

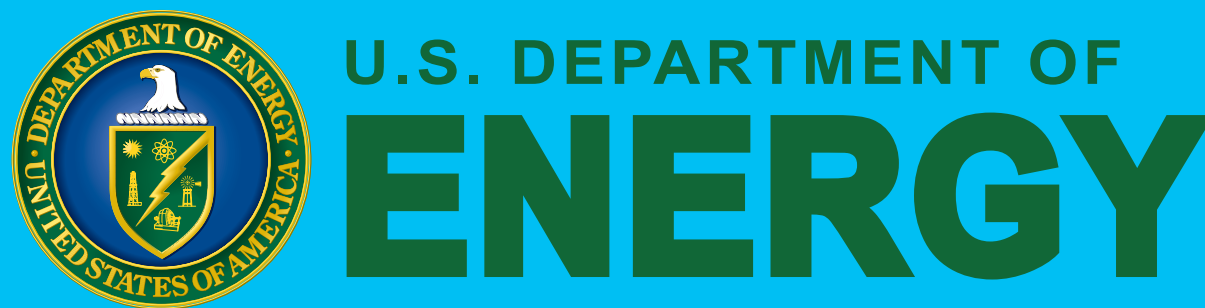
# ACCESSING SATURATION AND SUBNUCLEAR STRUCTURE WITH MULTIPLICITY DEPENDENT J/ $\psi$ PRODUCTION IN p+p AND p+Pb COLLISIONS

29TH INTERNATIONAL  
CONFERENCE ON ULTRA-  
RELATIVISTIC NUCLEUS-  
NUCLEUS COLLISIONS

APRIL 8, 2022  
KRAKÓW, POLAND

BJÖRN SCHENKE, BROOKHAVEN NATIONAL LABORATORY

BASED ON: F. SALAZAR, B. SCHENKE, A. SOTO-ONTOSO, PHYS.LETT.B 827 (2022) 136952, E-PRINT: 2112.04611



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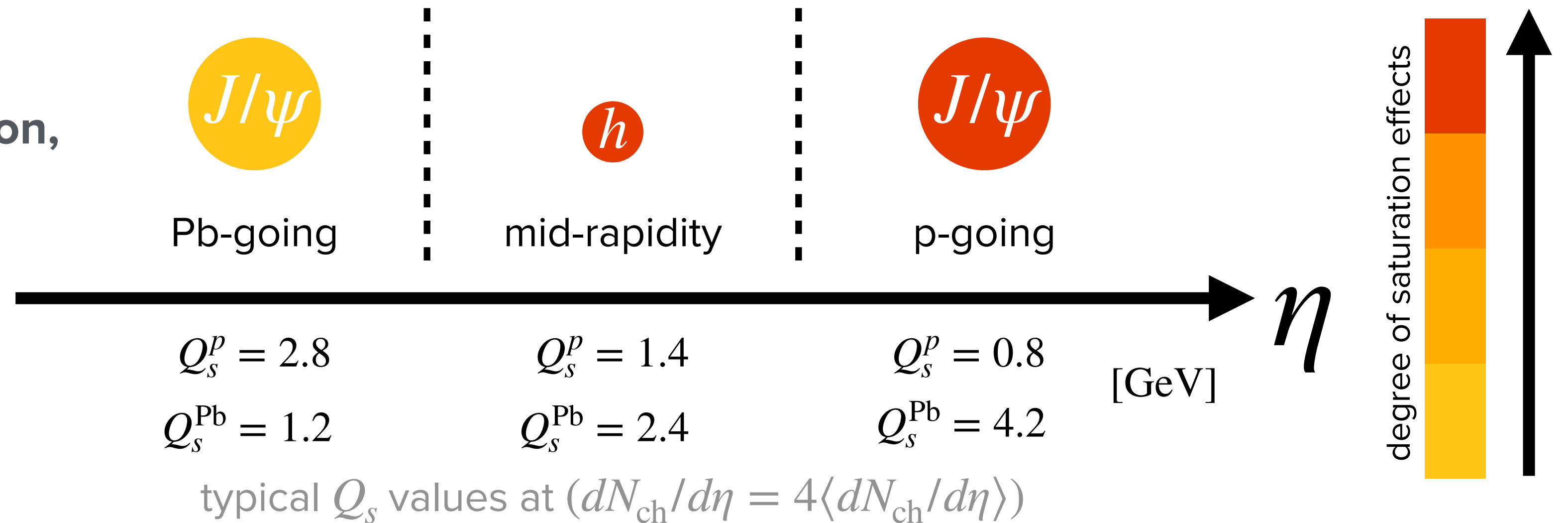
# SCANNING SATURATION WITH $J/\psi$ AND $h_c$

Study production of  $J/\psi$  at different rapidities relative to charged hadrons at midrapidity

Expect varying sensitivity to saturation, depending on probed  $Q_s$  and mass:

$$J/\psi \quad m_{J/\psi} = 3.1 \text{ GeV}$$

$$h \quad m_{h_c} \approx 0.5 \text{ GeV}$$



Most important physics in  $Q_s^2(x, \mathbf{R}_\perp) = T_A(\mathbf{R}_\perp) S_\perp Q_s^2(x)$ . Depends on rapidity ( $x$ ) and transverse space.

Spatial dependence in  $T_A(\mathbf{R}_\perp)$  includes fluctuations of nucleon positions and nucleon substructure:

3 hot spots locations per nucleon sampled from

$$P(\mathbf{R}_{\perp,i}) = \frac{1}{2\pi B_{qc}} e^{-R_{\perp,i}^2/(2B_{qc})} \quad \text{and hot spot density distribution} \quad T_q(\mathbf{R}_\perp - \mathbf{R}_{\perp,i}) = \xi_{Q_s^2} e^{-(\mathbf{R}_\perp - \mathbf{R}_{\perp,i})^2 / (2(\xi_{B_q}) B_q)}$$

fluctuating normalization

fluctuating size

# CHARGED HADRON AND J/ψ PRODUCTION

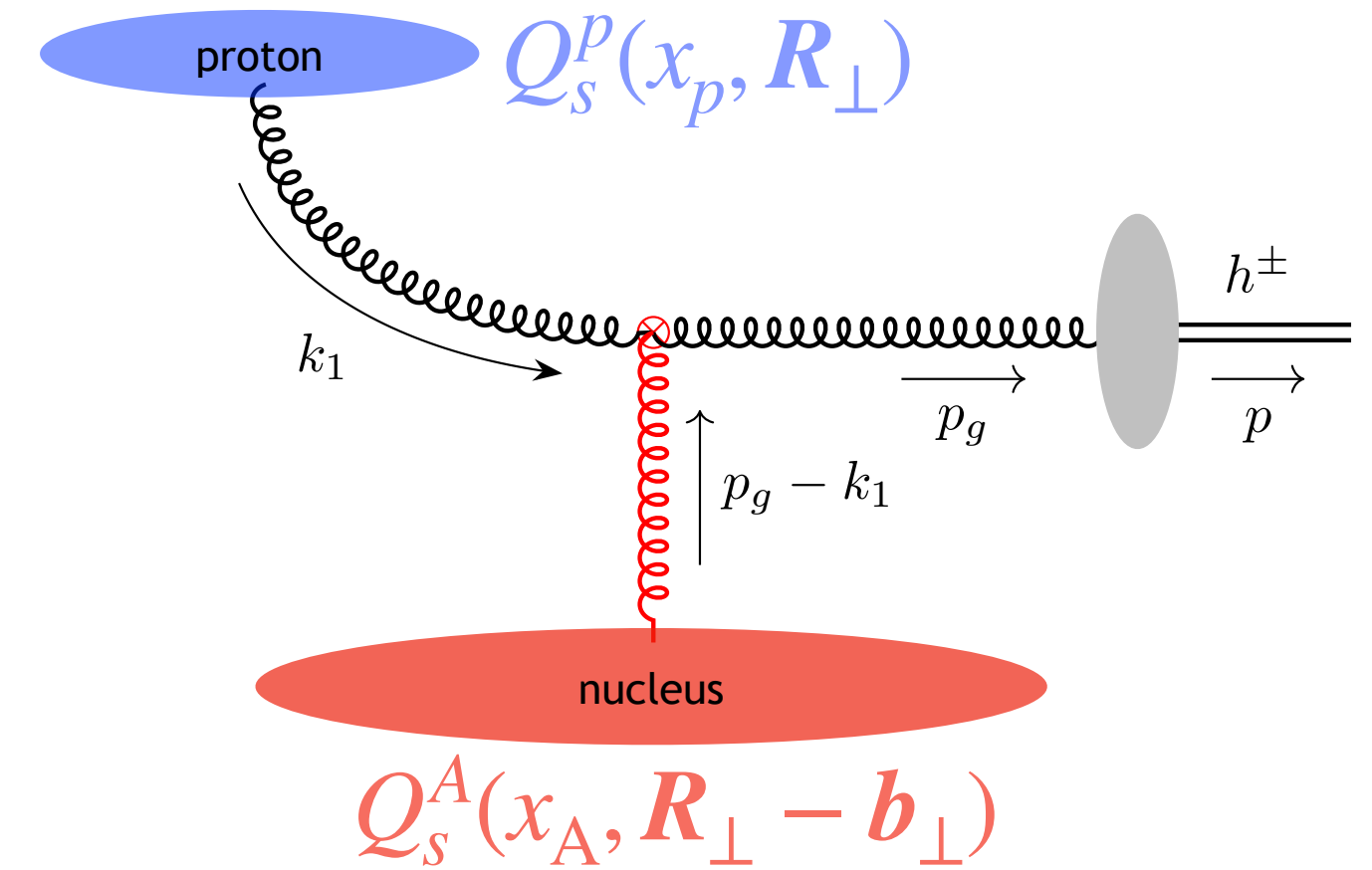
Use  $k_T$ -factorization for gluon production

