

Exploring jet transport coefficients in the strongly interacting quark-gluon plasma

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arXiv:2204.01561

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Dynamical QuasiParticle Model (DQPM)

- DQPM – effective model for the description of **non-perturbative** (strongly interacting) QCD based on IQCD EoS

- The QGP phase is described in terms of interacting **quasiparticles** - **massive quarks** and **gluons** - with **Lorentzian spectral functions**:

$$\rho_j(\omega, \mathbf{p}) = \frac{4\omega\gamma_j}{(\omega^2 - \mathbf{p}^2 - M_j^2)^2 + 4\gamma_j^2\omega^2}$$

- Field quanta are described in terms of dressed propagators with complex self-energies:

$$\text{gluon propagator: } \Delta^{-1} = P^2 - \Pi;$$

$$\text{gluon self-energy: } \Pi = M_g^2 - 2i\gamma_g\omega;$$

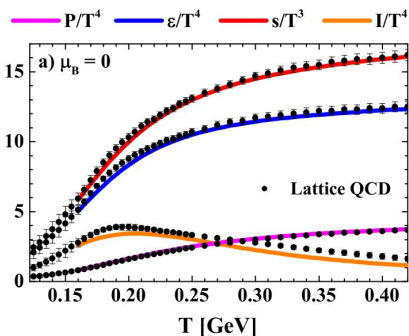
$$\text{quark propagator: } S_q^{-1} = P^2 - \Sigma_q$$

$$\text{quark self-energy: } \Sigma_q = M_q^2 - 2i\gamma_q\omega$$

- **Real part** of the self-energy - **thermal masses**
- **Imaginary part** of the self-energy - **interaction widths** of partons

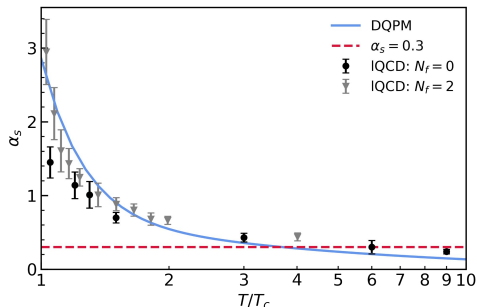
P. Moreau et al., PRC 100, 014911 (2019)

Input: entropy density vs T for $\mu_B=0$

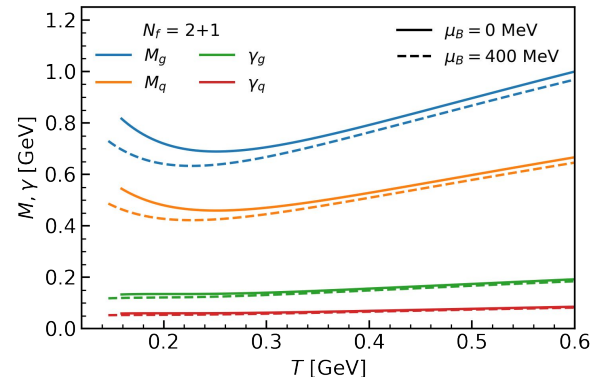


$$g^2(s/s_{SB}) = d((s/s_{SB})^e - 1)^f$$

$$s_{SB}^{QCD} = 19/9\pi^2 T^3$$



Masses and widths of quasiparticles depend on the temperature of the medium and μ_B



$$M_{q(\bar{q})}^2(T, \mu_q) = \frac{N_c^2 - 1}{8N_c} g^2(T, \mu_q) \left(T^2 + \frac{\mu_q^2}{\pi^2} \right)$$

$$M_g^2(T, \mu_q) = \frac{g^2(T, \mu_q)}{6} \left(\left(N_c + \frac{1}{2} N_f \right) T^2 + \frac{N_c}{2} \sum_q \frac{\mu_q^2}{\pi^2} \right)$$

$$\gamma_{q(\bar{q})}(T, \mu_q) = \frac{1}{3} \frac{N_c^2 - 1}{2N_c} \frac{g^2(T, \mu_q) T}{8\pi} \ln \left(\frac{2c}{g^2(T, \mu_q)} + 1 \right)$$

