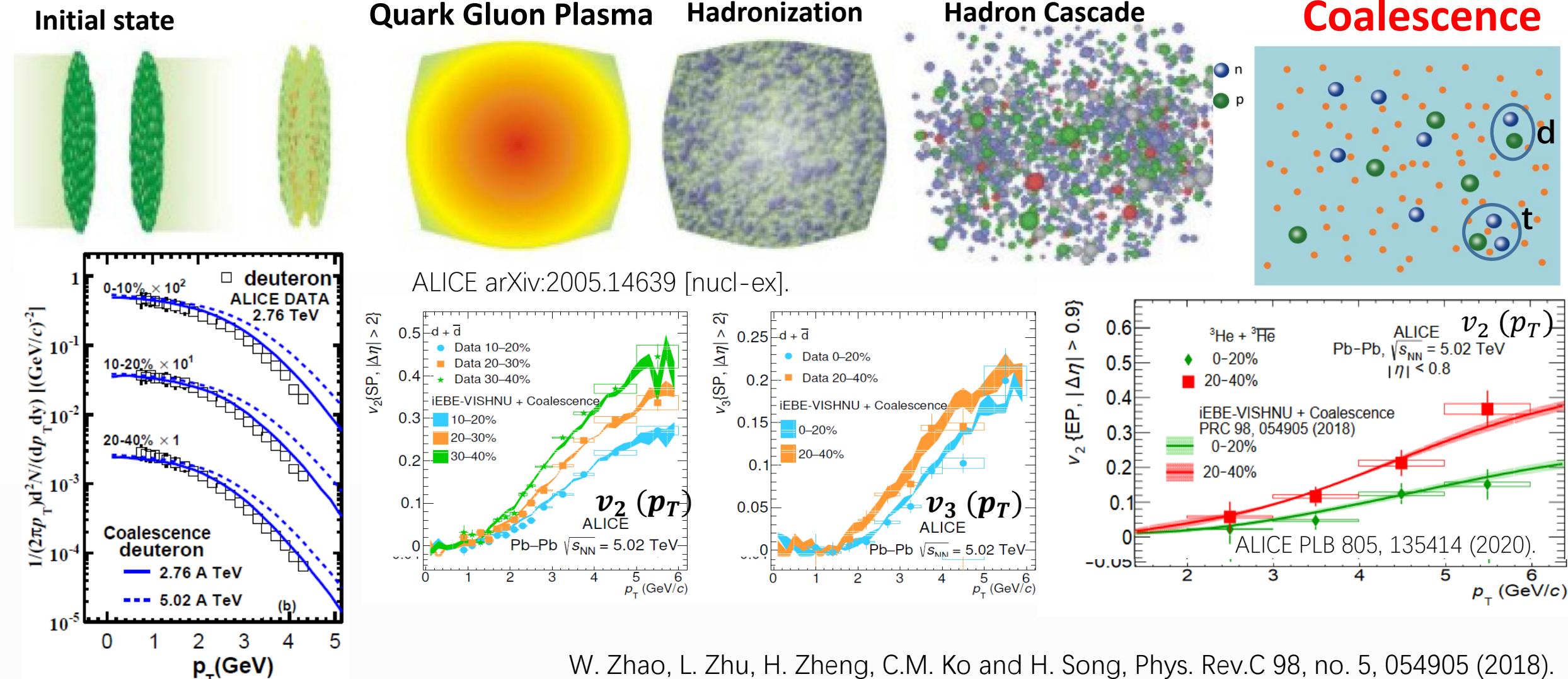




# Multiplicity scaling of light nuclei productions in heavy-ion collisions

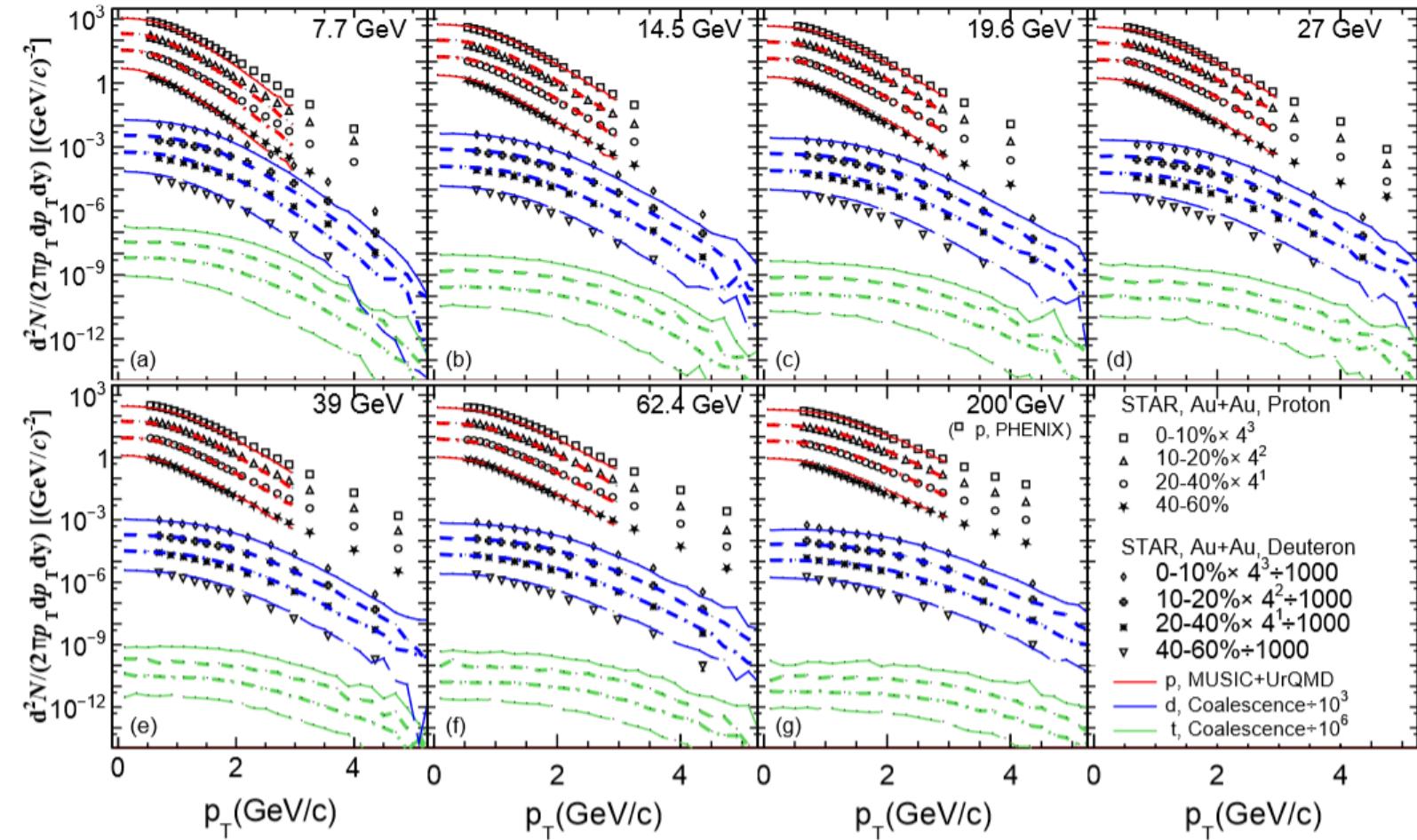
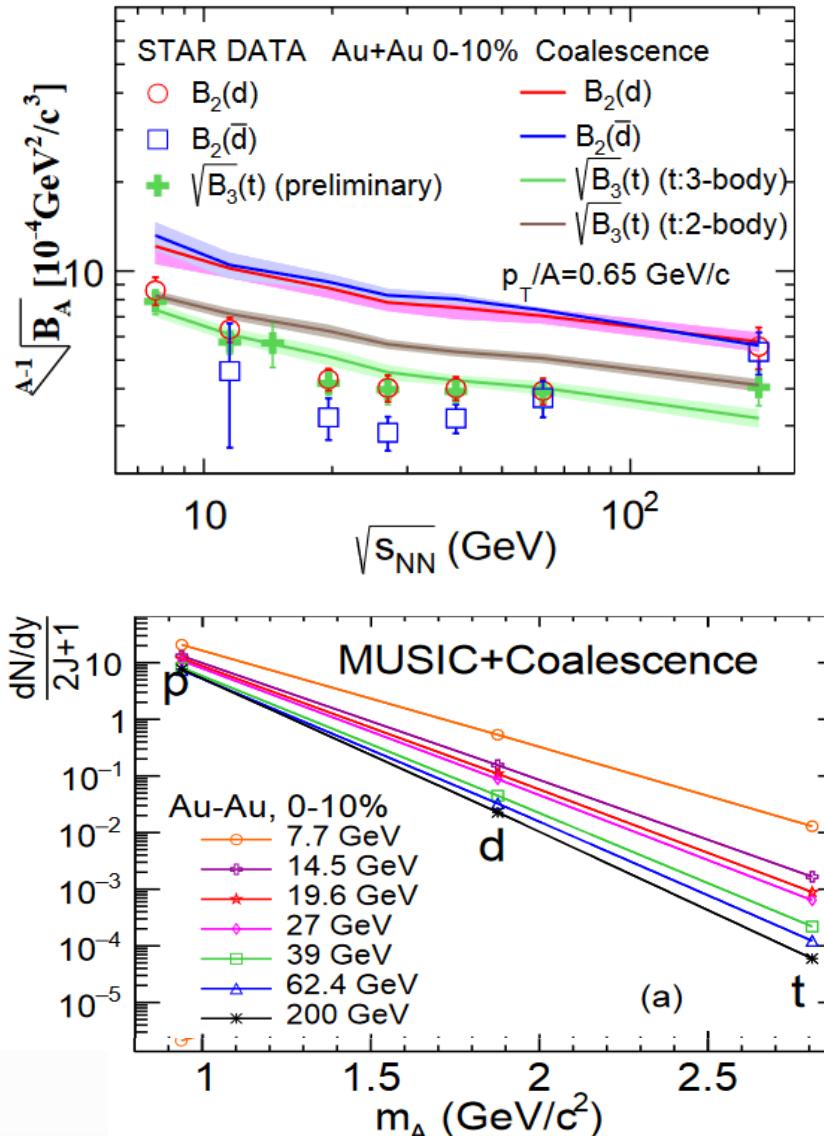
**Wenbin Zhao, Xiaofeng Luo**  
**Central China Normal University**  
**Quark Matter 2022**

# Predictions for spectra and $v_n(p_T)$ of light nuclei



- iEBE-VISHNU + Coalescence nicely predict spectra,  $v_2(p_T)$  and  $v_3(p_T)$  of light nuclei at different centrality bins for the ALICE measurements.

# Light nuclei production at RHIC BES region



- W. Zhao, K. j. Sun, C. M. Ko and X. Luo, [arXiv:2105.14204 [nucl-th]].  
 W. Zhao, L. Zhu, H. Zheng, C.M. Ko and H. Song, Phys. Rev.C 98, no. 5, 054905 (2018).  
 W. Zhao, C. Shen, C. M. Ko, Q. Liu and H. Song, PRC 102, 044912 (2020).

- iEBC-MUSIC +Coalescence well describe the spectra of light nuclei from 7.7 to 200 GeV.
- $B_2(d/\bar{d})$  and  $\sqrt{B_3(t)}$  decrease monotonically with multiplicity.  $dN/dy/(2J+1)$  decreases exponentially vs  $m_A$

