



# Equilibration of QCD plasmas at finite net-baryon density

Quark Matter 2022

April. 6th, 2022

**Kraków Poland** + **Cyberspace**

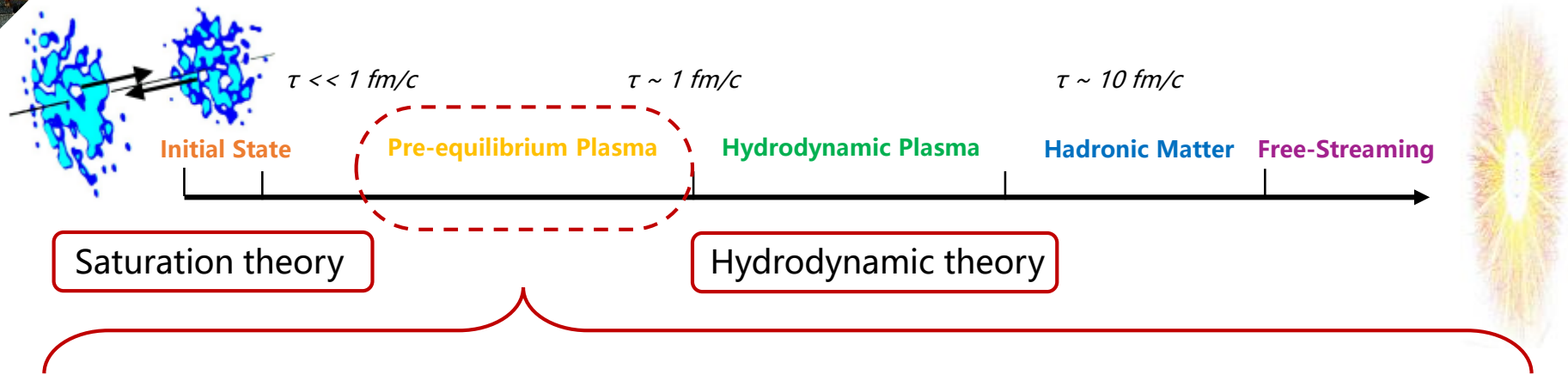
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# Initial stage in HICs



## QGP equilibration in HICs

- Connects initial condition to equilibrium states
  - Off-thermal initial states into near-thermal hydrodynamic states
  - Gluon saturated fields into quark-gluon plasma

## Kinetic Theory description of QGP equilibration

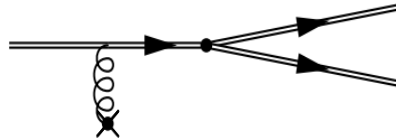
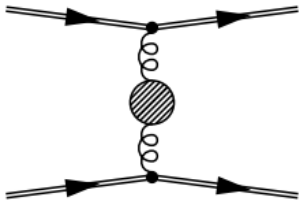
- Mechanism to thermalize states (kinetic equilibration)
- Include both gluon + quark degrees of freedom (chemical equilibration)

# QCD Effective Kinetic Theory

## First principle QCD Effective Kinetic Theory

$$\left(\frac{\partial}{\partial\tau} - \frac{p_{\parallel}}{\tau} \frac{\partial}{\partial p_{\parallel}}\right) f_a(\tau, p_T, p_{\parallel}) = -C_a^{2\leftrightarrow 2}[f](\tau, p_T, p_{\parallel}) - C_a^{1\leftrightarrow 2}[f](\tau, p_T, p_{\parallel})$$

- Gluon + all light quark/antiquark (finite net-baryon density)  $a = g, u, \bar{u}, d, \bar{d}, s, \bar{s}$
- LO  $2\leftrightarrow 2$  elastic scatterings &  $1\leftrightarrow 2$  inelastic scatterings



Arnold, Moore, Yaffe, JHEP01 (2003) 030  
Arnold, Moore, Yaffe, JHEP0206 (2002) 030  
Kurkela, Mazeliauskas, PRD99 (2019) 054018

## Application to HICs

- Boost-invariant simulation with Bjorken flow at pre-equilibrium stage of HICs
- Color Glass Condensate inspired initial state (over-occupied & gluon saturated)

