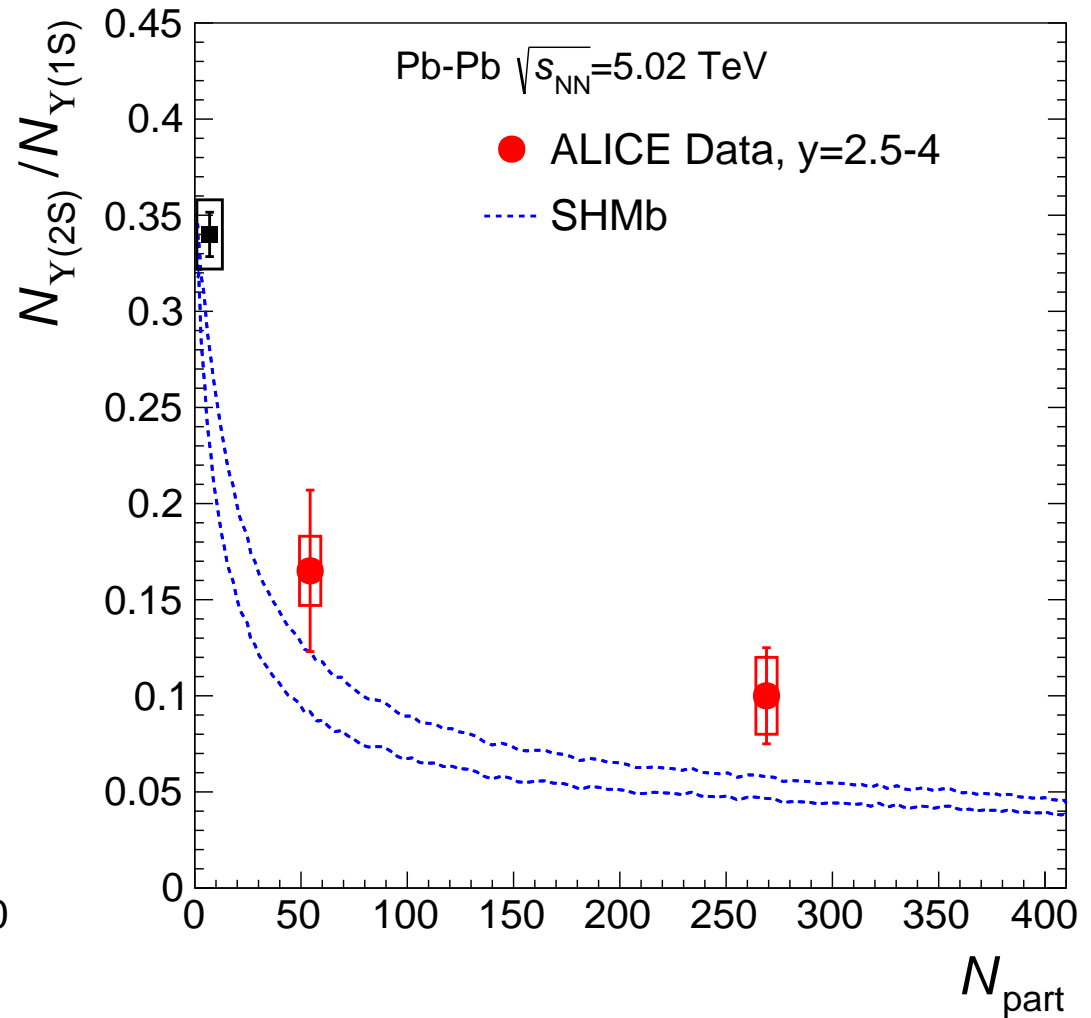
$\Upsilon(2S)/\Upsilon(1S)$ ratio (100% b thermalization)

