



Strong Interaction Studies in Λ^- hadron systems up to $S = -3$ with ALICE

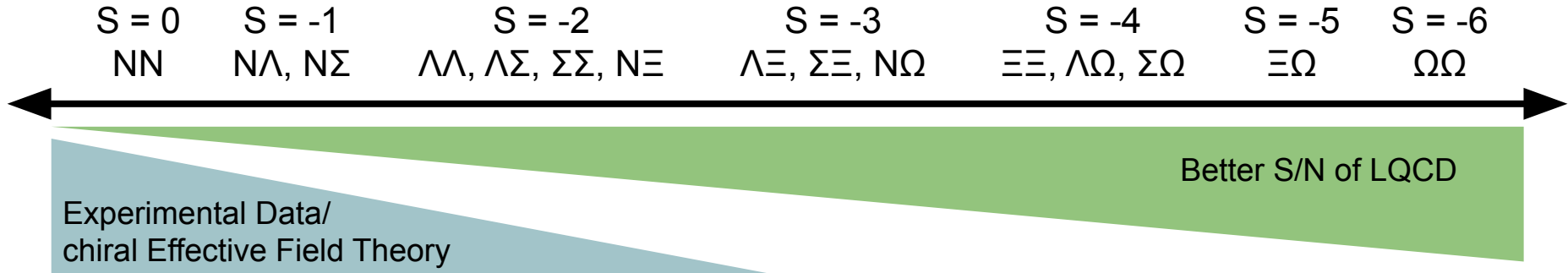
Georgios Mantzaridis
on behalf of the ALICE Collaboration
Technical University of Munich
29.06.2022

HYP
2022
PRAGUE

14th International Conference
on Hypernuclear and Strange
Particle Physics

June 27–July 1, 2022
Prague, Czech Republic

The strong interaction with Λ -hadrons



The strong interaction with Λ -hadrons

$S = 0$
NN

$S = -1$
 $\Lambda\Lambda, N\Sigma$

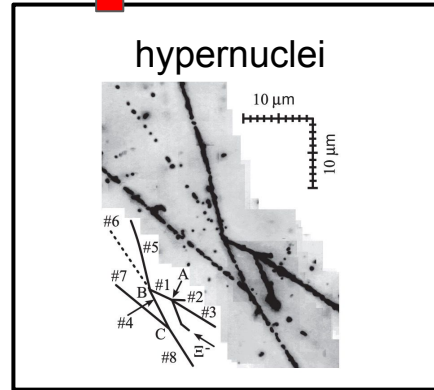
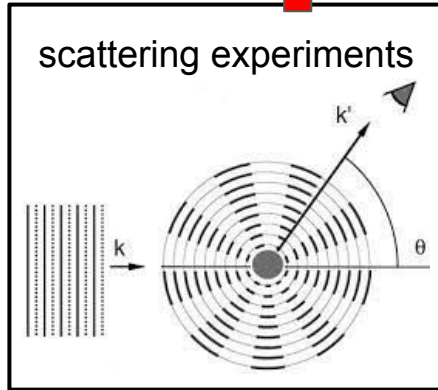
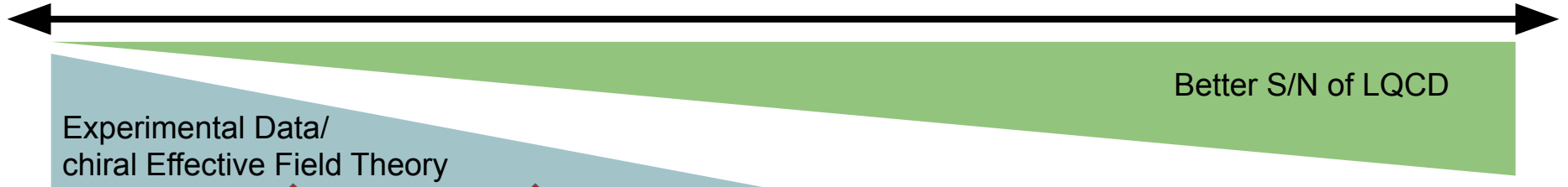
$S = -2$
 $\Lambda\Lambda, \Lambda\Sigma, \Sigma\Sigma, N\Xi$

$S = -3$
 $\Lambda\Xi, \Sigma\Xi, N\Omega$

$S = -4$
 $\Xi\Xi, \Lambda\Omega, \Sigma\Omega$

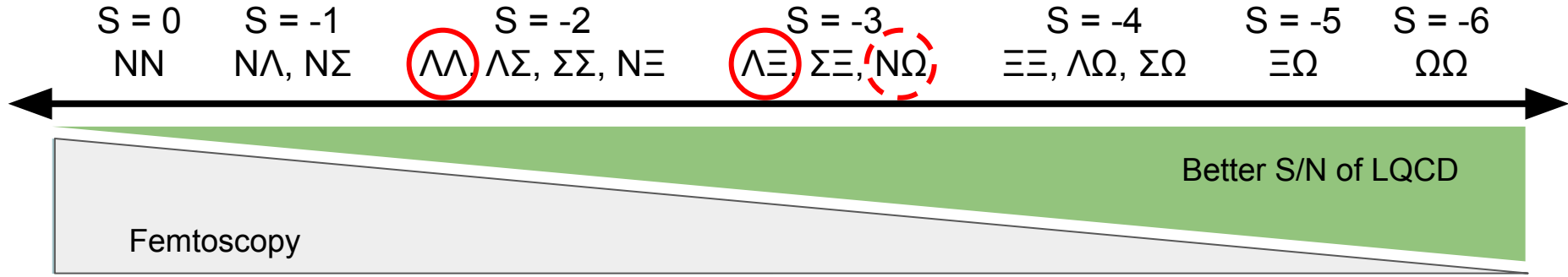
$S = -5$
 $\Xi\Omega$

$S = -6$
 $\Omega\Omega$



H. Takahashi et al., PRL 87 (2001) 212502

The strong interaction with Λ -hadrons



A Bridge to overcome this misalignment

Method: Femtoscopy

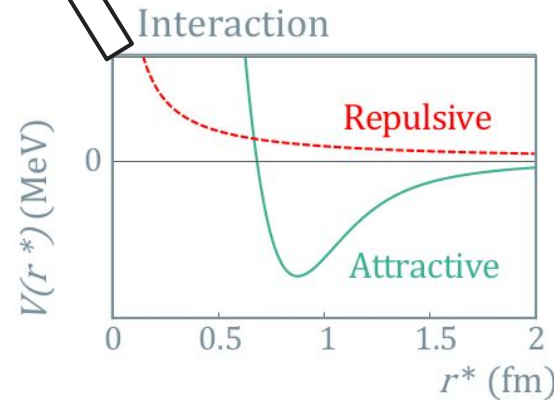
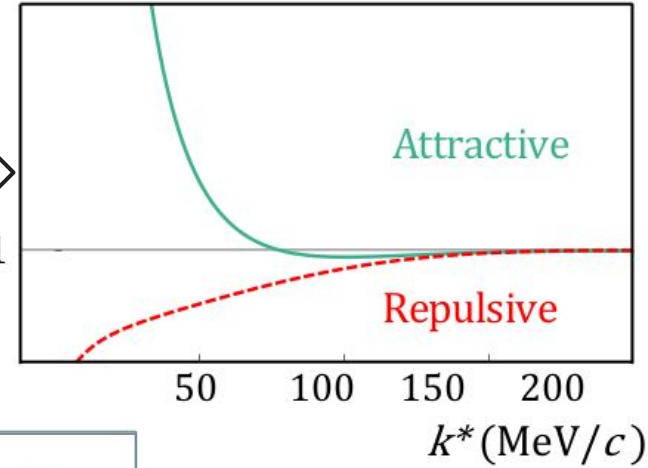
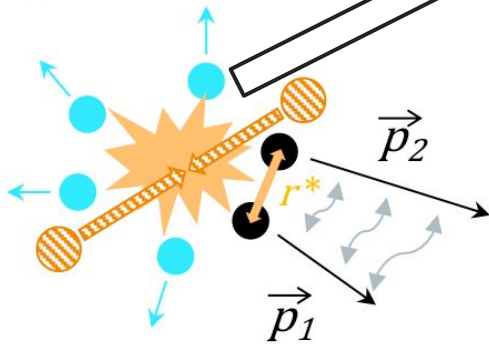
Figures: *Nature* 588, 232 (2020)

Central part: **The correlation function** in terms of the relative momentum k^*

$$k^* = 1/2 \cdot |\vec{p}_1^* - \vec{p}_2^*|$$

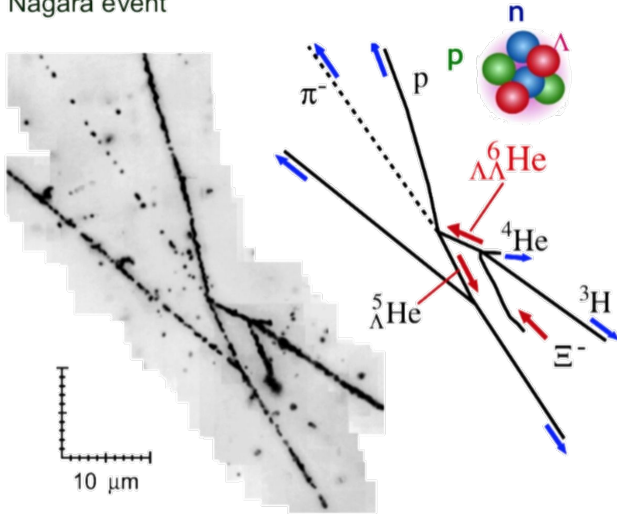
Correlation Function

$$C(k^*) = \xi(k^*) \otimes \frac{N_{\text{same}}(k^*)}{N_{\text{mixed}}(k^*)} = \int S(r^*) |\Psi(k^*, r^*)|^2 d^3r^*$$



|S| = 2: Λ - Λ interaction – before femtoscopy

Nagara event

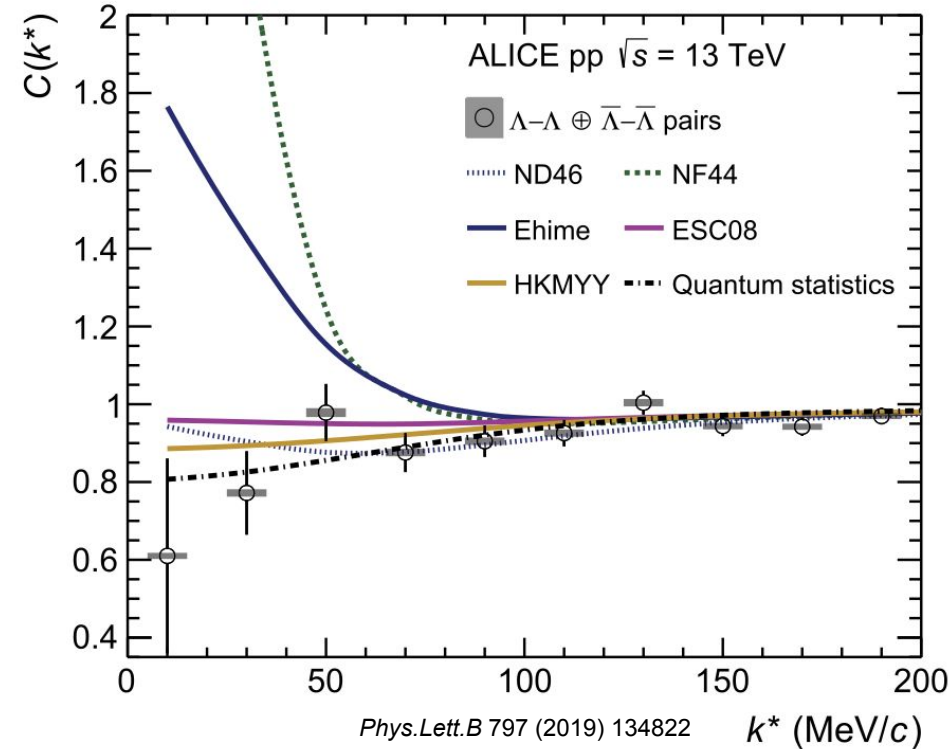


H. Takahashi et al., PRL 87 (2001) 212502

Search for H-dibaryon: bound state of $uusdd$ ($\Lambda\Lambda$)

