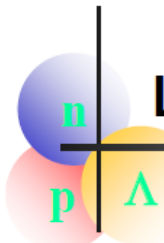


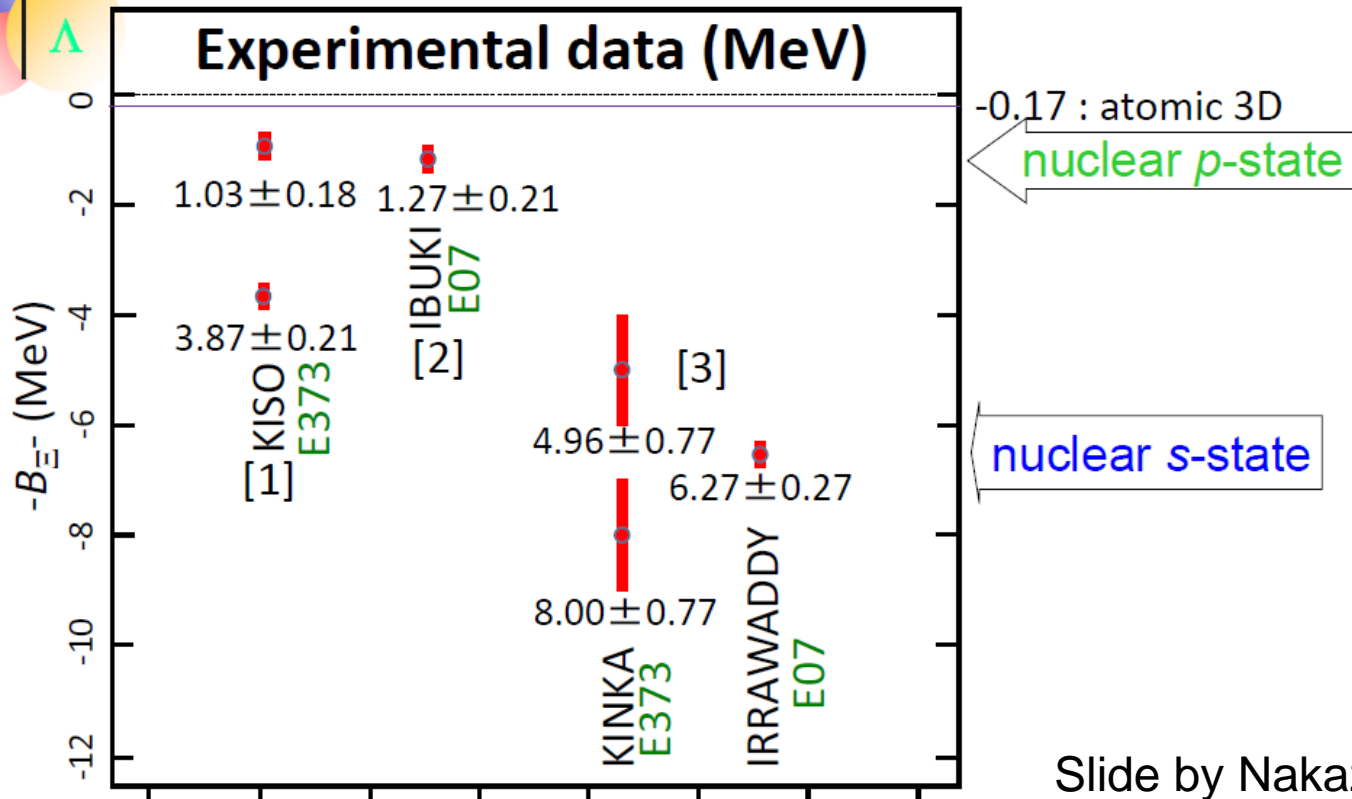
Structure of Ξ hypernuclei

E. Hiyama (Tohoku Univ./RIKEN)

Study of ΞN interaction is one of the important issue in hypernuclear physics.

$$V_{\Xi N} = V_0 + \boldsymbol{\sigma} \cdot \boldsymbol{\sigma} V_{\sigma \cdot \sigma} + \boldsymbol{\tau} \cdot \boldsymbol{\tau} V_{\boldsymbol{\tau} \cdot \boldsymbol{\tau}} + (\boldsymbol{\sigma} \cdot \boldsymbol{\sigma})(\boldsymbol{\tau} \cdot \boldsymbol{\tau}) V_{\sigma \cdot \sigma \boldsymbol{\tau} \cdot \boldsymbol{\tau}}$$


 Level scheme of Ξ hypernucleus (${}^{15}_{\Xi}C [{}_{\Xi}^{-}{}^{14}N]$)



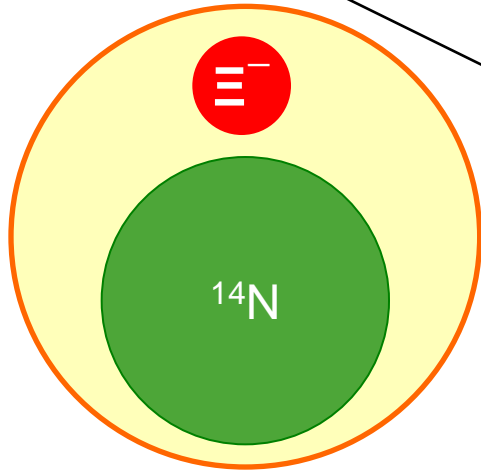
Slide by Nakazawa

- [1] K. Nakazawa, et. al., Prog. Theor. Exp. Phys. 2015, 033D02 (2015), E. Hiyama and K. Nakazawa, Ann. Rev. Nucl. Part. Sci. 68, 131 (2018).
- [2] S. Hayakawa, et. al., Phy. Rev. Lett., 126, 062501 (2021).
- [3] M. Yoshimoto, et. al., Prog. Theor. Exp. Phys. 2021, 073D02 (2021).

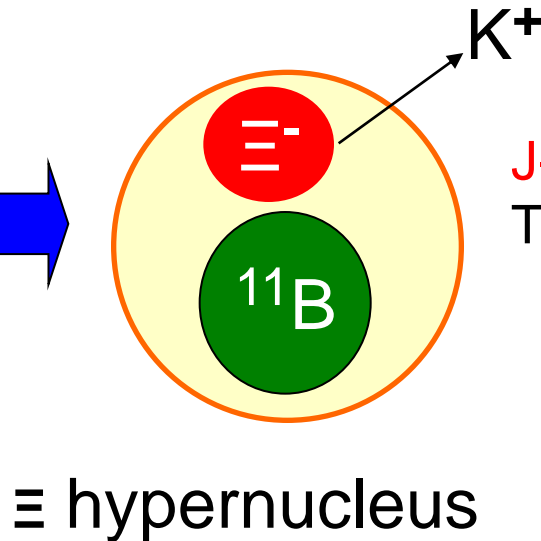
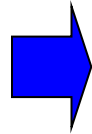
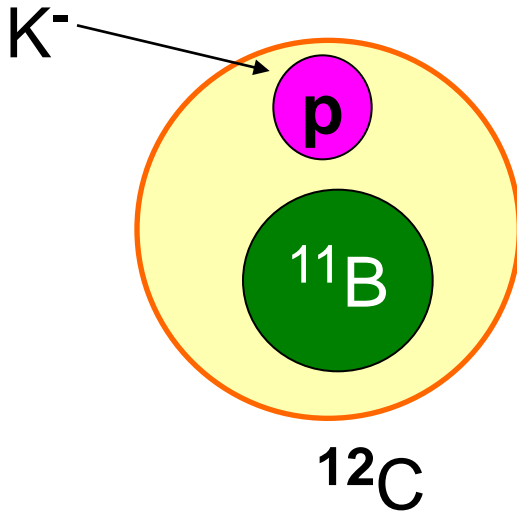
$$V_{\Xi N} = V_0 + \boldsymbol{\sigma} \cdot \boldsymbol{\sigma} V_{\sigma \cdot \sigma} + \boldsymbol{\tau} \cdot \boldsymbol{\tau} V_{\tau \cdot \tau} + (\boldsymbol{\sigma} \cdot \boldsymbol{\sigma})(\boldsymbol{\tau} \cdot \boldsymbol{\tau}) V_{\sigma \cdot \sigma \tau \cdot \tau}$$