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CMS, PRL 120 (2018) 142301



ALICE, PLB 822 (2021) 136579

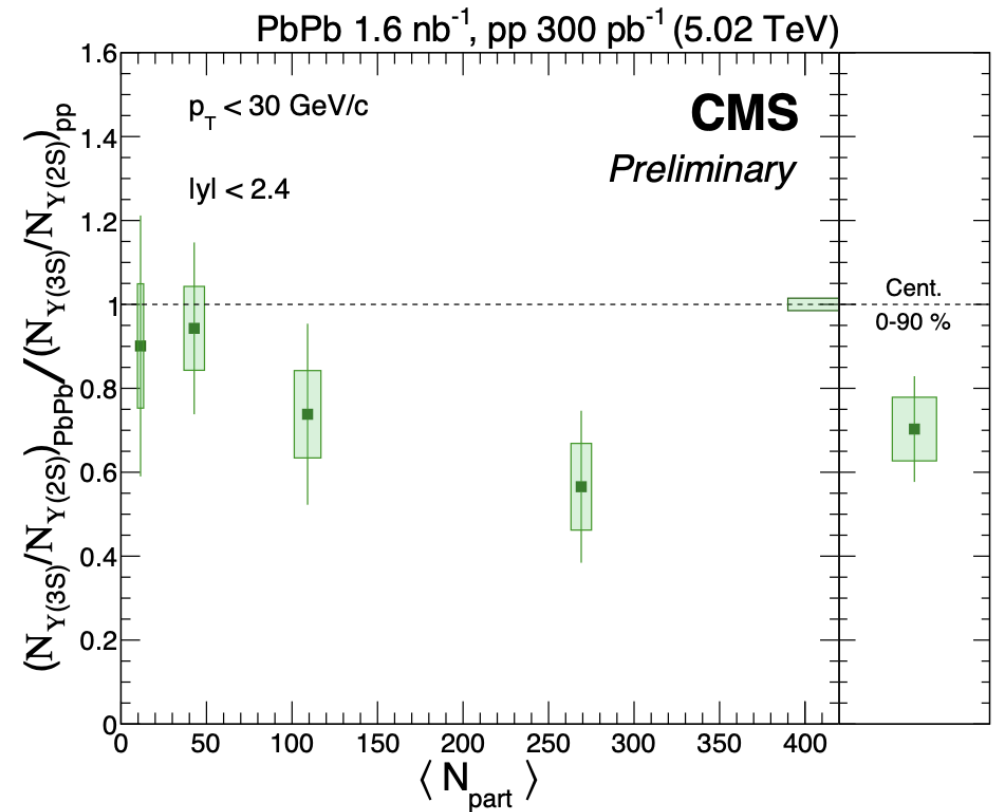
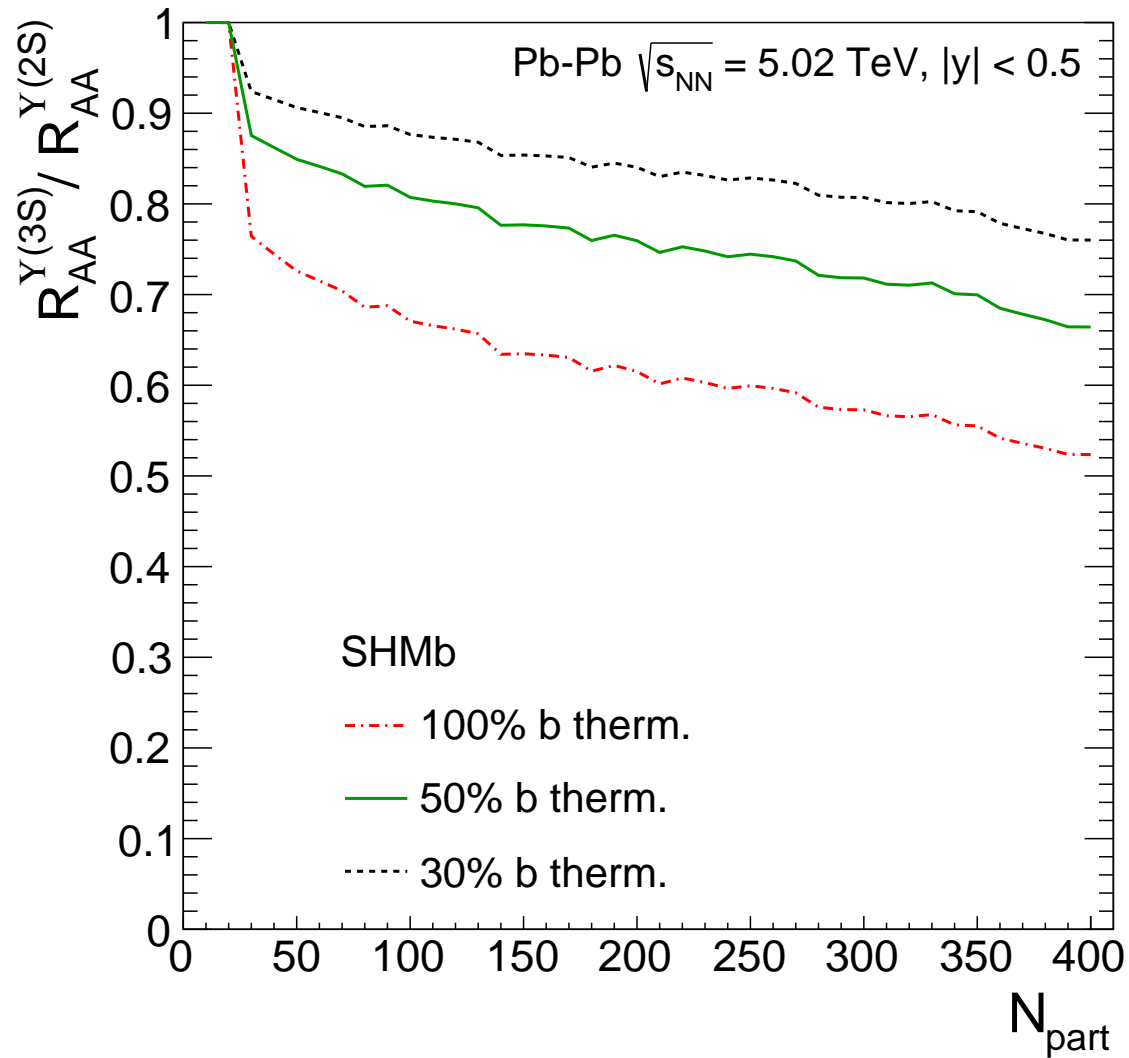
ALICE pp: $\Upsilon(2S)/\Upsilon(1S) = 0.5 \pm 0.1$, [arXiv:2109.15240](https://arxiv.org/abs/2109.15240)