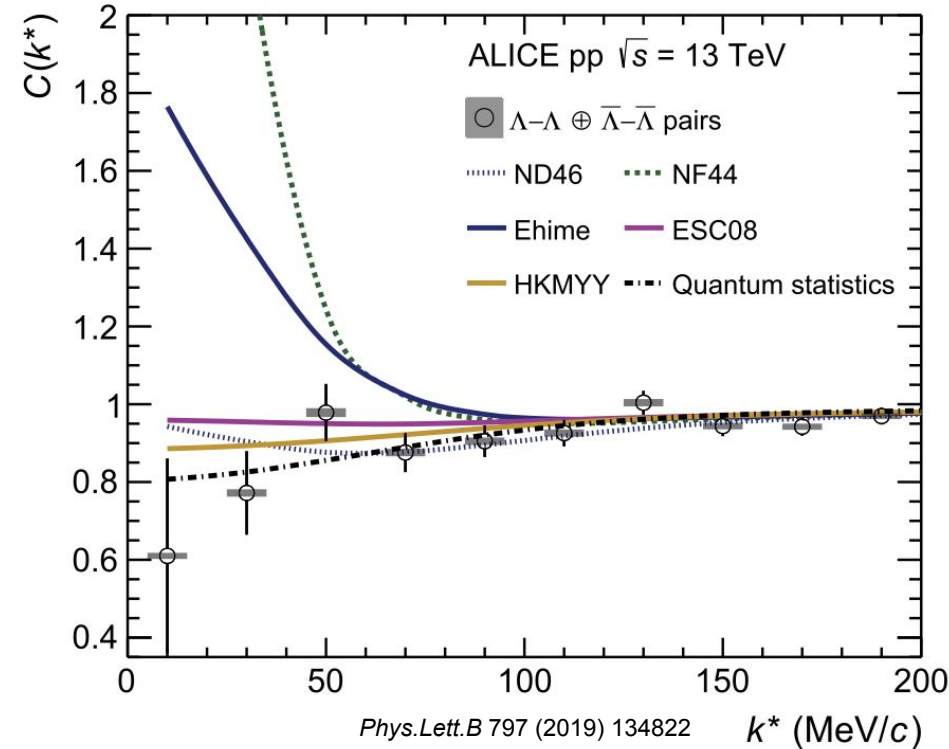
- No evidence of a H decay in elementary e^+e^- collisions
- Nagara event: Double $\Lambda\Lambda$ hypernuclei ${}^6_{\Lambda\Lambda}\text{He}$
 - Hints to a weak attractive interaction
 - Limit on binding energy: $B_{\Lambda\Lambda} = 6.91 \pm 0.16 \text{ MeV}$

$|S| = 2$: Λ - Λ interaction – with femtoscopy



- Combined measurement of pp (@ 7,13 TeV) and p-Pb (@ 5.02 TeV) collisions:
- Incompatible predictions:
 - Ehime: strongly attractive interaction
 - NF44: shallow bound state
- Compatible predictions:
 - ESC08 and HKMY: shallow attractive interaction
 - ND46: bound state

$|S| = 2$: Λ - Λ interaction – with femtoscopy

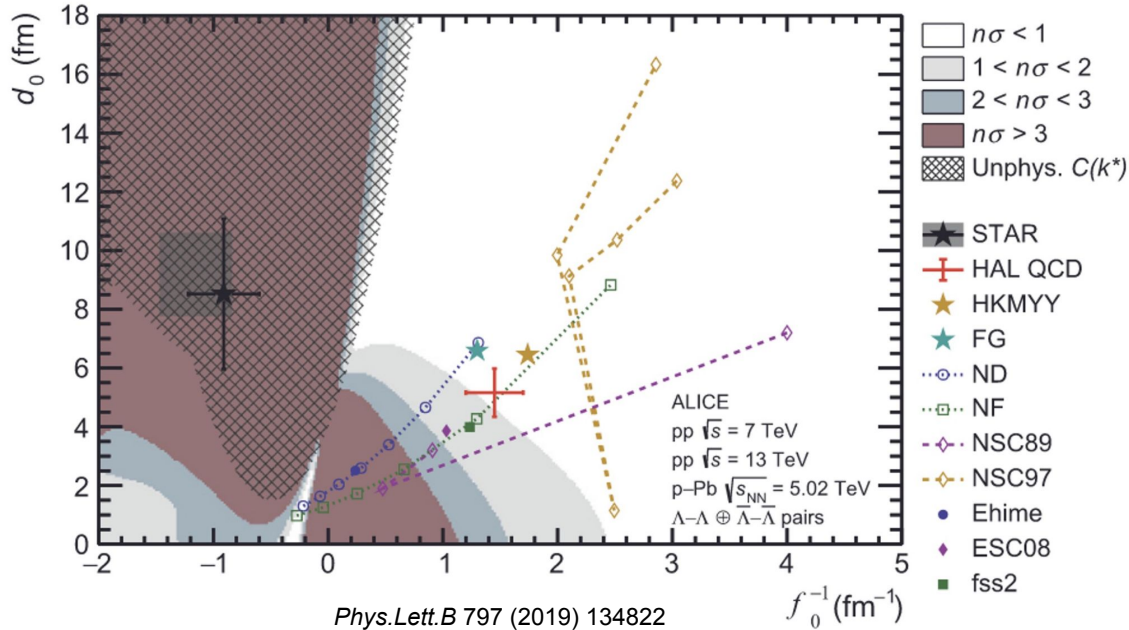


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- Incompatible predictions:
 - Ehime: strongly attractive interaction
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Effective-range expansion: d_0 and f_0 :

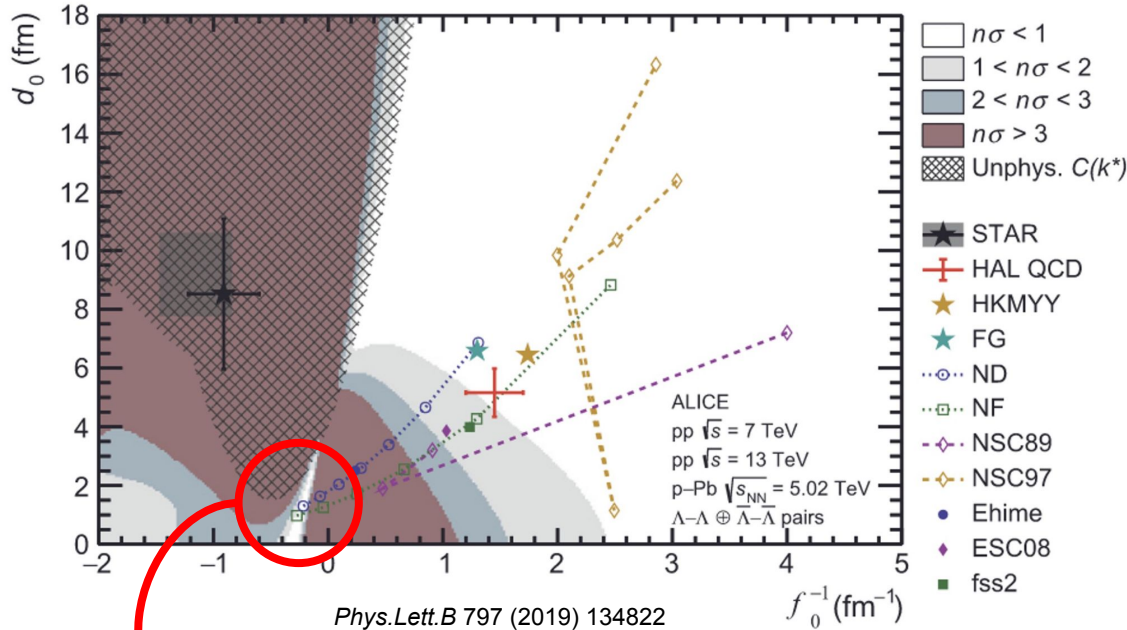
- $f_0 > 0$: attractive interaction
- $f_0 < 0$: repulsive interaction
- $f_0 < 0$ and $d_0 > |f_0|/2$: bound state

$|S| = 2$: Λ - Λ interaction – with femtoscopy



- Scan the (f_0^{-1}, d_0) parameter space with the Lednicky Lyuboshits model in terms of $n\sigma$ deviations
- Compatible with:
 - Shallow attractive interaction
 - Bound state

|S| = 2: Λ - Λ interaction – with femtoscopy



$$B_{\Lambda\Lambda} = 3.2_{-2.4}^{+1.6} \text{ (stat)}_{-1.0}^{+1.8} \text{ (syst) MeV}$$

- Scan the (f_0^{-1}, d_0) parameter space with the Lednicky Lyuboshits model in terms of $n\sigma$ deviations
- Compatible with:
 - Shallow attractive interaction
 - Bound state
- New upper limit on the binding energy of the H-dibaryon via a transformation from (f_0^{-1}, d_0) to $(B_{\Lambda\Lambda}, d_0)$ using

$$B_{\Lambda\Lambda} = \frac{1}{m_{\Lambda} d_0^2} \left(1 - \sqrt{1 + 2d_0 f_0^{-1}} \right)^2$$

