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Hyperonic equation of state for neutron stars at finite temperature



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Hristijan Kochankovski
Àngels Ramos
Laura Tolos

HYP2022
Prague, Czech Republic

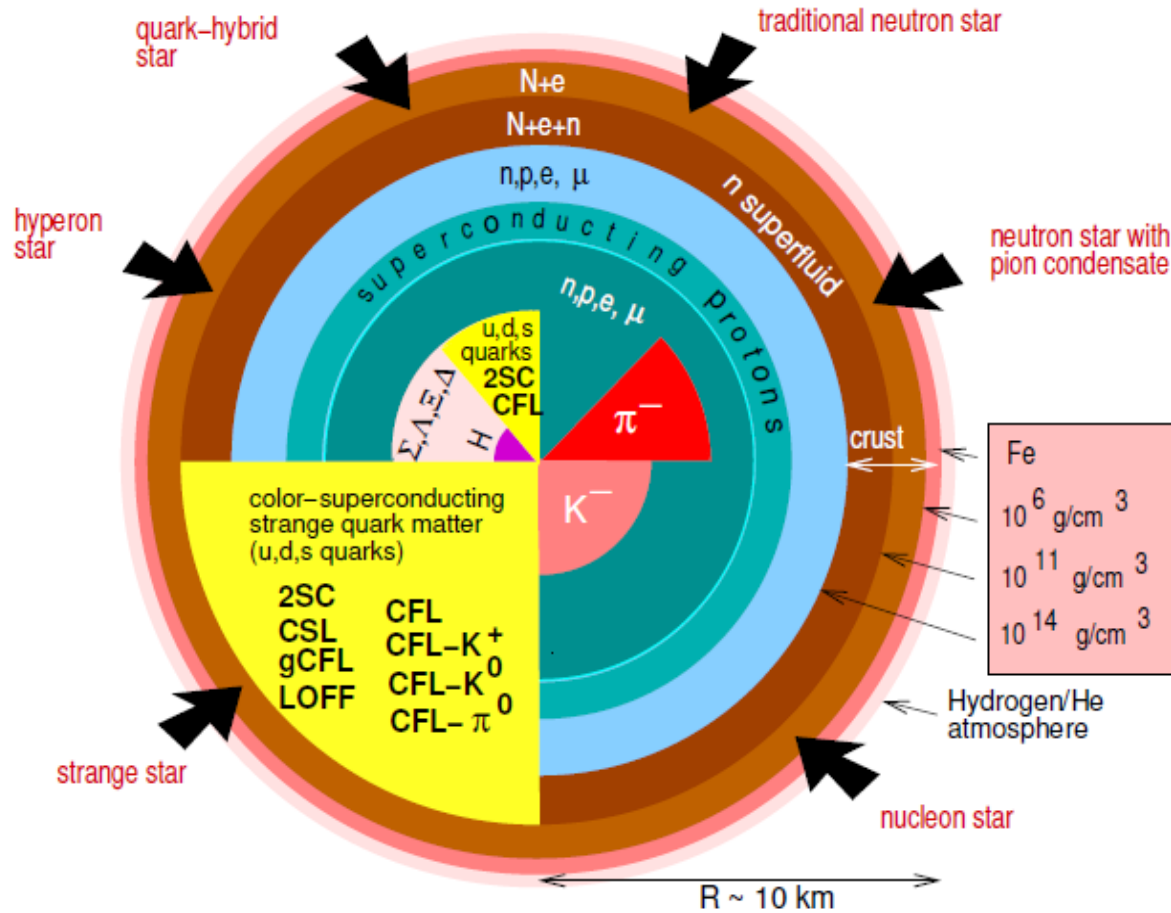
30.06.2022

Outline

- Why we need a finite temperature hyperonic Equation of State (EoS)?
- Brief introduction to the FSU2H* model.
- Equation of State (EoS) and composition of hyperonic matter at a constant charge fraction.
- A simple application: $M(R)$ curves for neutron stars at finite temperature.
- Summary

Why we need a finite temperature hyperonic Equation of State (EOS)? (I)

F. Weber, Prog.Part.Nucl.Phys.54:193-288,2005



- Hyperons are one type of exotic particles that can appear in the inner core of the neutron star.
- Hyperonic models are still not very well constrained (large parameter space due to uncertainties in the effective interactions at high densities).
- The finite temperature EoS is a necessary tool to understand the phenomena of core collapse supernovae and neutron star binary mergers.

Why we need a finite temperature hyperonic Equation of State (EOS)? (II)

- The pressure and the energy density at a fixed point in the star, at finite temperature can be decomposed as:

$$P(T) = P_0 + P_{ther}(T)$$

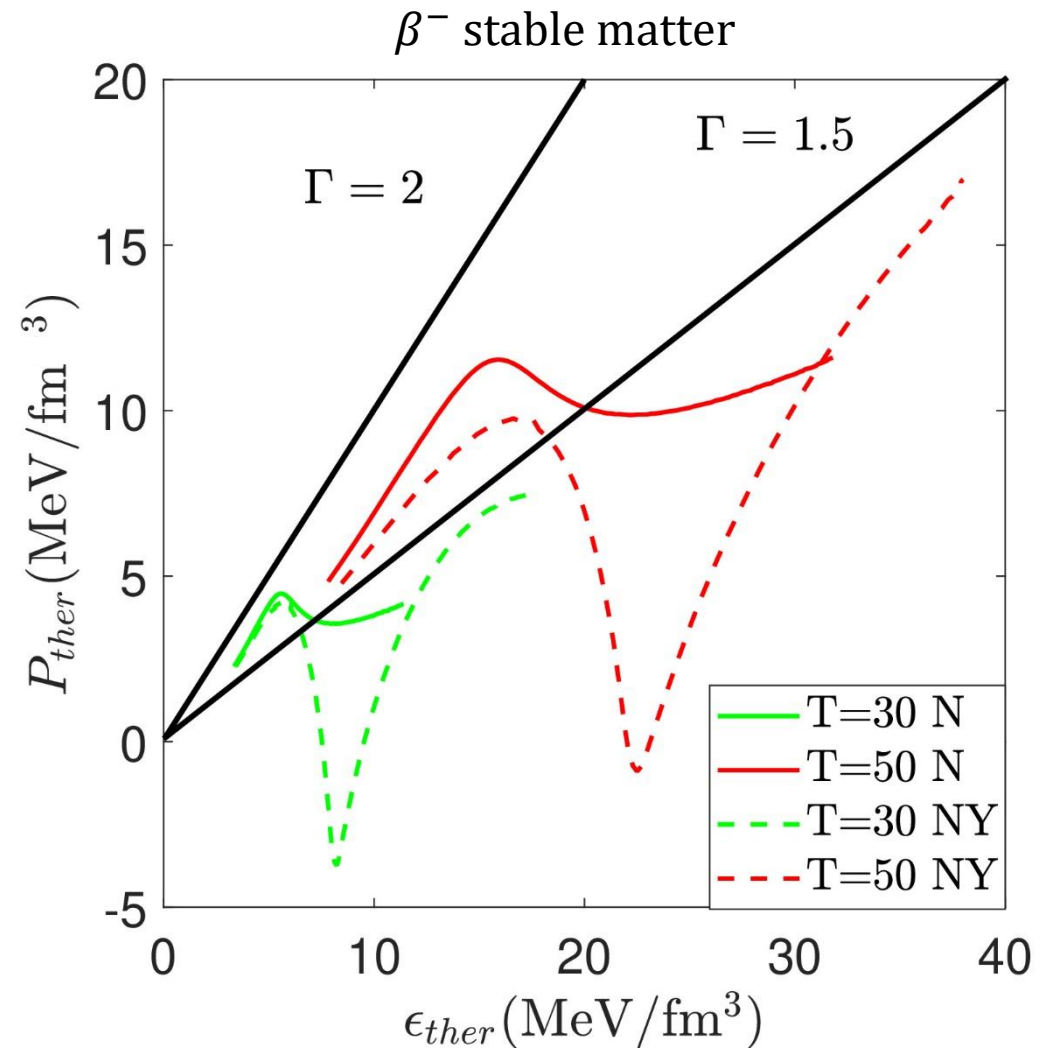
$$\epsilon(T) = \epsilon_0 + \epsilon_{ther}(T)$$

- The relation between $P_{ther}(T)$ and $\epsilon_{ther}(T)$ can be written as:

$$P_{ther}(\epsilon_{ther}) = (\Gamma - 1)\epsilon_{ther}$$

- If one assumes that the thermal index Γ is constant, one can obtain finite temperature EoS just by knowing $T = 0$ EoS.
- However, this approach can be inaccurate, as we showed in:

arXiv:2206.11266



Brief introduction to FSU2H* model

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- Belongs to the broad group of relativistic – mean field approaches:

$$\begin{aligned}\mathcal{L} &= \sum_b \mathcal{L}_b + \mathcal{L}_m \\ \mathcal{L}_b &= \bar{\Psi}_b (i\gamma_\mu \partial^\mu - q_b \gamma_\mu A^\mu - m_b \\ &\quad + g_{\sigma b} \sigma + g_{\sigma^* b} \sigma^* - g_{\omega b} \gamma_\mu \omega^\mu - g_{\phi b} \gamma_\mu \phi^\mu - g_{\rho, b} \gamma_\mu \vec{I}_b \vec{\rho}^\mu) \Psi_b, \\ \mathcal{L}_m &= \frac{1}{2} \partial_\mu \sigma \partial^\mu \sigma - \frac{1}{2} m_\sigma^2 \sigma^2 - \frac{\kappa}{3!} (g_{\sigma b} \sigma)^3 - \frac{\lambda}{4!} (g_{\sigma b} \sigma)^4 \\ &\quad + \frac{1}{2} \partial_\mu \sigma^* \partial^\mu \sigma^* - \frac{1}{2} m_{\sigma^*}^2 \sigma^{*2} \\ &\quad - \frac{1}{4} \Omega^{\mu\nu} \Omega_{\mu\nu} + \frac{1}{2} m_\omega^2 \omega_\mu \omega^\mu + \frac{\zeta}{4!} g_{\omega b}^4 (\omega_\mu \omega^\mu)^2 \\ &\quad - \frac{1}{4} \vec{R}^{\mu\nu} \vec{R}_{\mu\nu} + \frac{1}{2} m_\rho^2 \vec{\rho}_\mu \vec{\rho}^\mu + \Lambda_\omega g_{\rho b}^2 \vec{\rho}_\mu \vec{\rho}^\mu g_{\omega b}^2 \omega_\mu \omega^\mu \\ &\quad - \frac{1}{4} F^{\mu\nu} F_{\mu\nu} + \frac{1}{2} m_\phi^2 \phi_\mu \phi^\mu - \frac{1}{4} F^{\mu\nu} F_{\mu\nu},\end{aligned}$$

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- Main characteristics of the cold EoS:

- Reproduces experimental results around ρ_0 .

ρ_0 (fm ⁻³)	E/A (MeV)	K (MeV)	m_N^*/m_N (ρ_0)	$E_{sym}(\rho_0)$ (MeV)	L (MeV)	K_{sym} (MeV)
0.1505	-16.28	238.0	0.593	30.5	44.5	86.4

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- Reproduces astrophysical constraints at high densities.

M_{\max} (M_\odot)	$R(M_{\max})$ (km)	$R(1.4M_\odot)$ (km)	$\Lambda(1.4M_\odot)$
2.03	12.02	13.08	526.3

Equation of State (EoS) and composition of an hyperonic matter at a constant charge fraction (I)

- Contrary to an already evolved neutron star, some processes require baryonic EoS at an arbitrary charge fraction:

$$Y_Q = \sum_Q \frac{\rho_Q}{\rho_B}$$

- Thus, the finite temperature baryonic EoS becomes a function of three parameters: temperature T , baryonic density ρ_B and charge fraction Y_Q .
- For a general use of the EoS, one needs a table of the composition and the thermodynamic properties of the matter at each grid point

Wide range of values to **account for conditions in proto-neutron stars (PNS) and NS mergers:**

$$T = (0 - 100) \text{ MeV}$$

$$\rho_B = (0.5 - 10)\rho_0$$

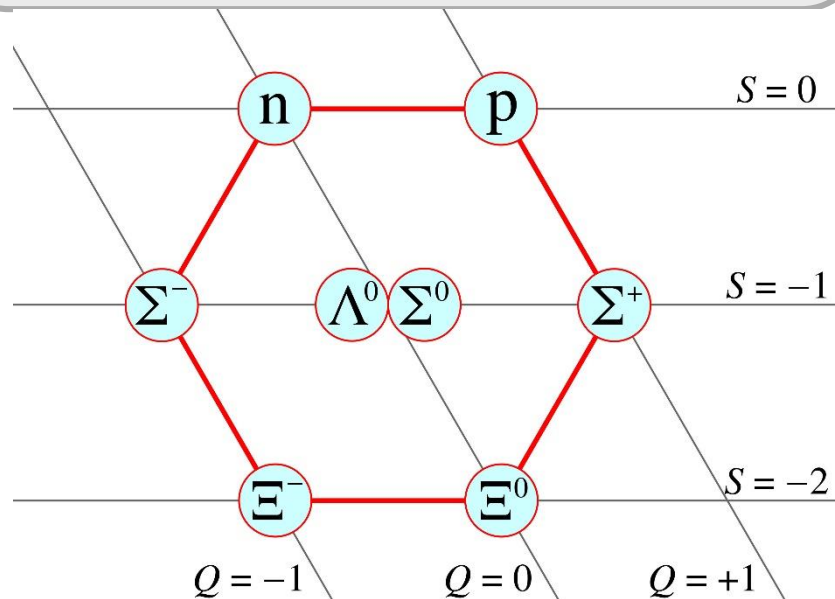
$$Y_Q = (0 - 0.6)$$

Equation of State (EoS) and composition of an hyperonic matter at a constant charge fraction (II)

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- Between different baryons a weak interaction equilibrium is assumed:

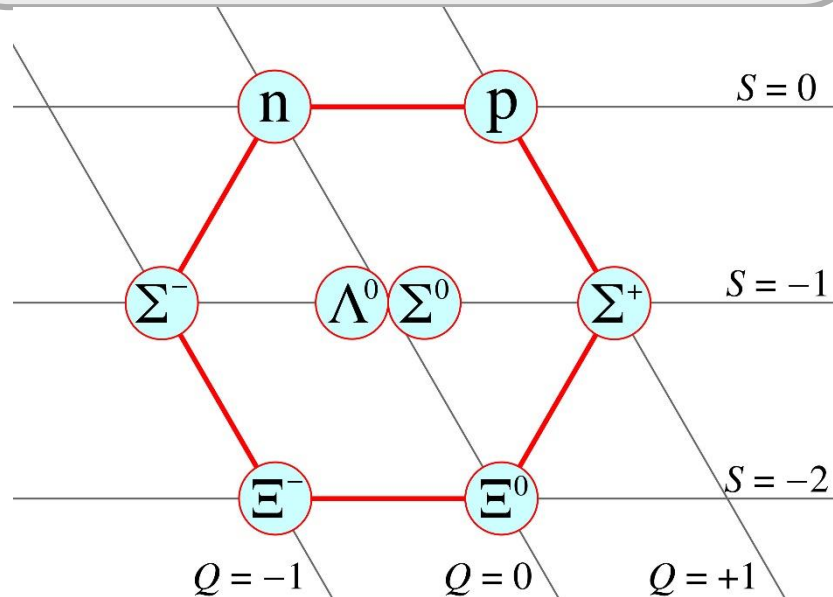
$$\begin{aligned}\mu_n &= \mu_\Lambda = \mu_{\Sigma^0} = \mu_{\Xi^0} \\ \mu_p &= \mu_{\Sigma^+} \\ \mu_{\Sigma^-} &= \mu_{\Xi^-} = 2\mu_n - \mu_p\end{aligned}$$



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- To inspect the properties of the EoS we show calculations for two temperatures:

$$T = 25 \text{ MeV and } T = 75 \text{ MeV}$$

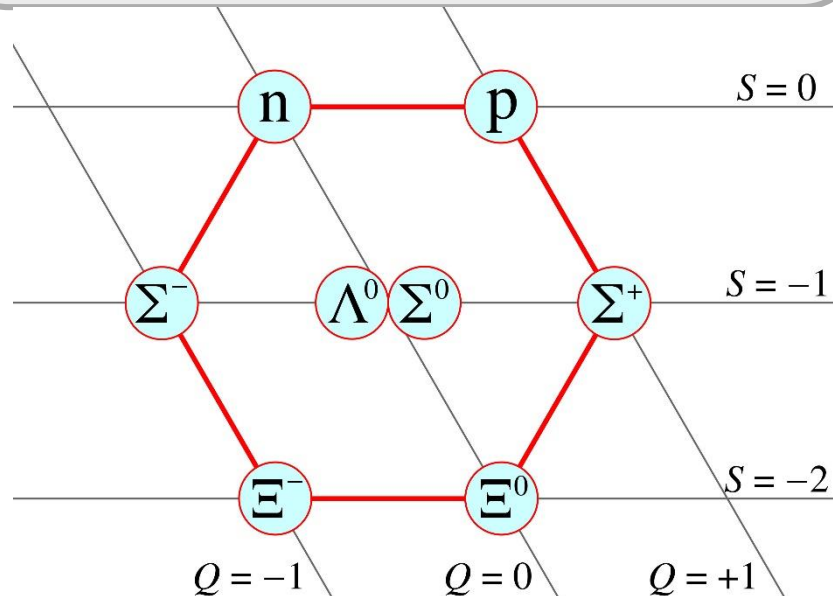
- and two different charge fractions:

$$Y_q = 0.01 \text{ and } Y_q = 0.5$$

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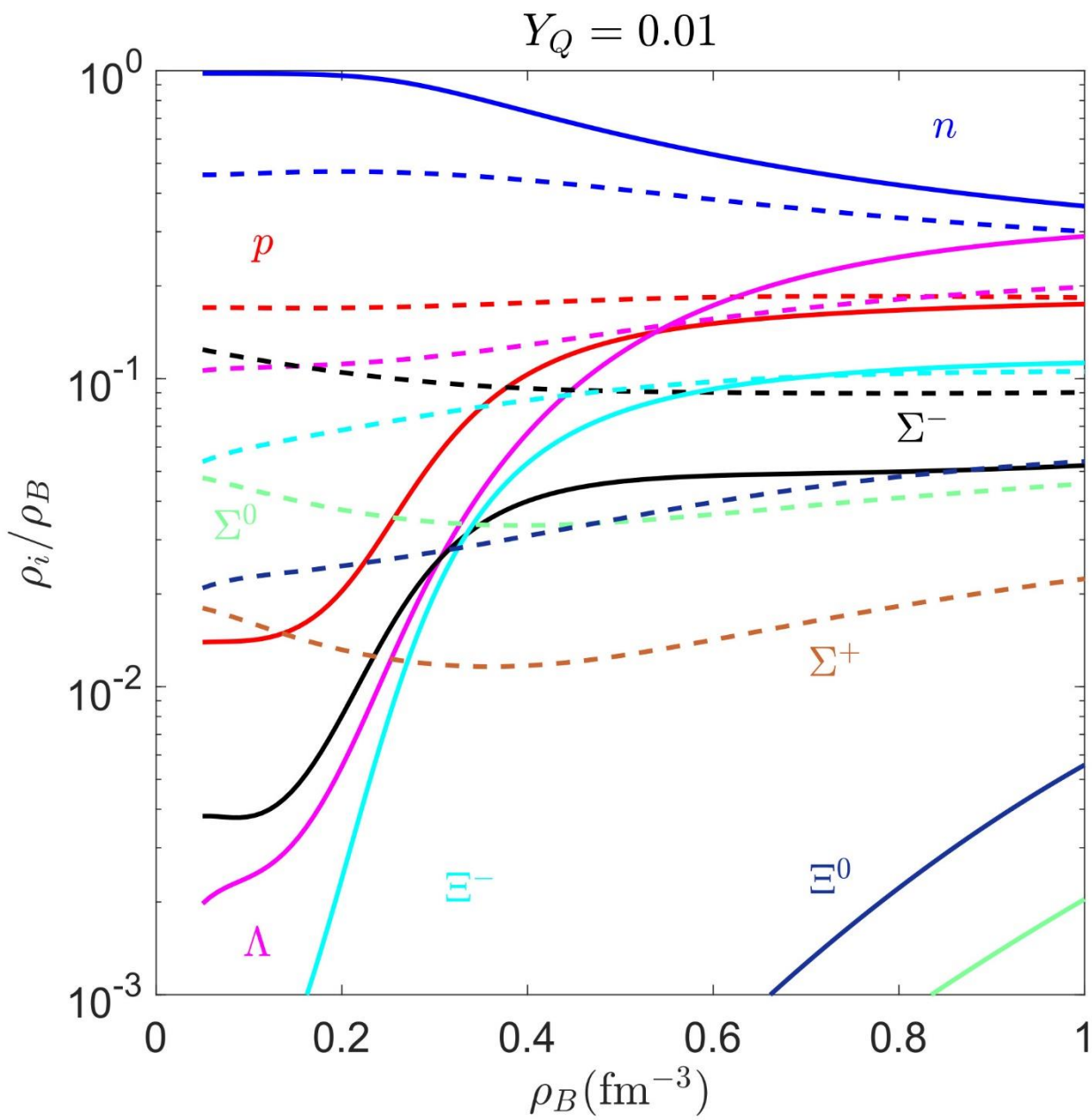
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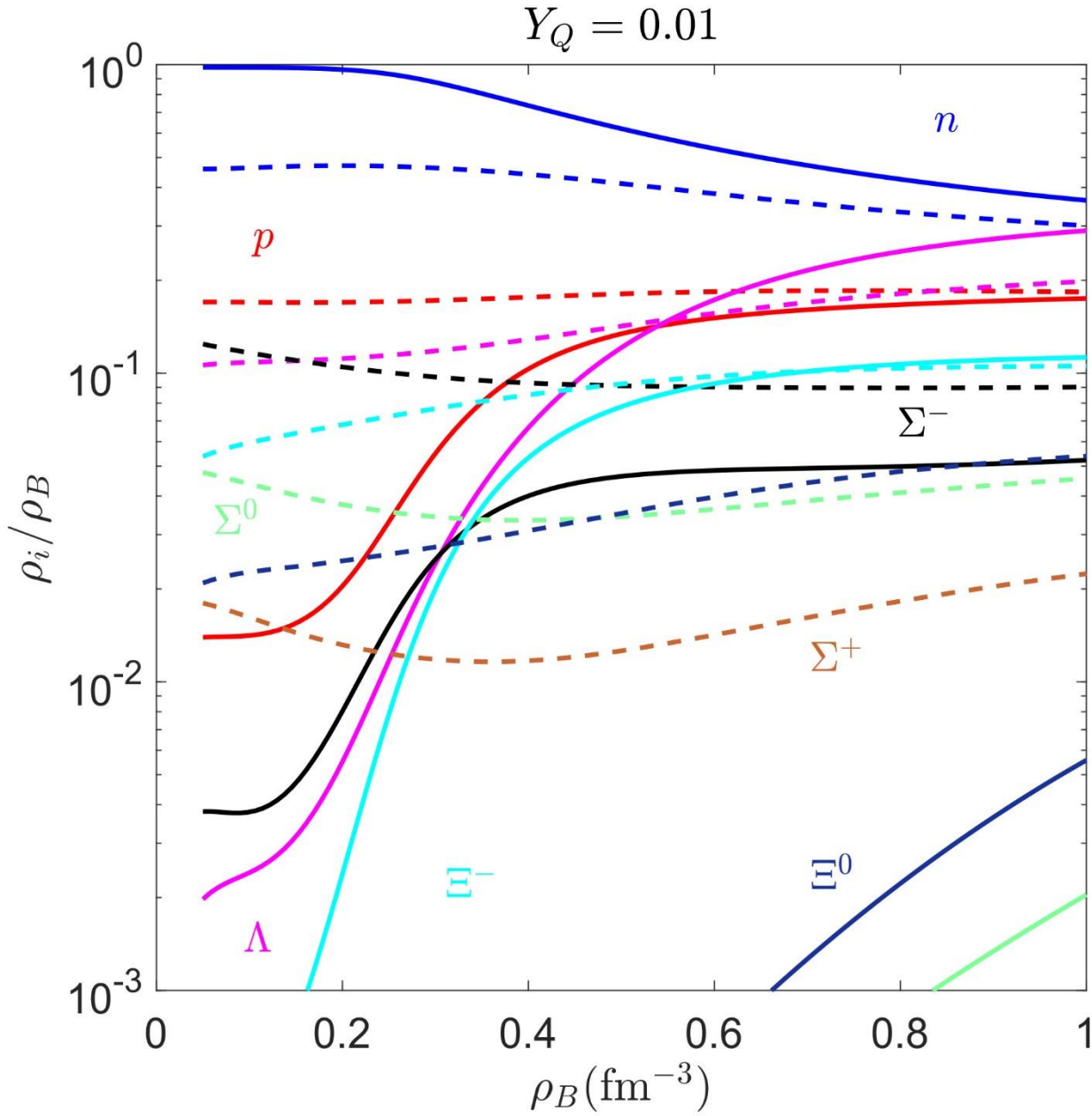
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In pure nucleonic matter, the first case would correspond to almost pure neutron matter, while the second one would correspond to symmetric nuclear matter.

Composition of hyperonic matter at fixed Y_Q (I)

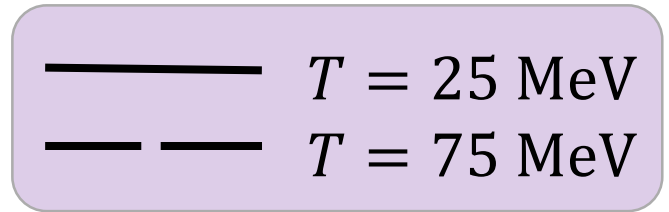
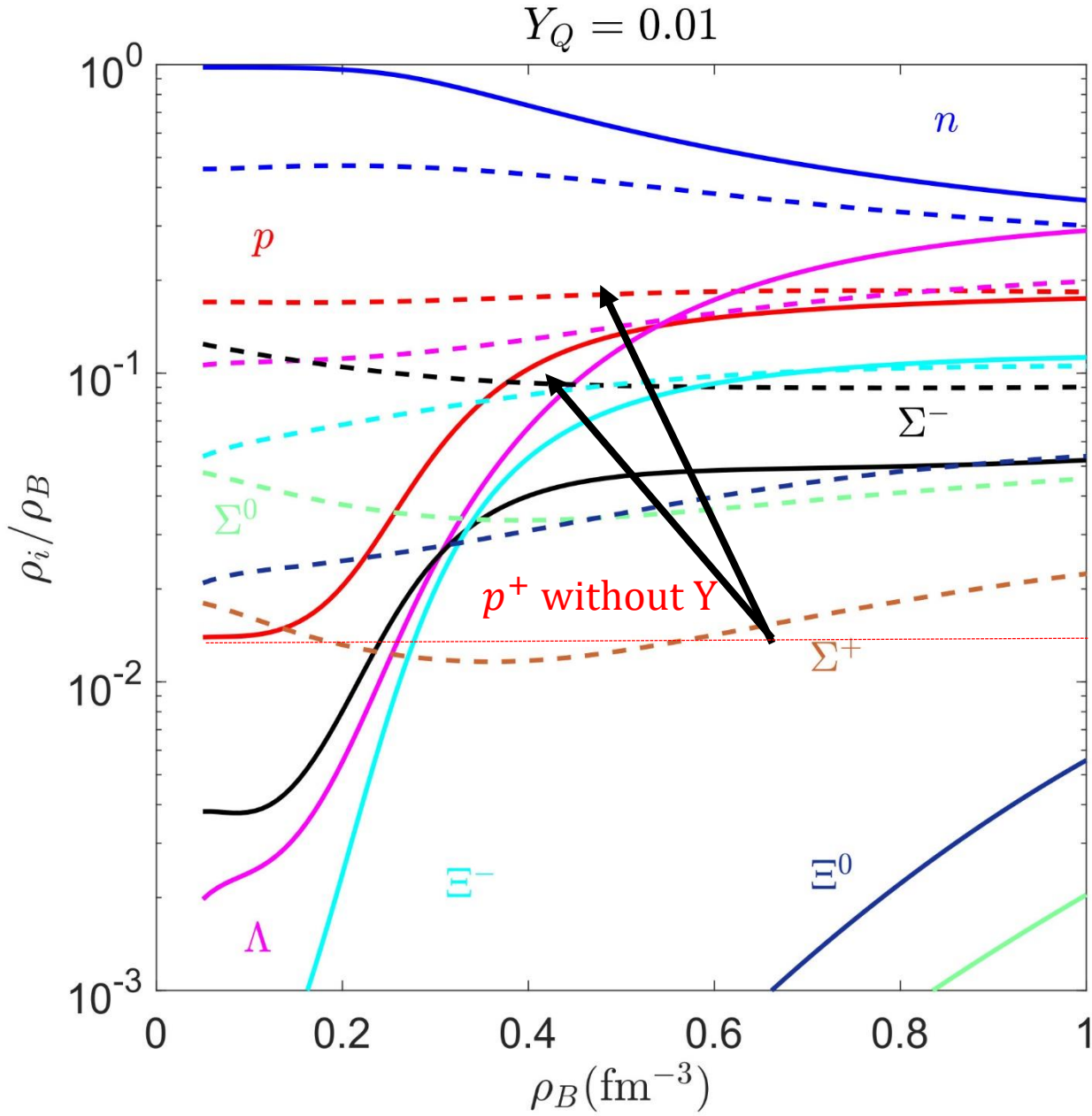