Y. V. Kovchegov, K. Tuchin, Phys. Rev. D 65, 074026 (2002)  
J. P. Blaizot, F. Gelis, R. Venugopalan, Nucl. Phys. A743, 13 (2004)

$$\frac{dN_g(\mathbf{b}_\perp)}{d^2\mathbf{p}_{g\perp}dy_g} = \frac{\alpha_s}{(\sqrt{2}\pi)^6 C_F p_{g\perp}^2} \int_{k_{1\perp}, R_\perp} \phi^P(x_p; \mathbf{k}_{1\perp}; \mathbf{R}_\perp) \phi^A(x_A; \mathbf{p}_{g\perp} - \mathbf{k}_{1\perp}; \mathbf{R}_\perp - \mathbf{b}_\perp)$$

Unintegrated gluon distributions  $\phi^P$  and  $\phi^A$  (with  $A = p, Pb$ ) from BK evolution with McLerran-Venugopalan initial conditions + spatial dependence

Hadronize using **KKP fragmentation function**



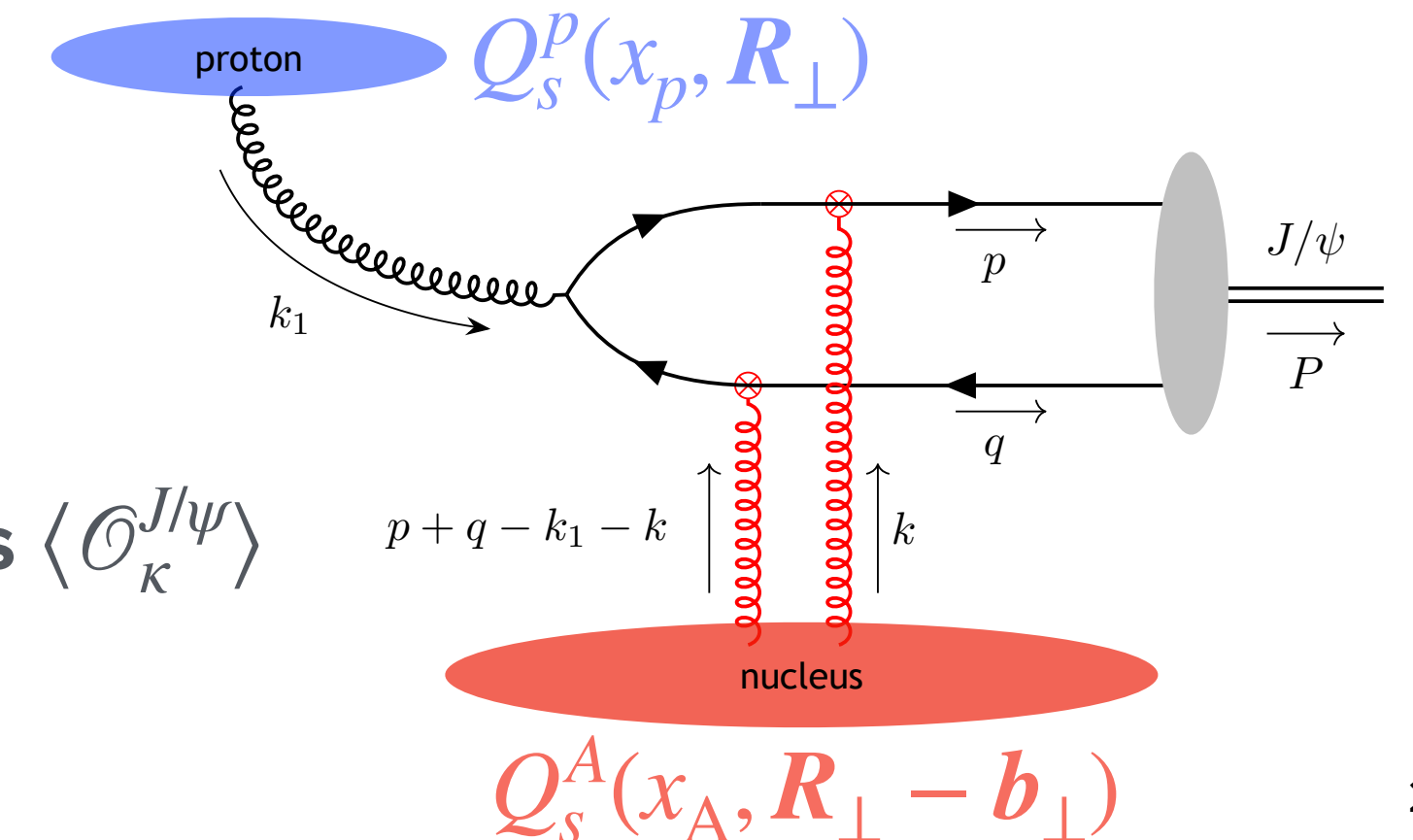
$c\bar{c}$ -pair production in NRQCD Z.-B. Kang, Y.-Q. Ma, and R. Venugopalan, JHEP 01, 056 (2014)

$$\frac{dN_{c\bar{c}}^\kappa(\mathbf{b}_\perp)}{d^2\mathbf{P}_\perp dY} = \frac{\alpha_s}{(2\pi)^9 (N_c^2 - 1)} \int_{k_{1\perp}, k_\perp, k'_\perp, R_\perp} \mathcal{H}^\kappa(\mathbf{P}_\perp - \mathbf{k}_{1\perp}, \mathbf{k}_\perp, \mathbf{k}'_\perp) \frac{\phi^P(x_p, \mathbf{k}_{1\perp}, \mathbf{R}_\perp)}{k_{1\perp}^2} \tilde{\Xi}^\kappa(x_A; \mathbf{P}_\perp - \mathbf{k}_{1\perp}, \mathbf{k}_\perp, \mathbf{k}'_\perp; \mathbf{R}_\perp - \mathbf{b}_\perp)$$

for quantum state  $\kappa$ . The pair momentum is  $\mathbf{P}_\perp = \mathbf{p}_\perp + \mathbf{q}_\perp$ ,  $\mathcal{H}^\kappa$  are the hard factors, and the  $\tilde{\Xi}^\kappa$  contain dipole amplitudes (related to  $\phi^A$ )

$$\frac{dN_{J/\psi}(\mathbf{b}_\perp)}{d^2\mathbf{P}_\perp dY} = \sum_\kappa \frac{dN_{c\bar{c}}^\kappa(\mathbf{b}_\perp)}{d^2\mathbf{P}_\perp dY} \langle \mathcal{O}_\kappa^{J/\psi} \rangle$$

with non-perturbative long distance matrix elements  $\langle \mathcal{O}_\kappa^{J/\psi} \rangle$