$|S| = 3$: Λ - Ξ^- interaction – before femtoscopy



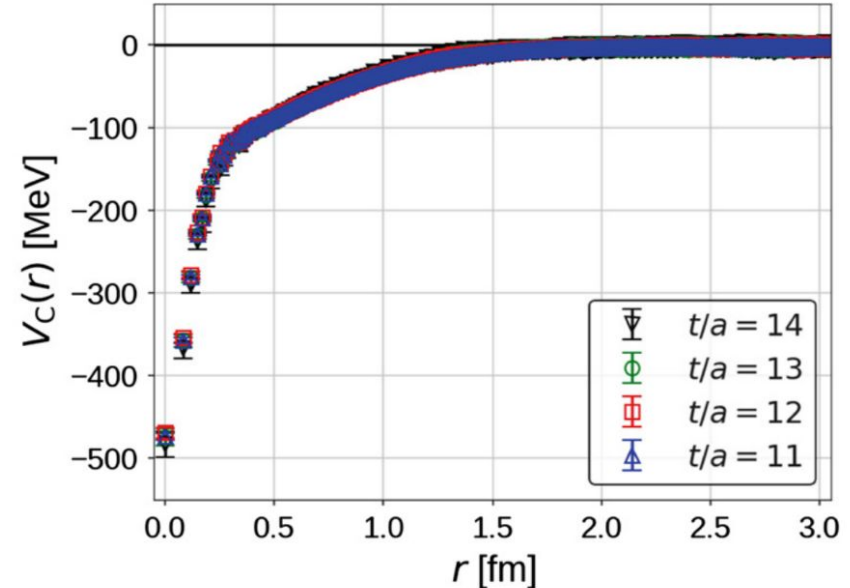
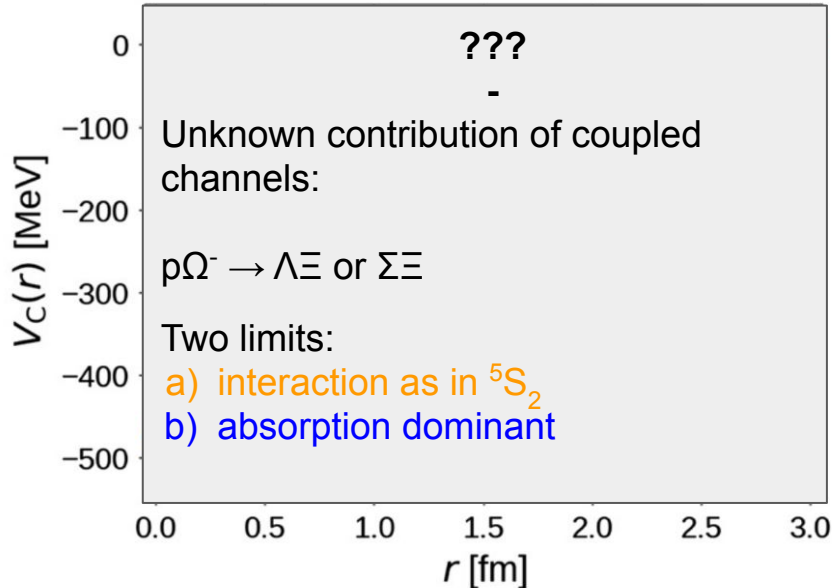
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$|S| = 3$: $p\text{-}\Omega^-$ interaction with femtoscopy

- Proton ($J_p = 1/2$) + Omega ($J_\Omega = 3/2$)
- angular momentum negligible

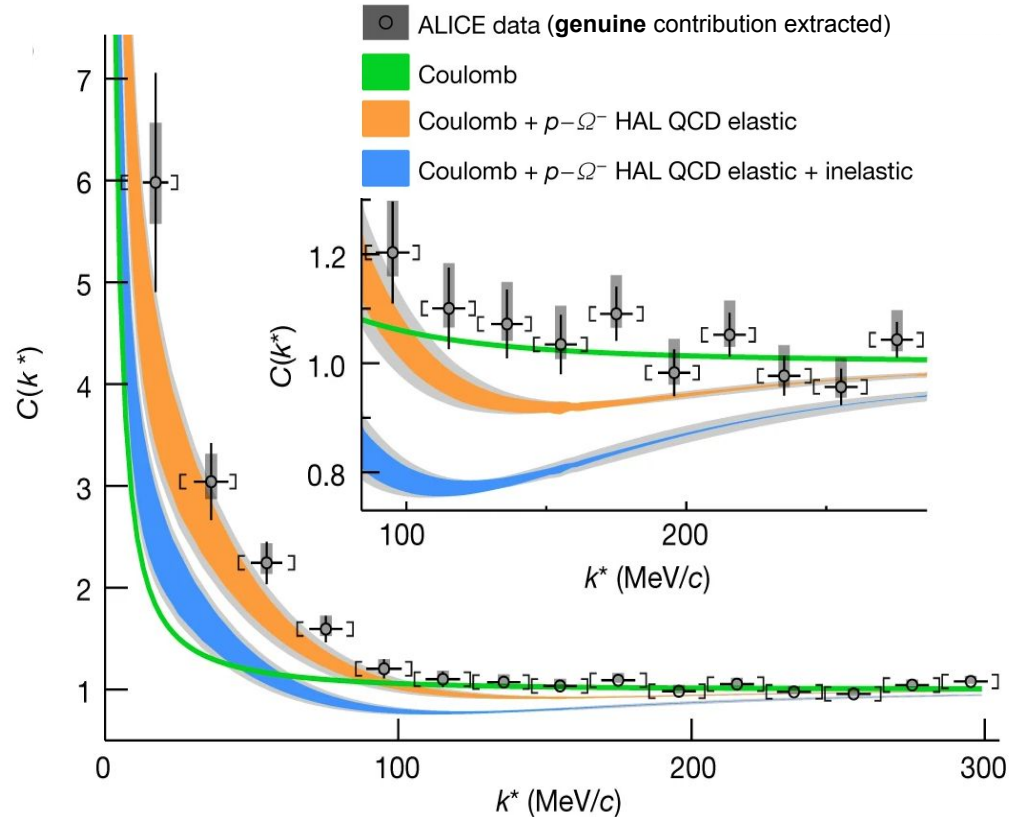
$N\Omega(^3S_1)$

$N\Omega(^5S_2)$



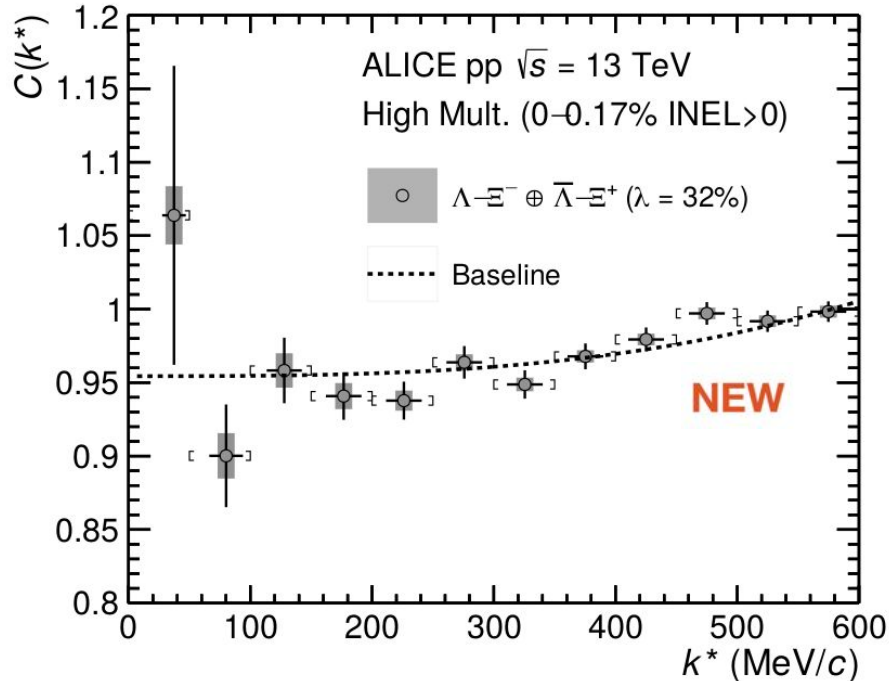
$|S| = 3$: $p\text{-}\Omega^-$ interaction with femtoscopy

- Indication of missing attractive interaction when considering only Coulomb
- Better agreement of data without inelastic contributions
- Higher accuracy in the data than in the theoretical calculation
- Prediction of a bound state with binding energy **2.5 MeV**
⇒ not reproduced by the data



$|S| = 3$: Λ - Ξ^- interaction – with femtoscopy

Baseline (no interaction):



arXiv:2204.10258, submitted to PLB

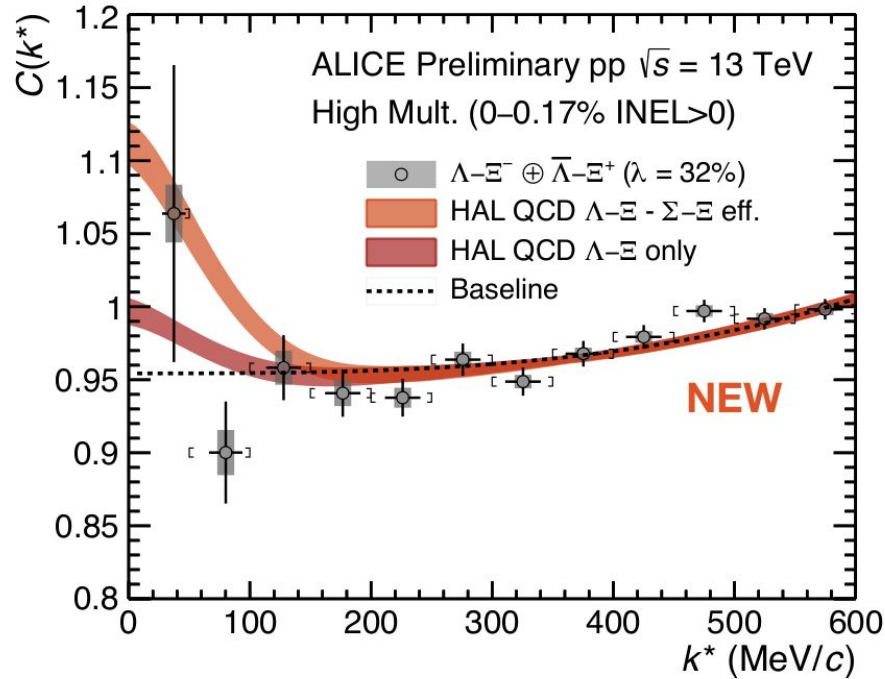
First experimental observation of the Λ - Ξ^- interaction

Baseline (dotted line):

- Constrained at large $k^* \in [200, 800]$ MeV/c
- Compatibility with the data @ $k^* < 200$ MeV/c:
 - 0.78 $n\sigma$**
 - ⇒ No significant deviation of the data from the baseline
 - ⇒ Indication of shallow Λ - Ξ^- interaction
 - ⇒ New publication: [arXiv:2204.10258](https://arxiv.org/abs/2204.10258)

$|S| = 3: \Lambda-\Xi^-$ interaction – with femtoscopy

Comparison with Lattice QCD^(*)