# Multiplicity scaling of $N_p \cdot N_t / N_d^2$

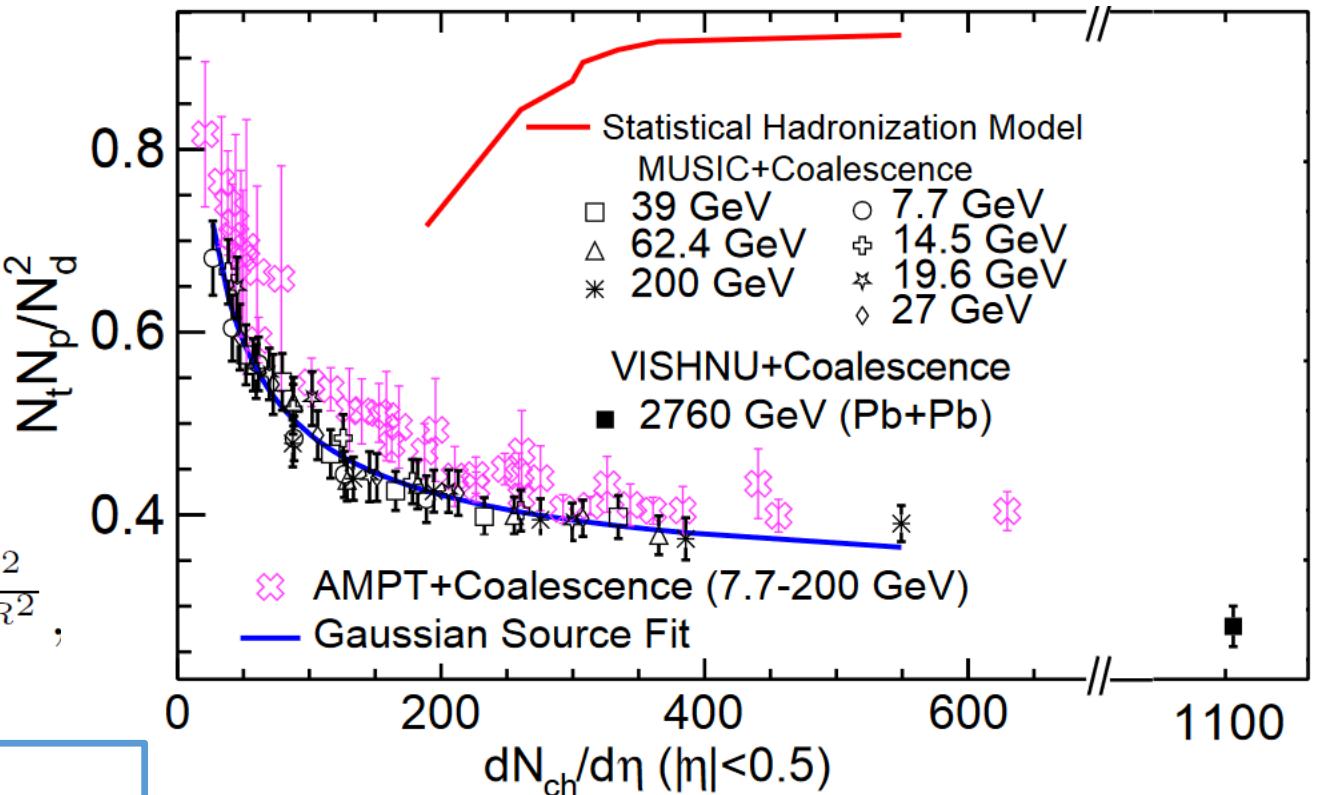
$$N_d = g_d \int d^3\mathbf{x}_1 d^3\mathbf{p}_1 d^3\mathbf{x}_2 d^3\mathbf{p}_2 f_n(\mathbf{x}_1, \mathbf{p}_1) \\ \times f_p(\mathbf{x}_2, \mathbf{p}_2) W_d(\mathbf{x}, \mathbf{p}),$$

$$N_t = g_t \int d^3\mathbf{x}_1 d^3\mathbf{p}_1 d^3\mathbf{x}_2 d^3\mathbf{p}_2 d^3\mathbf{x}_3 d^3\mathbf{p}_3 f_n(\mathbf{x}_1, \mathbf{p}_1) \\ f_n(\mathbf{x}_2, \mathbf{p}_2) f_p(\mathbf{x}_3, \mathbf{p}_3) W_t(\mathbf{x}, \boldsymbol{\lambda}, \mathbf{p}, \mathbf{p}_\lambda),$$

For Gaussian source:

$$f_{p,n}(\mathbf{x}, \mathbf{k}) = \frac{N_{p,n}}{(2\pi)^3 (mT_K R^2)^{\frac{3}{2}}} e^{-\frac{k^2}{2mT_K} - \frac{x^2}{2R^2}},$$

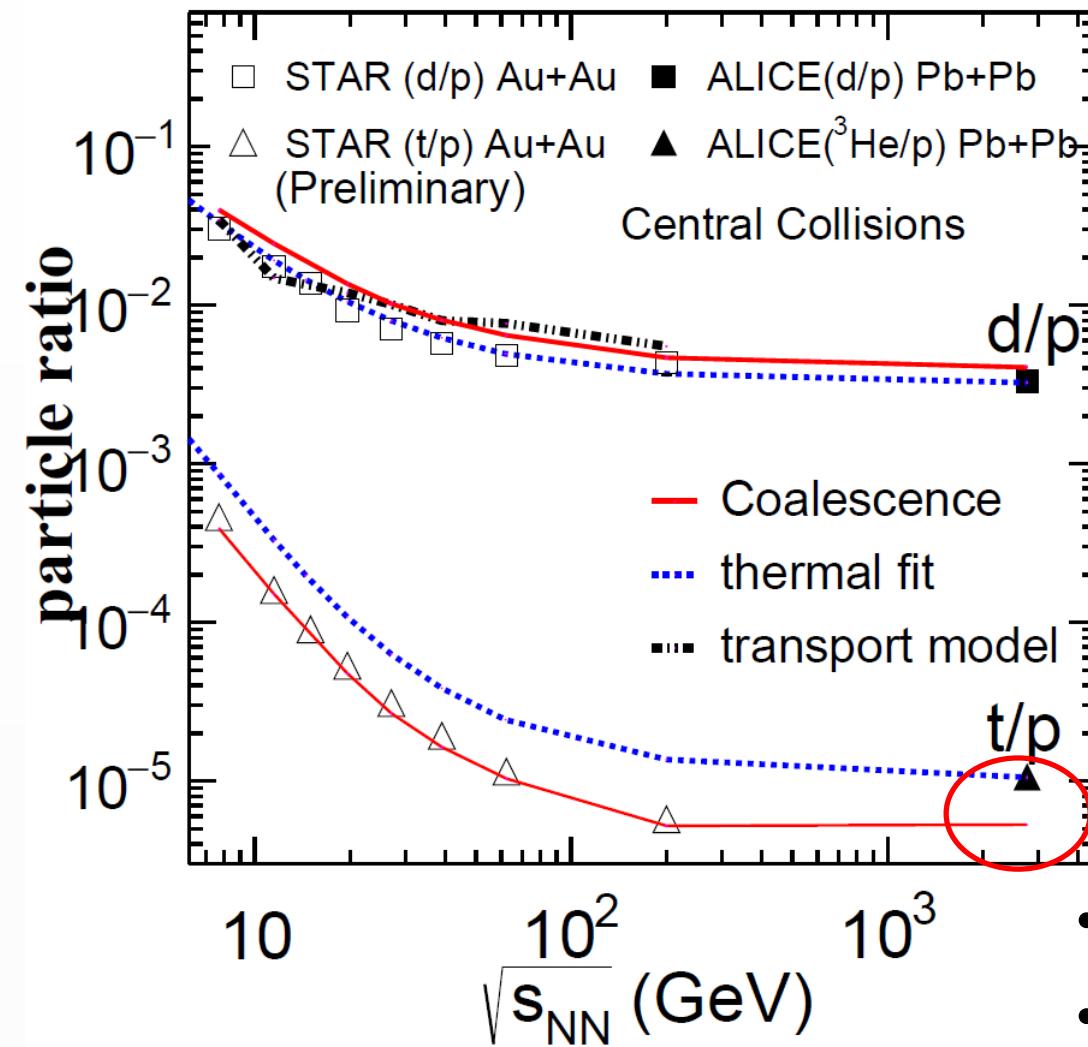
$$\frac{N_t N_p}{N_d^2} = \frac{4}{9} \left( \frac{1 + \frac{2r_d^2}{3R^2}}{1 + \frac{r_t^2}{2R^2}} \right)^3 = \frac{4}{9} \left( 1 + \frac{\frac{4}{3}r_d^2 - r_t^2}{2R^2 + r_t^2} \right)^3$$



