

Investigation of the Σ^0 Production Mechanism in $p(3.5 \text{ GeV})+p$ Collisions

Waleed Esmail
For the HADES Collaboration
GSI Helmholtzzentrum für Schwerionenforschung

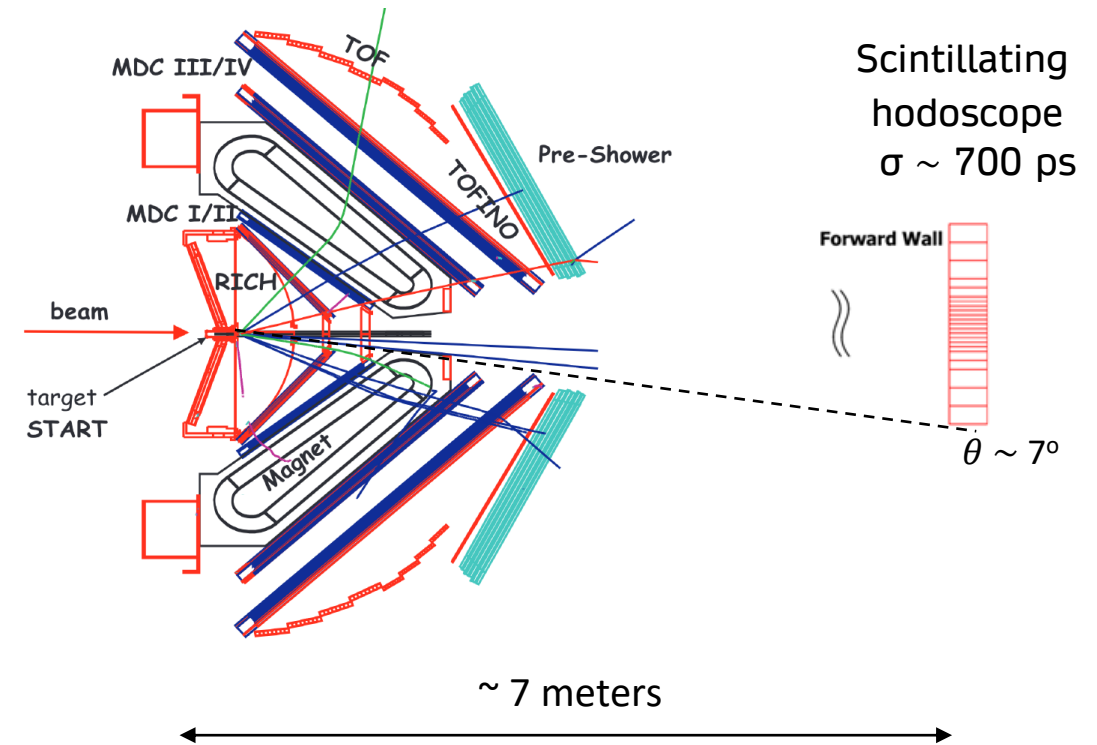
Investigation of the Σ^0 Production Mechanism in $p(3.5 \text{ GeV})+p$ collisions at HADES experiment

- Study of hyperon production serves as a tool to study QCD at the confinement scale
- Crucial for model calculations of heavy-ion collisions
- There are few measurements for Σ^0 compared to Λ hyperon production
- Focus on the **exclusive reaction**
 $p(3.5\text{GeV})+p \rightarrow p + K^+ + \Sigma^0$

$\Sigma^0 \rightarrow \Lambda \gamma$ (BR~100%) and $\Lambda \rightarrow p\pi^-$ (BR~64%)



High Acceptance Di-Electron Spectrometer HADES



Analysis strategy:

1. Signal Reconstruction

- Particle Identification (PID)
- Intermediate Λ reconstruction
- Kinematic Refit

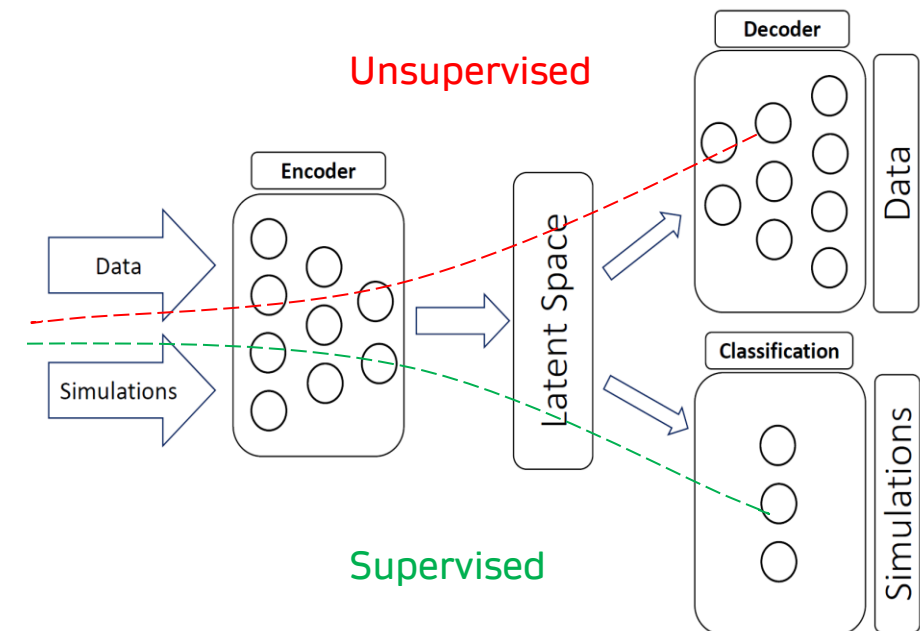
2. Physics of the Σ^0 hyperon production

- Study of final state particles in various reference frames
CMS, Gottfried-Jackson and helicity frames
- Partial Wave Analysis (PWA)

Investigation of the Σ^0 Production Mechanism in $p(3.5 \text{ GeV})+p$ collisions at HADES experiment

- Statement of the problem: identify the type of the charged tracks (p , K^+ , π^+)
- PID was performed based on **Deep Learning (DL)** techniques
- Potential solution is **semi-supervised** training on *simulations* and *data* using an **autoencoder**
- Training features: **momentum components, energy loss and time of flight.**
- Inspired by the **M2 model*** Dropout were used to quantify the **network uncertainty**[§]

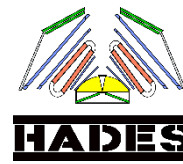
Particle	Accuracy %
p	98 %
K^+	76 %
π^+	92 %



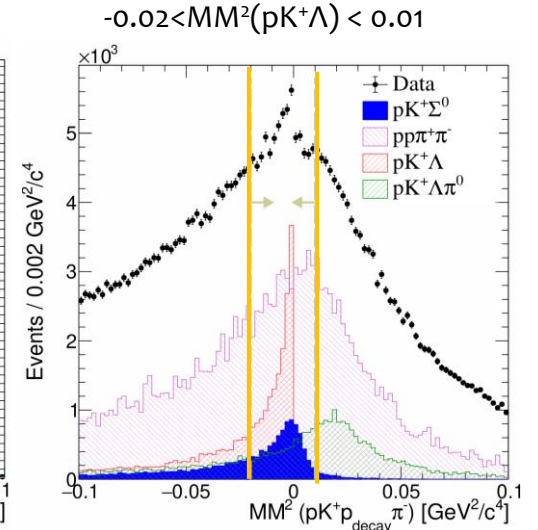
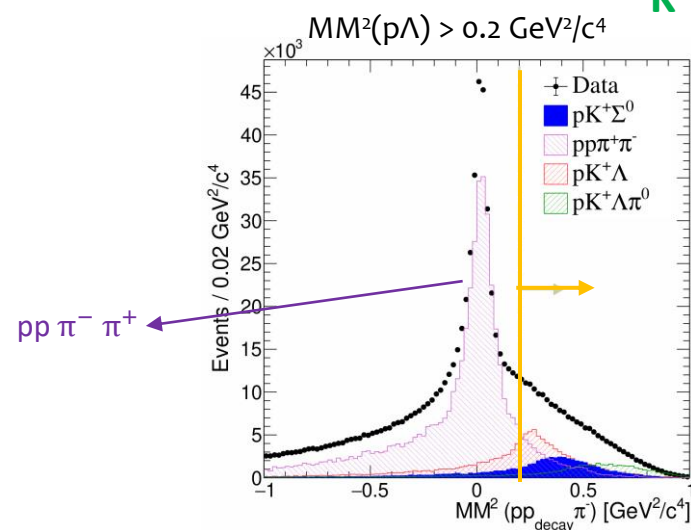
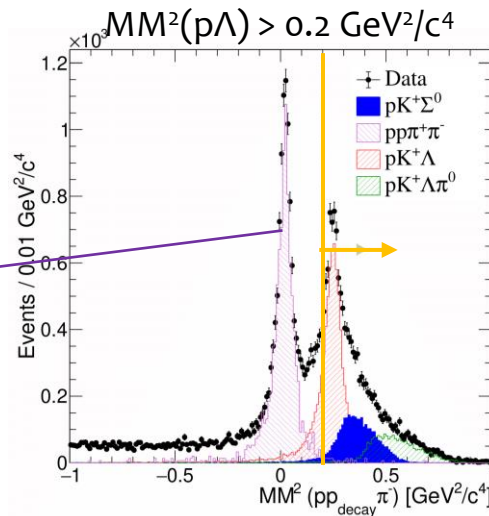
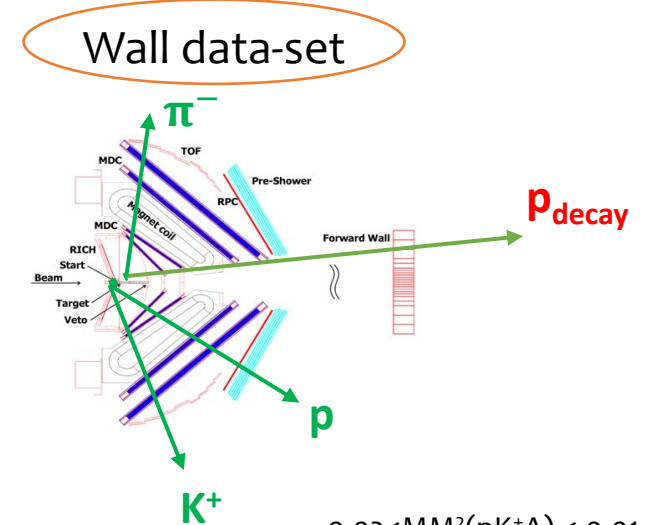
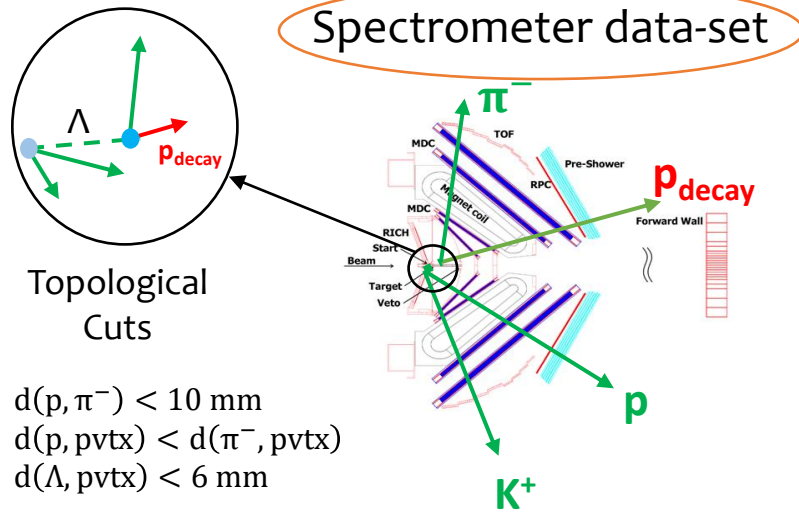
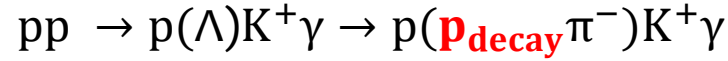
* Durk P Kingma et al. "Semi-supervised Learning with Deep Generative Models"

