

# Analysis of coupled-channel potentials with quark and hadron degrees of freedom

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As a recent topic of heavy flavor systems, exotic charmonia called  $X$ ,  $Y$ ,  $Z$  have been observed experimentally above the meson-meson threshold. Masses of  $X$ ,  $Y$ ,  $Z$ , however, are not reproduced by the Cornell potential only with the degrees of freedom of  $\bar{c}c$ . This indicates that the  $X$ ,  $Y$ ,  $Z$  states have coupled channel effects of  $\bar{c}c$  and meson-meson states strongly.

Because of the color confinement of quarks, the  $\bar{c}c$  potentials diverge at large distance. On the other hand, the meson-meson potentials vanish at large distance, because the interaction range is limited by the inverse pion mass. What then is the effect of the coupling to the two-hadron channels in the  $\bar{c}c$  potentials and vice versa? It is expected that the coupling to the meson-meson channel affect  $\bar{c}c$  potentials and the coupling of mesons with  $\bar{c}c$  affect meson-meson potentials.

In this talk, we consider the channel couplings between the  $\bar{c}c$  and meson-meson potentials, and investigate the properties of the effective potentials which are obtained by eliminating one of the channels.[1]

We show that these effective potentials  $V_{\text{eff}}(E)$  at energy  $E$  are written as follows

$$\langle \boldsymbol{D} | V_{\text{eff}}^{\bar{D}D}(E) | \boldsymbol{D} \rangle = V^{\bar{D}D}(\boldsymbol{D}) + \sum_n \frac{\langle \boldsymbol{D} | V^t | \phi_n \rangle \langle \phi_n | V^t | \boldsymbol{D} \rangle}{E - E_n},$$

$$\langle \boldsymbol{c} | V_{\text{eff}}^{\bar{c}c}(E) | \boldsymbol{c} \rangle = V^{\bar{c}c}(\boldsymbol{c}) + \int d \boldsymbol{p} \frac{\langle \boldsymbol{c} | V^t | \boldsymbol{p} \rangle \langle \boldsymbol{p} | V^t | \boldsymbol{c} \rangle}{E - E_{\boldsymbol{p}} + i0^+},$$

where

$\boldsymbol{D}$  and

$\boldsymbol{D}$  and  $\boldsymbol{D}'$  are coordinates before and after interactions,  $V$  is potentials of internal interactions,  $V^t$  is the transition potential of channel couplings,  $|\phi_n\rangle$  is the eigenstate of the  $\bar{c}c$  Hamiltonian with energy  $E_n$ , and  $|\boldsymbol{p}\rangle$  is the meson-meson eigenstate with energy  $E_{\boldsymbol{p}}$ .

We discuss that the coupling to the eliminated channel induces the non-local and energy dependent effective potential, irrespective of the behavior of the transition potential. In addition, when the hadron channel having continuous scattering eigenstates is eliminated, the resulting  $\bar{c}c$  potential contains an imaginary part. The physical property which stems from imaginary part, however, may be lost by the finite terms of the derivative expansion.

[1] H. Feshbach, Ann. Phys. 5, 357 (1958); *ibid.*, 19, 287 (1962).

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