W. Zhao, K. j. Sun, C. M. Ko and X. Luo, [arXiv:2105.14204 [nucl-th]].  
 W. Zhao, L. Zhu, H. Zheng, C.M. Ko and H. Song, PRC 98, 054905 (2018).  
 W. Zhao, C. Shen, C. M. Ko, Q. Liu and H. Song, PRC 102, 044912 (2020).  
 K.-J. Sun, C. M. Ko, and B. Donigus, Phys. Lett.B792,132 (2019).

- Multiplicity scaling of  $N_p \cdot N_t / N_d^2$  from MUSIC or AMPT+Coalescence is observed.
- Statistical model gives the opposite trend of  $N_p \cdot N_t / N_d^2$ .

# Comparisons between different models



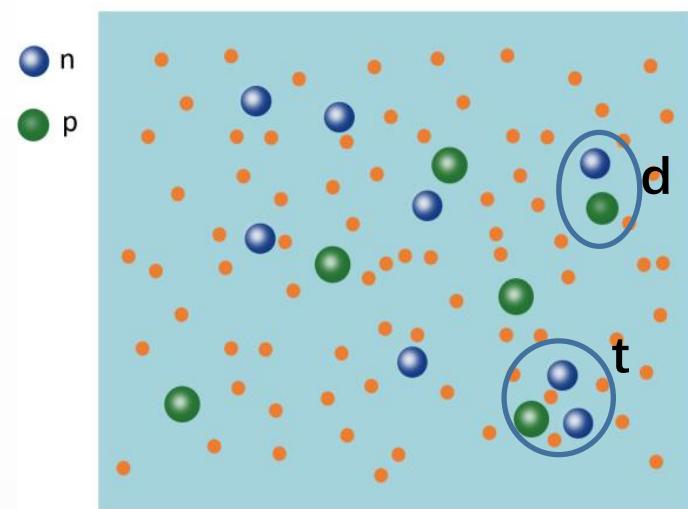
- Thermal model:  $N_A \approx g_A V(2\pi m_A T)^{3/2} e^{(A\mu_B - m_A)/T}$ 
  1. It nicely describe the d/p from RHIC to LHC energies.
  2. It overestimate the t/p at RHIC, but fit that at LHC.
- Transport model:  $\pi NN \leftrightarrow \pi d, NNN \leftrightarrow Nd, NN \leftrightarrow \pi d,$ 
  1. It nicely describe the d/p at RHIC.
  2. No t/p calculations.
- Coalescence model:
  1. It reasonably describes the d/p from RHIC to LHC energies.
  2. It well describe the t/p at RHIC, but underestimate that at LHC.
- The t/p at LHC is much larger than that at top RHIC.
- **Discrepancy of triton (helium-3) productions between top RHIC energy and LHC energy needs to be understood.**

# **Back Up**

# Coalescence model

$$\frac{d^3 N_A}{d\mathbf{P}_A^3} = \frac{g_A}{Z! \cdot N!} \int \prod_{i=1}^A p_i^\mu d^3 \sigma_{i\mu} \frac{d^3 \mathbf{p}_i}{E_i} f(\mathbf{x}_i, \mathbf{p}_i, t) \times f_A(\mathbf{x}'_1, \dots, \mathbf{x}'_A; \mathbf{p}'_1, \dots, \mathbf{p}'_A; t') \delta^{(3)} \left( \mathbf{P}_A - \sum_{i=1}^A \mathbf{p}_i \right),$$

H. Sato and K. Yazaki, PLB98, 153 (1981); E. Remler, Ann. Phys. 136, 293 (1981); M. Gyulassy, K. Frankel, and E. Remler, NPA402,596 (1983); S. Mrowczynski, J. Phys. G 13, 1089 (1987); S. Leupold and U. Heinz, PRC50, 1110 (1994); R. Scheibl and U. W. Heinz, PRC59, 1585(1999);



$$f_2(\rho, \mathbf{p}_\rho) = 8g_2 \exp \left[ -\frac{\rho^2}{\sigma_\rho^2} - \mathbf{p}_\rho^2 \sigma_\rho^2 \right], \quad \rho = \frac{1}{\sqrt{2}}(\mathbf{x}'_1 - \mathbf{x}'_2), \quad \mathbf{p}_\rho = \sqrt{2} \frac{m_2 \mathbf{p}'_1 - m_1 \mathbf{p}'_2}{m_1 + m_2},$$

$$f_3(\rho, \lambda, \mathbf{p}_\rho, \mathbf{p}_\lambda) = 8^2 g_3 \exp \left[ -\frac{\rho^2}{\sigma_\rho^2} - \frac{\lambda^2}{\sigma_\lambda^2} - \mathbf{p}_\rho^2 \sigma_\rho^2 - \mathbf{p}_\lambda^2 \sigma_\lambda^2 \right],$$

$$\lambda = \sqrt{\frac{2}{3}} \left( \frac{m_1 \mathbf{x}'_1 + m_2 \mathbf{x}'_2}{m_1 + m_2} - \mathbf{x}'_3 \right),$$

$$\mathbf{p}_\lambda = \sqrt{\frac{3}{2}} \frac{m_3 (\mathbf{p}'_1 + \mathbf{p}'_2) - (m_1 + m_2) \mathbf{p}'_3}{m_1 + m_2 + m_3},$$

**No free parameters.** Here,  $\sigma_\rho$  and  $\sigma_\lambda$  are taken from [Atom. Data Nucl. Data Tabl. 99, 69 (2013)].