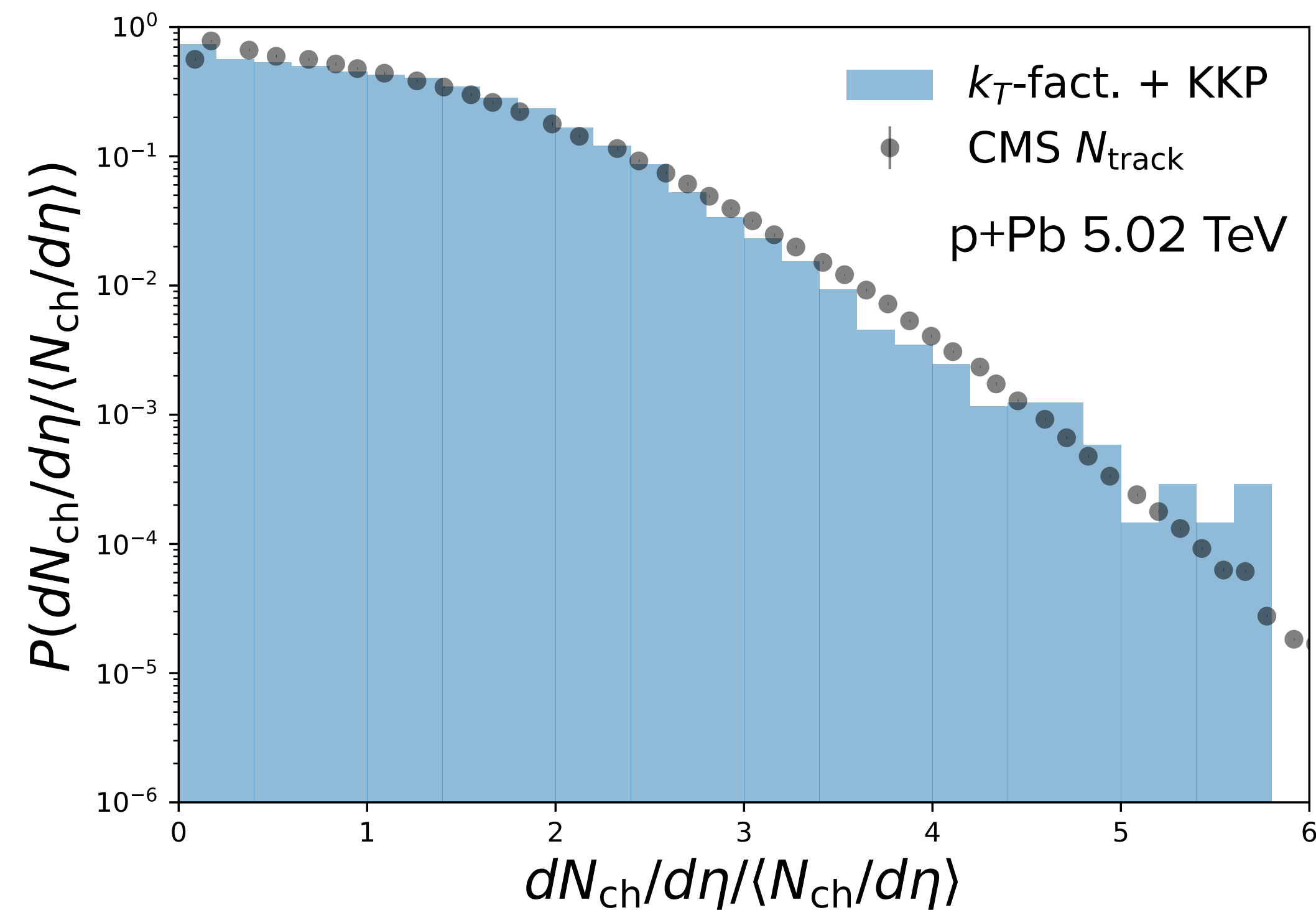


K.-T. Chao, Y.-Q. Ma, H.-S. Shao, K. Wang, Y.-J. Zhang, Phys. Rev. Lett. 108, 242004 (2012)  
Y.-Q. Ma, R. Venugopalan, H.-F. Zhang, Phys. Rev. D 92, 071901 (2015)

# RESULTS: FLUCTUATIONS

## Charged hadron multiplicity distribution

Experimental data: CMS Collaboration, Phys.Lett. B718, 795 (2013), <https://twiki.cern.ch/twiki/bin/view/CMSPublic/PhysicsResultsHIN12015>



Parameter	Value	Parameter	Value
$N_q$	3	$\alpha_s$	0.16
$B_{qc}$	$3 \text{ GeV}^{-2}$	$m_{\text{IR}}$	0.2 GeV
$B_q$	$1 \text{ GeV}^{-2}$	$m_{J/\psi}$	3.1 GeV
$\sigma_{B_q}$	0.7	$m_c$	$m_{J/\psi}/2$
$\sigma_{Q_s^2}$	0.1	$m_D$	1.87 GeV
$S_{\perp}$	13 mb		

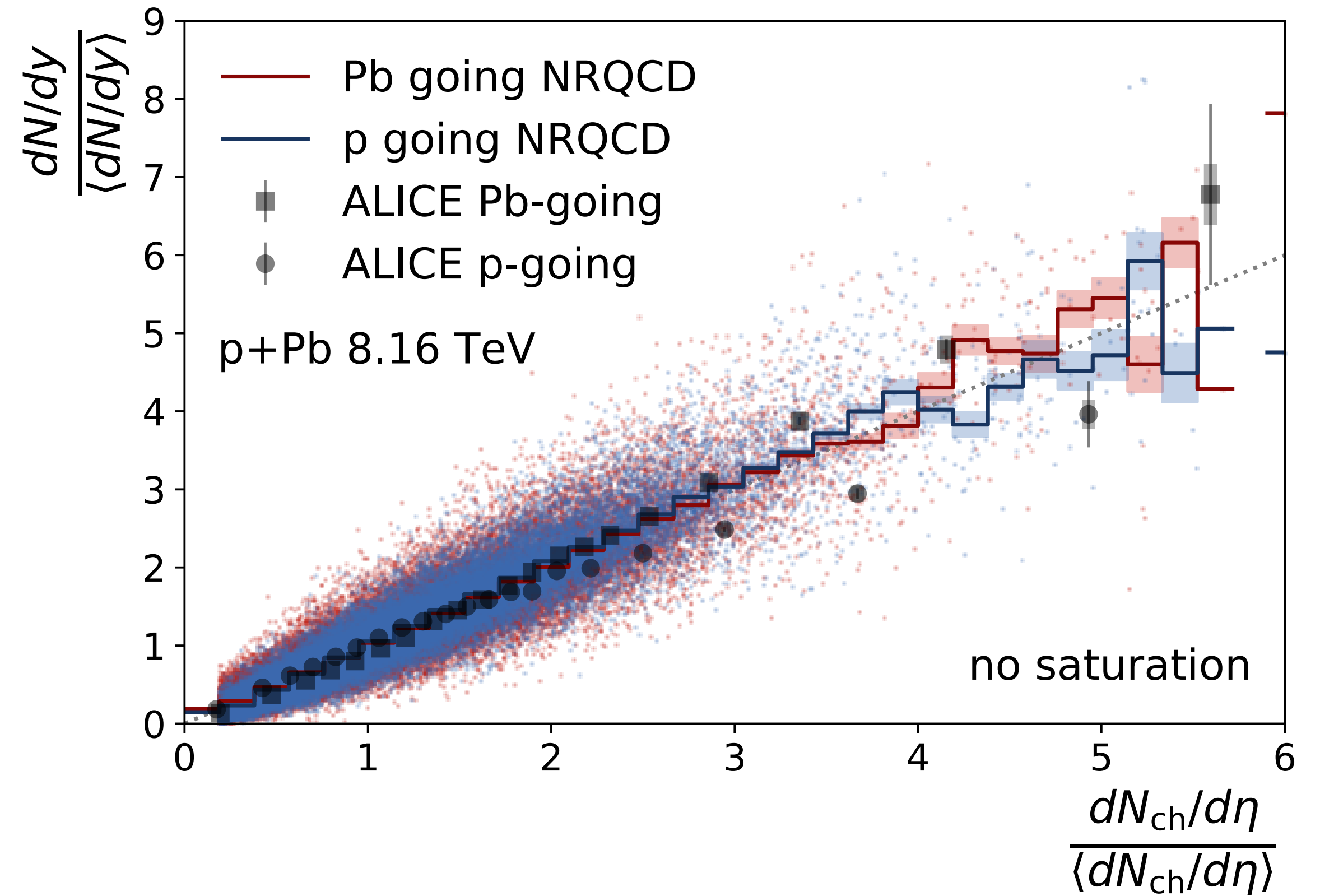
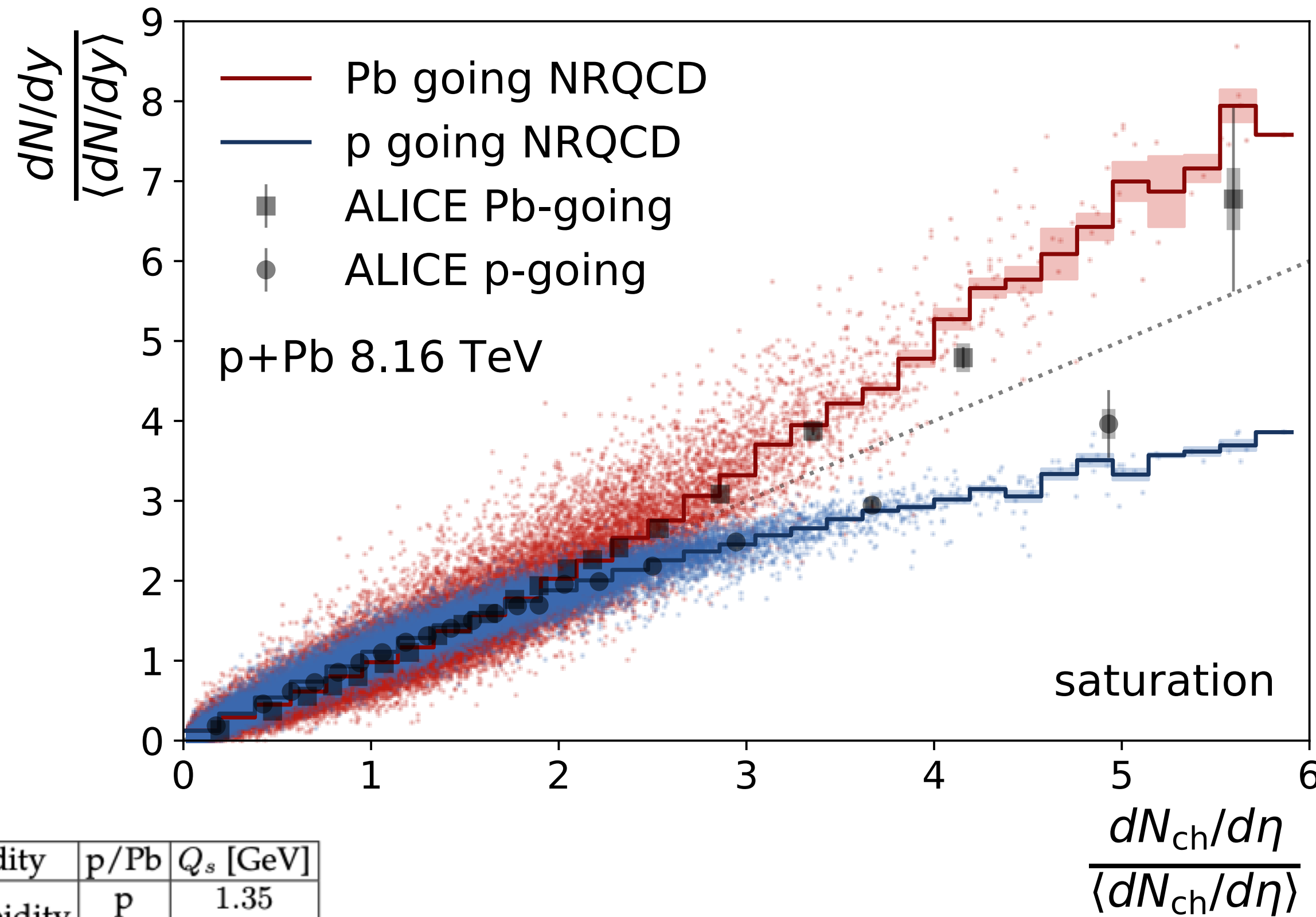
$\sigma_{B_q}$  and  $\sigma_{Q_s}$ : width parameters in log-normal fluctuations  $\xi$