Composition of hyperonic matter at fixed Y_Q (I)



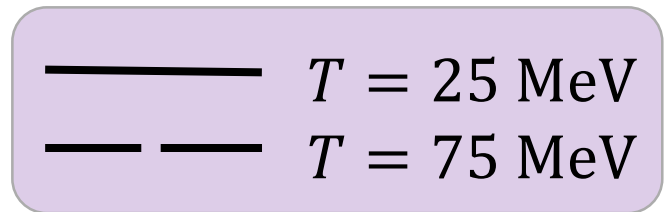
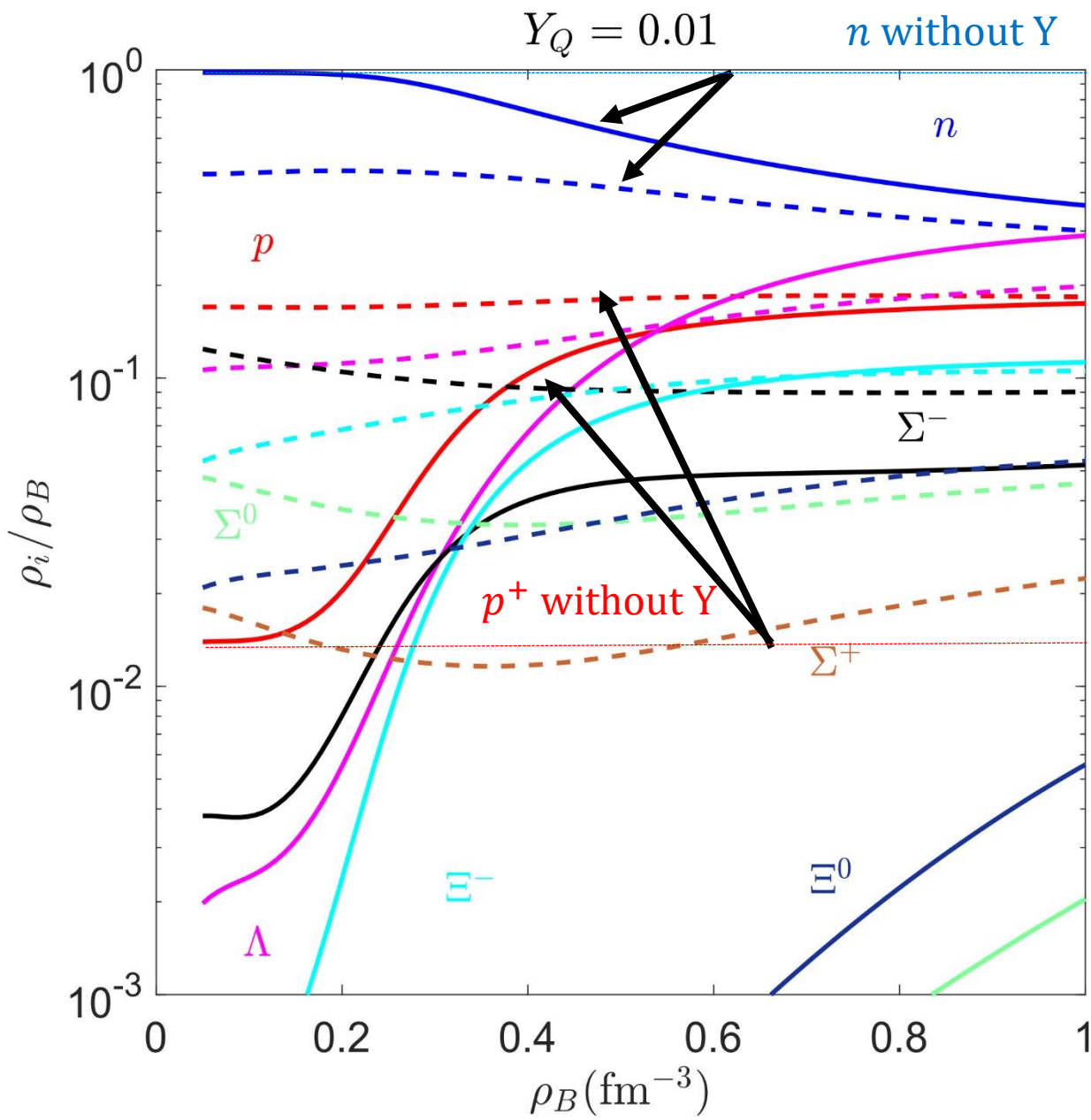
- Hyperons significantly change the composition pattern of matter.

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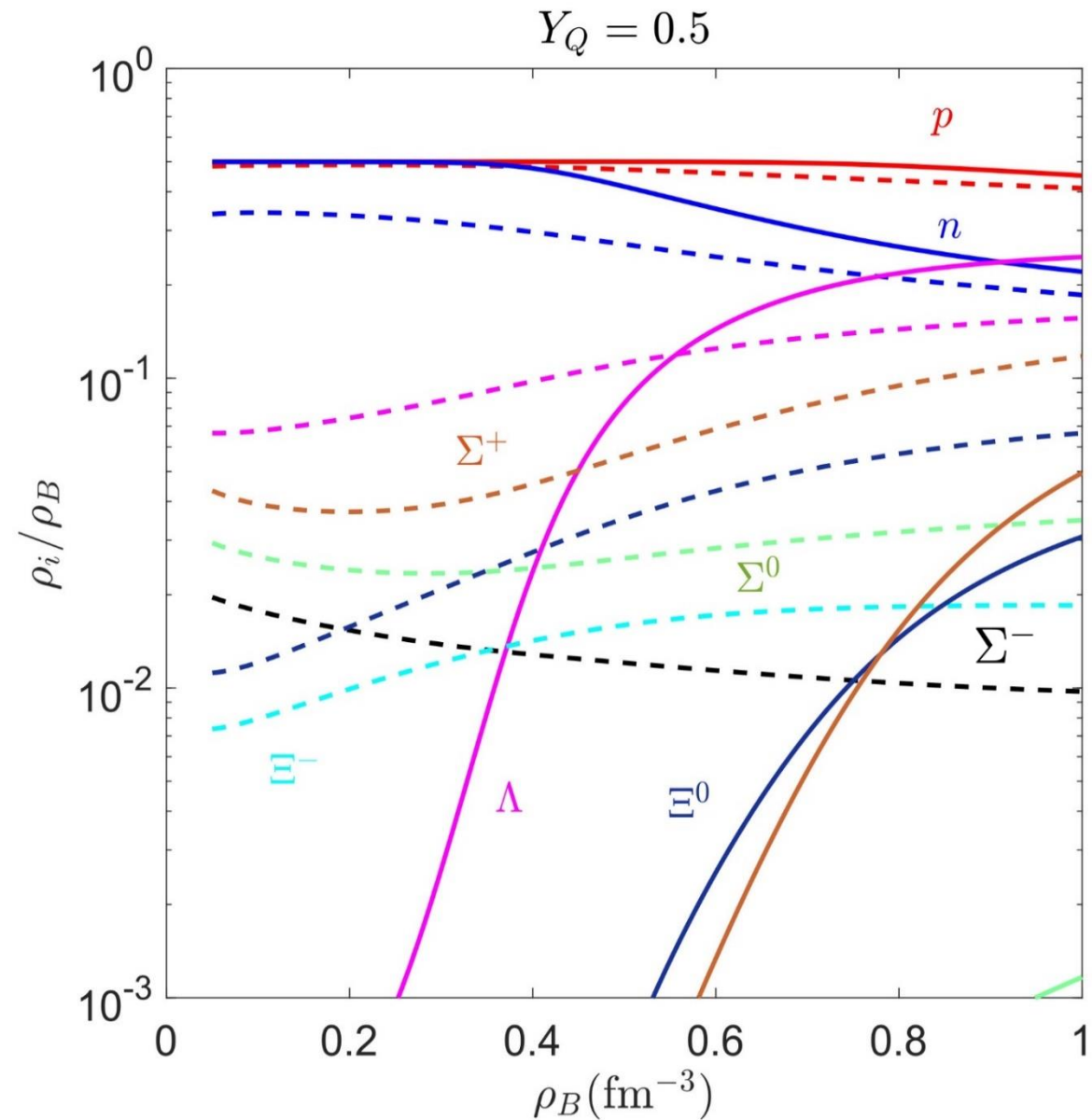
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- Producing negative charged hyperons allow for protons to be much more abundant than in case without hyperons.

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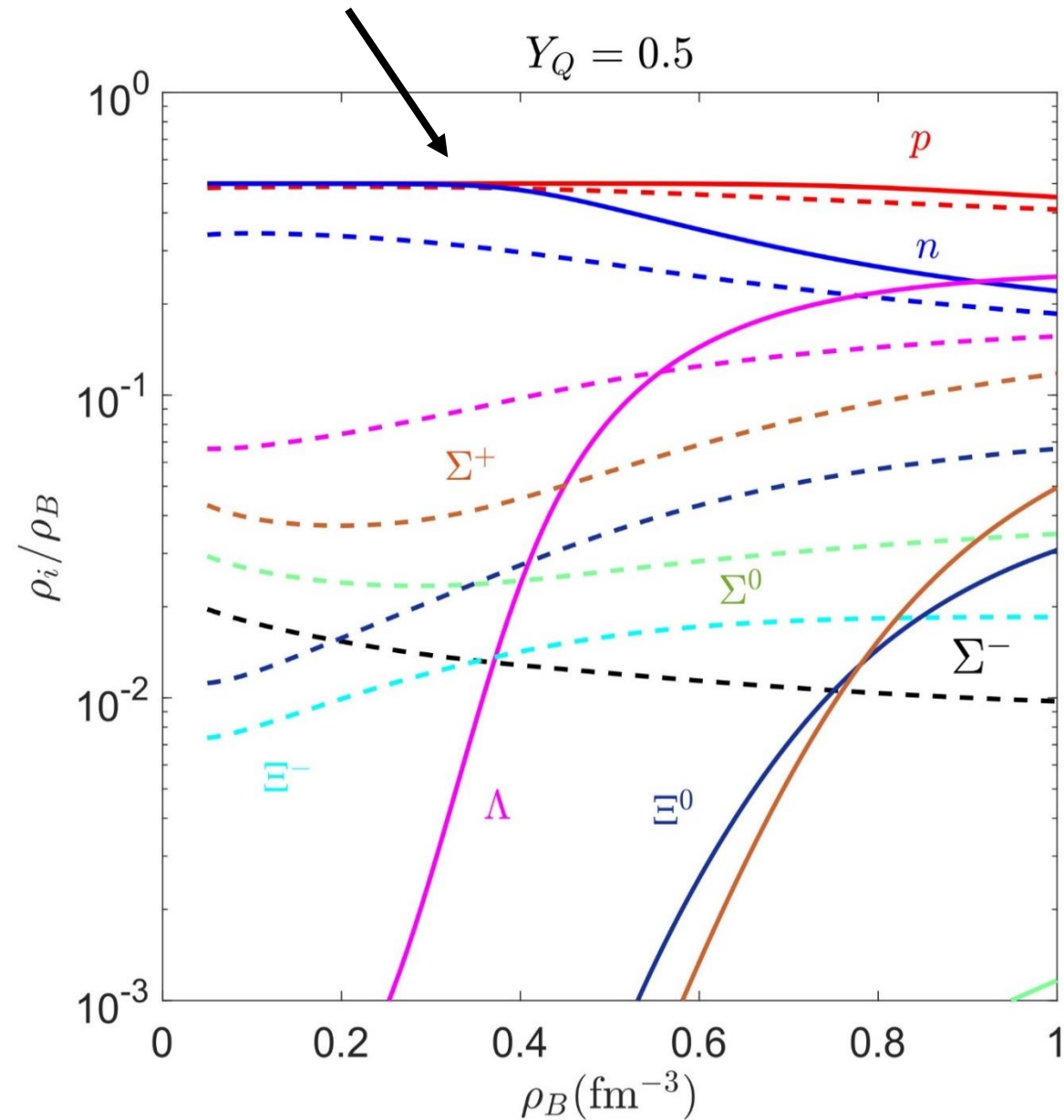


- Hyperons significantly change the composition pattern of matter.
- Producing negative charged hyperons allow for protons to be much more abundant than in case without hyperons.
- On the contrary, neutron abundance is significantly reduced.
- The increase of the temperature has an effect of smoothing out the changes – the composition pattern at high temperatures varies slowly.

