

Heavy flavour hadron production in a coalescence plus fragmentation approach from AA to pp

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**COALESCENCE
INTEGRAL**

Statistical factor colour-spin-isospin Parton Distribution function Hadron Wigner function

$$\frac{dN_{Hadron}}{d^2 p_T} = g_H \int \prod_{i=1}^n p_i \cdot d\sigma_i \frac{d^3 p_i}{(2\pi)^3} f_q(x_i, p_i) f_W(x_1, \dots, x_n; p_1, \dots, p_n) \delta(p_T - \sum_i p_{iT})$$

Fireball Parameters

Constraints from Experiment

RHIC → LHC

Lifetime and Volume

$\tau \sim 4.5 \text{ fm}/c \rightarrow 7.8 \text{ fm}/c$

$\beta_0 = 0.37 \rightarrow 0.63$

$V \sim 1100 \text{ fm}^3 \rightarrow 2500 \text{ fm}^3$

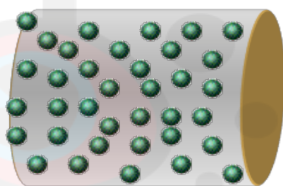
In agreement with HBT

$dE_T/dy \sim 740 \text{ GeV} \rightarrow 2100 \text{ GeV}$

$dN_{ch}/dy \sim 670 \rightarrow 1600$

$T_c \sim 165 \text{ MeV}$

$|\Delta y| \leq 0.5$



LIGHT QUARK

- Thermal Distr. ($p_T < 2 \text{ GeV}$)
w/Collective flow

$$\frac{dN_{q,\bar{q}}}{d^2 p_T} \sim \exp\left(-\frac{y_T - p_T \cdot \beta_T \mp \mu_q}{T}\right)$$

$$\beta(r) = \frac{r}{R} \beta_{max}$$

- Minijet Distr. ($p_T > 2 \text{ GeV}$)

HEAVY QUARK (initial state) Fixed-Order plus Next-to-Leading-Log (FONLL)

M. Cacciari, P. Nason, R. Vogt, PRL 95 (2005) 122001

$$f_H(\dots) = \prod_{i=1}^{N_q-1} A_W \exp\left(-\frac{x_{ri}^2}{\sigma_{ri}^2} - p_{ri}^2 \sigma_{ri}^2\right)$$

A_W fixed to have all charm hadronizing at $p_T \rightarrow 0$
 σ_r width parameter related to the oscillator frequency ω with reduced mass and linked to the hadron size

$$\sigma_{ri} = \frac{1}{\sqrt{\mu_i \omega}}$$

$$\langle r^2 \rangle_{ch} = \frac{3}{2} \frac{m_2^2 Q_1 + m_1^2 Q_2}{(m_1 + m_2)^2} \sigma_{r1}^2$$

$$+ \frac{3}{2} \frac{m_3^2 (Q_1 + Q_2) + (m_1 + m_2)^2 Q_3}{(m_1 + m_2 + m_3)^2} \sigma_{r2}^2$$

$$\langle r^2 \rangle_{ch}^{D^0} = 0.184 \text{ fm}^2 \quad \sigma_p^{D^0} = \sigma_r^{-1 D^0} = 0.283 \text{ GeV} \quad \sigma_{p2}^{A_c} = 0.342 \text{ GeV}$$

$$\langle r^2 \rangle_{ch}^{A_c} = 0.15 \text{ fm}^2 \quad \sigma_{p1}^{A_c} = 0.18 \text{ GeV}$$

References

S. Plumari, V. Minissale, et al., *Eur.Phys.J.* **C78** (2018) no.4, 348

Y. Oh, C.M. Ko, S.H. Lee, S. Yasui, *Phys. Rev.* **C79**,044905 (2009)

F. Scardina, S.K. Das, V. Minissale, S. Plumari, V. Greco, *Phys.Rev.* **C96** (2017) no.4, 044905

V.Minissale, F. Scardina,V.Greco, *Phys.Rev.C* **92** (2015)

V.Greco, C.M. Ko, P. Levai, *Phys.Rev.C* **68** (2003) 034904

Fragmentation function

$$\frac{dN_h}{d^2 p_h} = \sum_f \int dz \frac{dN_f}{d^2 p_f} D_{f \rightarrow h}(z)$$