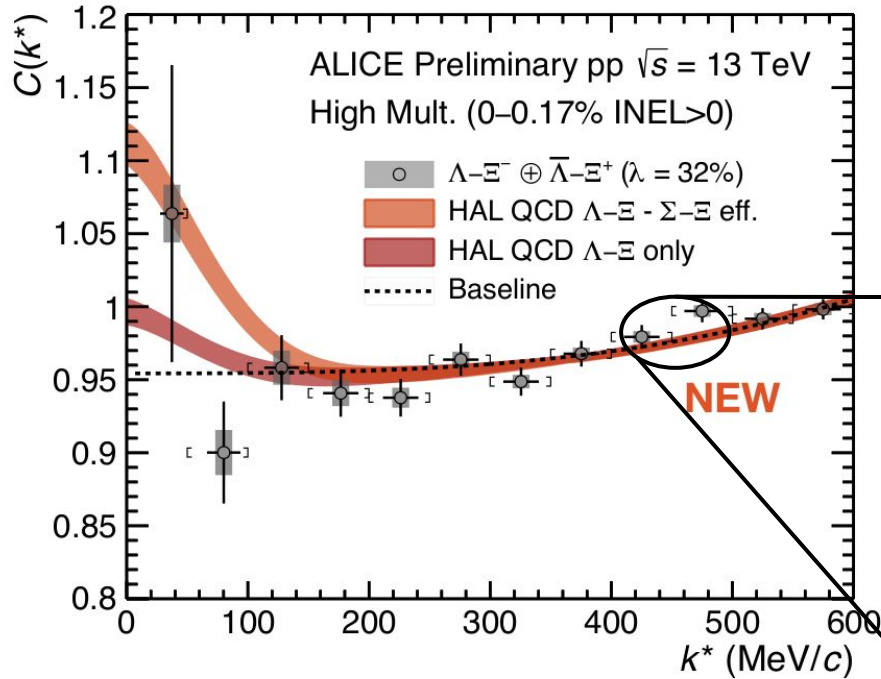
arXiv:2204.10258, submitted to PLB

- Unknown contribution from coupled channels in Lattice QCD calculations (see p- Ω^- interaction)
 - Coupling $\Lambda\Xi-\Sigma\Xi$ sizable in HAL QCD calculation
 - “No coupling” preferred: 0.64 $n\sigma$ vs. 1.43 $n\sigma$ but no sensitivity yet
- No $N\Omega$ cusp visible \Rightarrow hint to negligible coupling

^(*) N. Ishii et al.. EPJ Web of Conferences 175, 05013 (2018)

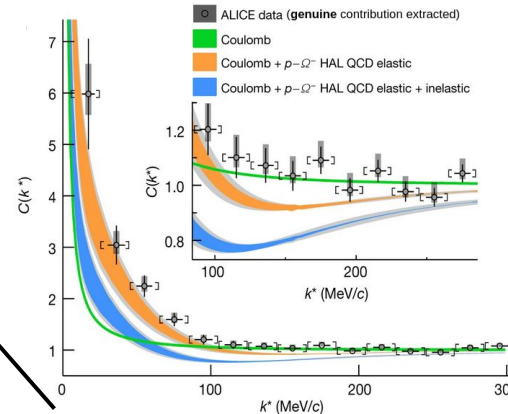
$|S| = 3: \Lambda-\Xi^-$ interaction – with femtoscopy

Comparison with Lattice QCD(*)



arXiv:2204.10258, submitted to PLB

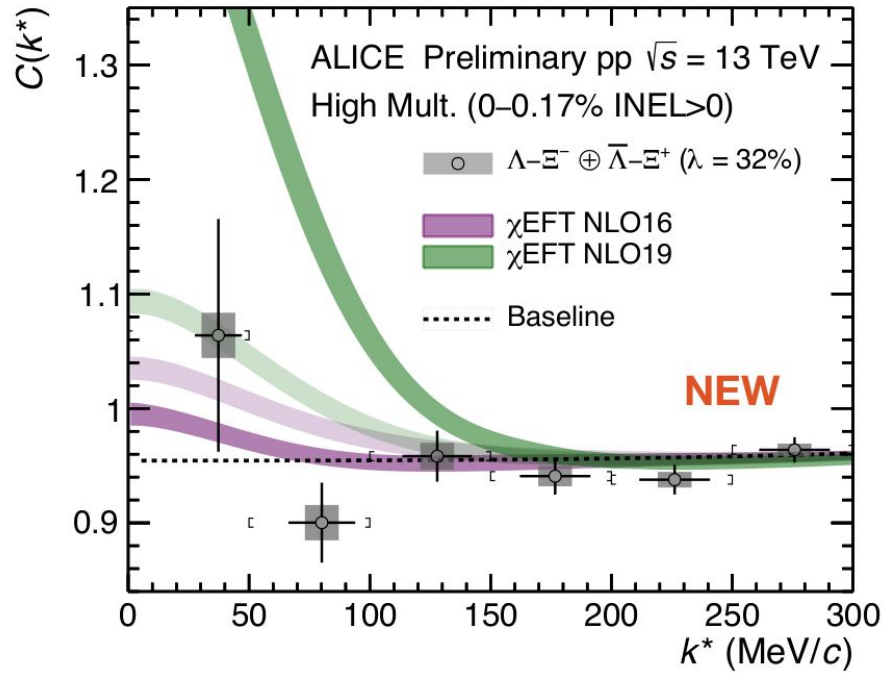
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(*) N. Ishii et al. EPJ Web of Conferences 175, 05013 (2018)

$|S| = 3$: Λ - Ξ^- interaction – with femtoscopy

Comparison with χ EFT NLO^(*)



arXiv:2204.10258, submitted to PLB

potential (cut-off)	singlet		triplet		$n\sigma$
	f_0	d_0	f_0	d_0	
NLO16 (500)	0.99	5.77	-0.026	142.9	0.56 – 0.93
NLO16 (650)	0.91	4.63	0.12	32.02	0.91 – 1.61
NLO19 (500)	0.99	5.77	1.66	1.49	5.47 – 7.26
NLO19 (650)	0.91	4.63	0.42	6.33	1.30 – 2.10

* J. Haidenbauer, U.-G. Meißner, arXiv:2201.08238v1 [nucl-th] (2022)

- Data favour with shallow interaction
- Best compatibility with lowest scattering lengths
- Constraints on SU(3) symmetry breaking parameters

Summary and Outlook

Λ - Λ interaction:

- Compatible with LQCD
- Bound state not excluded \Rightarrow new limit

p - Ω^- interaction:

- Most precise measurement of the interaction
- Bound state not observed

Λ - Ξ^- interaction:

- First observation of a shallow Λ - Ξ^- interaction and comparison to LQCD
- New paper public on arXiv
- Greater improvements expected in upcoming Run 3 and 4 of the LHC

Backup

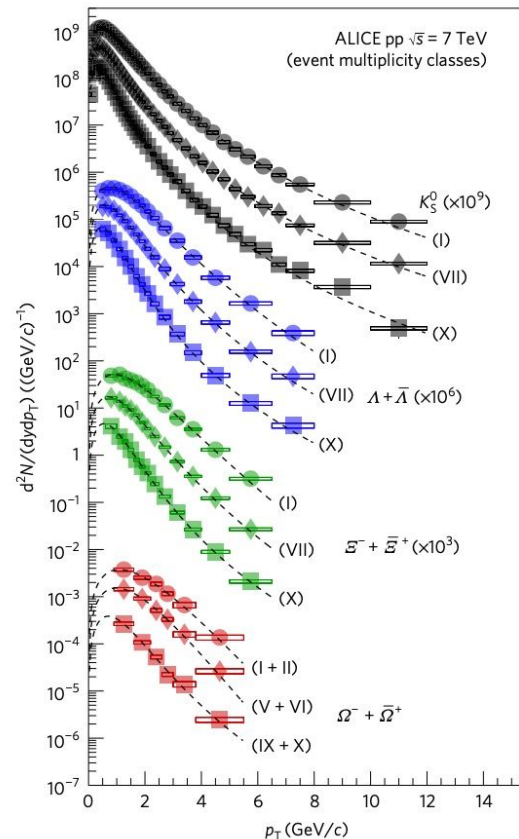


High multiplicity pp collisions

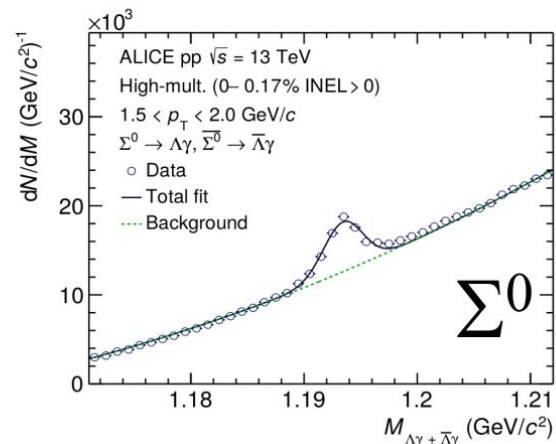
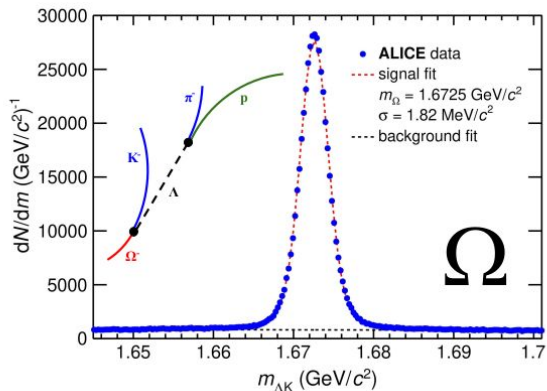
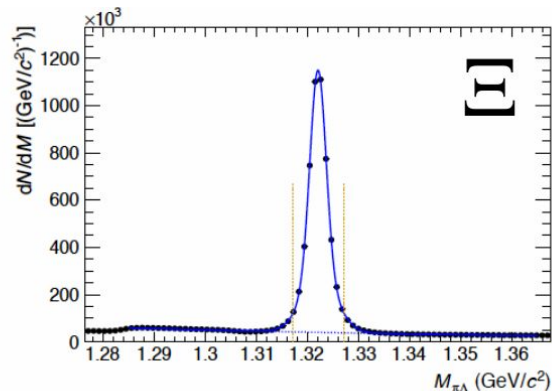
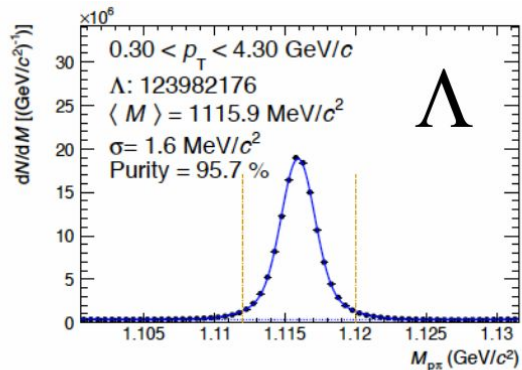
- pp collisions at ALICE are a perfect factory to produce a large amount of multi-strange hyperons
- enhanced strangeness containing particle yield detected in pp collisions at 13 TeV:

ALICE Coll. Nature Phys. 13 (2017) 535-539

- Excellent particle reconstruction and identification capabilities of the ALICE detector
 - In particular: Detection of Hyperons via their weak decay
 - high purities and resolutions archived



