

Space-time evolution of critical fluctuations in an expanding system

Azumi Sakai (Hiroshima Univ.)

azumi-sakai@hiroshima-u.ac.jp



Co-authors:

Koichi Murase (YITP, Kyoto Univ.)

Hirotsugu Fujii (Tokyo Univ.)

Tetsufumi Hirano (Sophia Univ.)



Introduction

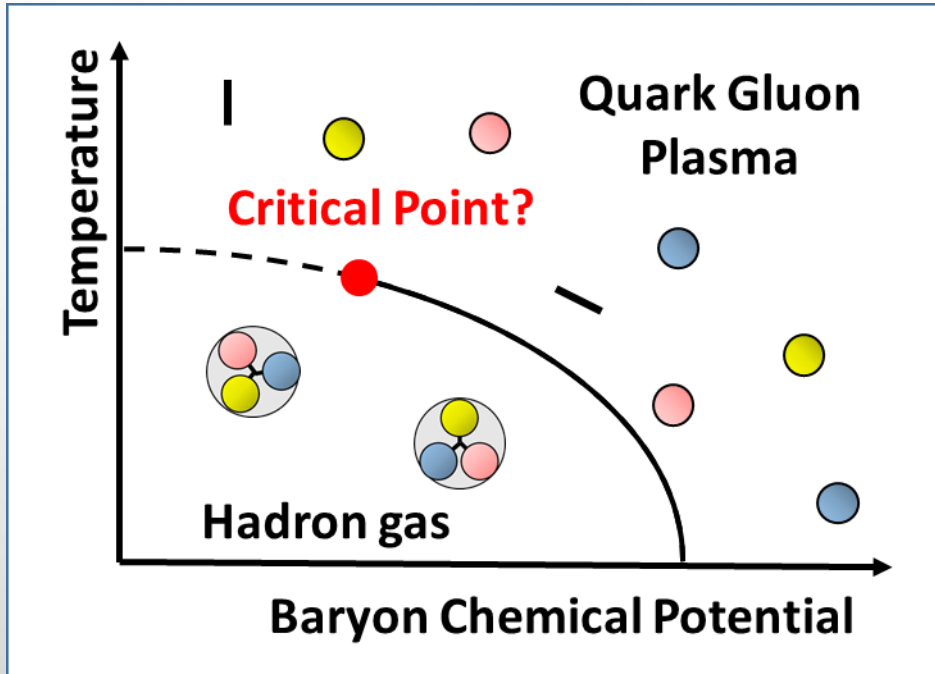


Fig. QCD Phase Diagram

Search for the QCD Critical Point

Dynamical modeling of heavy-ion collisions

Equilibrium: Infinite

Chiral condensate σ (Fast mode) \rightarrow Ignored

Heavy-ion collisions: Finite

Time-scale separation is unclear

$\rightarrow \sigma$ could affect the critical dynamics

Purpose of study:

We construct dynamical model of critical fluctuations

\rightarrow Coupling of Baryon number density n + Chiral condensate σ

\rightarrow Relaxation of baryon diffusion current from causality

Analyze the effects on correlation of baryon number density n

Model: coupled Langevin equations

$$\frac{d(\delta\sigma)}{dt} = -\Gamma \frac{\delta F}{\delta(\delta\sigma)} + \tilde{\lambda} \nabla^2 \frac{\delta F}{\delta(\delta n)} + \xi_\sigma$$

$$\frac{\tau_R dV}{dt} + V = \tilde{\lambda} \nabla \frac{\delta F}{\delta(\delta\sigma)} + \lambda \nabla \frac{\delta F}{\delta(\delta n)} + \xi_n$$

$$\frac{d(\delta n)}{dt} = -\nabla \cdot V$$

Fluctuation-dissipation relation

$$\langle \xi_i(x) \xi_j(x') \rangle = 2T \gamma_{ij} \delta^4(x - x')$$

$\Gamma, \tilde{\lambda}, \lambda$: Transport coefficient

T : Temperature

D.T. Son, M.A. Stephanov, Phys.Rev. D70 (2004) 056001
H. Fujii, M. Ohtani, Phys.Rev.D70:014016,2004

