

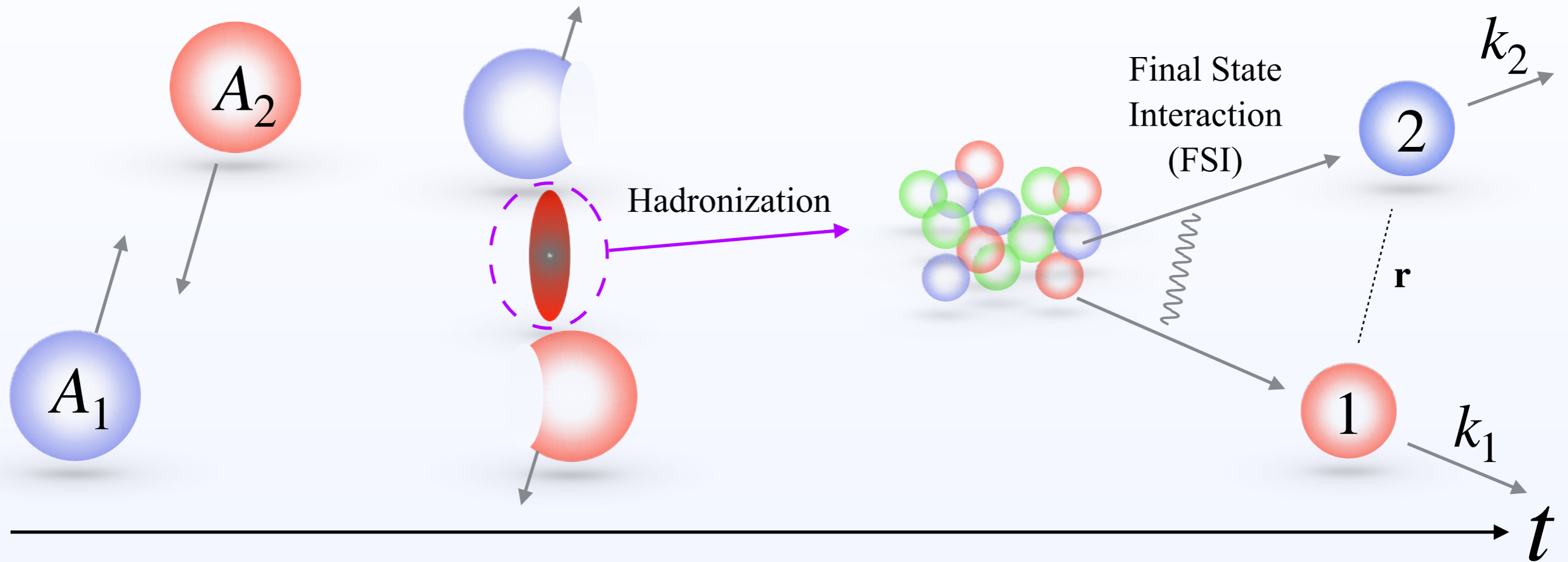
Yuki Kamiya
HISKP, Bonn Univ.

Study on hadron-hadron interaction with femtoscopic technique

14th International Conference on Hypernuclear
and Strange Particle Physics (HYP2022)
@ Prague, Czech Republic, 2022/6/29

Hadron correlation in high energy nuclear collision

- High energy nuclear collision and FSI



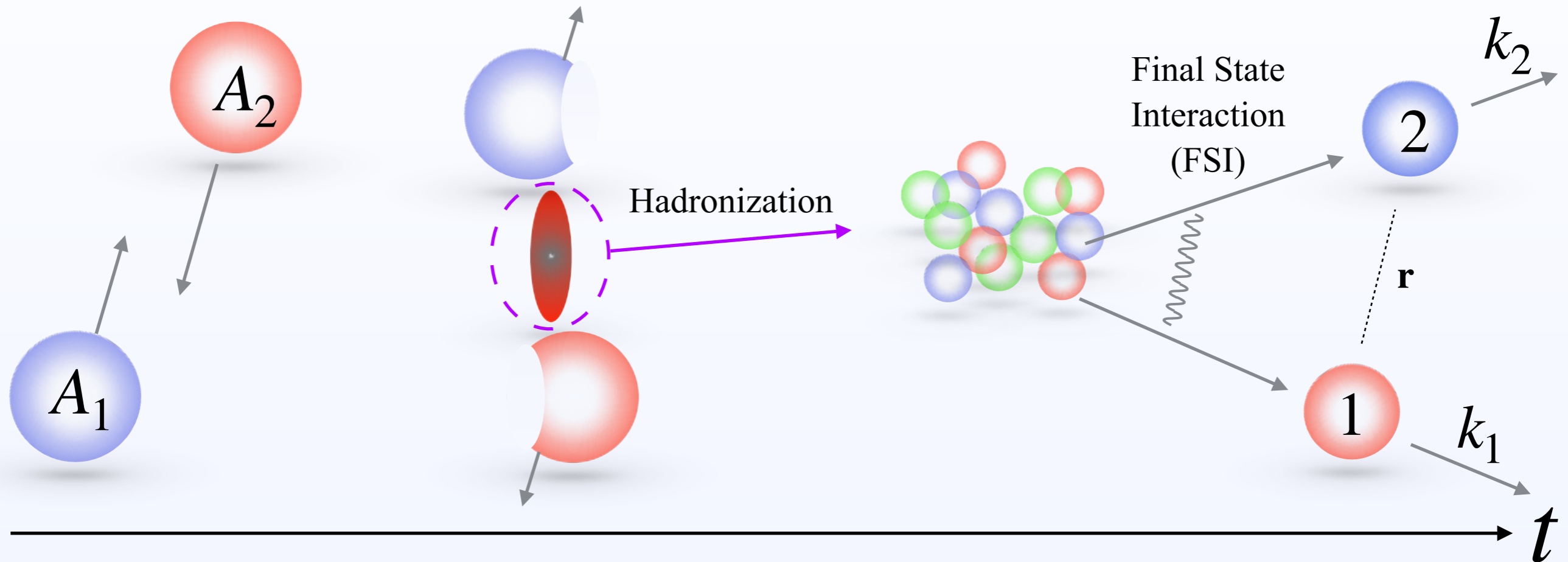
- Hadron-hadron correlation

$$C_{12}(k_1, k_2) = \frac{N_{12}(k_1, k_2)}{N_1(k_1)N_2(k_2)}$$

$$= \begin{cases} 1 & \text{(w/o correlation)} \\ \text{Others (w/ correlation)} \end{cases}$$

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- Hadron-hadron correlation

- Koonin-Pratt formula : S.E. Koonin, PLB 70 (1977)
S. Pratt et. al. PRC 42 (1990)

$$C(\mathbf{q}) \simeq \int d^3\mathbf{r} S(\mathbf{r}) |\varphi^{(-)}(\mathbf{q}, \mathbf{r})|^2$$

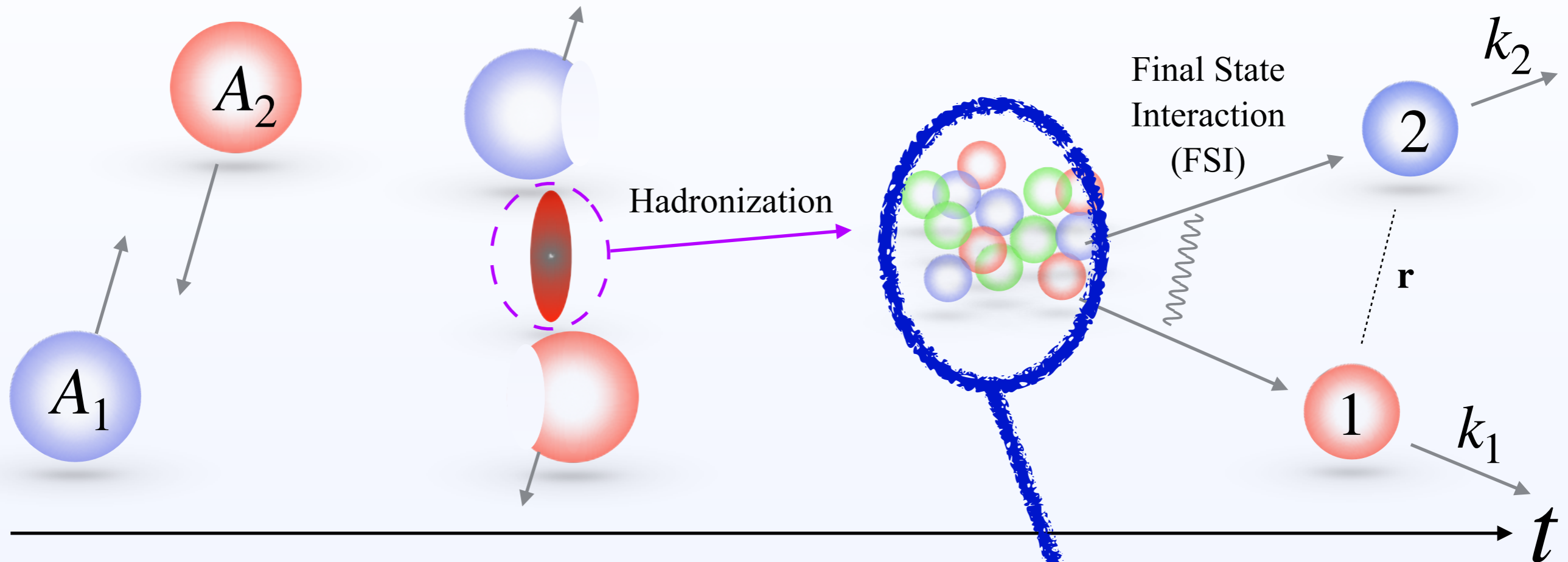
$$\mathbf{q} = (m_2\mathbf{k}_1 - m_1\mathbf{k}_2)/(m_1 + m_2)$$

$S(\mathbf{r})$: Source function

$\varphi^{(-)}(\mathbf{q}, \mathbf{r})$: Relative wave function

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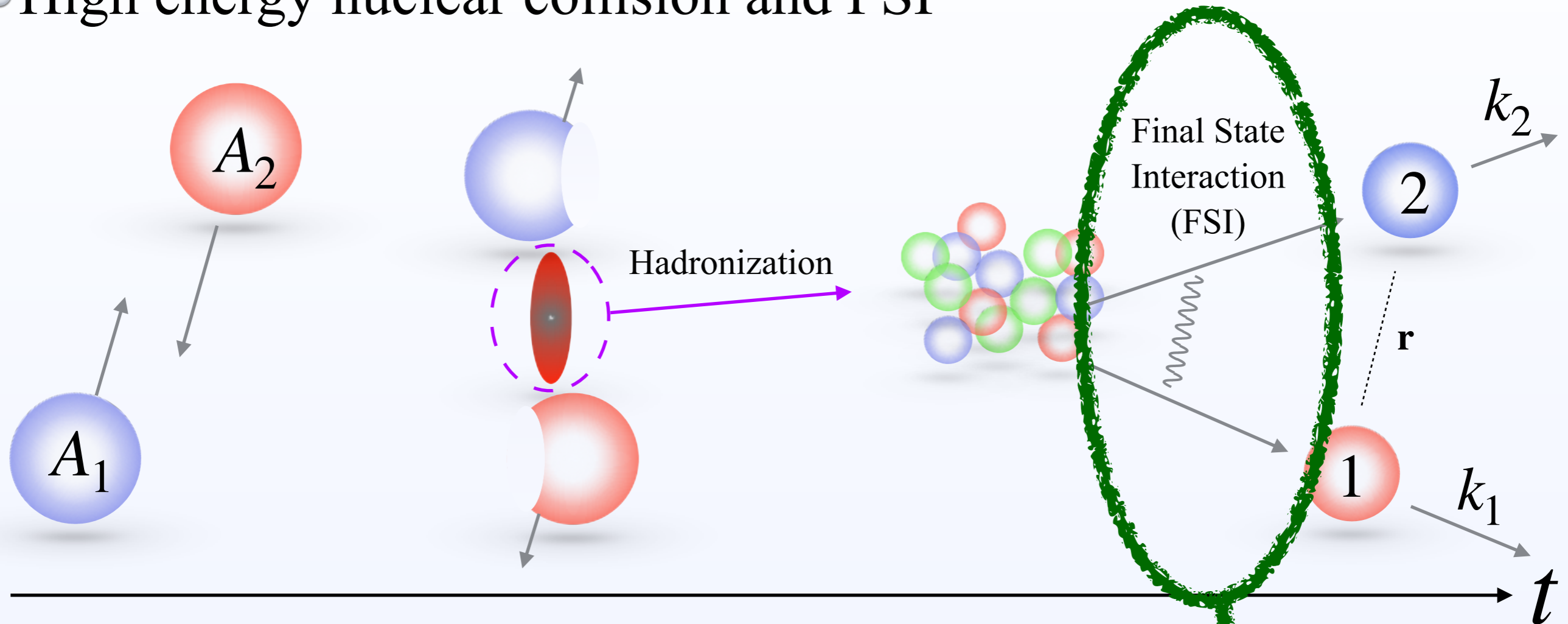
$S(\mathbf{r})$: Source function

$\varphi^{(-)}(\mathbf{q}, \mathbf{r})$: Relative wave function

- Depends on ...
Collision detail (A_i , energy, centrality)
- Including information of...
size of hadron source,
momentum dependence, weight...

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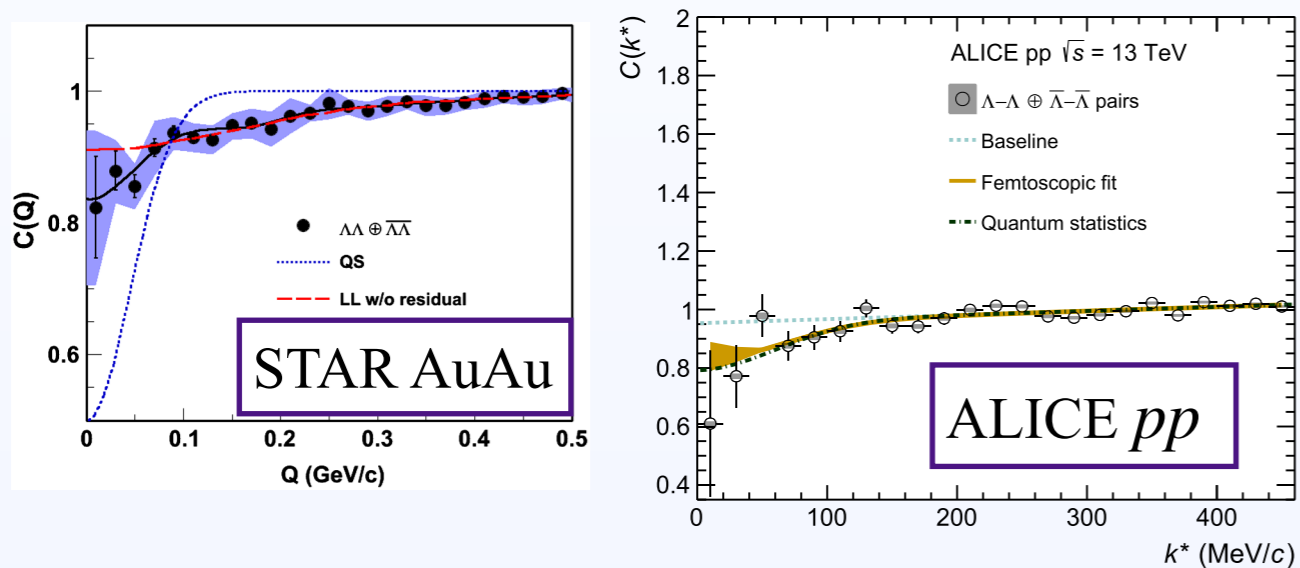
Interaction (strong and Coulomb)

quantum statistics (Fermion, boson)

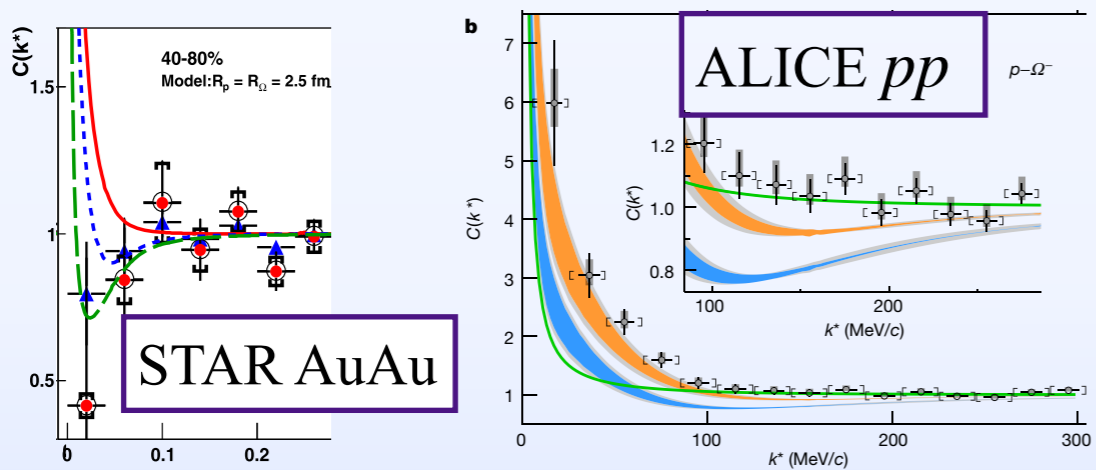
Hadron correlation in high energy nuclear collision

Experimental data in various sectors

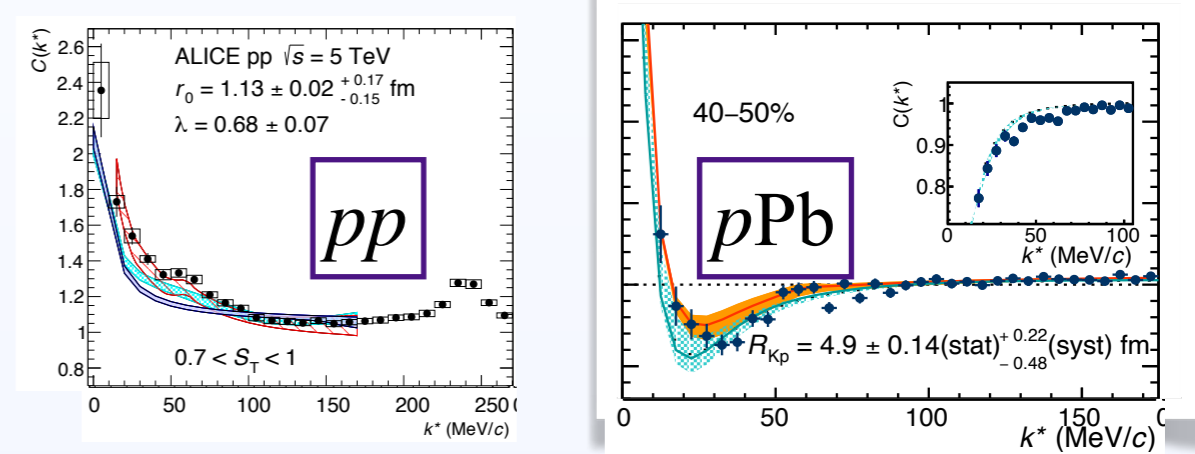
- $\Lambda\Lambda$
 - STAR AuAu: PRL 114,022301(2015)
 - ALICE pp: PLB 797 (2019) 134822
 - PbPb: PRC99, 024001 (2019)



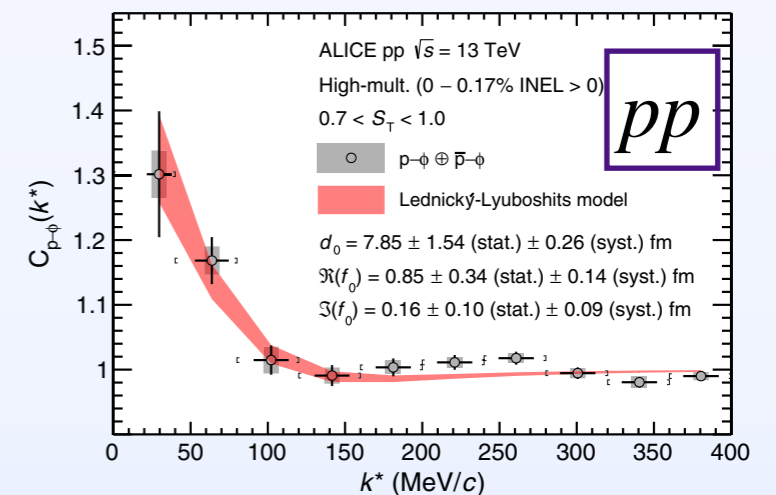
- $p\Omega$
 - STAR AuAu: PLB 790, 490 (2019)
 - ALICE pp: Nature 588 (2020) 232



- $K^\pm p$
 - ALICE pp: PRL 124 (2020) 9, 092301
 - PbPb: PLB 822 (2021) 136708
 - STAR AuAu: NPA 982 (2019) 359



- $p\phi$
 - ALICE pp: PRL 127 (2021) 17, 172301





Related talks in HYP 2022

● ALICE

- $Dp, D\pi, DK$ D. Battistini (28.6 poster session)
- $p\Lambda, pp\Lambda, Dp, D\pi$ D. L. Mihaylov (29.6, 14:30-)
- $p-d, K-d, \Lambda-d$ B. Singh (29.6, 15:45-)
- Λ -Hadrons G. Mantzaridis (29.6, 17:30-)
- K^-p R. Lea (30.6, 9:20-)
- (Over view) O. Vazquez Doce (1.7 9:00-)

● STAR

- $K^\pm K^\pm, K_s^0 K_s^0, K_s^0 K^\pm$ D. Pawłowska (29.6 16:00-)



Contents

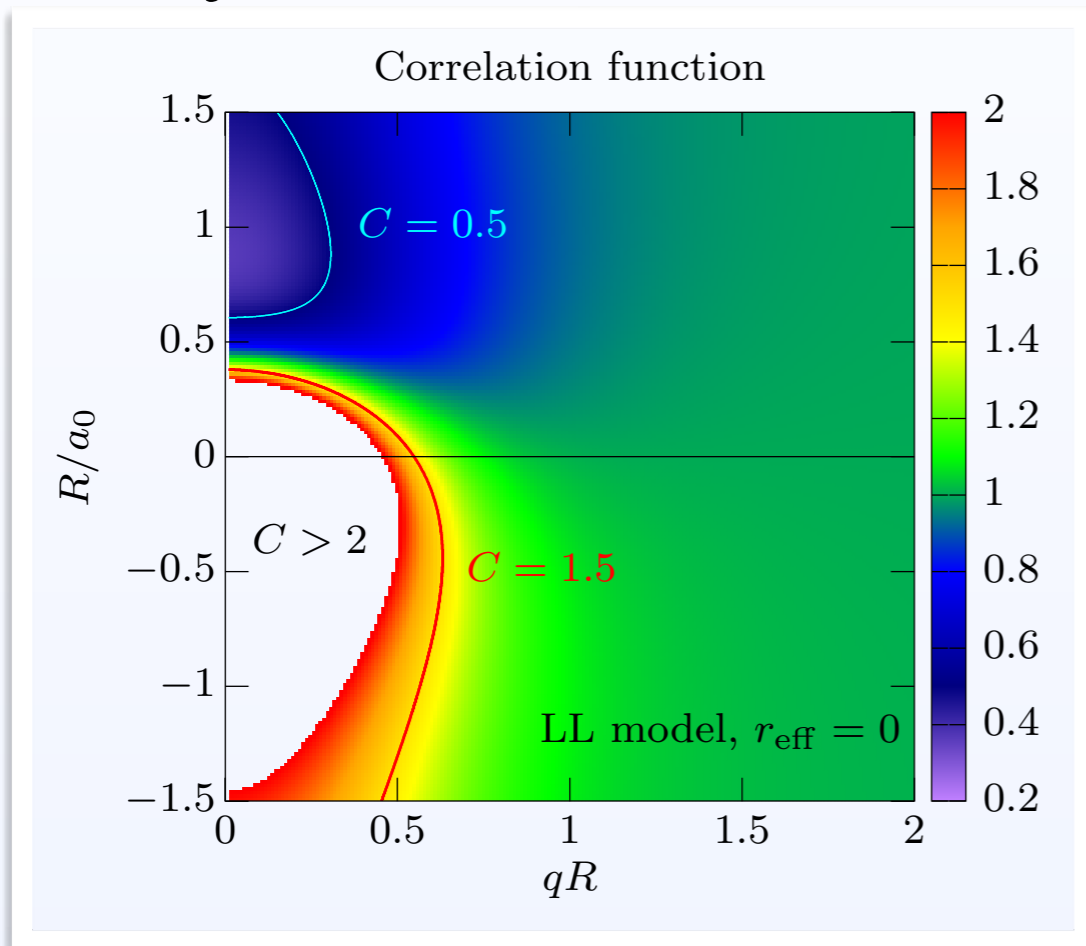
- Introduction: hadron-hadron momentum correlation function in high-energy nuclear collisions
- Key ingredients for femtoscopic study
 - Source size dependence
 - Coupled-channel effect
- Experimental and theoretical studies for various channels
 - Strangeness sector
 - Charm sector

Hadron correlation in high energy nuclear collision

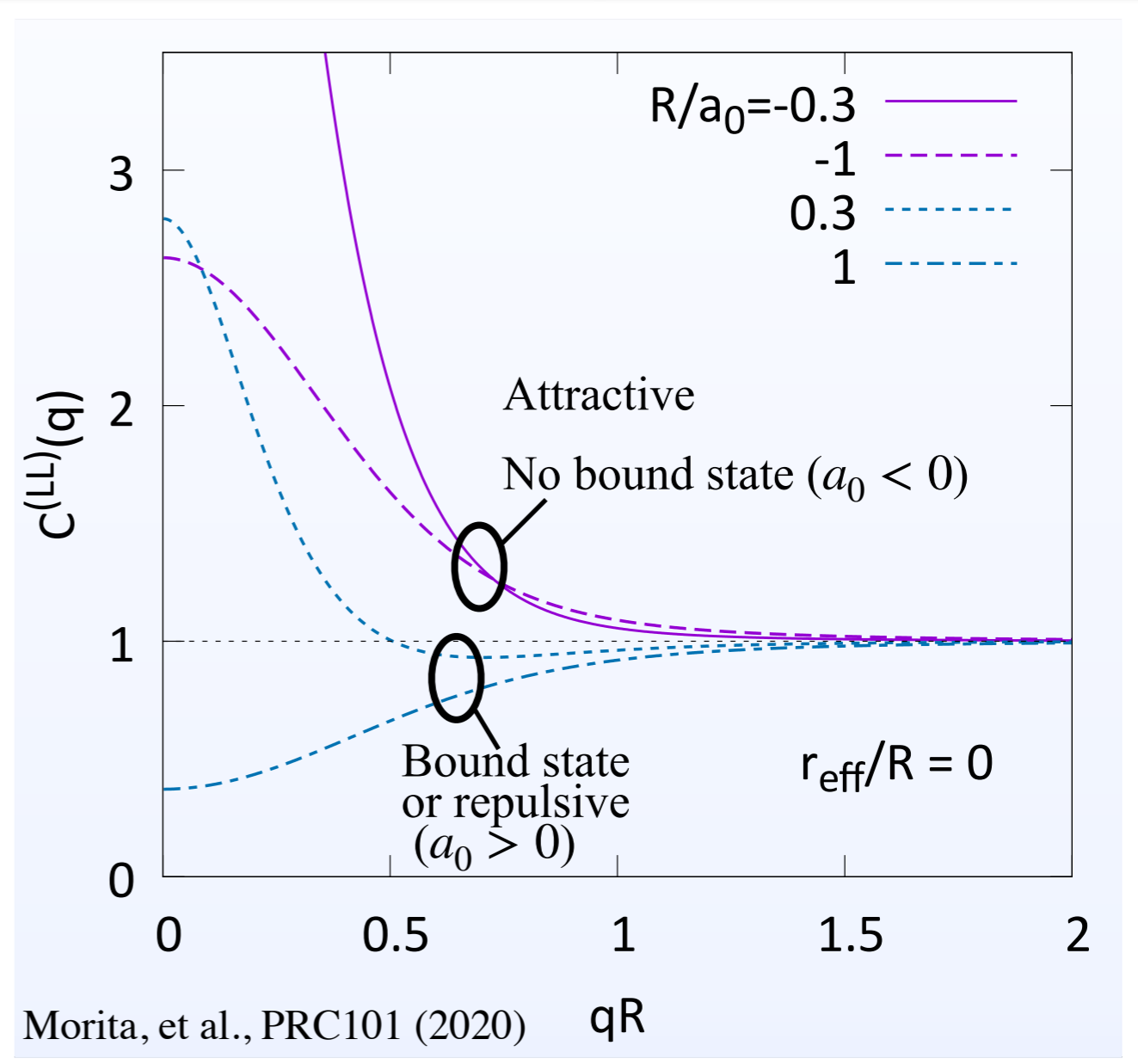
- Simple model: Lednicky-Lyuboshits (LL) formula

$$C(\mathbf{q}) \simeq \int d^3\mathbf{r} S(\mathbf{r}) |\varphi^{(-)}(\mathbf{q}, \mathbf{r})|^2 = C(qR, R/a_0)$$