By observation of $^{14}\text{N}-\Xi$, we understand

$V_{\Xi N}$ is attractive.



Based on this observation,
Now it is important to predict
the level structure of $^{11}\text{B}+\Xi$ system.

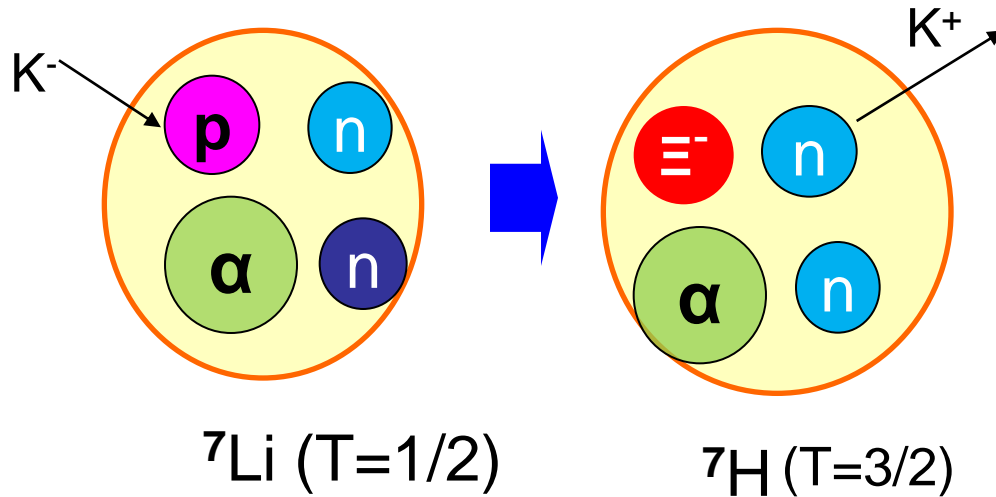


J-PARC: E70: spokesperson
T. Nagae

The theoretical calculation
will be introduced by
Y. Tanimura at the end of this
Session.

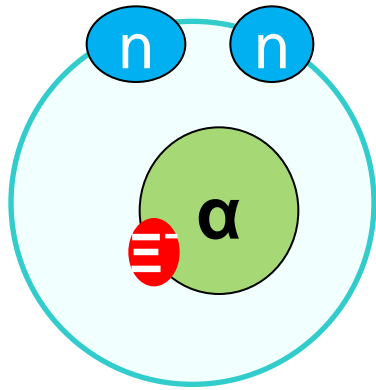
After observation of $^{11}\text{B}-\Xi$ (J-PARC-E70 exp.), we want to know V_0 term, first.

$$V_{\Xi N} = V_0 + \sigma \cdot \sigma V_{\sigma \cdot \sigma} + \tau \cdot \tau V_{\tau \cdot \tau} + (\sigma \cdot \sigma)(\tau \cdot \tau) V_{\sigma \cdot \sigma \tau \cdot \tau}$$



E. H. PRC78,054316(2008).

(more realistic illustration)



Core nucleus ${}^6\text{He}$ is known to be halo nucleus. Then, valence neutrons are located far away from α particle.

Valence neutrons n are located in **p-orbit**, whereas Ξ particle Ξ is located in **0s-orbit**.

${}^7\text{H}$ ($T=3/2$)
 Ξ

Then, distance between Ξ and n is much larger than the interaction range of Ξ and n .

Then, $\alpha\Xi$ potential, in which only V_0 term works, plays a dominant role in the binding energies of this system.

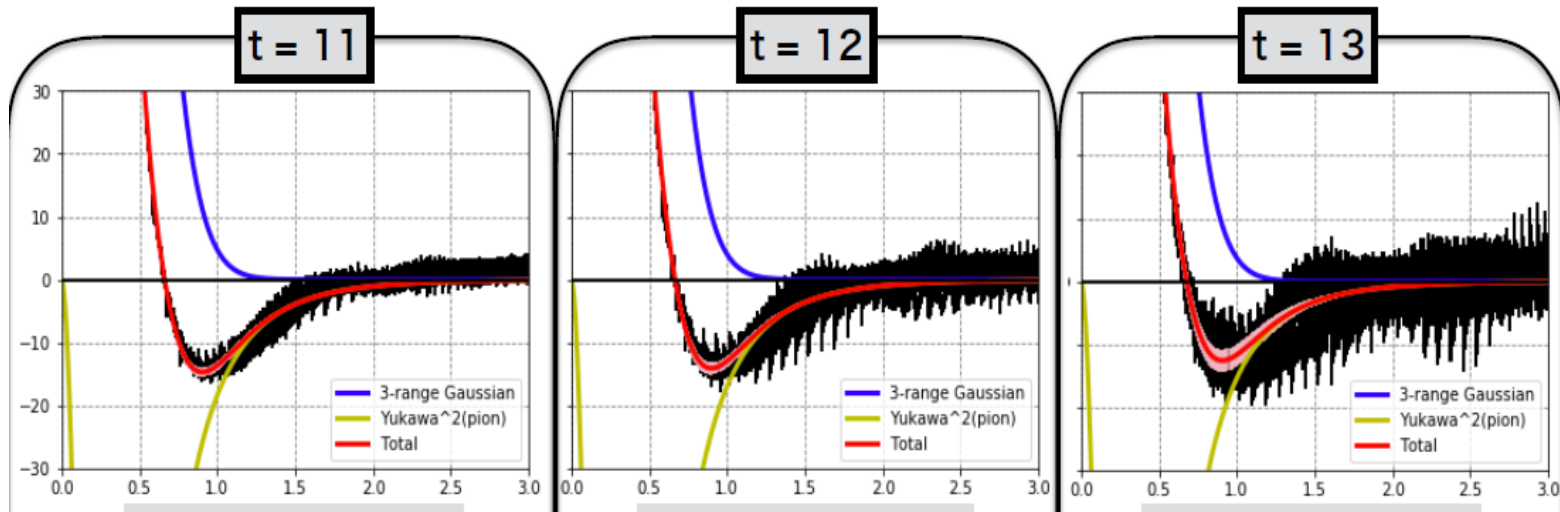
ΞN interaction

Nijmegen potential : Nijmegen model-D(ND), E. Hiyama et al.,
Extended soft core '04d PRC78 (2008) 054316

HAL potential(Base on Lattice QCD potential:HAL collaboration)
by K. Sasaki, Miyamoto, T. Doi, T. Hatsuda et al.

$$V_{\Xi N} = V_0(r) + (\sigma_{\Xi} \cdot \sigma_N) V_s(r) + (\tau_{\Xi} \cdot \tau_N) V_t(r) + (\sigma_{\Xi} \cdot \sigma_N)(\tau_{\Xi} \cdot \tau_N) V_{ts}(r)$$

All terms are central parts only.