1. The light nuclei productions encode the phase-space information of nucleons.

# Coalescence Parameters ( $A^{-1}\sqrt{B_A}$ )

$B_A$  ( $A=2,3$ ) describe the coalescence probability

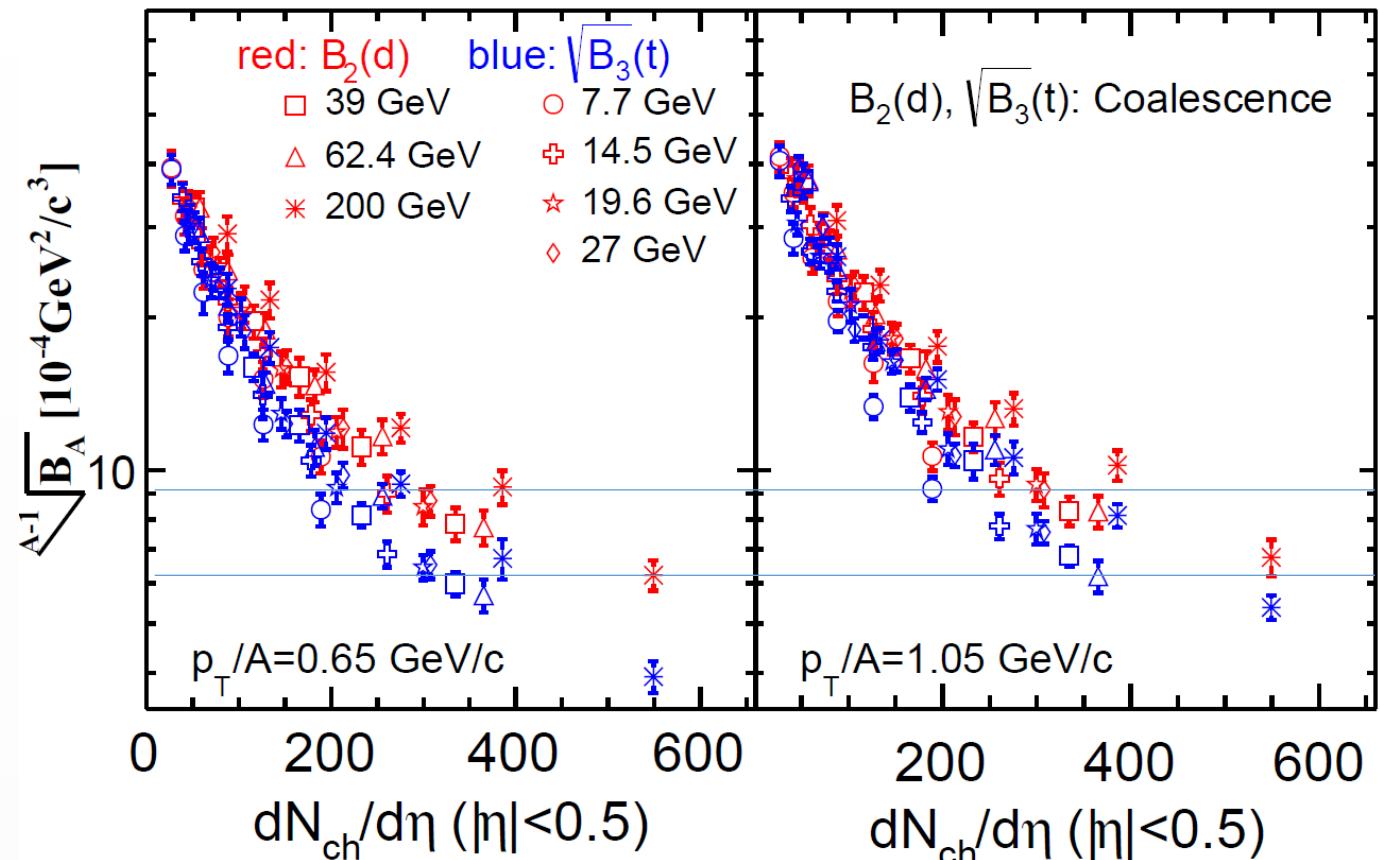
$$\begin{aligned} E_A \frac{d^3 N_A}{dp_A^3} &= B_A \left( E_p \frac{d^3 N_p}{dp_p^3} \right)^Z \left( E_n \frac{d^3 N_n}{dp_n^3} \right)^{A-Z} \\ &\approx B_A \left( E_p \frac{d^3 N_p}{dp_p^3} \right)^A \Big|_{\vec{p}_p = \vec{p}_n = \frac{\vec{p}_A}{A}} \end{aligned}$$

$B_A \propto V_{eff}^{1-A}$ .  $V_{eff}$ : effective volume.

S. Leupold and U. Heinz, PRC50, 1110 (1994);  
 R. Scheibl and U. W. Heinz, PRC59, 1585(1999);

Triton productions:

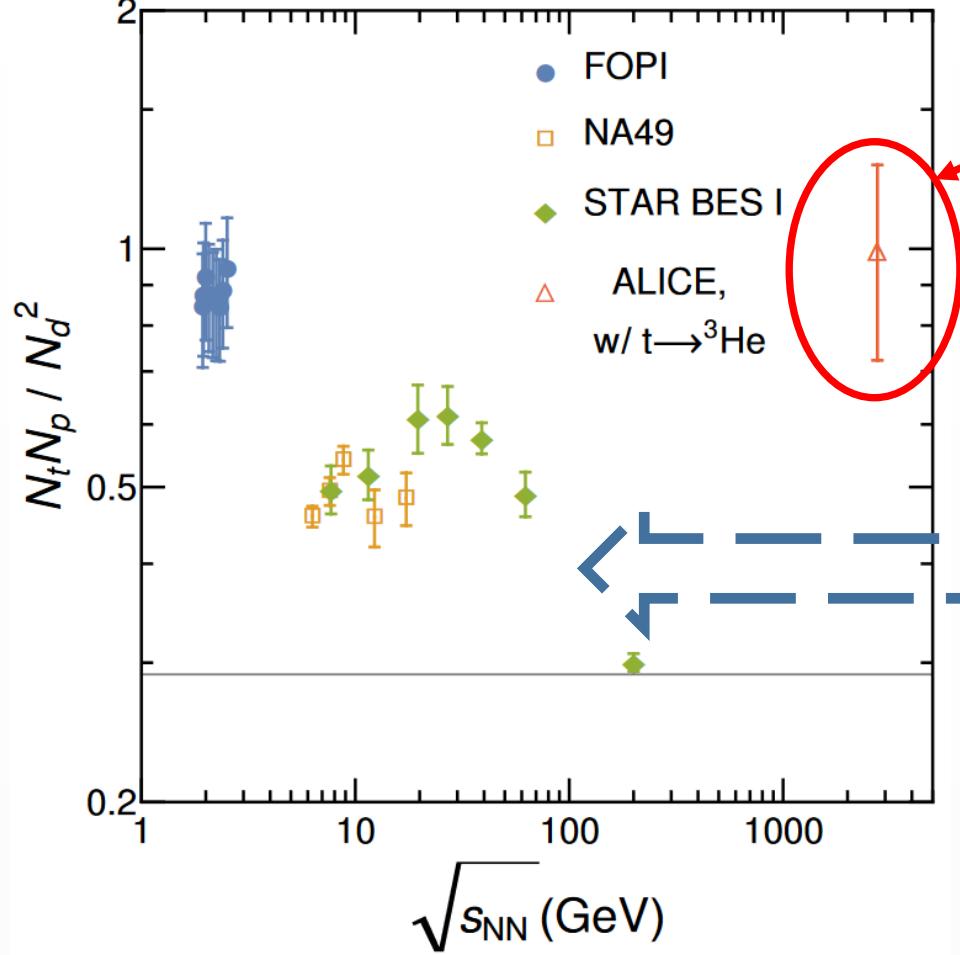
Three body:  $p + n + n \rightarrow t$



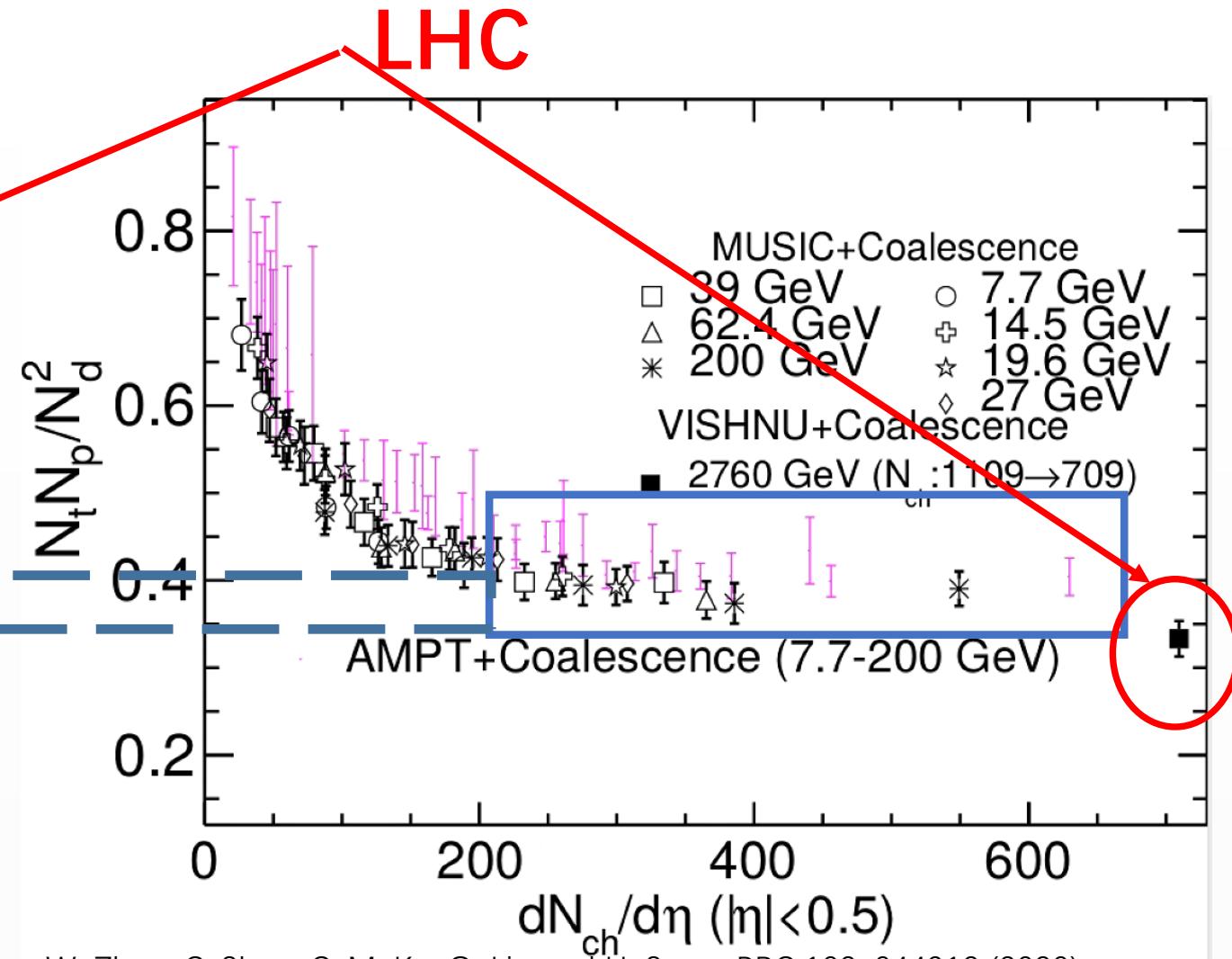
W. Zhao, C. Shen, C. M. Ko, Q. Liu and H. Song, PRC 102, 044912 (2020).  
 W. Zhao, K. j. Sun, C. M. Ko and X. Luo, [arXiv:2105.14204 [nucl-th]].

- $B_2(d/\bar{d})$  and  $\sqrt{B_3(t)}$  decrease monotonically with multiplicity.
- The slopes of  $B_2(d/\bar{d})$  and  $\sqrt{B_3(t)}$  are different, attribute to the different sizes of deuteron and triton.
- $A^{-1}\sqrt{B_A}$  at  $p_T/A = 1.05$  GeV is slightly larger than  $p_T/A = 0.65$  GeV, caused by the smaller  $V_{eff}$  at higher  $p_T$ .