Hyperons at ALICE in pp Collisions

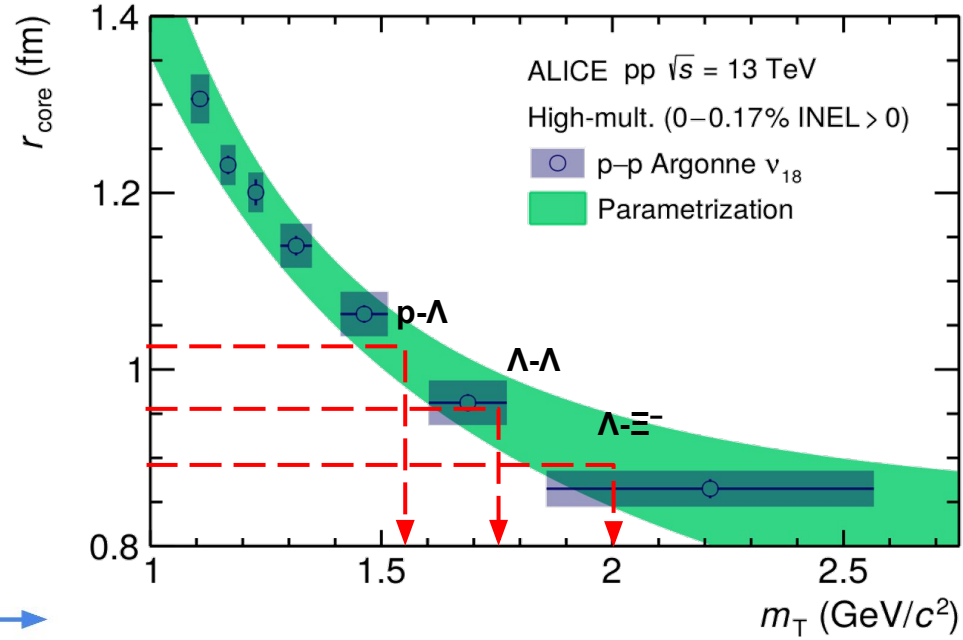
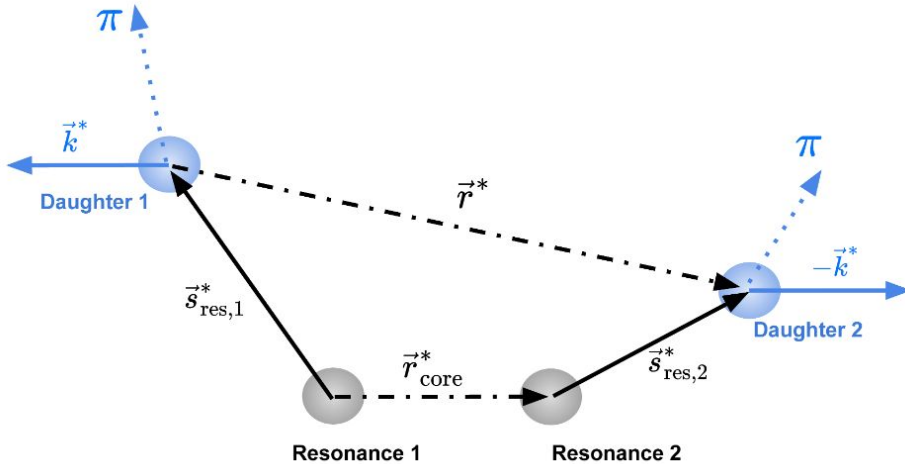


Source Function

ALICE Coll., Physics Letters B. 811 (2920) 135849

Consists of two parts:

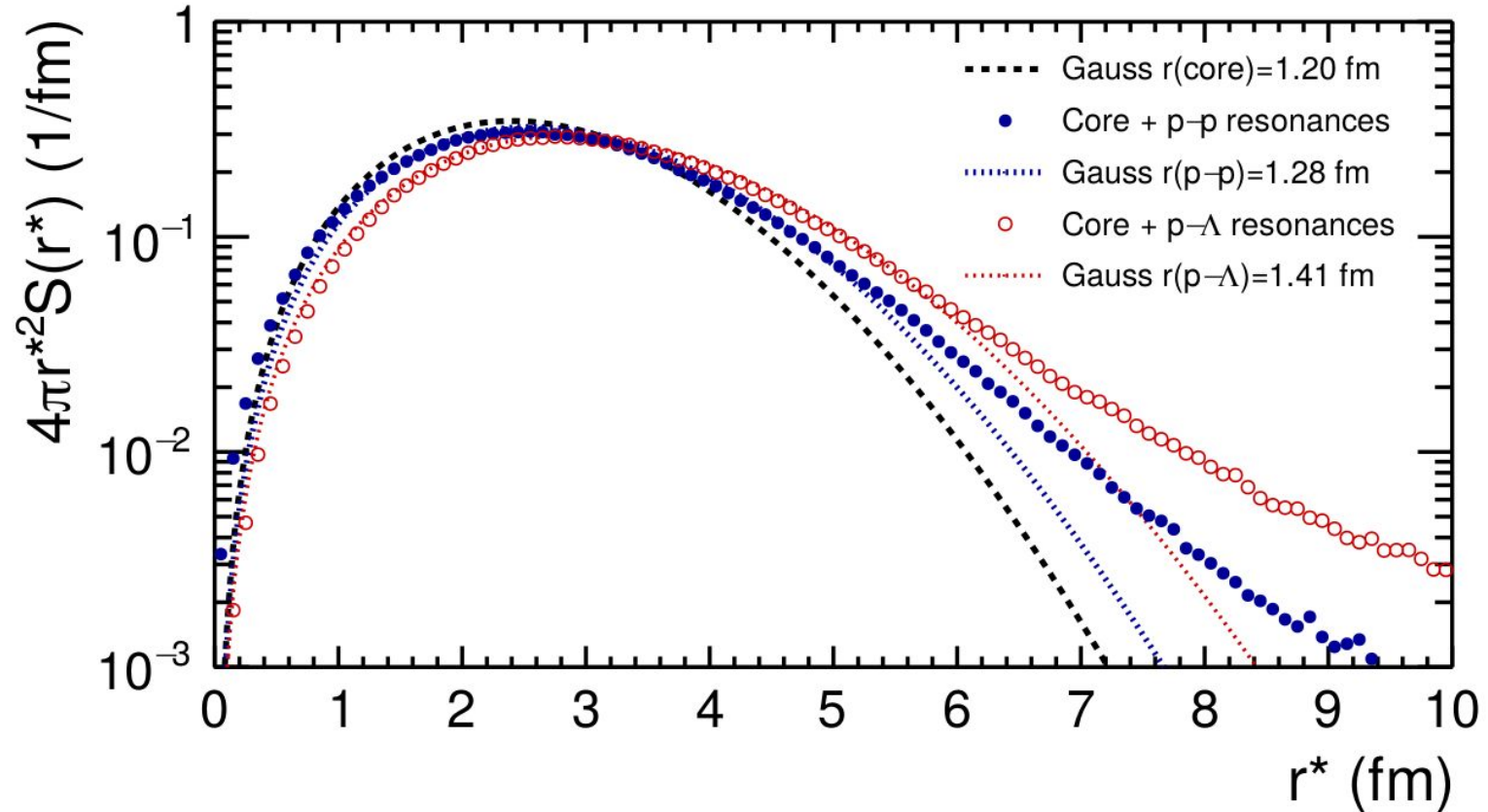
- Common m_T scaling of the core radius r_{Core}^*
- Extension to an effective source size r_{eff}^* by strongly decaying resonances (specific for each baryon pair)



$$m_T = \sqrt{k_T^2 + m^2}$$

Source Function: Common source

[ALICE Coll., Physics Letters B, 811 \(2020\) 135849](#)



The Lednický-Lyuboshits model

Analytical approach to model CF for strong final state interactions with the scattering amplitude f_0

$$C(k^*)_{\text{Lednický}} = 1 + \sum_S \rho_S \left[\frac{1}{2} \left| \frac{f(k^*)^S}{r_0} \right|^2 \left(1 - \frac{d_0^S}{2\sqrt{\pi}r_0} \right) + \frac{2\Re f(k^*)^S}{\sqrt{\pi}r_0} F_1(2k^*r_0) - \frac{\Im f(k^*)^S}{r_0} F_2(2k^*r_0) \right]$$

d_0 : effective range

f_0 : scattering length

$$f(k^*) = \left(\frac{1}{f_0} + \frac{1}{2}d_0k^{*2} - ik^* \right)^{-1}$$

The Lednický-Lyuboshits model

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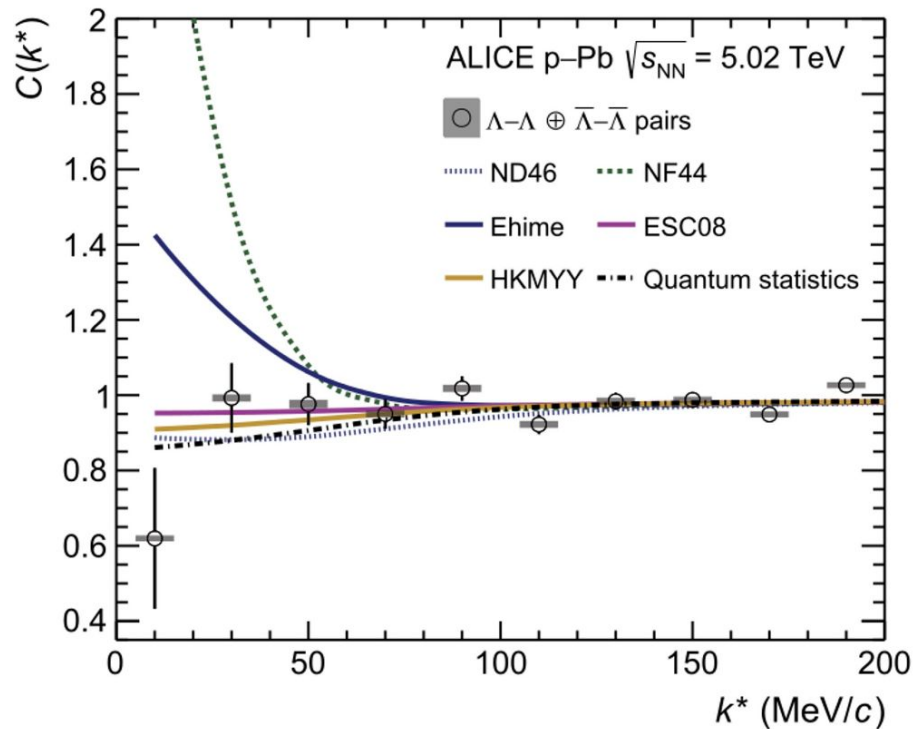
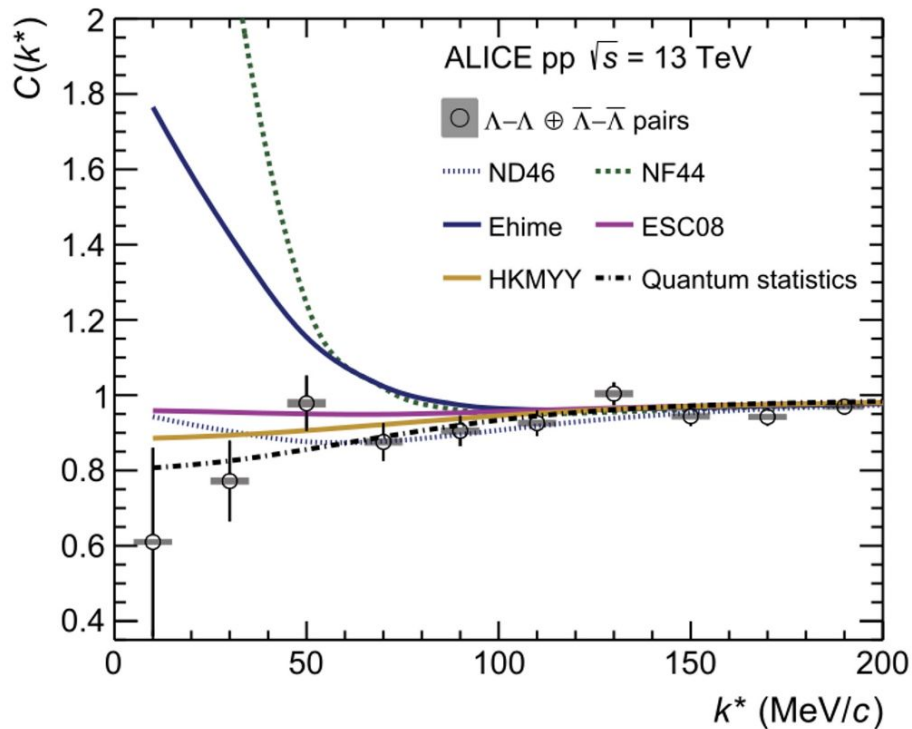
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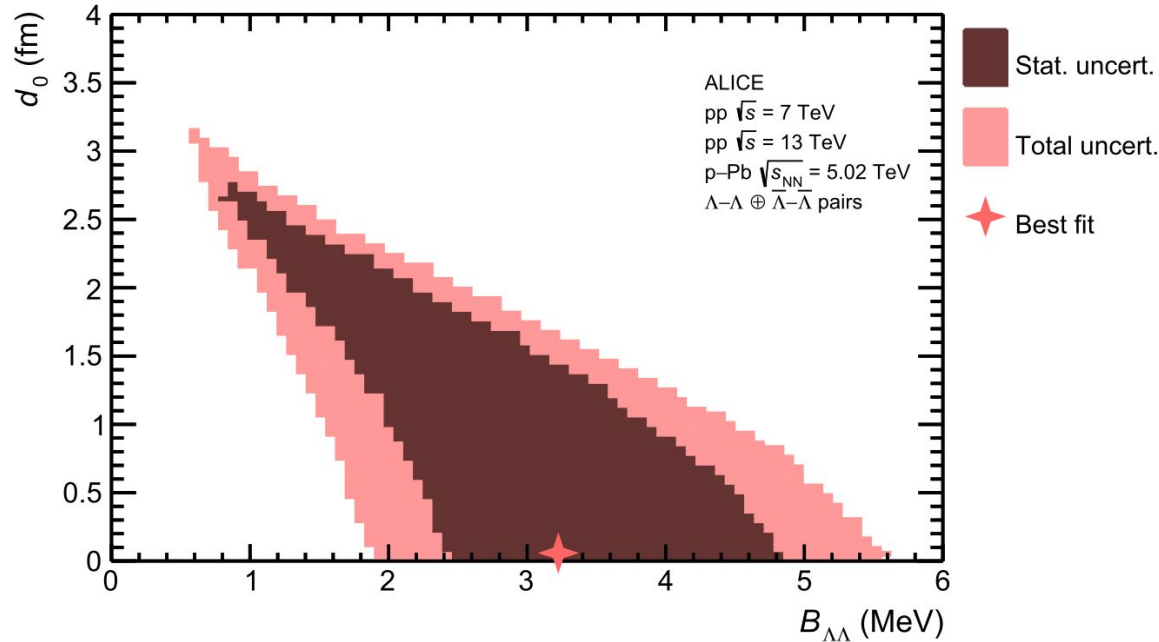
Λ - Λ Correlation function in different systems