- Gaussian source with radius R
- $\mathcal{F}(q) = [-1/a_0 - iq]^{-1}$ with scat. length a_0



Y. Kamiya, K. Sasaki, T. Fukui, K. Morita, K. Ogata, A. Ohnishi, T. Hatsuda, *Phys.Rev.C* 105 (2022) 1, 014915



Morita, et al., PRC101 (2020) qR

- Clear relation between $C(q)$ and interaction
- Sensitive to (non)existence of bound state

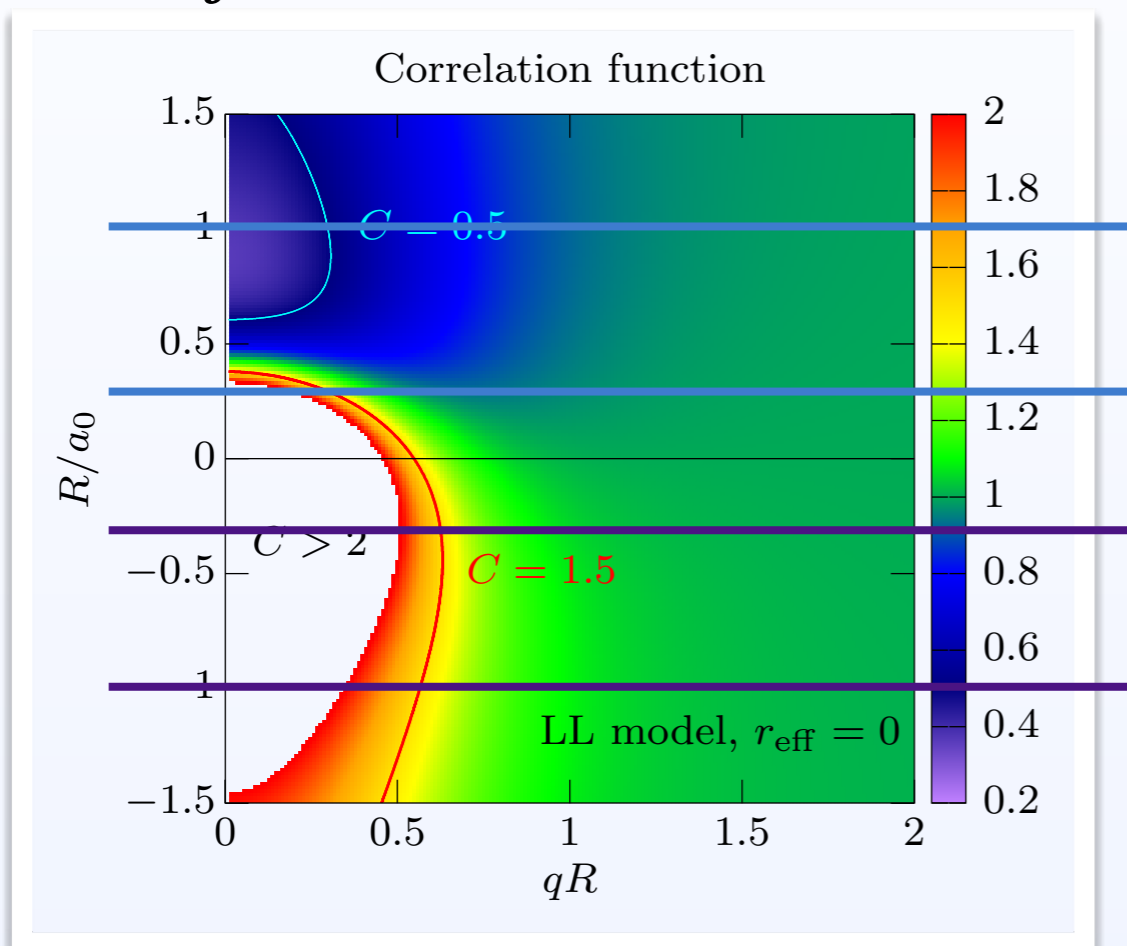
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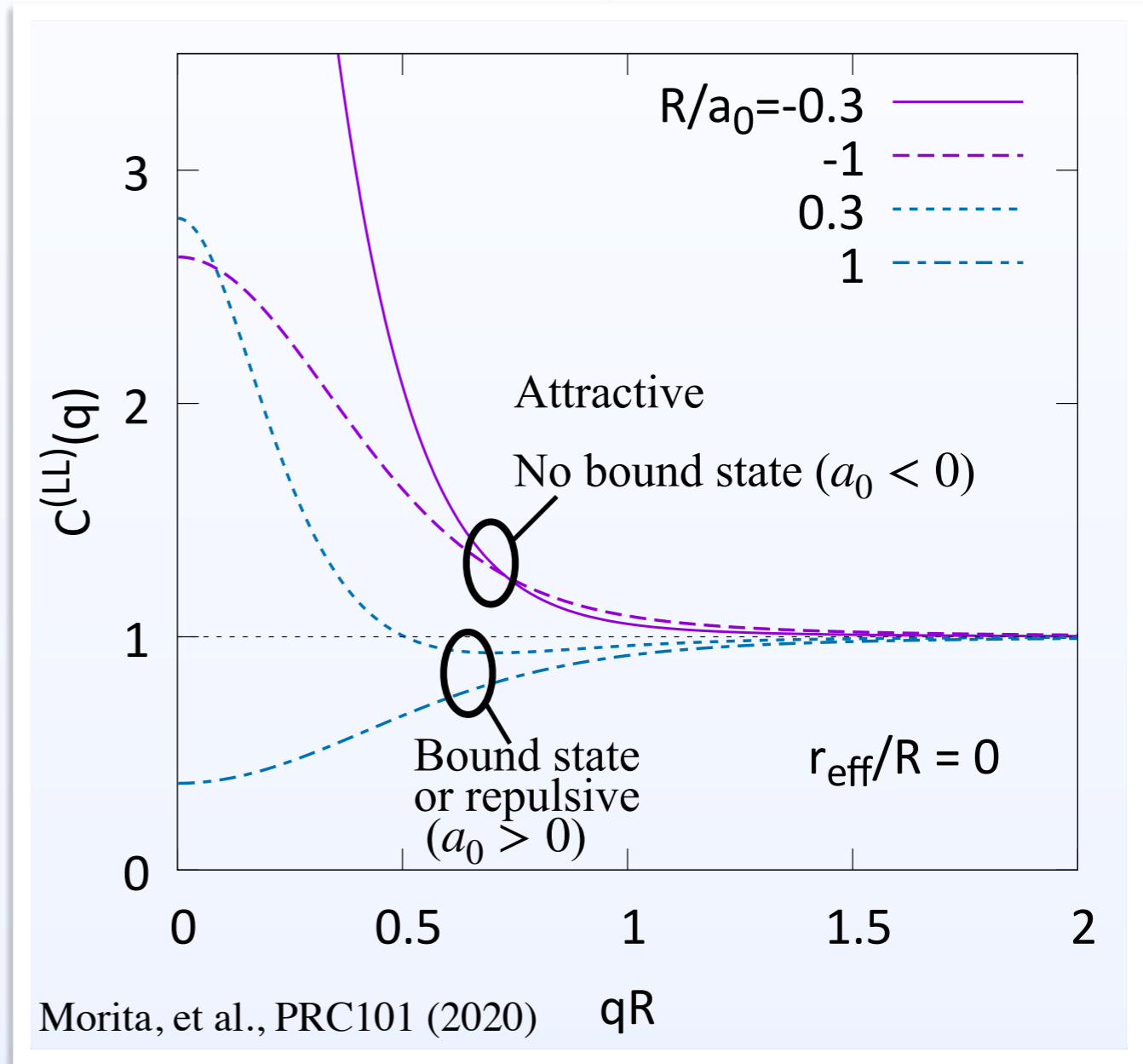
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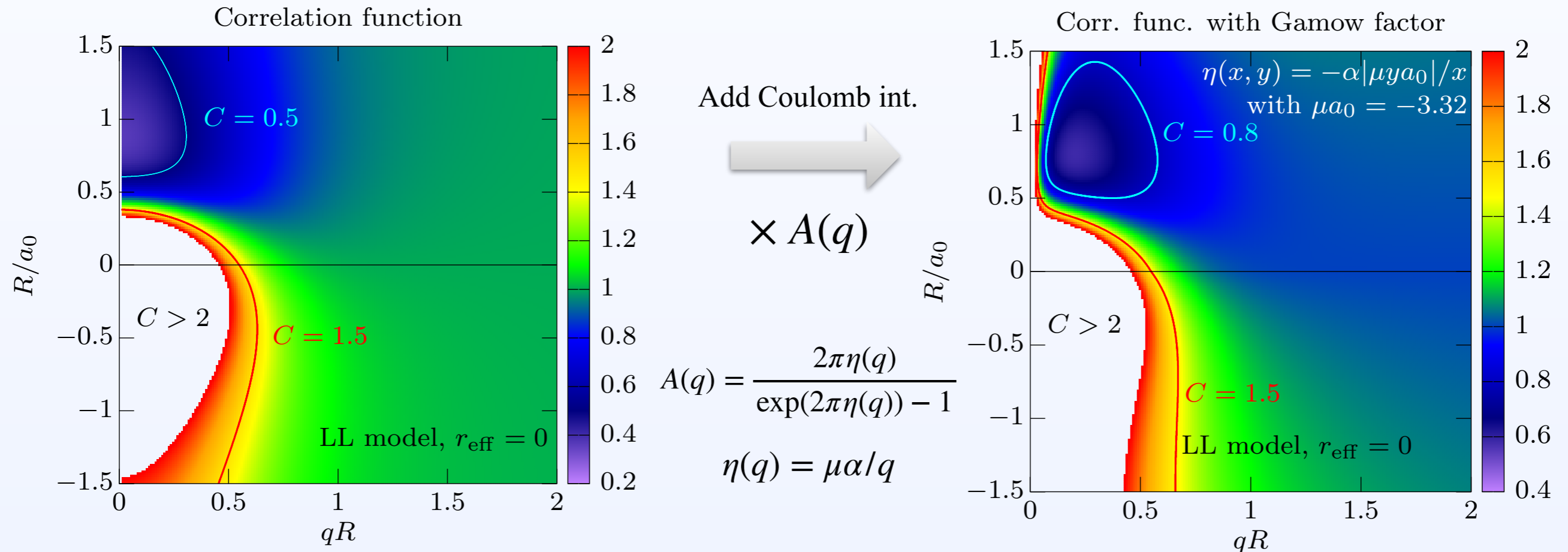
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Coulomb interaction

● Coulomb interaction with LL formula + Gamow correction

- w/o Coulomb interaction
 - Only with strong int.

- w/ Coulomb interaction (attractive case)
 - Coulomb int. with Gamow factor
 - Coulomb attractive case (for $p\Xi^-$)



- Low energy region: Coulomb effect dominant
- Strong int. effect: found as deviation from pure Coulomb case
- Bound state signal : Suppression \implies Dip structure (attractive case)

Y. Kamiya, K. Sasaki, T. Fukui, K. Morita, K. Ogata, A. Ohnishi, T. Hatsuda,
Phys.Rev.C 105 (2022) 1, 014915

Coupled-channel effect

- Koonin-Pratt-Lednicky-Lyuboshits-Lyuboshits (KPLLL) formula

$$C(\mathbf{q}) = \int d^3\mathbf{r} S(\mathbf{r}) |\psi^{(-)}(q; r)|^2 + \sum_{j \neq i} \omega_j \int d^3\mathbf{r} S_j(\mathbf{r}) |\psi_j^{(-)}(q; r)|^2$$

S.E. Koonin, PLB 70 (1977)
 S. Pratt et. al. PRC 42 (1990)
 R. Lednicky, et.al. Phys. At. Nucl. 61(1998)

Contribution from Coupled-channel Source

- Coupled-channel wave function

$\psi_i \rightarrow$ (out-going wave) + S^\dagger (incoming wave)

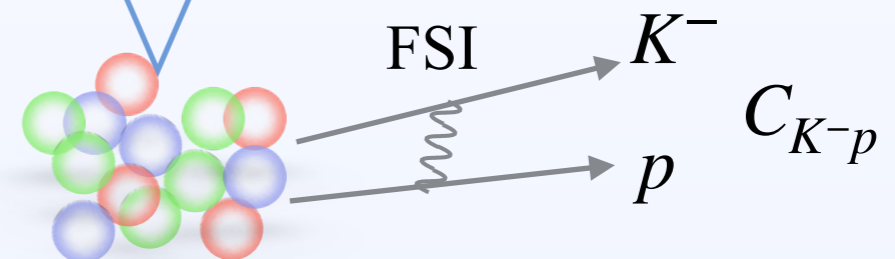
- $|S_{ij}| < 1 \rightarrow$ Decrease the correlation
- At channel threshold \rightarrow Cusp structure
- ψ_i : obtained by solving the c.c. Schrödinger eq.

$$\begin{pmatrix} -\frac{\nabla^2}{2\mu_1} + V_{11}(r) & V_{12}(r) & \cdots & V_{1n}(r) \\ V_{21}(r) & -\frac{\nabla^2}{2\mu_2} + V_{22}(r) + \Delta_2 & \cdots & V_{2n}(r) \\ \vdots & \vdots & \ddots & \vdots \\ V_{n1}(r) & V_{n2}(r) & \cdots & -\frac{\nabla^2}{2\mu_n} + V_{nn}(r) + \Delta_n \end{pmatrix} \Psi(q_1, r) = E\Psi(q_1, r),$$

$V_{ij} = V_{ij}^{\text{strong}} (+V^{\text{Coulomb}})$ Δ_i ; threshold energy diff.

- Contribution from coupled-channel source

$K^-p, \bar{K}^0n, \pi^0\Sigma^0, \pi^+\Sigma^-, \pi^-\Sigma^+, \pi^0\Lambda$



- Enhance $C(q)$
- Enhance cusp structure
- ω_i : production rate (compared to measured channel)

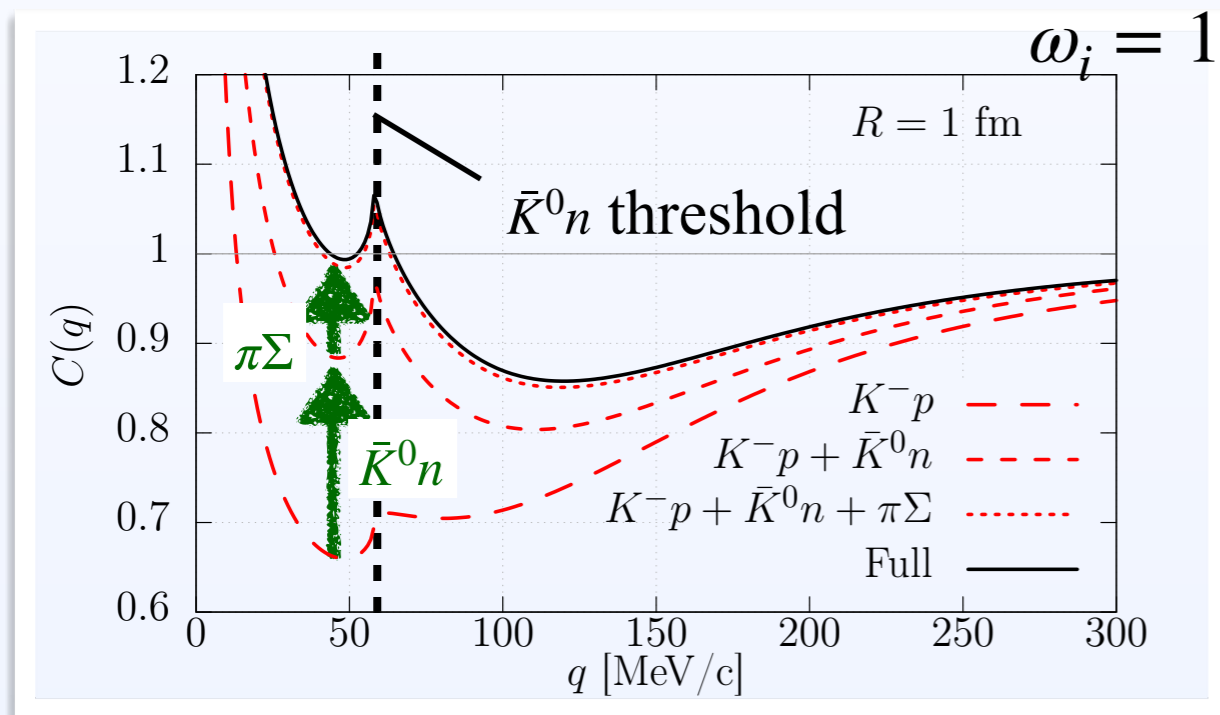
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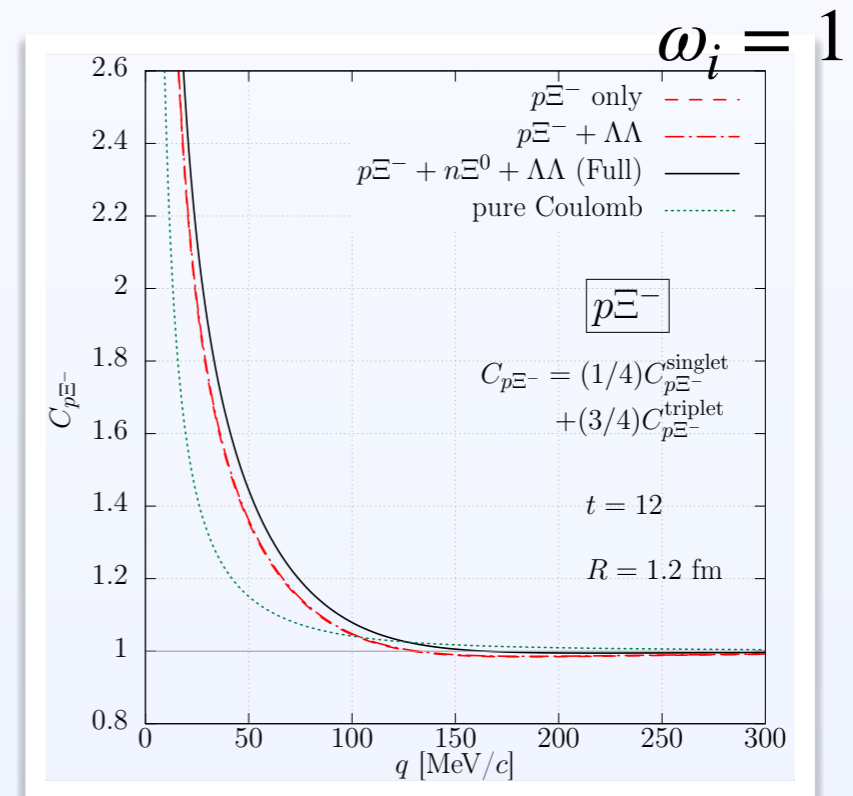
- K^-p with chiral SU(3) model
 - strongly couples to $\pi\Sigma$ and \bar{K}^0n



Kamiya, Hyodo, Morita, Ohnishi, Weise, PRL 124 (2020) 13, 132501

- \bar{K}^0n cusp enhanced
- \bar{K}^0n and $\pi\Sigma$ source gives sizable enhancement
- $\pi\Lambda$ coupling is negligible

- $p\Xi^-$ with HAL QCD potential
 - weakly couples to $n\Xi^0$ and $\Lambda\Lambda$

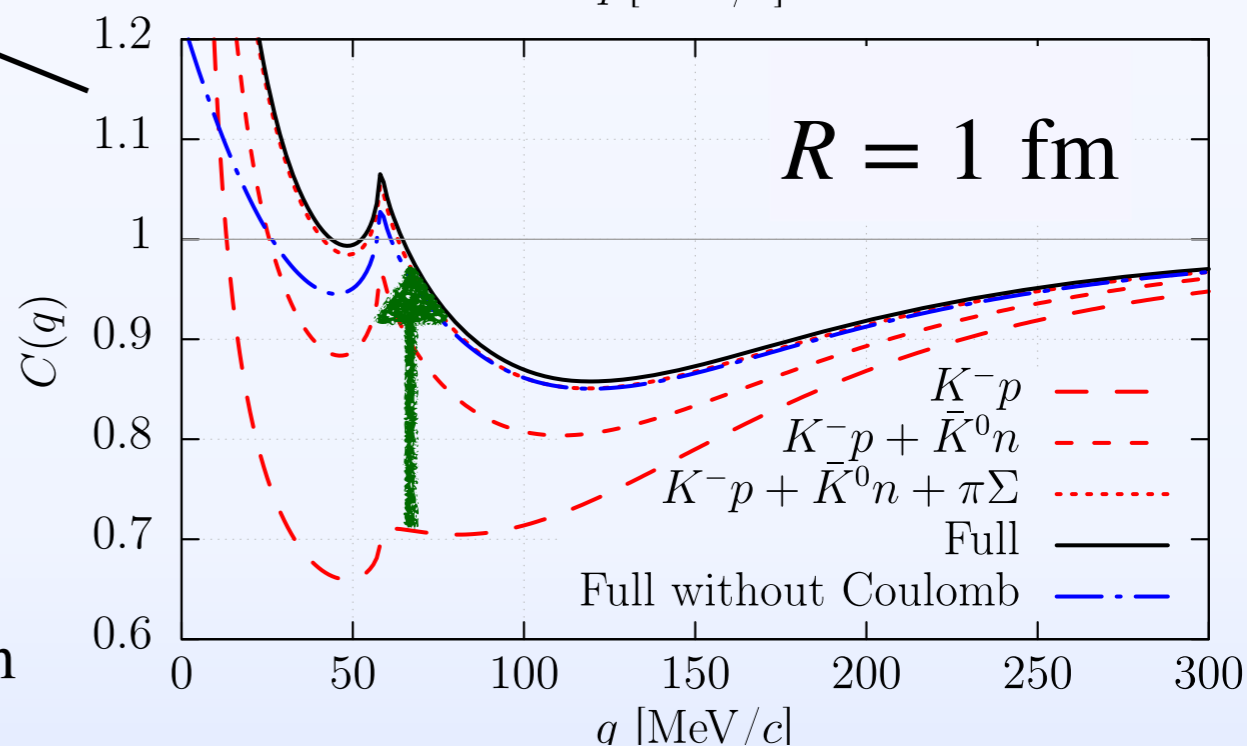
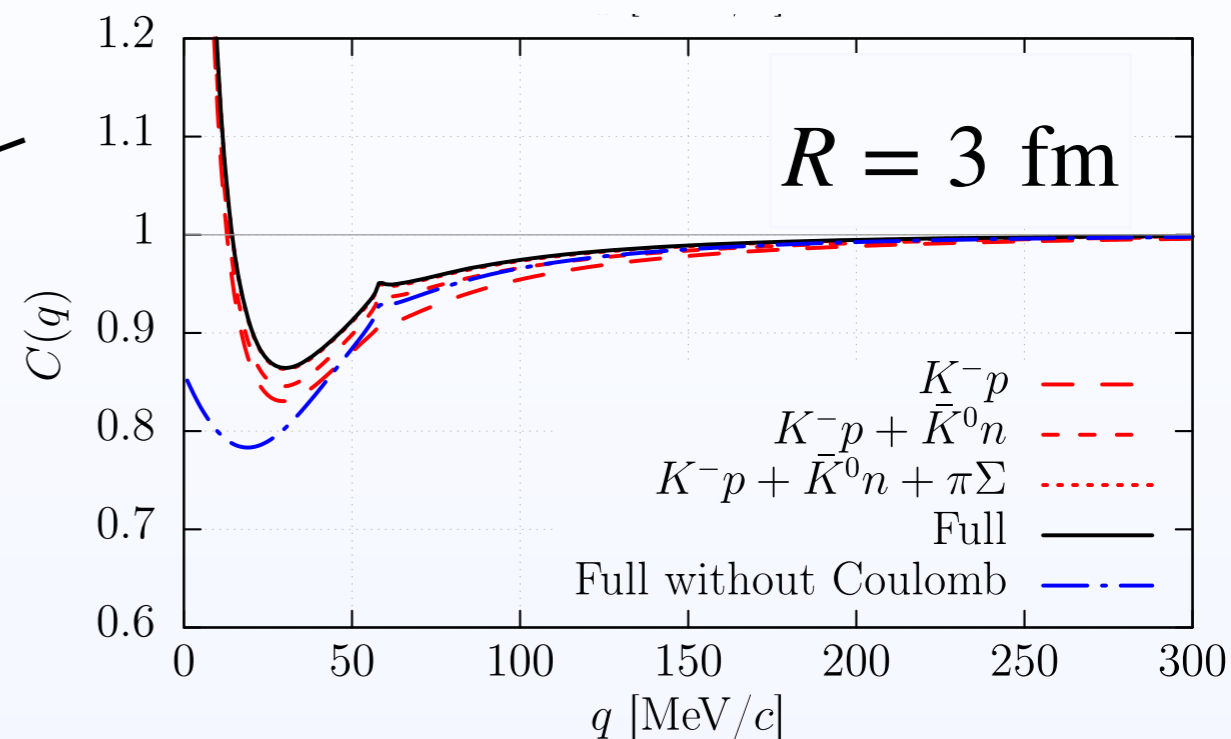
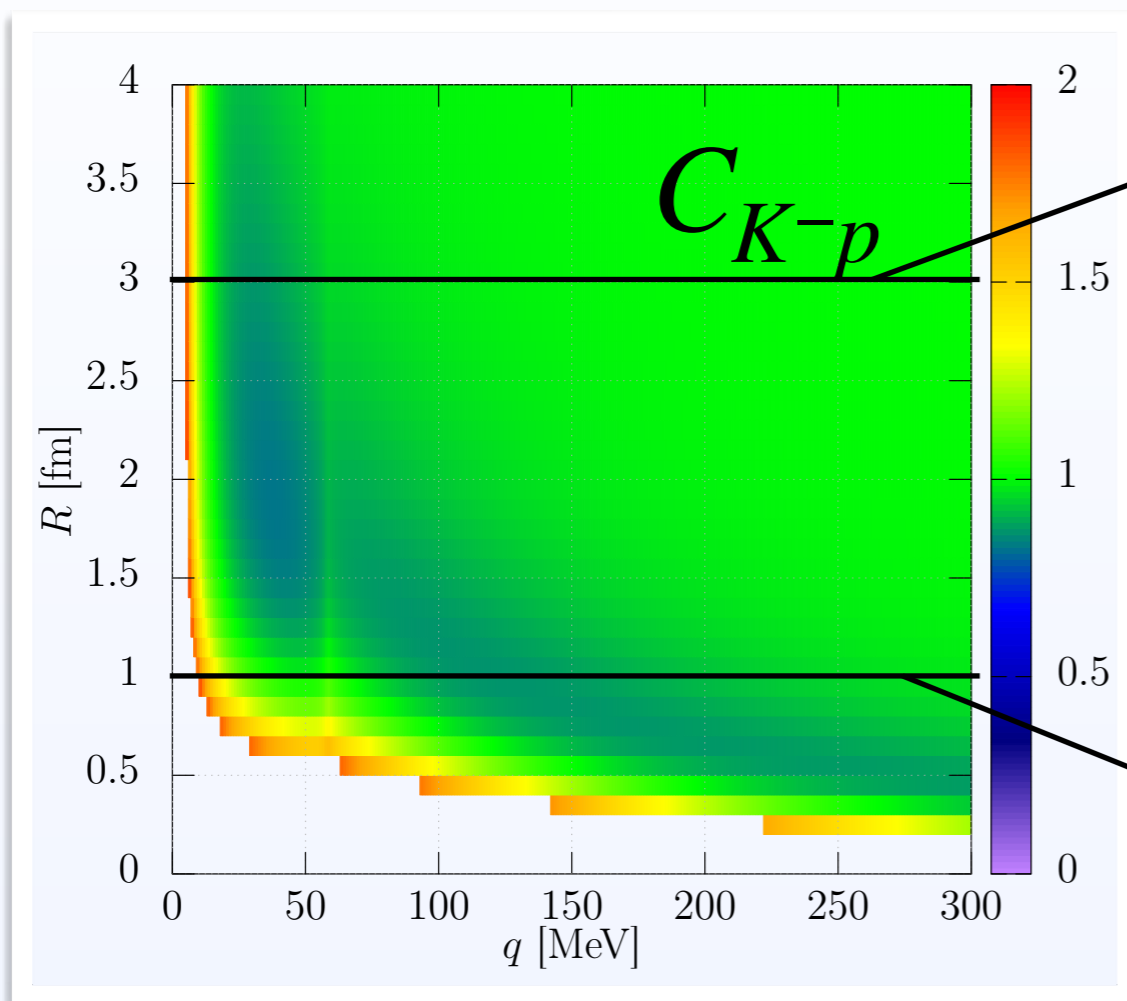


Kamiya, Sasaki, Fukui, Morita,
 Ogata, Ohnishi, Hatsuda, PRC 105, 014915 (2022)

