



# LGAD Efficiency and Stability

---

Evangelos –Leonidas Gkougkousis

CERN, EP-R&D WG 1.1: Hybride Pixel Detectors



Geneva – November 19<sup>th</sup>, 2020

# • Introduction

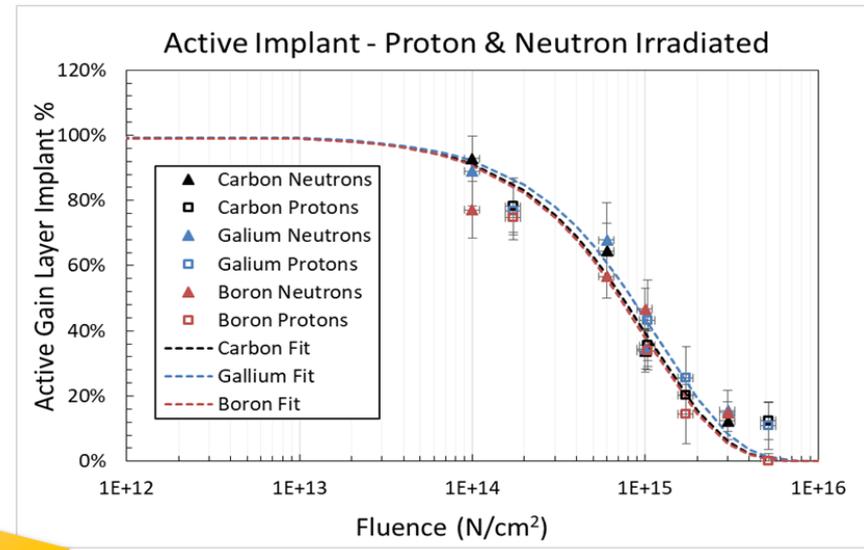
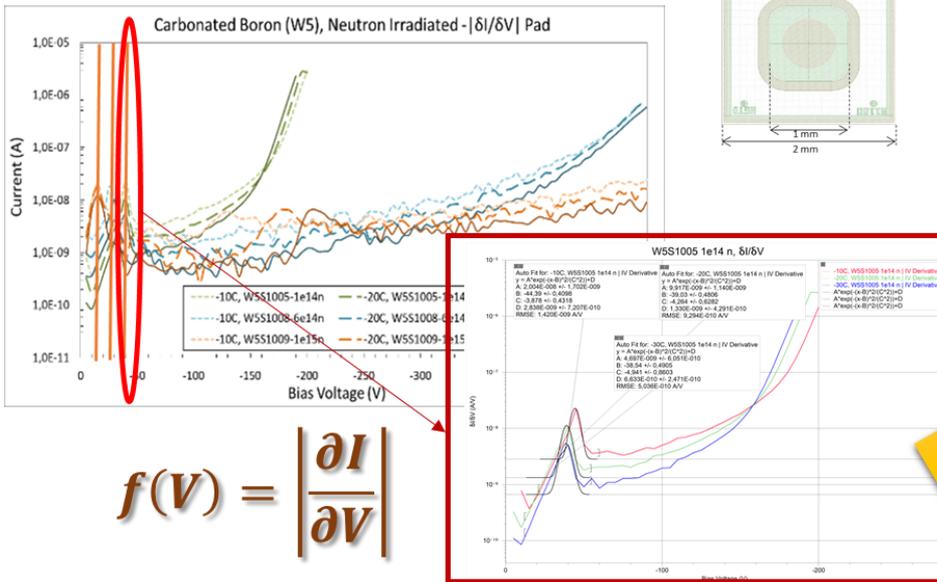
## Implant radiation hardness studies

- ✓ 1x1 mm<sup>2</sup> CNM diodes, runs 10478 (W4 & W5) and 10924 (W6)
  - ✓ 50 μm on 250 μm 4" Sol wafers
  - ✓ **Boron**, **Boron + Carbon** diffused and **Gallium** implanted gain layer
- ✓ Irradiations:
  - ✓ 23 GeV PS protons
  - ✓ fast (~10MeV) neutrons at JSI
  - ✓ 5 fluences: 1e14, 6e14, 1e15, 3e15, 6e15 n<sub>eq</sub>/cm<sup>2</sup>
- ✓ Tested at -10C, -20C and -30C

30 sensors x 3 temp.  
90 Series of measurements!!