Peterson fragmentation function
C. Peterson, et al. PRD 27 (1983) 105

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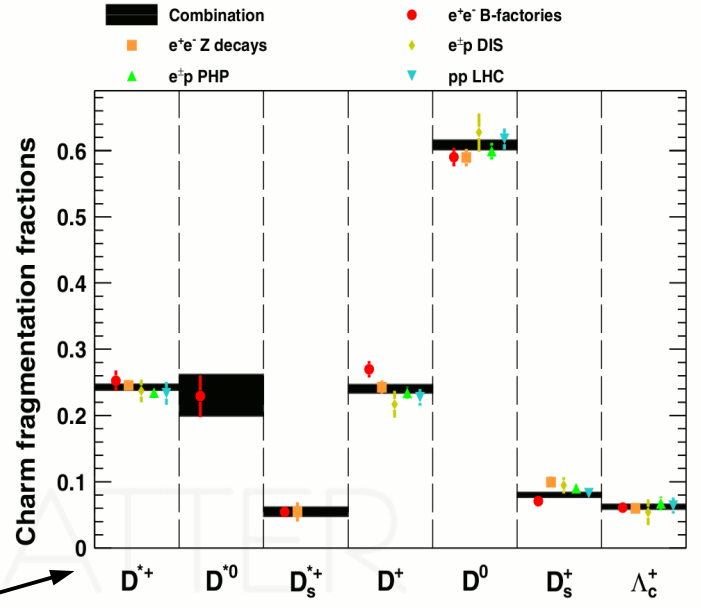
The distribution function is evaluated at the Fixed-Order plus Next-to-Leading-Log (FONLL)

M. Cacciari, P. Nason, R. Vogt, PRL 95 (2005) 122001

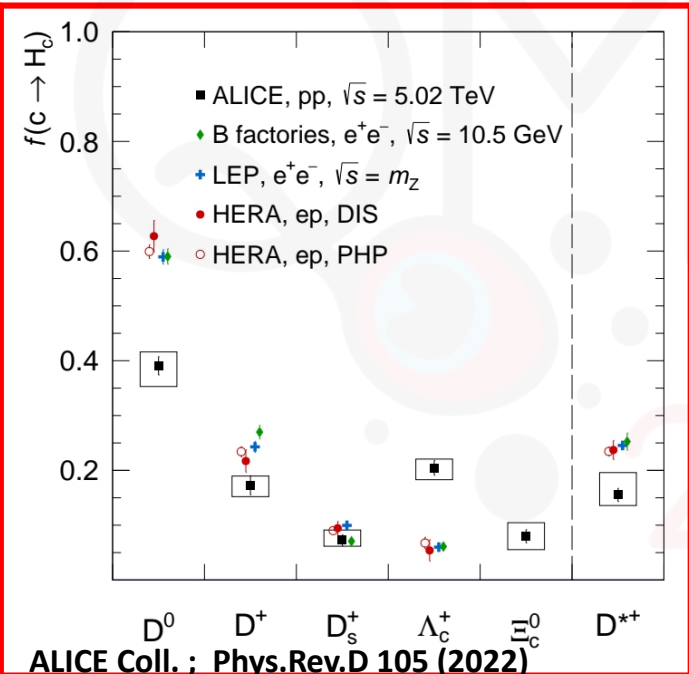
In AA: bulk+charm evolution with Relativistic Transport Boltzmann Equation

$$D_{f \rightarrow h}(z) \propto \frac{1}{z \left[1 - \frac{1}{z} - \frac{\epsilon}{1-z} \right]^2}$$

ϵ set to reproduce tail of the Λ_c and D^0 spectra



M. Lisovyi, et al. EPJ C76 (2016) no.7, 397



- Normalization of f_w requiring that $P_{\text{coal}}=1$ at $p=0$
- The charm that does not coalesce undergo fragmentation

Charm fragmentation fractions come from analysis of charm hadrons production in elementary collisions systems

Updated fractions after experimental evidence in pp@5TeV:

Fragmentation fractions ($c \rightarrow h$) depends on collision system...and QGP presence?