- moderate contribution from coupled-channels

Coupled-channel effect

- Source size dependence of coupled-channel effect

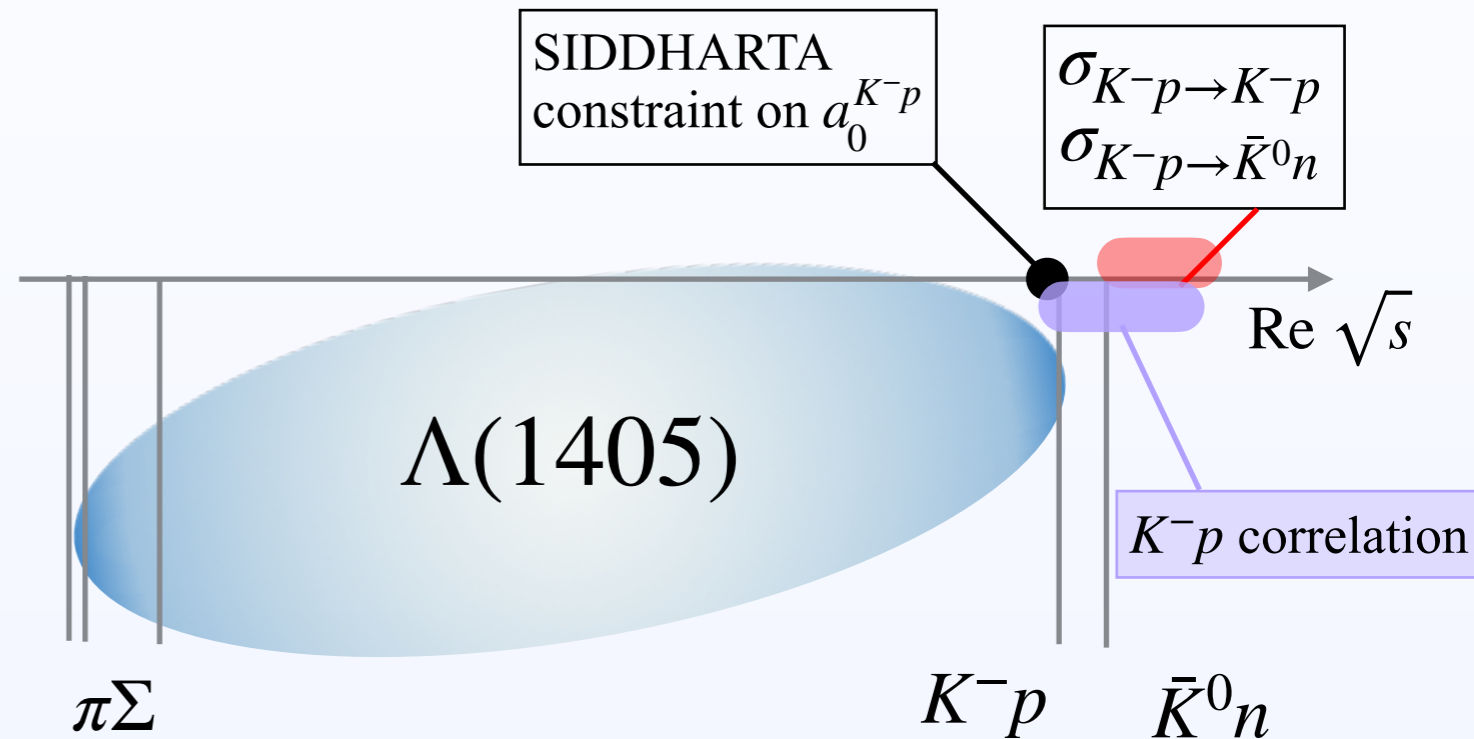


- Strong source size dependence
 - < == Due to the near-threshold $\Lambda(1405)$ pole
- $C(q)$ with large source
 - Less prominent cusp structure
 - Weaker coupled-channel source contribution

$\bar{K}N$ interaction and K^-p correlation

- $\bar{K}(s\bar{l})N$ interaction and $\Lambda(1405)$

- Coupled-channel system of $\pi\Sigma$ - $\pi\Lambda$ - $\bar{K}N$
- Strong attraction reproducing quasi-bound state $\Lambda(1405)$
- Strong constraint on $a_0^{K^-p}$ by SIDDHARTA experiment of Kaonic hydrogen
M. Bazzi, et al., PLB 704 (2011)
- Structure of $\Lambda(1405)$
 - two pole structure
J. A. Oller and U. G. Meißner, PLB500, 263 (2001)
 - $\bar{K}N$ molecular picture (high-mass pole)
R.H. Dalitz, S.F. Tuan, PRL 425 (1959).



- Chiral SU(3) based $\bar{K}N$ - $\pi\Sigma$ - $\pi\Lambda$ potential

Miyahara, Hyodo, Weise, PRC 98 (2018)

- Constructed based on the amplitude with NLO chiral SU(3) dynamics $\leftarrow a_0^{K^-p}$, σ fitted
Ikeda, Hyodo, Weise, NPA881 (2012)
- Coupled-channel, energy dependent as

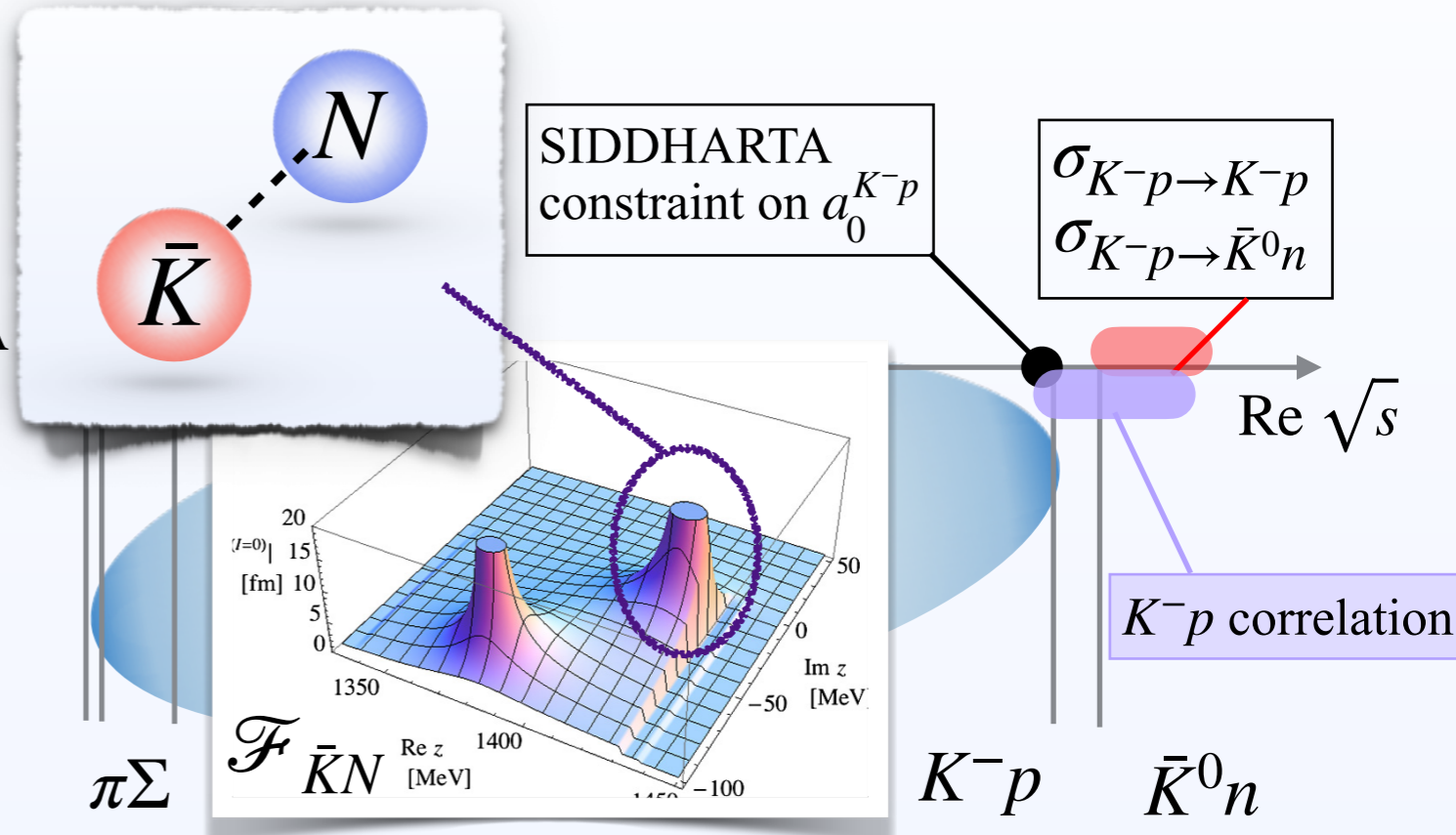
$$V_{ij}^{\text{strong}}(r, E) = e^{-(b_i/2 + b_j/2)r^2} \sum_{\alpha=0}^{\alpha_{\text{max}}} K_{\alpha,ij} (E/100 \text{ MeV})^\alpha$$

- Constructed to reproduce the chiral SU(3) amplitude around the $\bar{K}N$ sub-threshold region

$\bar{K}N$ interaction and K^-p correlation

- $\bar{K}(s\bar{l})N$ interaction and $\Lambda(1405)$ resonance

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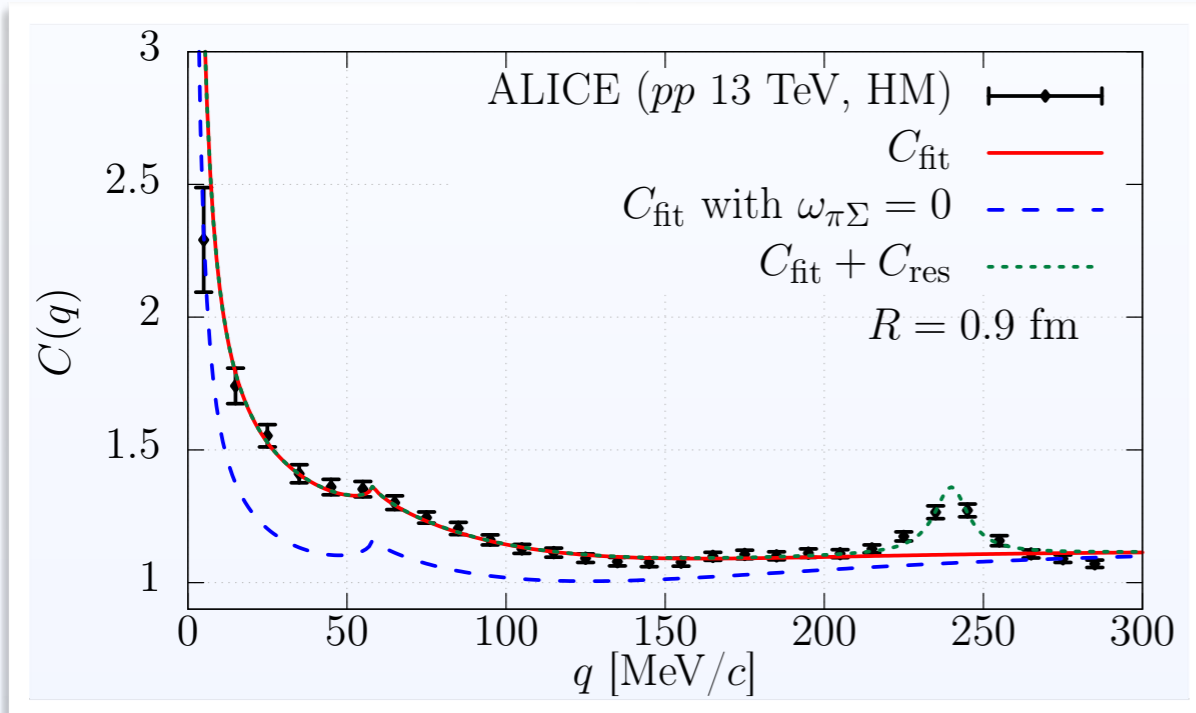
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$\bar{K}N$ interaction and K^-p correlation

Source size dependence with K^-p data

- ALICE pp collision data

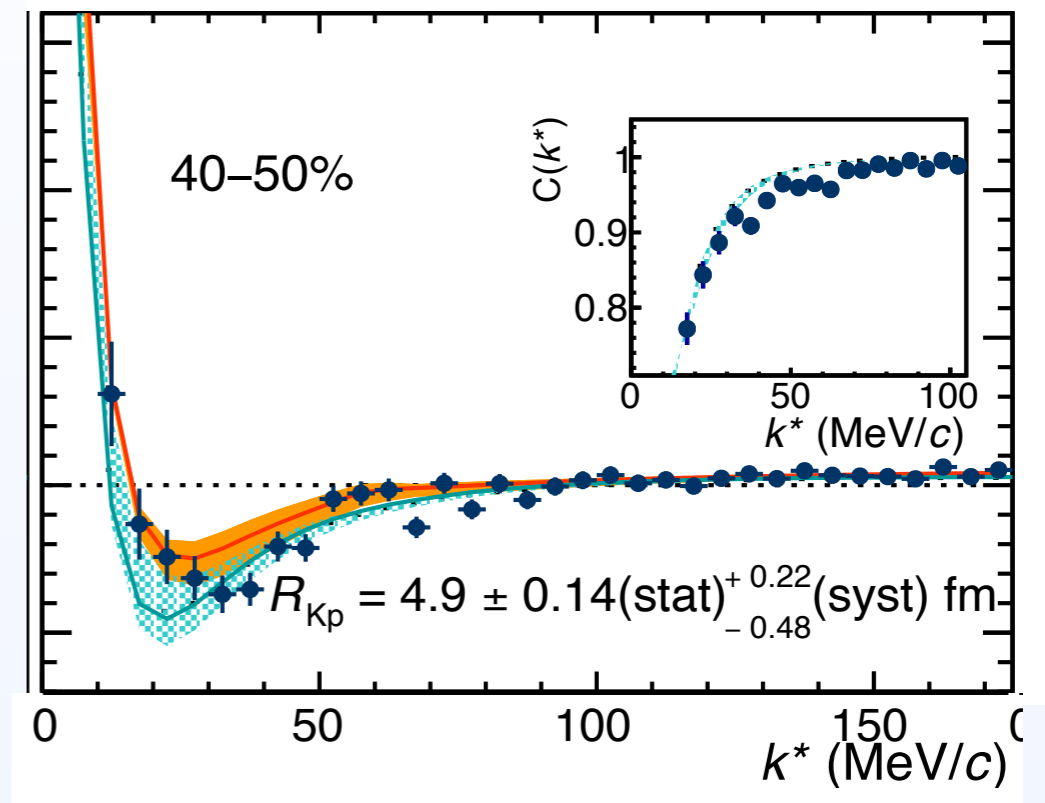
ALICE PRL 124, 092301 (2020)



Kamiya, Hyodo, Morita, Ohnishi, Weise, PRL 124 (2020) 13, 132501

- ALICE PbPb collision data

ALICE PLB 822 (2021) 136708



- Large source

- Weaker cusp
- Consistent with analysis only with K^-p source



- Chiral SU(3) dynamics describes the both correlation data well.

$\bar{K}N$ interaction and K^-p correlation

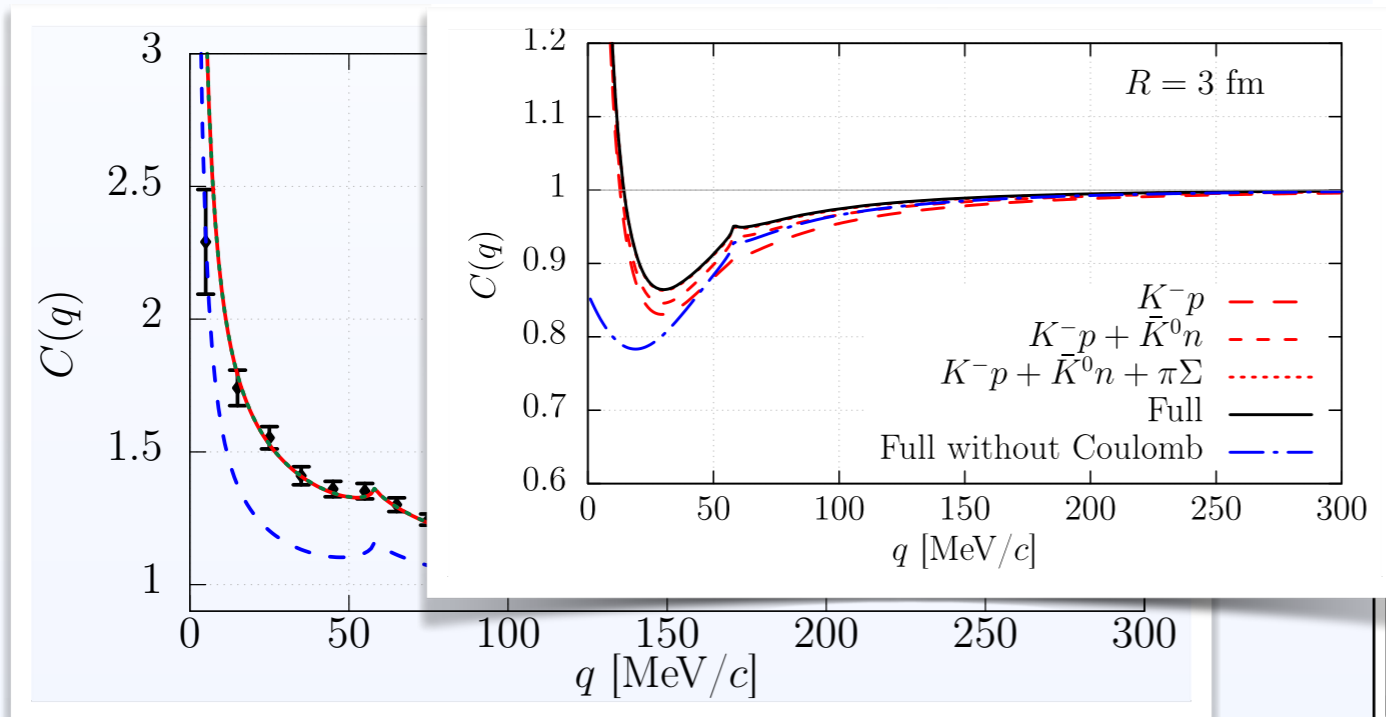
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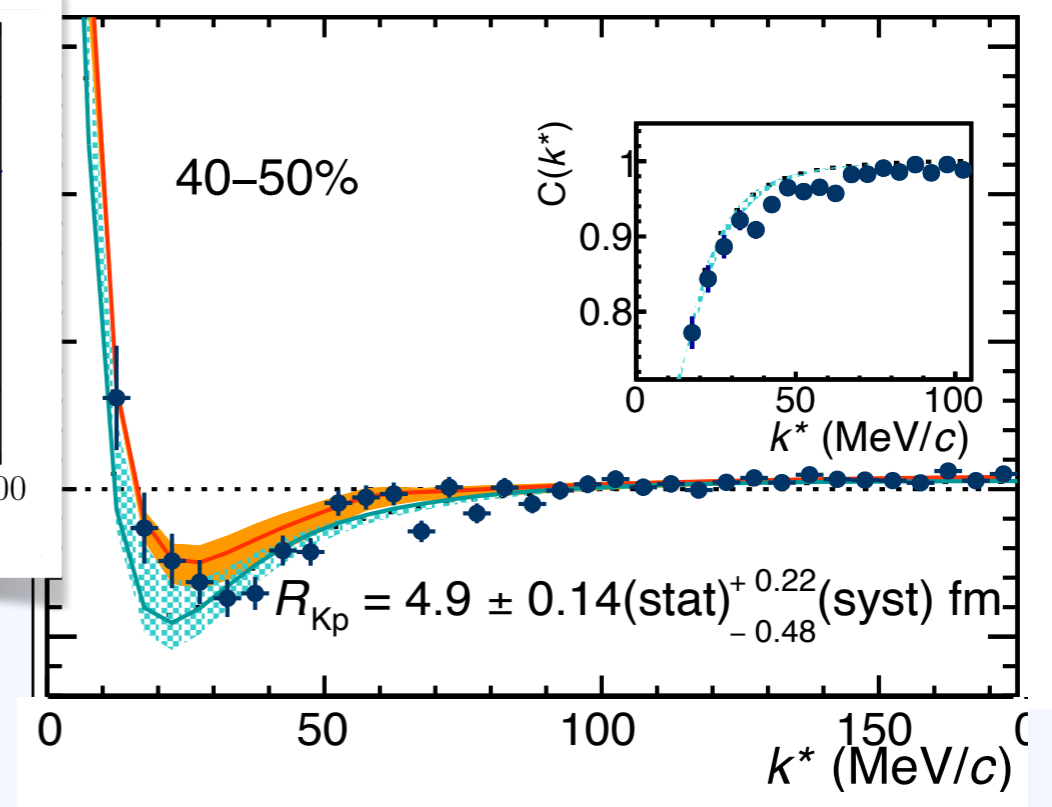
- ALICE PbPb collision data

ALICE PLB 822 (2021) 136708



Kamiya, Hyodo, Morita, Ohnishi, Weise, PRL 124 (2020) 13, 132501

- Small source
 - Clear \bar{K}^0n cusp structure
 - Sizable contribution from coupled-channel source required to reproduce data



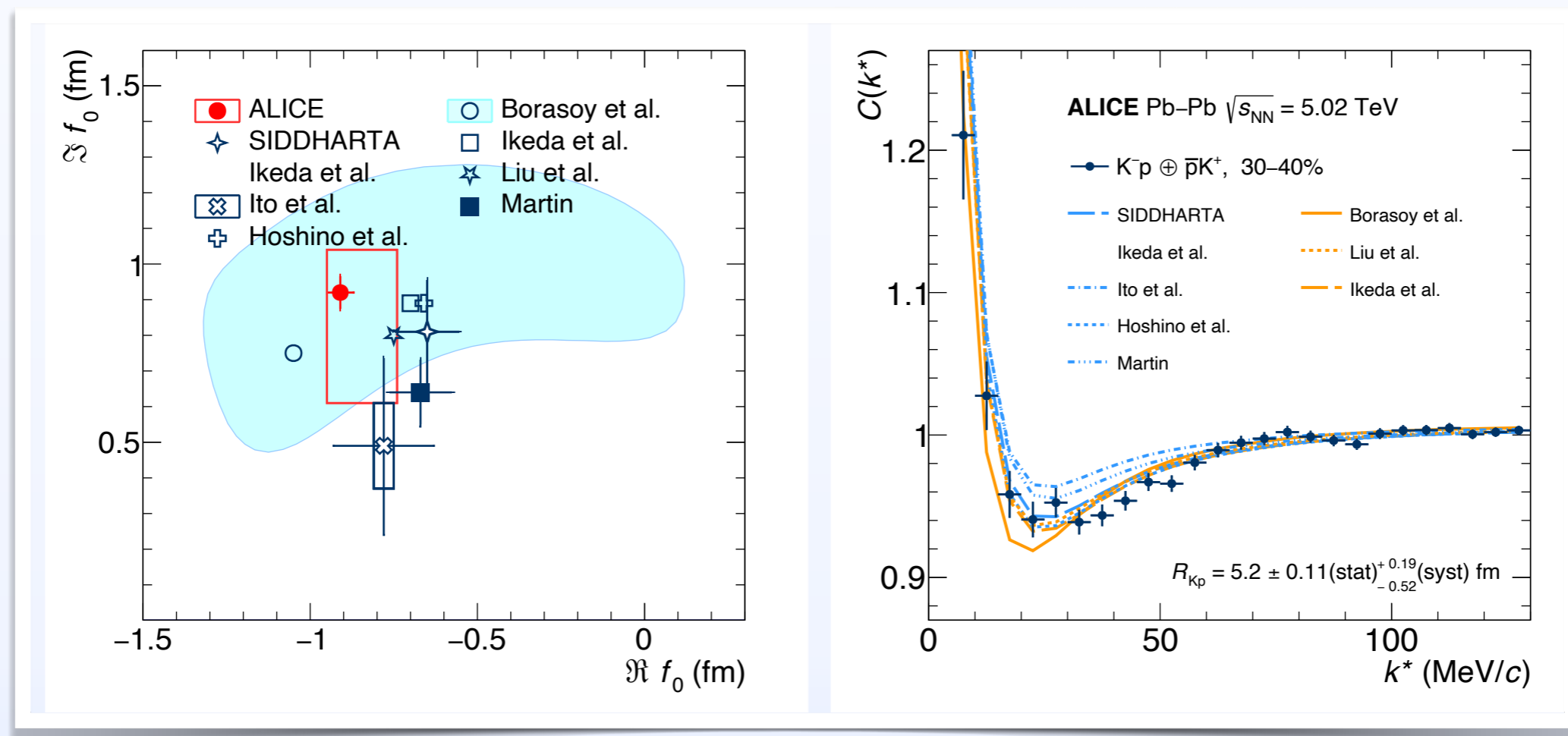
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$\bar{K}N$ interaction and K^-p correlation

- Source size dependence of K^-p
 - ALICE data PbPb collisions data ALICE PLB 822 (2021) 136708
 - Large source \rightarrow weaker coupled-channel effect
 \rightarrow more direct approach to interaction of the measured channel
 - Extraction of the K^-p scattering length from correlation function
 - * Fitting with 1 channel LL model with Gaussian source

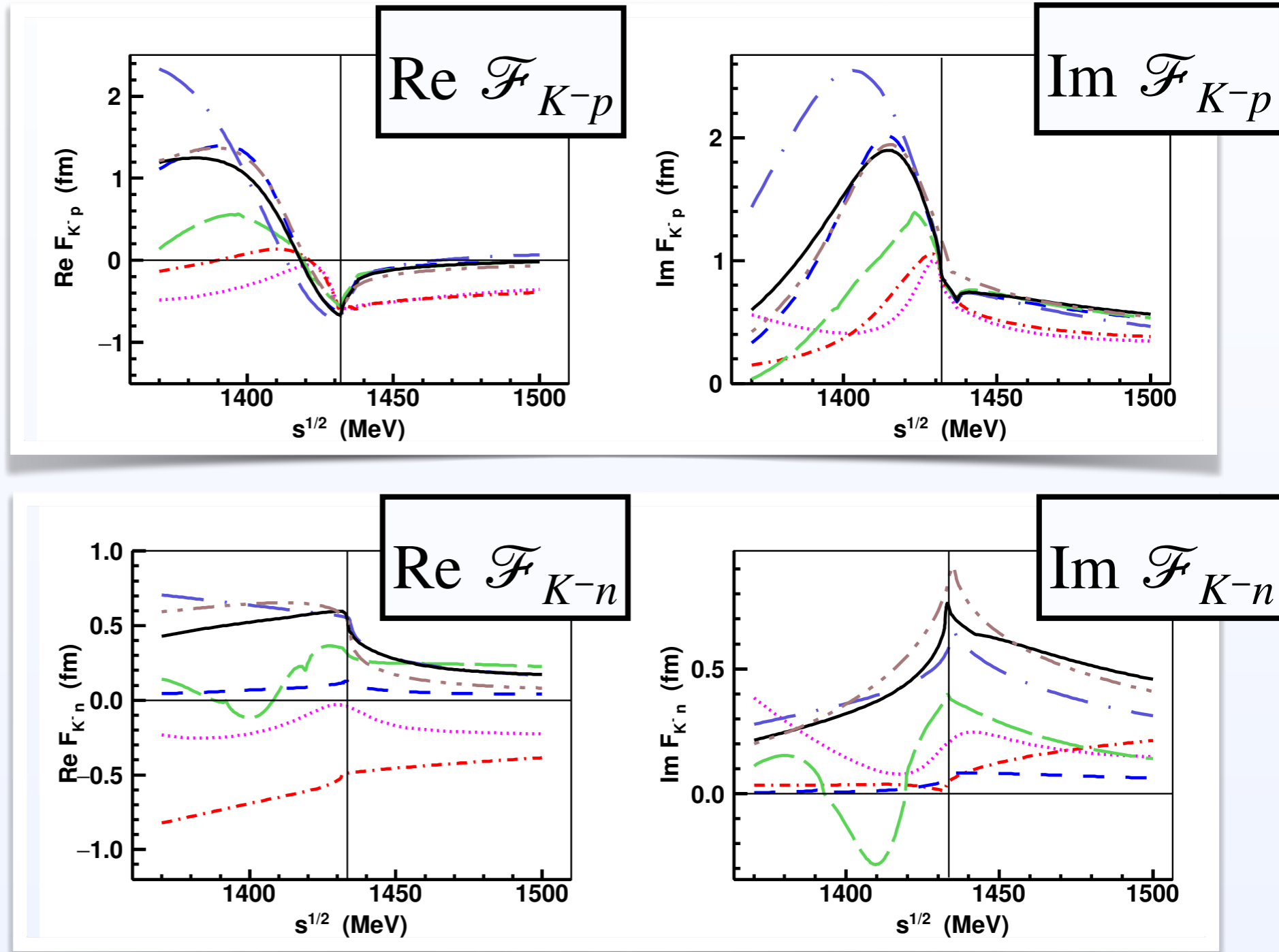
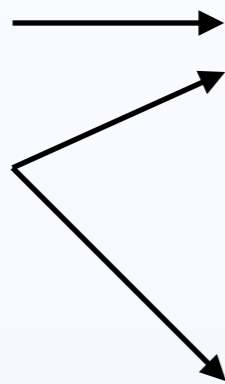


Further constraint on $\bar{K}N$ interaction?