- Depletion voltage by Gaussian fit on IV derivative
- Repeated for -10, -20 & -30°C
- Active dopant extrapolated

$$V_d = V_0 e^{-C_v \Phi}$$

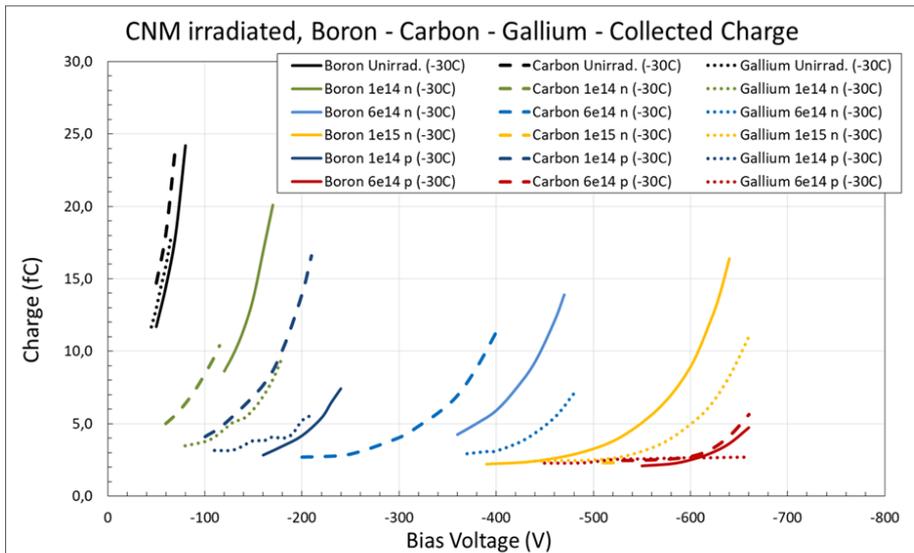


No active dopant difference between different implantation types – neutron/proton

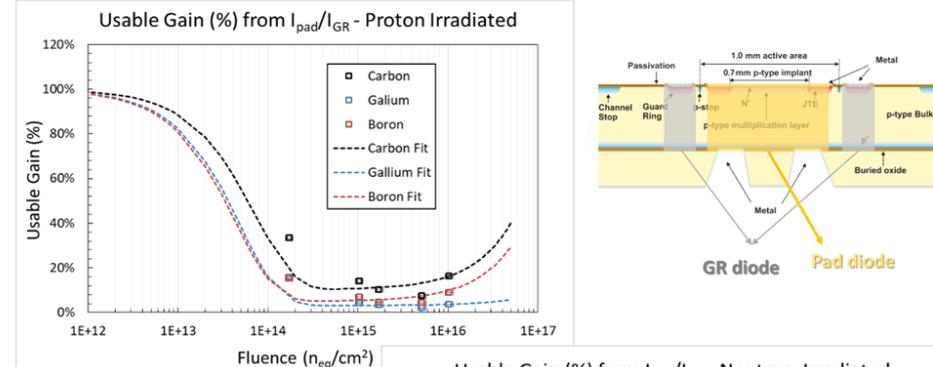
# • Introduction

## MIP measurements & Gain Extraction

- ✓ Collected charge measured with MIPs
  - ✓ 5k events, beta measurements with Sr90
  - ✓ Repeated in -10°C, -20°C -30°C with concurrent results