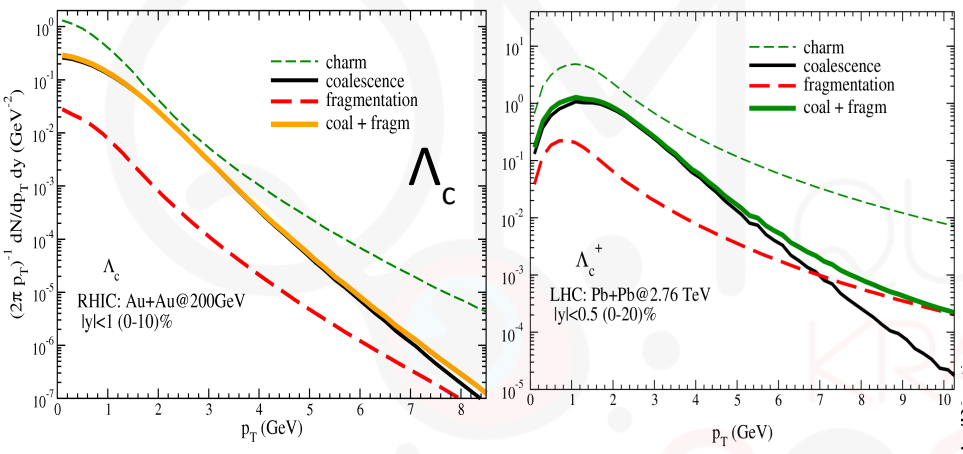
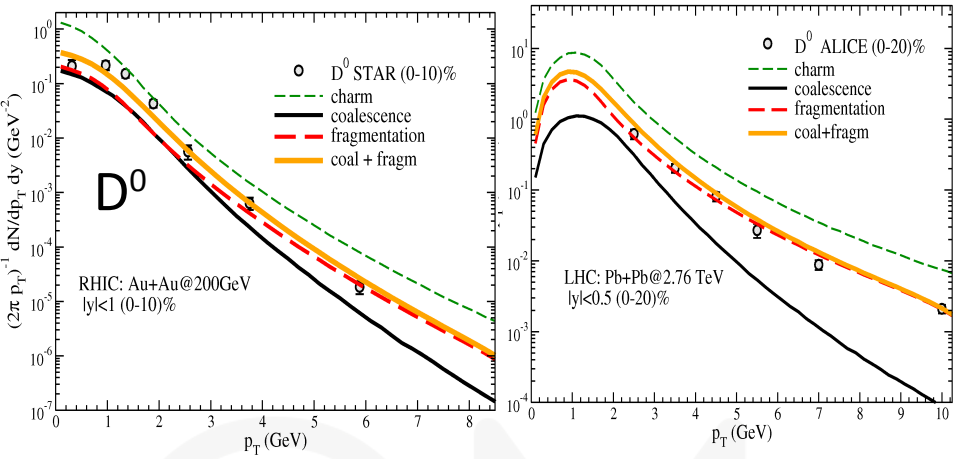
No more Universality?

In AA collisions:

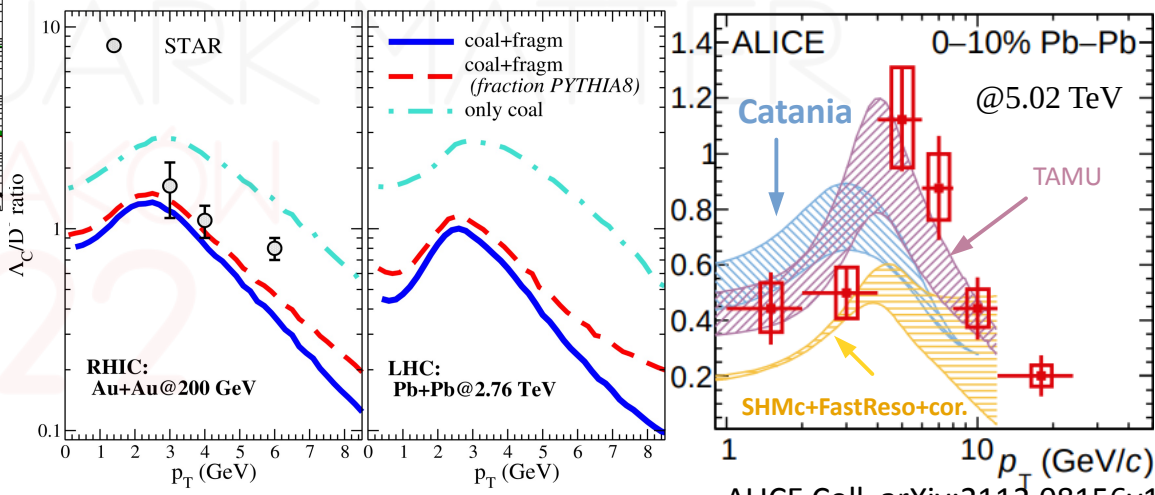
Only Coalescence ratio is similar at both energies.
 Fragmentation ~ 0.1 at both energies.