Property of the spin- and isospin-components of ESC04, ND, HAL

V(T,S)	ESC04	ND	HAL
T=0, S=1	strongly attractive (a bound state)	} weakly attractive	Weakly attractive
T=0, S=0	weakly repulsive		Strongly attractive
T=1, S=1	weakly attractive		Weakly attractive
T=1, S=0	weakly repulsive		Weakly repulsive

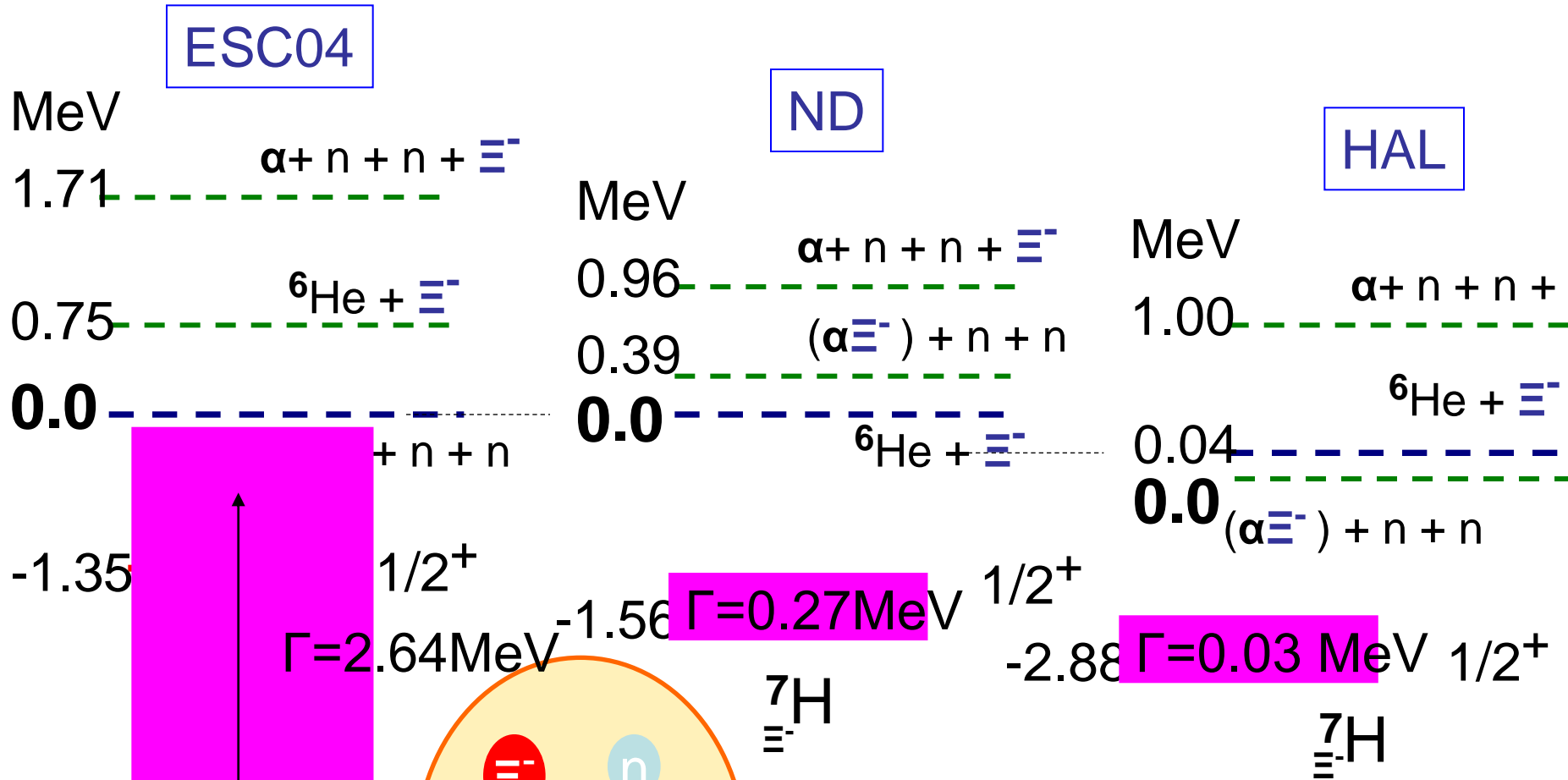
Although the spin- and isospin-components of these potentials are very different (due to the different meson contributions), we find that the spin- and isospin-averaged property,

$$V_0 = [V(0,0) + 3V(0,1) + 3V(1,0) + 9V(1,1)] / 16,$$

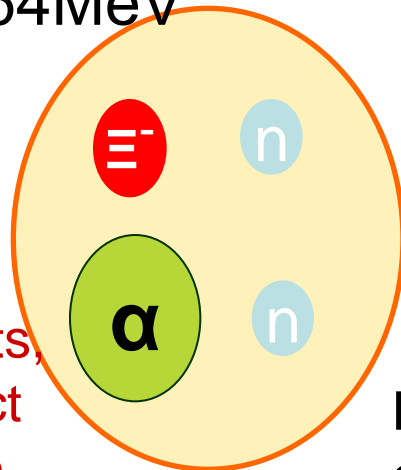
namely, strength of the V_0 - term is similar to each other.

4-body calculation of ${}^7_{\Xi^-}\text{H}$

E. Hiyama et al.,
PRC78 (2008) 054316



In experiments, we can expect a bound state.