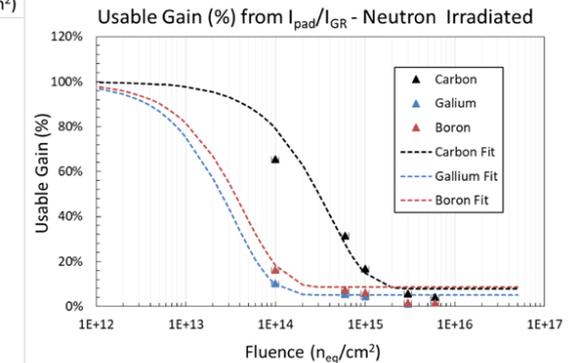


- ✓ Usable gain estimated by comparing GR-pad leakage current
  - ✓ GR – gain region share same cathode
  - ✓ Separate removal factors for Protons/ neutrons
  - ✓ Exponential behavior in depleted region



$$N_{eff}(\Phi) = N_{eff0} - N_c(1 - e^{-c\Phi}) + g_c\Phi$$

Effective dopant concentration:  $N_{eff0}$   
 Initial dopant concentration:  $N_c$   
 Acceptor level introduction rate:  $c$   
 Gain extraction constant:  $g_c$



**Both methods agree: Gallium ~20% worse, carbon ~ 20% for sensors calibrated to performed equally**

↓  
 Acceptor removal in all three cases is the same (same fraction of active dopant from  $V_{GL}$ ), trapping is not (different gain for same fluence, starting from the same point)

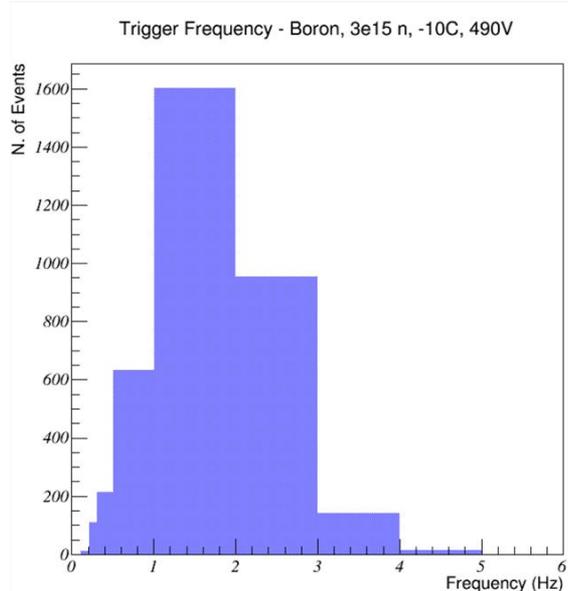
# • Efficiency

## Poisson Fitting

- Frequency of events of radioactive decay follows Poisson distribution
- Record trigger time and convert to event frequency
- Add normalization and scaling parameters

**Poisson Distribution:**  $f(n) = \mu^n * \frac{e^{-\mu}}{n!}$

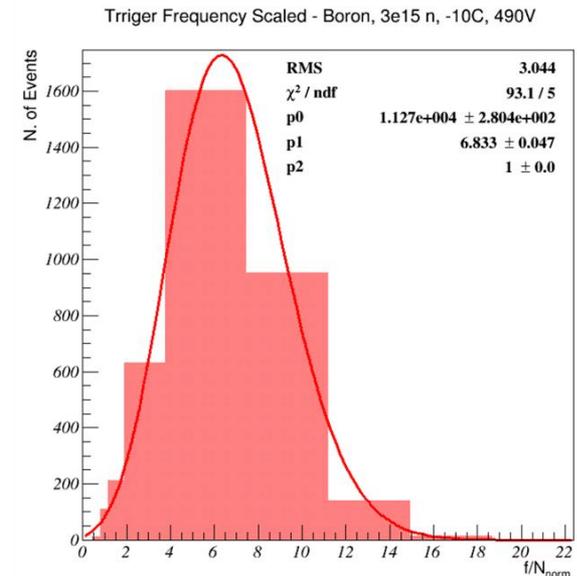
Where: **n** number of events in interval  
 **$\mu$**  mean  
**f(n)** frequency