the **combined ratio is different** because the coalescence over fragmentation ratio at LHC is smaller than at RHIC

Therefore at LHC the larger contribution in particle production from fragmentation leads to a final ratio that is smaller than at RHIC.



Coalescence lower at LHC than at RHIC
 For D^0 main contribution from Fragmentation
 For Λ_c main contribution from Coalescence



Possible presence of QGP in smaller system.
Assuming QGP formation what coal.+fragm. predicts?

pp collisions

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CHARM

FONLL Distribution

p+p @ 5 TeV

- $\tau_{pp}=2 \text{ fm}/c$
- $\beta_0=0.4$
- $R=2.5 \text{ fm}$
- $V\sim 30 \text{ fm}^3$

LIGHT

Thermal Distribution ($p_T < 2 \text{ GeV}$)

$$\frac{dN_q}{d^2 r_T d^2 p_T} = \frac{g_q \tau m_T}{(2\pi)^3} \exp\left(-\frac{\gamma_T (m_T - p_T \cdot \beta_T)}{T}\right)$$

Minijet Distribution ($p_T > 2 \text{ GeV}$)

NO QUENCHING

Reduction of rise-and-fall behaviour in Λ_c / D^0 ratio:

-Confronting with AA: Coal. smaller w.r.t. Fragm.