- $\bar{K}N$ interaction

$$\mathcal{F}_{\bar{K}N, I=0}$$

$$\mathcal{F}_{\bar{K}N, I=1}$$



B2, B4: Mai, Meißner, EPJA 51 (2015)

M1, MII: Guo, Oller, PRC 87 (2013)

PNLO: Cieplý, Smejkal, NPA 881 (2012)

KMNLO: Ikeda, Hyodo Weise NPA 881 (2012)

Cieplý and Mai, EPJ Web Conf. 130, 02001 (2016)

- Can we constrain $\bar{K}N I = 1$ interaction / amplitude from femtoscopy?

$\bar{K}N$ interaction and K^-p correlation

- Latest K^-p correlation results

ALICE [2205.10258]

- pPb : 0-20%, 20-40% 40-100%
- $PbPb$: 60-70%, 70-80% 80-90%

- **Discrepancy** around \bar{K}^0n threshold between chiral SU(3) model and exp. data for small source data

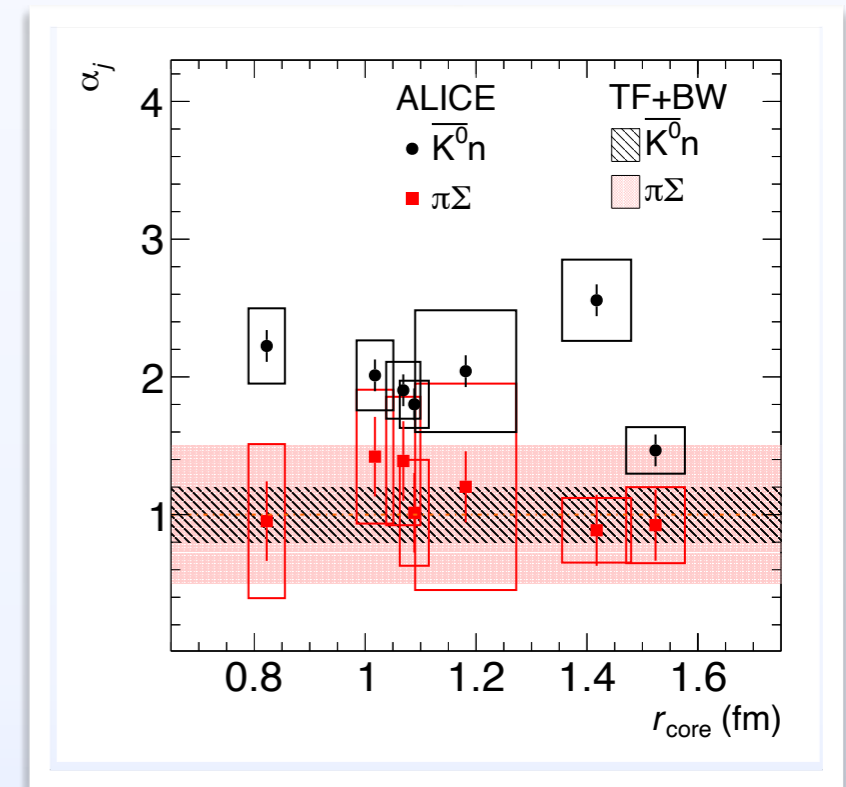
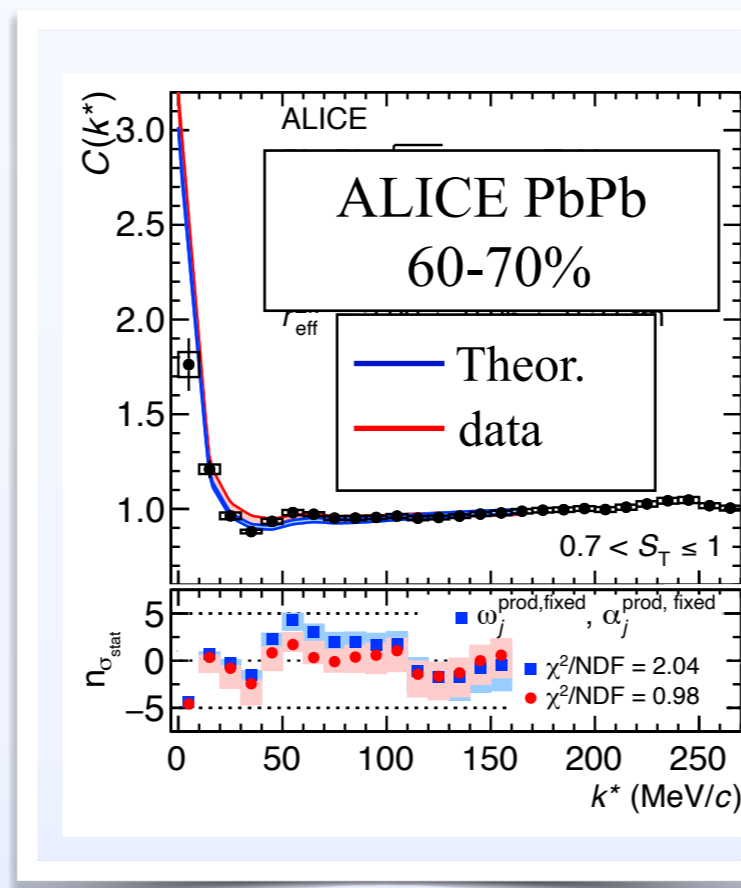
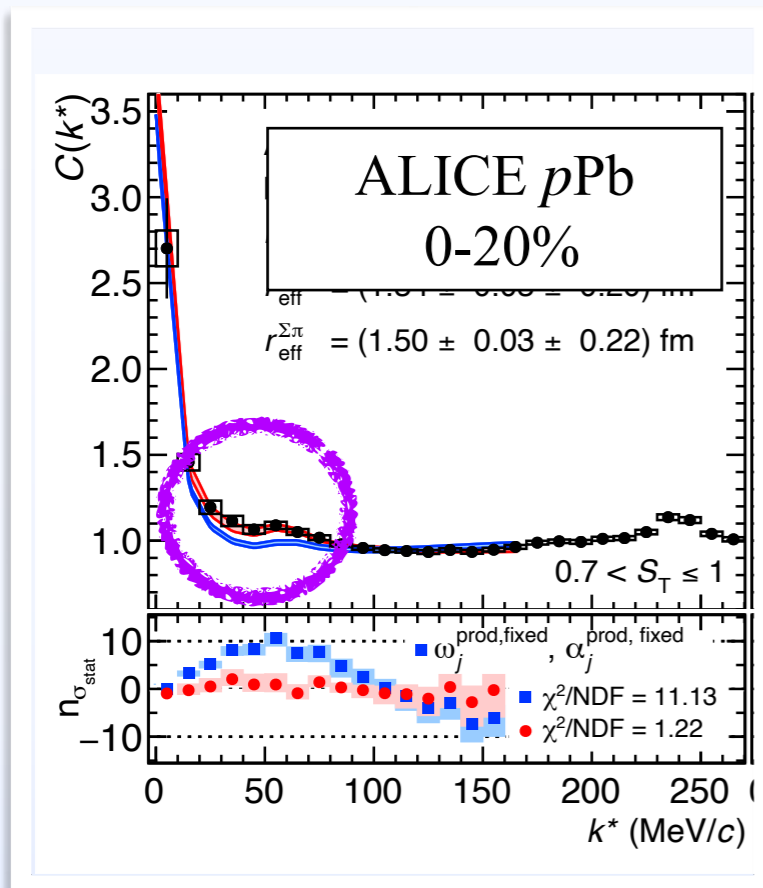
- Analysis with scale factor α_j

- Scale the coupled-channel source contribution by scaling factor

$$C_{K^-p} = C_{K^-p}^{\text{el}} + \sum_j \alpha_j C_j^{\text{inel}}$$

- $\alpha_{\bar{K}^0n} \sim 2$ gives better agreement

→ implying the stronger coupling



Detail → Talk by R. Lea 9am on Thursday!

$\bar{K}N$ interaction from $K_S^0 p$ correlation function

Y. Kamiya, T. Hyodo, A. Ohnishi. in preparation

$K_S^0 p$ correlation

$$|K_S^0 p\rangle = [|\bar{K}^0 p\rangle - |K^0 p\rangle]/\sqrt{2}$$

$\bar{K}N, I = 1$

$KN, I = 0, 1$

$$C_{K_S^0 p} = [C_{\bar{K}^0 p} + C_{K^0 p}]/2$$

- $I = 1$ component only

- Well determined with scat. exp.

- Chiral amplitude

- Chiral amplitude

Ikeda, Hyodo, Weise, NPA881 (2012)

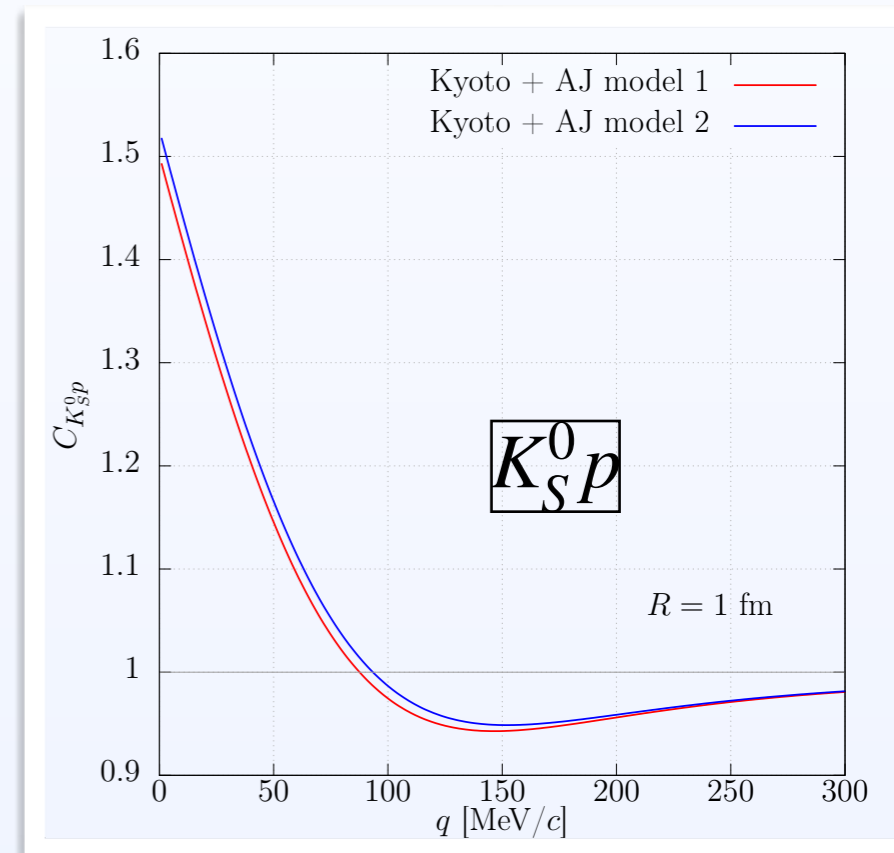
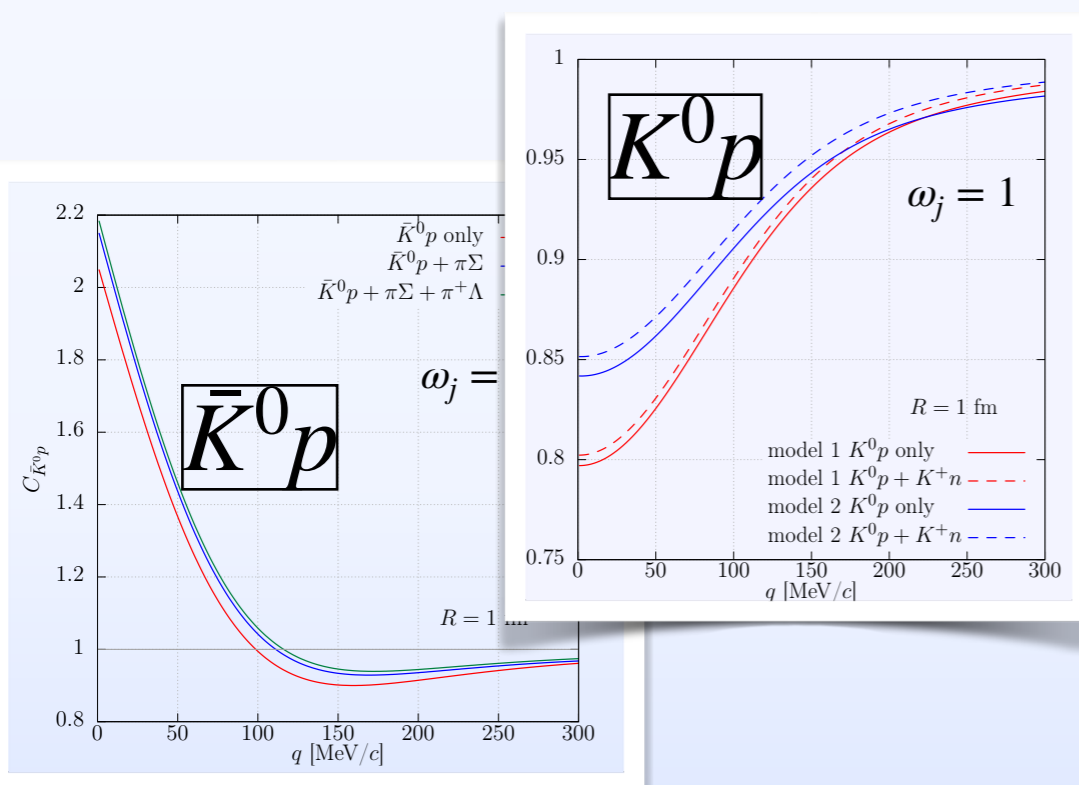
K. Aoki and D. Jido, PTEP (2019)

- Effective potential

- Effective potential

Miyahara, Hyodo, Weise, PRC 98 (2018)

Constructed from chiral amp.



- Enhancement by $\bar{K}^0 p (\bar{K}N I = 1)$ is sizable.
- Prediction for the future $K_0 p$ data

$\Lambda\Lambda$ - $N\Xi$ interaction and $\Lambda\Lambda$ and $p\Xi^-$ correlation function

- $\Lambda\Lambda$ - $N\Xi$ interaction ($S = -2$) and H -dibaryon

- Long history of discussion on $(J, I) = (0, 0)$ sector related to $H(uuddss)$ -dibaryon.

R. L. Jaffe, PRL 38 (1977), 195.

- Binding energy of double Λ hypernucleus

→ $\Lambda\Lambda$ does NOT (deeply) bound

Takahashi et al., PRL87 (2001) 212502.

- STAR $\Lambda\Lambda$ correlation

L. Adamczyk et al. [STAR] PRL 114 (2015).

→ weak $\Lambda\Lambda$ interaction

- $\Lambda\Lambda$ - $N\Xi$ coupled-channel system

→ Possibility of $N\Xi$ quasibound

- HAL QCD $\Lambda\Lambda$ - $N\Xi$ coupled-channel potential

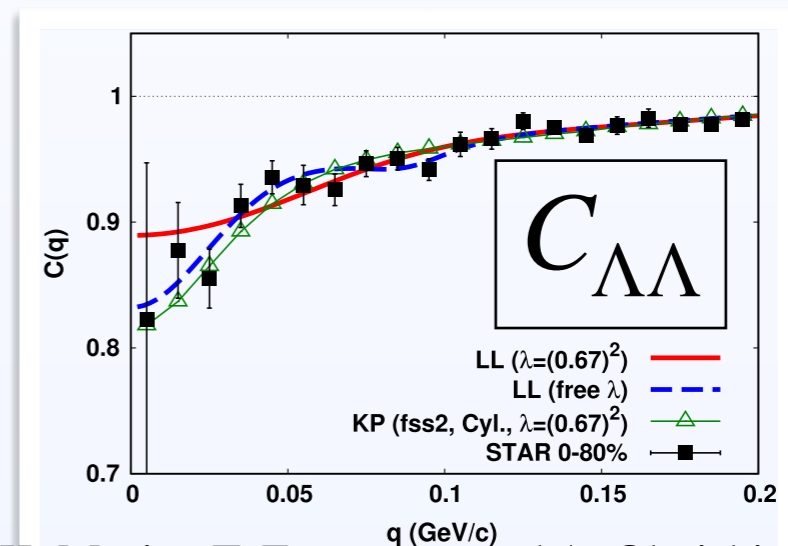
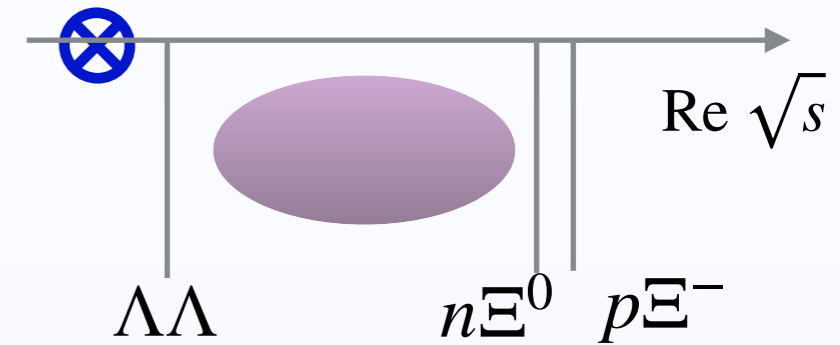
K. Sasaki et al. [HAL QCD], NPA 998 (2020), 121737.

- Strong attraction in $J = 0, I = 0$ $N\Xi$ channel

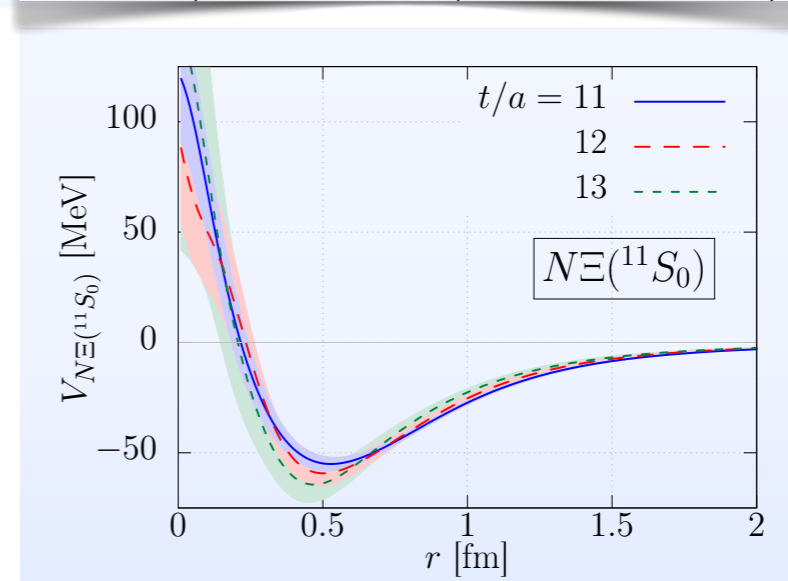
$$a_0^{p\Xi^-(J=0)} = -1.21 - i1.52$$

H dibaryon state is just barely unbound.

Fate of H -dibaryon?



K. Morita, T. Furumoto, and A. Ohnishi, PRC91(2015)



$\Lambda\Lambda$ - $N\Xi$ interaction and $\Lambda\Lambda$ and $p\Xi^-$ correlation function

$\Lambda\Lambda$ correlation function

$$C_{\Lambda\Lambda} = 1 - \frac{1}{2} e^{-4q^2 R^2} \quad \text{Quantum statistics (QS) for octet-octet}$$

$$+ \frac{1}{2} \sum_j \omega_j \int d^3r S_j(r) [|\psi_{j,s}(r)|^2 - |j_0(r)|^2 \delta_{j1}]$$

ALICE $p\text{Pb}$, pp collisions data

S. Acharya et al. [ALICE], PLB 797 (2019).

$N\Xi$ cusps related to the coupling and existence of H-dibaryon

J. Haidenbauer, Nucl. Phys. A 981 (2019),

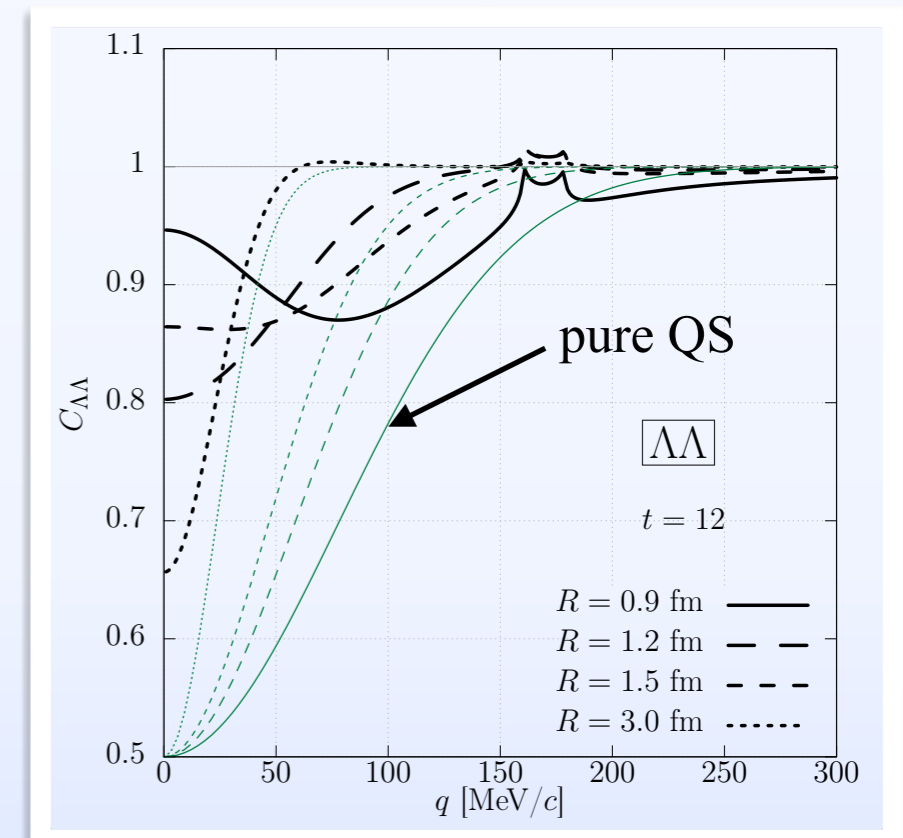
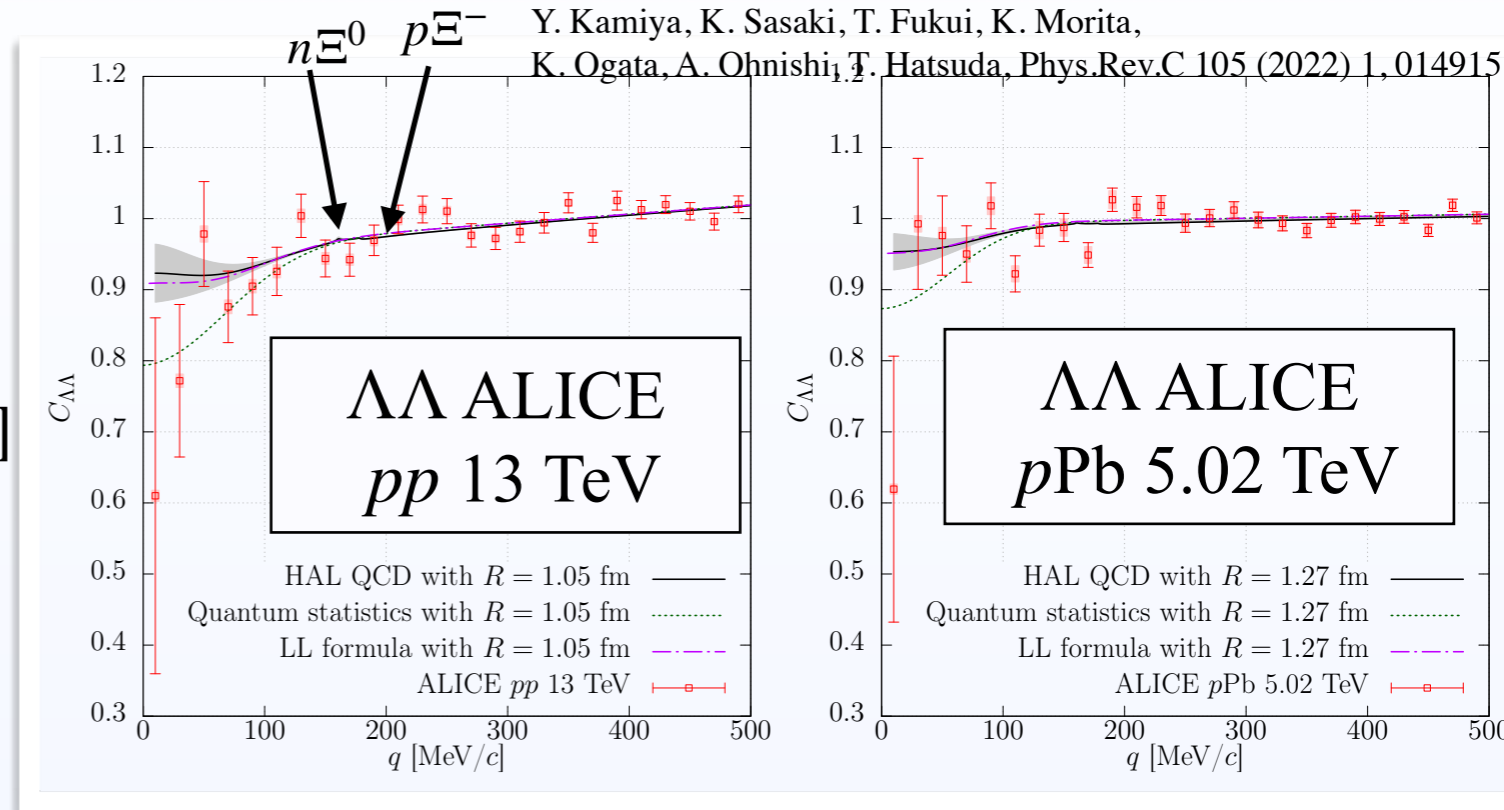
→ Almost invisible due to small coupling

Small source size dependence

Small deviation from QS effect

Due to the small scat. length: $a_0 = -0.78$ fm

→ Weak attraction of $\Lambda\Lambda$ confirmed
There is no signal of H-dibaryon



$\Lambda\Lambda$ - $N\Xi$ interaction and $\Lambda\Lambda$ and $p\Xi^-$ correlation function

Y. Kamiya, K. Sasaki, T. Fukui, K. Morita,
K. Ogata, A. Ohnishi, T. Hatsuda, Phys.Rev.C 105 (2022) 1, 014915

$p\Xi^-$ correlation function

$$C_{p\Xi^-} = \frac{1}{4} C_{p\Xi^-, \text{singlet}} \text{ (Couples to } \Lambda\Lambda \text{ (H-dibaryon channel))} + \frac{3}{4} C_{p\Xi^-, \text{triplet}}$$

ALICE data

pp : ALICE Nature 588 (2020)