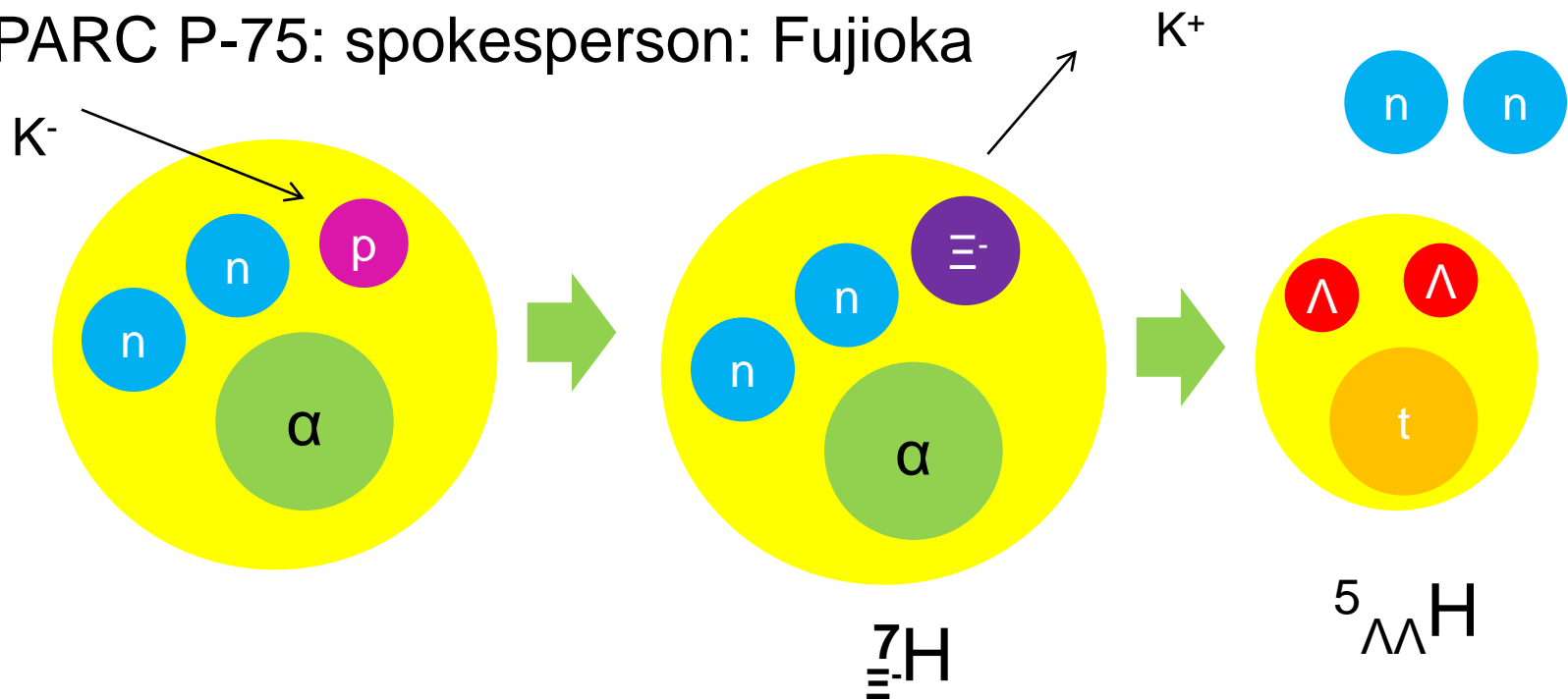
${}^7_{\Xi^-}\text{H}$

Similar binding energies using ND and ESC04.

However, decay width is dependent on on employed ΞN potential

In this way, the binding energy of Ξ hypernucleus with $A=7$ is dominated by $\alpha\Xi$ potential, namely, spin-, and iso-spin independent ΞN interaction (V_0).


J-PARC P-75: spokesperson: Fujioka



$$V_0 = [V(0,0) + 3V(0,1) + 3V(1,0) + 9V(1,1)] / 16,$$

which partial contribution makes attractive for V_0 ?

ΞN interaction:

$T=0, S=0$	
$T=0, S=1$	
$T=1, S=0$	
$T=1, S=1$	

$t=1/2$	$t=1/2$
$S=1/2$	$S=1/2$

we have a two-body bound state for ΞN system?
No idea

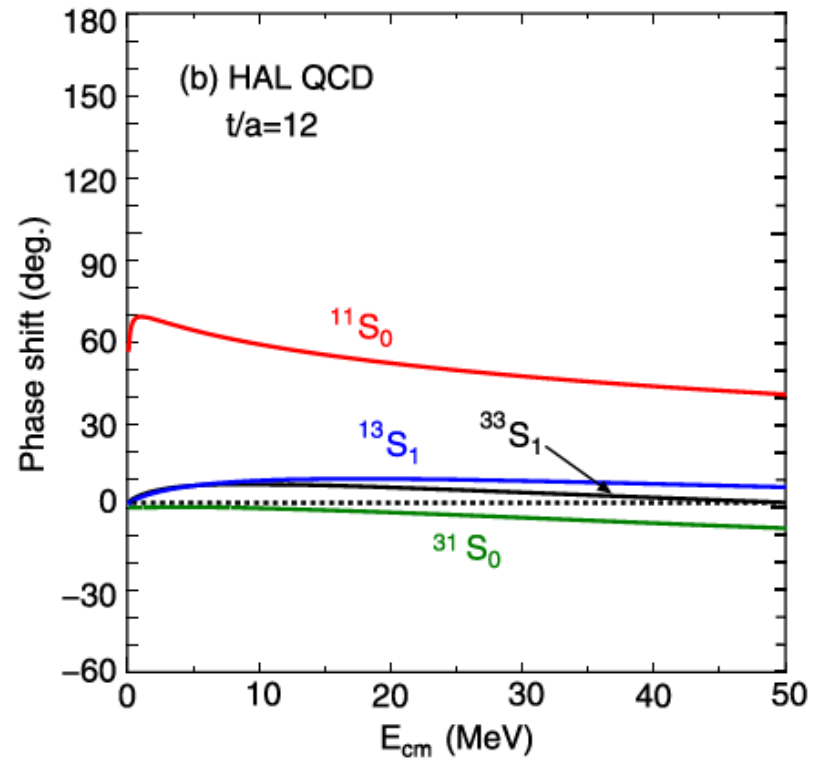
Cf. NN interaction



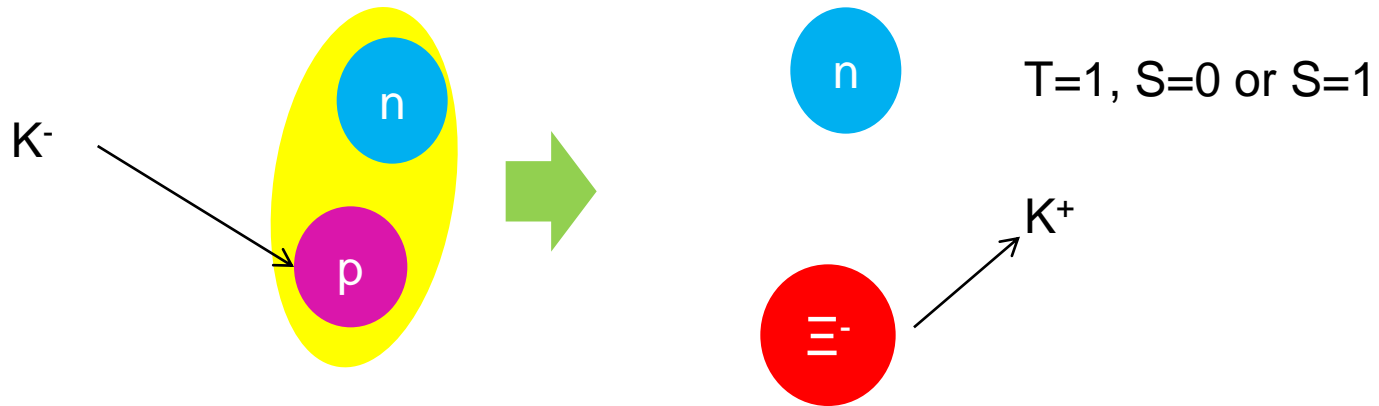
- $T=0, S=0$
- $T=0, S=1$ ➔ strong attraction to have a bound state as a deuteron
- $T=1, S=0$
- $T=1, S=1$