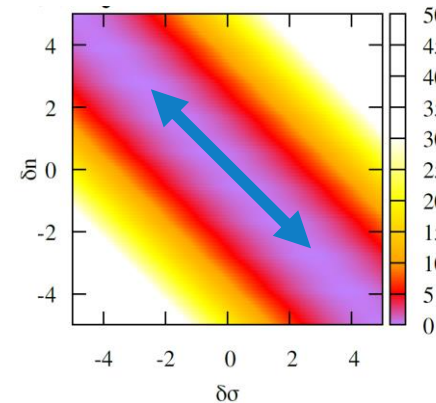
Critical fluctuations

Chiral condensate $\delta\sigma \equiv \bar{q}q - \langle \bar{q}q \rangle$

Baryon number density $\delta n \equiv \bar{q}\gamma_0 q - \langle \bar{q}\gamma_0 q \rangle$

Potential of free energy functional $F[\delta\sigma, \delta n]$

$$V(\delta\sigma, \delta n) = \frac{A}{2} \delta\sigma^2 + \boxed{B\delta\sigma\delta n} + \frac{C}{2} \delta n^2$$



Coupling term

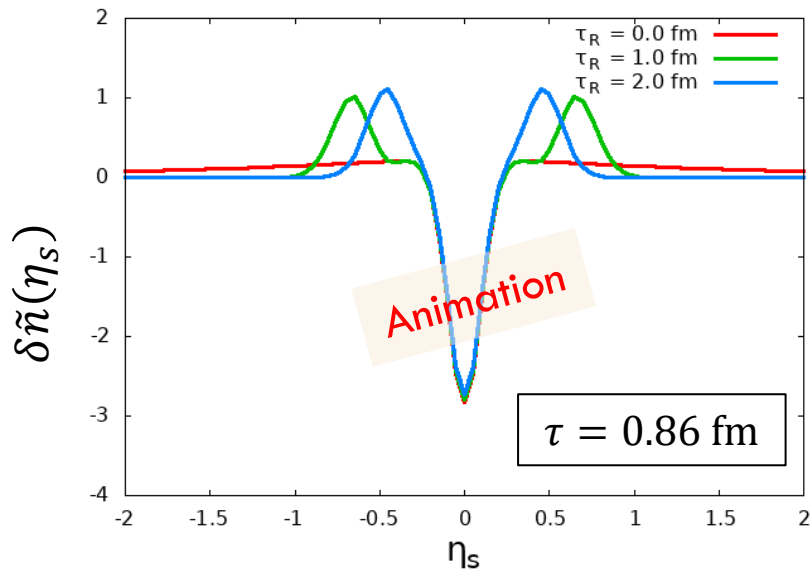
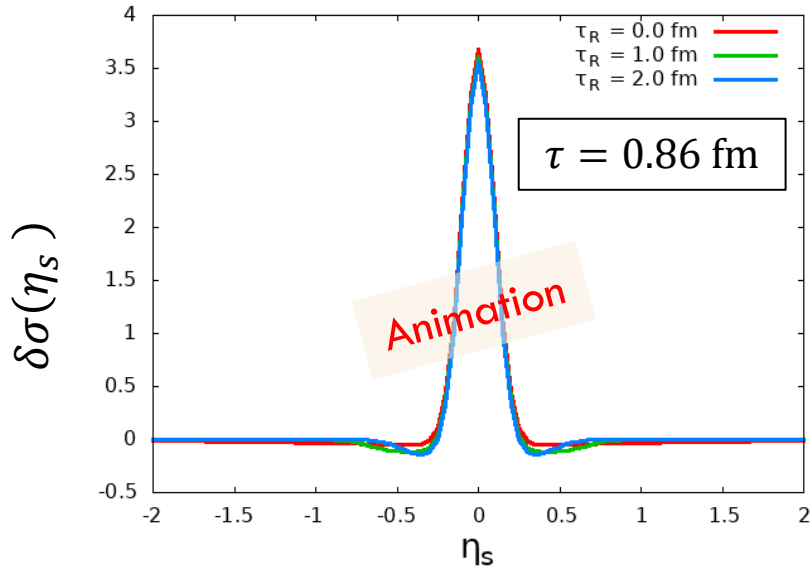
Flat direction
 $T_c = 160 \text{ MeV}$

Diffusion equation violates causality

➔ Introduce **relaxation time τ_R**
to make the propagation speed finite

New!