-FONLL distribution flatter w/o evolution in QGP

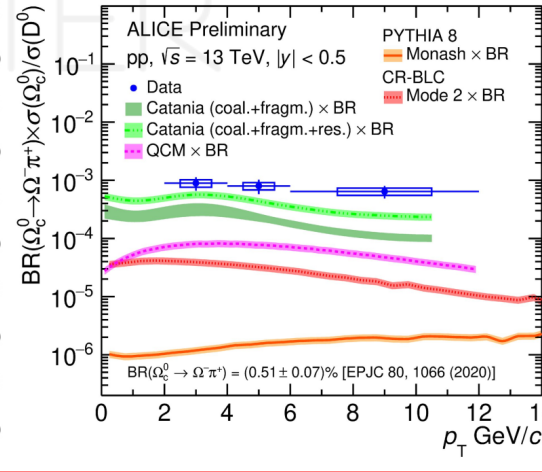
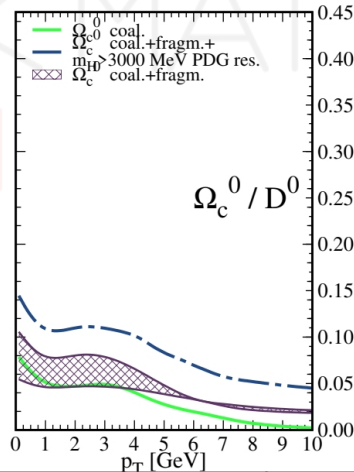
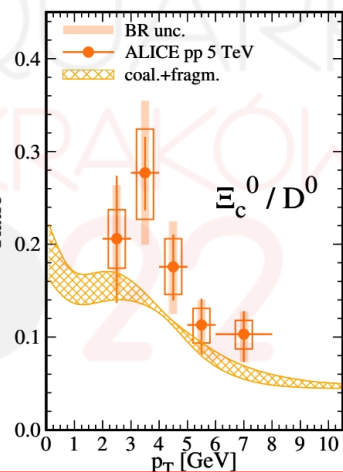
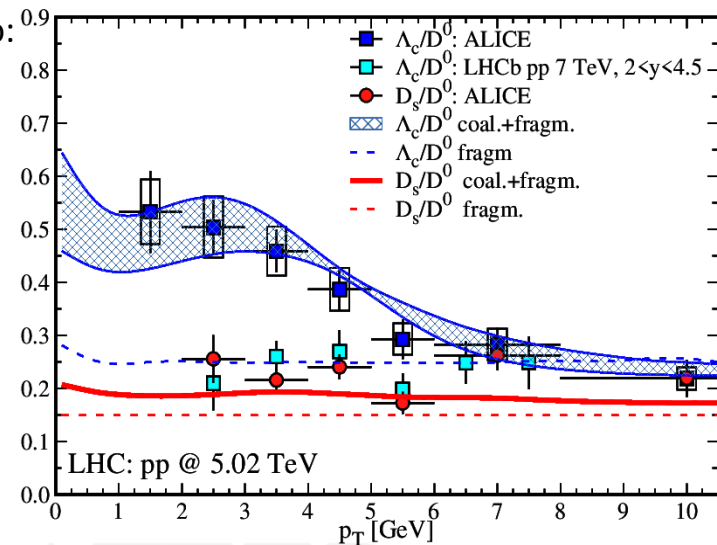
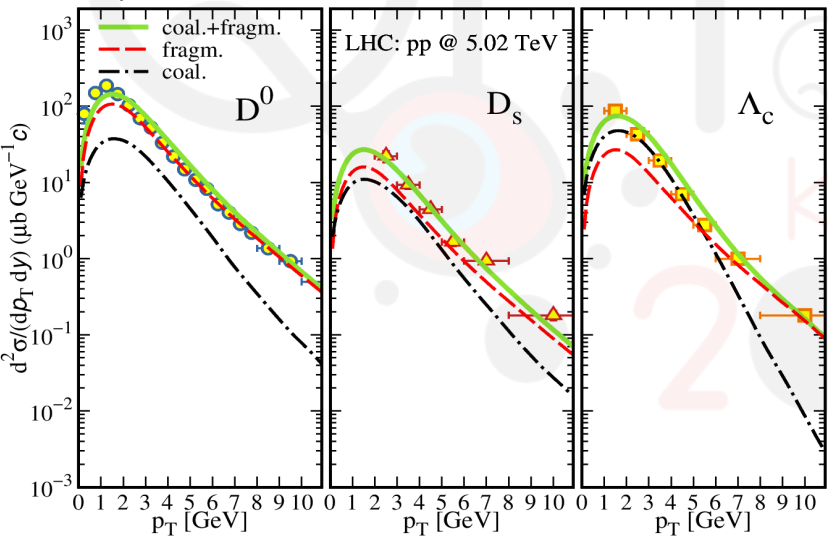
-Volume size effect

New measurements of heavy hadrons at ALICE:

- Ξ_c/D^0 ratio, same order of Λ_c/D^0 :
coalescence gives enhancement

- very large Ω_c/D^0 ratio, our model does not get the big enhancement

V. Minissale, S. Plumari, V. Greco,
Phys.Lett.B821 (2021) 136622



Implications, developments and outlooks:

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Bulk evolution

$$p^\mu \partial_\mu f_{q,g}(x,p) + \underbrace{M(x) \partial_\mu^x M(x) \partial_p^\mu f_{q,g}(x,p)}_{\text{field interaction } \epsilon-3p \neq 0} = \underbrace{C_{22}[f_{q,g}]}_{\text{collisions } \eta \neq 0}$$