Property of the spin- and isospin-components of HAL

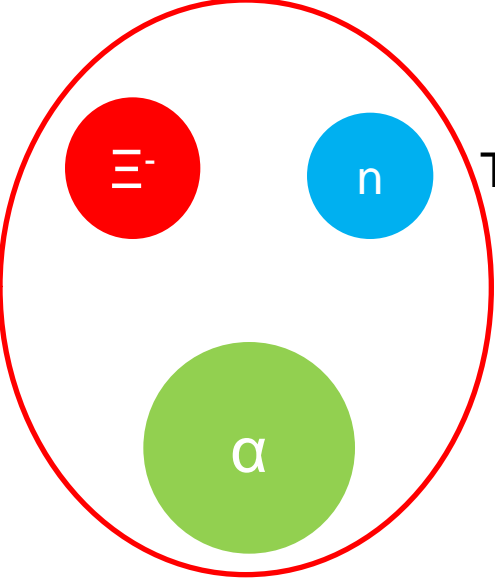
$V(T,S)$	HAL
$T=0, S=1$	Weakly attractive
$T=0, S=0$	Strongly attractive
$T=1, S=1$	Weakly attractive
$T=1, S=0$	Weakly repulsive



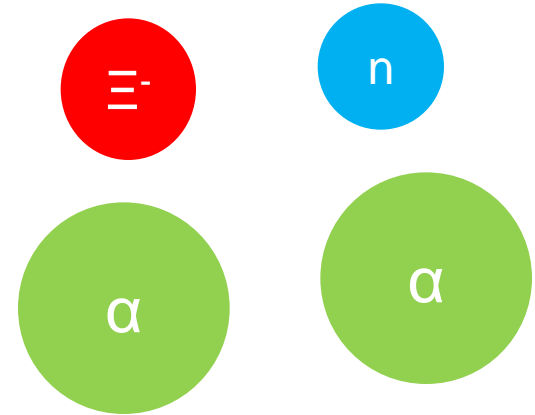
To investigate bound state of ΞN system, it might be possible to perform the following experiment:



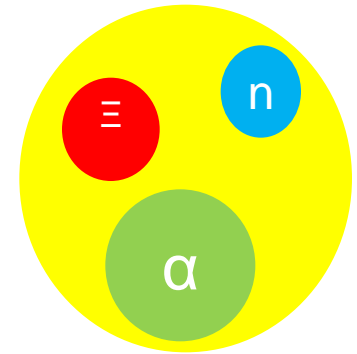
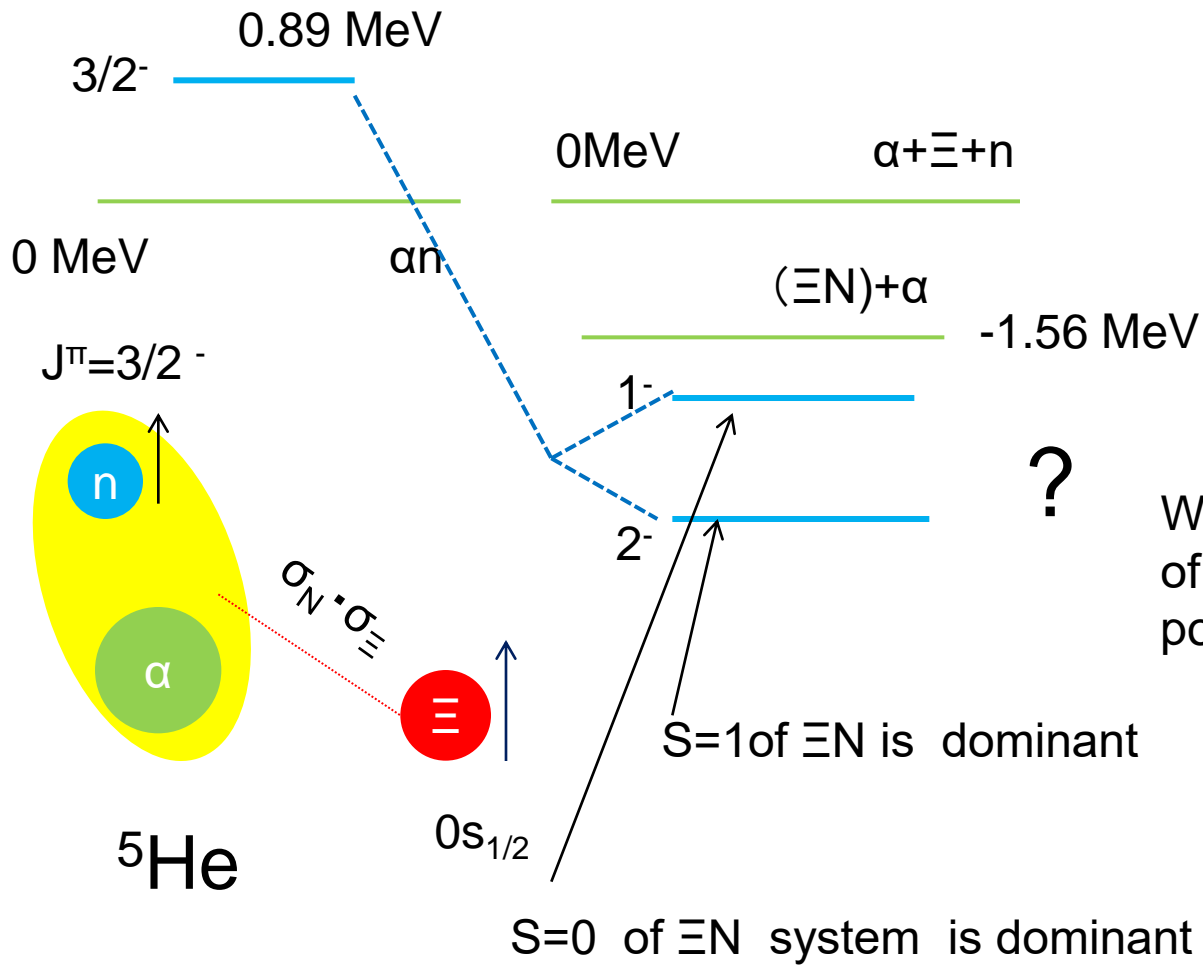
It would be difficult to obtain information on ΞN interaction ($T=1, S=0$ or 1). Because, there might be no bound state for this system.