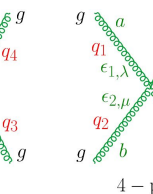
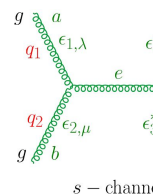
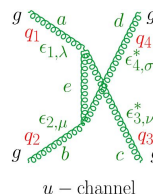
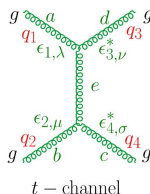
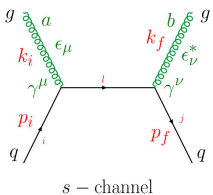
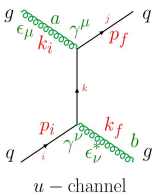
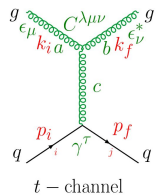
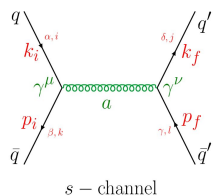
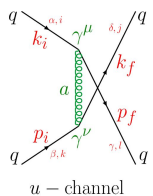
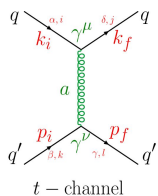
$$\gamma_g(T, \mu_q) = \frac{1}{3} N_c \frac{g^2(T, \mu_q) T}{8\pi} \ln \left(\frac{2c}{g^2(T, \mu_q)} + 1 \right)$$

Partonic interactions in DQPM

DQPM partonic cross sections: leading order diagrams

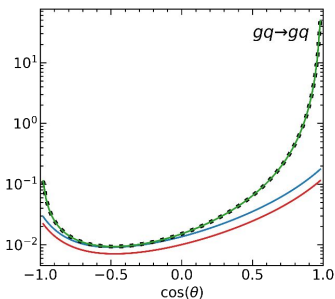
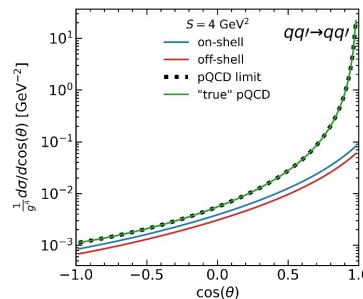
quark propagator:
$$i \xrightarrow{q} j = i\delta_{ij} \frac{q + M_q}{q^2 - M_q^2 + 2i\gamma_q q_0}$$

gluon propagator:
$$\begin{matrix} \mu, a \\ \text{-----} \\ \nu, b \\ q \end{matrix} = -i\delta_{ab} \frac{g^{\mu\nu} - q^\mu q^\nu / M_g^2}{q^2 - M_g^2 + 2i\gamma_g q_0}$$

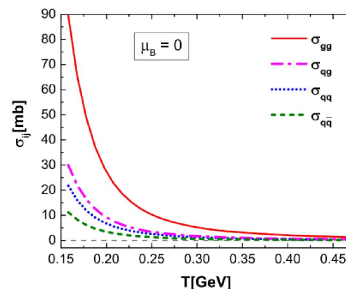


On-shell: final masses = pole masses

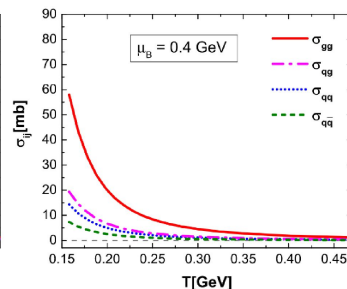
Off-shell: integration over final masses



→ can reproduce pQCD cross sections



→ strong T dependence

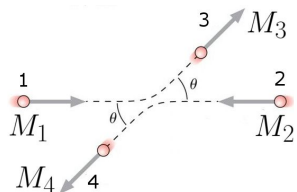


→ weak μ_B dependence

Transport coefficients in kinetic theory

On-shell:

- integration over momentums
- masses = pole masses



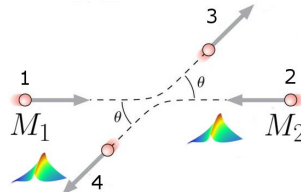
$$E^2 = m^2 + p^2$$

$$\begin{aligned} \langle \mathcal{O} \rangle^{\text{on}} &= \frac{1}{2E_i} \sum_{j=q,\bar{q},g} d_j f_j \int \frac{d^3 p_j}{(2\pi)^3 2E_j} \\ &\times \int \frac{d^3 p_1}{(2\pi)^3 2E_1} \int \frac{d^3 p_2}{(2\pi)^3 2E_2} \\ &\times (1 \pm f_1)(1 \pm f_2) \mathcal{O} |\overline{\mathcal{M}}|^2 (2\pi)^4 \delta^{(4)}(p_i + p_j - p_1 - p_2) \end{aligned}$$

$$\langle \mathcal{O} \rangle = \begin{cases} \mathcal{A}, & \mathcal{O} = (\mathbf{p} - \mathbf{p}') \\ dE/d\tau, & \mathcal{O} = (E - E') \\ \hat{q}, & \mathcal{O} = (p_t^2 - p_t'^2) \end{cases}$$