Composition of hyperonic matter at fixed Y_Q (II)



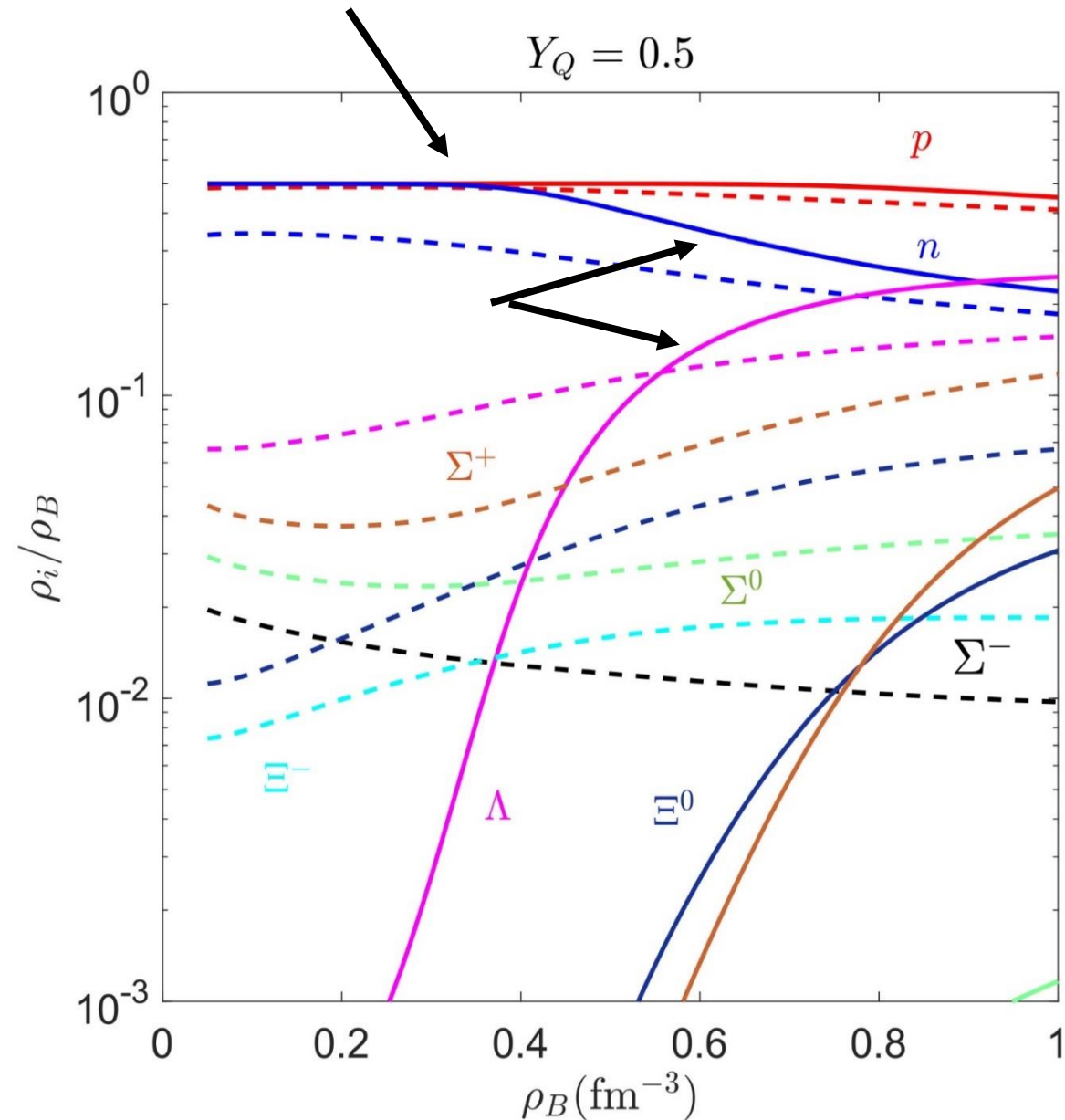
Composition of hyperonic matter at fixed Y_Q (II)



— $T = 25 \text{ MeV}$
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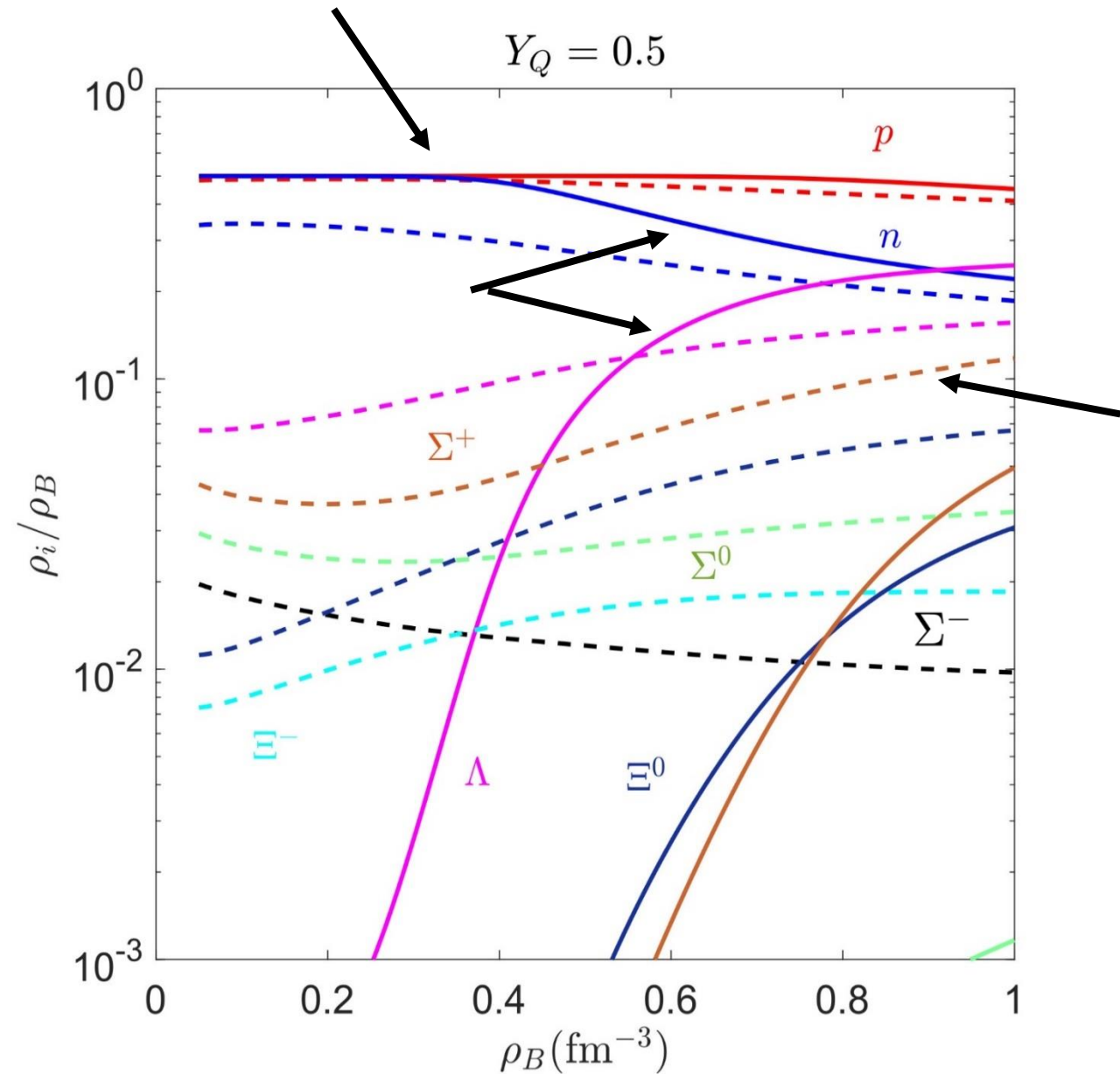
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Composition of hyperonic matter at fixed Y_Q (II)



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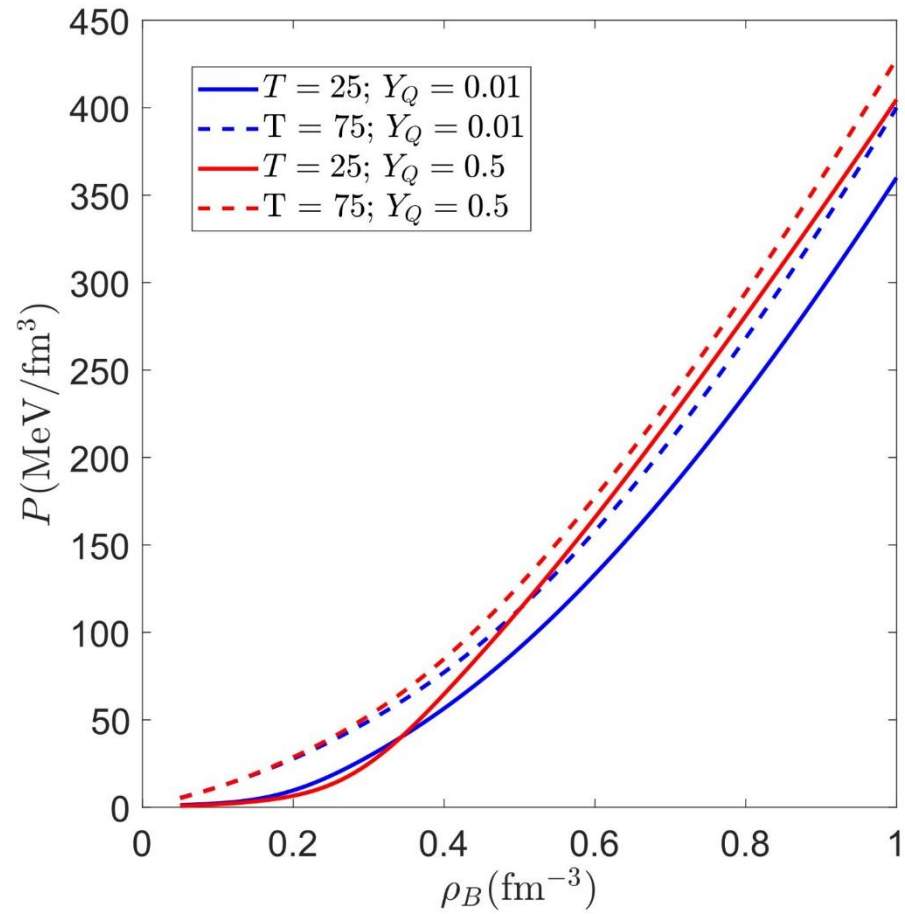


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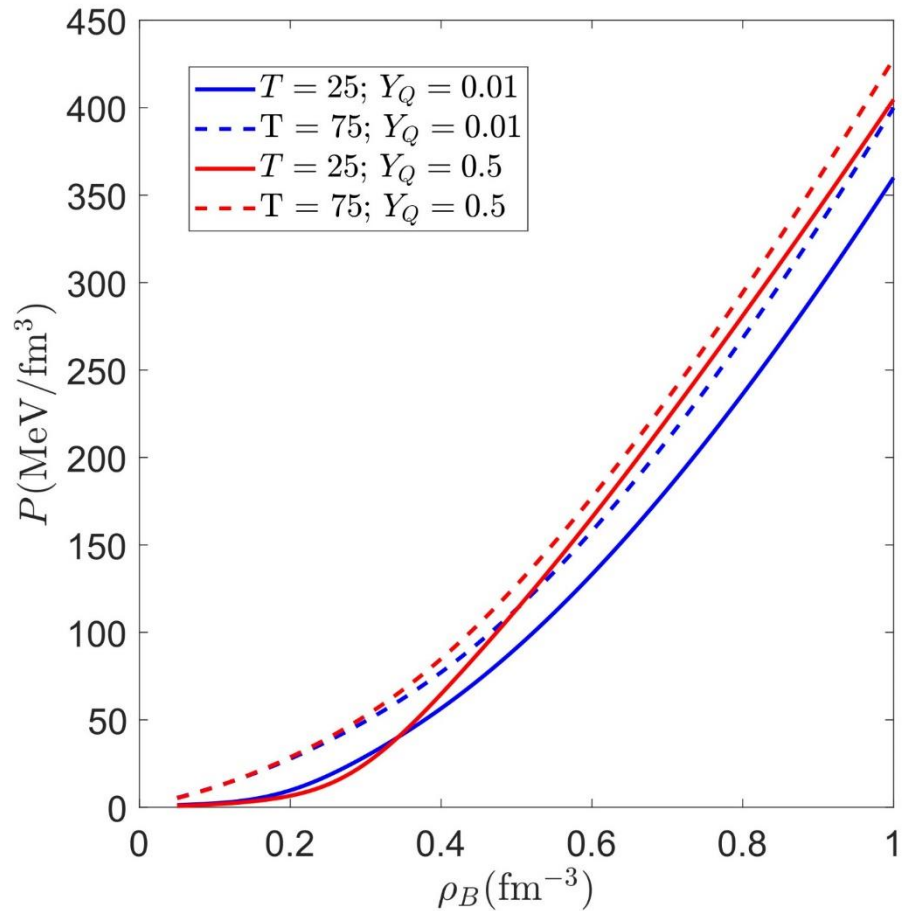
- At low and moderate temperatures such as $T = 25 \text{ MeV}$, matter stays isospin symmetric at the beginning of the core.
- At higher densities the symmetry is broken and neutrons are quickly converted into Λ hyperons.
- At high temperatures, there is a considerable amount of Σ^+ at any point of the core.