$T=1, S=0$ or $S=1$

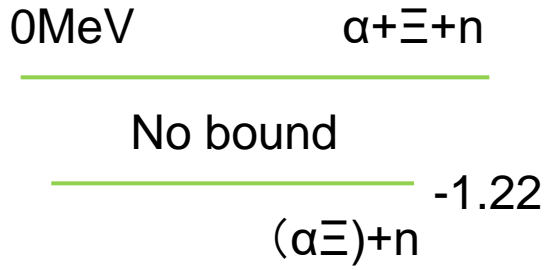


We can add a α or two α_s .
 Due to the attraction of $\alpha\Xi$ and αN interactions,
 ΞN system might have bound system.



What about level structure of $\alpha\Xi N$ system using HAL potential?

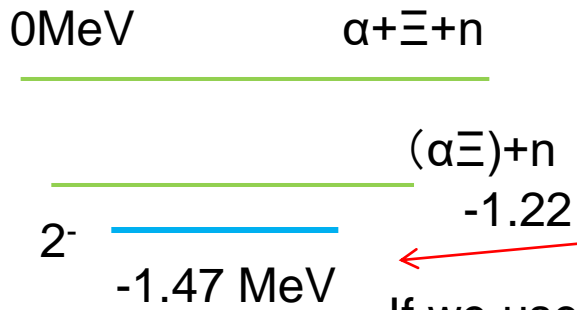
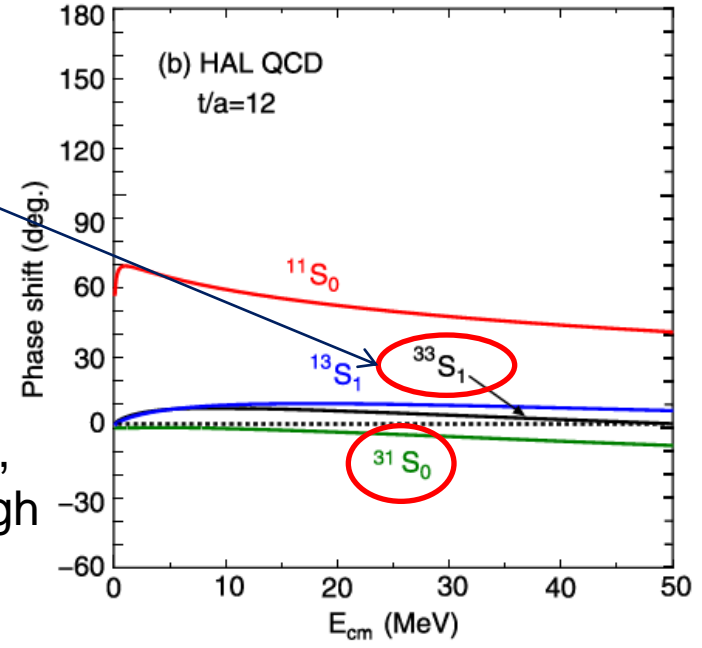
HAL



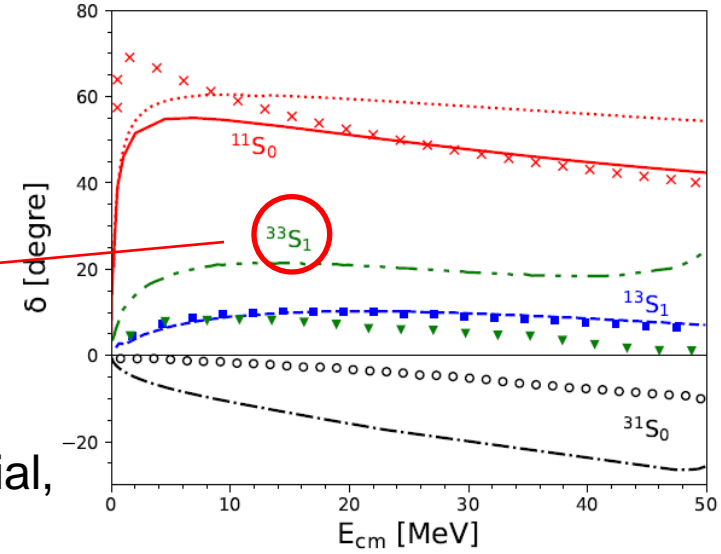
T=1

T=1, S=1

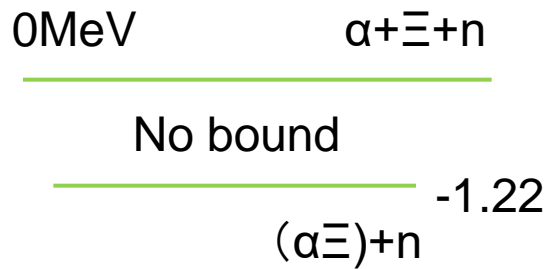
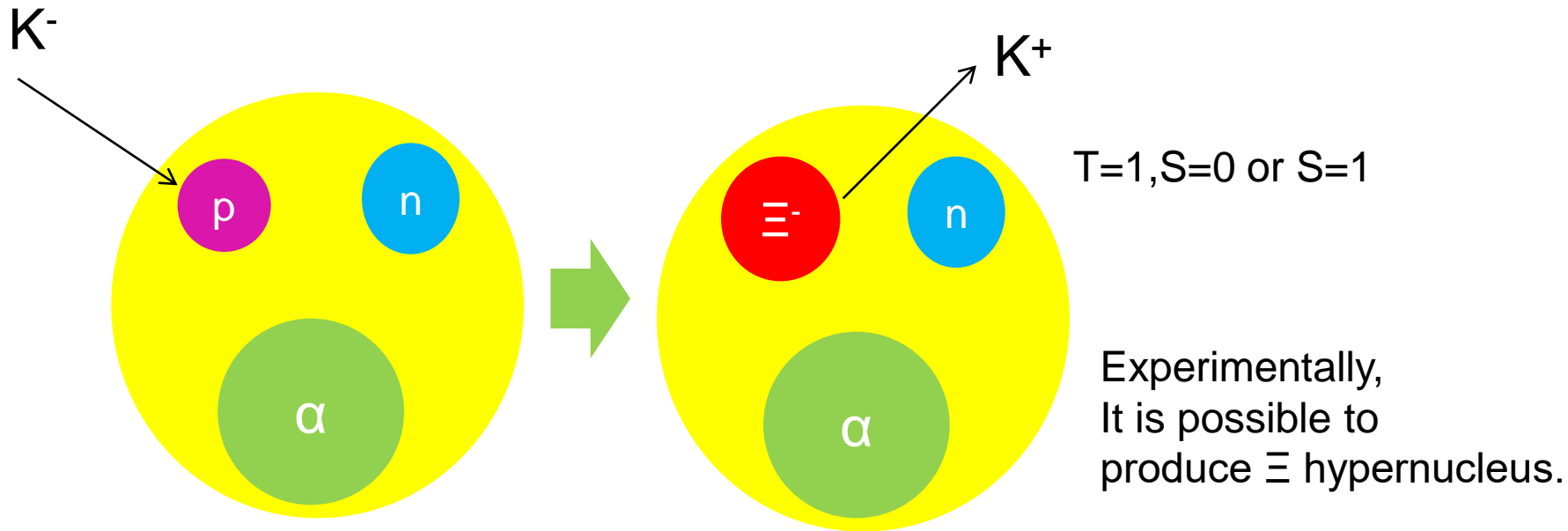
Attractions of T=1, S=1, T=1, S=0 are not enough to make bound states.