$m_{\text{IR}}$ : infrared regulator in the charged hadron calculation

# RESULTS: J/ψ VS. CHARGED HADRON YIELD

## — Saturation drives the correlation between J/ψ and charged hadrons

Experimental data: S. Acharya et al. (ALICE), JHEP 09, 162 (2020), arXiv:2004.12673 [nucl-ex].



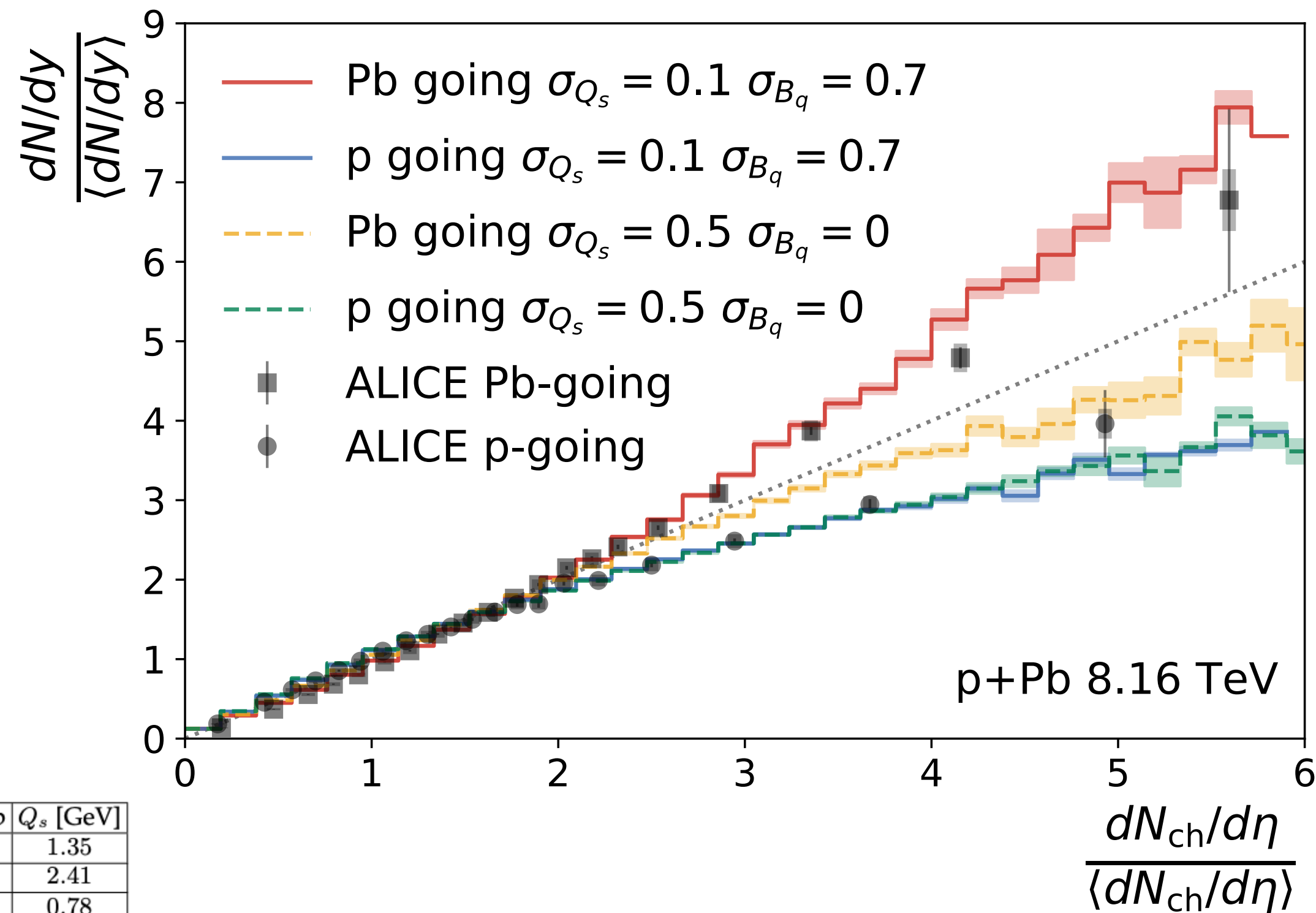
Rapidity	p/Pb	$Q_s$ [GeV]
midrapidity	p	1.35
	Pb	2.41
p-going	p	0.78
	Pb	4.18
Pb-going	p	2.78
	Pb	1.18

$$dN_{ch}/d\eta = 4\langle dN_{ch}/d\eta \rangle$$

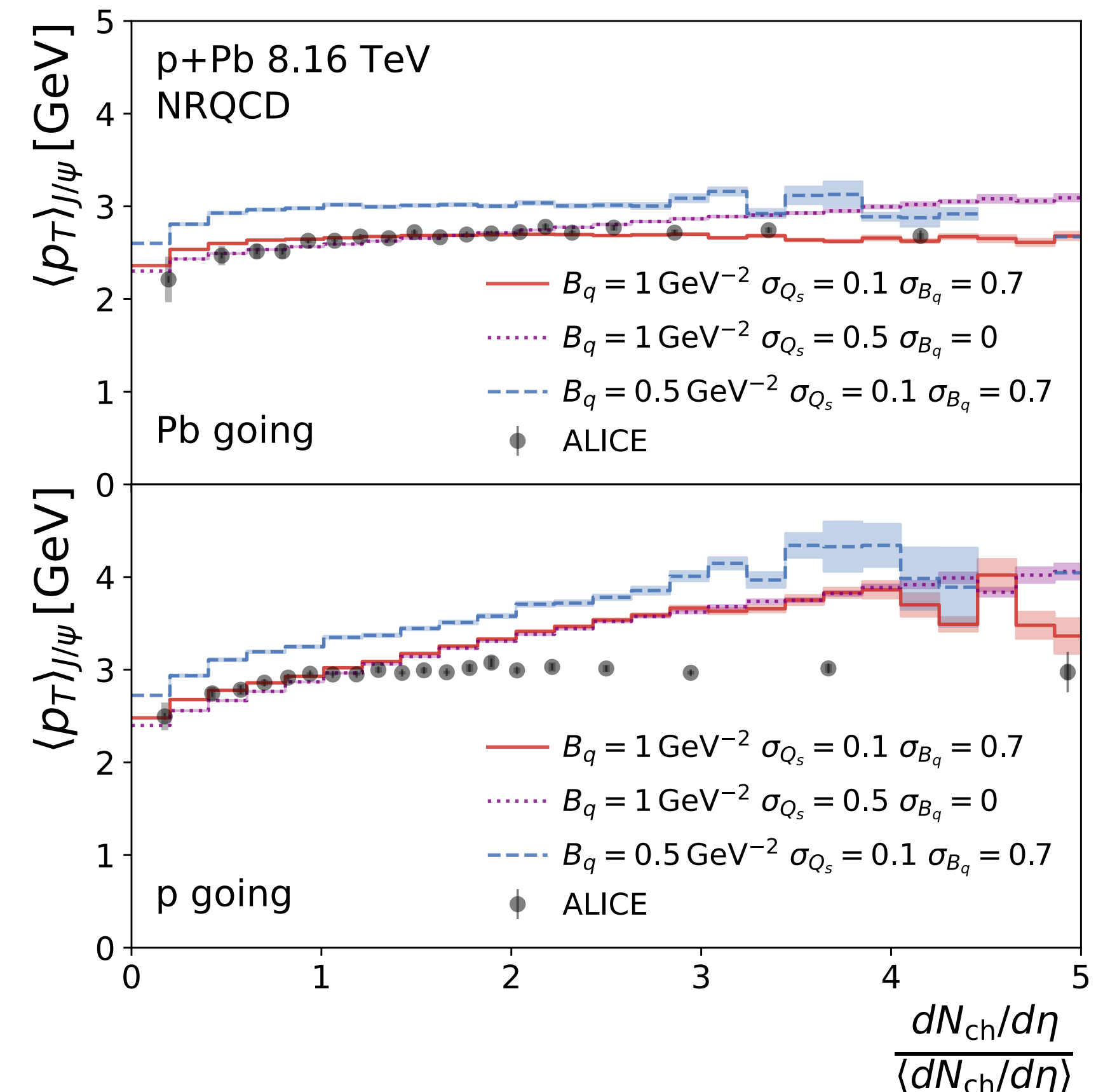
# FLUCTUATIONS AFFECT SATURATION AND $\langle p_T \rangle$