$p(\rho_B)$ and $E/A(\rho_B)$ of hyperonic matter at fixed Y_Q

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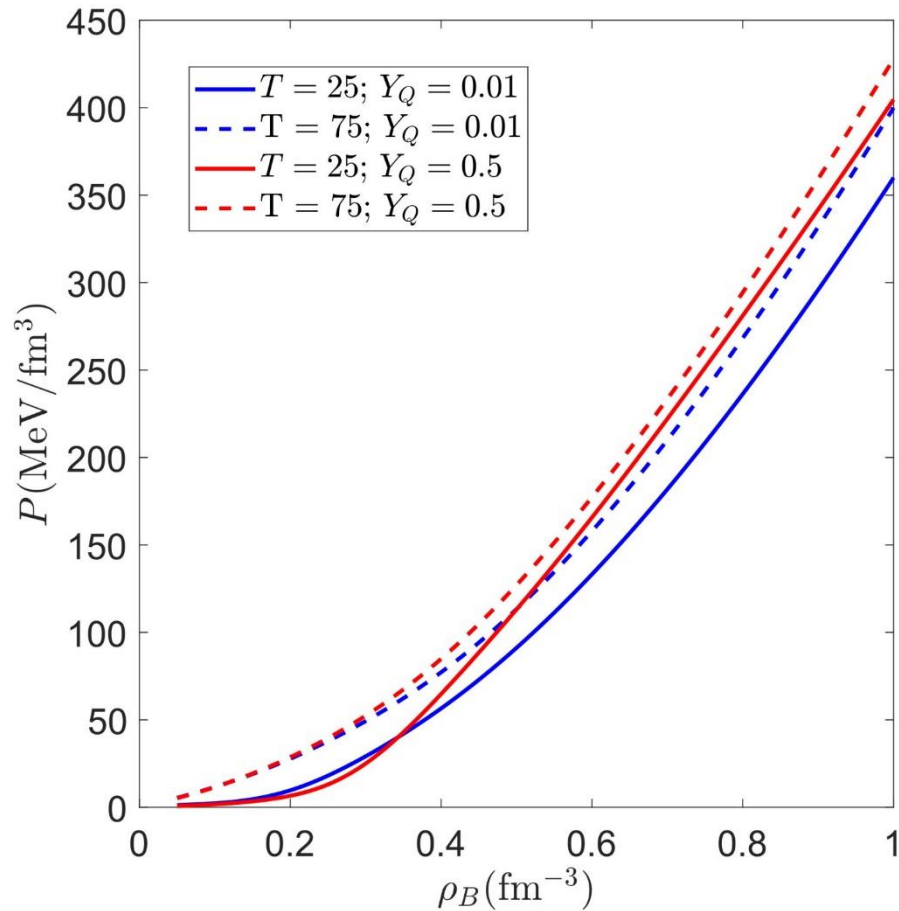


$p(\rho_B)$ and $E/A(\rho_B)$ of hyperonic matter at fixed Y_Q



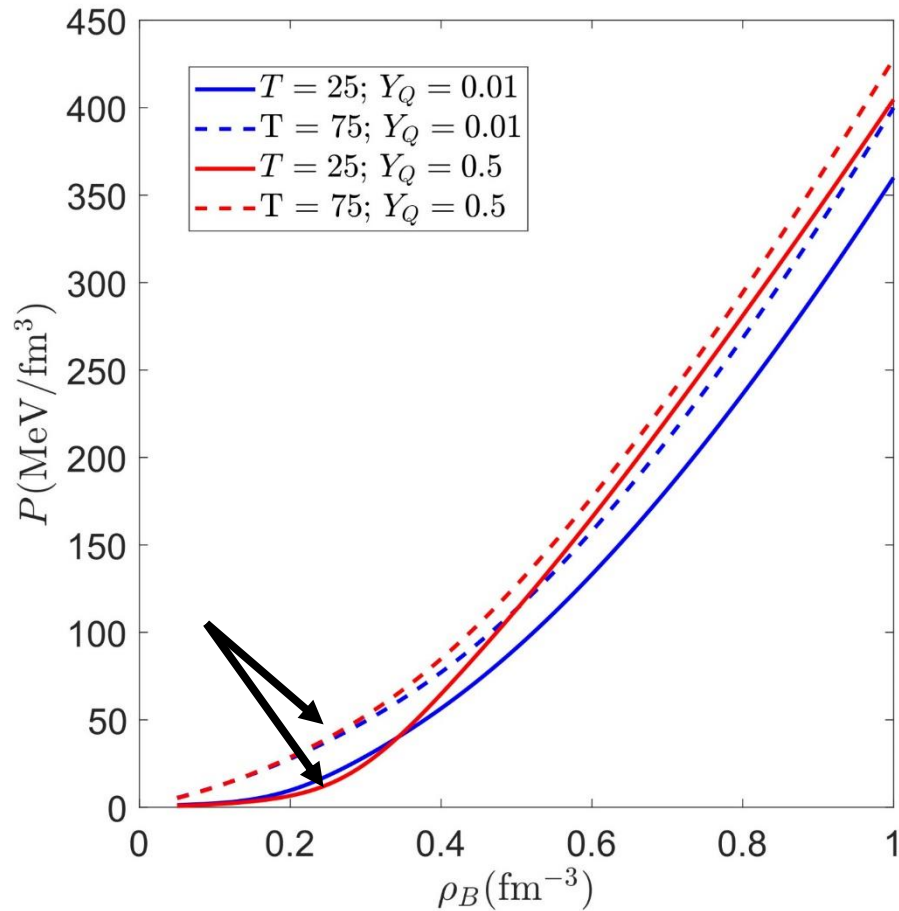
- The pressure strongly depends on T and Y_Q .

$p(\rho_B)$ and $E/A(\rho_B)$ of hyperonic matter at fixed Y_Q



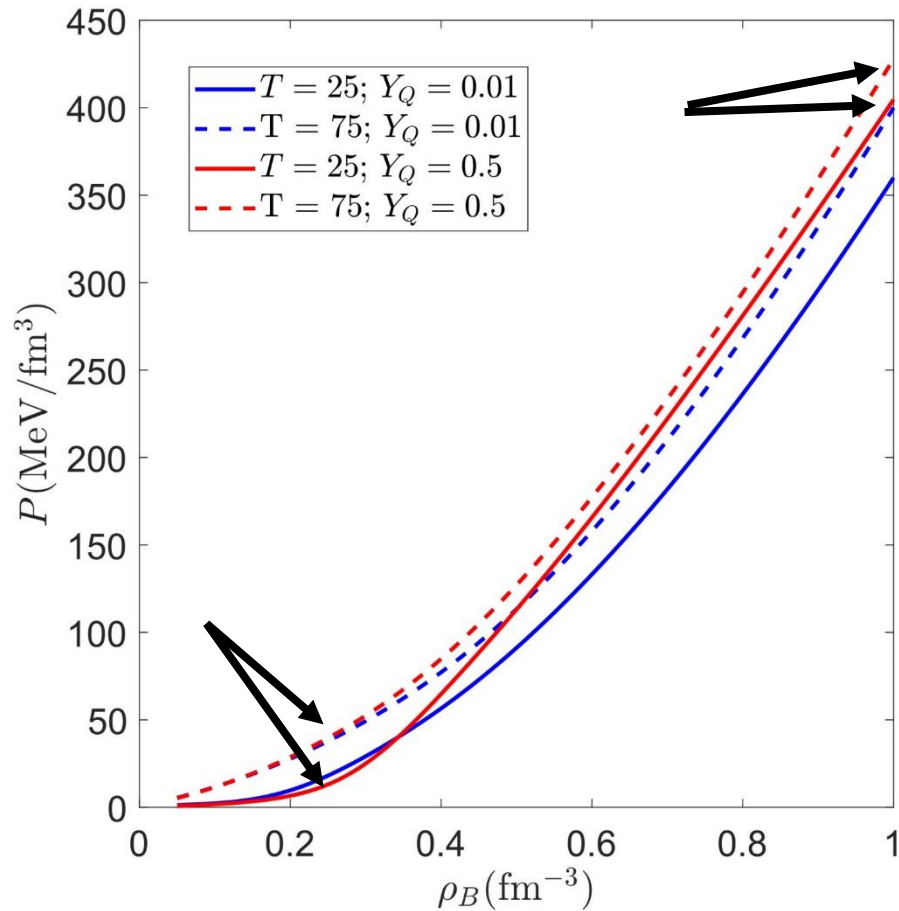
- The pressure strongly depends on T and Y_Q .
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$p(\rho_B)$ and $E/A(\rho_B)$ of hyperonic matter at fixed Y_Q



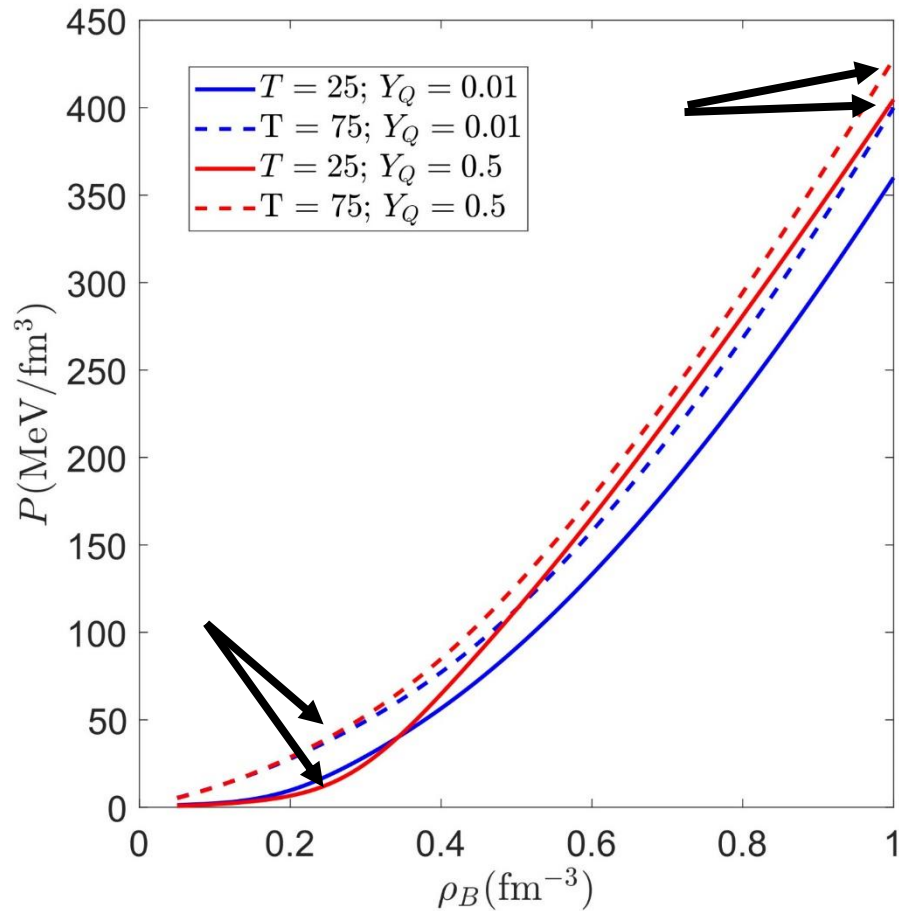
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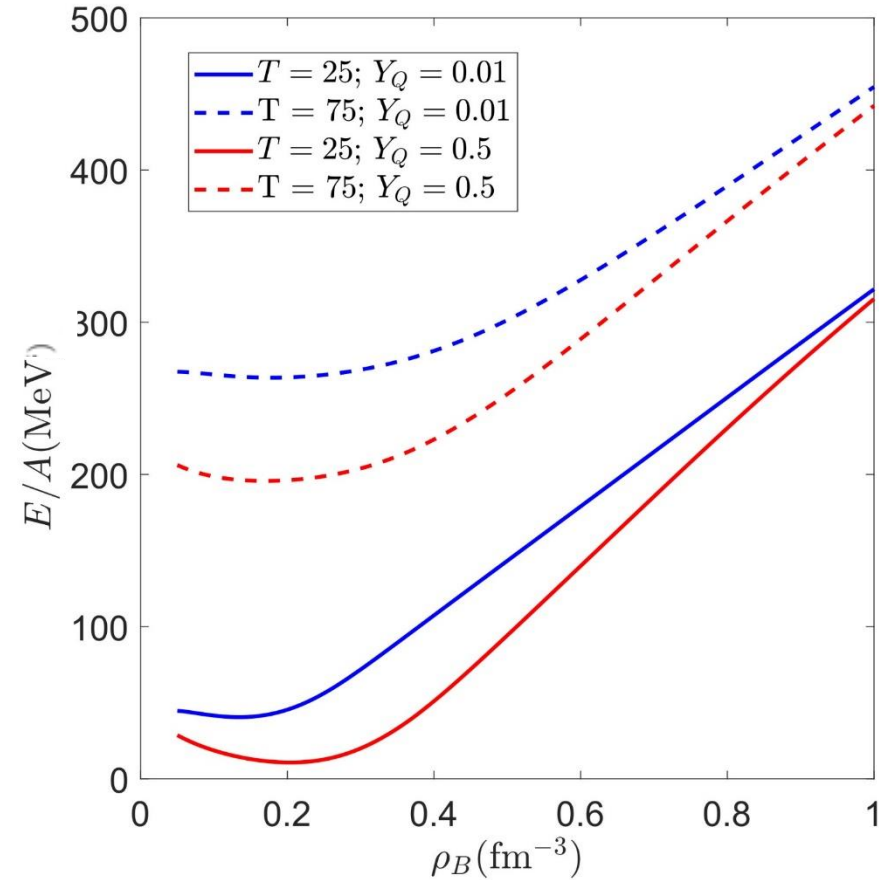


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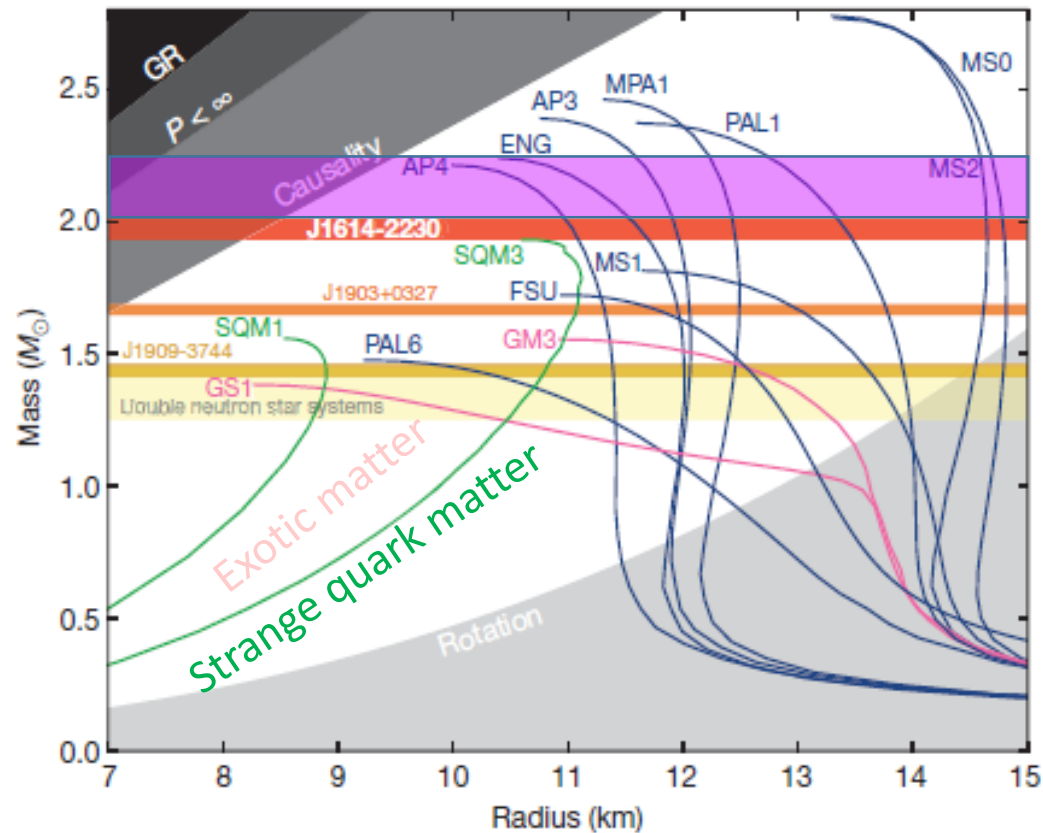


- E/A is larger at higher temperatures.
- E/A weakly depends on Y_Q , at high densities.