SHMb uncert.: corona (fraction)

$\Upsilon(3S)/\Upsilon(2S) R_{AA}$ ratio

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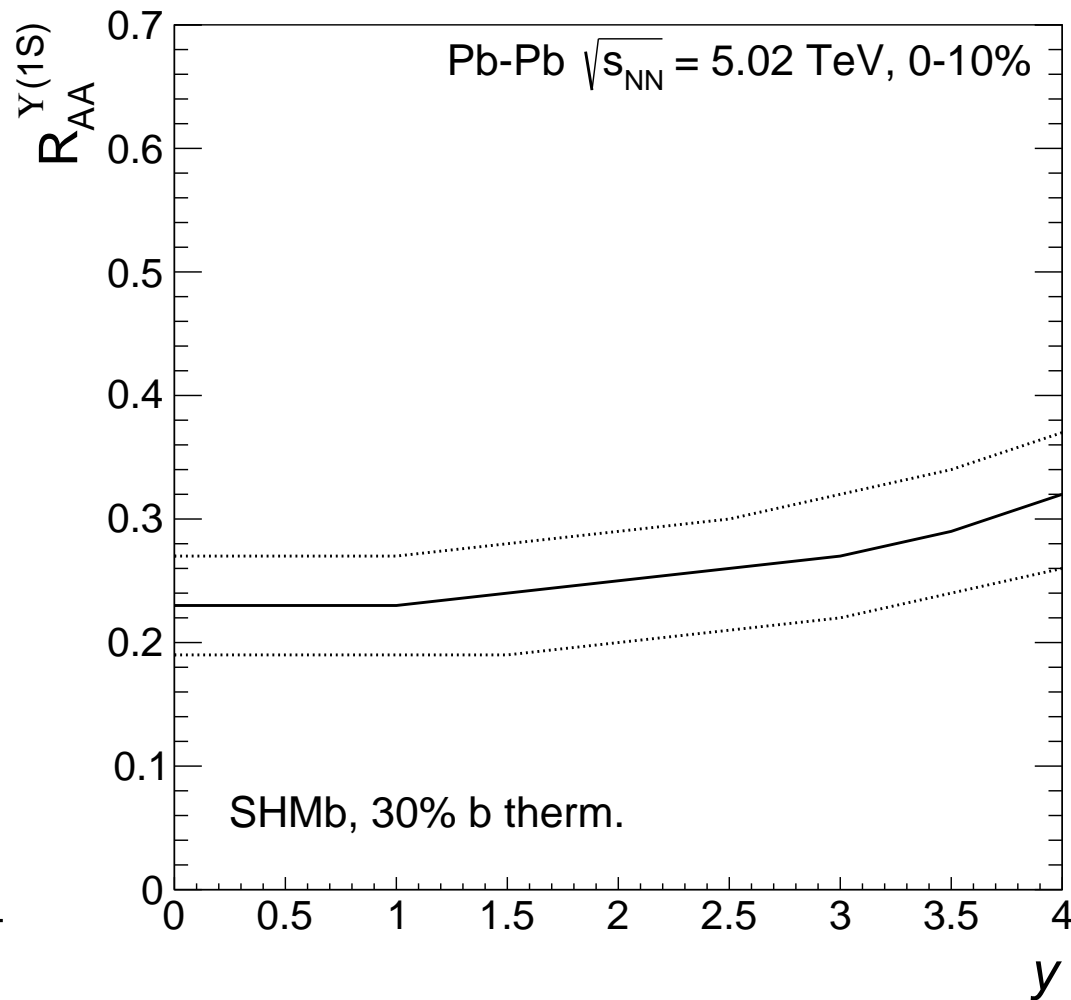
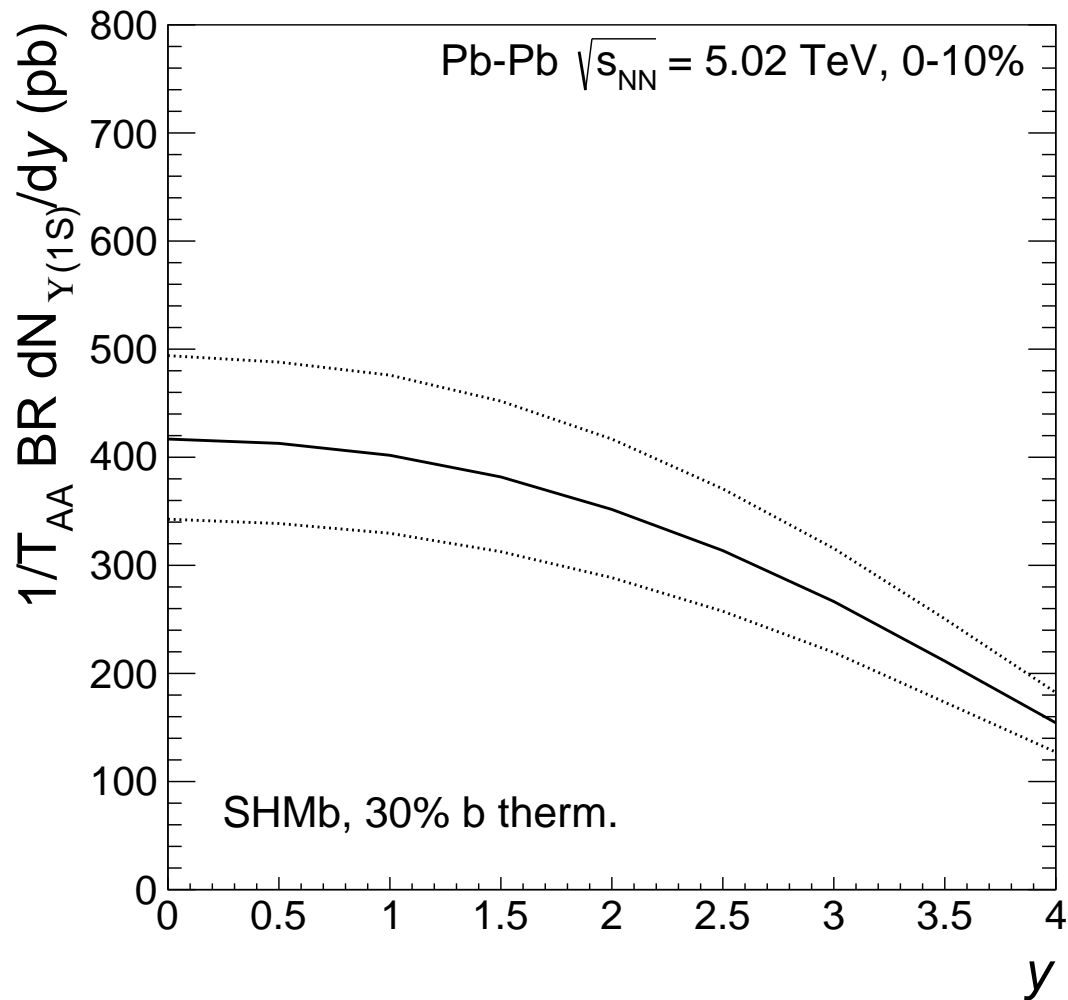
CMS, QM'22, [HIN-21-007](#)