Experimental data: ALICE Collaboration, JHEP 09, 162 (2020)

- More normalization fluctuations (less size fluctuations) lead to stronger saturation effects on the  $J/\psi$  in the Pb-going direction



- Mean  $p_T$  driven by mass and  $Q_s$
- $Q_s$  fluctuations and hot spot size matter



Rapidity	p/Pb	$Q_s$ [GeV]
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$$dN_{ch}/d\eta = 4\langle dN_{ch}/d\eta \rangle$$

**BACKUP**

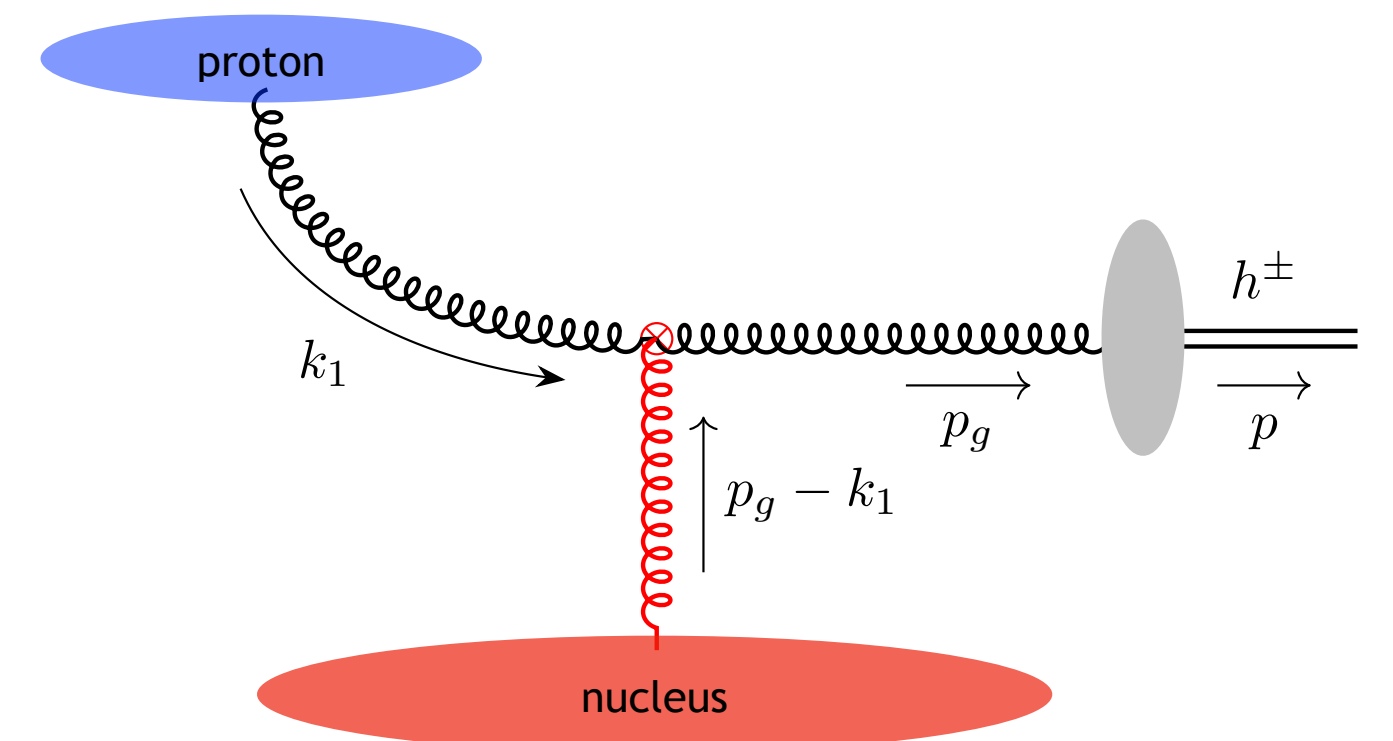
# MODEL: CHARGED HADRON PRODUCTION

Use  $k_T$ -factorization for gluon production

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$$\frac{dN_g(\mathbf{b}_\perp)}{d^2\mathbf{p}_{g\perp}dy_g} = \frac{\alpha_s}{(\sqrt{2}\pi)^6 C_F p_{g\perp}^2} \int_{k_{1\perp}, R_\perp} \phi^P(x_p; \mathbf{k}_{1\perp}; \mathbf{R}_\perp) \phi^A(x_A; \mathbf{p}_{g\perp} - \mathbf{k}_{1\perp}; \mathbf{R}_\perp - \mathbf{b}_\perp)$$

Unintegrated gluon distributions  $\phi^P$  and  $\phi^A$  (with  $A = p, \text{Pb}$ )  
from Balitsky-Kovchegov evolution with McLerran-Venugopalan initial conditions



Modified to include spatial dependence with nucleon substructure. 3 hot spots locations sampled from

$$P(\mathbf{R}_{\perp,i}) = \frac{1}{2\pi B_{qc}} e^{-R_{\perp,i}^2/(2B_{qc})} \quad \text{and hot spot density distribution} \quad T_q(\mathbf{R}_\perp - \mathbf{R}_{\perp,i}) = \xi_{Q_s^2} e^{-(\mathbf{R}_\perp - \mathbf{R}_{\perp,i})^2 / (2(\xi_{B_q})B_q)}$$

$B_q$  is given an  $x$  dependence motivated by JIMWLK evolution of proton size

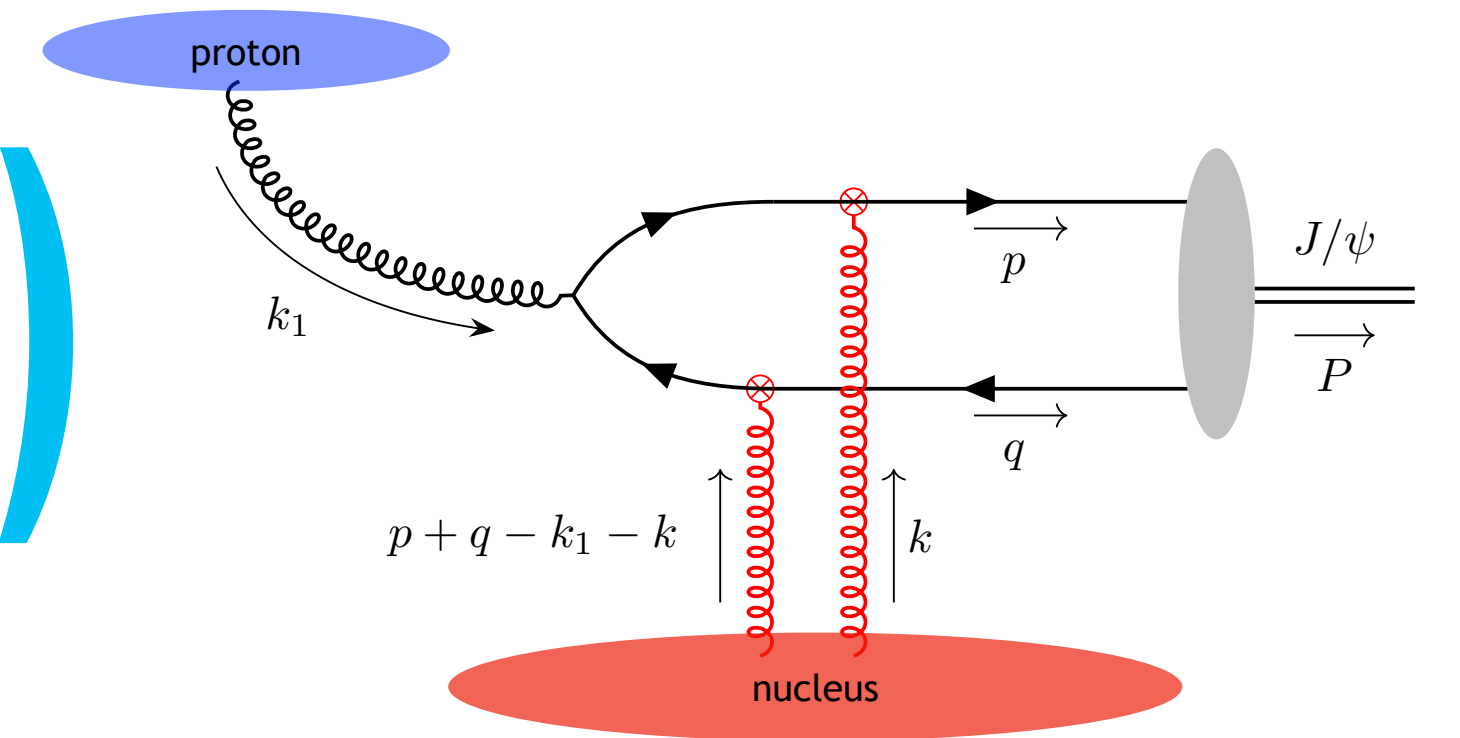
fluctuating normalization  
fluctuating size