XD, Schlichting, PRD104(2021)054011  
XD, Schlichting, PRL127(2021)122301



# Hydrodynamization of QGP

## Kinetic equilibration

- First-order hydrodynamics

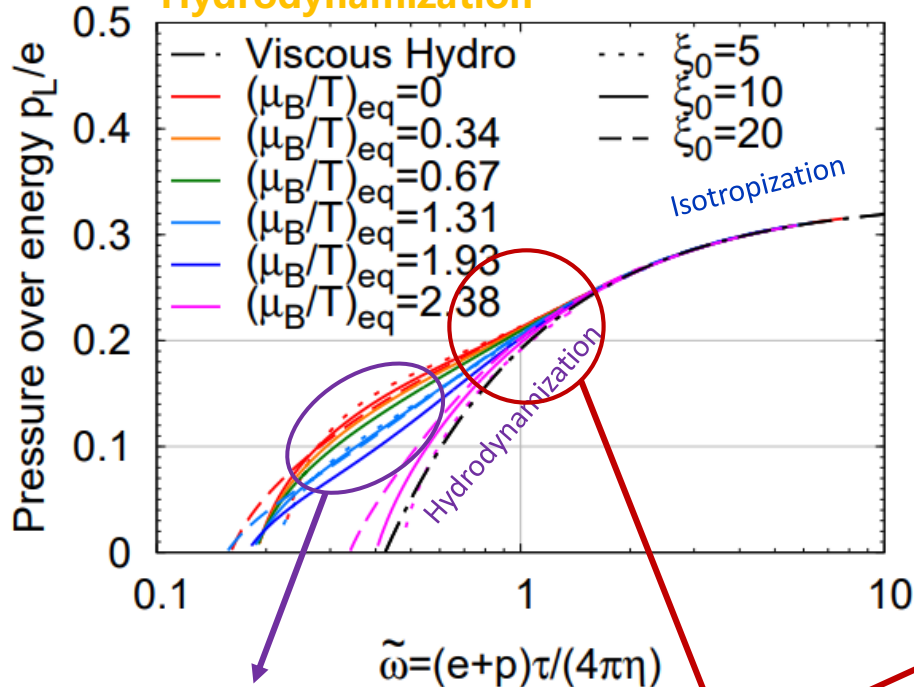
$$\frac{p_L}{e} = \frac{1}{3} - \frac{4}{9\pi\tilde{\omega}} \quad \tilde{\omega} = \frac{(e+p)\tau}{4\pi\eta}$$

Universal time scale

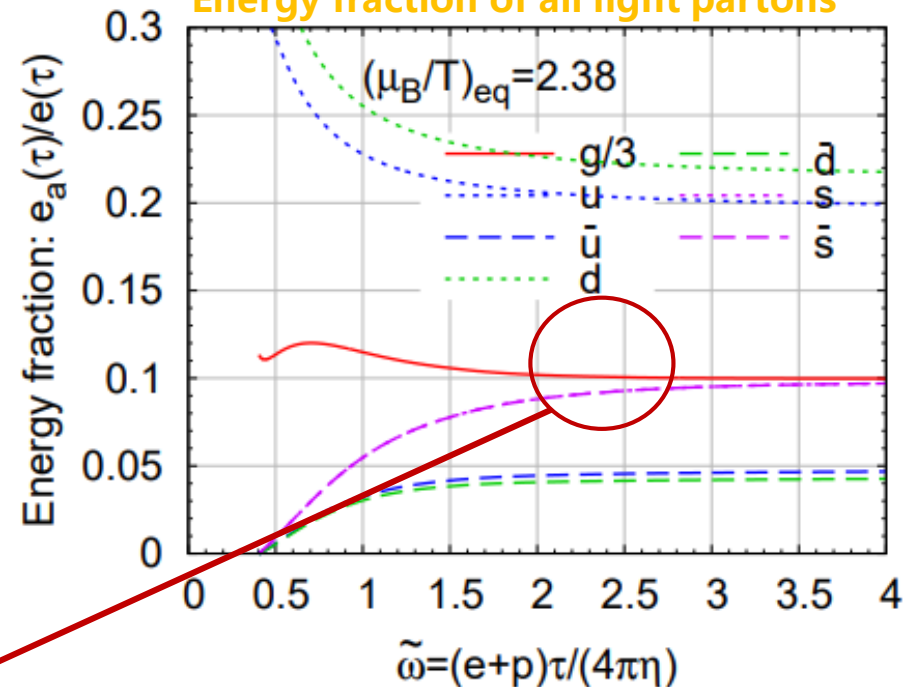
## Chemical equilibration

- Fractions of gluon/quark/antiquark evolve to equilibrium value

### Hydrodynamization



### Energy fraction of all light partons



Quarks slow down equilibration

Chemical equilibration persists after kinetic equilibration (hydrodynamization)