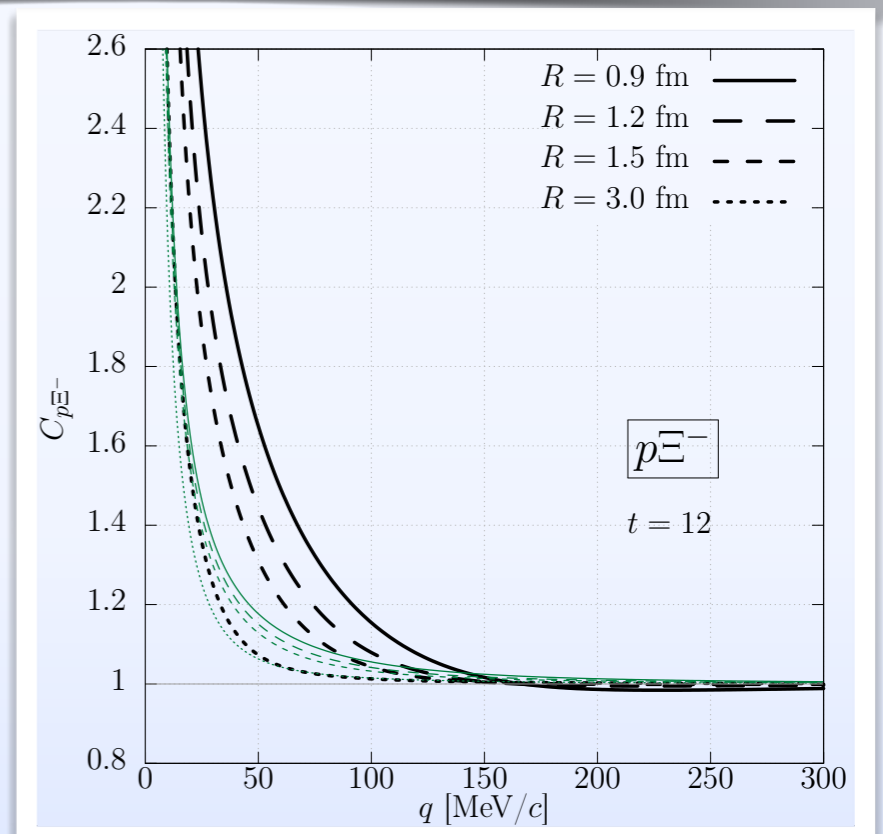
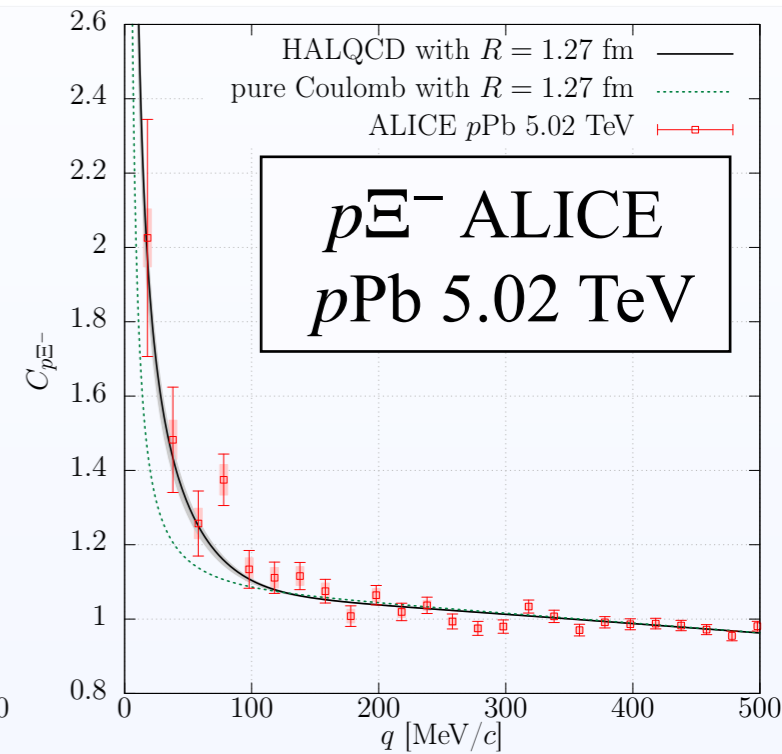
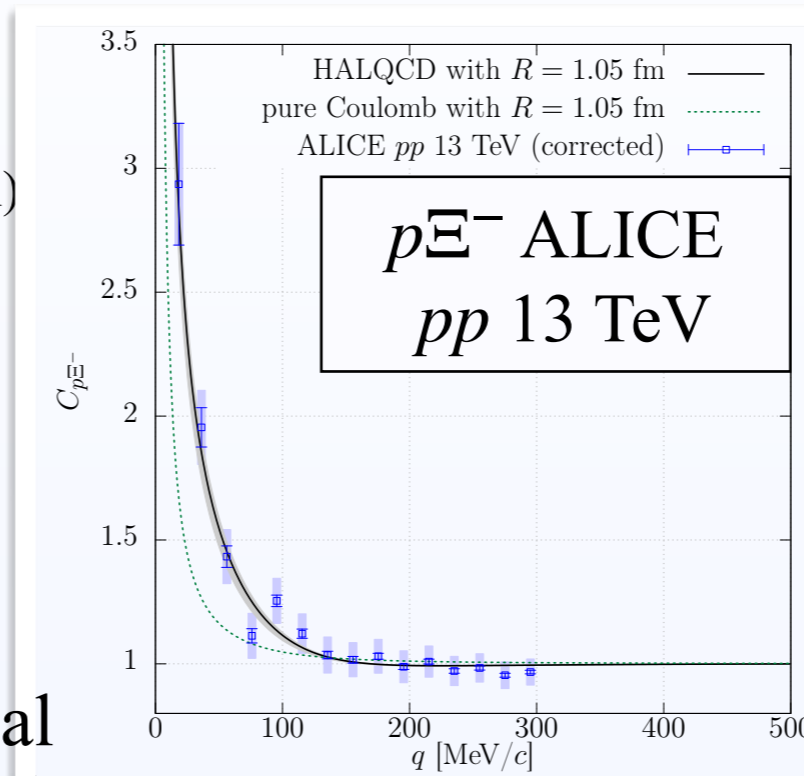
pPb : ALICE PRL 123 (2019).

in good agreement w/ HAL potential

- Small coupled-channel source effect
- No dip structure for every source sizes
→ No dibaryon state
- Source size dependence
Small R : sizable enhancement (from Coulomb)
Large R : Coulomb effect dominant

Barely unbound scenario:

Good agreement for both channels ($\Lambda\Lambda$, $p\Xi^-$)



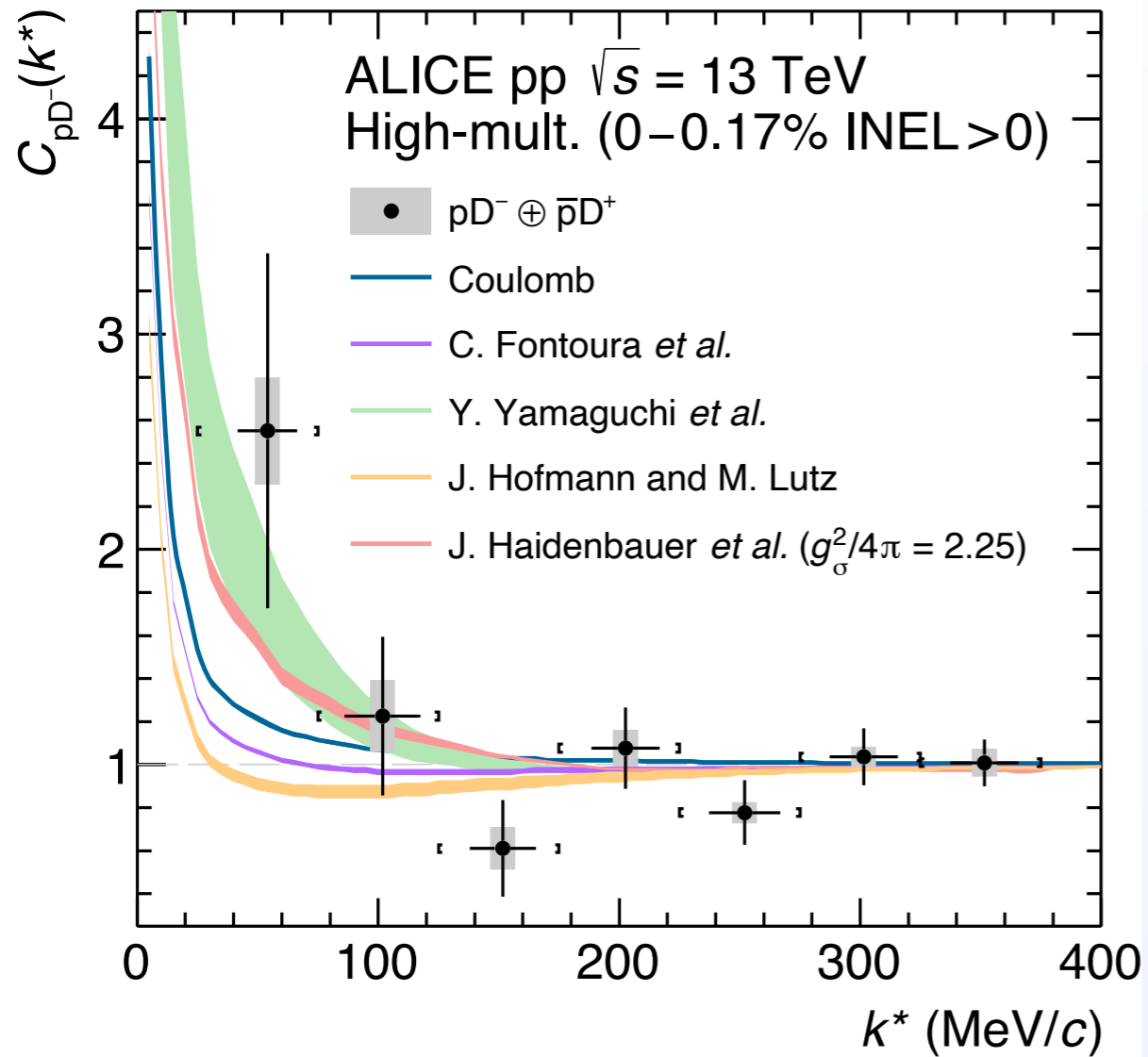
$\bar{D}N$ interaction and D^-p correlation function

• $\bar{D}(\bar{c}l)N$ interaction ($C = -1$)

Poster by D. Battistini

$f_0 \equiv \mathcal{F}(E = E_{\text{th}})$
 + : attractive w/o bound
 - : repulsive
 or attractive w/ bound

• D^-p correlation function ALICE arXiv [2201.05352]



• Model scattering lengths f_0

Model	$f_0 (I=0)$	$f_0 (I=1)$	n_σ
Coulomb			(1.1–1.5)
Haidenbauer et al. [21]			
– $g_\sigma^2/4\pi = 1$	0.14	–0.28	(1.2–1.5)
– $g_\sigma^2/4\pi = 2.25$	0.67	0.04	(0.8–1.3)
Hofmann and Lutz [22]	–0.16	–0.26	(1.3–1.6)
Yamaguchi et al. [24]	–4.38	–0.07	(0.6–1.1)
Fontoura et al. [23]	0.16	–0.25	(1.1–1.5)

- pure Coulomb case is compatible with data
- Better agreement with strongly attractive interaction models for $I = 0$.
- pion exchange model of Yamaguchi et al. predicting 2 MeV bound state gives the lowest n_σ

* Background including miss PID is subtracted

$\bar{D}N$ interaction and D^-p correlation function

• Constraint on $I = 0$ scattering length f_0

ALICE arXiv [2201.05352]

- Analysis with one range Gaussian potential

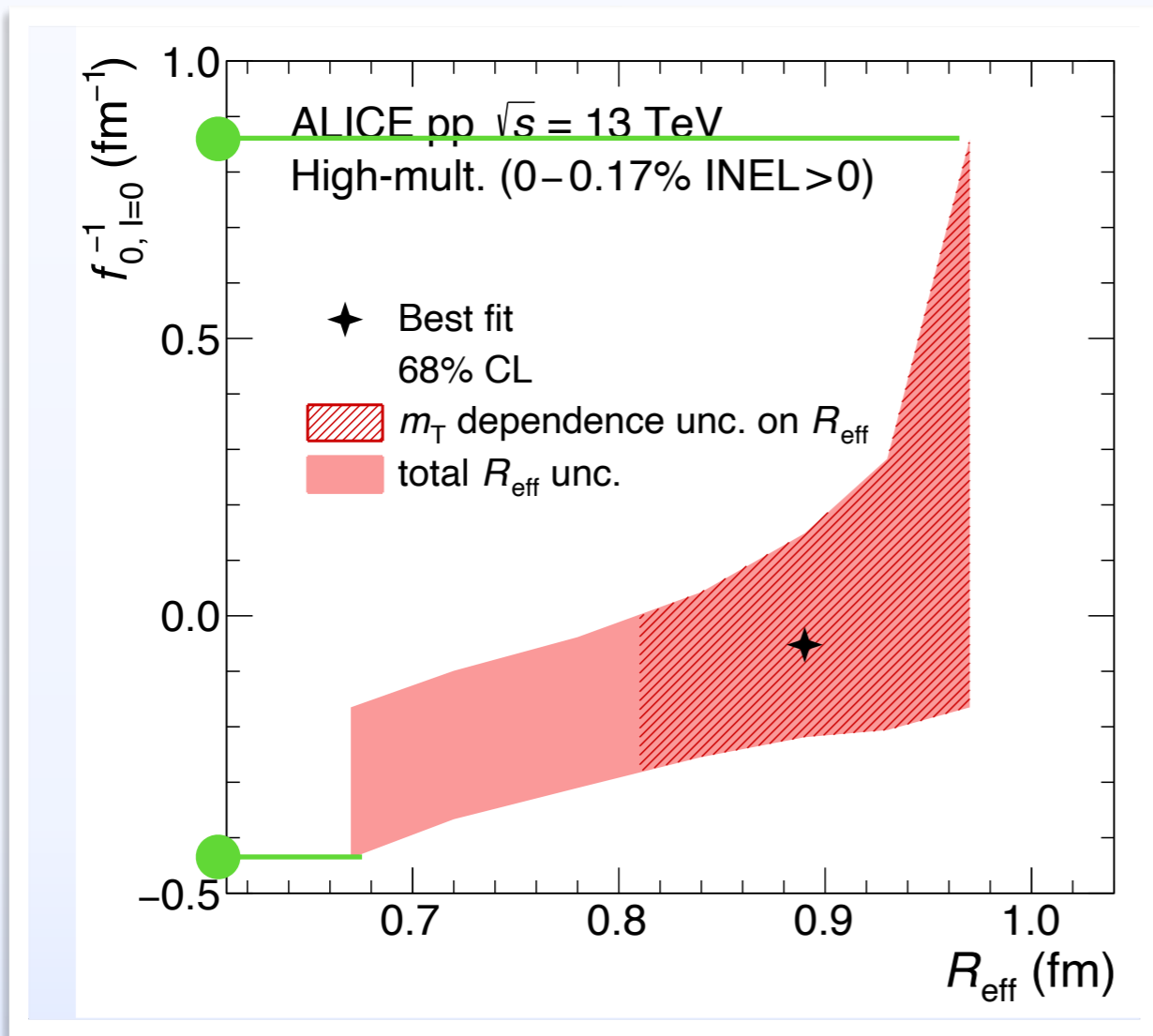
$$V(r) = V_0 \exp(-m^2 r^2)$$

- $m \leftarrow \rho$ exchange ($m = m_\rho$)

- Assume negligible $I = 1$ int.

- Constraint on $f_{0, I=0}$

$f_0 \equiv \mathcal{F}(E = E_{\text{th}})$
 + : attractive w/o bound
 - : repulsive
 or attractive w/ bound



- 1σ constraint $\rightarrow f_{0, I=0}^{-1} \in [-0.4, 0.9] \text{ fm}^{-1}$:
- strongly attractive with or without bound state
- * Most models predicts repulsive int. for $I = 1$
 $\rightarrow I = 0$ may have more attraction in reality.

DN interaction and D^+p correlation function

- $D(c\bar{l})N$ interaction ($C = 1$)

- Model scattering lengths ($I = 1$)

Modes	$a_0^{DN(I=1)}$ [fm]	bound state ($I = 1$)
[1] J. Hofmann and M. Lutz, NPA 763 (2005).	-0.41	2620 - i 1
[2] T. Mizutani and A. Ramos, PRC 74 (2006).	-1.47 + i 0.65	2695 - i 77
[3] C. Garcia-Recio et al., PRD 79 (2009).	0.33 + i 0.05	2637 - i 40
[4] J. Haidenbauer, et. al. EPJA 47 (2011).	-2.07 + i 0.57	2793 - i 6
[5] U. Raha, et. al.. PRC98 (2018).	-0.764 + i 0.615(D^0n)	2806 - i 72

$$a_0 \equiv \mathcal{F}(E = E_{\text{th}})$$

+ : attractive w/o bound

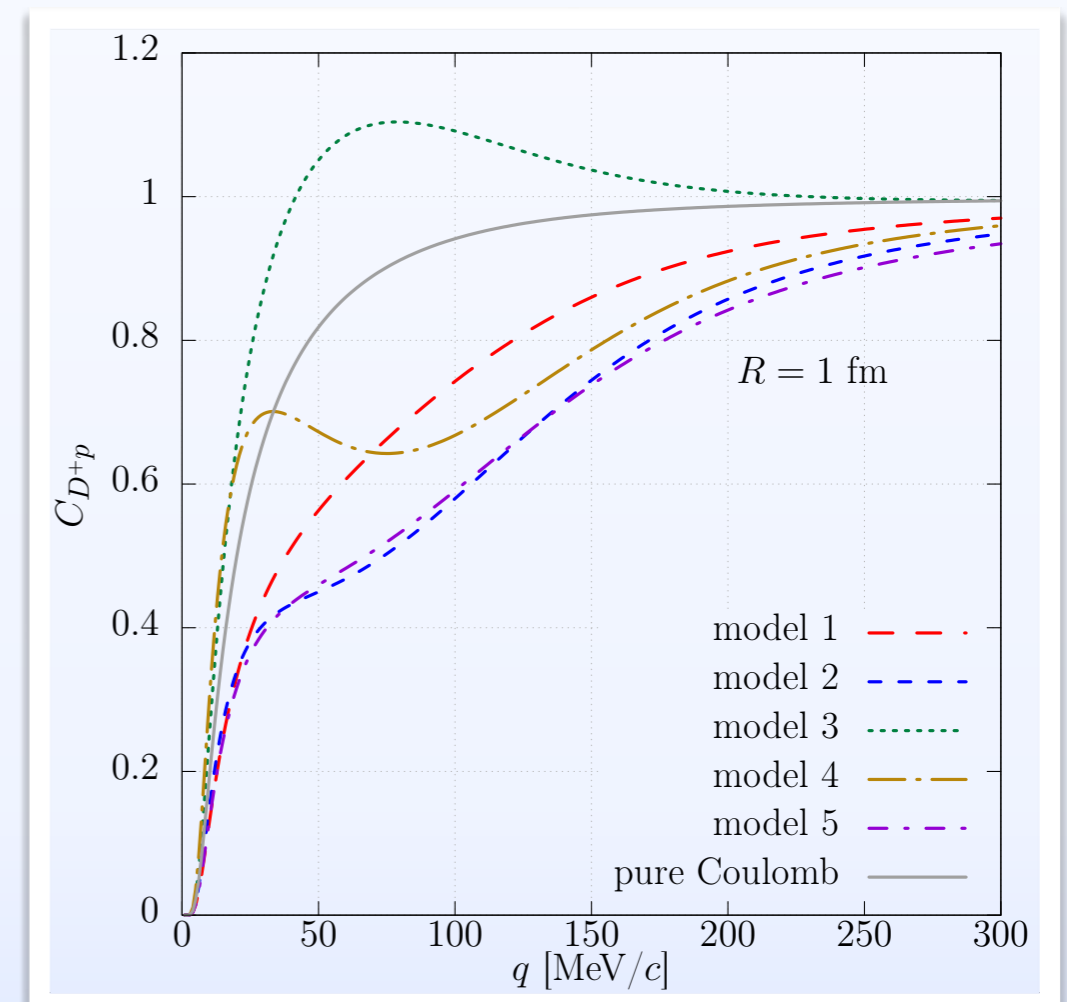
- : repulsive

or attractive w/ bound

- D^+p channel: only $I = 1$ interaction
- Complex value of a_0 due to decay channels
- Large uncertainty for pole position and scat. lengths

- D^+p correlation

- Gaussian potential ($I = 1$) and Gaussian source
- Depending on the interaction (scattering length), C_{D^+p} shows enough enhancement, suppression.

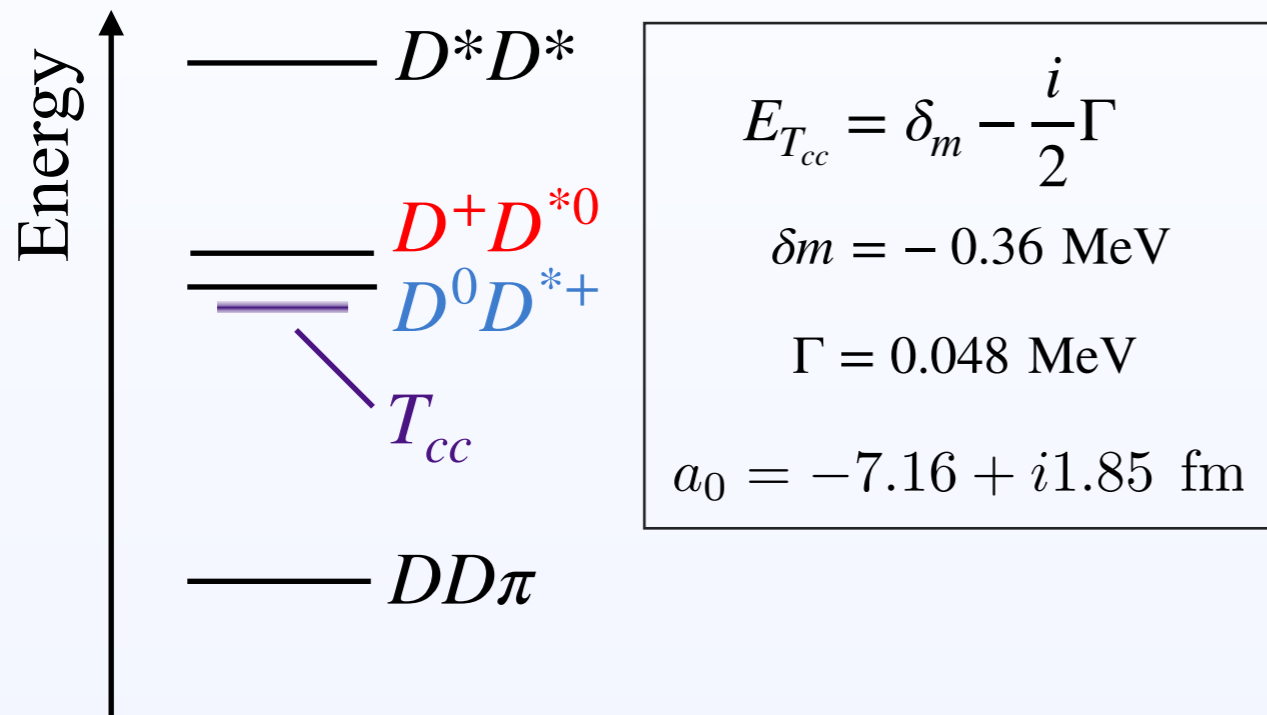


DD^* and $D\bar{D}^*$ int. from femtoscopy

• DD and $D\bar{D}$ sector

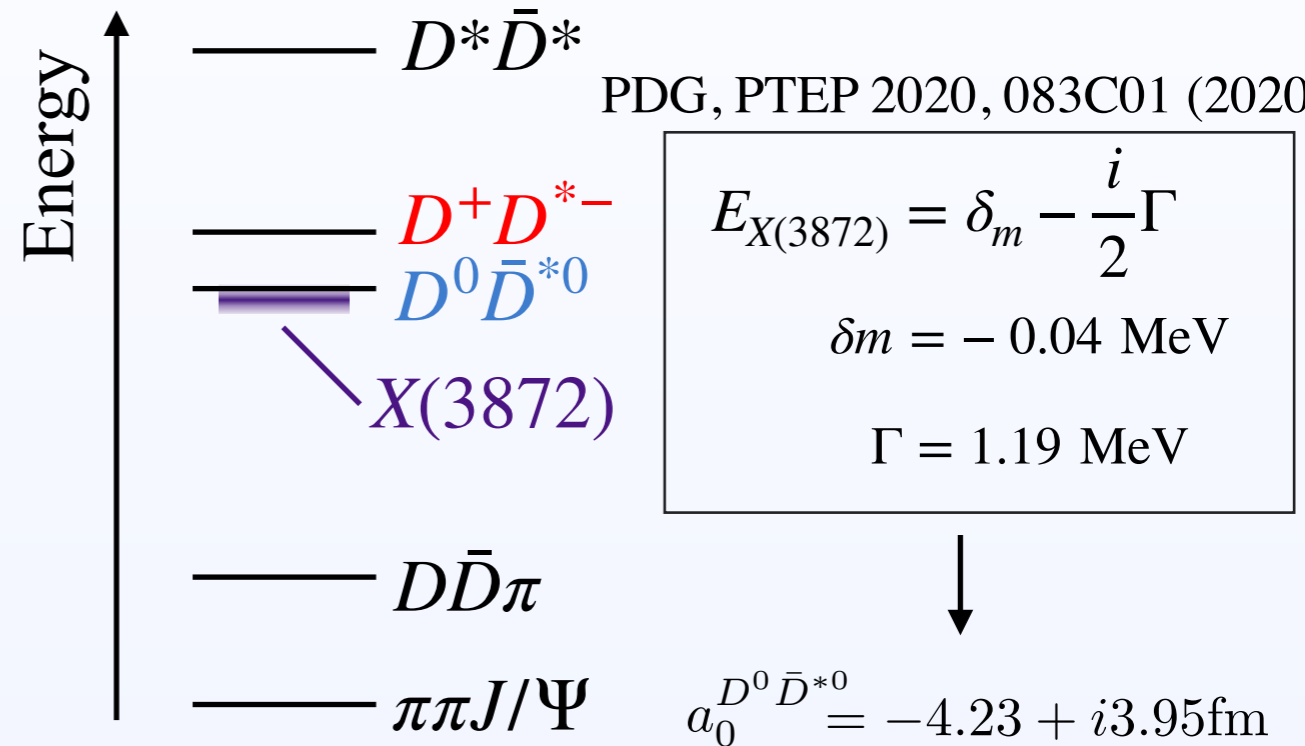
$C = 2$

LHCb, Nature Com. 13 (2022) 1



$C = 0$

PDG, PTEP 2020, 083C01 (2020).



$$a_0 \equiv \mathcal{F}(E = E_{\text{th}})$$

+ : attractive w/o bound

- : repulsive

or attractive w/ bound

- $T_{cc}/X(3872)$ lies nearby $DD^*/D\bar{D}^*$

==> meson-meson molecule?