$n' = n * C$   
**Variable change**  
 $\mu = B/C$

$$f(n') = A * \left(\frac{n'}{C}\right)^{B/C} * \frac{e^{-B/C}}{\Gamma\left(\frac{n'}{C} + 1\right)}$$

Where: **A** Normalization parameter  
**B/C** mean  
**f(n')** Scaled frequency



# • Efficiency

## Per event frequency calculation

- Correction applied for instrument accuracy

**Trigger Frequency:**  $f_i^{trig} = 1/(t_{i+1}^{trig} - t_i^{trig})$

**Low frequency correction:** If  $t_{i+1}^{trig} - t_i^{trig} = 0 \implies f_{i+N}^{trig} = N/(t_{i+N}^{trig} - t_i^{trig})$  for least N on which  $t_{i+N}^{trig} - t_i^{trig} > 0$

## Iterative Re-fitting

- A number of fits is performed per distribution with different parameters
- Best fit result selected by maximizing  $N_{DF}/x^2$  parameter

- ✓ Iterative refitting:
  - Bin size:  $(n + 1) \cdot 0.2 \cdot 1 / T_{acc}$ .
  - Iterations:  $0 < n < 20$
  - Acceptance : **satisfy constraints**

bin size from 0,2 to 4 times trigger time accuracy

- ✓ Asymmetric fit limits:
  - lower:  $x_{min} = 0$
  - upper:  $x_{max} = f_{max}/A_{norm}$

11 out of 936 measurement series  
~ **99% success**

- ✓ Final constraints:
  - $B/C > 0$
  - $f_{min} < B/C < f_{max}$
  - Valid Minuit uncertainties**

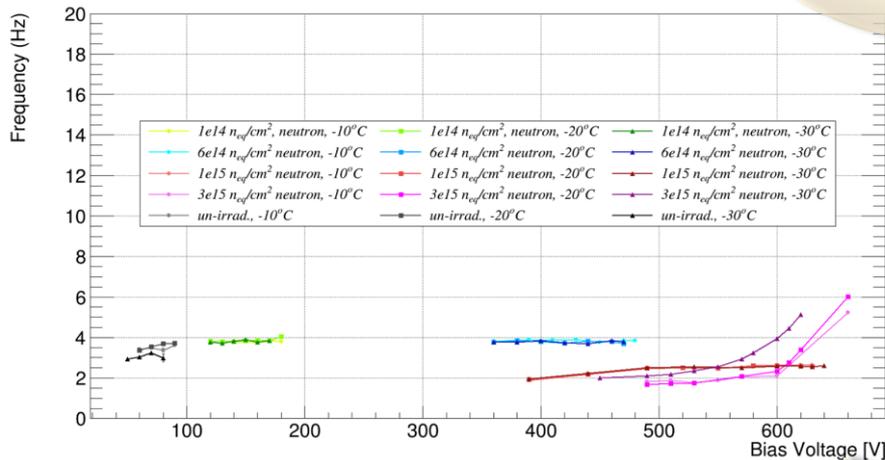
### Fitting Failure rate

219 Boron, 1e15 p, -20C, 340  
 220 Boron, 1e15 p, -20C, 380  
 309 Carbon, 1e14 n, -10C, 120  
 327 Carbon, 1e14 n, -30C, 100  
 333 Carbon, 1e14 n, -30C, 70  
 335 Carbon, 1e14 n, -30C, 90  
 379 Carbon, 6e14 n, -30C, 400  
 645 Gallium, 1e14 n, -20C, 180  
 650 Gallium, 1e14 n, -30C, 110  
 654 Gallium, 1e14 n, -30C, 150  
 659 Gallium, 1e14 n, -30C, 80