XD, Schlichting, PRL127(2021)122301

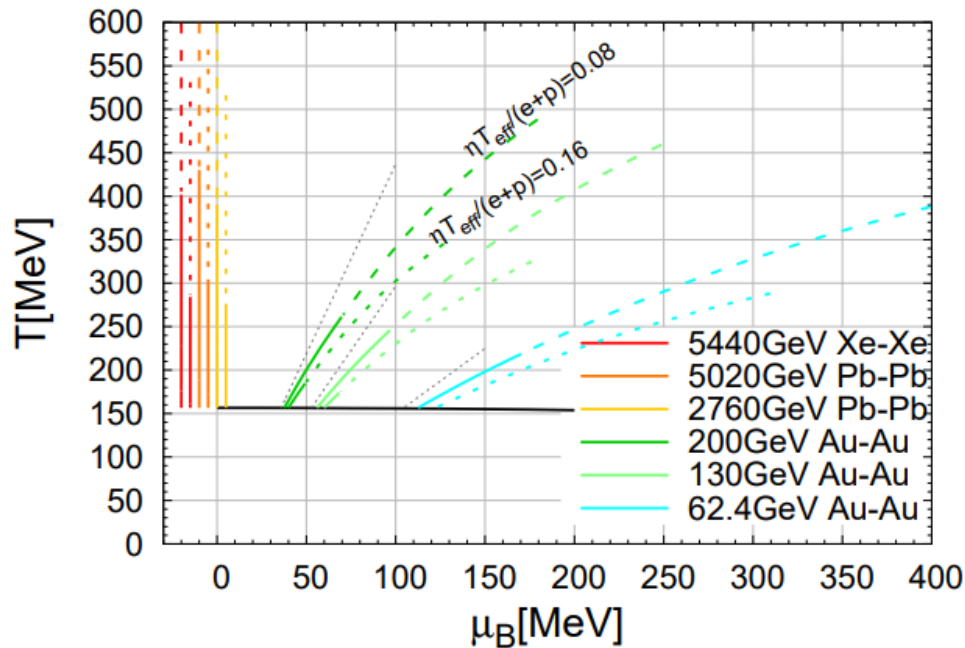
# Pre-equilibrium QGP in HICs

## Pre-equilibrium QGP evolution

- Pre-equilibrium description connects initial states to hydrodynamics in HICs

$$(\tau^{4/3} e)_{\tilde{\omega}} = \left( 4\pi \frac{\eta T_{\text{eff}}}{e + p} \right)^{\frac{4}{9}} \left( \frac{\pi^2}{30} v_{\text{eff}} \right)^{\frac{1}{9}} (\tau e)_0^{\frac{8}{9}} C_{\infty} \mathcal{E}(\tilde{\omega})$$

$$(\tau \Delta n_f)_{\tilde{\omega}} = (\tau \Delta n_f)_0$$



QGP trajectory in QCD T-μ diagram

## More phenomenology

- Chemical equilibration important

### Quark production

before or even during hydro period

- Electromagnetic probes in pre-equilibrium stage, see

M. Coquet

Poster Session 2 T05 / T13 Apr 6

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# Conclusions & Outlook

## Conclusions:

- We develop a QCD kinetic solver at finite net-baryon density
- We discuss both kinetic and chemical equilibration of QGP in HICs
- Chemical equilibration is essential to phenomenology in the early stage of HICs