Off-shell:

- integration over momentums
- + two additional integrations over medium partons energy

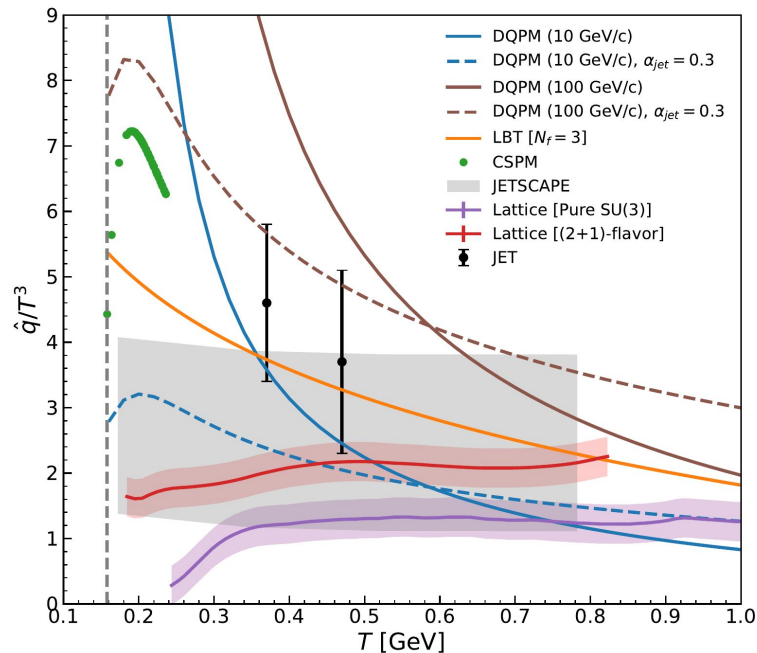


$$\frac{1}{2E} \rightarrow \int \frac{d\omega}{(2\pi)} \rho(\omega, \mathbf{p}) \theta(\omega)$$

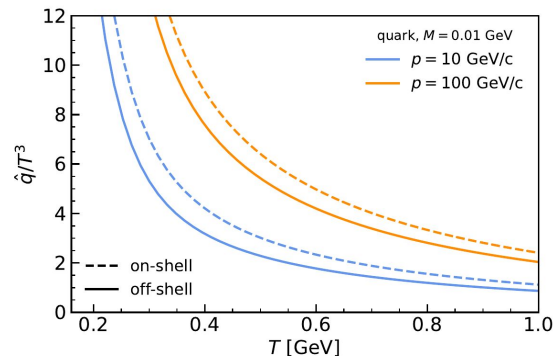
$$\begin{aligned} \langle \mathcal{O} \rangle^{\text{off}} &= \frac{1}{2E_i} \sum_{j=q,\bar{q},g} d_j f_j \int \frac{d^4 p_j}{(2\pi)^4} \rho(\omega_j, \mathbf{p}_j) \theta(\omega_j) \\ &\times \int \frac{d^3 p_1}{(2\pi)^3 2E_1} \int \frac{d^4 p_2}{(2\pi)^4} \rho(\omega_2, \mathbf{p}_2) \theta(\omega_2) \\ &\times (1 \pm f_1)(1 \pm f_2) \mathcal{O} |\overline{\mathcal{M}}|^2 (2\pi)^4 \delta^{(4)}(p_i + p_j - p_1 - p_2) \end{aligned}$$

Results: q-hat

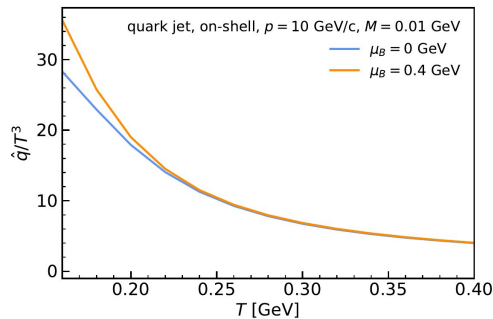
The DQPM \hat{q} (T) for elastic scattering of a jet quark vs other models