# p-d-t ratio $N_p \cdot N_t / N_d^2$



D. Zhang (STAR), arXiv:2002.10677(2020).

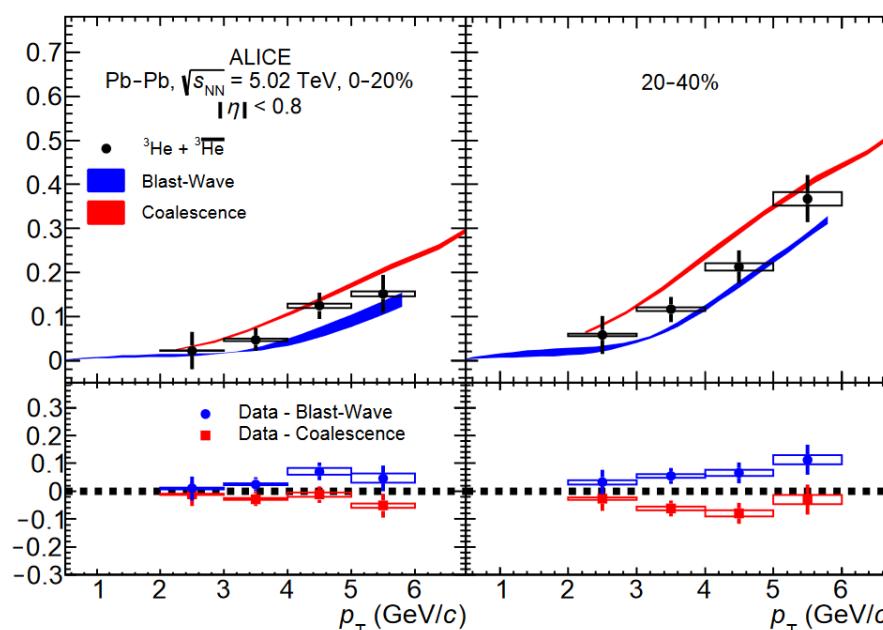
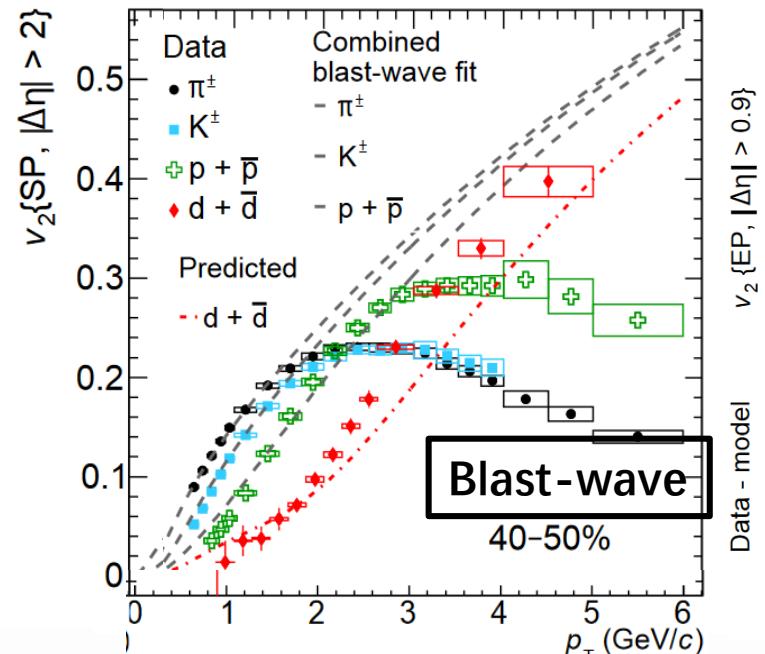


W. Zhao, C. Shen, C. M. Ko, Q. Liu and H. Song, PRC 102, 044912 (2020).

W. Zhao, K. j. Sun, C. M. Ko and X. Luo, [arXiv:2105.14204 [nucl-th]].

- The STAR data observes the non-monotonic dependence of  $N_p \cdot N_t / N_d^2$  on collision energy in central collisions at RHIC.
- In central collisions at RHIC,  $N_p \cdot N_t / N_d^2$  calculated by iEBE-MUSIC +Coalescence is flat.
- $N_p \cdot N_t / N_d^2$  at Pb-Pb at LHC from coalescence much smaller than the ALICE data.

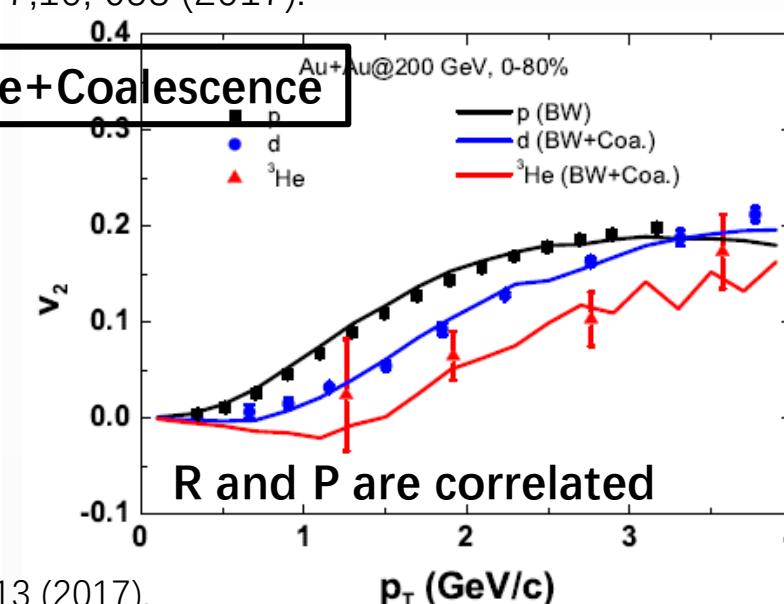
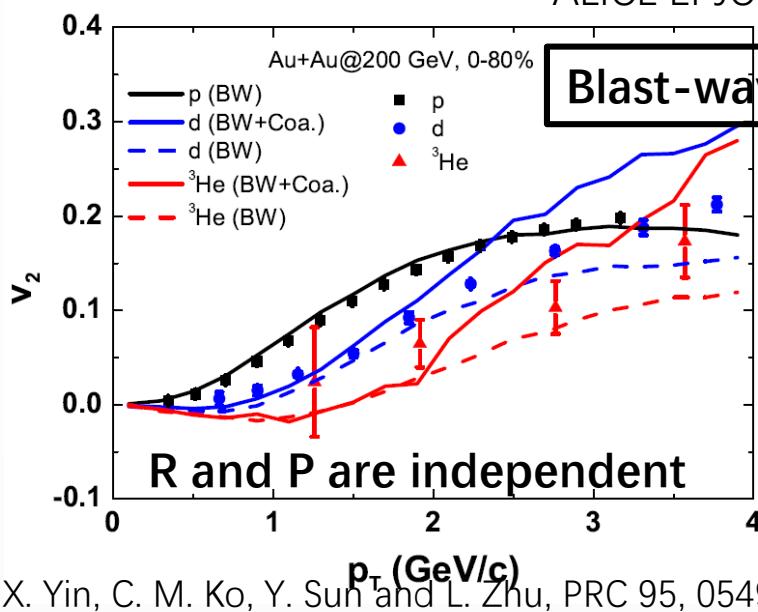
# Collective flow of light nuclei