Results: Space-time evolution (1+1D)



Setups:

Temperature: $T(\tau) = T_0 \left(\frac{\tau_0}{\tau}\right)^{c_s^2}$

Initial temperature: $T_0 = 220$ MeV

Initial time: $\tau_0 = 0.6$ fm

Sound velocity: $c_s^2 = 0.15$

Critical temperature: $T_c = 160$ MeV

Without noise $\xi = 0$

Conserved quantity $\delta\tilde{n} \equiv \tau\delta n$

Initial conditions:

$$\delta\sigma(\eta_s, \tau_0) = \frac{1}{\sqrt{2\pi w^2}} e^{-\frac{\eta_s^2}{2w^2}}$$

$$\delta\tilde{n}(\eta_s, \tau_0) = 0$$

$\delta\tilde{n} \neq 0$ at $\tau > \tau_0$

$\rightarrow \delta\sigma$ affects δn evolution in $\tau - \eta$ space (1+1D)

$\tau_R = 0$ fm: $\delta\tilde{n}$ instantly diffuse to large η_s

$\tau_R > 0$ fm: $\delta\tilde{n}$ diffuse at finite time

**Signal propagates in a finite time
by considering relaxation time τ_R**

Results: Correlation evolution vs τ_R

Correlation function:

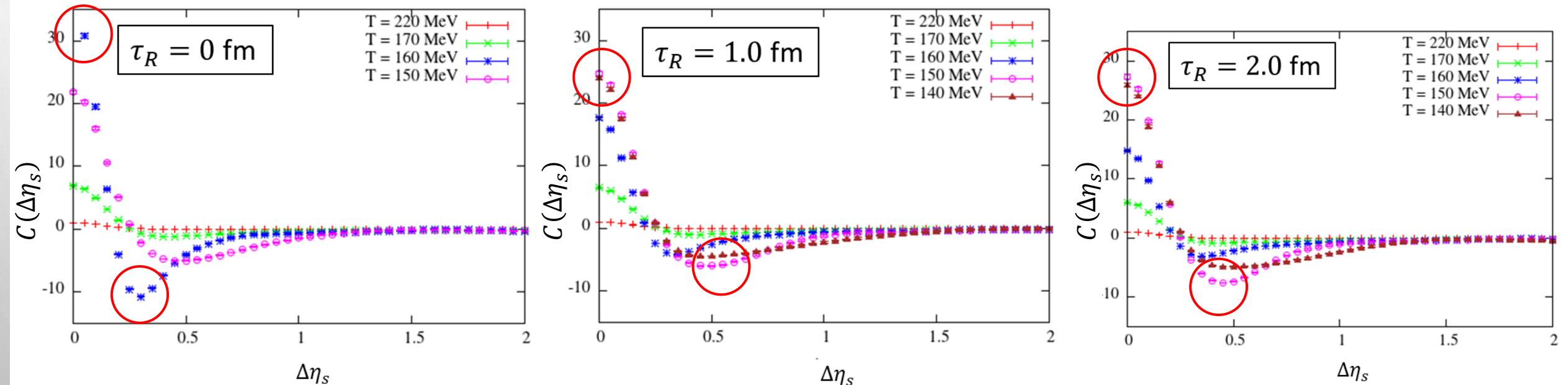
$$C(\Delta\eta_s) = \frac{\langle \delta\tilde{n}(\eta_s)\delta\tilde{n}(\eta_s + \Delta\eta_s) \rangle}{\langle \delta\tilde{n}(\eta_s)\delta\tilde{n}(\eta_s + \Delta\eta_s) \rangle_{T=220 \text{ MeV}, \Delta\eta_s=0}}$$

Setups:

$$\delta(\eta - \eta') \Rightarrow \frac{1}{\sqrt{2\pi w^2}} e^{-\frac{(\eta - \eta')^2}{2w^2}} \quad w: \text{Gaussian width } (w = 0.1)$$

Initial conditions:

$$\delta\sigma(\eta_s, \tau_0) = 0, \text{ Thermal equilibrium for } \delta\tilde{n}(\eta_s, \tau_0) \quad B = 0$$



Peak at $T_c = 160$ MeV

Peak between 150 MeV and 160 MeV

Peak around $T \sim 150$ MeV

$C(\Delta\eta_s)$ at $\Delta\eta_s = 0$ reaches its peak value earlier for $\tau_R = 0$ fm than $\tau_R = 1, 2$ fm cases

Finite relaxation time τ_R causes a delay of response

Summary and Outlook

◆ We constructed a second-order model for critical fluctuations in 1+1D and analyzed the space-time evolution and correlation evolution

- Coupled Baryon density δn and Chiral condensate $\delta\sigma$
- Introduced relaxation time τ_R

◆ Space-time evolution of $\delta\sigma$ and δn

- $\delta\sigma$ distribution affects δn distribution
- Signal **propagates in a finite time** by considering relaxation time τ_R

◆ Correlation evolution vs τ_R

- Peak at $\Delta\eta_s \sim 0$
- Finite relaxation time τ_R causes **a delay of response**

◆ Outlook

- Analyze the effect on observables