§ W. Esmail, Deep learning for track finding and the reconstruction of excited hyperons in proton induced reactions, PhD Thesis, 2021

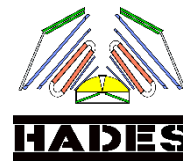
Λ Reconstruction



Investigation of the Σ^0 Production Mechanism in $p(3.5 \text{ GeV})+p$ collisions at HADES experiment

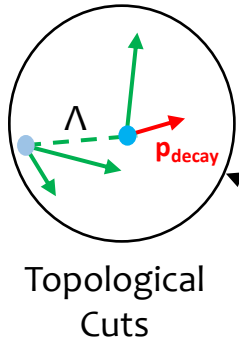


Λ Reconstruction

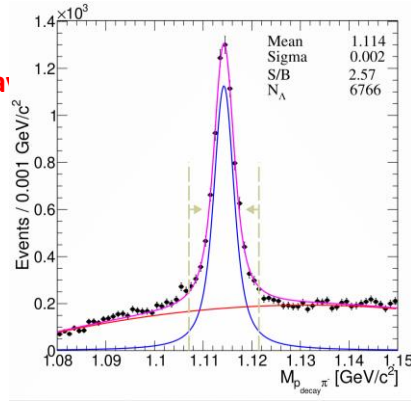
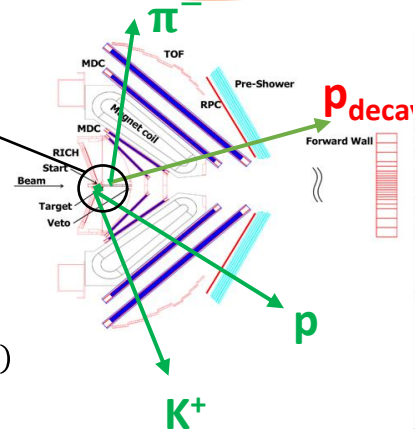


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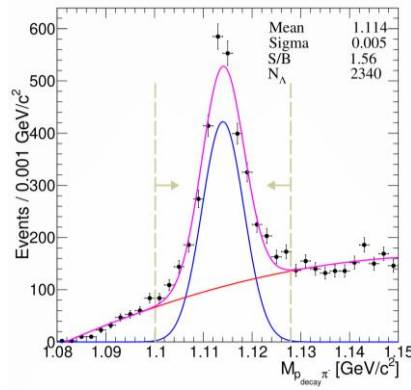
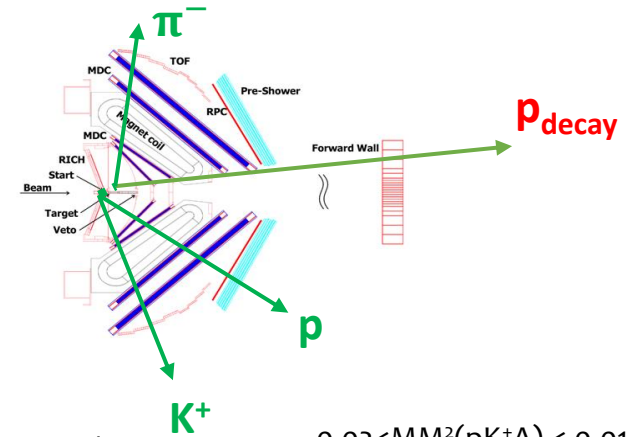
$$pp \rightarrow p(\Lambda)K^+\gamma \rightarrow p(\mathbf{p}_{\text{decay}}\pi^-)K^+\gamma$$



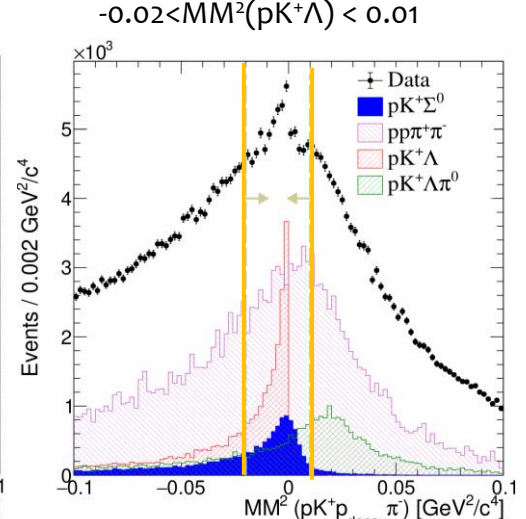
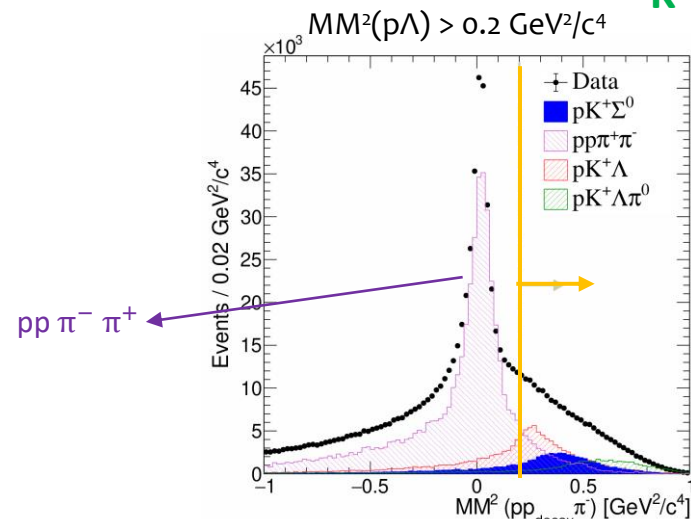
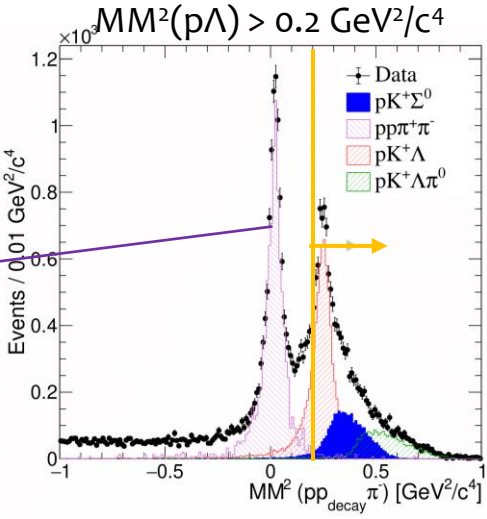
Spectrometer data-set



Wall data-set



- $d(p, \pi^-) < 10 \text{ mm}$
- $d(p, \text{pvtx}) < d(\pi^-, \text{pvtx})$
- $d(\Lambda, \text{pvtx}) < 6 \text{ mm}$



Investigation of the Σ^0 Production Mechanism in $p(3.5 \text{ GeV})+p$ collisions at HADES experiment

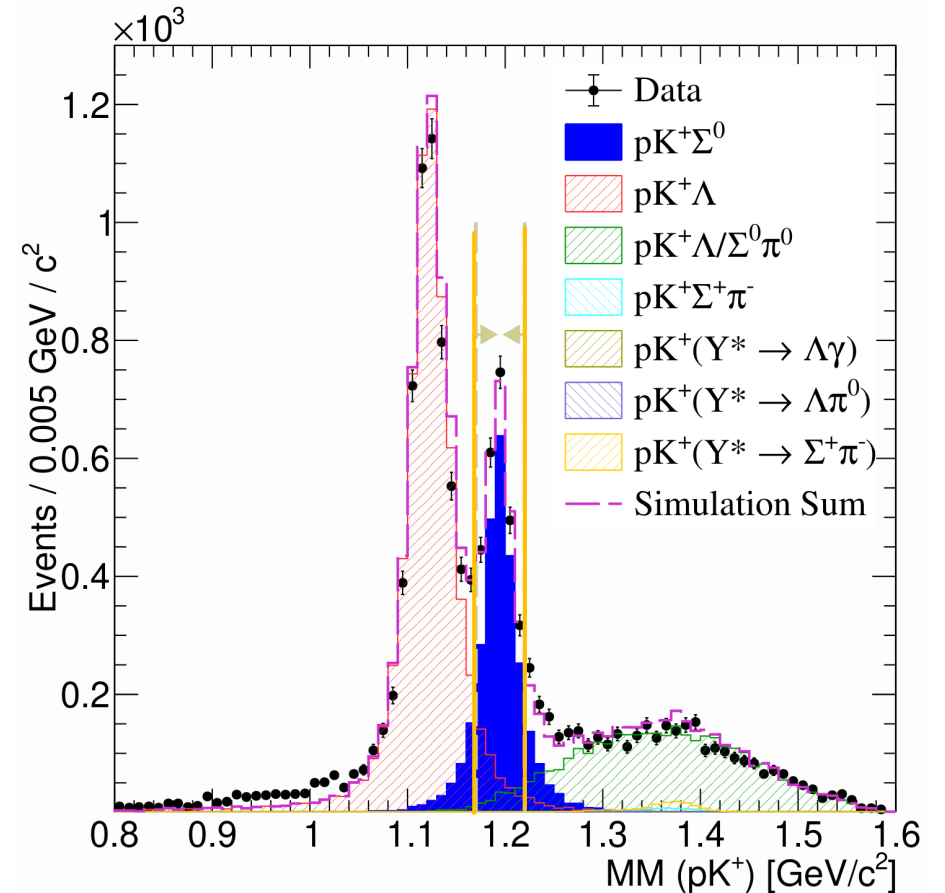
1. $pp \rightarrow pK^+ \Lambda \gamma \rightarrow pK^+ p\pi^- \gamma$
 2. $pp \rightarrow pK^+ \Lambda \gamma \rightarrow pK^+ p\pi^- \gamma$
- Events with $P(\chi^2) > 0.01$ were selected