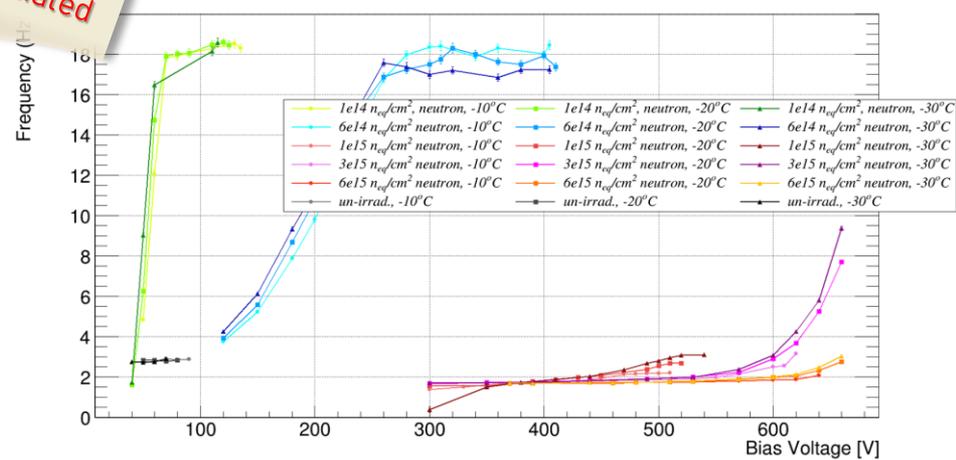
# • Efficiency

## Event frequency estimation – Boron, Carbon

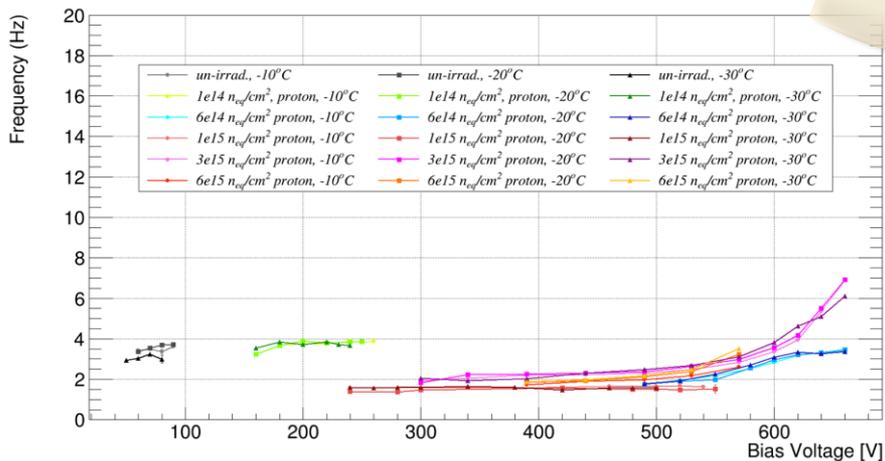
Boron Implanted Gain Layer - Triger Frequency - Neutron Irradiated



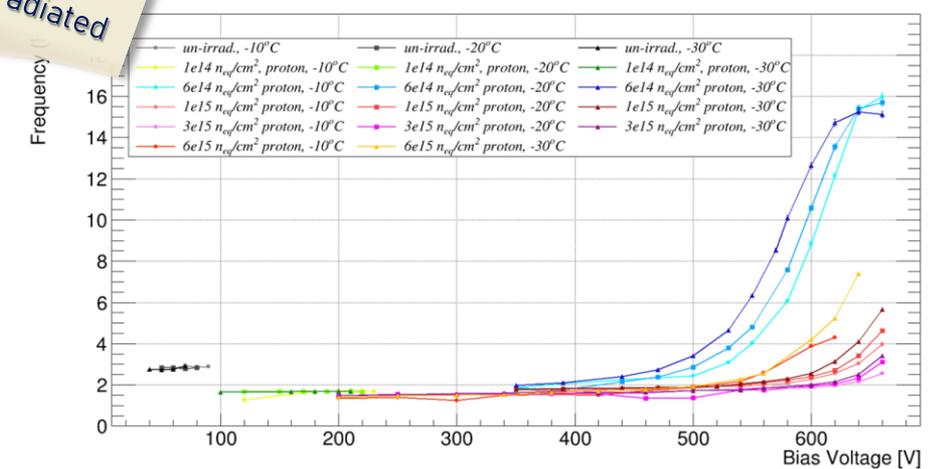
Carbon Implanted Gain Layer - Triger Frequency - Neutron Irradiated