free-streaming

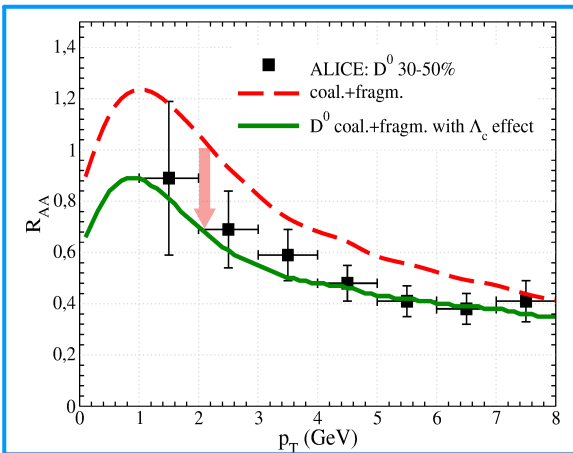
field interaction
 $\epsilon-3p \neq 0$

collisions
 $\eta \neq 0$

Heavy quark evolution

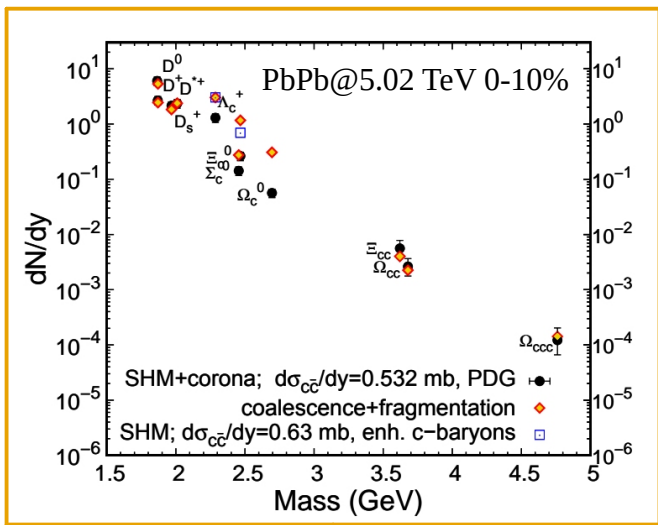
$$p^\mu \partial_\mu f_Q(x,p) = C[f_Q, f_g, f_q]$$

The Relativistic Boltzmann transport eq. simulations give us the parton distribution of charm and bottom, and allow us to extend the study of the impact of hadronization.



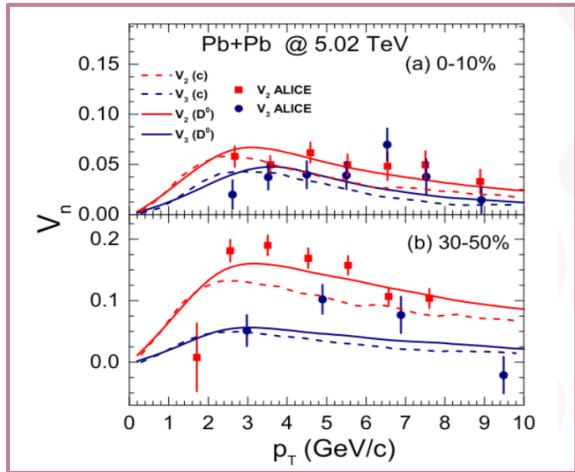
The large Λ_c production has effects on the R_{AA} of D^0 , because of the charm conservation

MULTICHARM



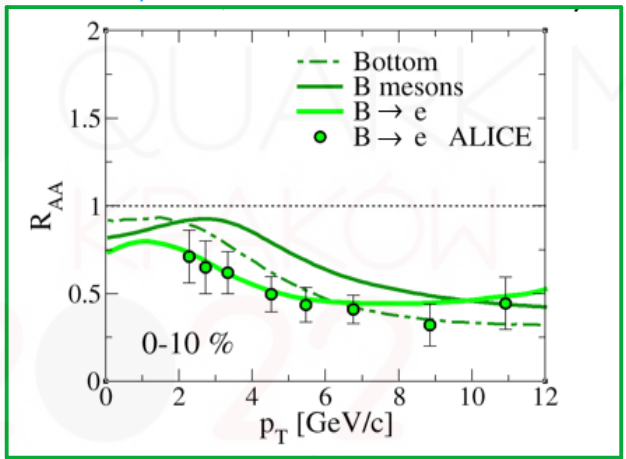
Yields of multicharm hadrons similar to SHM in PbPb, possible effects with system size and on the distribution vs p_T are under investigation. A baryon like Ω_{ccc} formed only by heavy quarks can give insights on the baryon wave function and the potential $V_{cc}(r,T)$ between quarks. Enhancement for single charmed baryons as seen in pp collisions.

Minissale, Plumari, Greco (in preparation)



Coalescence give an enhancement to the $v_n(p_T)$ of final hadrons compared to the charm $v_n(p_T)$.

Sambataro, Sun, Minissale, Plumari, Greco (in preparation)



Electrons from semileptonic B meson decay with a coal + fragm model for B meson production

Sambataro, Minissale et al. (in preparation)