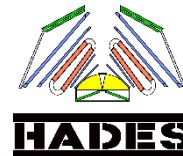
$$M_\Lambda = 1.115683 \text{ GeV}/c^2 \quad \chi^2 = (y - \eta)^T V^{-1} (y - \eta) \approx \text{minimum}$$

$$M_\gamma = 0 \text{ GeV}/c^2 \quad f(\eta, \xi) = 0$$

$$1.170 < MM(pK^+) [\text{GeV}/c^2] < 1.220$$

- 2613 Σ s: 58% HADES
42% Wall
- The signal purity $\sim 81\%$
- Background: $pK^+ \Lambda \sim 14\%$
 $pK^+ \Lambda \pi^0 \sim 5\%$





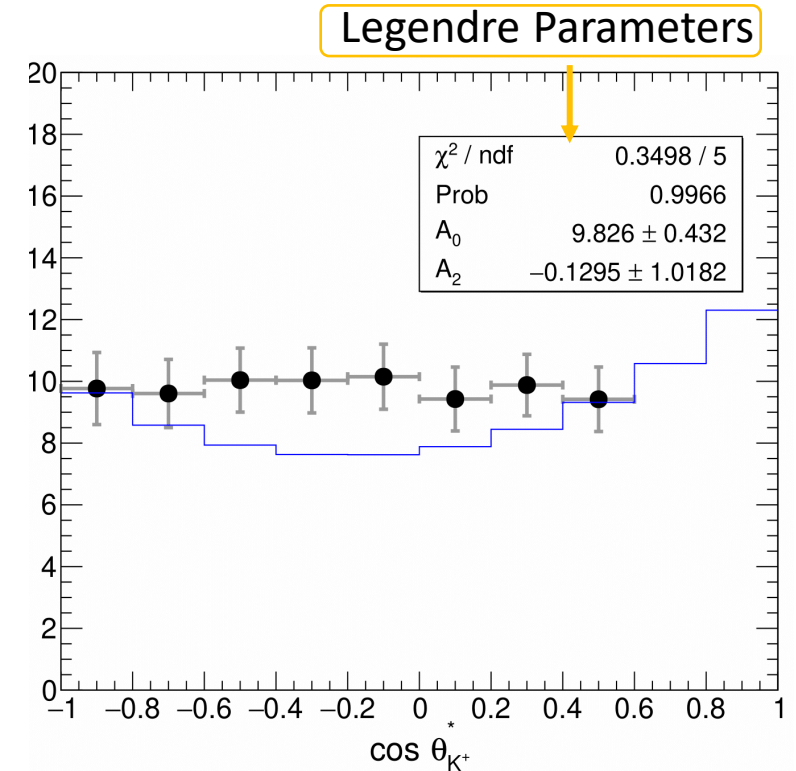
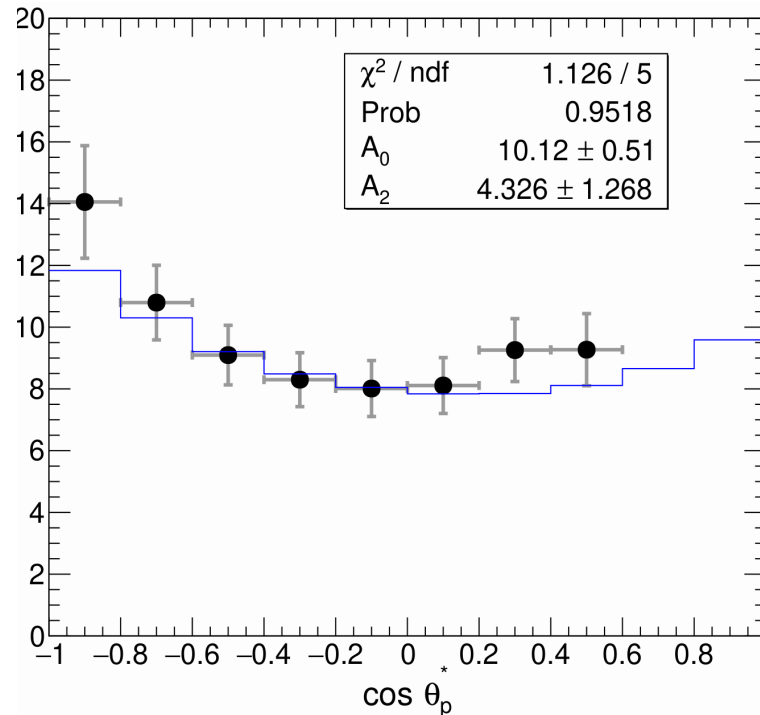
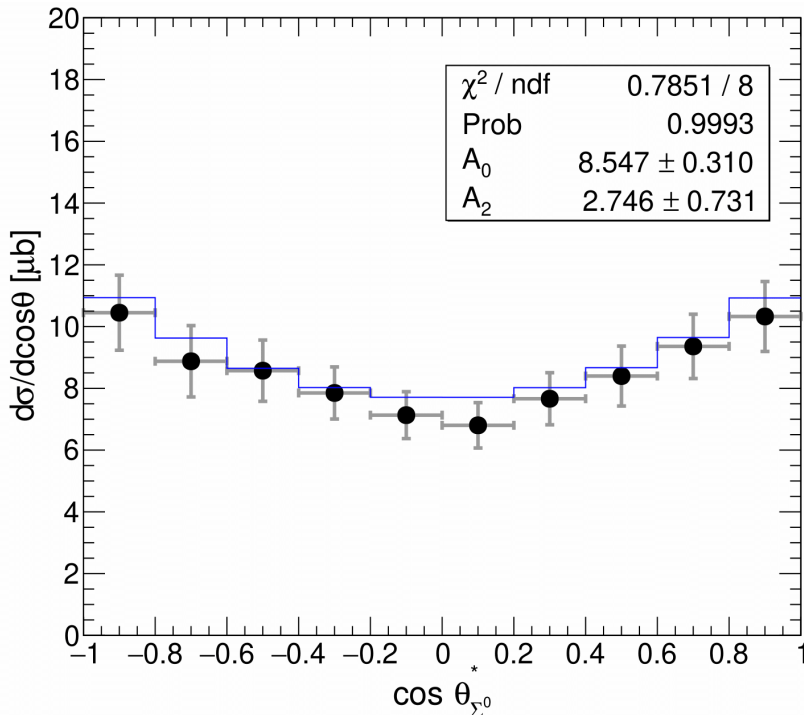
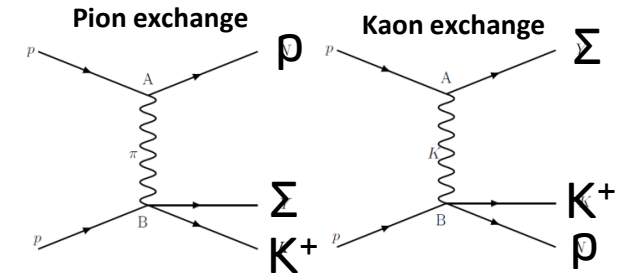
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Physics Results

Investigation of the Σ^0 Production Mechanism in $p(3.5 \text{ GeV})+p$ collisions at HADES experiment

Data were investigated in three reference frames $pK^+\Sigma^0$

- Center of Mass Frames \rightarrow exchange boson properties
- Gottfried-Jackson Frames \rightarrow exchange boson properties & intermediate resonances
- Helicity Frames \rightarrow "projection" of the Dalitz plot

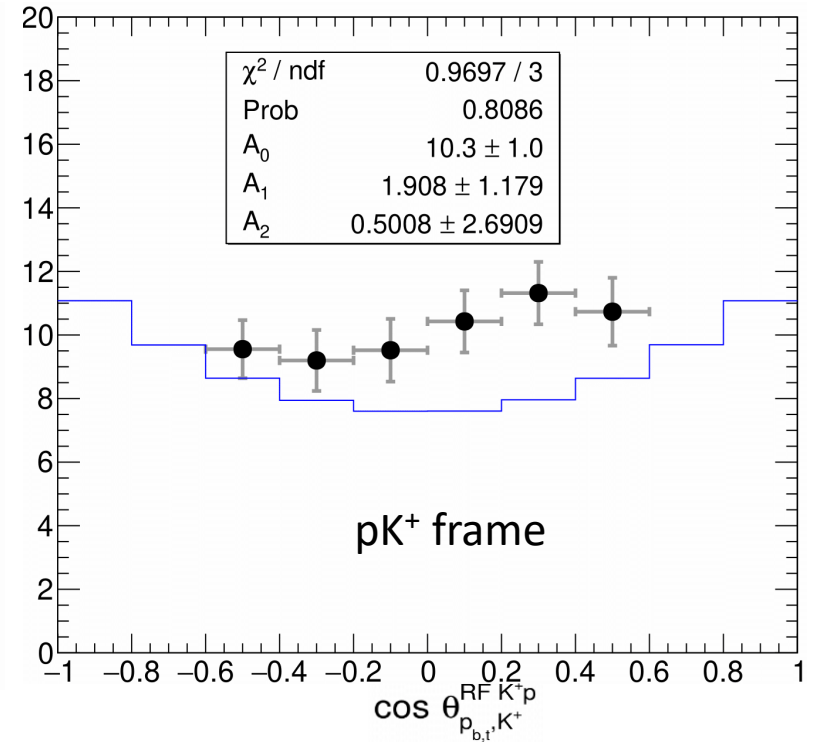
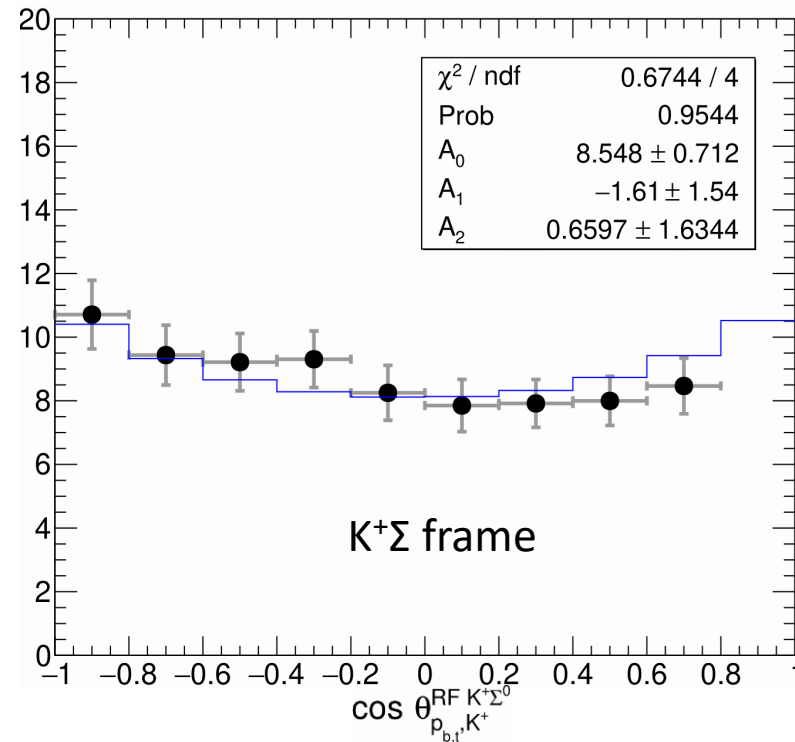
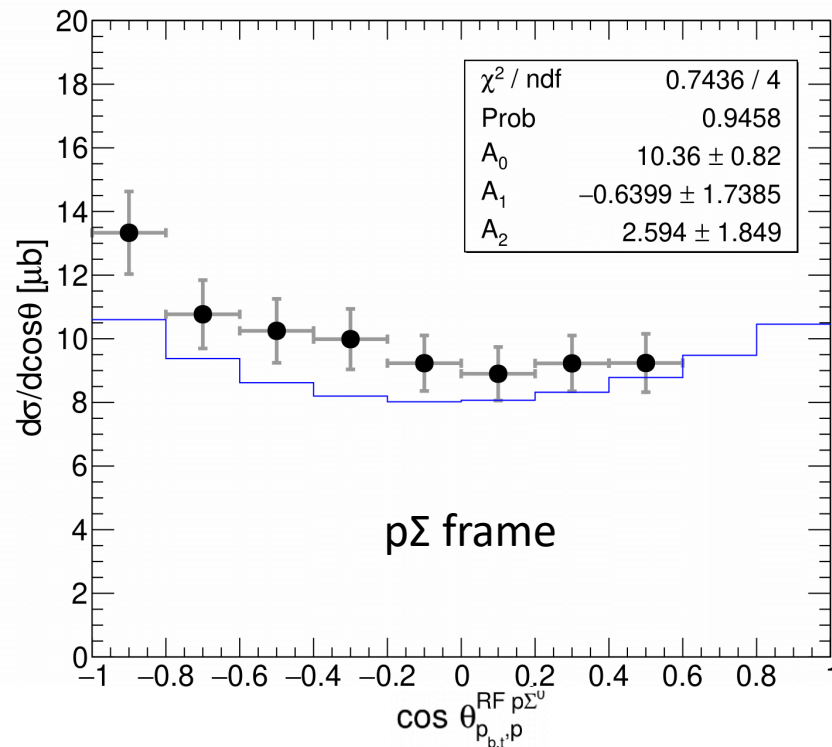
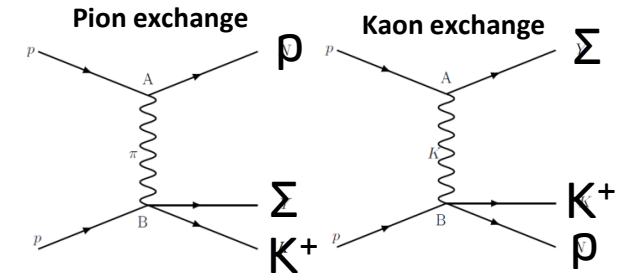