## Outlook:

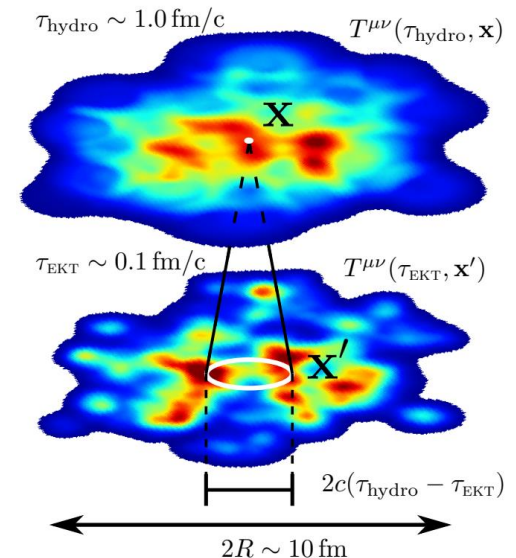
### Propagation of space-time perturbation

- Linearized Effective Kinetic Theory to calculate energy-momentum tensor

$$T^{\mu\nu}(\tau_{\text{EKT}}, \mathbf{x}') = \underbrace{\bar{T}_{\mathbf{x}}^{\mu\nu}(\tau_{\text{EKT}})}_{\substack{\text{Background} \\ \text{EKT}}} + \underbrace{\delta T_{\mathbf{x}}^{\mu\nu}(\tau_{\text{EKT}}, \mathbf{x}')}_{\substack{\text{Perturbation} \\ \text{Linearized EKT}}}$$

- Charge fluctuation in QCD plasma

XD, Schlichting, in progress







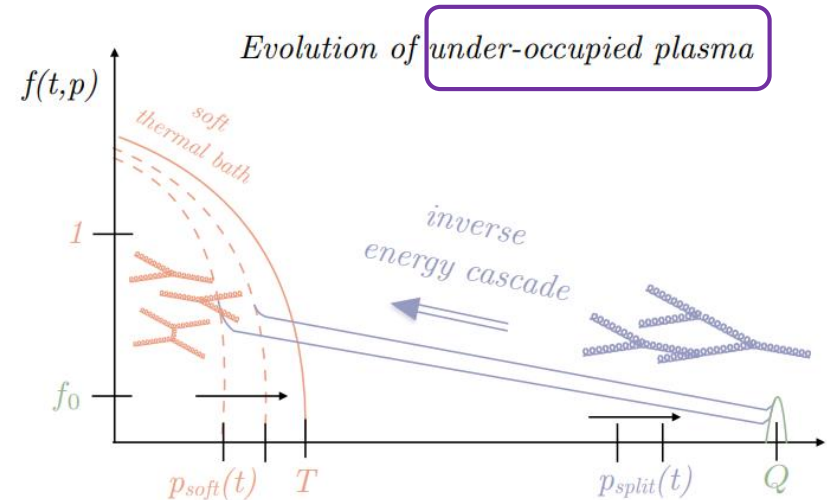
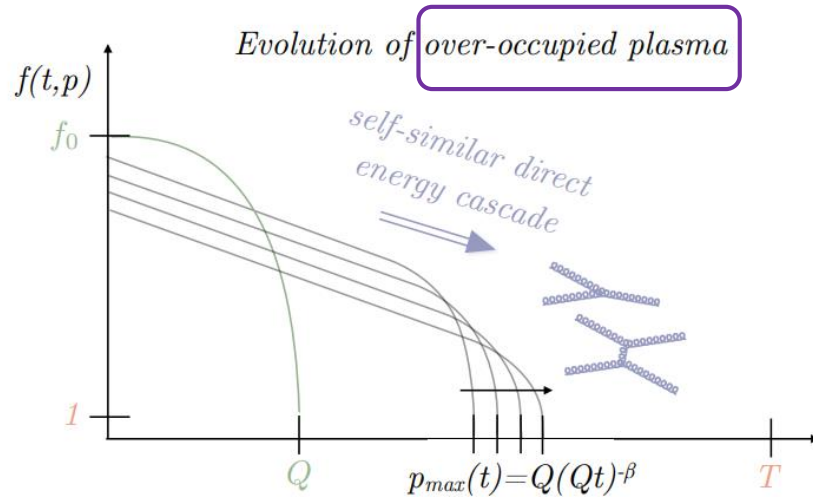
# **Supplementary slides**