==> Strong attractive interaction

- Gaussian potential

$$V(r) = V_0 \exp(-m^2 r^2)$$

- $m \leftarrow \rho$ exchange ($m = m_\rho$)

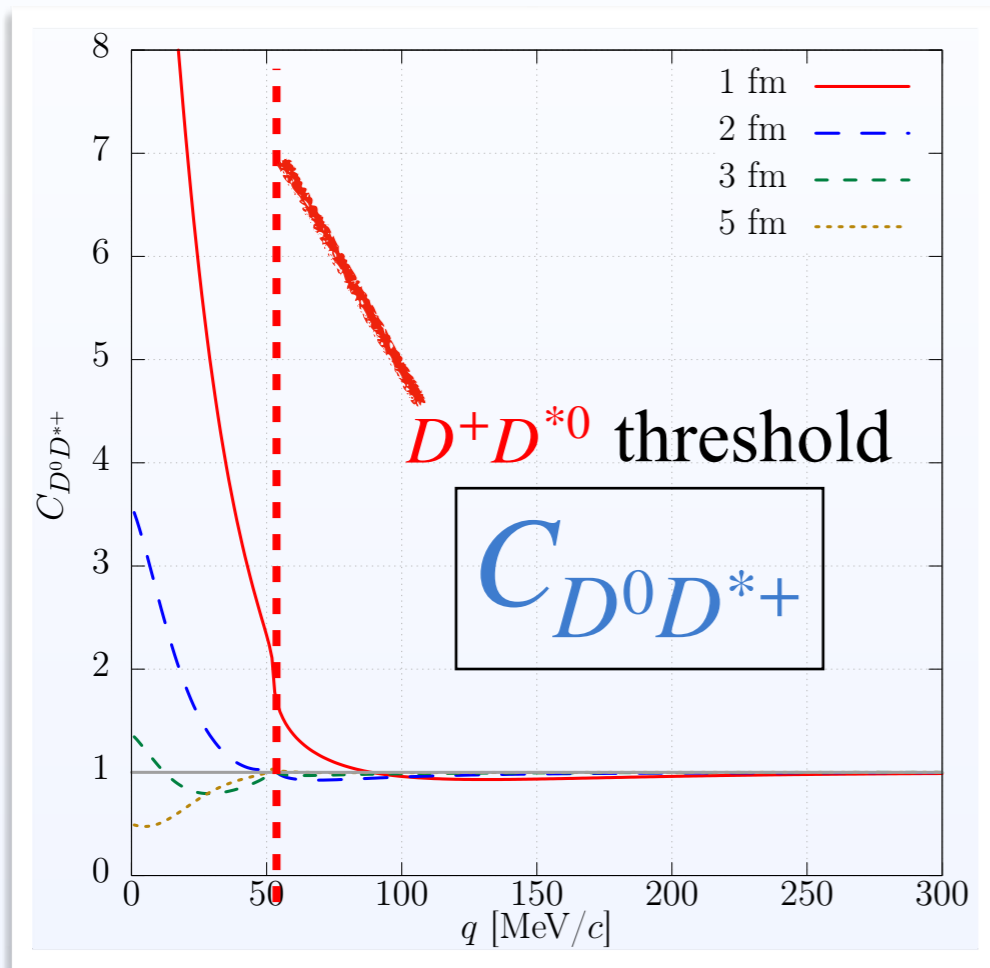
- $V_0 \leftarrow$ scattering lengths

- Assume dominant contribution from exotic channel ($I = 0$)

- Coupled-channel of two isospin channels

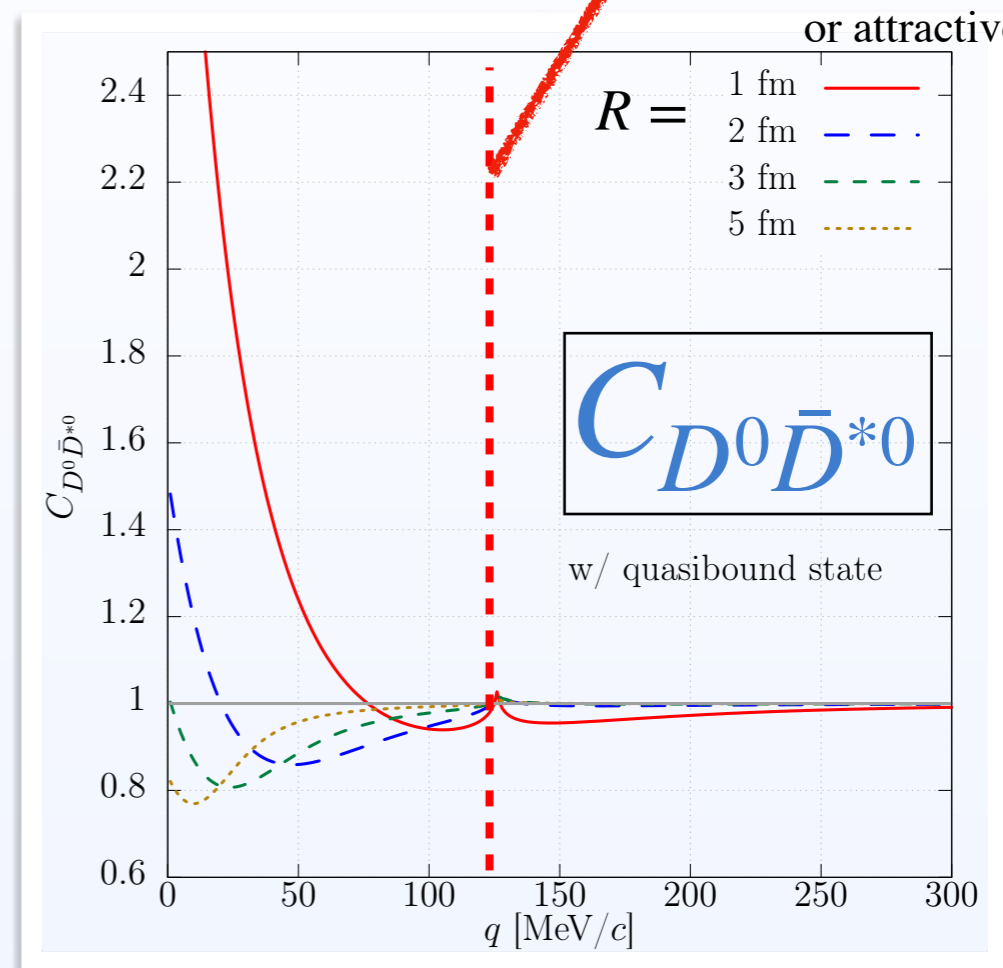
DD^* and $D\bar{D}^*$ int. from femtoscopy

DD



$D\bar{D}$

$a_0 \equiv \mathcal{F}(E = E_{\text{th}})$
 $D^+ D^{*-}$ threshold
 + : attractive w/o bound
 - : repulsive
 or attractive w/ bound



- Larger signal in the lower channels
- Bound state like behavior for both pairs
- Clear source size dependence
- Moderate $D^+ D^{*0}/D^+ D^{*-}$ cusp

DD^* and $D\bar{D}^*$ int. from femtoscopy

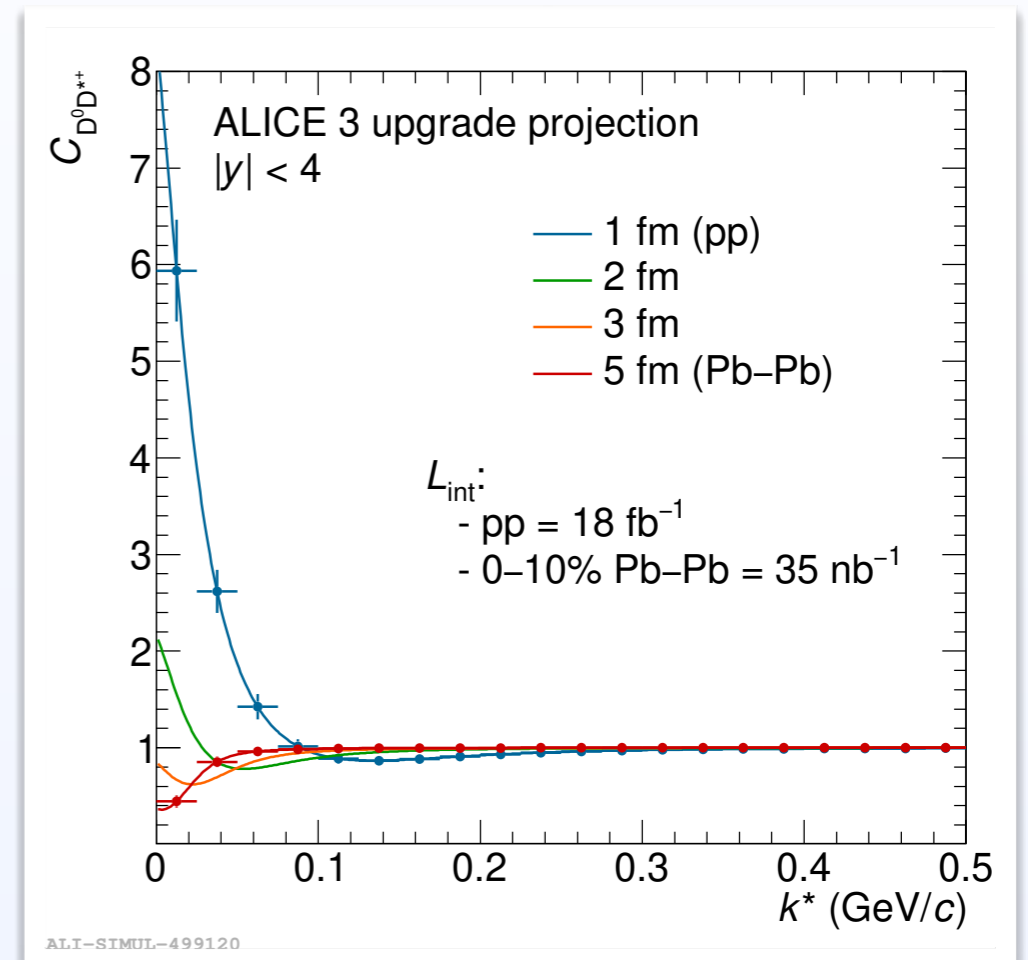
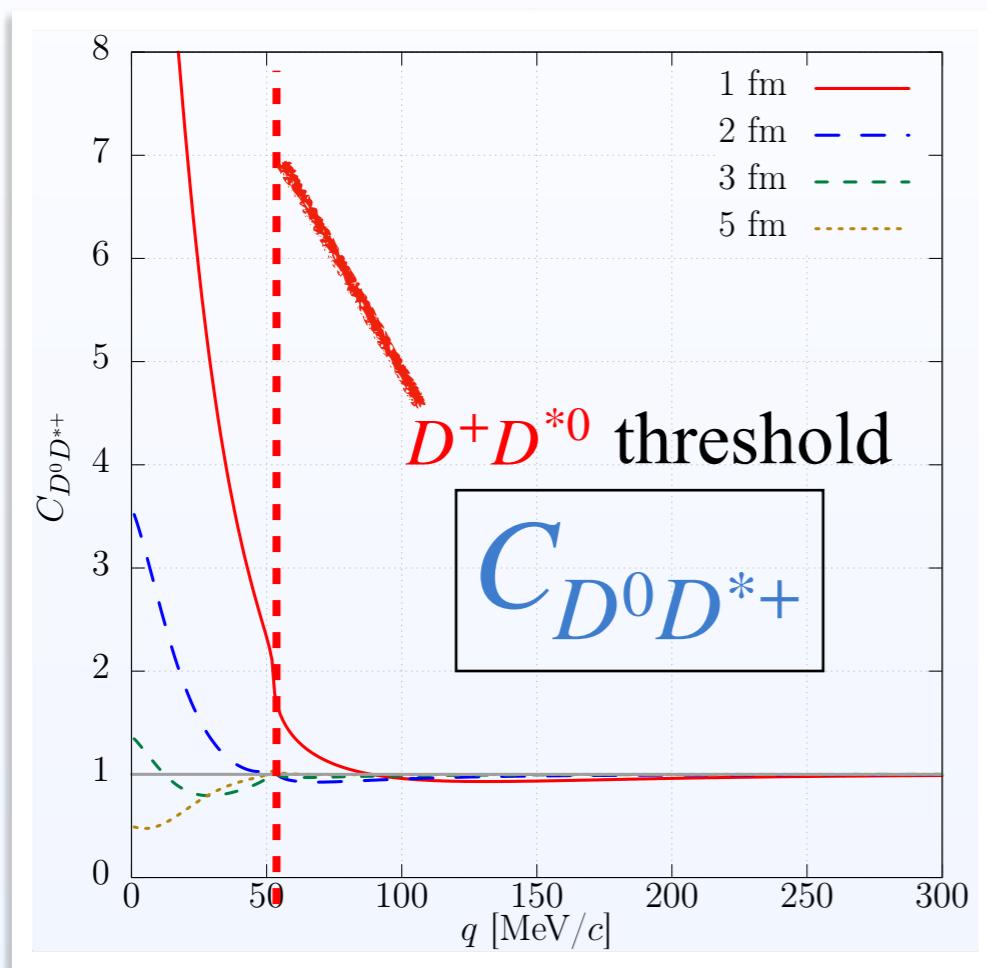
● DD

$$a_0 \equiv \mathcal{F}(E = E_{\text{th}})$$

+ : attractive w/o bound

- : repulsive

or attractive w/ bound



ALICE collab., CERN-LHCC-2022-009 (2022).

- Larger signal in the lower channels
- Bound state like behavior for both pairs
- Clear source size dependence
- Moderate $D^+ D^{*0}/D^+ D^{*-}$ cusp

- Well investigated
with future ALICE 3 upgrade

Summary

- Femtoscopic correlation function in high energy nuclear collisions is a powerful tool to investigate the hadron-hadron interaction.
- Source size dependence is important to see the interaction detail especially for the coupled-channel case.
- K^-p
Chiral SU(3) dynamics model is consistent with the large source data while small deviation is found in small source data.
- $\Lambda\Lambda-p\Xi^-$
Coupled-channel HAL-QCD potential is consistent with current data from pp and pPb collisions.
- D^-p
Non-interacting model can explain data but strong attractive interaction reduce the standard deviation.
- $DD^*/D\bar{D}^*$
The lower isospin partner channels are expected to show the strong source size dependence due to the near threshold $T_{cc}/X(3872)$ states.

Thank you for your attention!

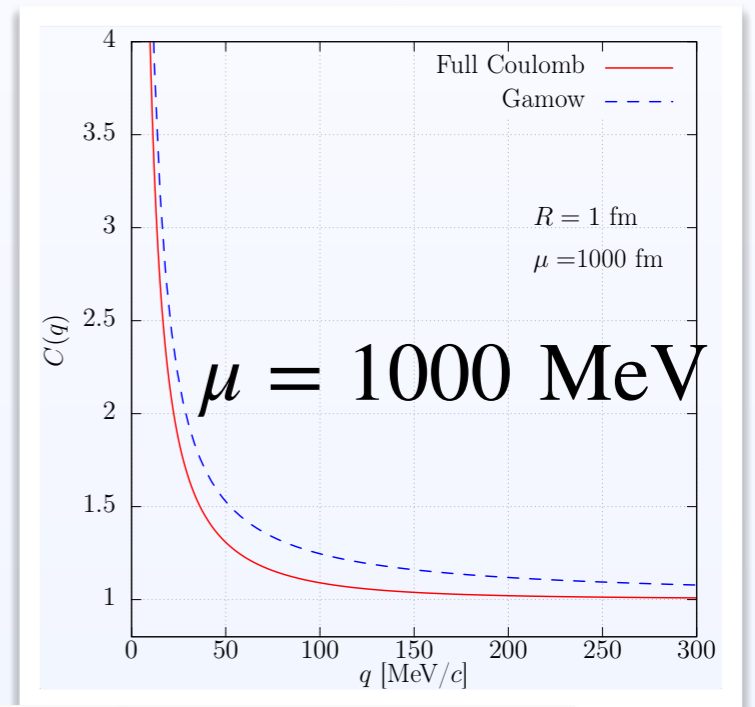
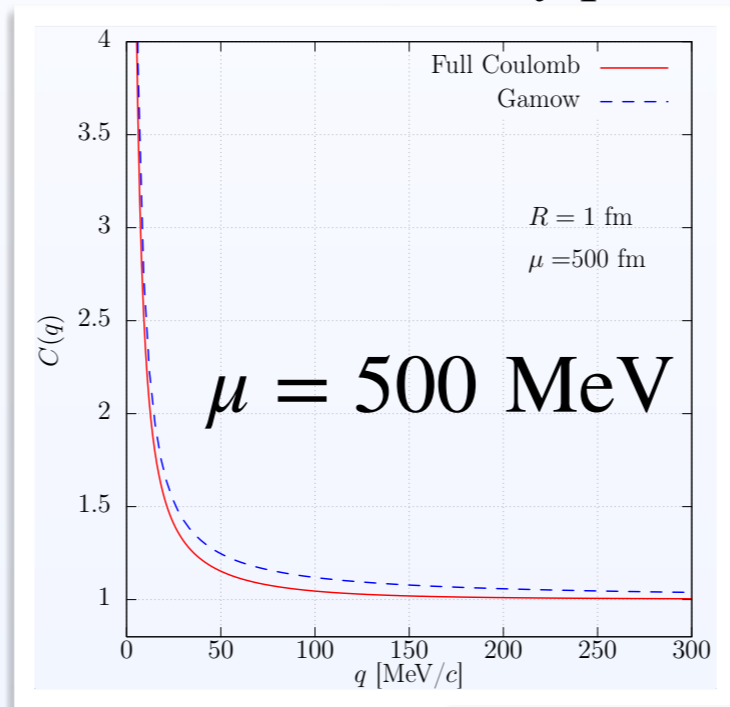
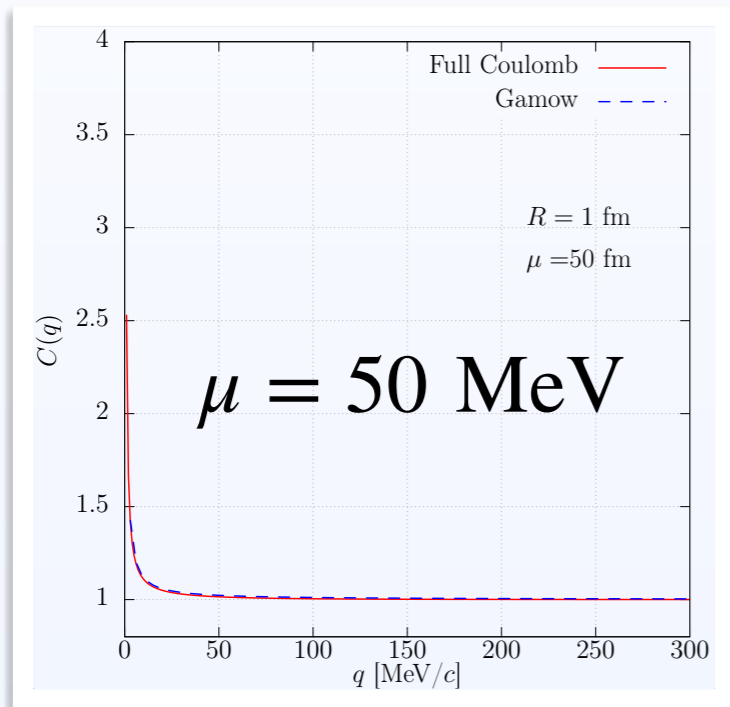
The background features a decorative pattern of swirling, concentric lines in shades of purple, blue, and orange, set against a dark purple gradient. A horizontal band of a slightly lighter purple color runs across the middle of the page, containing the text.

Thank you!

Coulomb interaction

- Coulomb interaction: Full calculation

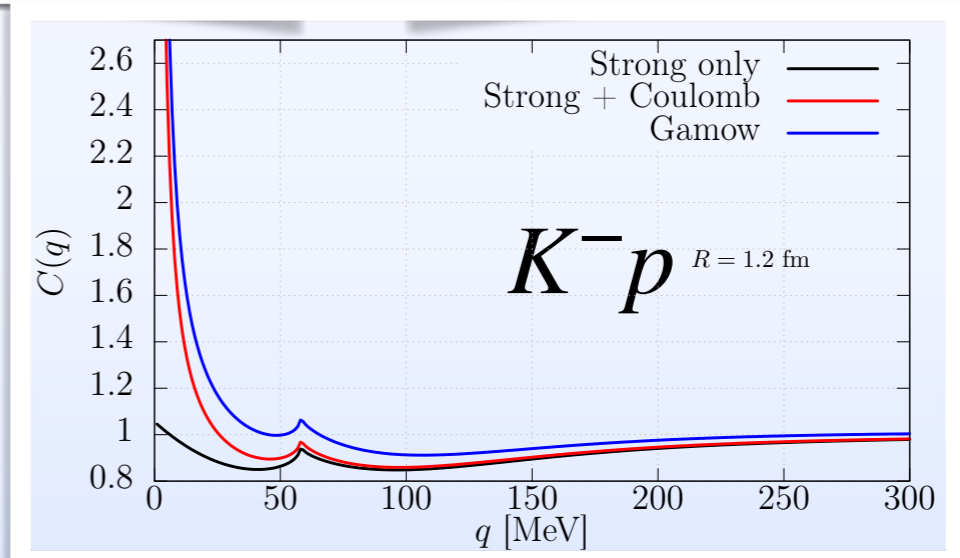
- For the quantitative discussion, fully calculated Coulomb w.f. ψ^C is needed:
 - $[H_0 + V]\psi^C = E\psi^C$ with $V = V_{\text{strong}} + V_{\text{Coulomb}}$
- Pure Coulomb cases ($V_{\text{strong}} = 0$)
 - LL formula over estimates the Coulomb int. for heavy particle pairs.



- With strong int. ($V_{\text{strong}} \neq 0$)
 - Interference of V_{strong} and V_{Coulomb}



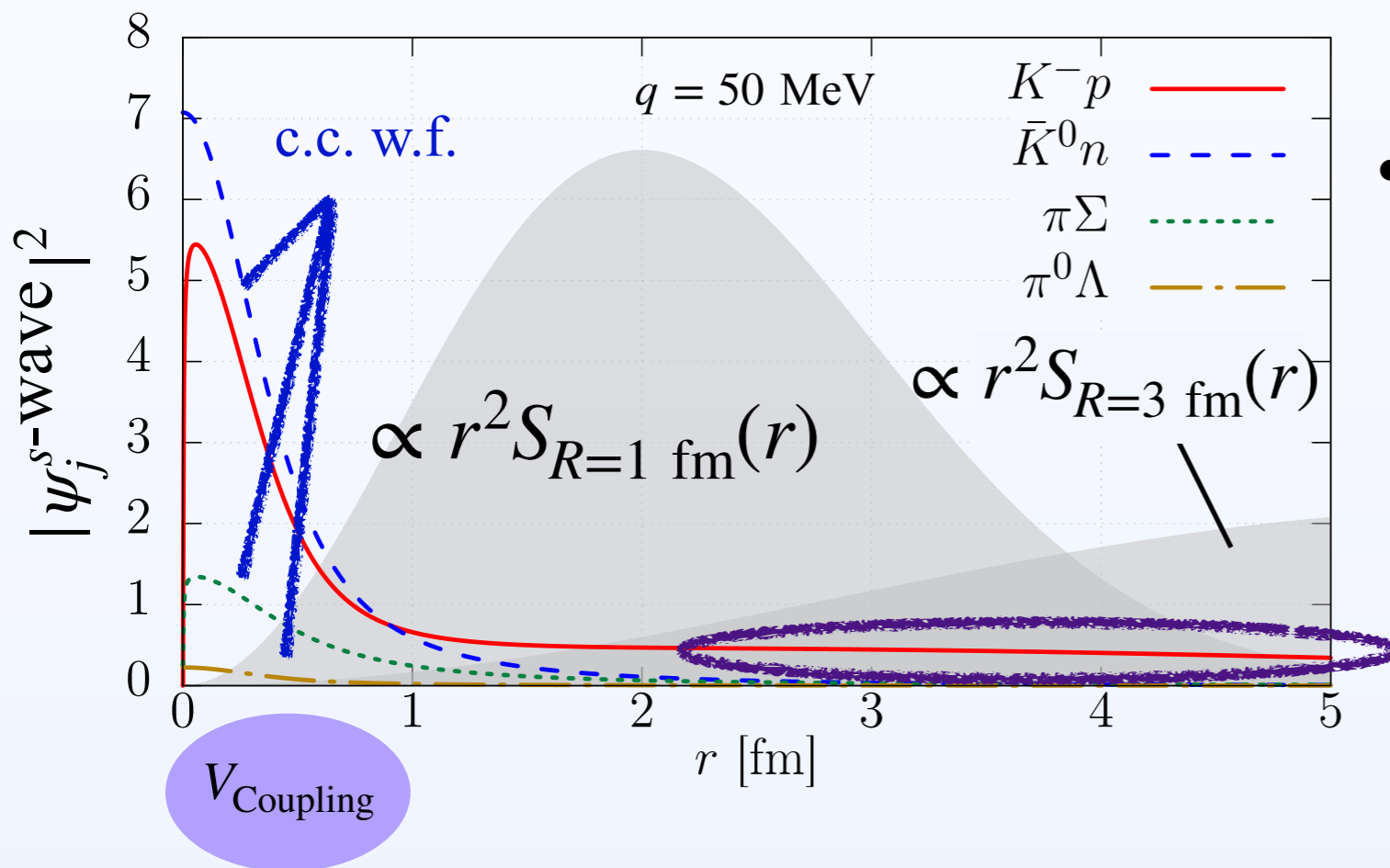
- For the femtoscopic study, full calculation is mandatory.



Source size dependence

- Coupled-channel wave function

$$C_{K^-p}(\mathbf{q}) = \int d^3\mathbf{r} S_{K^-p}(\mathbf{r}) |\psi_{K^-p}^{C,(-)}(q; r)|^2 + \sum_{j \neq i} \omega_j \int d^3\mathbf{r} S_j(\mathbf{r}) \underbrace{|\psi_j^{C,(-)}(q; r)|^2}_{\text{Coupled-channel wave function } \bar{K}^0 n, \pi^0 \Sigma^0, \dots}$$



- Coupled-channel wave function satisfies the out-going boundary condition
 - Measured channel (K^-p) has out going wave
 - Coupled-channel w.f. emerges only in int. region

- Small source \implies W.F. of Coupled-channels counts
- Small source \implies Measured channel contribution dominant

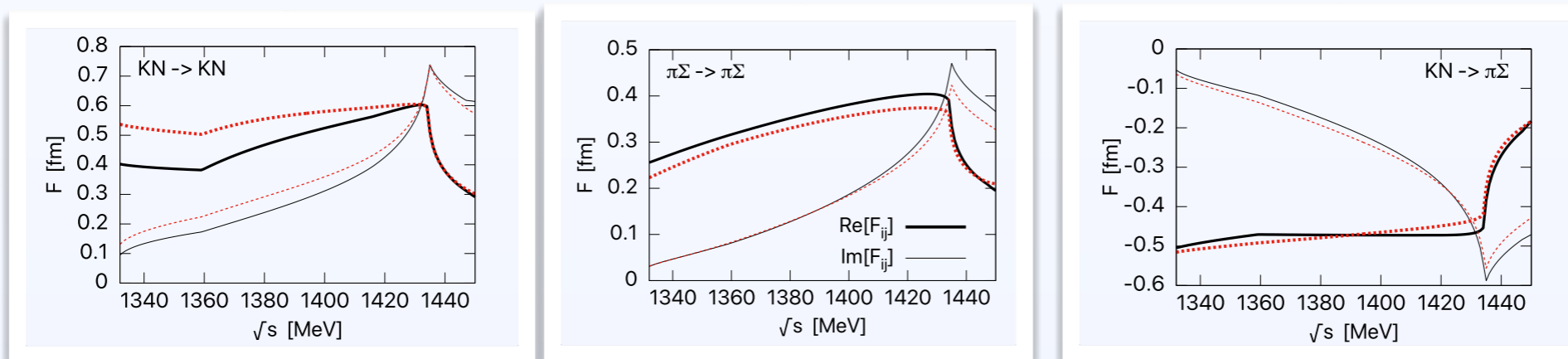
$\bar{K}N$ interaction and K^-p correlation

- Chiral SU(3) based $\bar{K}N$ - $\pi\Sigma$ - $\pi\Lambda$ potential Miyahara, Hyodo, Weise, PRC 98 (2018)

- Constructed based on the amplitude with NLO chiral SU(3) dynamics Ikeda, Hyodo, Weise, NPA881 (2012)
- Coupled-channel, energy dependent as

$$V_{ij}^{\text{strong}}(r, E) = e^{-(b_i/2 + b_j/2)r^2} \sum_{\alpha=0}^{\alpha_{\text{max}}} K_{\alpha,ij} (E/100 \text{ MeV})^\alpha$$

- Constructed to reproduce the chiral SU(3) amplitude around the $\bar{K}N$ sub-threshold region



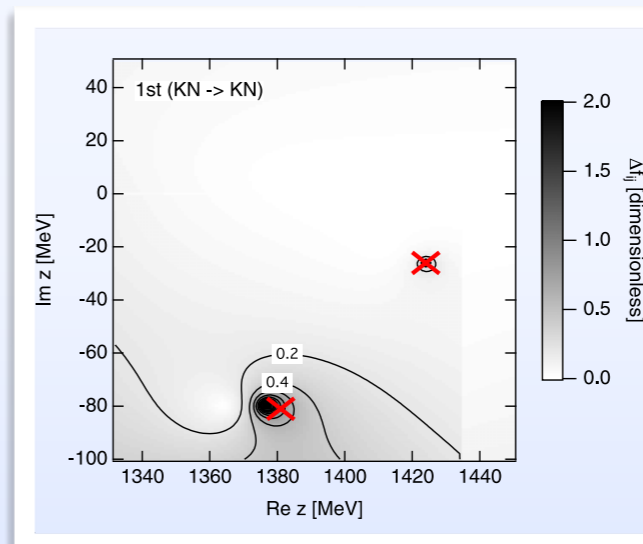
- Two pole structure of $\Lambda(1405)$: well reproduced