Hadronize using **KKP fragmentation function**

$$\frac{dN_{\text{ch}}(\mathbf{b}_\perp)}{d\eta} = \int_{\mathbf{p}_\perp} \int_{z_{\text{min}}}^1 dz \frac{D_h(z)}{z^2} \mathcal{F}_{y \rightarrow \eta} \left. \frac{dN_g(\mathbf{b}_\perp)}{d^2\mathbf{p}_{g\perp}dy_g} \right|_{\mathbf{p}_{g\perp} = \mathbf{p}_\perp/z}$$



# MODEL: J/ψ PRODUCTION (NRQCD)



$c\bar{c}$ -pair production in NRQCD Z.-B. Kang, Y.-Q. Ma, and R. Venugopalan, JHEP 01, 056 (2014)

$$\frac{dN_{c\bar{c}}^\kappa(\mathbf{b}_\perp)}{d^2\mathbf{P}_\perp dY} = \frac{\alpha_s}{(2\pi)^9(N_c^2 - 1)} \int_{k_{1\perp}, k_\perp, k'_\perp, \mathbf{R}_\perp} \mathcal{H}^\kappa(\mathbf{P}_\perp - \mathbf{k}_{1\perp}, \mathbf{k}_\perp, \mathbf{k}'_\perp) \frac{\phi^p(x_p, \mathbf{k}_{1\perp}, \mathbf{R}_\perp)}{k_{1\perp}^2} \tilde{\Xi}^\kappa(x_A; \mathbf{P}_\perp - \mathbf{k}_{1\perp}, \mathbf{k}_\perp, \mathbf{k}'_\perp; \mathbf{R}_\perp - \mathbf{b}_\perp)$$

for quantum state  $\kappa$ . The pair momentum is  $\mathbf{P}_\perp = \mathbf{p}_\perp + \mathbf{q}_\perp$ ,  $\mathcal{H}^\kappa$  are the hard factors, and  $\tilde{\Xi}^\kappa$  the Wilson line correlators:

$$\tilde{\Xi}^{[8]}(x; \mathbf{l}_\perp, \mathbf{k}_\perp, \mathbf{k}'_\perp; \mathbf{R}_\perp) = (2\pi)^2 \delta^{(2)}(\mathbf{k}_\perp - \mathbf{k}'_\perp) \tilde{\mathcal{S}}_F^A(x; \mathbf{k}_\perp; \mathbf{R}_\perp) \tilde{\mathcal{S}}_F^A(x; \mathbf{l}_\perp - \mathbf{k}_\perp; \mathbf{R}_\perp) + \mathcal{O}(1/N_c) \text{ (octet)}$$

$$\tilde{\Xi}^{[1]}(x; \mathbf{l}_\perp, \mathbf{k}_\perp, \mathbf{k}'_\perp; \mathbf{R}_\perp) = \tilde{\mathcal{S}}_F^A(x; \mathbf{k}_\perp; \mathbf{R}_\perp) \tilde{\mathcal{S}}_F^A(x; \mathbf{k}'_\perp; \mathbf{R}_\perp) \tilde{\mathcal{S}}_F^A(x; \mathbf{l}_\perp - \mathbf{k}_\perp - \mathbf{k}'_\perp; \mathbf{R}_\perp) + \mathcal{O}(1/N_c) \text{ (singlet)}$$

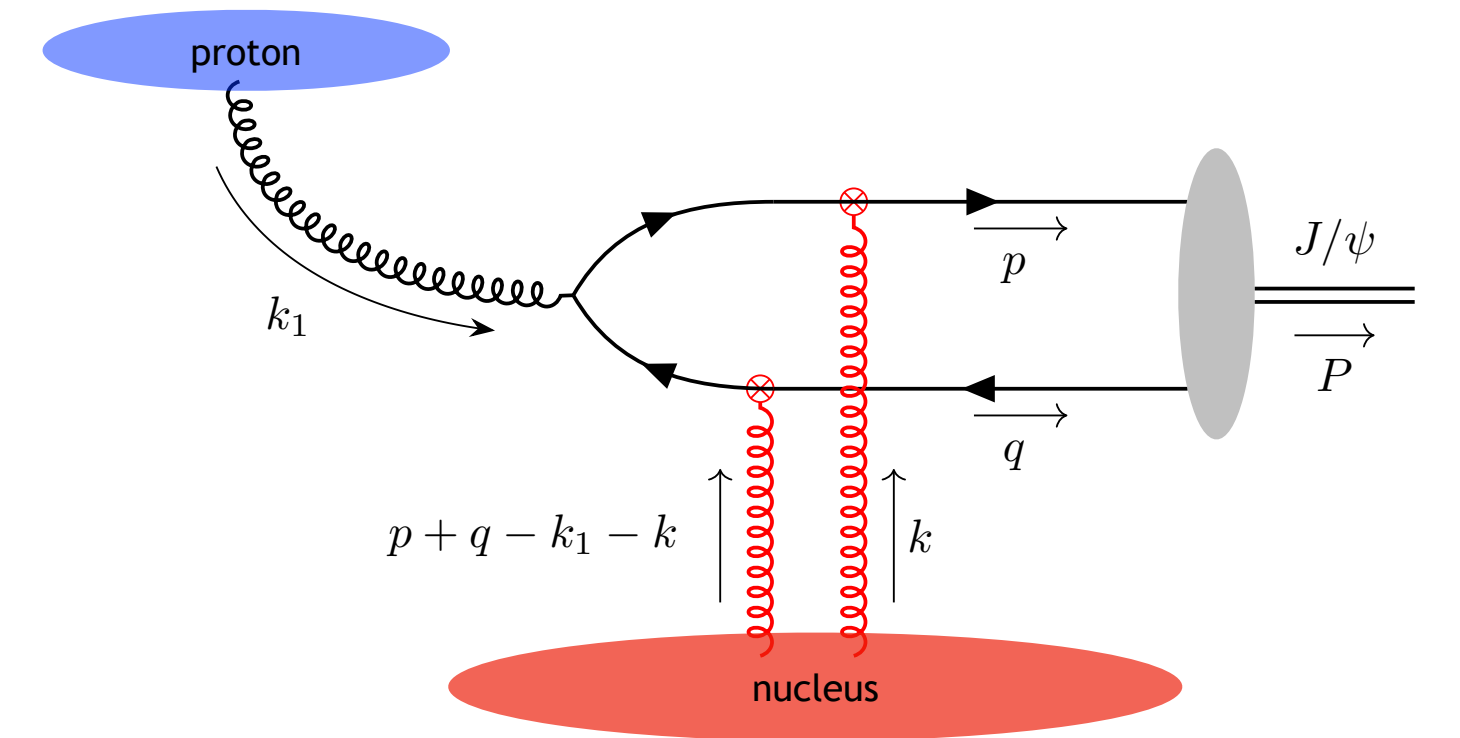
$$\frac{dN_{J/\psi}(\mathbf{b}_\perp)}{d^2\mathbf{P}_\perp dY} = \sum_\kappa \frac{dN_{c\bar{c}}^\kappa(\mathbf{b}_\perp)}{d^2\mathbf{P}_\perp dY} \langle \mathcal{O}_\kappa^{J/\psi} \rangle \text{ with non-perturbative long distance matrix elements } \langle \mathcal{O}_\kappa^{J/\psi} \rangle$$

K.-T. Chao, Y.-Q. Ma, H.-S. Shao, K. Wang, Y.-J. Zhang, Phys. Rev. Lett. 108, 242004 (2012)

Y.-Q. Ma, R. Venugopalan, H.-F. Zhang, Phys. Rev. D 92, 071901 (2015)

Again, spatial dependence in  $\phi^p$  and  $\tilde{\mathcal{S}}_F^A$

# MODEL: J/ψ PRODUCTION (ICEM)



$\bar{c}c$ -pair production in the Improved Color Evaporation Model (ICEM):