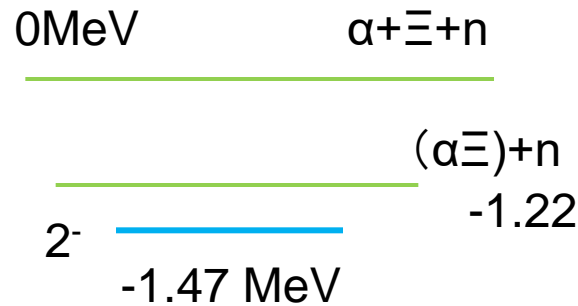
If we use $^{33}\text{S}_1$ information based on chiral EFT potential, We have a bound state in 2^- .



H. Le, et al., EPJA57,339(2021)
Chiral EFT ΞN interaction.

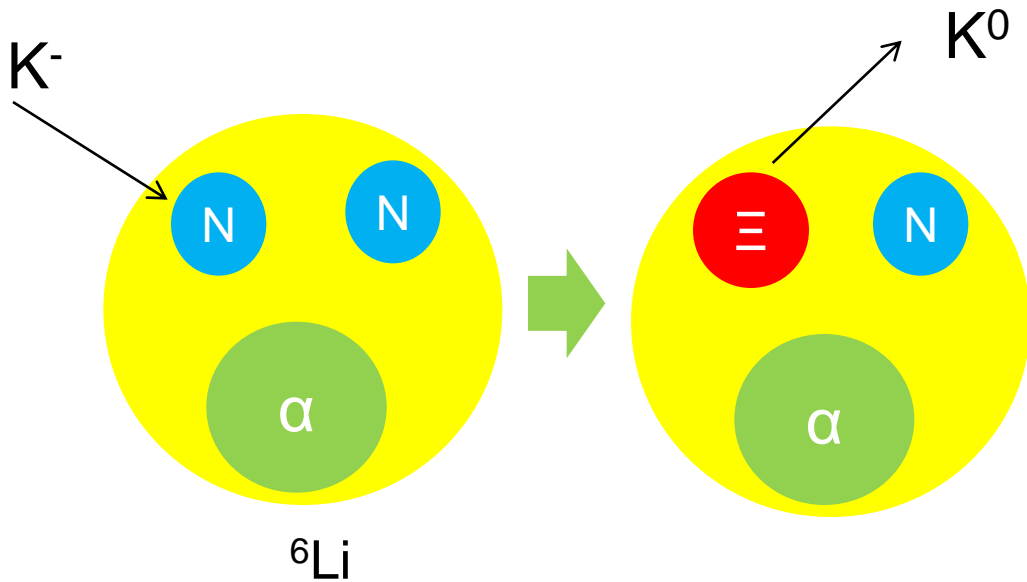


HAL



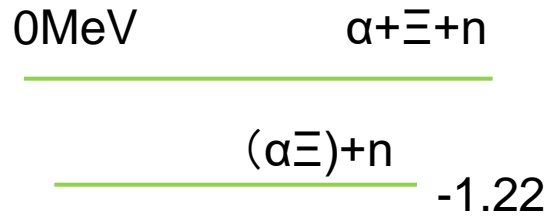
Chiral EFT

Bound state is dependent on ΞN potential employed. Then, it would be risky to use 6Li target by (K^-, K^+) reaction.



$T=0, S=0$ or $S=1$

We can obtain information on $T=0, S=0$ and $S=1$ ΞN interaction.