The $\Upsilon(3S)/\Upsilon(2S) R_{AA}$ ratio is quite sensitive to the degree of b thermalization

Rapidity dependence $\Upsilon(1S)$, 30% $b\bar{b}$ thermalized

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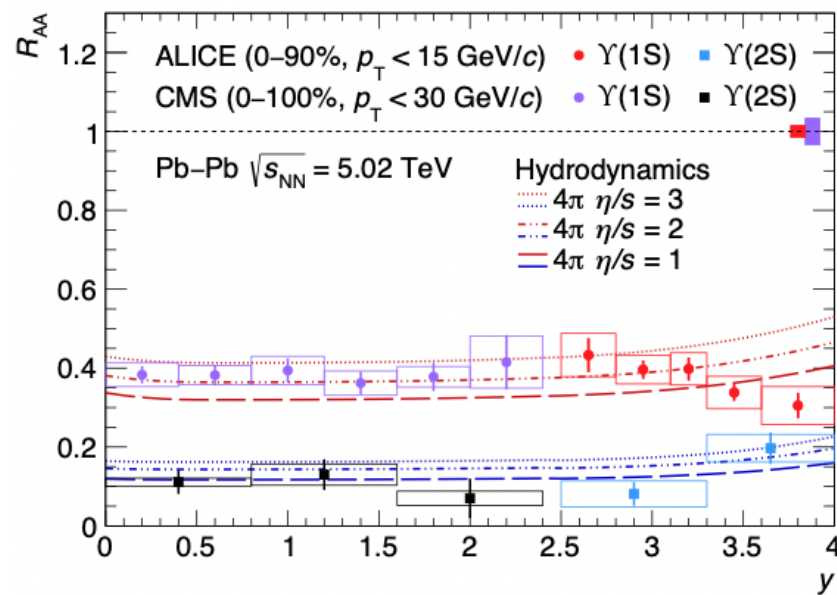