H. Fujii, F. Gelis, and R. Venugopalan, Nucl. Phys. A 780, 146 (2006); H. Fujii, K. Watanabe, Nucl. Phys. A 915, 1 (2013)

$$\frac{dN_{\bar{c}c}(\mathbf{b}_\perp)}{d^2\mathbf{p}_\perp d^2\mathbf{q}_\perp dy_c dy_{\bar{c}}} = \frac{\alpha_s N_c^2}{2(2\pi)^{10}(N_c^2 - 1)} \int_{k_{1\perp}; k_\perp; \mathbf{R}_\perp} \frac{\phi^p(x_p; \mathbf{k}_{1\perp}; \mathbf{R}_\perp)}{k_{1\perp}^2} \tilde{\mathcal{S}}_F^A(x_A; \mathbf{k}_\perp; \mathbf{R}_\perp - \mathbf{b}_\perp) \tilde{\mathcal{S}}_F^A(x_A; \mathbf{p}_\perp + \mathbf{q}_\perp - \mathbf{k}_{1\perp} - \mathbf{k}_\perp; \mathbf{R}_\perp - \mathbf{b}_\perp) \mathcal{H}(\mathbf{p}_\perp, \mathbf{q}_\perp, \mathbf{k}_{1\perp}, \mathbf{p}_\perp + \mathbf{q}_\perp - \mathbf{k}_{1\perp} - \mathbf{k}_\perp) + \mathcal{O}(1/N_c)$$

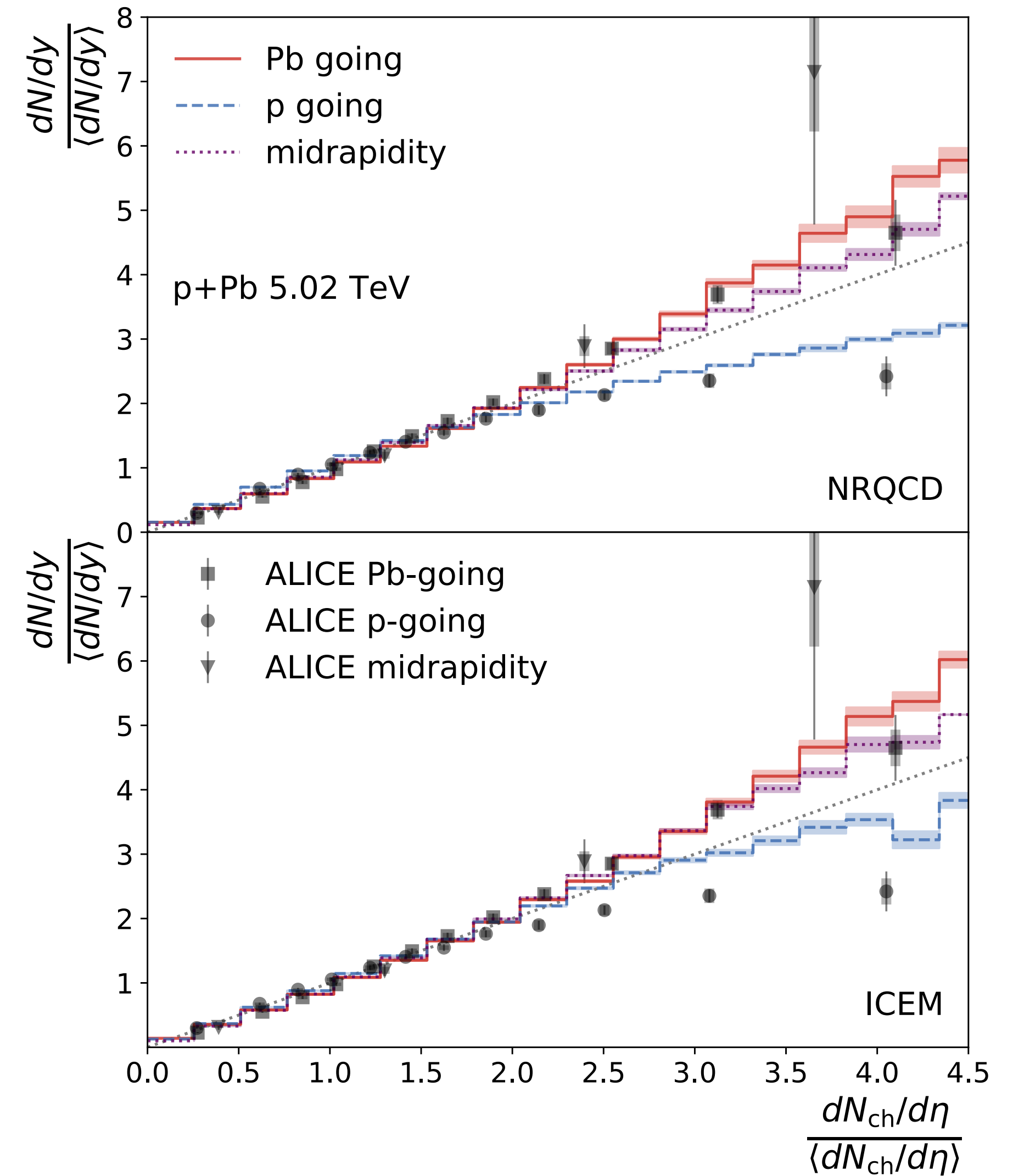
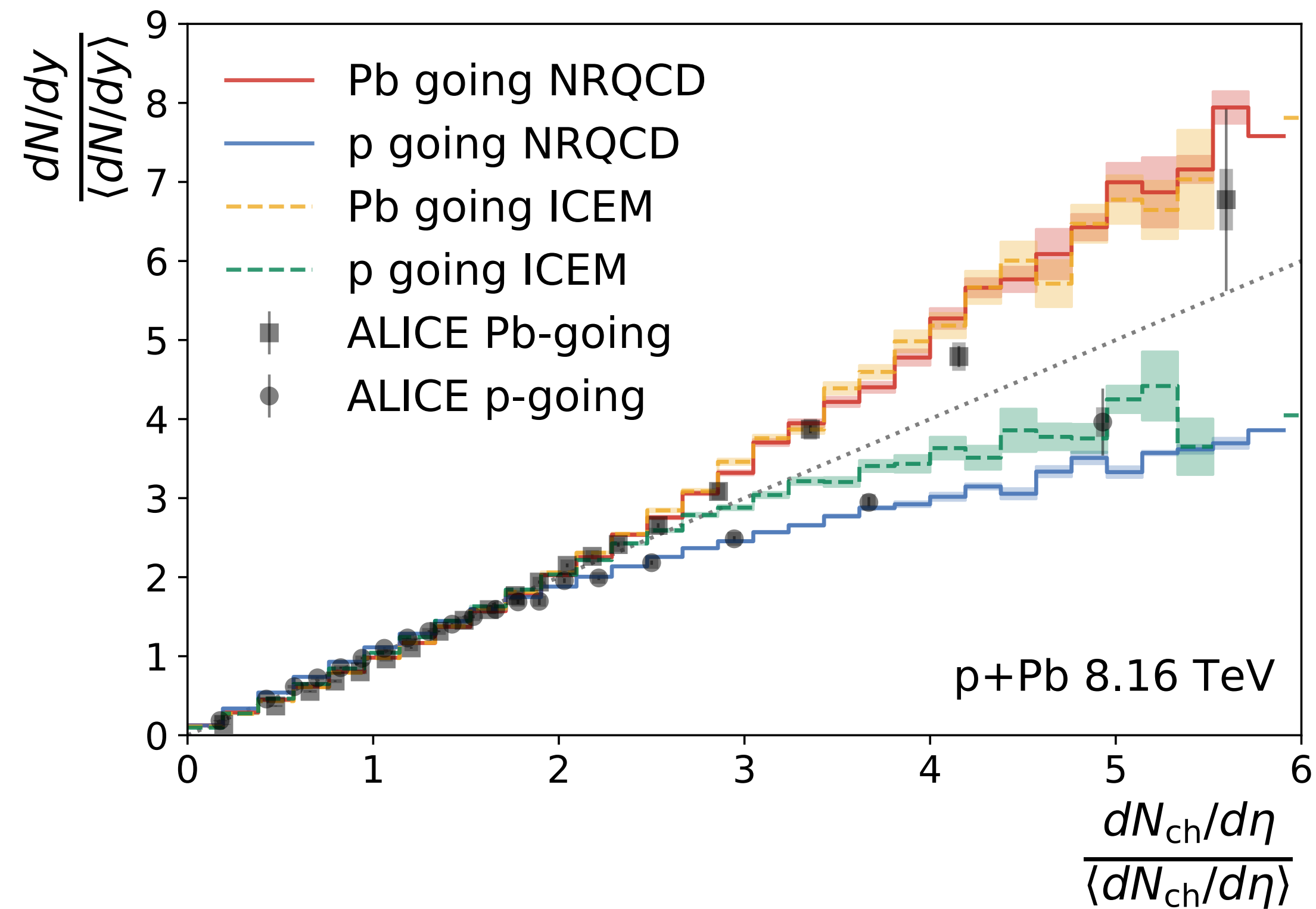
with the Wilson line correlator  $\tilde{\mathcal{S}}_F^A$  in the fundamental representation (with  $A = p, \text{Pb}$ )