Boron Implanted Gain Layer - Triger Frequency - Proton Irradiated



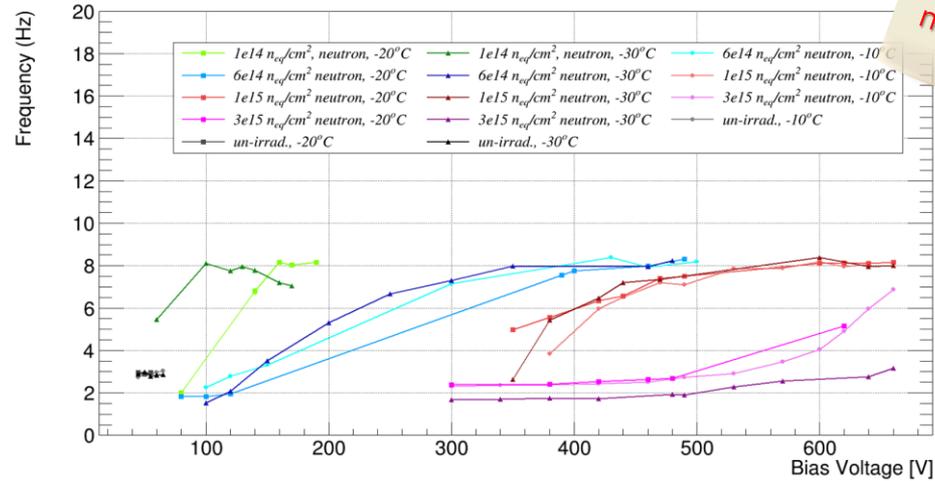
Carbon Implanted Gain Layer - Triger Frequency - Proton Irradiated