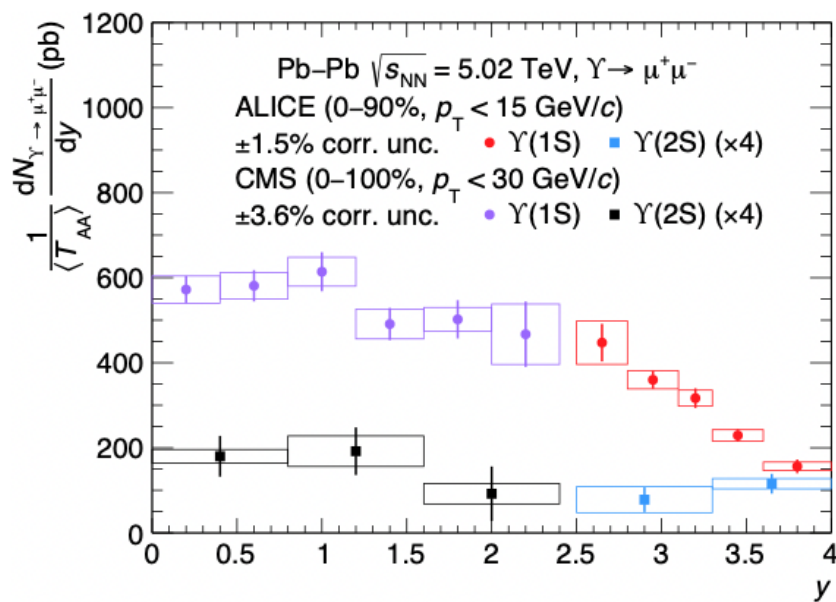
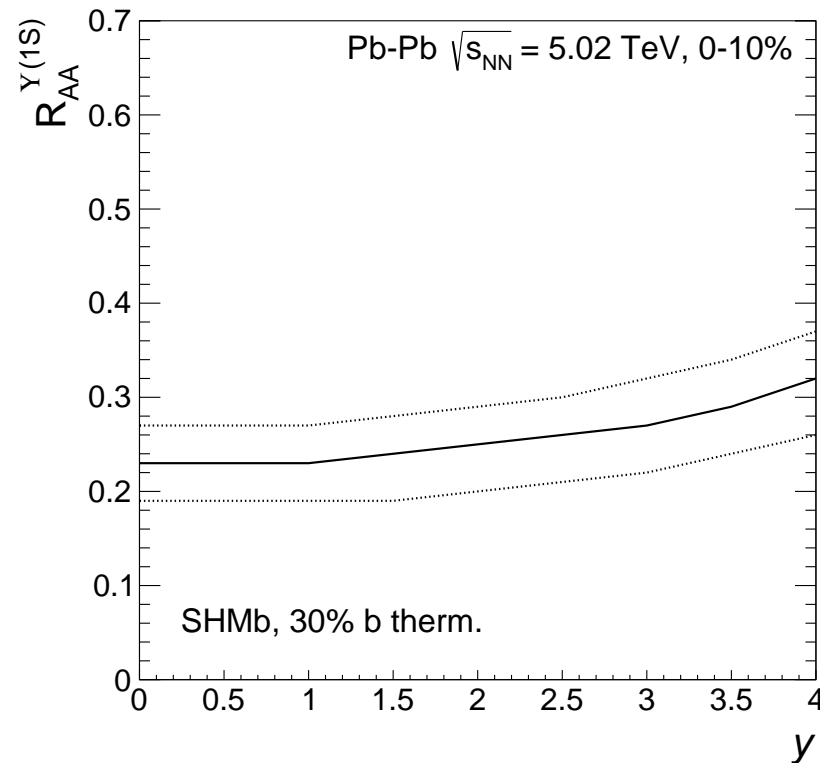
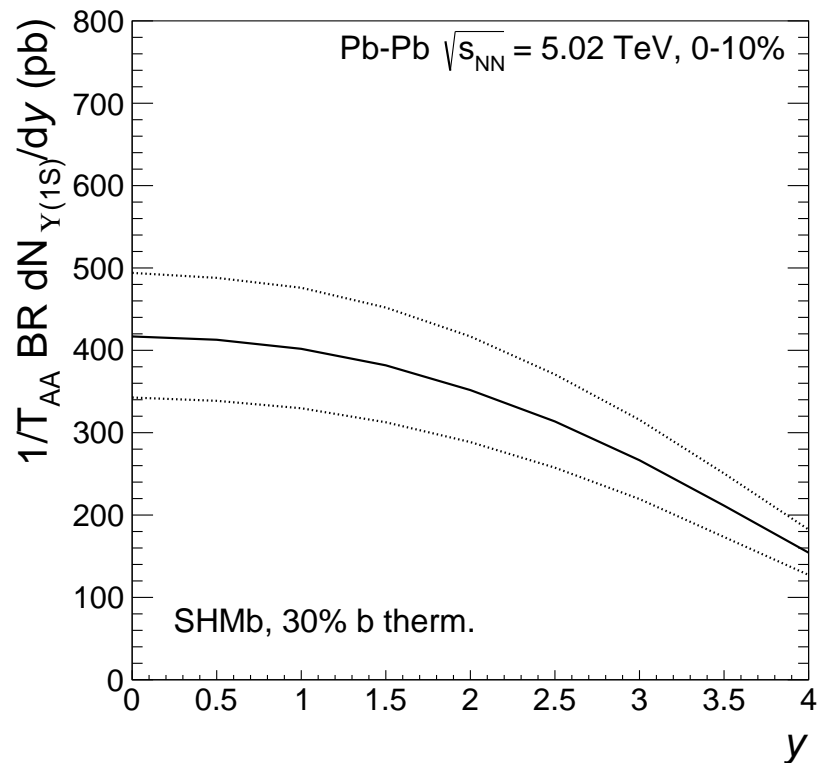


Data available only centrality-integrated ...is 0-10% (or 0-20%) doable?