Production of J/ψ is then given by

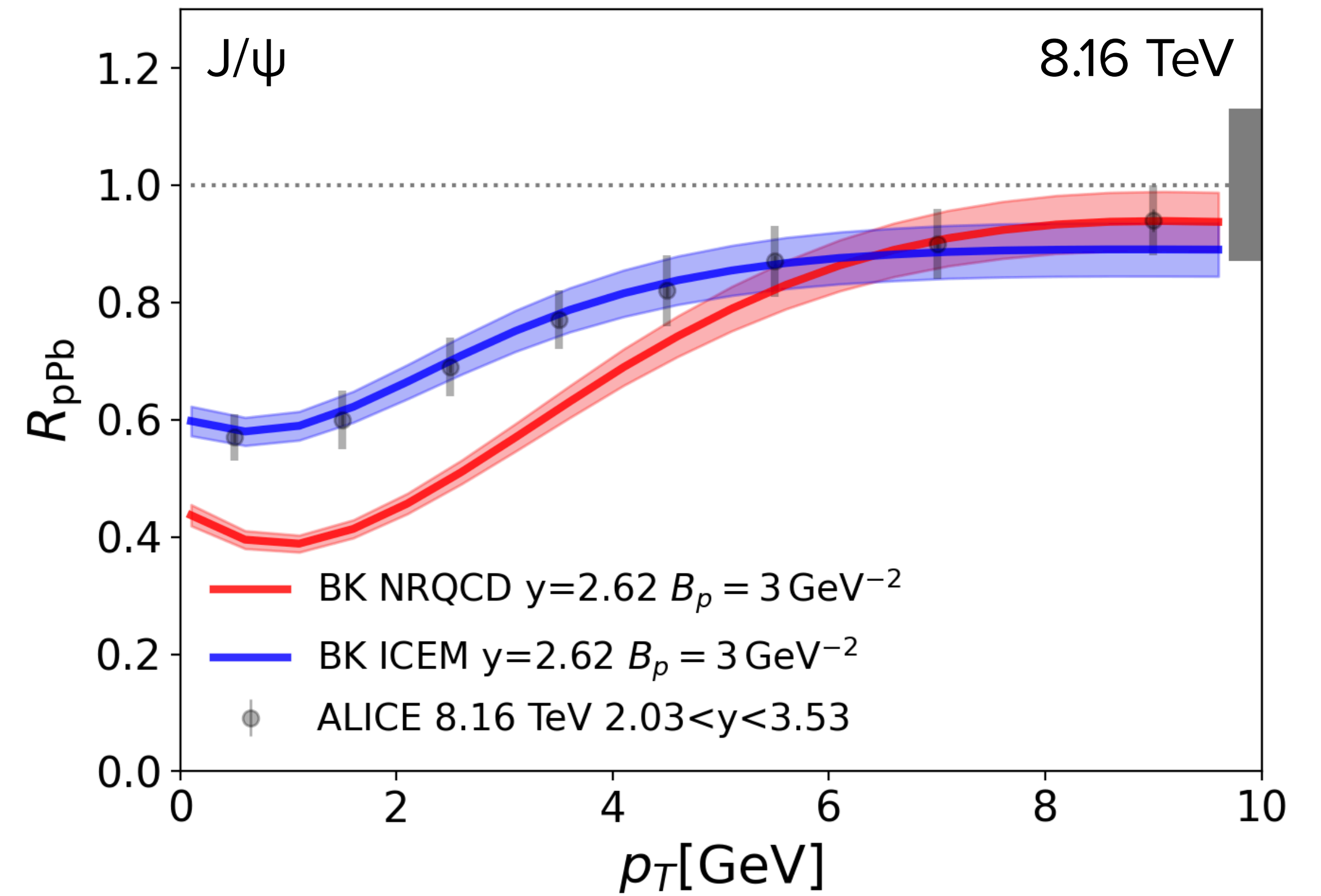
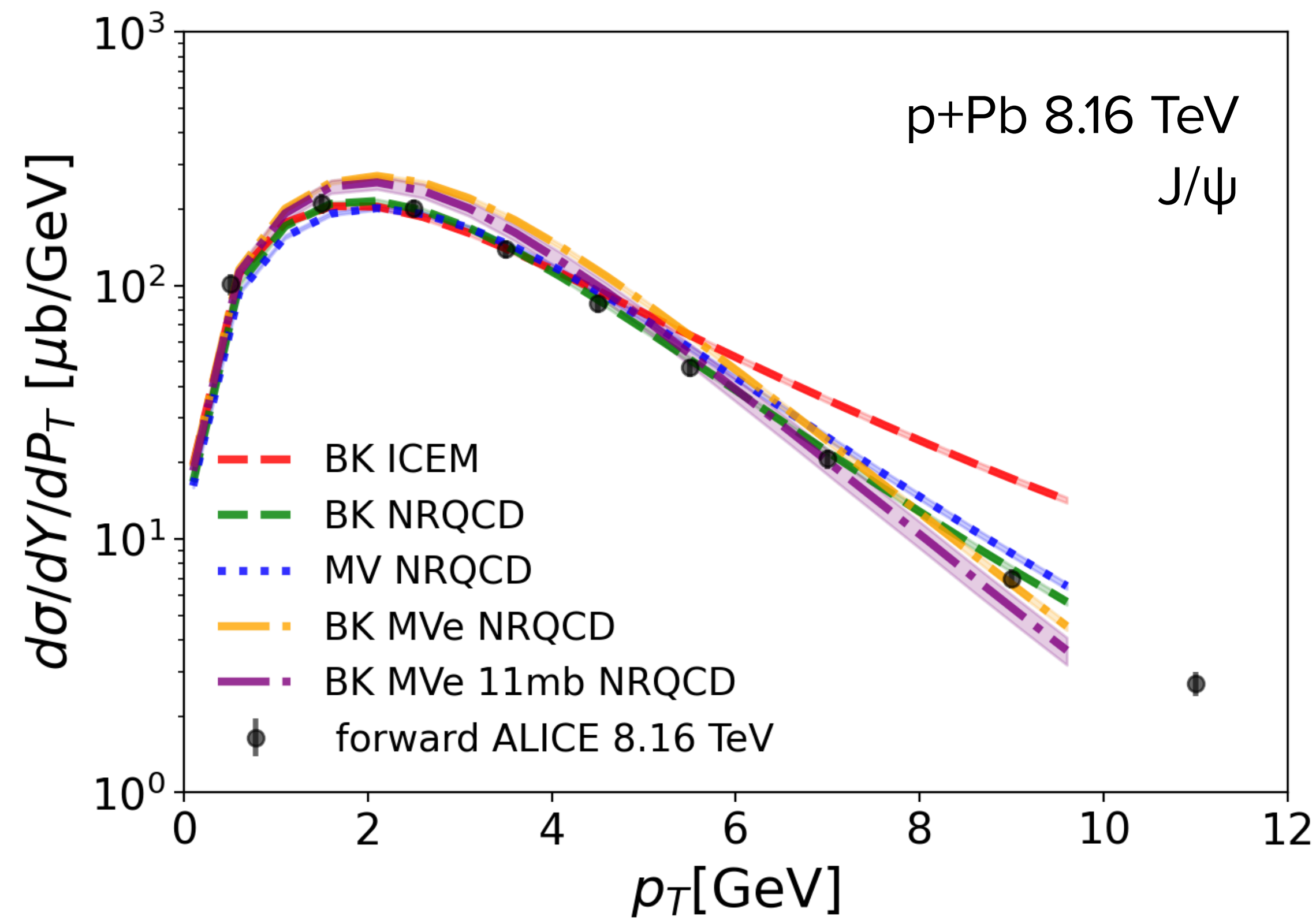
$$\frac{dN_{J/\psi}(\mathbf{b}_\perp)}{d^2\mathbf{P}_\perp dY} = F \int_{m_{J/\psi}^2}^{4m_D^2} dM^2 \frac{M^2}{m_{J/\psi}^2} \frac{dN_{c\bar{c}}(\mathbf{b}_\perp)}{dM^2 d^2\mathbf{P}_\perp dY}, \text{ where } \frac{dN_{c\bar{c}}(\mathbf{b}_\perp)}{dM^2 d^2\mathbf{P}_\perp dY} = \int_0^{\sqrt{\frac{M^2}{4} - m_c^2}} d\tilde{q} \int_0^{2\pi} d\phi \mathcal{F} \frac{dN_{c\bar{c}}(\mathbf{b}_\perp)}{d^2\mathbf{p}_\perp d^2\mathbf{q}_\perp dy_p dy_q}$$

where  $\tilde{q}$  and  $\phi$  are the relative transverse momentum and angle between the  $c$  and the  $\bar{c}$  in the rest frame of the pair.

# NRQCD VS ICEM



# J/ψ SPECTRA AND $R_{pPb}$



# $Q_s$ VS. MULTIPLICITY