[ALICE Coll., Physics Letters B, 811 \(2920\) 135849](#)



Λ - Λ Limits for the binding energy from femtoscopy

[ALICE Coll., Physics Letters B, 811 \(2020\) 135849](#)

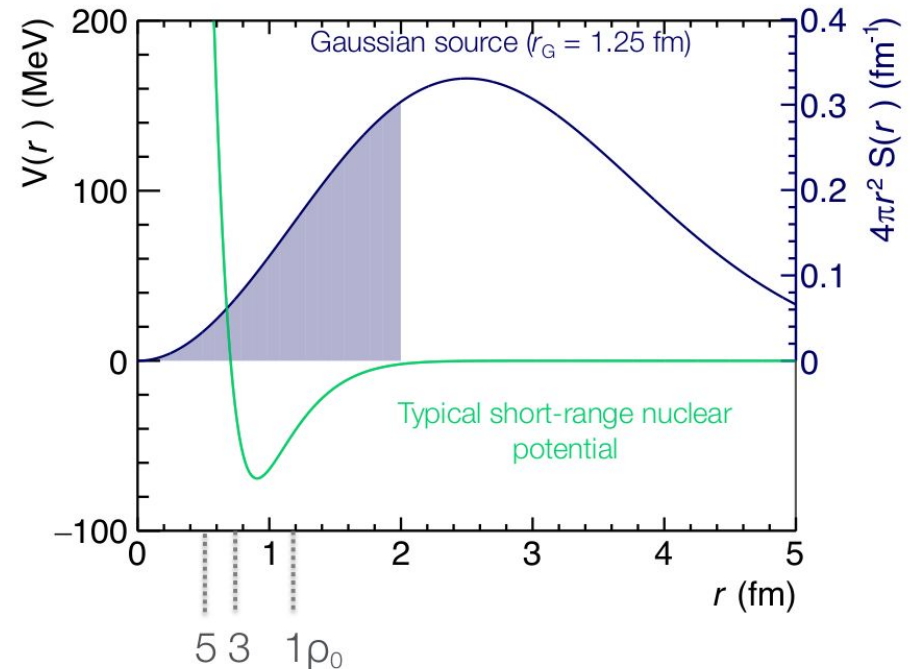
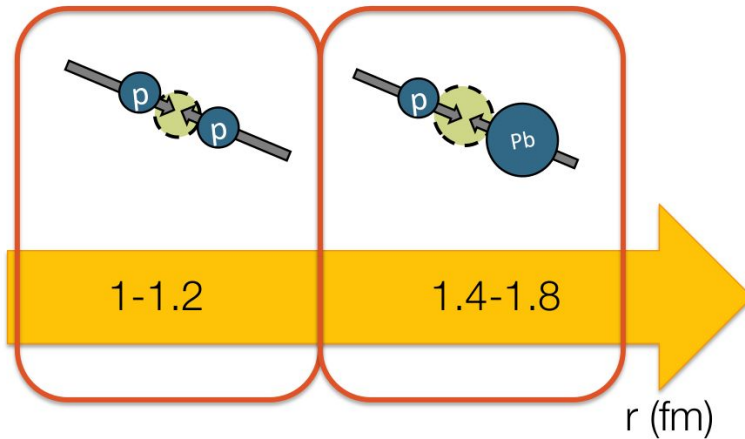


$$B_{\Lambda\Lambda} = 3.2^{+1.6}_{-2.4} \text{ (stat)}^{+1.8}_{-1.0} \text{ (syst)} \text{ MeV}$$

Femtoscscopy in small colliding systems

V. M. S., L. Fabbietti and O. Vazquez-Doce nucl-ex 2012.09806

- small collision systems necessary to study the short ranged strong interaction
- short interparticle distances → mimic large densities

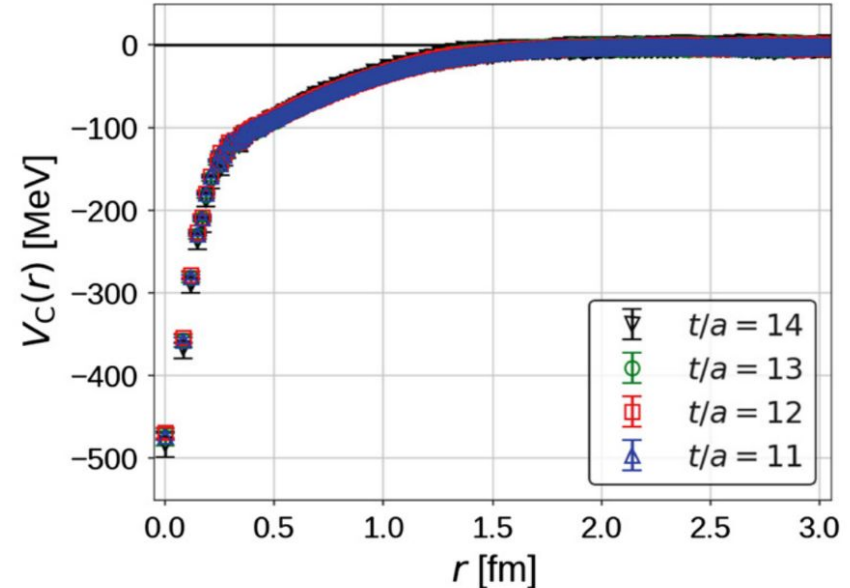
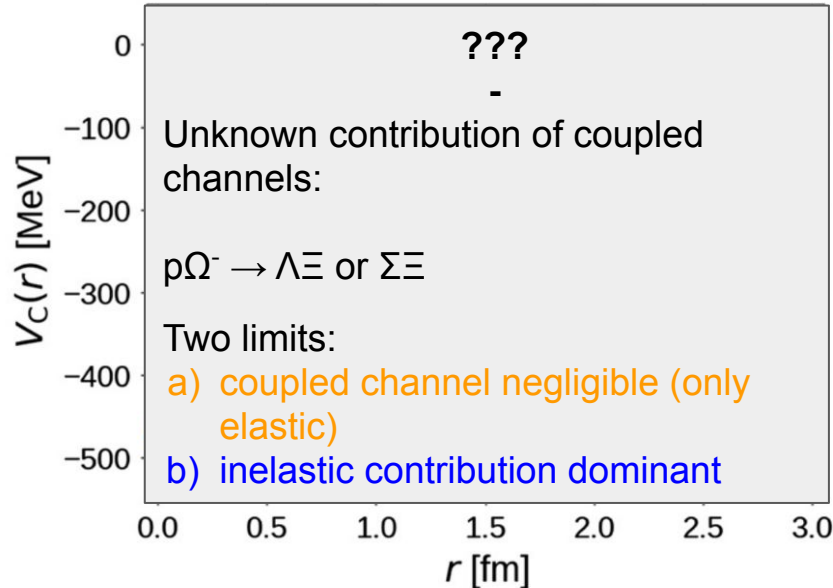


p- Ω^- : Detailed look at the interaction

- Proton ($J_p = 1/2$) + Omega ($J_\Omega = 3/2$)
- angular momentum negligible

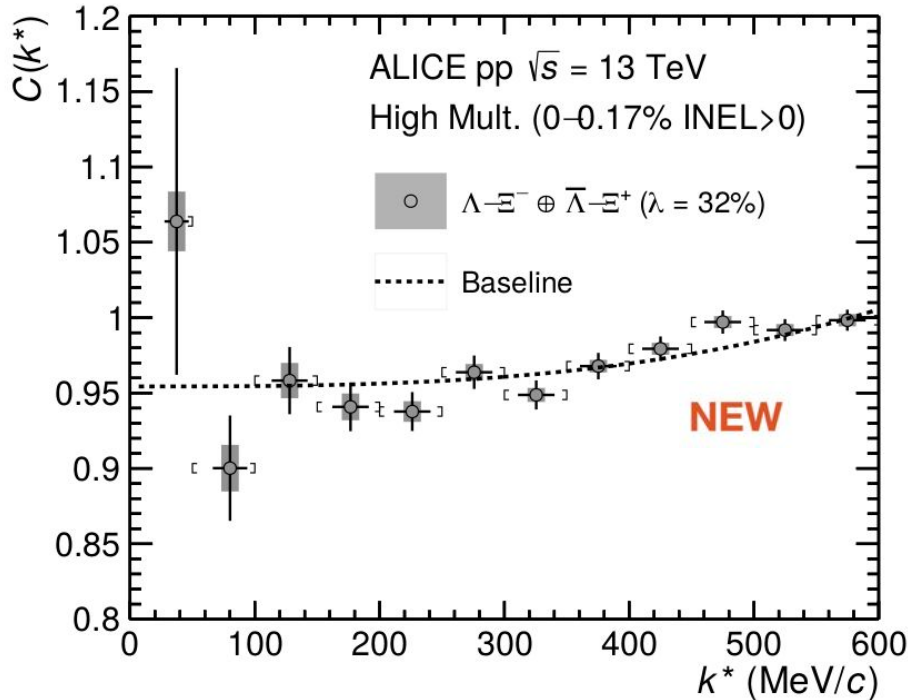
$N\Omega(^3S_2)$ – inelastic

$N\Omega(^5S_2)$ – elastic



$|S| = 3$: Λ - Ξ^- interaction – with femtoscopy

Baseline (no interaction):