High-mass pole : $1424 - 27i$

Low-mass pole : $1380 - 81i$

Original chiral SU(3) : $1424 - 26i$

$1381 - 81i$



Comparison with ALICE data

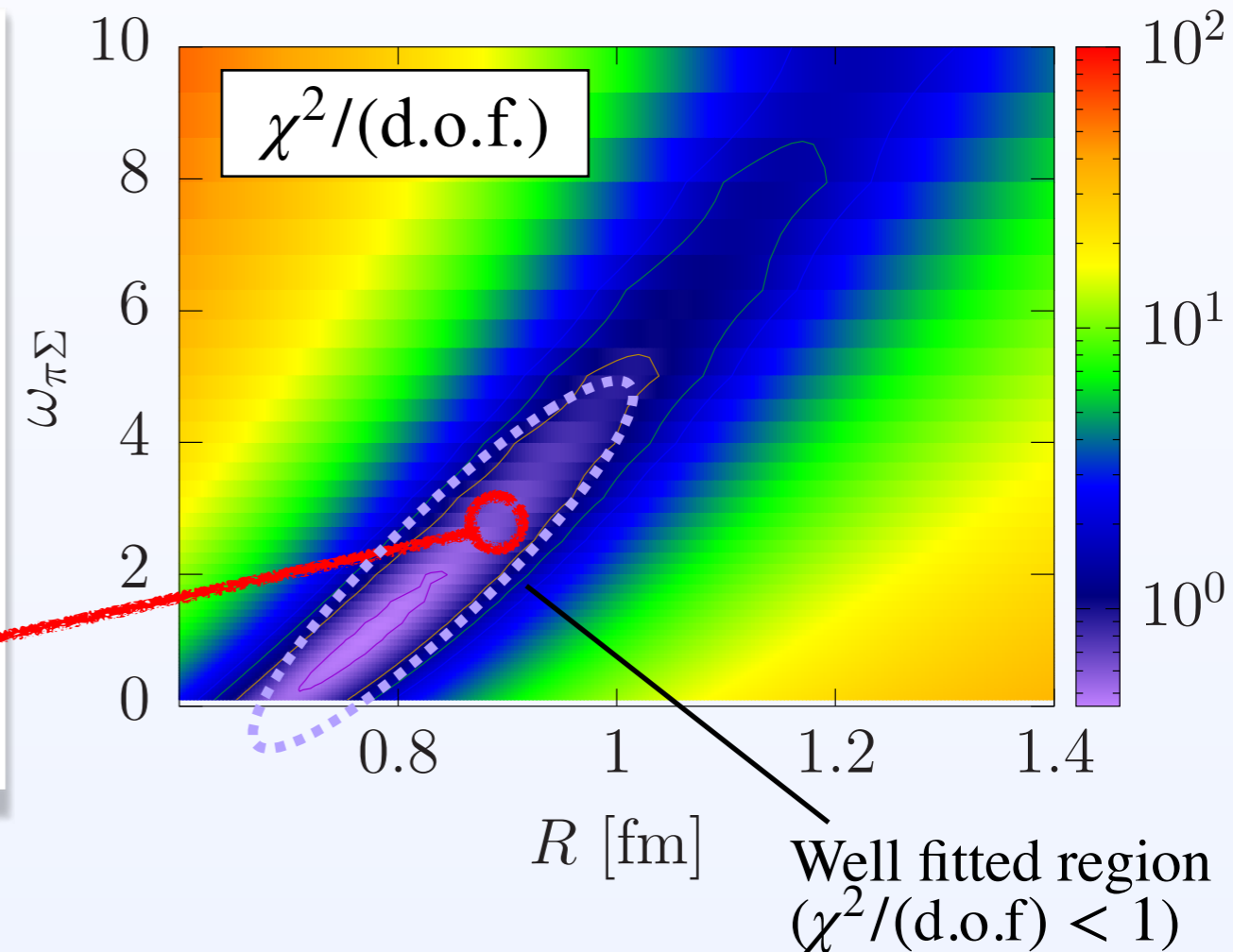
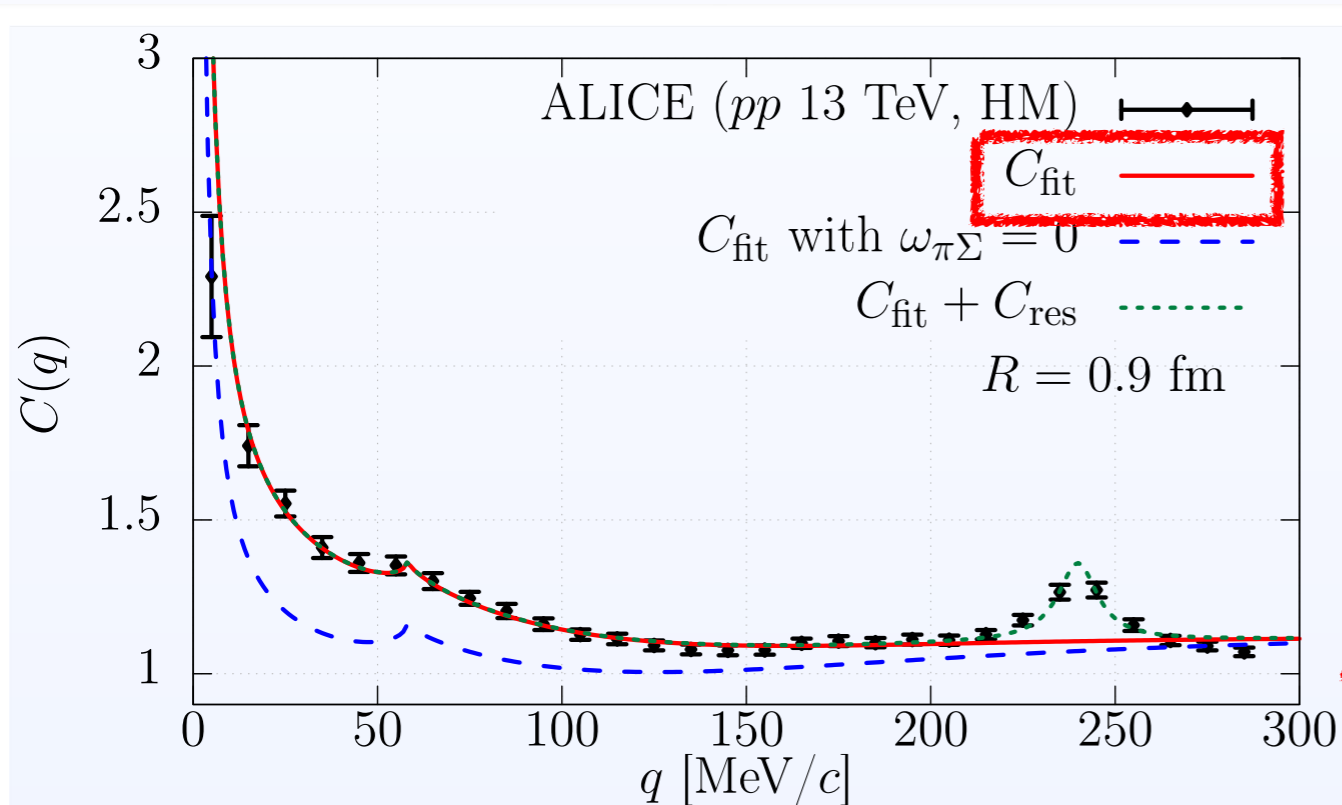
- Fitting result

- Fitting function

$$C_{\text{fit}}(q) = \mathcal{N}[1 + \lambda\{C_{K-p}(q) - 1\}]$$

$$C_{K-p}(q) = \sum_j \omega_j \int d^3\mathbf{r} S(\mathbf{r}) |\Psi_j^{C,(-)}(q, r)|^2$$

- Fitting range: $q < 120 \text{ MeV}/c$

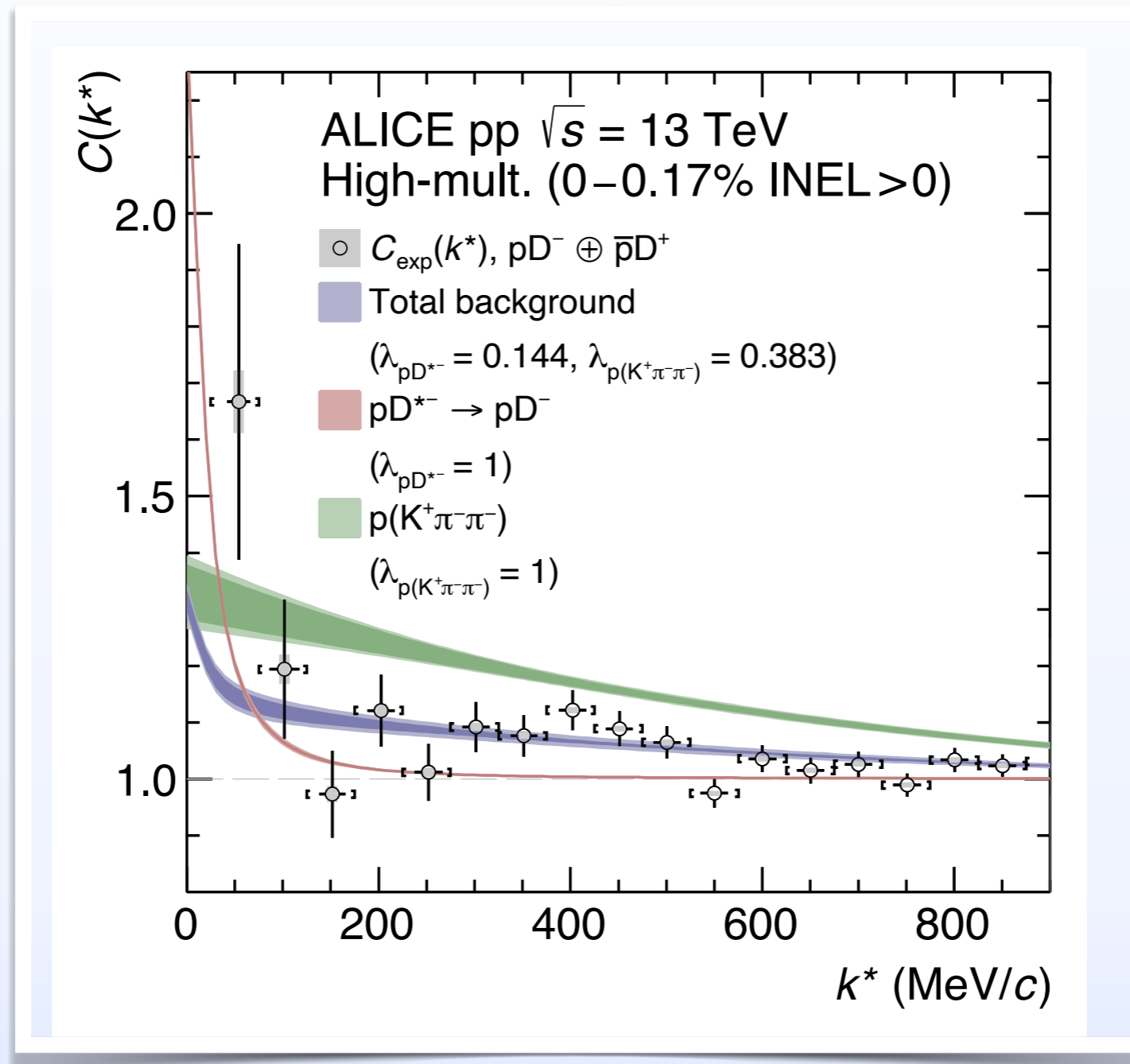


- ALICE data has been well reproduced with the reasonable values of parameters.
- Coupled-channel source contribution is essential to reproduce the data.

$\bar{D}N$ interaction and D^-p correlation function

- Background for D^-p correlation function

ALICE arXiv [2201.05352]



$\bar{D}N$ interaction and D^-p correlation function

● Constraint on $l = 0$ scattering length f_0

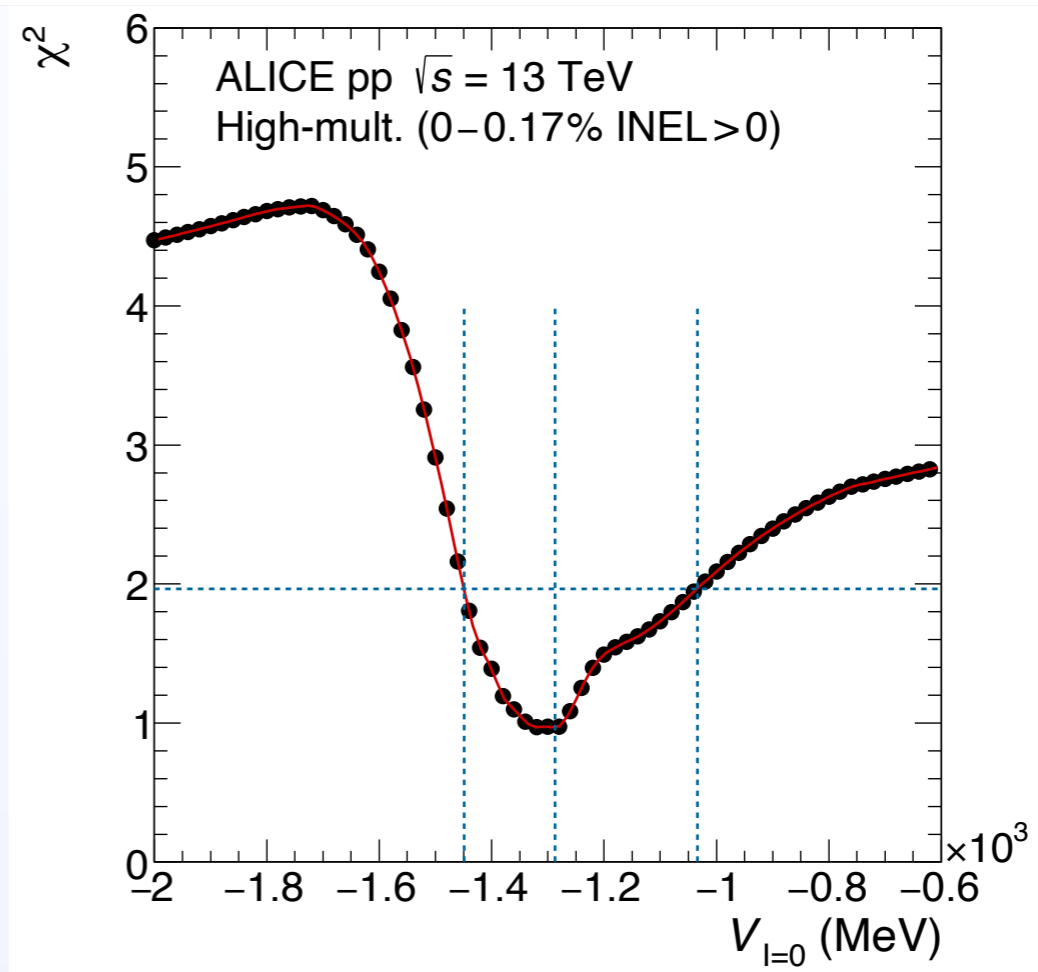
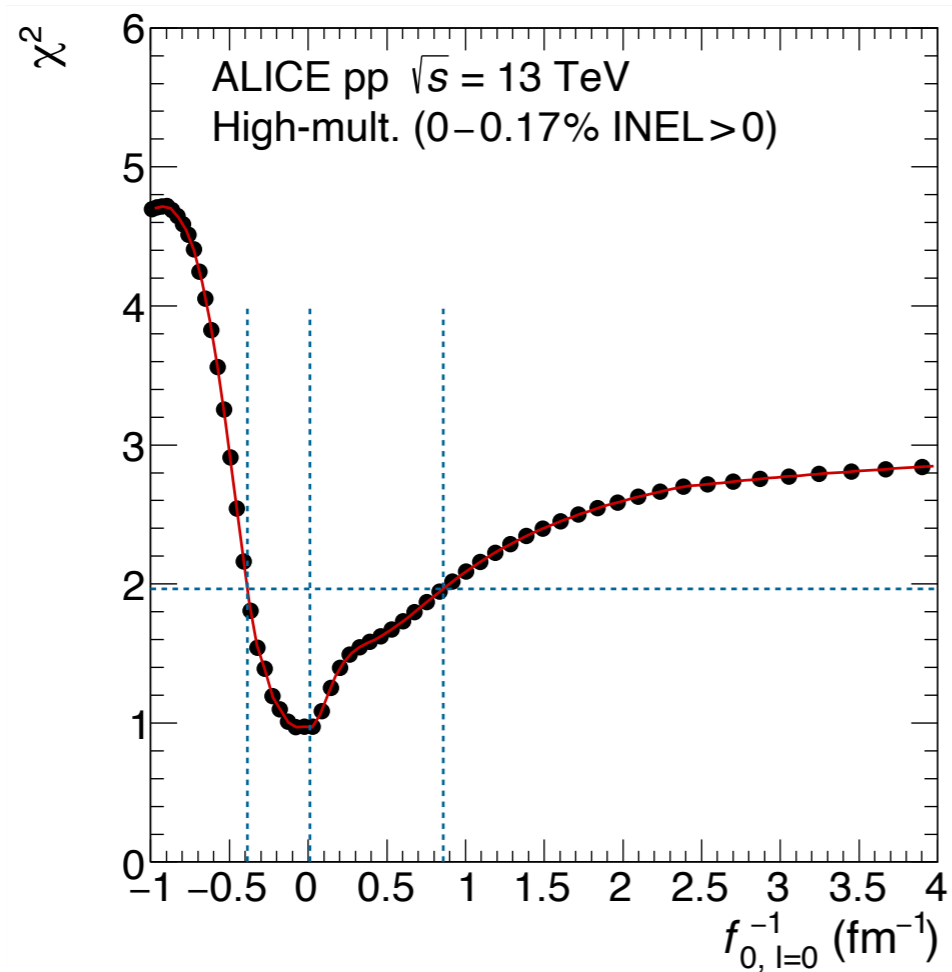
ALICE arXiv [2201.05352]

$$f_0 \equiv \mathcal{F}(E = E_{\text{th}})$$

+ : attractive w/o bound

- : repulsive

or attractive w/ bound



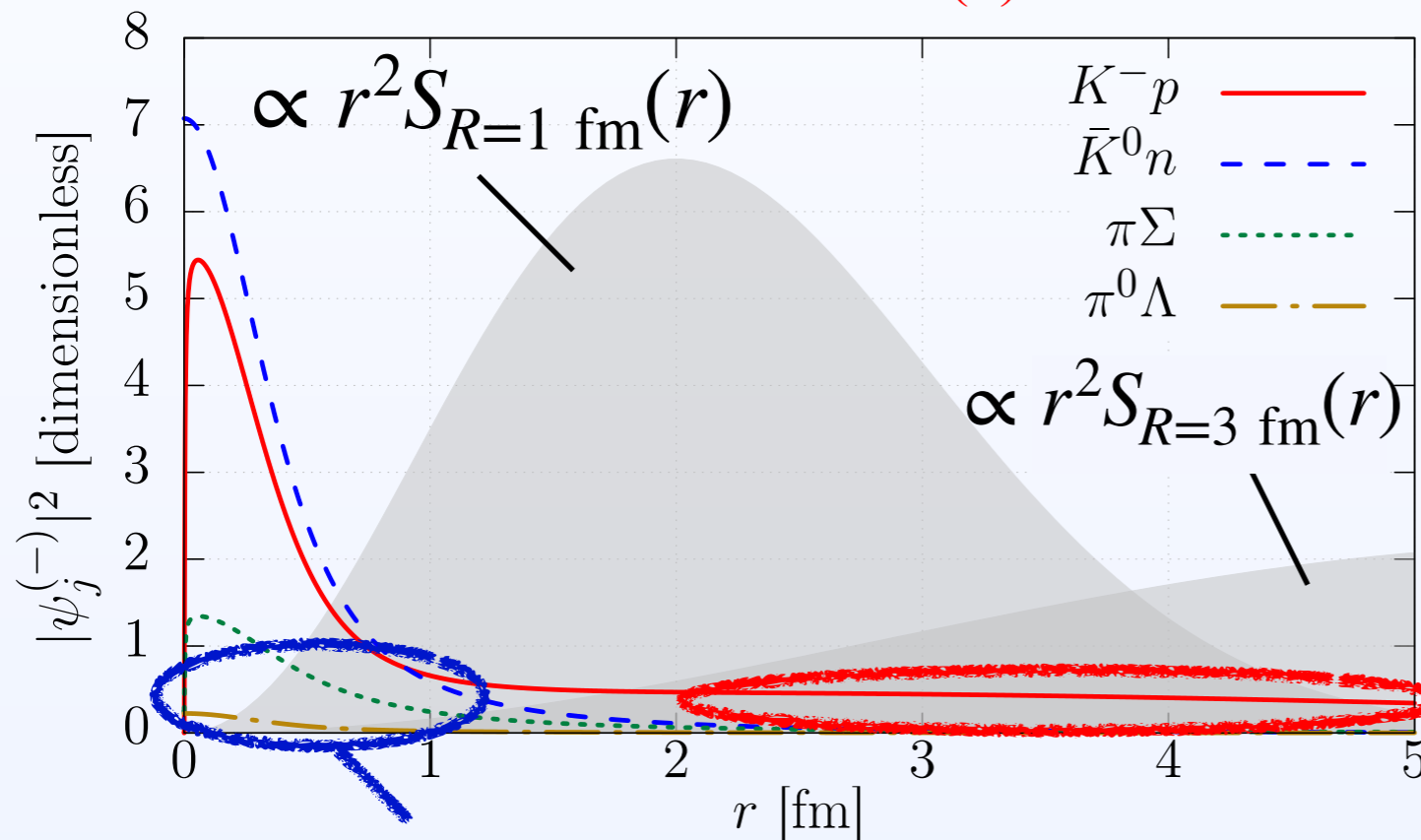
K^-p correlation with Koonin-Pratt Formula

- Coupled-channel effect and source size

$$C_{K^-p}(\mathbf{q}) = \int d^3\mathbf{r} S_{K^-p}(\mathbf{r}) \left[\sum_{l \geq 1} |\varphi_l^C(\mathbf{q}; \mathbf{r})|^2 + |\psi_{K^-p}^{C,(-)}(q; r)|^2 \right] + \sum_{j \neq i} \omega_j \int d^3\mathbf{r} S_j(\mathbf{r}) |\psi_j^{C,(-)}(q; r)|^2$$

(1) Modification of $\psi_{K^-p}^{C,(-)}$

(2) C.c. source contribution



Effect (1)

Does not depend on the source size R

$$\psi_{K^-p}^{(-)} \rightarrow \frac{1}{2iq_1 r} \left(e^{iq_1 r} - \mathcal{S}_{11}^\dagger e^{-iq_1 r} \right)$$

(w/o Coulomb)

Effect (2)

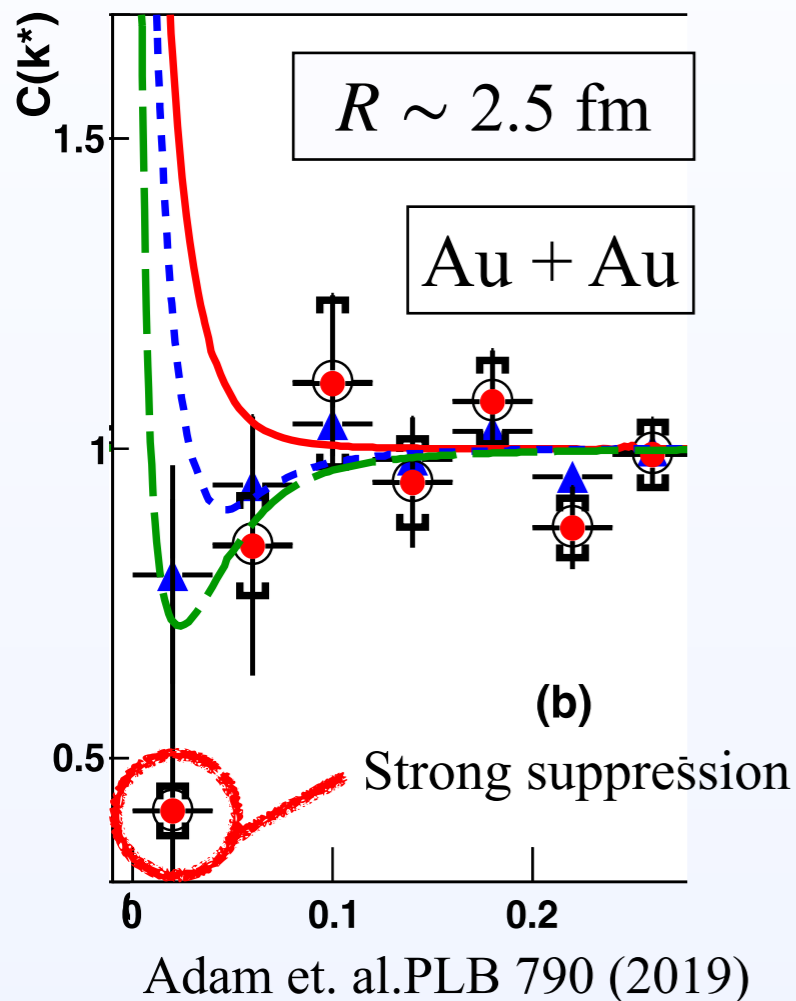
becomes moderate for larger source

- For the larger source, effect (2) gives just a small enhancement.

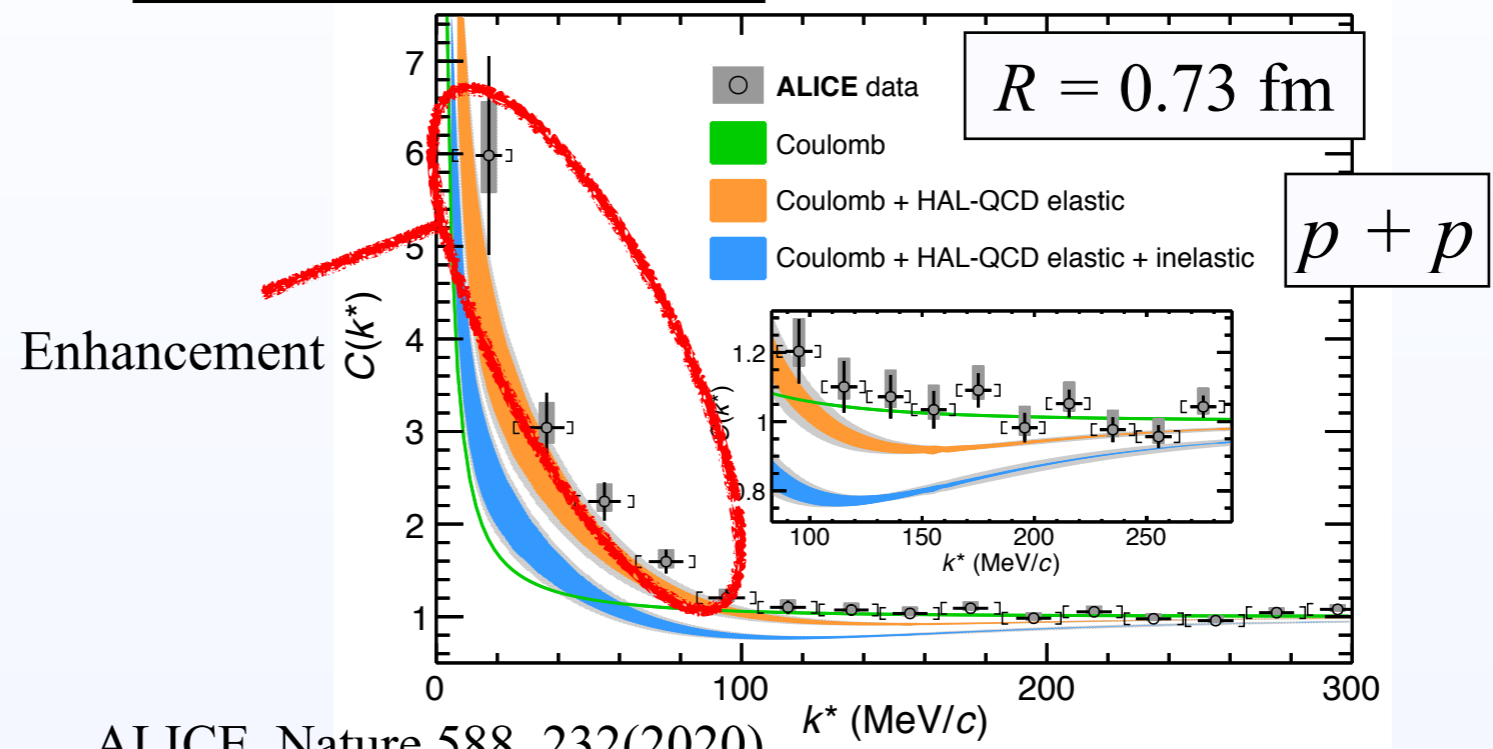
$N\Omega$ dibaryon and $p\Omega$ correlation

- Current situation of experimental data of $p\Omega$ correlation

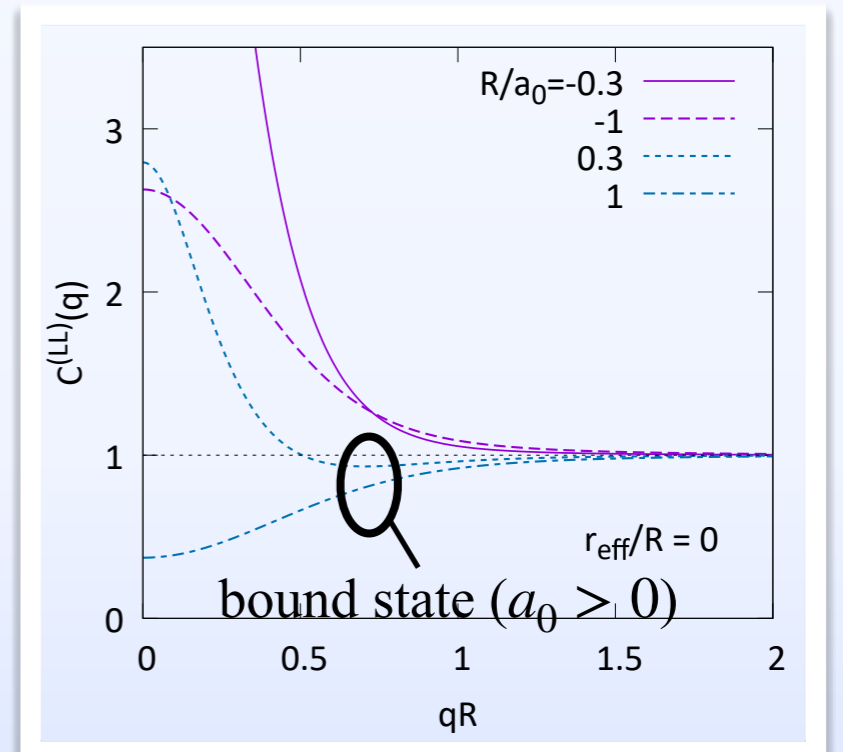
- STAR collaboration



- ALICE collaboration



- Strong source size dependence \implies large $|a_0|$
- Strong suppression at larger source ($R=2.5$ fm) \implies $p\Omega$ dibaryon state?