Legendre Parameters

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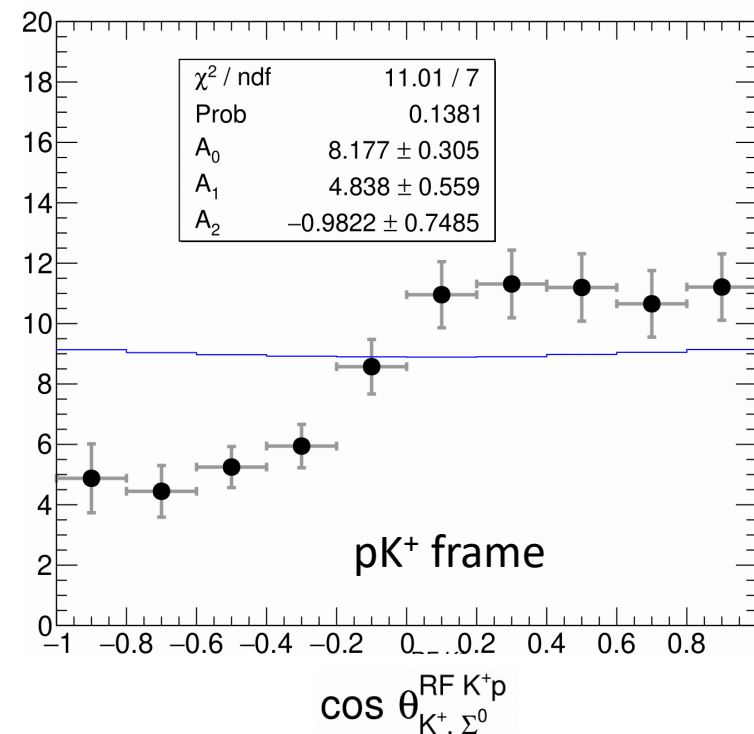
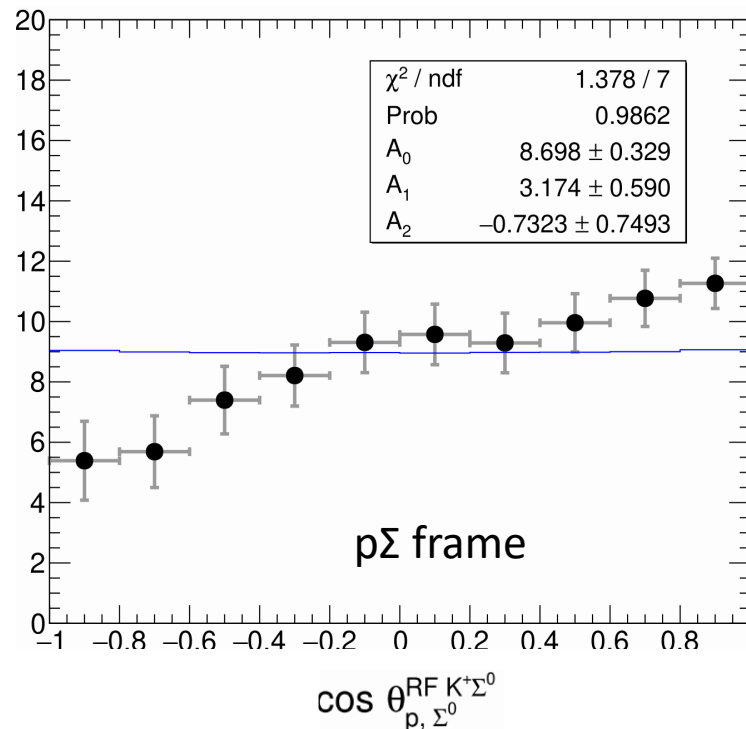
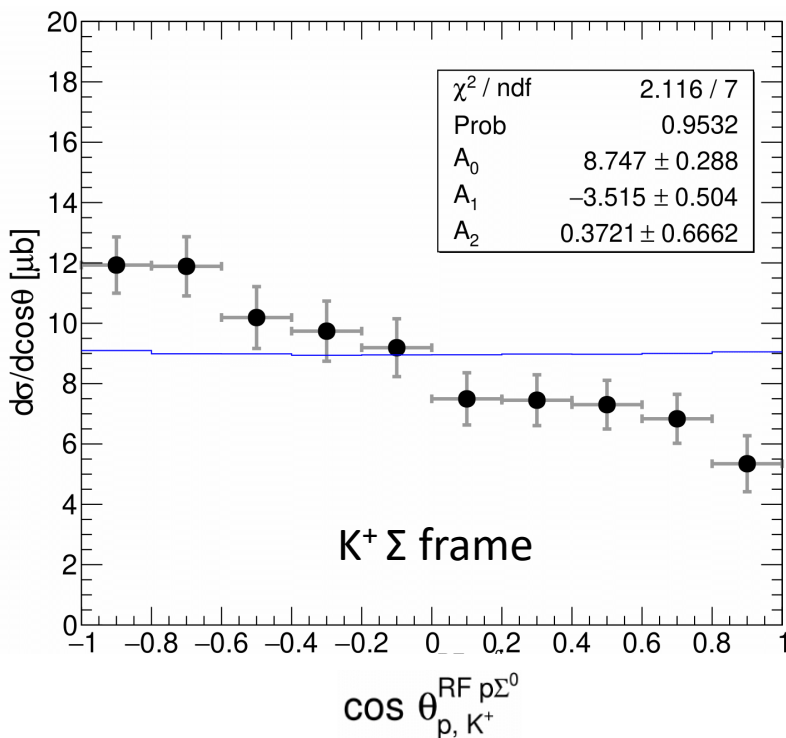
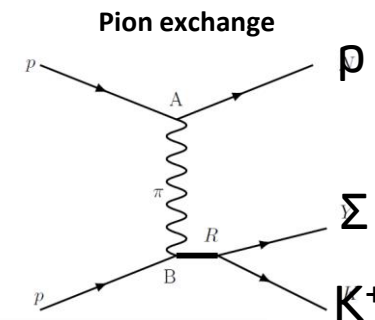
1. Center of Mass Frames \rightarrow exchange boson properties
2. Gottfried-Jackson Frames \rightarrow exchange boson properties & intermediate resonances
3. Helicity Frames \rightarrow "projection" of the Dalitz plot