Application: $M(R)$ of a β^- stable star

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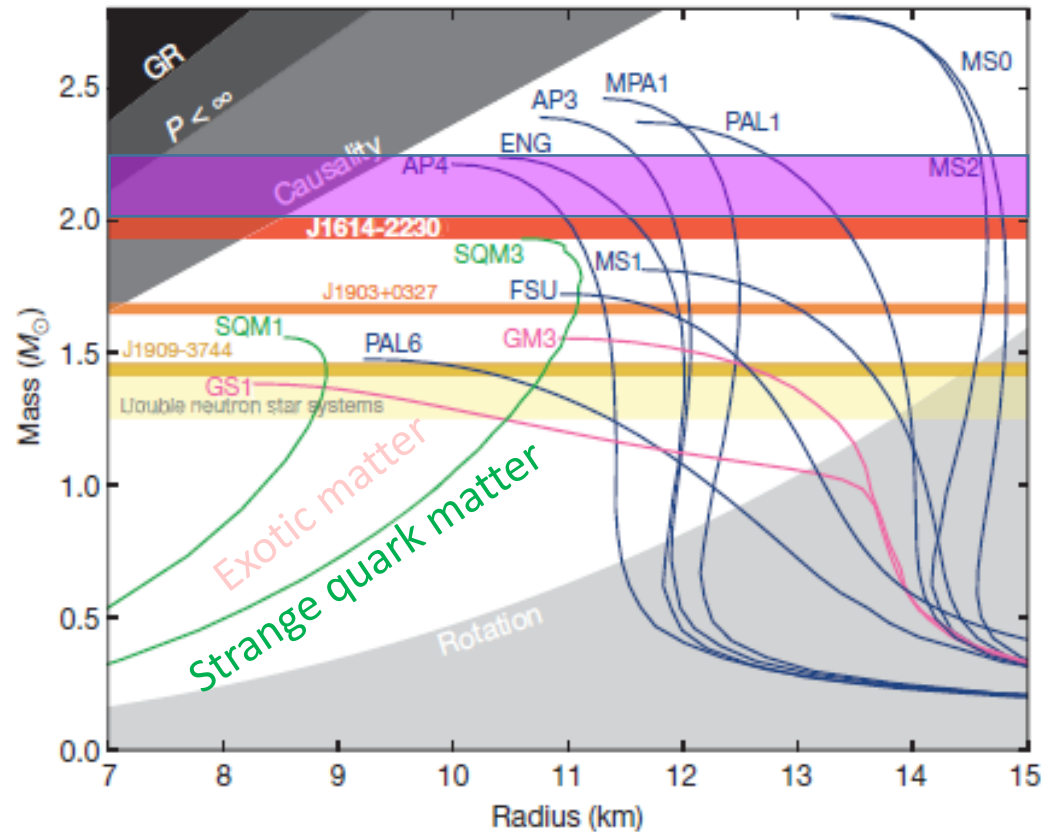
- One of the strongest constraints that we have is the maximum mass that the model predicts.



doi:10.1038/nature09466

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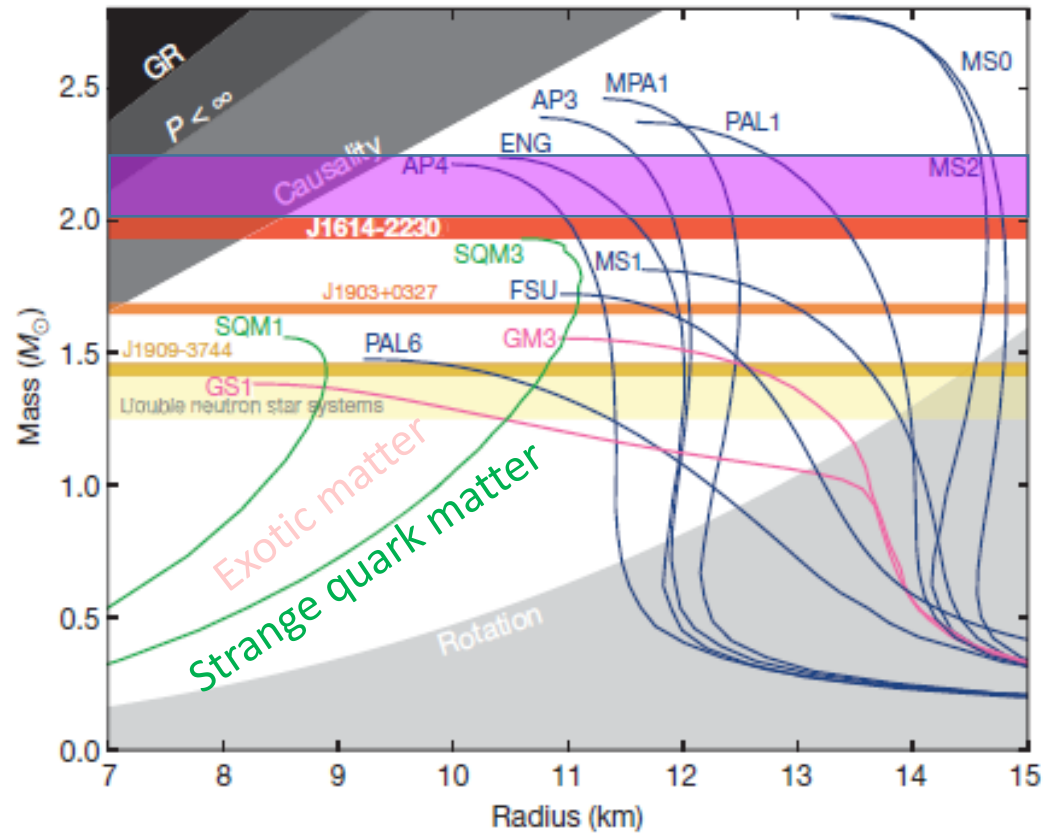
- $M(R)$ is obtained as a solution of the TOV – equations with an only input – **EoS**.

$$\frac{dP}{dr} = -\frac{G\rho m}{r^2} \left(1 + \frac{P}{\rho c^2}\right) \left(1 + \frac{4\pi Pr^3}{mc^2}\right) \left(1 - \frac{2Gm}{c^2 r}\right)^{-1}$$

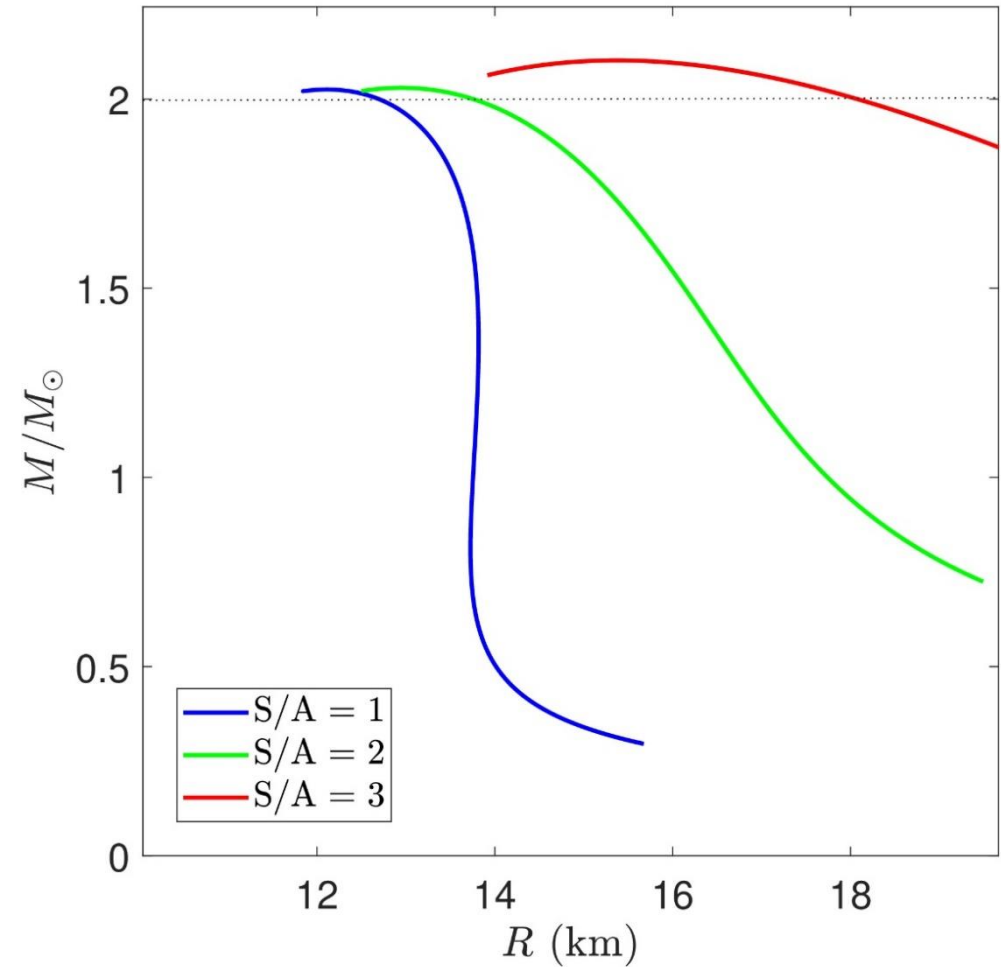
$$\frac{dm}{dr} = 4\pi r^2 \rho$$

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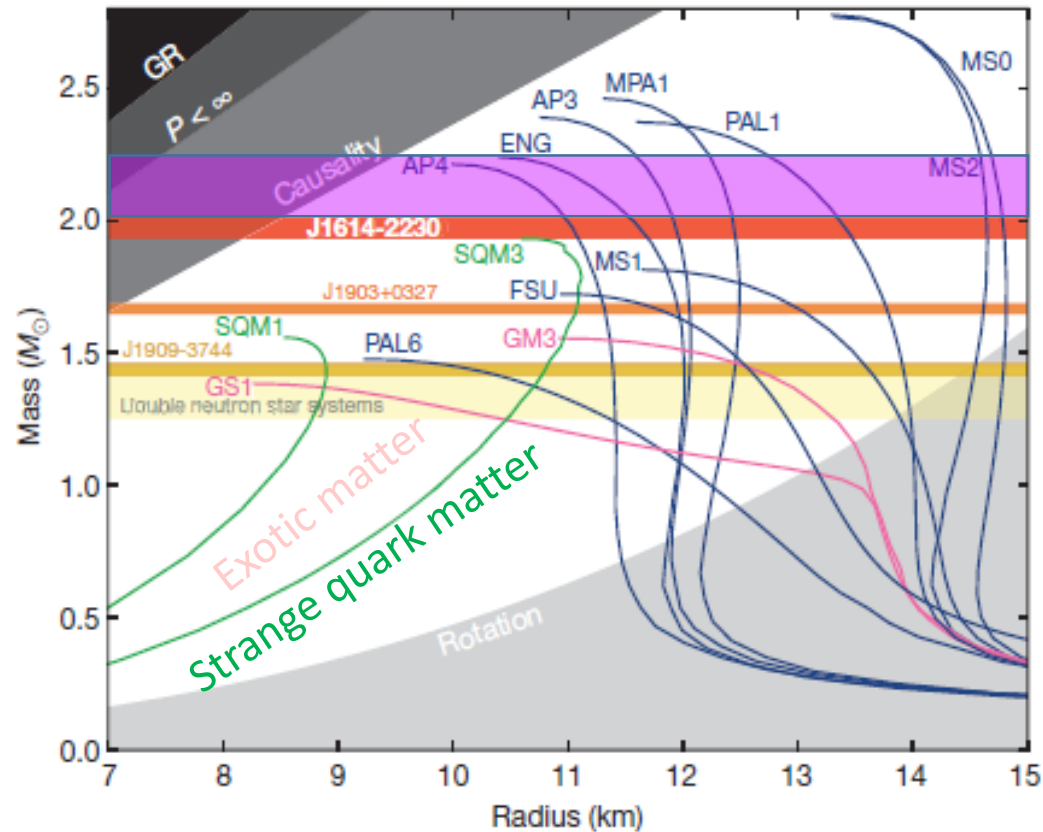