Rapidity dependence $\Upsilon(1S)$, 30% $b\bar{b}$ thermalized

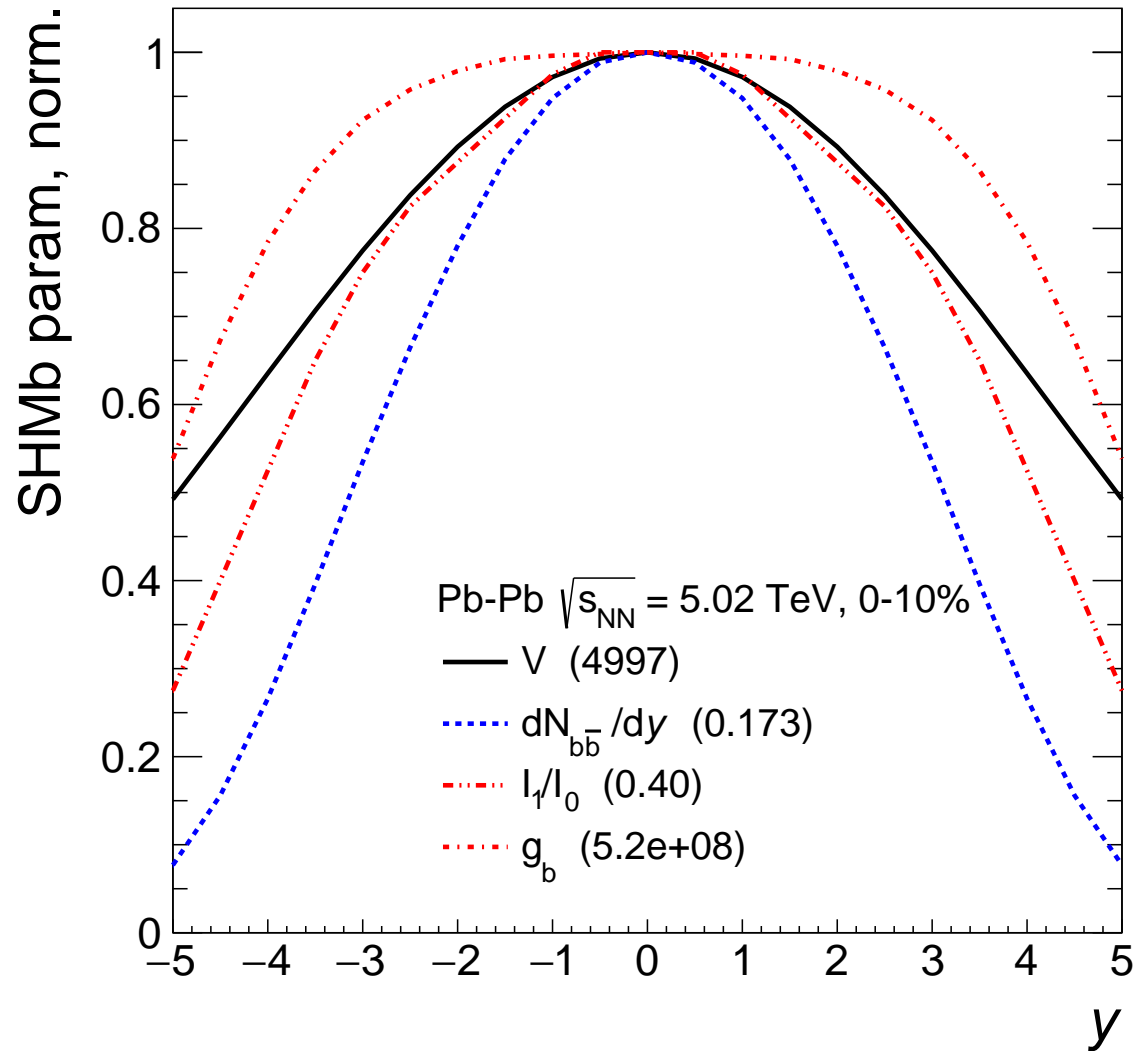
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SHMb parameters

NB: none is a free parameter, except the 30% b thermalization fraction



Summary and conclusions

- SHMb can predict the full suite of beauty hadrons
- Full beauty thermalization seems not realized in nature
...with 30-50% of beauty quarks fully thermalized we can explain the Υ data
- What does non/partially-thermalized beauty produce?
no Υ because strong coupling with the medium destroys the $b\bar{b}$ correlation?
...related: is there non-screened bottomonium at all? (...or maybe just $\Upsilon(1S)$?)
- Another difficulty: $R_{AA}^{Y(1S)}(p_T)$ is flat (we would predict a bump), v_2 is small
similar to Reygers et al., [PRC 101 \(2020\) 064905](#)

forthcoming LHC data will (hopefully) clarify these questions (...in a while)