$J=1^-$ $E=-1.47, \Gamma=0.08$

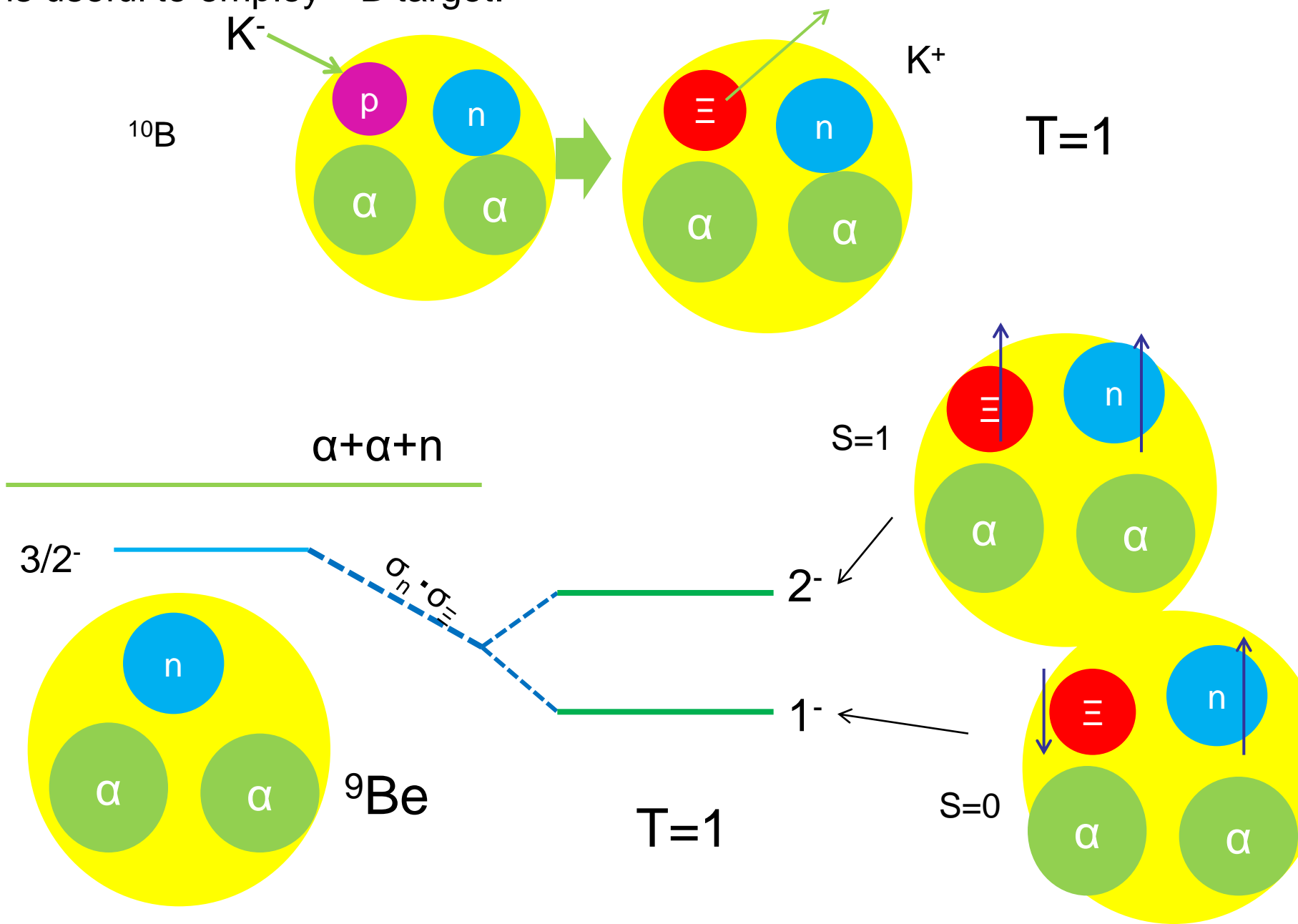
$T=0, S=0$ of ΞN interaction dominate

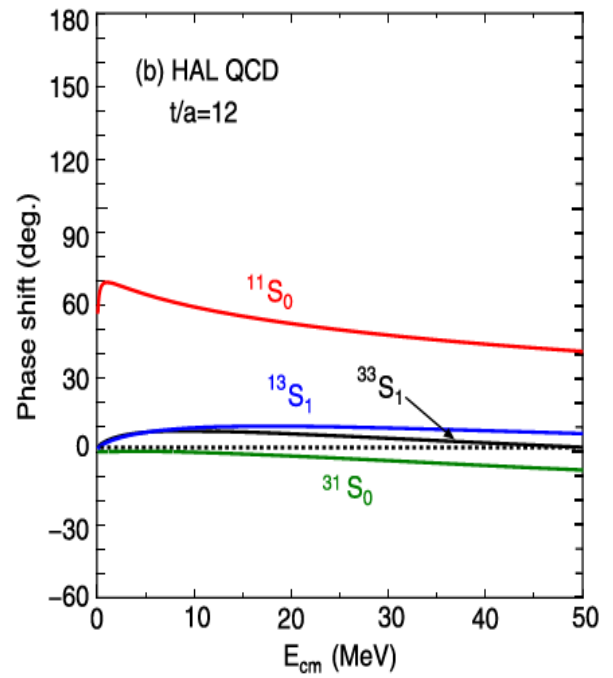
HAL

$T=0$

Currently, (K^-, K^0) reaction would be difficult experiment. Then, it might be risky to use ${}^6\text{Li}$ target.

To obtain information on two-body partial wave contribution, it is useful to employ ^{10}B target.





If the level structure of $A=10$ Ξ hypernuclei, we obtain information on partial wave of ΞN interaction. Level ordering is important.

preliminary

Conclusion

Since the observation of $^{14}\text{N}+\Xi$ hypernucleus, it is important to obtain information on ΞN interaction. In this talk, I introduce the study of $A=6$ and 10 Ξ hypernuclei, to obtain information on partial wave of ΞN interaction.

Currently, the production experiments of $A=7$ and 12 Ξ hypernuclei at J-PARC are planned.

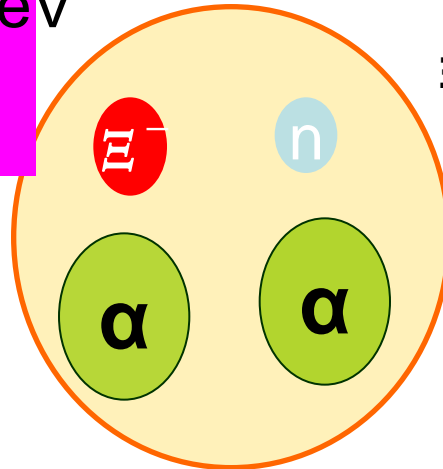
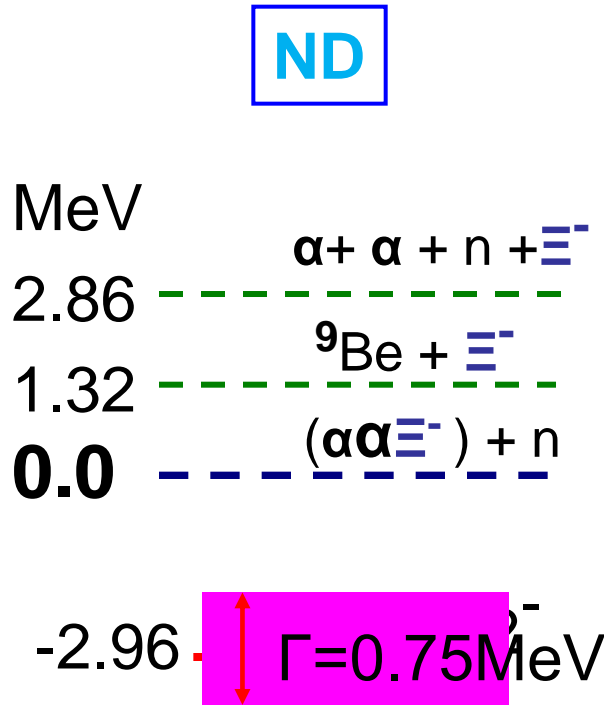
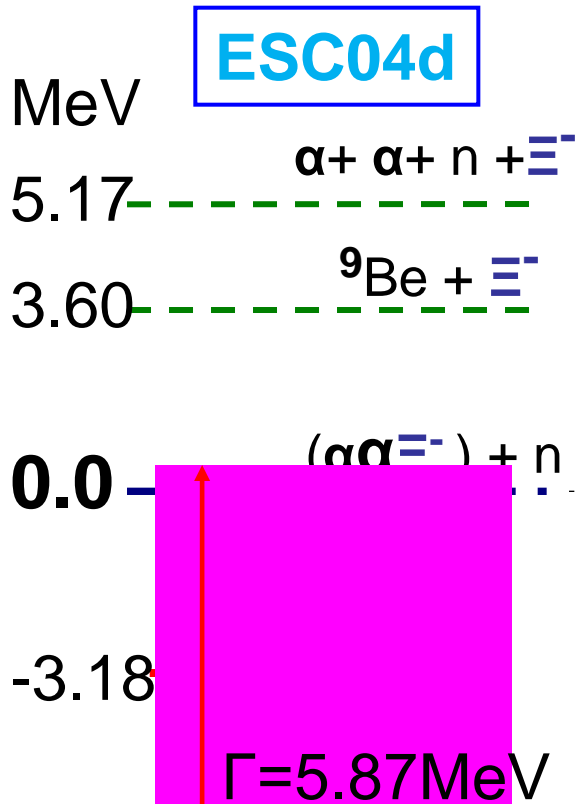
Since the bound states of $A=6$ Ξ hypernuclei are dependent on ΞN potentials employed, then it would be risky to perform experiment using ^6Li target.

Then, I suggest to perform experiment using ^{10}B target at J-PARC.

Thank you!

4-body calculation of ${}_{\Xi}^{10}\text{Li}$

${}_{\Xi}^{10}\text{Li}$ E. Hiyama et al.,
PRC78 (2008) 054316



${}_{\Xi}^{10}\text{Li}$

Similar binding energies using ND and ESC04d.

Independent on employed ΞN potential

But, decay width is dependent on employed ΞN interaction.

In experiments, we can expect a bound state.