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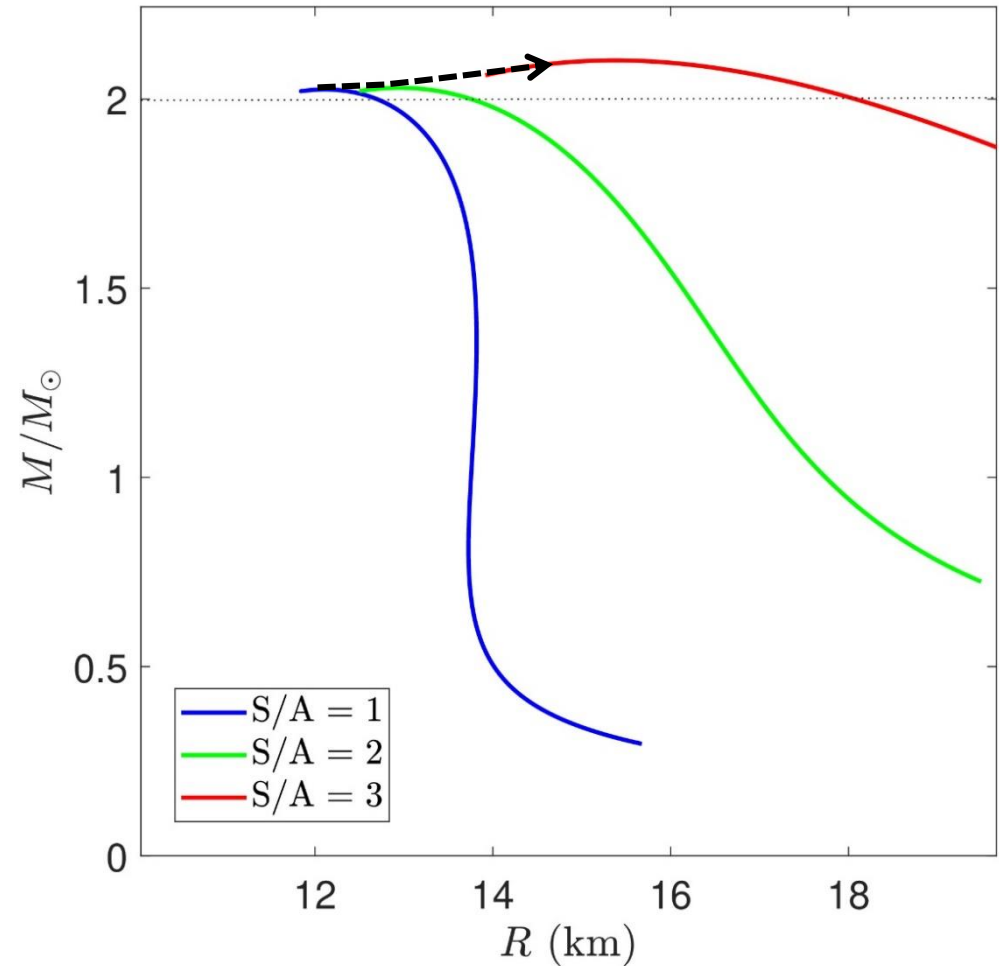


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- M_{max} increases with S/A .
- The radius significantly shifts toward higher values with an increase of S/A .

Summary

- We extended the **FSU2H** hyperonic model to finite temperature, constructing the new so-called **FSU2H*** model, in order to be used in early stages of NS evolution and in NS mergers.
- The baryonic EoS is properly tabulated, making it useful for relativistic simulations.
- All baryons of the baryon octet can be found in the core of the star and in certain regimes their contribution can be significant.
- $P(\rho_B)$ and $\epsilon(\rho_B)$ are sensitive to the temperature and charge fraction of star matter at which the star is considered.
- To show the usefulness of the EoS we obtained the $M(R)$ relation for beta stable stars at constant S/A .



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RMF model extended I

$$(i\gamma_\mu \partial^\mu - m_b^* - g_{\omega b} \gamma_0 \omega^0 - g_{\phi b} \gamma_0 \phi^0 - g_{\rho b} I_{3b} \gamma_0 \rho_3^0) \Psi_b = 0,$$

$$(i\gamma_\mu \partial^\mu - q_l \gamma_\mu A^\mu - m_l) \psi_l = 0,$$

Baryon's and lepton's equations of motions

$$m_\sigma^2 \bar{\sigma} + \frac{\kappa}{2} g_{\sigma b}^3 \bar{\sigma}^2 + \frac{\lambda}{3!} g_{\sigma b}^4 \bar{\sigma}^3 = \sum_b g_{\sigma b} \rho_b^s,$$

$$m_{\sigma^*}^2 \bar{\sigma}^* = \sum_{b^*} g_{\sigma b^*} \rho_b^s,$$

$$m_\omega^2 \bar{\omega} + \frac{\zeta}{3!} g_{\omega b}^4 \bar{\omega}^3 + 2\Lambda_\omega g_{\rho,b}^2 g_{\omega,b}^2 \bar{\omega} \bar{\rho}^2 = \sum_b g_{\omega b} \rho_b,$$

$$m_\rho^2 \bar{\rho} + 2\Lambda_\omega g_{\rho,b}^2 g_{\omega,b}^2 \bar{\omega}^2 \bar{\rho} = \sum_b g_{\rho b} I_{3b} \rho_b,$$

$$m_\phi^2 \bar{\phi} = \sum_b g_{\phi b} \rho_b,$$

Meson's equation of motion in RMF approximation

$$\rho_b = \langle \bar{\Psi}_b \gamma^0 \Psi_b \rangle = \frac{\gamma_b}{2\pi^2} \int_0^\infty dk k^2 f_b(k, T),$$

$$\rho_b^s = \langle \bar{\Psi}_b \Psi_b \rangle = \frac{\gamma_b}{2\pi^2} \int_0^\infty dk k^2 \frac{m_b^*}{\sqrt{k^2 + m_b^{*2}}} f_b(T, k)$$

Scalar and baryonic density

$$f_b(k, T) = \left[1 + \exp \left(\frac{\sqrt{k^2 + m_b^{*2}} - \mu_b^*}{T} \right) \right]^{-1}$$

Fermi – dirac distribution

$$\mu_b^* = \mu_b - g_{b\omega} \bar{\omega} - g_{b\rho} \bar{\rho} - g_{b\phi} \bar{\phi}.$$

$$m_b^* = m_b - g_{\sigma b} \sigma - g_{\sigma^* b} \sigma^*,$$

Effective chemical potential and charge neutrality

RMF model extended II

$$\mu_{b^0} = \mu_n,$$

$$\mu_{b^-} = 2\mu_n - \mu_p,$$

$$\mu_{b^+} = \mu_p,$$

$$\mu_n - \mu_p = \mu_e - \mu_{\nu_e},$$

$$\mu_e = \mu_\mu + \mu_{\nu_e} - \mu_{\bar{\nu}_\mu},$$

β equilibrium

$$\rho_B = \sum_b \rho_b,$$

$$Y_l \cdot \rho_B = \rho_l + \rho_{\nu_l}$$

Conservation of baryon and lepton numbers

$$T_{\mu\nu} = \frac{\partial \mathcal{L}}{\partial (\partial_\mu \Phi_\alpha)} \partial^\mu \Phi_\alpha - \eta_{\mu\nu} \mathcal{L},$$

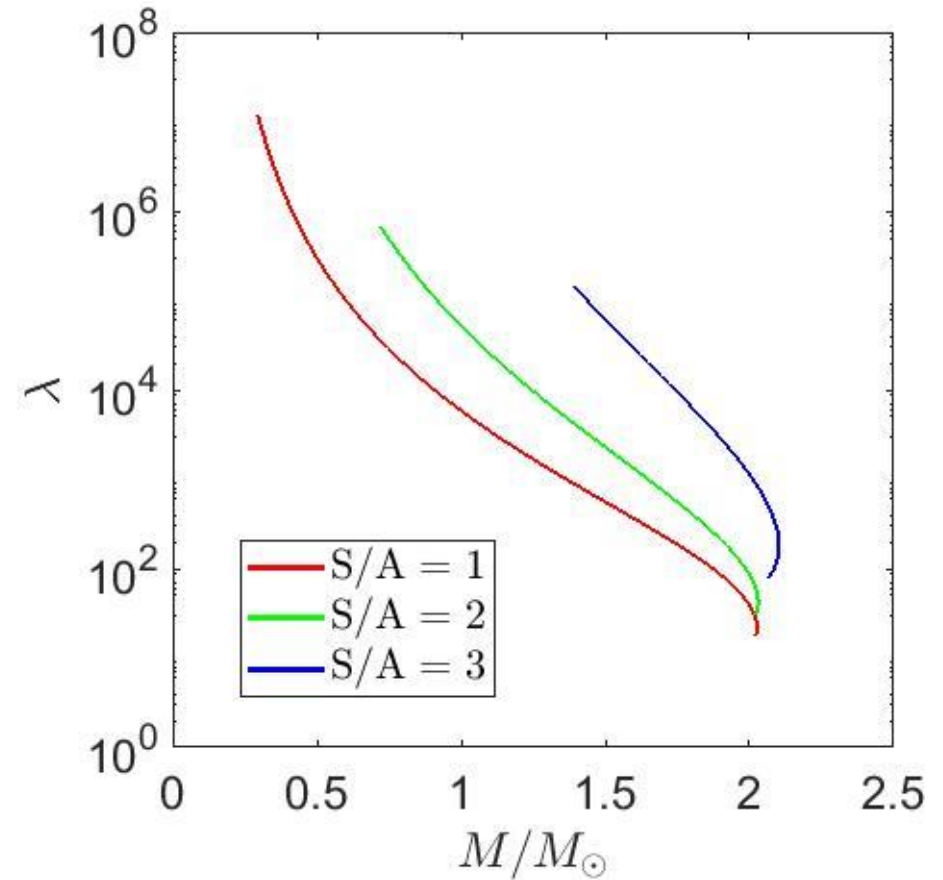
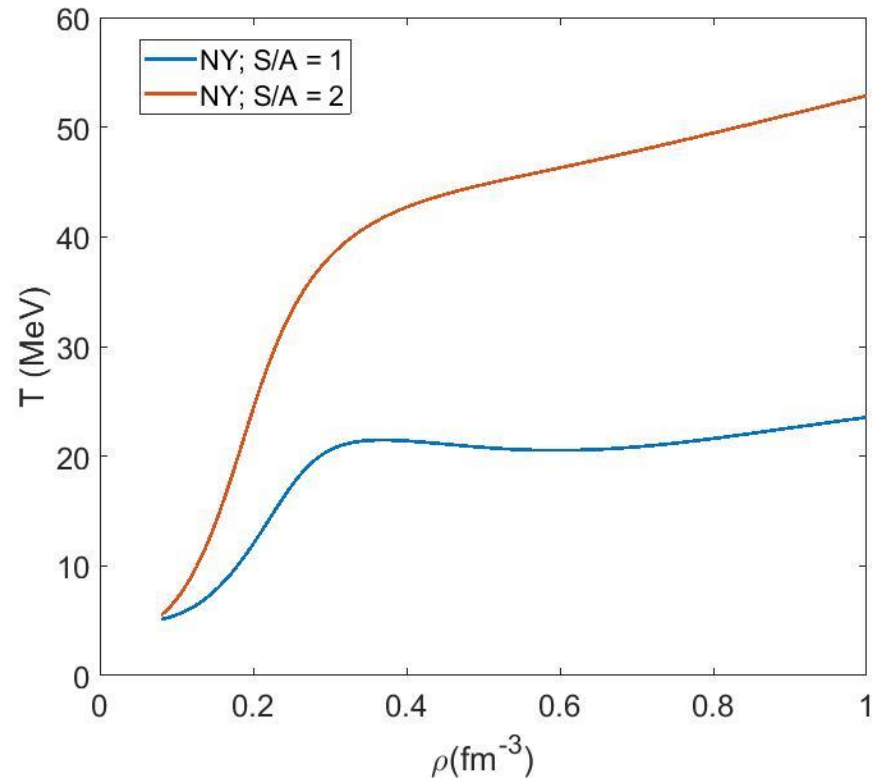
Energy-momentum tensor

$$\begin{aligned} \epsilon &= \langle T_{00} \rangle \\ &= \frac{1}{2\pi^2} \sum_b \gamma_b \int_0^\infty dk k^2 \sqrt{k^2 + m_b^{*2}} f_b(k, T) \\ &\quad + \frac{1}{2\pi^2} \sum_l \gamma_l \int_0^\infty dk k^2 \sqrt{k^2 + m_l^2} f_l(k, T) \\ &\quad + \frac{1}{2} (m_\omega^2 \bar{\omega}^2 + m_\rho^2 \bar{\rho}^2 + m_\sigma^2 \bar{\phi}^2 + m_\sigma^2 \bar{\sigma}^2 + m_\sigma^2 \cdot \bar{\sigma}^{*2}) \\ &\quad + \frac{\kappa}{3!} (g_\sigma \bar{\sigma})^3 + \frac{\lambda}{4!} (g_\sigma \bar{\sigma})^4 + \frac{\zeta}{8} (g_\omega \bar{\omega})^4 + 3\Lambda_\omega (g_\rho g_\omega \bar{\rho} \bar{\omega})^2, \\ P &= \frac{1}{3} \langle T_{jj} \rangle \\ &= \frac{1}{6\pi^2} \sum_b \gamma_b \int_0^\infty dk \frac{k^4}{\sqrt{k^2 + m_b^{*2}}} f_b(k, T) \\ &\quad + \frac{1}{6\pi^2} \sum_l \gamma_l \int_0^\infty dk \frac{k^4}{\sqrt{k^2 + m_l^2}} f_l(k, T) \\ &\quad + \frac{1}{2} (m_\omega^2 \bar{\omega}^2 + m_\rho^2 \bar{\rho}^2 + m_\sigma^2 \bar{\phi}^2 - m_\sigma^2 \bar{\sigma}^2 - m_\sigma^2 \cdot \bar{\sigma}^{*2}) \\ &\quad - \frac{\kappa}{3!} (g_\sigma \bar{\sigma})^3 - \frac{\lambda}{4!} (g_\sigma \bar{\sigma})^4 + \frac{1}{24} \zeta (g_\omega \bar{\omega})^4 + \Lambda_\omega (g_\rho g_\omega \bar{\rho} \bar{\omega})^2, \end{aligned}$$

$$\begin{aligned} s &= \frac{1}{T} \left(\epsilon + P - \sum_i \mu_i \rho_i \right) \\ f &= \sum_i \mu_i \rho_i - P. \end{aligned}$$

Thermodynamic quantities

Temperature profiles and tidal deformability



Why FSU2H* model? I

PASA, 34, e065 (2017)

ρ_0 (fm^{-3})	E/A (MeV)	K (MeV)	m_N^*/m_N (ρ_0)	$E_{\text{sym}}(\rho_0)$ (MeV)	L (MeV)	K_{sym} (MeV)
0.1505	-16.28	238.0	0.593	30.5	44.5	86.4

Consistent with the majority of the calculations, variety of nuclear data from terrestrial experiments, astrophysical observations...