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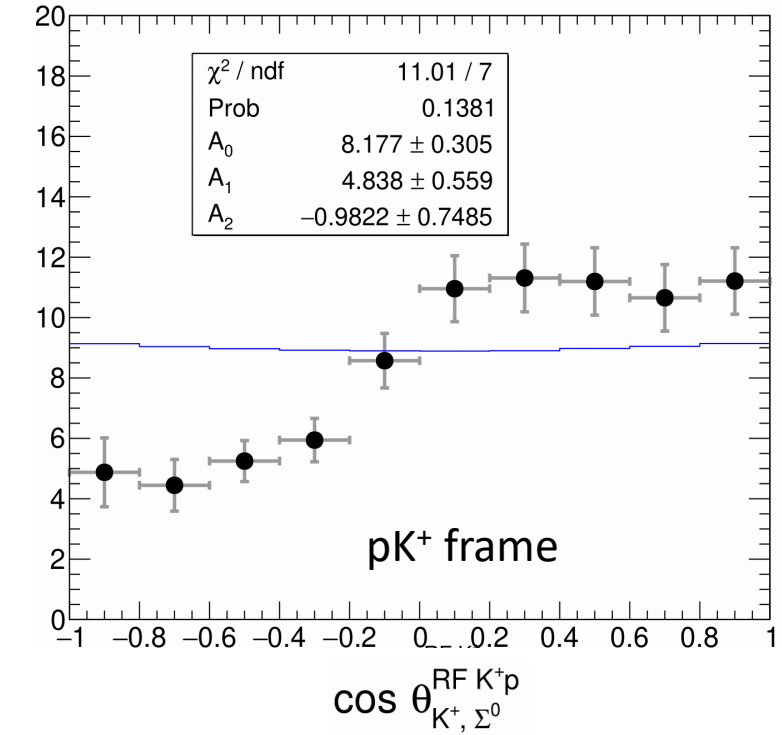
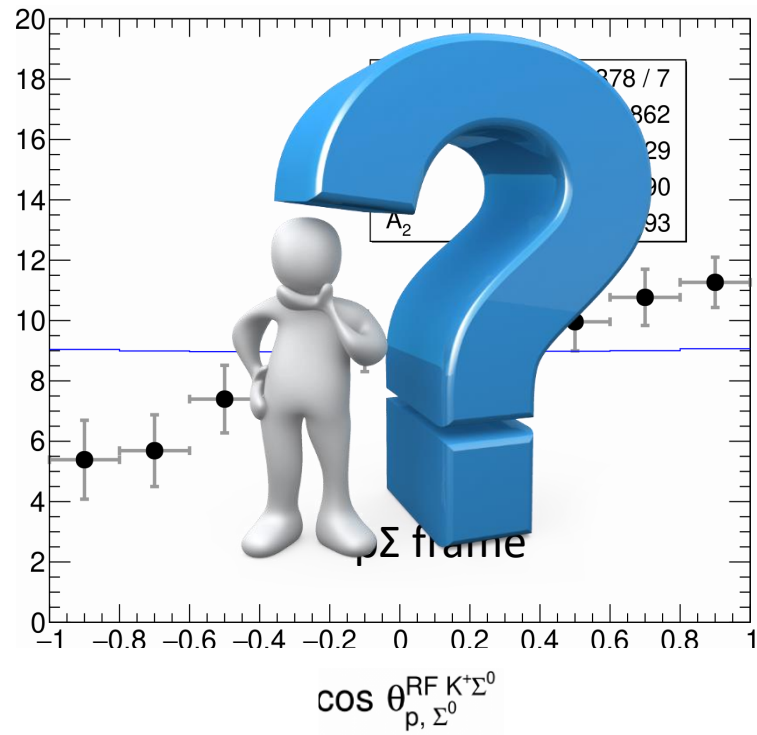
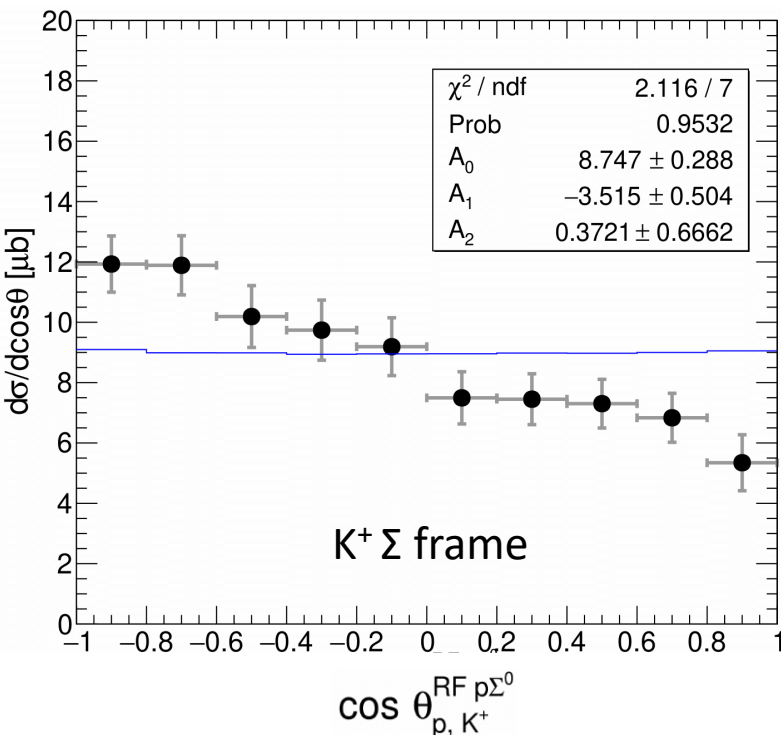
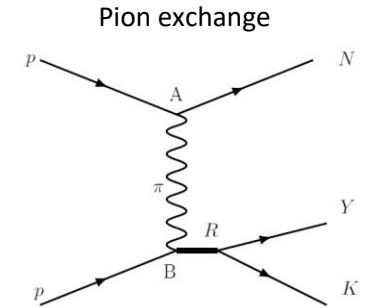
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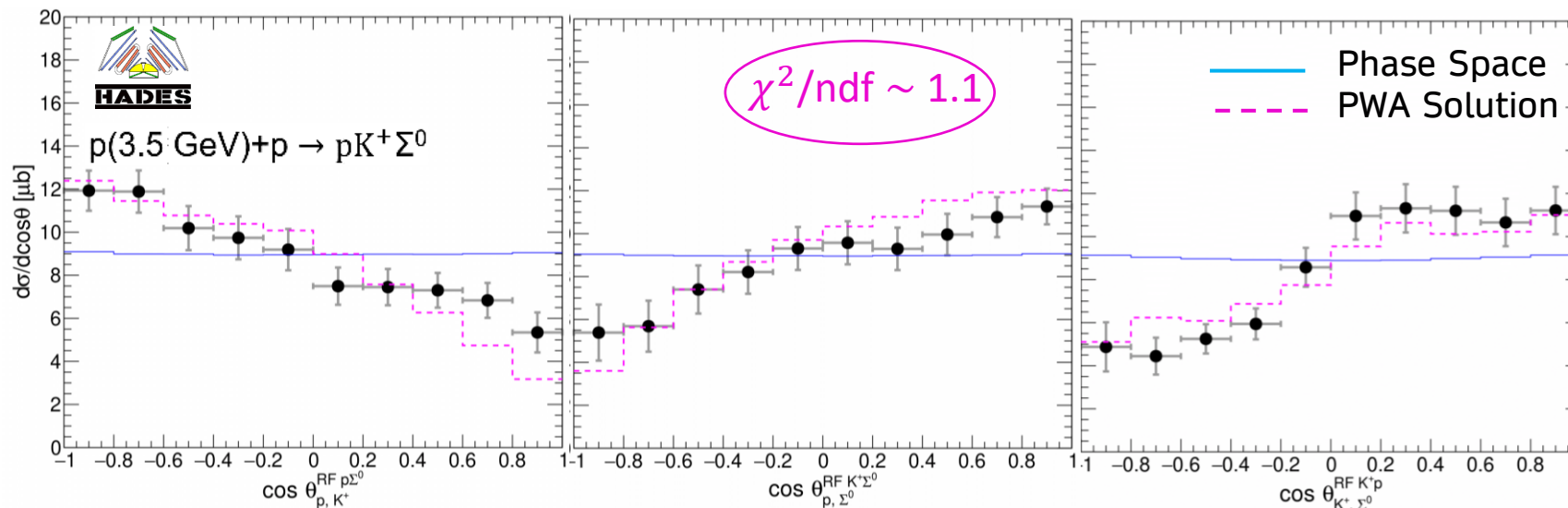
Investigation of the Σ^0 Production Mechanism in $p(3.5 \text{ GeV})+p$ collisions at HADES experiment

- **Partial Wave Analysis (PWA)** was performed in order to estimate resonant contributions
- PWA aims to determine the transition amplitude
- Tool used: **Bonn-Gatchina PWA** (log-likelihood minimization)

Helicity Frames Revisited: PWA solution provides a good description of angular distributions

- Nucleon resonances involved are:

$N^*(1710)$ ($J^P = 1/2^+$), $N^*(1900)$ ($J^P = 3/2^+$) and $\Delta^*(1900)$ ($J^P = 1/2^-$)



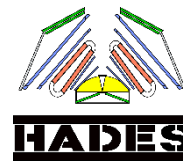
➤ Eight resonances:

$N^*(1710)$, $N^*(1875)$, $N^*(1880)$, $N^*(1895)$, $N^*(1900)$, $\Delta^*(1900)$, $\Delta^*(1910)$ and $\Delta^*(1920)$

➤ Eight non-resonant contributions:

1S_0 , 3P_0 , 3P_1 , 3P_2 , 1D_2 , 3F_2 , 3F_3 and 3F_4

Production Cross Section



Investigation of the Σ^0 Production Mechanism in $p(3.5 \text{ GeV})+p$ collisions at HADES experiment

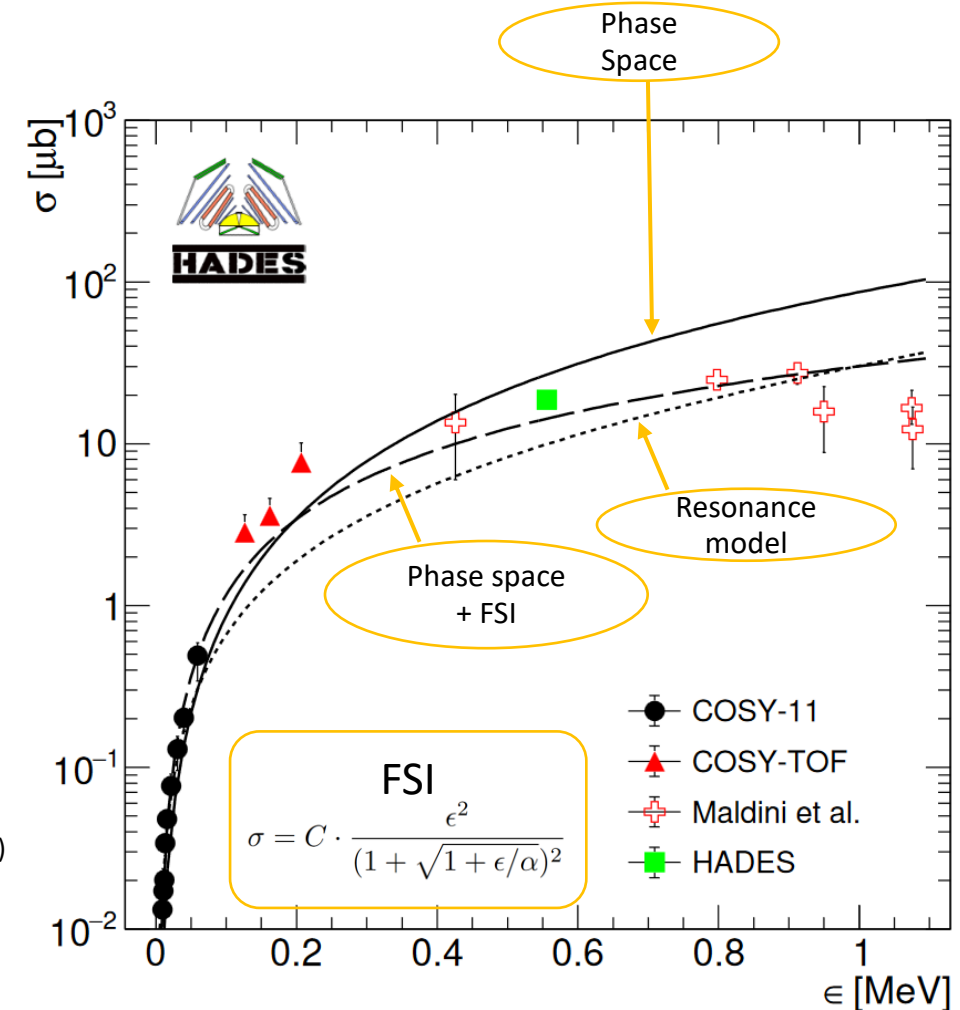
- The cross section is obtained by integrating the yield of the angular distributions

$$\sigma(pK^+\Sigma^0)[\mu b] = 18.74 \pm 1.01(\text{stat}) \pm 1.71(\text{syst})$$

$$\sigma(pK^+\Lambda)/\sigma(pK^+\Sigma^0) = 1.90 \pm 0.41$$

- Systematic error sources:

1. PID: $\pm 5\%$ error
2. Analysis Cuts: $\pm 2\%$ error
3. Normalization: $\pm 7\%$ error

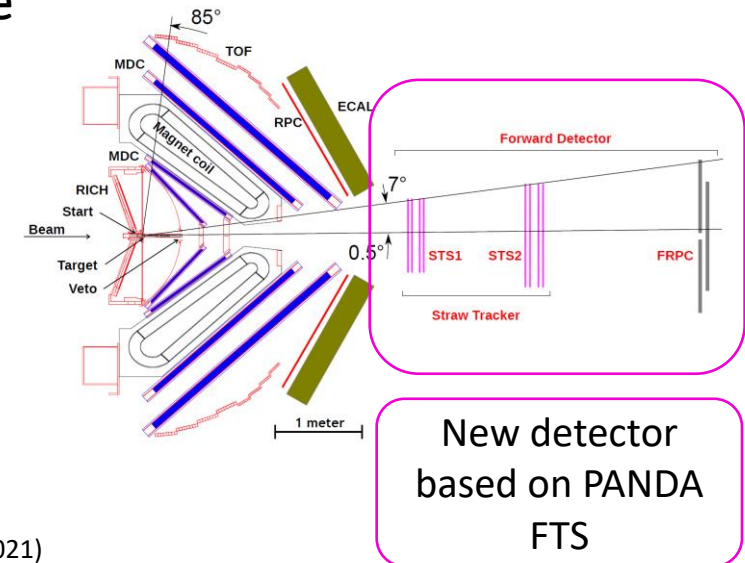


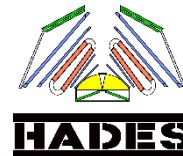
- Resonance model study of kaon production in baryon-baryon reactions for heavy-ion collisions, K. Tsushima, **Phys. Rev. C** 59 (1999)
- Comparison of the near-threshold production of η - and K -mesons in proton-proton collisions, G. Fäldt *Zeitschrift für Physik A Hadrons and Nuclei* 357, (1997)
- **Partial Wave Analysis of the Reaction $p(3.5\text{GeV}) + p \rightarrow pK^+\Lambda$ to Search for the " ppK^- " Bound State**
HADES Collaboration *Phys.Lett.B* 742 (2015)

Investigation of the Σ^0 Production Mechanism in $p(3.5 \text{ GeV})+p$ collisions at HADES experiment

- Investigation of the Σ^0 production mechanism in $p(3.5\text{GeV})+p$ collisions
- Phase space description is not sufficient
- Dominance of pion exchange mechanism
- Resonances with mass around **1.710** GeV/c^2 and **1.900** GeV/c^2 are preferred by the PWA fit
- Due to limited statistics, there is a significant uncertainty to the relative contributions of the different resonances

- **Upgraded HADES setup (Recent data $p(4.5\text{GeV})+p$)**





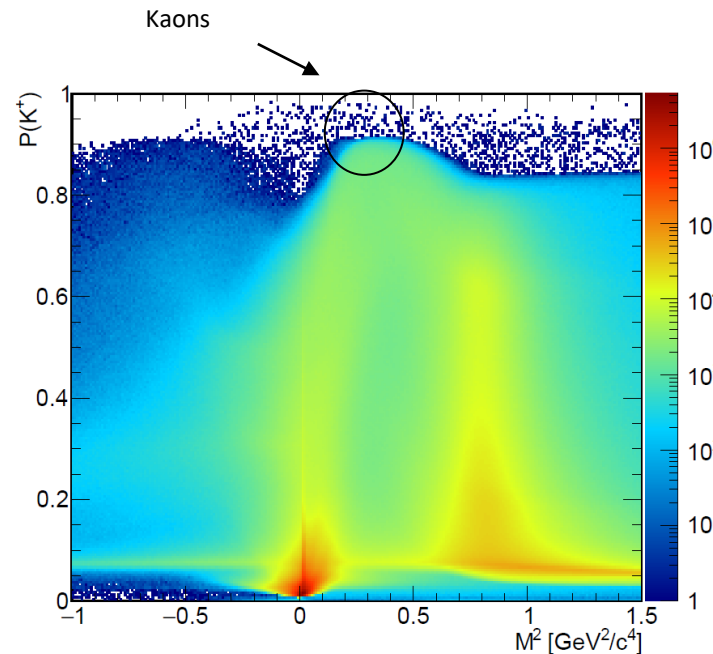
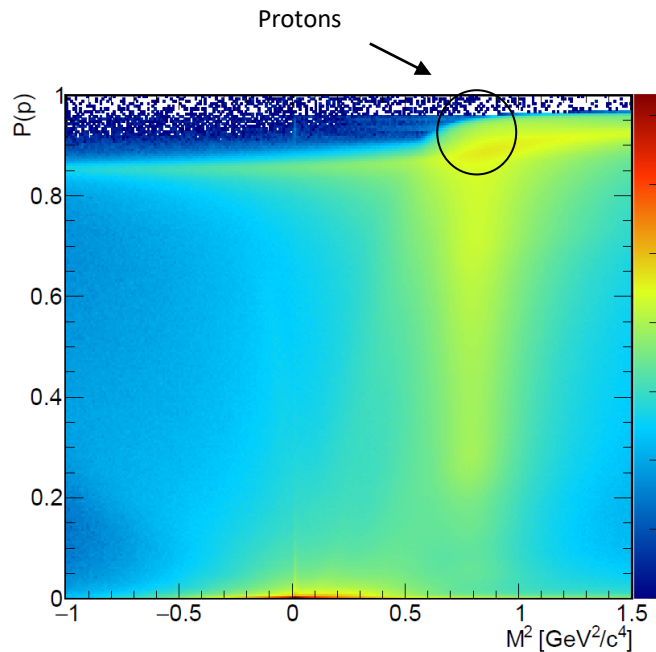
Investigation of the Σ^0 Production Mechanism in $p(3.5 \text{ GeV})+p$ collisions at HADES experiment

Thank You

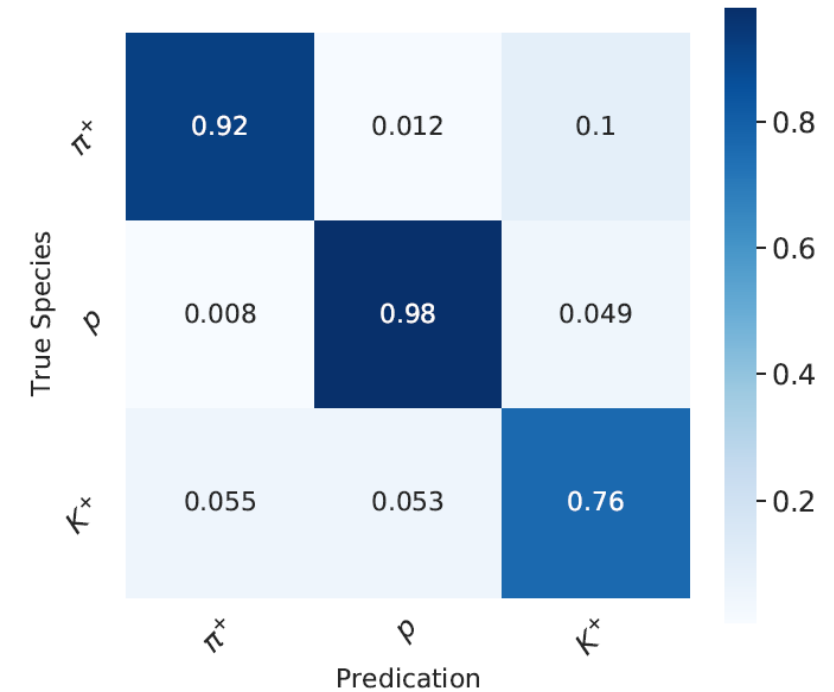
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- Training Features: $p_i(\text{GeV}/c)$, $dE/dx(\text{a.u.})$, $\text{TOF}(\text{ns})$, $d_{\text{META}}(\text{m})$