ALICE Coll. arXiv:2204.10258, submitted to PLB

Λ - Ξ^- pairs:

$1.3 \cdot 10^6$ ($6.1 \cdot 10^3$ for $k^* < 200$ MeV/c)

Baseline (dotted line):

- constrained at large $k^* \in [200, 800]$ MeV/c
- Compatibility with the data @ $k^* < 200$ MeV/c:

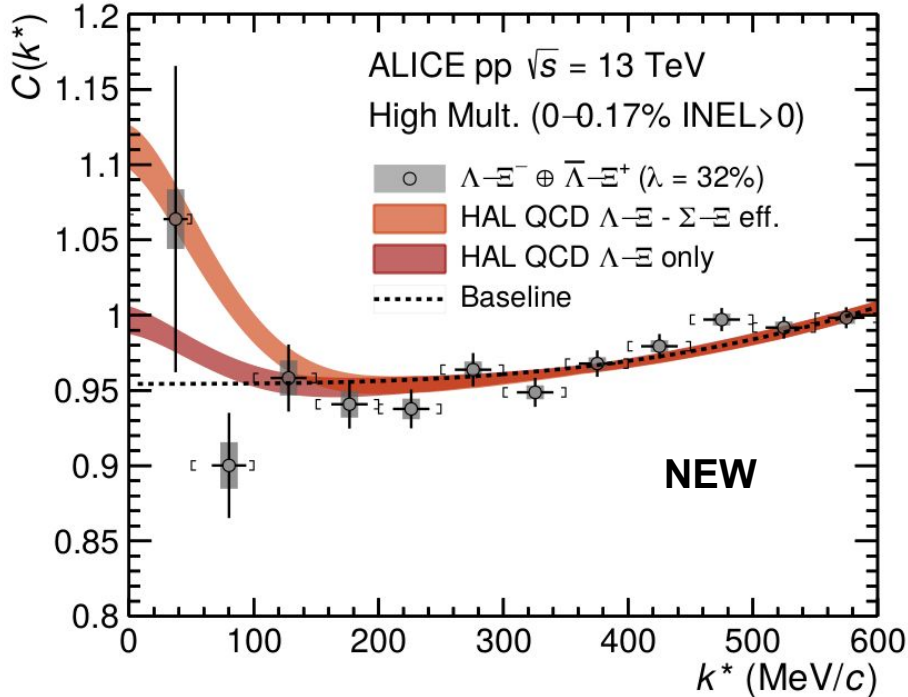
$0.78 n\sigma$

⇒ No significant deviation of the data from the baseline

⇒ indication of shallow Λ Ξ interaction

$|S| = 3: \Lambda-\Xi^-$ interaction – with femtoscopy

Comparison with Lattice QCD:



Compatibility with theory

potential

$\Lambda\Xi - \Sigma\Xi$ effective

$\Lambda\Xi - \Lambda\Xi$ only

$n\sigma$ band

1.43 – 2.34

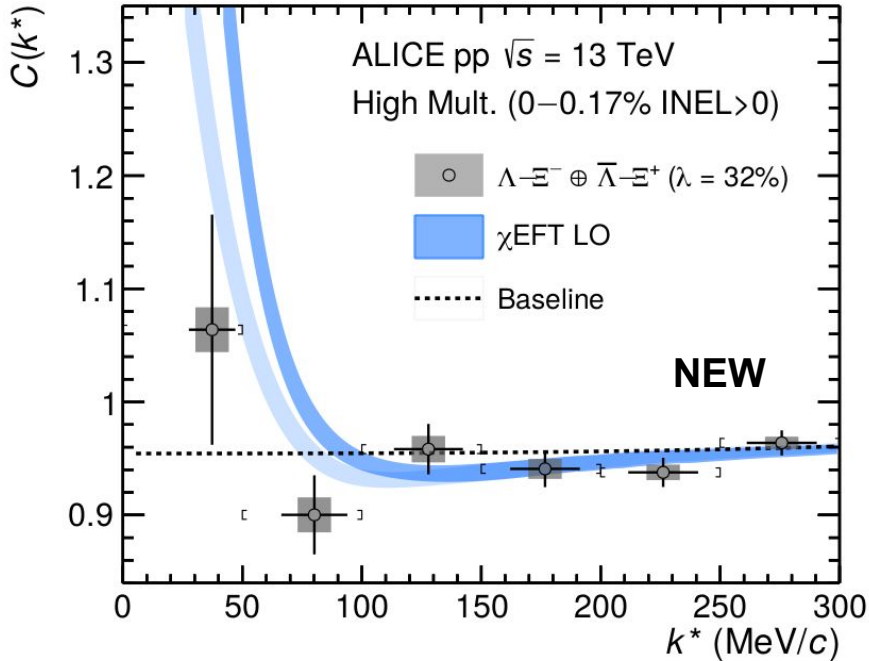
0.64 – 1.04

Conclusions

- Noticeable $\Lambda\Xi - \Sigma\Xi$ coupling in HAL QCD potential
- no experimental sensitivity on the coupling

$|S| = 3: \Lambda-\Xi^-$ interaction – with femtoscopy

Comparison with χ EFT: LO



ALICE Coll. arXiv:2204.10258, submitted to PLB

Scattering parameters and compatibility

potential (cut-off)	singlet		triplet		$n\sigma$
	f_0	d_0	f_0	d_0	
LO (500)	33.5	1.00	-0.33	-0.36	3.06 – 5.12
LO (700)	-9.07	0.87	-0.31	-0.27	0.78 – 1.60

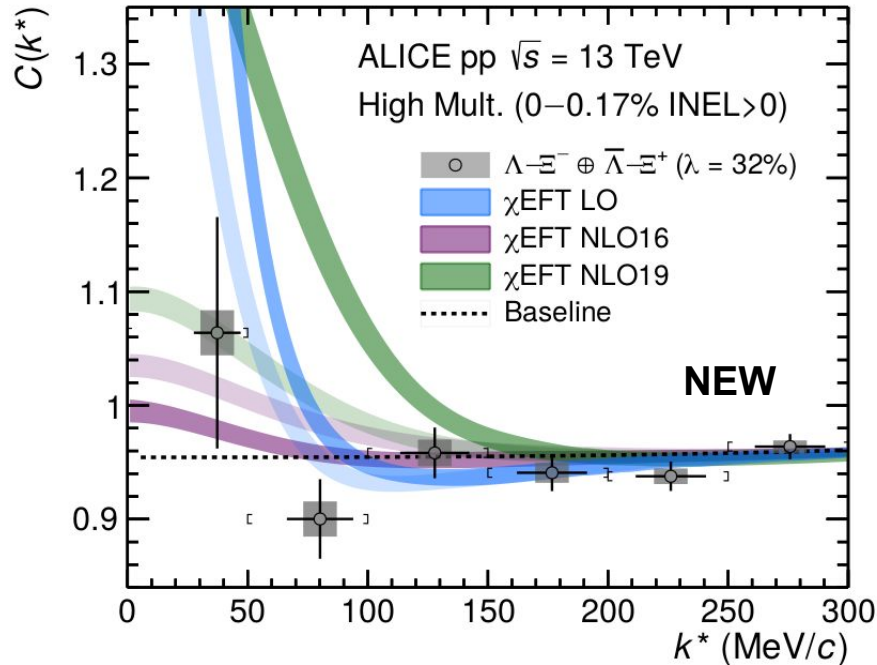
Conclusions:

- strong attraction in the singlet channel
- mild repulsion in the triplet channel
- for LO (700): bound state with 0.43 MeV
- \Rightarrow strong attraction of LO (500) excluded
- \Rightarrow better compatibility with smaller scattering length

* J. Haidenbauer, U.-G. Meißner, Phys. Lett. B, 684 (2010)

$|S| = 3: \Lambda-\Xi^-$ interaction – with femtoscopy

Comparison with χ EFT: NLO^(*)



ALICE Coll. arXiv:2204.10258, submitted to PLB

Scattering parameters and compatibility

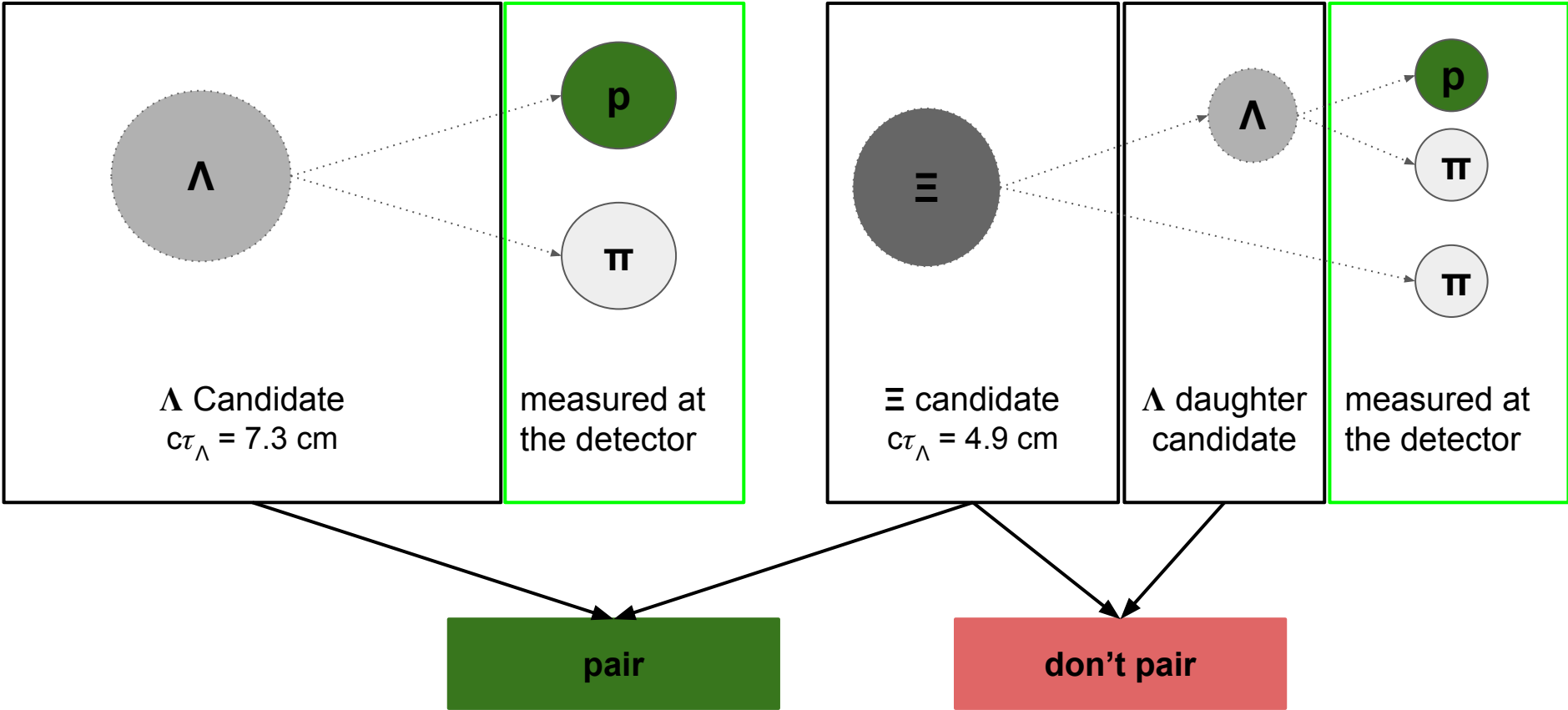
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Conclusions:

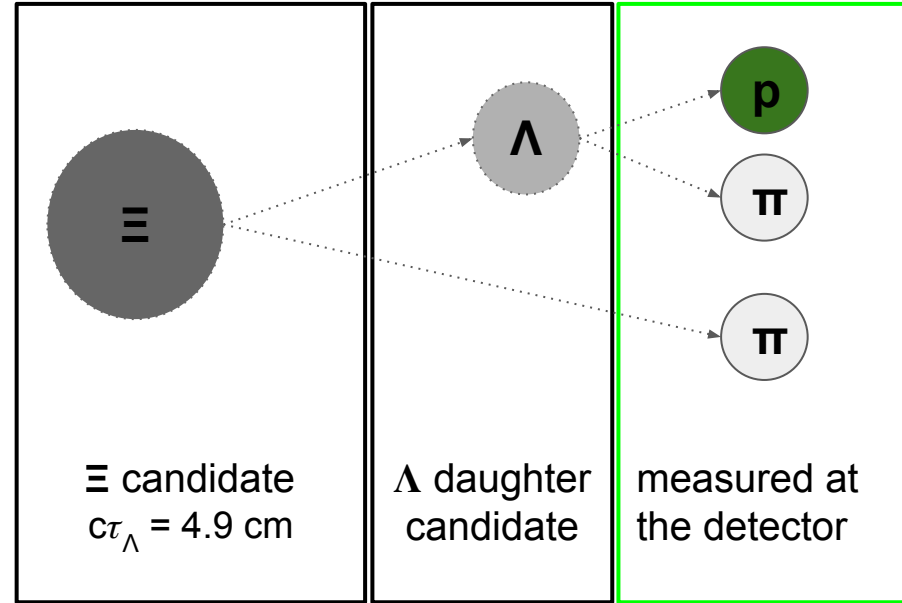
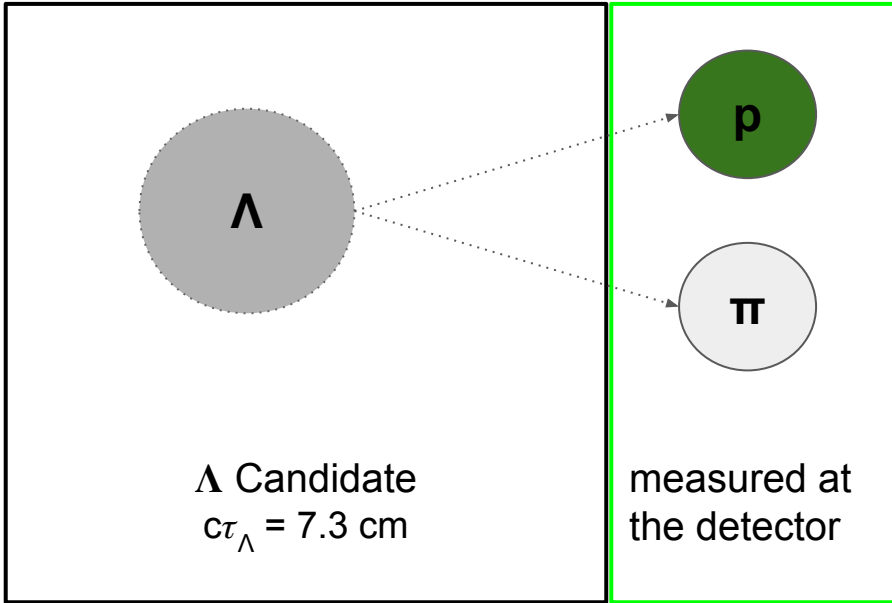
- no bound state in NLO potentials
 - best compatibility with lowest scattering lengths
- \Rightarrow important constraints for free SU(3) breaking parameters in the potentials by ALICE

^{*} J. Haidenbauer, U.-G. Meißner, arXiv:2201.08238v1 [nucl-th] (2022)

Data analysis Λ - Ξ



Data analysis Λ - Ξ^-



Λ - Ξ^- pairs:

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Modelling the correlation function

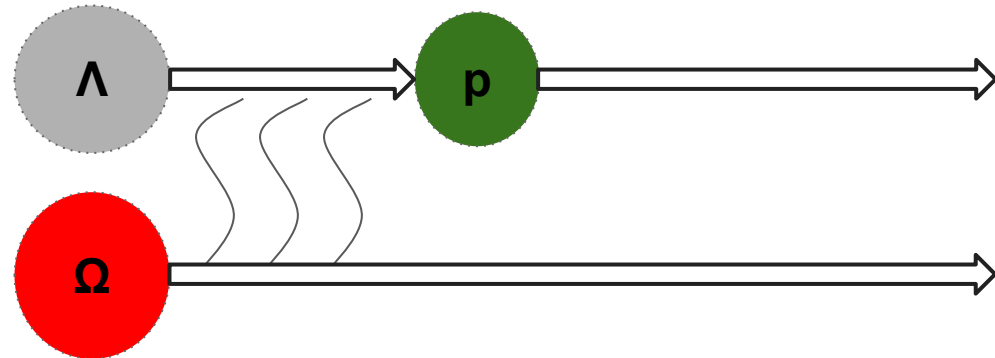
$$C_{\text{exp}}(k^*) = C_{\text{non-femto}}(k^*) \cdot C_{\text{femto}}(k^*)$$

$C_{\text{non-femto}}(k^*)$ Baseline from non-femto effects such as energy conservation

$C_{\text{femto}}(k^*)$ Final state interactions, depending on the analysed baryon pairs

$$C_{\text{femto}}(k^*) = \lambda_{\text{gen}} \cdot C_{\text{gen}}(k^*) + \lambda_{\text{bkg}} \cdot C_{\text{bkg}}(k^*) + \lambda_{\text{feed}} \cdot C_{\text{feed}}(k^*)$$

Example for feeddown correlation:



Experimental Λ - Ξ^- correlation function

Femto $C(k^*)$:

$C_{\text{gen}}(k^*)$	33%:	Lednický model
$C_{\text{bkg}}(k^*)$	11%:	2nd degree polynomial
$C_{\text{feed}}(k^*)$	56%:	Flat

$C_{\text{non-femto}}(k^*)$:

- a) $A(1 + p k^{*2})$
- b) $A(1 + p k^{*3})$

Source Function:

$\langle m_T \rangle = 2.0 \text{ GeV}/c$
 $r_{\text{core}} = 0.89 \pm 0.05 \text{ fm}$
 $r_{\text{eff}} = \mathbf{1.03 \pm 0.05 \text{ fm}}$

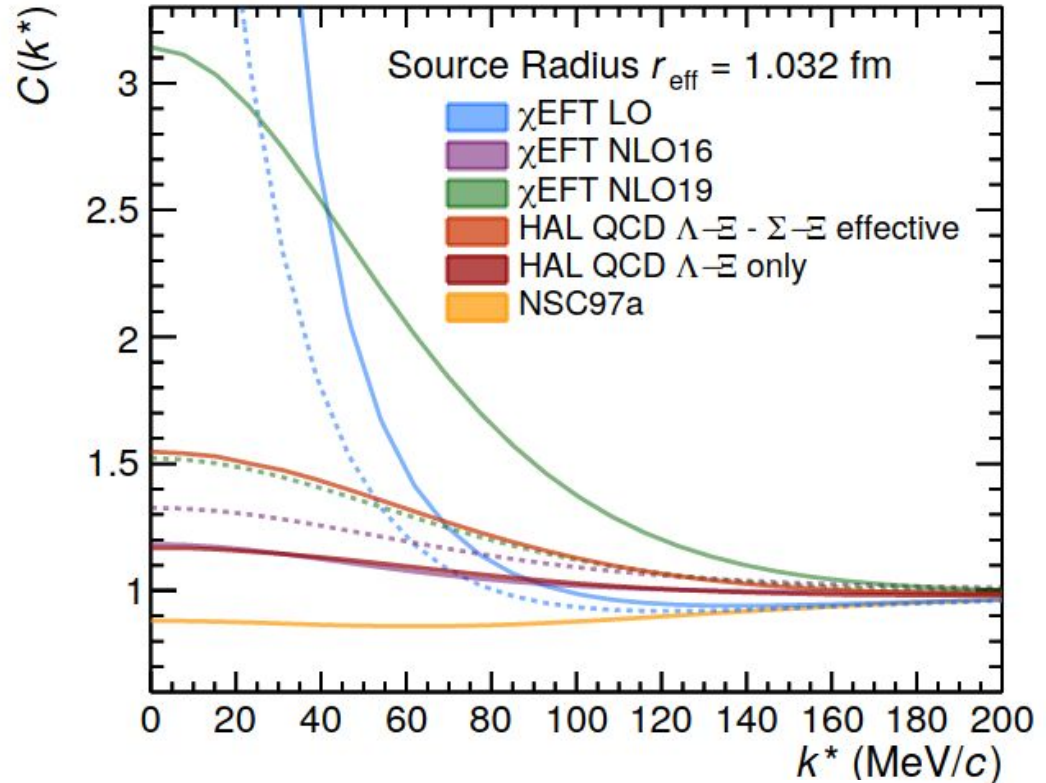
Correct the genuine theoretical calculated $C(k^*)$ for the additional contributions:

$$C_{\text{femto}}(k^*) = \lambda_{\text{gen}} \cdot C_{\text{gen}}(k^*) + \lambda_{\text{bkg}} \cdot C_{\text{bkg}}(k^*) + \lambda_{\text{feed}} \cdot C_{\text{feed}}(k^*)$$

$$C_{\text{exp}}(k^*) = C_{\text{non-femto}}(k^*) \cdot C_{\text{femto}}(k^*)$$

Genuine $\Lambda\Xi^-$ interaction

- Theoretical correlation functions from the discussed potentials
- dotted lines correspond to the larger cut-off version in χ EFT potentials



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