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m_σ (MeV)	m_ω (MeV)	m_ρ (MeV)	m_{σ^*} (MeV)	m_ϕ (MeV)	$g_{\sigma N}^2$	$g_{\omega N}^2$	$g_{\rho N}^2$	κ (MeV)	λ	ζ	Λ_ω
497.479	782.500	763.000	980.000	1020.000	102.72	169.53	197.27	4.00014	-0.0133	0.008	0.045

Values of parameters in the model

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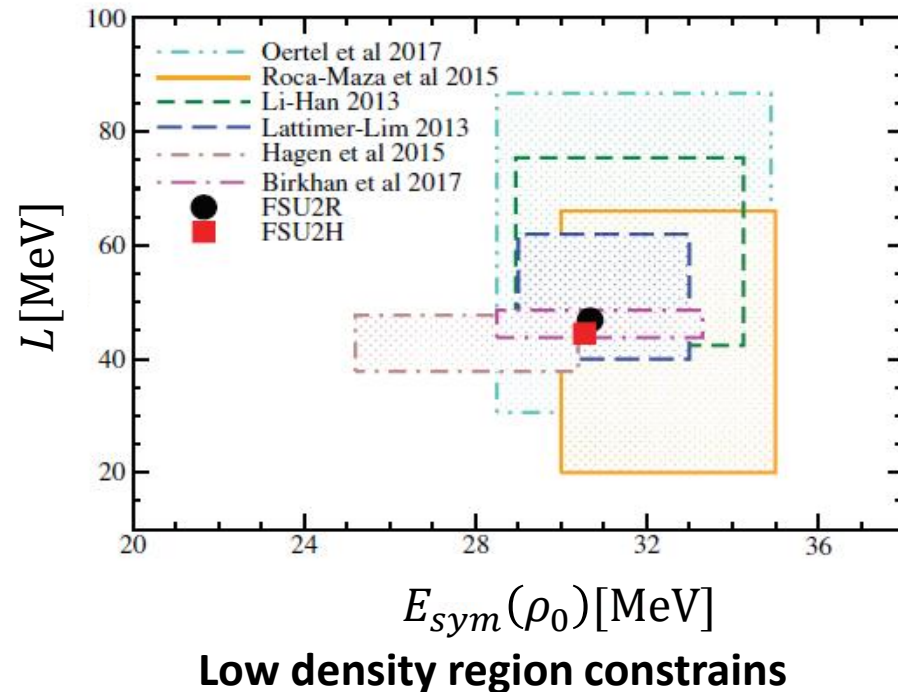
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Why FSU2H* model? II

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Values of the parameters in the model
related to hyperons

Y	$R_{\sigma Y}$	$R_{\omega Y}$	$R_{\rho Y}$	$R_{\sigma^* Y}$	$R_{\phi Y}$
Λ	0.6613	2/3	0	0.2812	$-\sqrt{2}/3$
Σ	0.4673	2/3	2	0.2812	$-\sqrt{2}/3$
Ξ	0.3305	1/3	1	0.5624	$-2\sqrt{2}/3$

$$R_{iY} = \frac{g_{iY}}{g_{iN}}; i = (\sigma, \omega, \rho); R_{\sigma^* Y} = \frac{g_{\sigma^* Y}}{g_{\sigma Y}}; R_{\phi Y} = \frac{g_{\phi Y}}{g_{\omega N}}$$

Flavour SU(3) symmetry, the vector
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Flavour SU(3) symmetry, the vector dominance model, and ideal mixing for the physical ω and ρ field

Potential felt by a hyperon i in j -particle matter is given by

$$U_i^{(j)}(\rho_j) = -g_{\sigma i} \bar{\sigma}^{(j)} - g_{\sigma i} \bar{\sigma}^{*(j)} + g_{\omega i} \bar{\omega}^{(j)} + g_{\rho i} I_{3i} \bar{\rho}^{(j)} + g_{\phi i} \bar{\phi}^{(j)}$$

Why FSU2H* model? II

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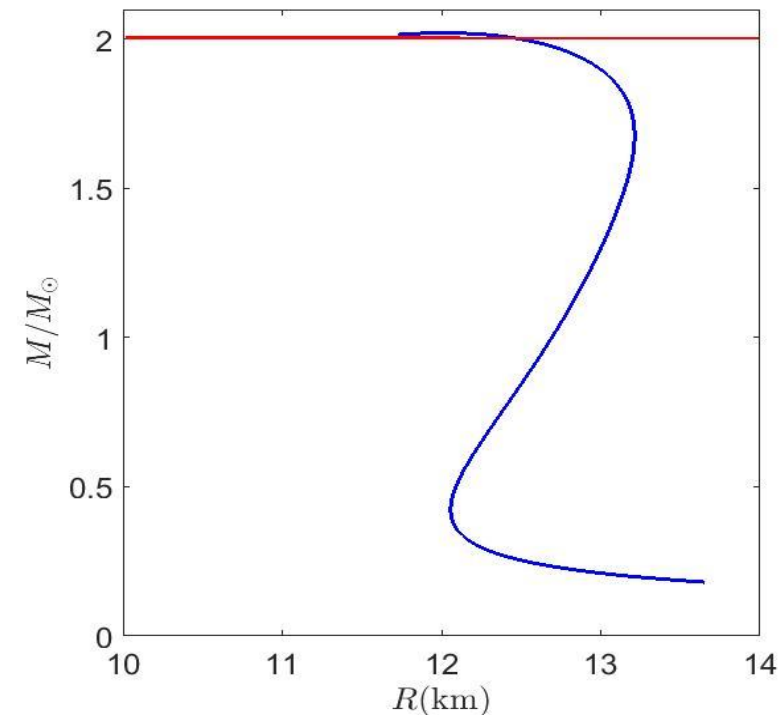
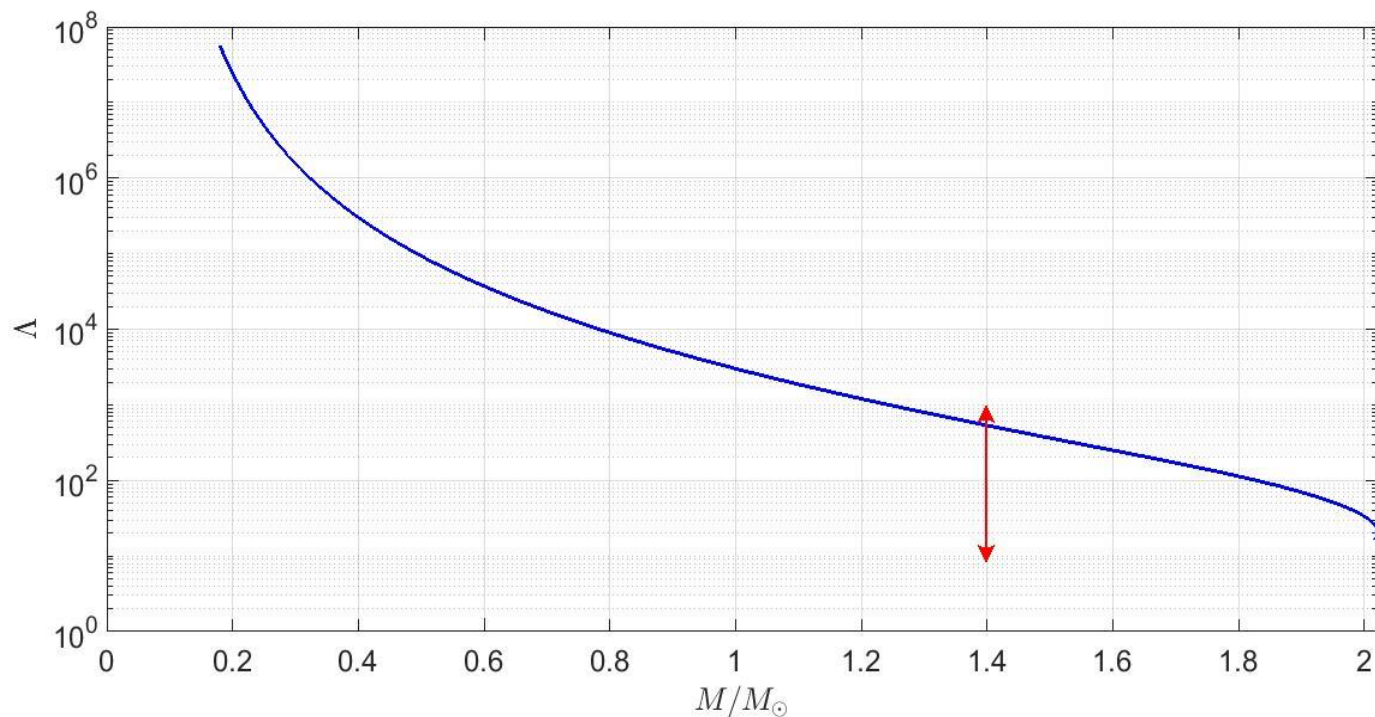
$$U_{\Lambda}^{(N)}(\rho_0) = -28 \text{ MeV};$$

$$U_{\Sigma}^{(N)}(\rho_0) = 30 \text{ MeV};$$

$$U_{\Xi}^{(N)}(\rho_0) = -22 \text{ MeV};$$

Hyperon potentials in SNM

Why FSU2H* model? III



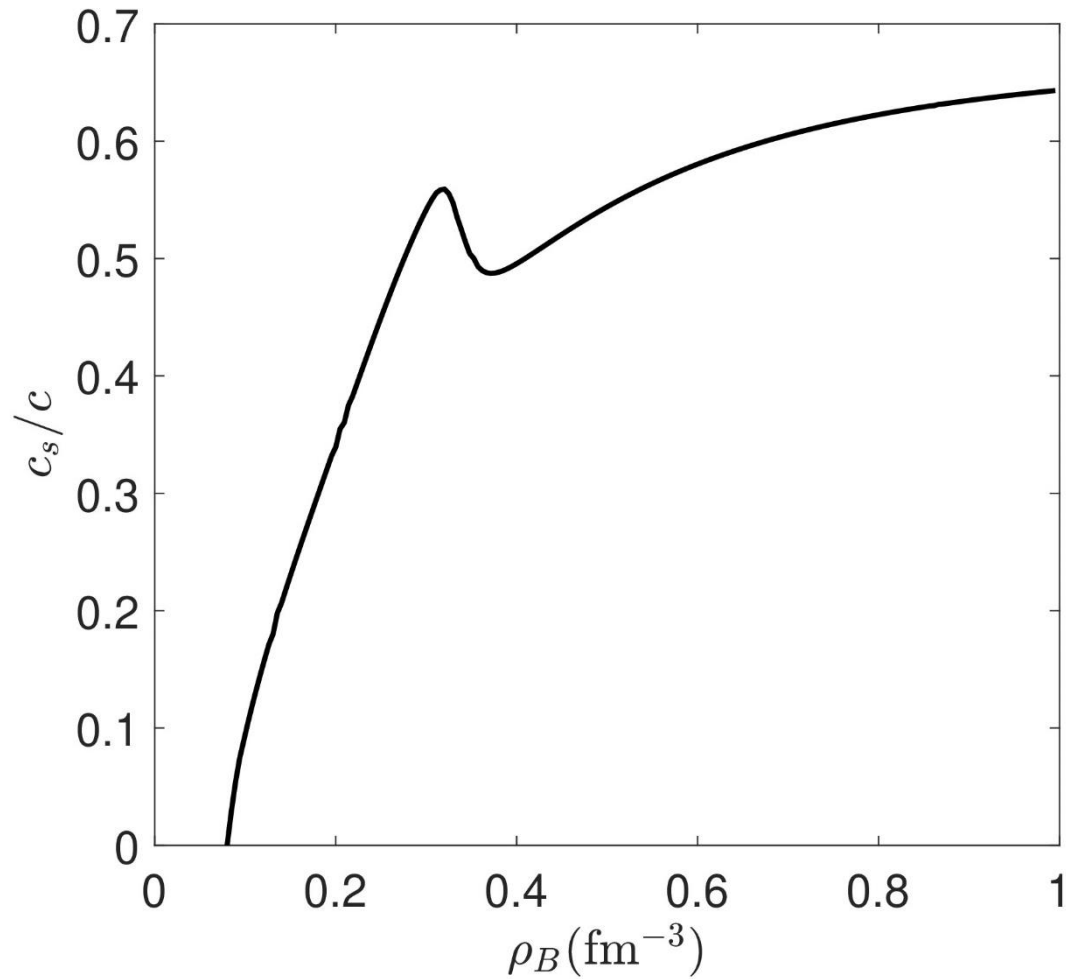
Intermediate and high density regions constrains

M_{\max} (M_{\odot})	$R(M_{\max})$ (km)	$R(1.4M_{\odot})$ (km)	$\Lambda(1.4M_{\odot})$
2.03	12.02	13.08	526.3

In agreement with:

- $M_{\max} > 2M_{\odot}$
- $70 < \Lambda(1.4M_{\odot}) < 580$
- $10.5 \text{ km} < R(1.4M_{\odot}) < 13.3 \text{ km}$

Speed of sound ($T = 0$)



$$\frac{c_s}{c} = \sqrt{\frac{dp}{d\epsilon}}$$