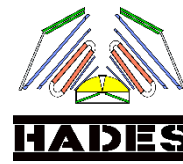
Performance evaluated on real data



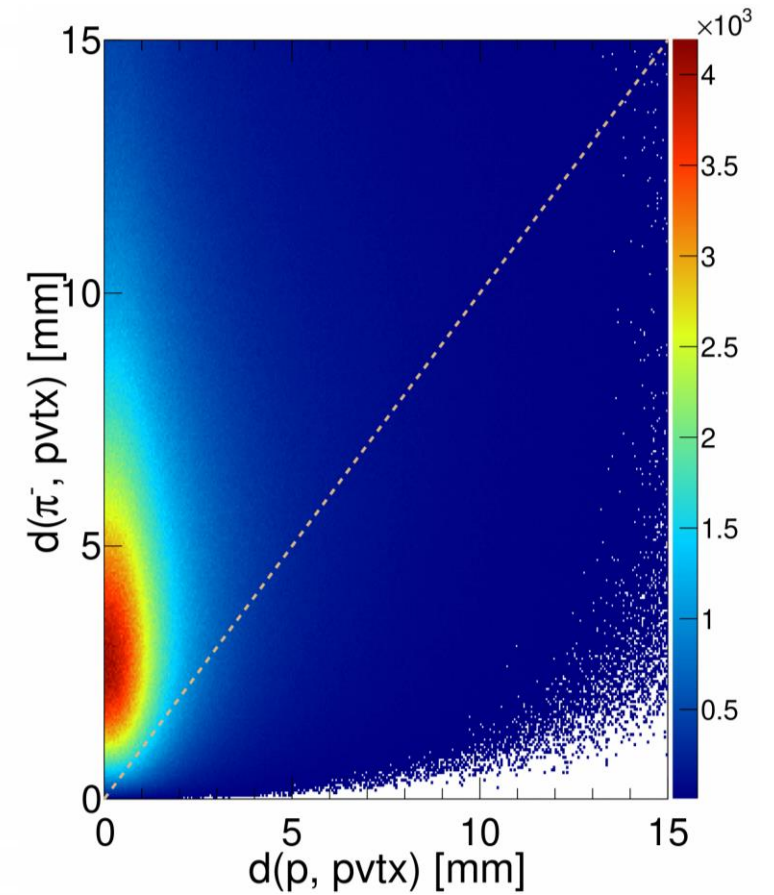
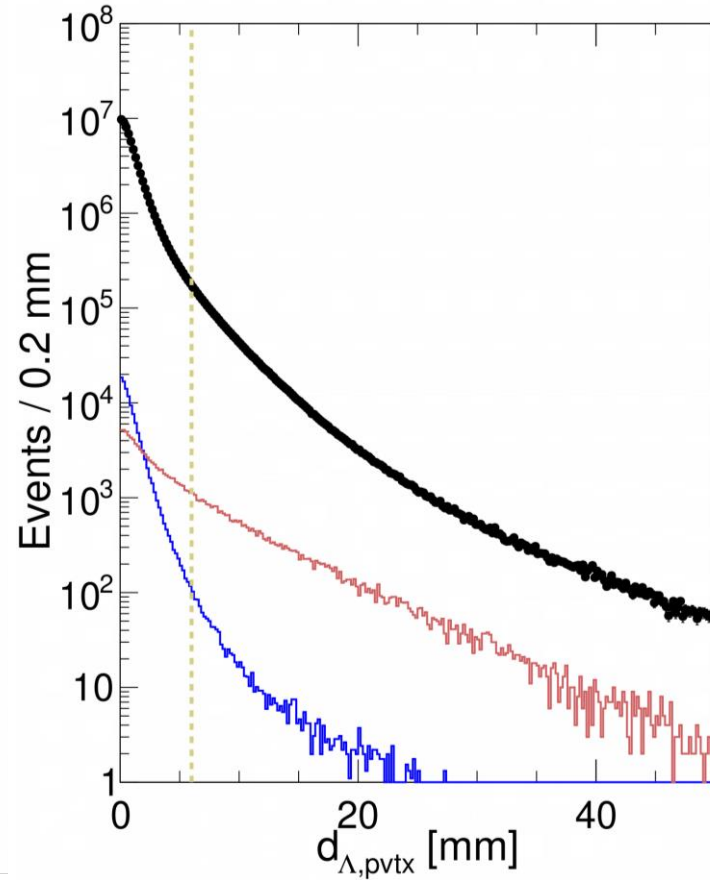
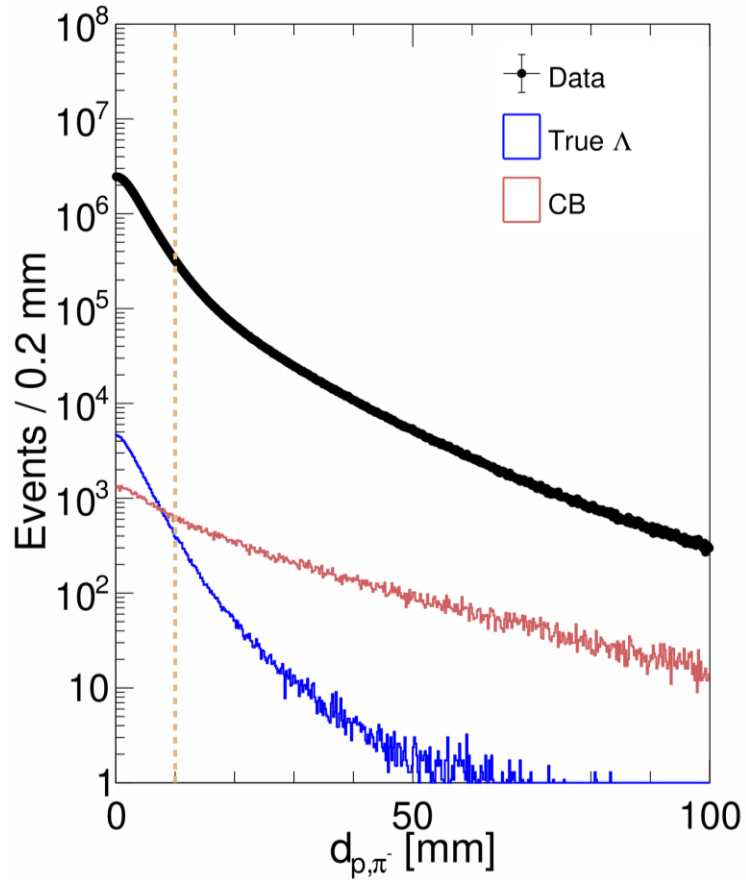
Confusion Matrix (Simulations)



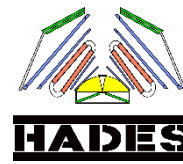
Backups: Lambda Selection



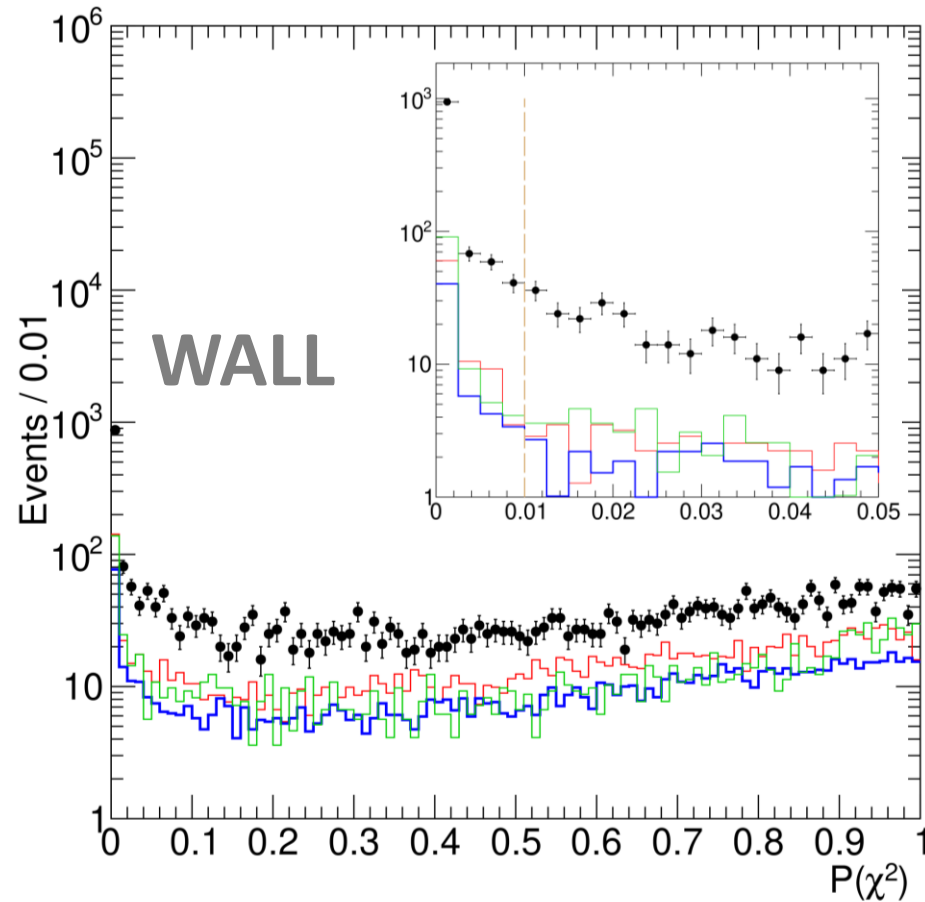
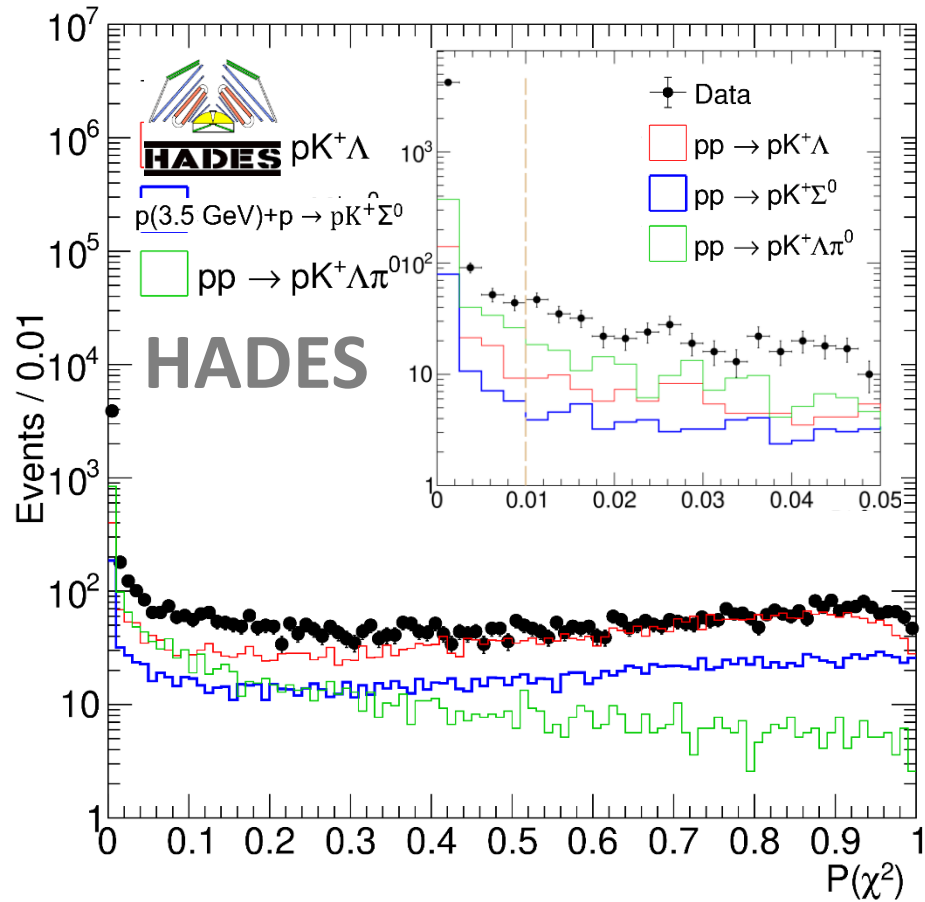
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Backups: Kinematic Refit



Investigation of the Σ^0 Production Mechanism in $p(3.5 \text{ GeV})+p$ collisions at HADES experiment



Investigation of the Σ^0 Production Mechanism in $p(3.5 \text{ GeV})+p$ collisions at HADES experiment

1. Center of Mass CMS Frame:

- The beam and target proton have identical momenta in opposite directions

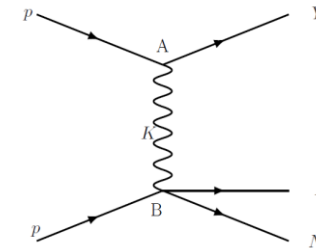
2. Gottfried Jackson G-F Frame:

- is the polar angle between the final state particle B and the initial proton as measured in the rest frame of particles A and B

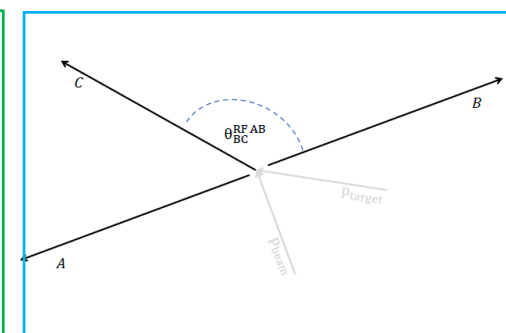
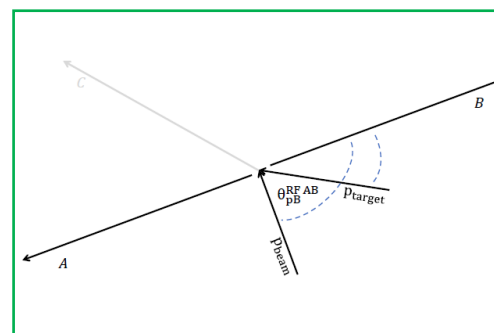
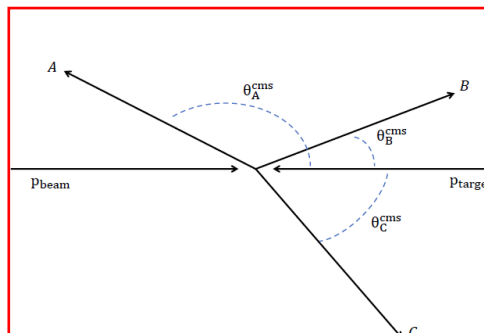
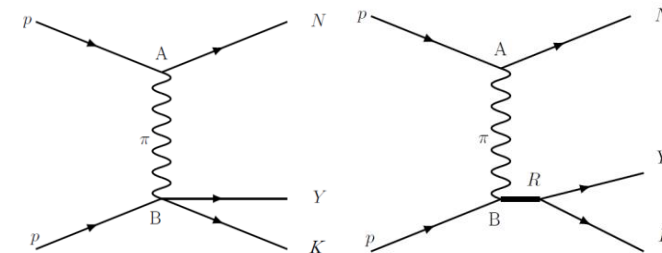
3. Helicity Frame:

- Defined similar to the G-F angle, but the angle with respect to the third produced particle is used

Kaon exchange



Pion exchange



Investigation of the Σ^0 Production Mechanism in $p(3.5 \text{ GeV})+p$ collisions at HADES experiment

- Experimental distributions are represented by binned histograms

$$M = RT$$

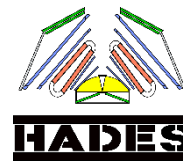
- **R** is the **detector response** and **T** is the **true distribution**
- **R** now is represented as a *matrix*

$$R_{ij} = P(\text{reconstructed in bin } i \mid \text{generated in bin } j)$$

- **Correction** or data unfolding means to **invert** the **response matrix**
- **Inversion** is done via the Singular Value Decomposition **SVD** implemented using **RooUnfold framework**
- Since there are background events, a **purity matrix** is defined as

$$P_{bin} = \frac{n(pK^+\Sigma^0)}{n(pK^+\Lambda) + n(pK^+\Sigma^0) + n(pK^+\Lambda\pi^0)}$$

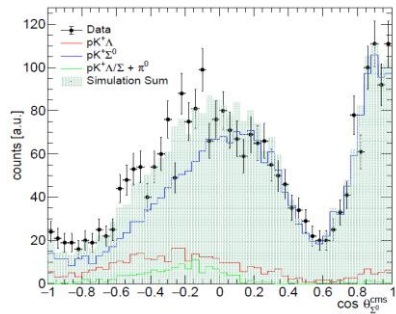
Backups: Efficiency Corrections



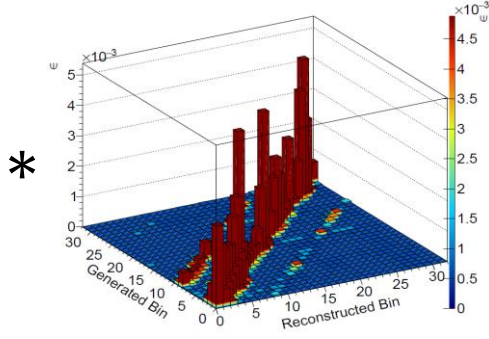
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- Example: Correction of the Σ^0 CMS angular distribution
- 2D correction in $\cos\theta_{\Sigma^0}^{\text{cms}}$ and $p_{\Sigma^0}^{\text{cms}}$
- The corrected number of Σ^0 events are transformed into a cross section by normalizing to elastic collisions at the same beam energy

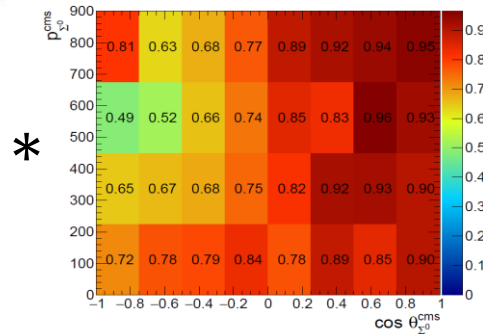
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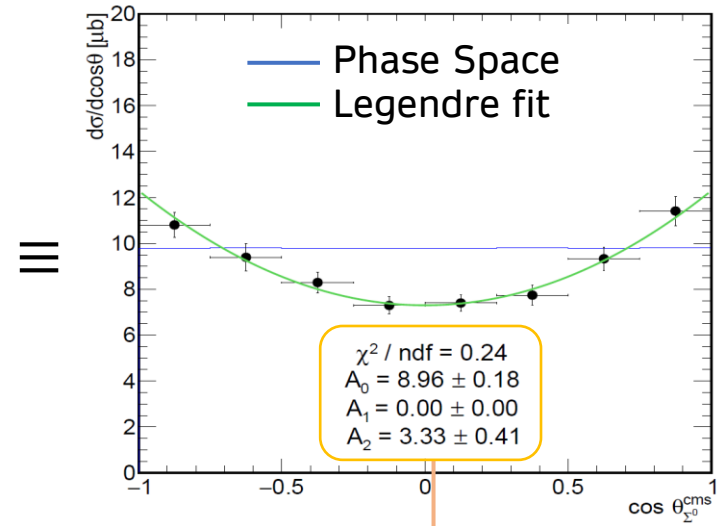
The measured distribution
M



Inverse of the response matrix
R⁻¹



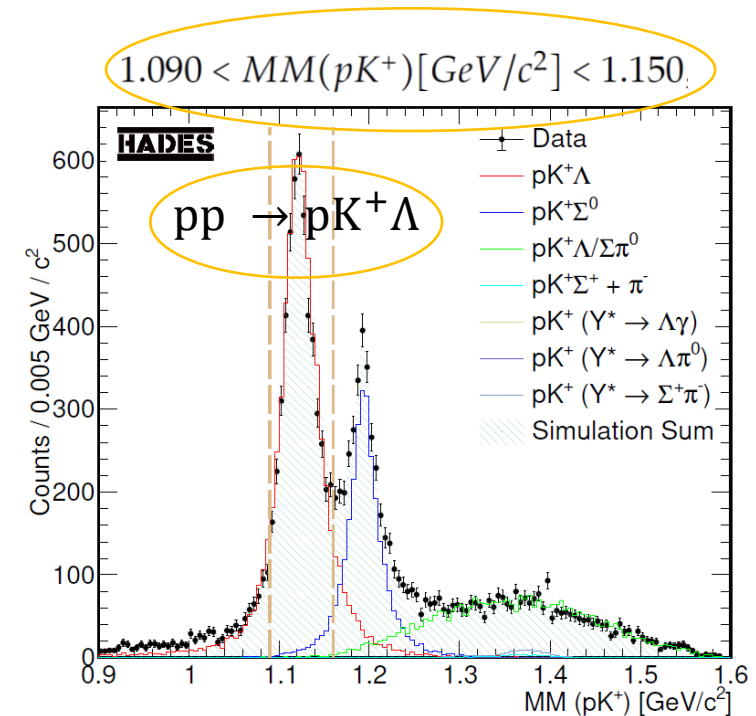
Purity matrix
P



Legendre Parameters

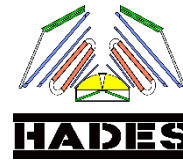
Investigation of the Σ^0 Production Mechanism in $p(3.5 \text{ GeV})+p$ collisions at HADES experiment

- **Partial Wave Analysis (PWA)** was performed in order to estimate resonant contributions
- PWA aims to determine the transition amplitude $A_{tr}^\alpha(s) = (\alpha_1 + \alpha_3\sqrt{s})e^{i\alpha_2}$
- Tool used: Bonn-Gatchina PWA (log-likelihood minimization)
- Eight **resonances** + eight **non-resonant** contributions ($^1S_0, ^3P_0, ^3P_1, ^3P_2, ^1D_2, ^3F_2, ^3F_3$ and 3F_4)
- Resonance masses and widths were fixed to the PDG values
- PWA is first applied to **pp** \rightarrow **pK⁺ Λ**
- Solution No. 8/1 from * including :
(N*(1650), N*(1710), N*(1720) and N*(1900))
- An estimate of **pp** \rightarrow **pK⁺ Λ** within the signal region is \sim **290** events



* Partial Wave Analysis of the Reaction $p(3.5 \text{ GeV}) + p \rightarrow pK^+\Lambda$ to Search for the " ppK^- " Bound State
HADES Collaboration *Phys.Lett.B* 742 (2015)

Backups: Partial Wave Analysis

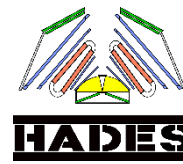


Investigation of the Σ^0 Production Mechanism in $p(3.5 \text{ GeV})+p$ collisions at HADES experiment

Resonance	Mass [GeV/c ²]	Width [GeV/c ²]	J ^P
N*(1710)	1.710	0.140	$\frac{1}{2}^+$
N*(1875)	1.875	0.200	$\frac{3}{2}^-$
N*(1880)	1.880	0.300	$\frac{1}{2}^+$
N*(1895)	1.895	0.120	$\frac{1}{2}^-$
N*(1900)	1.920	0.200	$\frac{3}{2}^+$
$\Delta^*(1900)$	1.860	0.250	$\frac{1}{2}^-$
$\Delta^*(1910)$	1.900	0.300	$\frac{1}{2}^+$
$\Delta^*(1920)$	1.920	0.300	$\frac{3}{2}^+$

Solution No.	Initial State	Partial Wave Contributions	\mathcal{L}
1	$^1S_0, ^1D_2, ^3P_0, ^3P_1, ^3P_2, ^3F_2$	$pK^+\Sigma^0 \approx 41\%$ $N^*(1710) \approx 23\%$ $N^*(1900) \approx 17\%$ $\Delta^*(1900) \approx 19\%$	-333
2	$^1S_0, ^1D_2$	$pK^+\Sigma^0 \approx 27\%$ $N^*(1710) \approx 22\%$ $N^*(1900) \approx 9\%$ $\Delta^*(1900) \approx 42\%$	-184
3	$^1S_0, ^1D_2, ^3P_0, ^3P_1, ^3P_2$	$pK^+\Sigma^0 \approx 63\%$ $N^*(1710) \approx 18\%$ $N^*(1900) \approx 18\%$ $\Delta^*(1900) \approx 2\%$	-182
4	$^1S_0, ^1D_2, ^3P_0, ^3P_1, ^3P_2, ^3F_2$	$pK^+\Sigma^0 \approx 33\%$ $N^*(1710) \approx 27\%$ $N^*(1880) \approx 40\%$	-151
5	1S_0	$pK^+\Sigma^0 \approx 17\%$ $N^*(1710) \approx 79\%$ $\Delta^*(1900) \approx 5\%$	-123

Backups: Treiman-Yang Angle



Investigation of the Σ^0 Production Mechanism in $p(3.5 \text{ GeV})+p$ collisions at HADES experiment

For a **pure pion exchange**
the Treiman-Yang angle measured in the
 $K^+\Sigma^0$ rest frame
is expected to be an **isotropic distribution**