Turbulence



# Equilibration of QCD plasmas

## Two typical far-from-equilibrium systems



### Over-occupied plasma

- Separation of scale

$$\langle p \rangle_0 \ll T$$

- Direct energy cascade

low  $\rightarrow$  high momentum

- Initial state in HICs

### Under-occupied plasma

- Separation of scale

$$\langle p \rangle_0 \gg T$$

- Inverse energy cascade

high  $\rightarrow$  low momentum

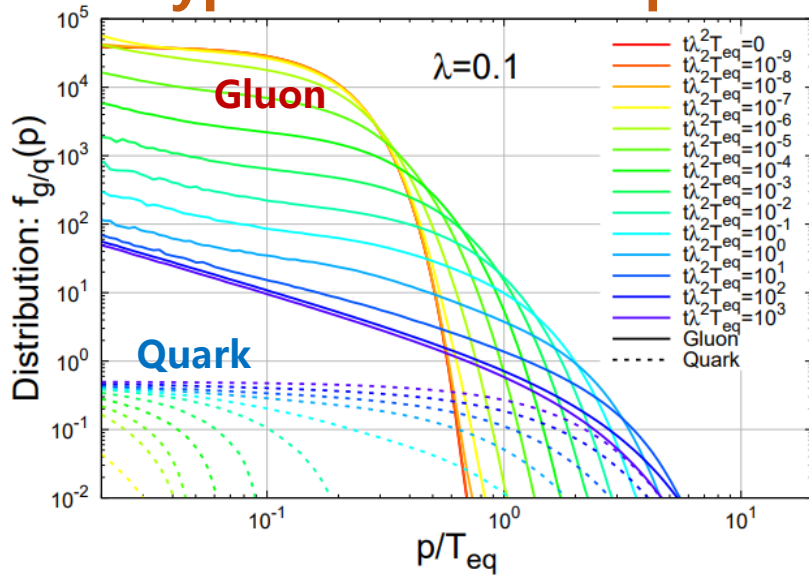
- Jets in HICs

Schlichting, Teaney, ARNPS 69 (2019) 447



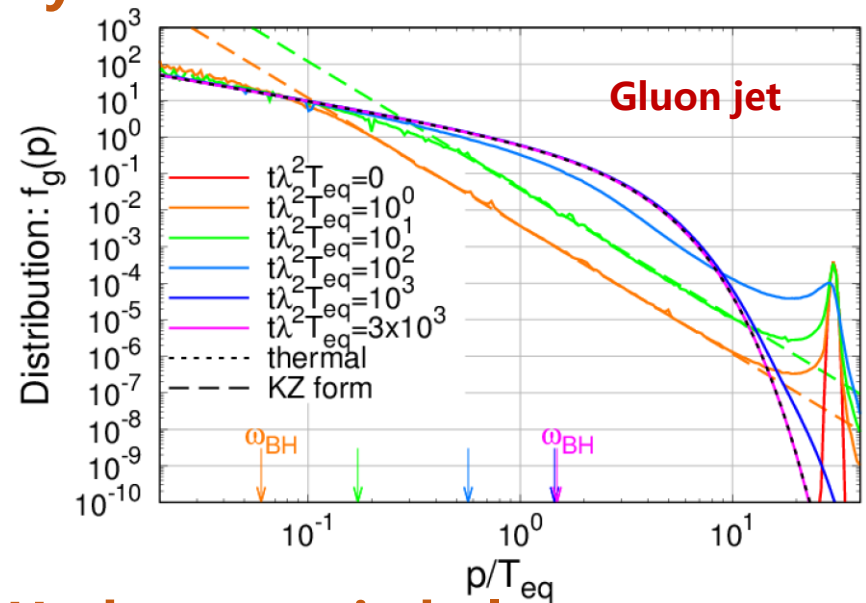
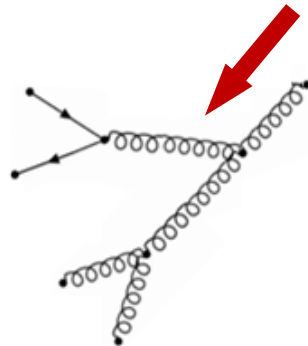
# Equilibration of QCD plasmas

## Two typical far-from-equilibrium systems



### Over-occupied plasma

- Self-similar evolution of QCD plasma



### Under-occupied plasma

- Kolmogorov-Zakharov spectrum (orange, green)

- Bottom-up thermalization

XD, Schlichting, PRD104(2021)054011