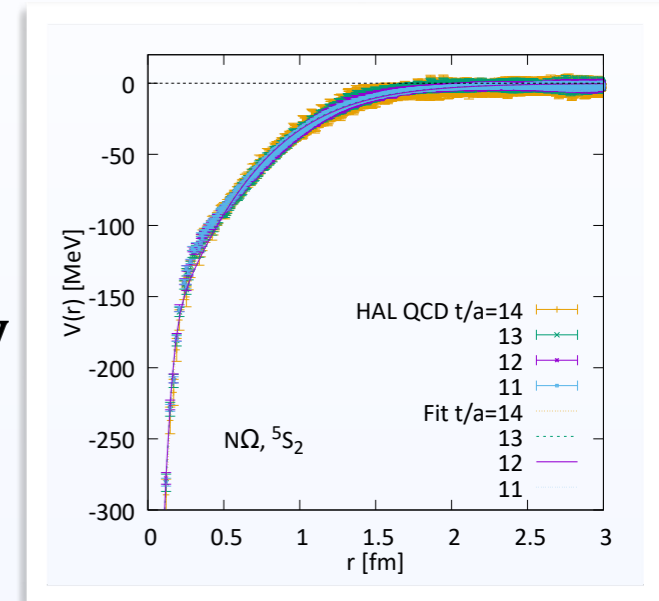


$N\Omega$ dibaryon and $p\Omega$ correlation

- Updated 5S_2 $N\Omega$ potential by HAL QCD

T. Iritani et al. PLB 792 (2019) 284–289

- Nearly physical quark mass: $m_\pi = 146$ MeV, $m_K = 525$ MeV
- No repulsive core $\leftarrow N(lll) \Omega(sss)$
- Strong attraction with $N\Omega$ dibaryon $B = 1.54(0.30)({}^{+0.04}_{-0.10})$ MeV
 \rightarrow Next Dr. Sasaki's talk $(a_0 \simeq 5.3$ fm)



- $p\Omega^-$ correlation function with HALQCD potential

Morita, et al., PRC101 (2020)

- Neglect the channel coupling
- Two assumptions on $J = 1$ wave function $\varphi_{J=1}^{(-)}$

$$C_{p\Omega}(\mathbf{q}) \simeq \frac{5}{8} \int d^3\mathbf{r} S(\mathbf{r}) |\varphi_{J=2}^{(-)}(\mathbf{q}; \mathbf{r})|^2 + \frac{3}{8} \int d^3\mathbf{r} S(\mathbf{r}) |\varphi_{J=1}^{(-)}(\mathbf{q}; \mathbf{r})|^2$$

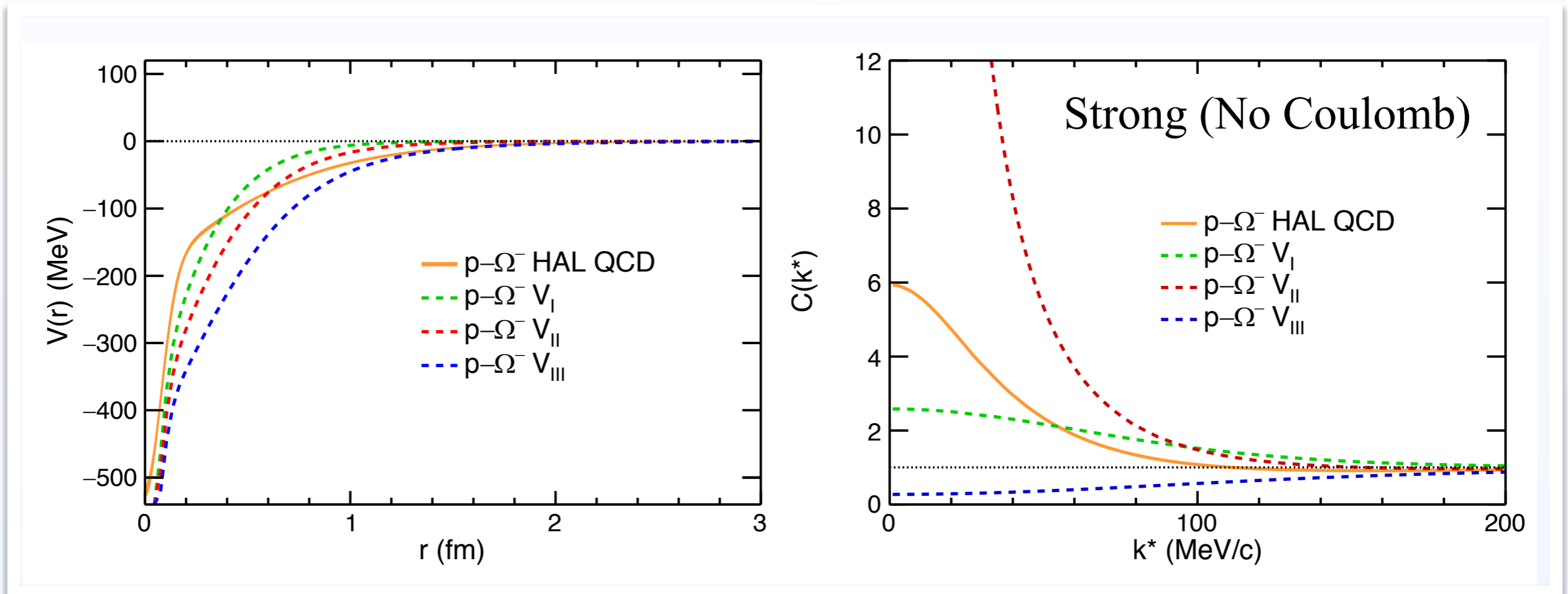
Reference : $\varphi_{J=1}^{(-)} = \varphi_{J=2}^{(-)}$ (Same attraction for $J = 1$ channel)

Minimum : $\varphi_{J=1, \text{s-wave}}^{(-)} = 0$ (Suppressed by channel coupling)

Difference of “Reference” and “Minimum” can be regarded as theoretical uncertainty from the unknown $J = 1$ interaction.

$N\Omega$ dibaryon and $p\Omega$ correlation

- Comparison with previous results



Fabbietti, et.al. [2012.09806]

	Strong	Strong + Coulomb
V_I	–	–
V_{II}	0.05 MeV	0.63 MeV
V_{III}	24.8 MeV	26.9 MeV

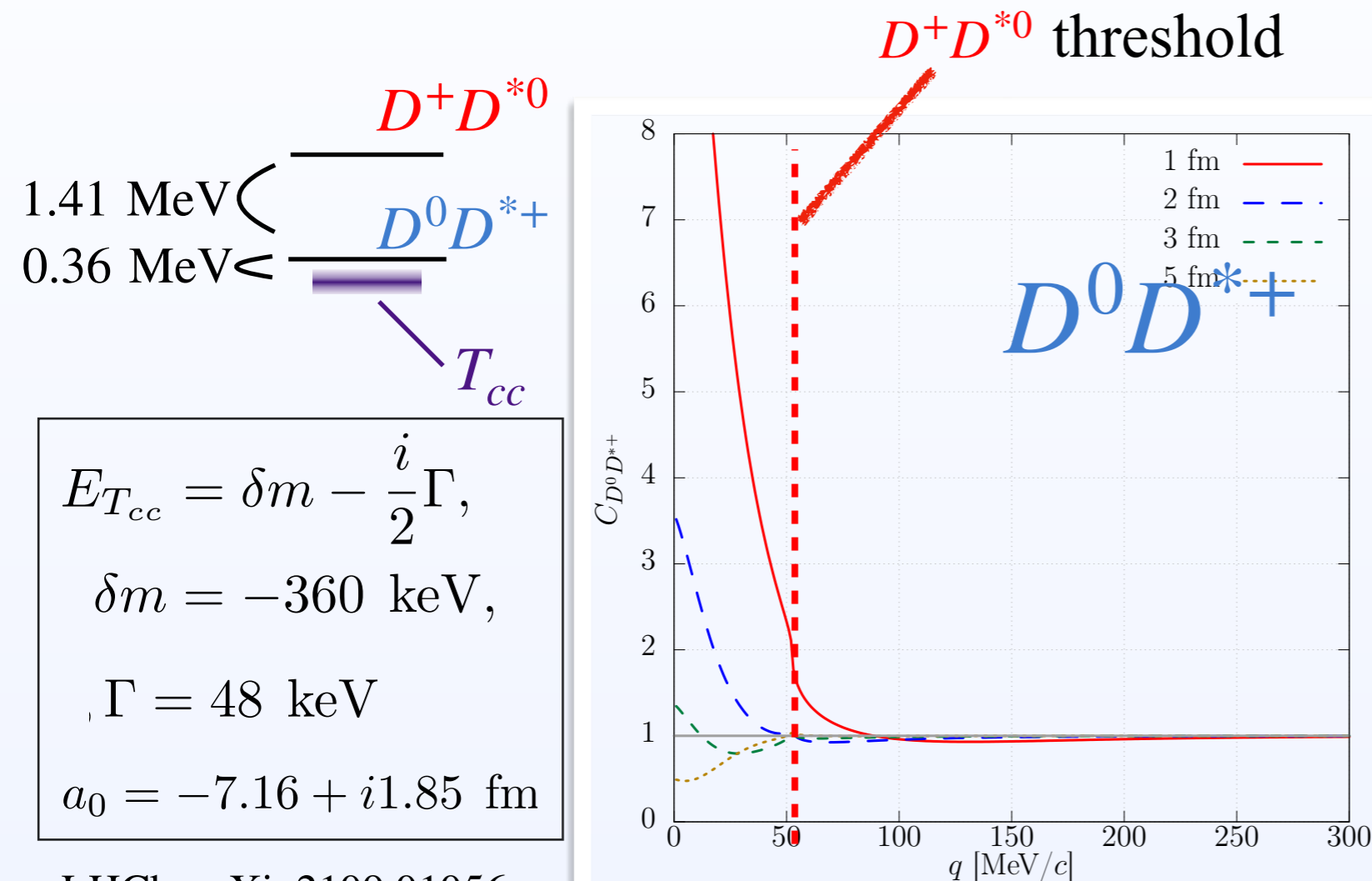
Morita K, Ohnishi A, Etminan F, Hatsuda T. PRC 94 (2016)

Morita K, et al. PRC (2020)

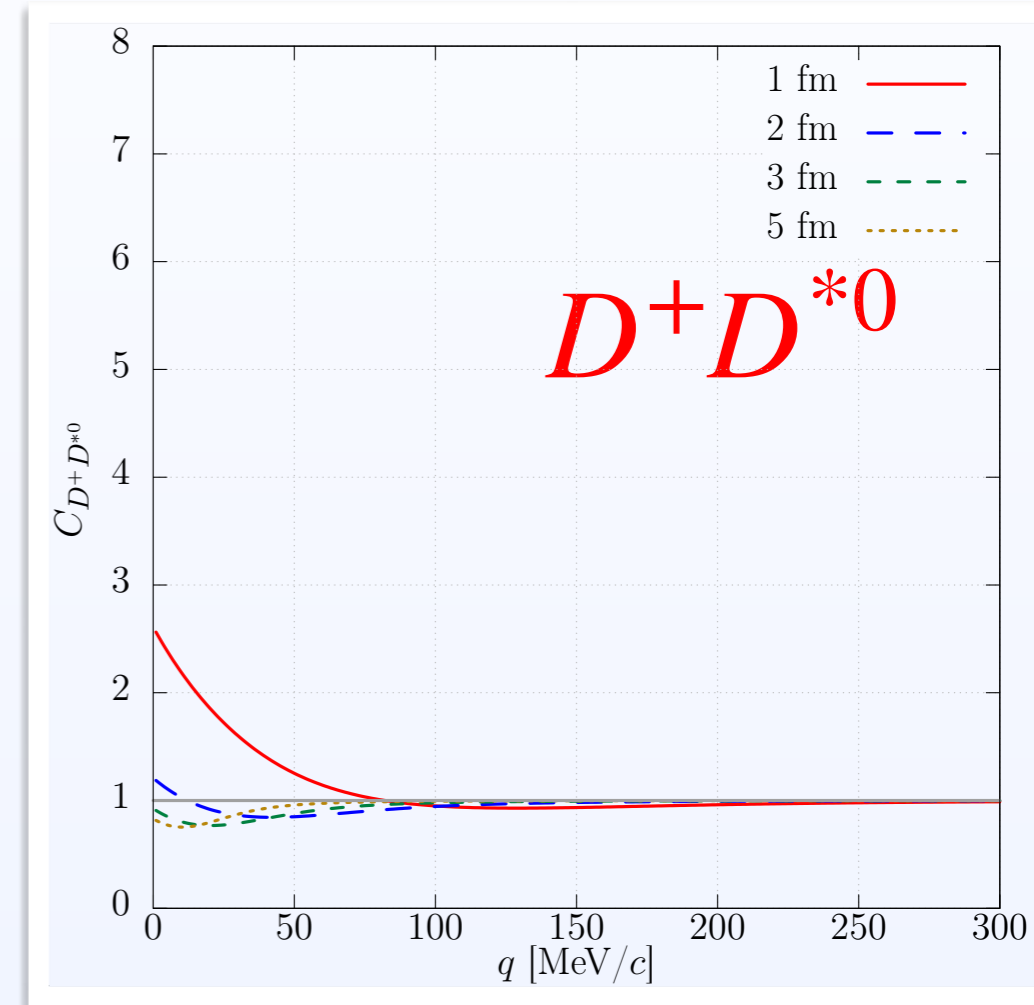
T. Iritani et al. PLB 792 (2019) 284–289

DD^* and $D\bar{D}^*$ int. from femtoscopy

- DD^* correlation and T_{cc} state



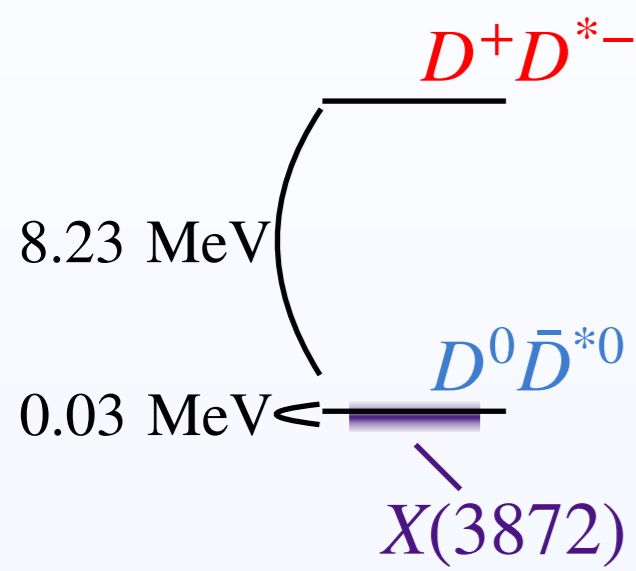
LHCb, arXiv2109.01056



- Bound state like behavior for both pairs
- Stronger source size dep. for $D^0 D^{*+}$
- $D^+ D^{*0}$ cusp is not prominent

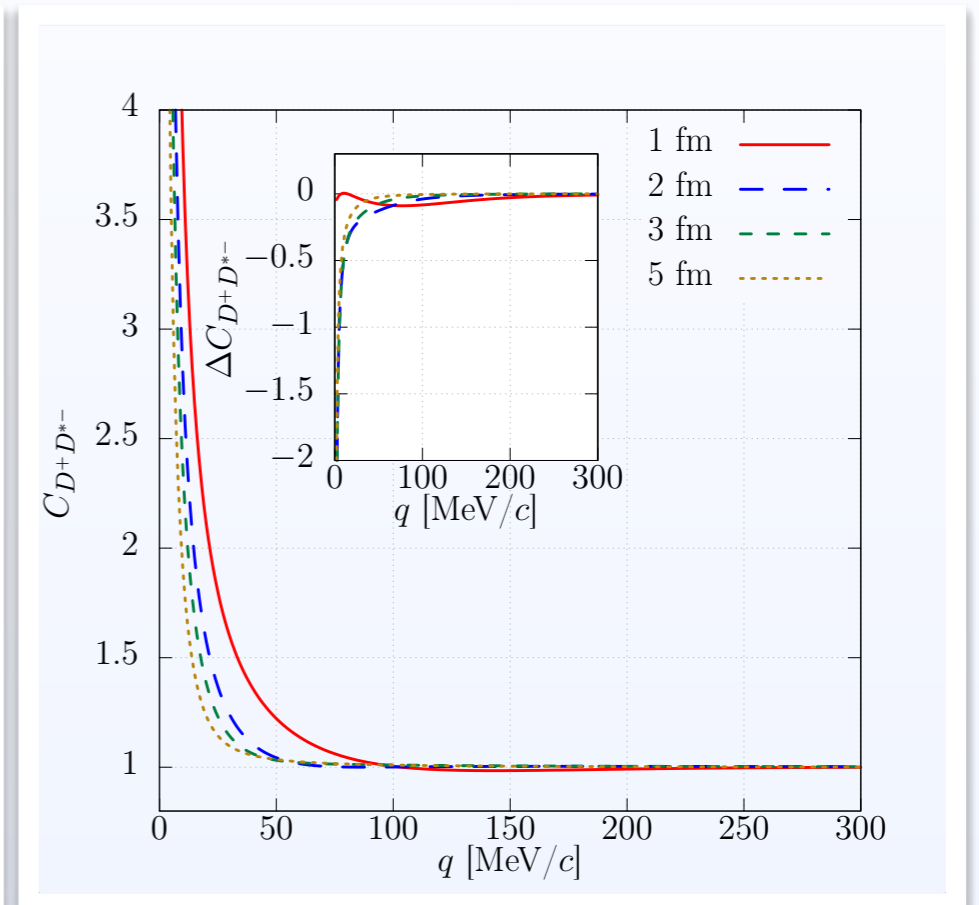
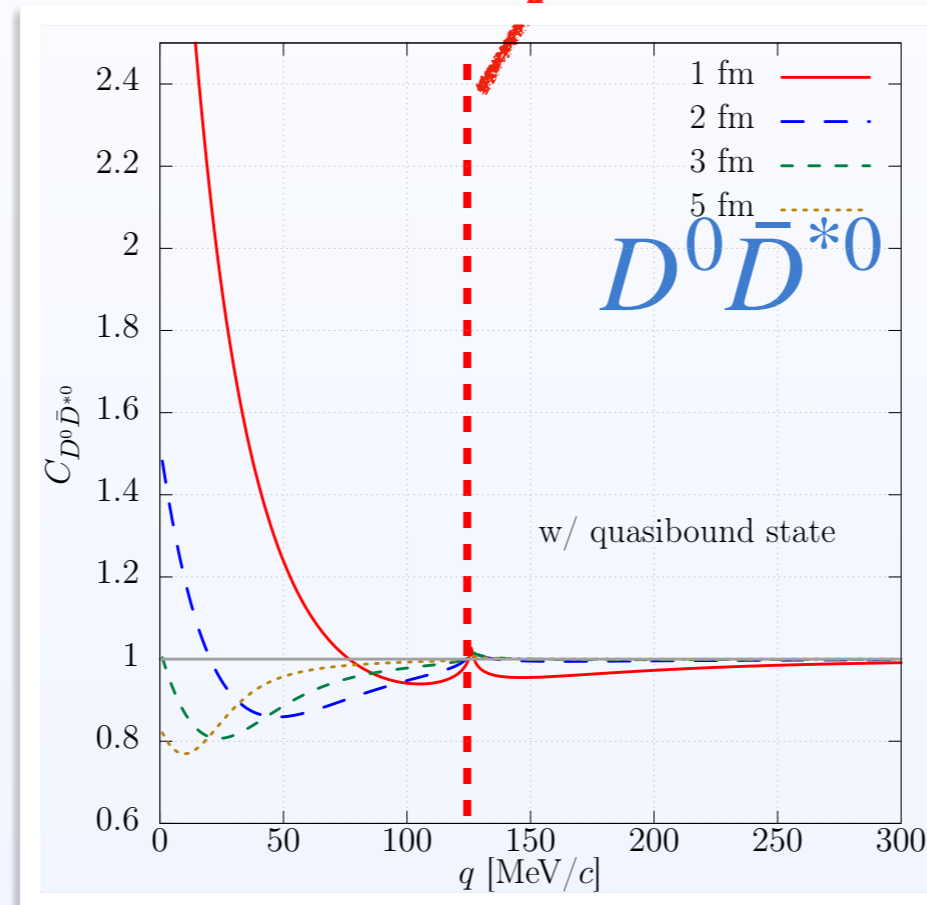
DD^* and $D\bar{D}^*$ int. from femtoscopy

- $D\bar{D}^*$ correlation and $X(3872)$ state



D^+D^{*-} threshold

$R =$



PDG, PTEP 2020, 083C01 (2020)

$$E_{X(3872)} = \delta_m - \frac{i}{2}\Gamma$$

$$\delta m = -0.04 \text{ MeV}$$

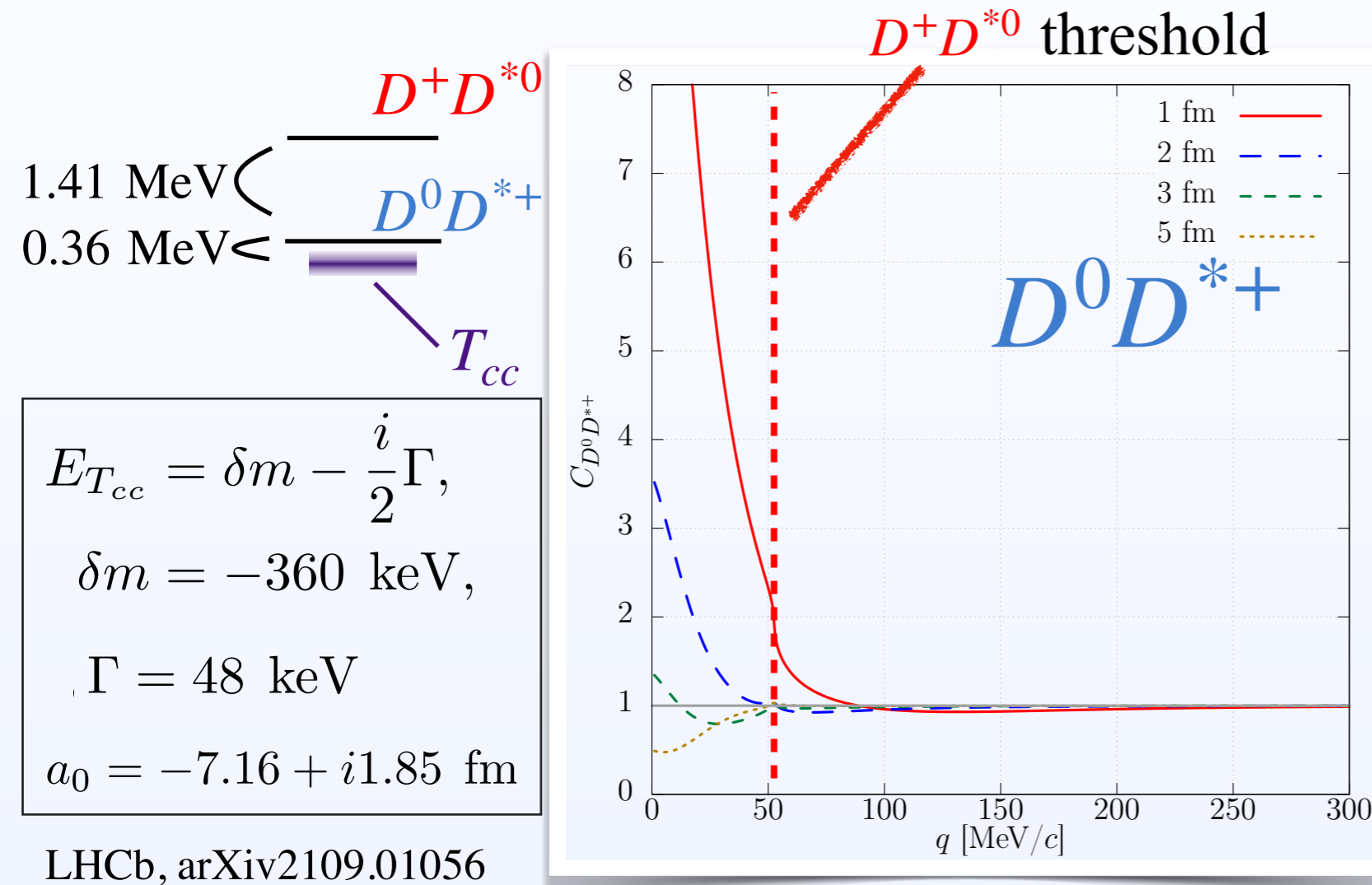
$$\Gamma = 1.19 \text{ MeV}$$

$$a_0^{D^0\bar{D}^{*0}} = -4.23 + i3.95 \text{ fm}$$

- D^0D^{*+} : Strong source size dep.
- D^+D^{*-} : Small effect of the strong int. (Coulomb int dominance)
- Moderate D^+D^{*+} cusp

DD^* and $D\bar{D}^*$ int. from femtoscopy

- DD^* correlation and T_{cc} state



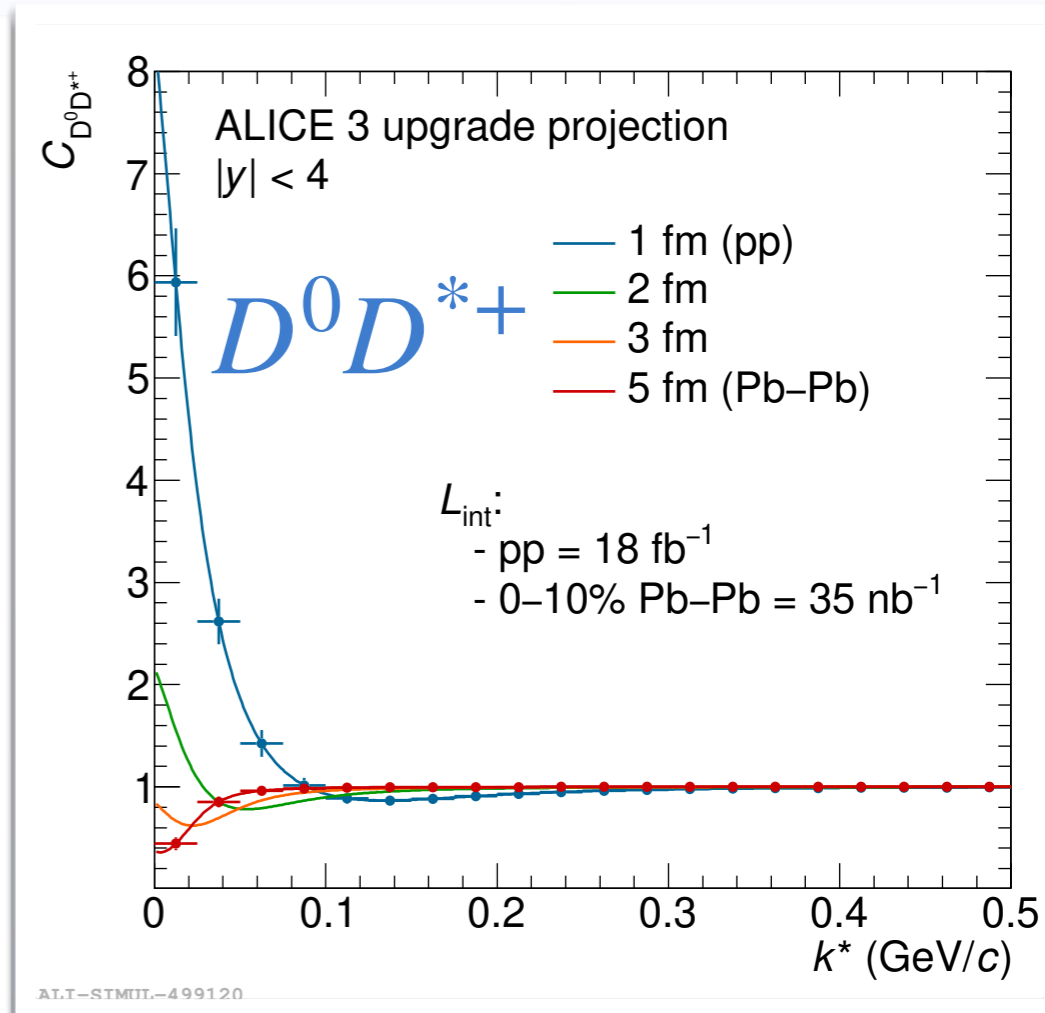
$$E_{T_{cc}} = \delta m - \frac{i}{2}\Gamma,$$

$$\delta m = -360 \text{ keV},$$

$$\Gamma = 48 \text{ keV}$$

$$a_0 = -7.16 + i1.85 \text{ fm}$$

LHCb, arXiv2109.01056



ALICE collab., CERN-LHCC-2022-009 (2022).

- Bound state like behavior for both pairs
- Stronger source size dep. for $D^0 D^{*+}$
- $D^+ D^{*+}$ cusp is not prominent