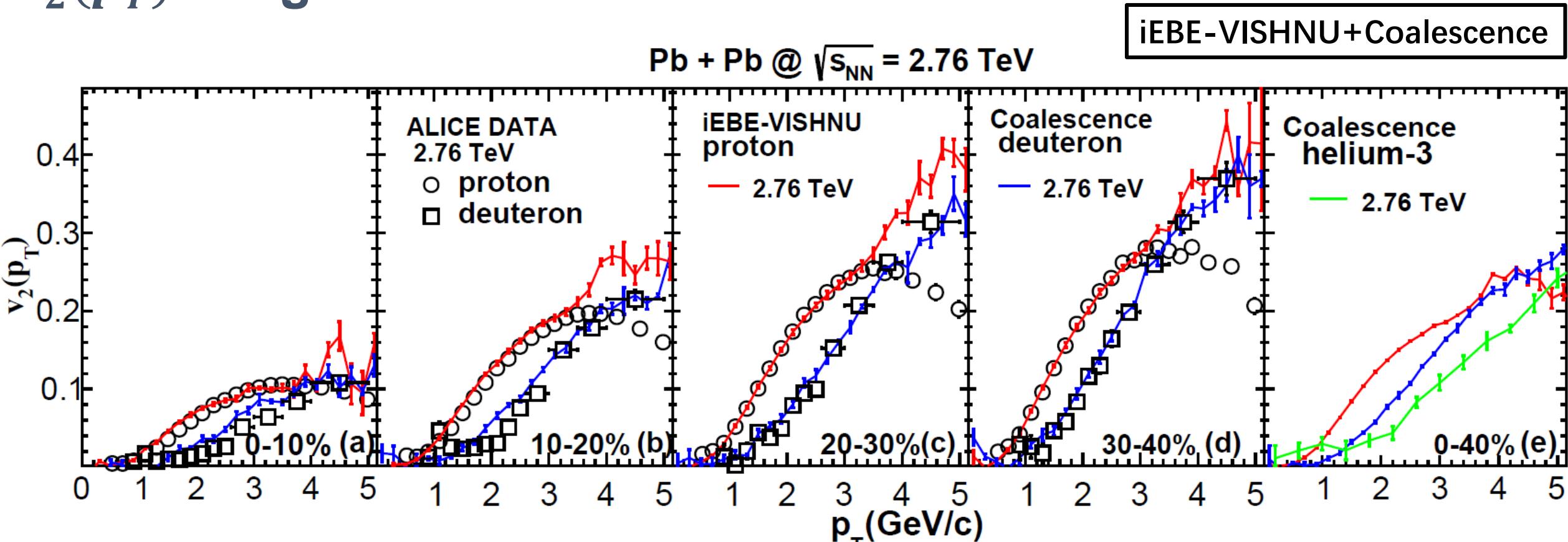
- Blast wave underpredicts  $v_2(p_T)$  of d and 3He.
- Simple Coalescence overestimates  $v_2(p_T)$  of d and 3He.

$$v_{2,^3\text{He}}(p_T) = \frac{3v_{2,p}(p_T/3) + 3v_{2,p}^3(p_T/3)}{1 + 6v_{2,p}^2(p_T/3)}.$$

- In the framework of coalescence model, the collective flow of light nuclei is sensitive to the correlations between spatial and momentum distributions of nucleon.

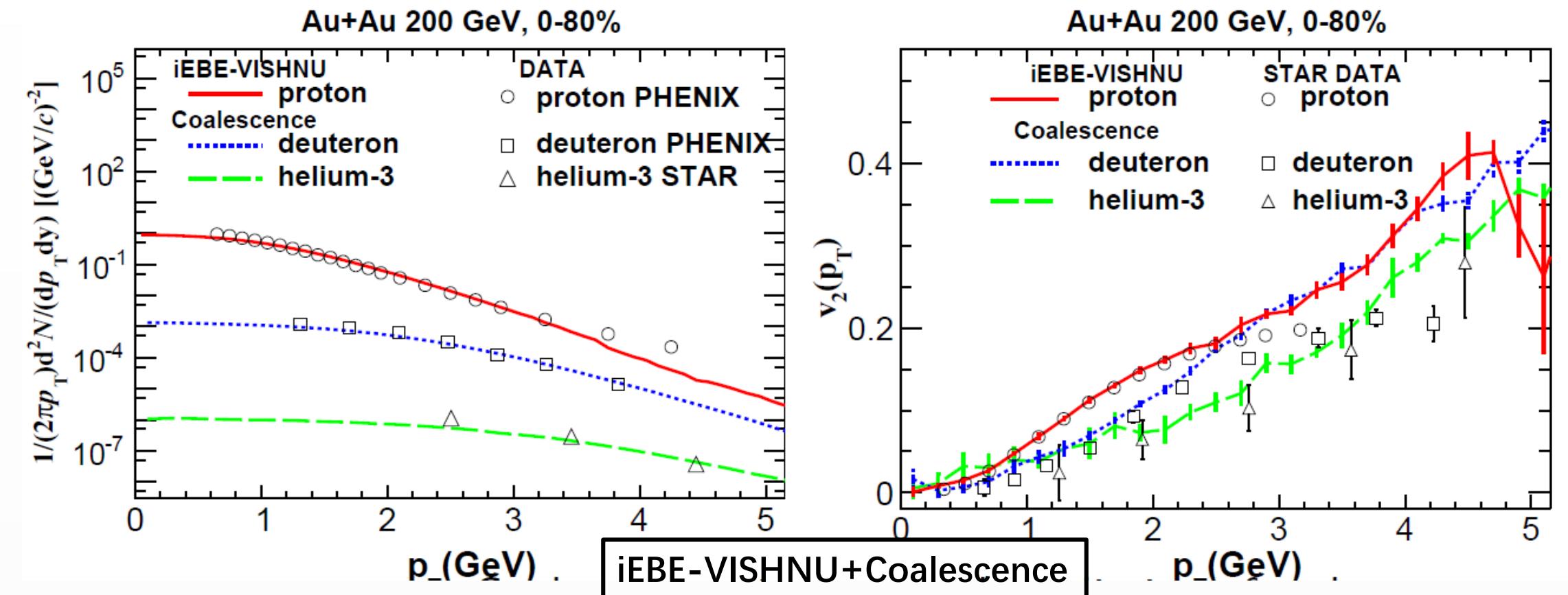


# $v_2(p_T)$ of light nuclei in Pb + Pb 2.76 TeV



- iEBE-VISHNU + Coalescence well reproduce the  $v_2(p_T)$  of deuteron in all centrality bins in Pb+Pb at 2.76 TeV.
- iEBE-VISHNU naturally gives a good description of spatial-momentum correlations of nucleon at kinetic freeze-out.
- No free parameters in the model simulations.

# Light nuclei production in Au + Au at 200 GeV



- iEBE-VISHNU + Coalescence gives a good predictions for the spectra and  $v_2(p_T)$  of d and  ${}^3\text{He}$  in Au+Au 200 GeV.