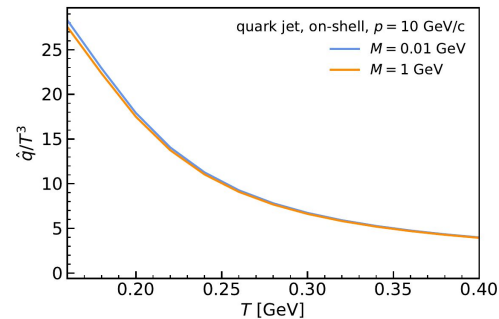
On-shell vs off-shell



μ_B dependence



Mass dependence

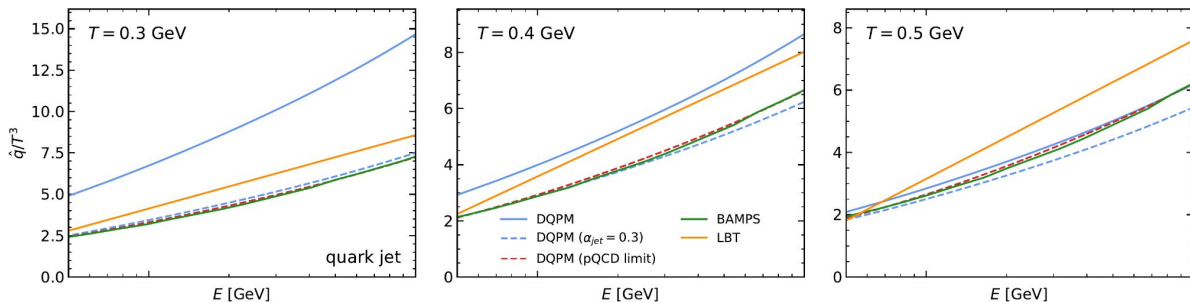


JET: K. M. Burke et al., *PRC* 90, 014909 (2014); **IQCD:** A. Kumar et al., *arxiv:2010.14463*;

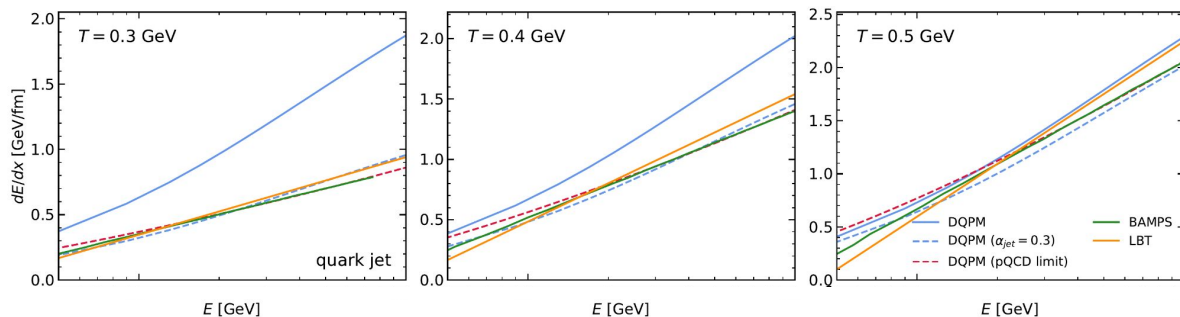
LBT: Y. He et al., *PRC* 91 (2015); **JETSCAPE:** S. Cao et al. *PRC* 104, 024905 (2021); **CSPM:** A. Mishra et al., *Physics* 4, 315 (2022)

Results: \hat{q} -hat and energy loss

Momentum dependence of the scaled \hat{q} -hat



Momentum dependence of the energy loss



Summary:

- Transport coefficients \hat{q} -hat and dE/dx are evaluated for the propagation of the jet parton (quark and gluon) through the strongly interacting QGP based on the DQPM
 - ◆ \hat{q} -hat coefficient is calculated as a function of medium temperature, jet momentum, jet mass, chemical potential
 - ◆ dE/dx is calculated as a function of jet momentum
- DQPM predicts stronger energy loss than pQCD models due to the elastic interaction of jet parton with non-perturbative QGP
- DQPM reproduces the pQCD limits for zero masses and widths of medium partons

Future:

- Investigate radiative processes