# • Efficiency

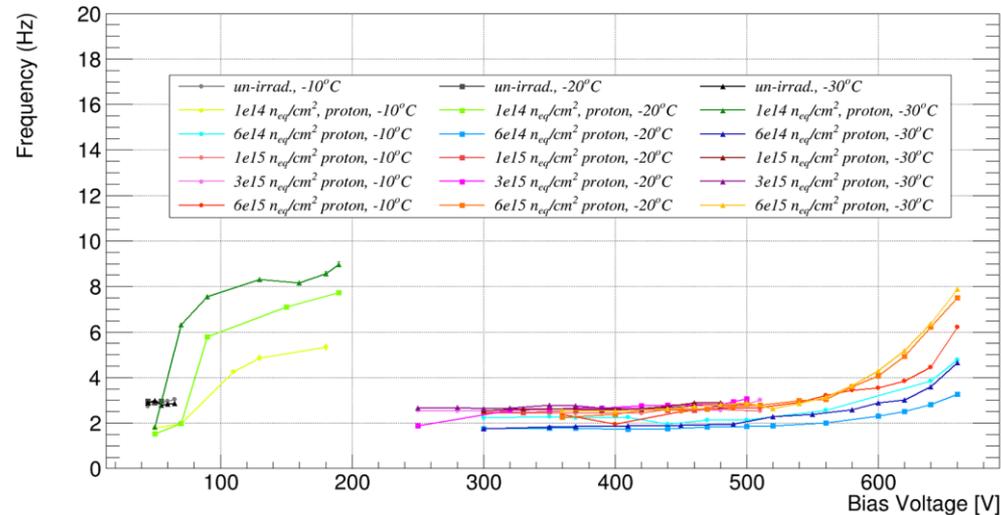
## Event frequency estimation - Gallium

Gallium Implanted Gain Layer - Triger Frequency - Neutron Irradiated



n irradiated

Gallium Implanted Gain Layer - Triger Frequency - Proton Irradiated



p irradiated

# • Efficiency

## Efficiency vs Headroom

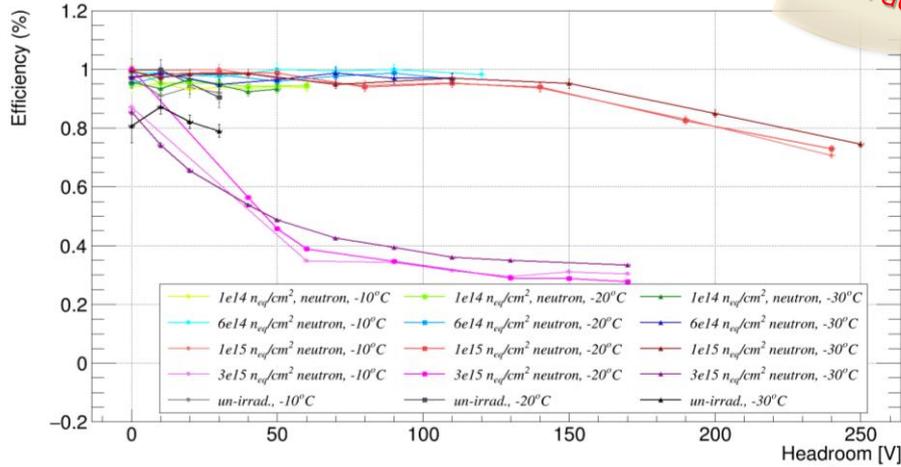
- Set maximum voltage point per temperature as 0
- Assume identical alignment between different temperature measurement series
- Define as 100% efficiency the highest measured trigger frequency using all temperature series
- Recalculate efficiency at each point with respect to max.
- Repeat for each sensor (x30)
- Plot distance from Breakdown (Headroom) vs Relative efficiency
- Since this is relative to the highest, only stability at the beginning of the curve indicates 100% efficiency
- Sensors not reaching a plateau do not achieve 100% operational efficiency
- More evident at SNR vs efficiency and Collected Charge vs Efficiency plots



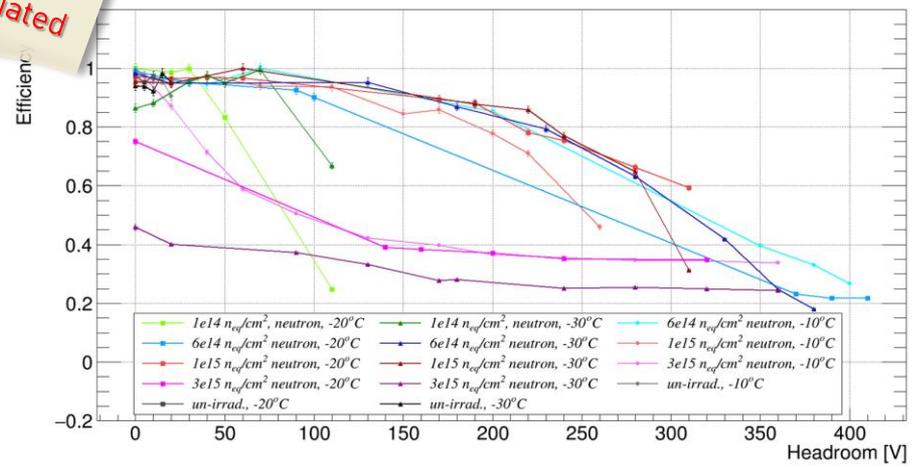
# • Efficiency

## Efficiency vs Headroom – Boron, Gallium

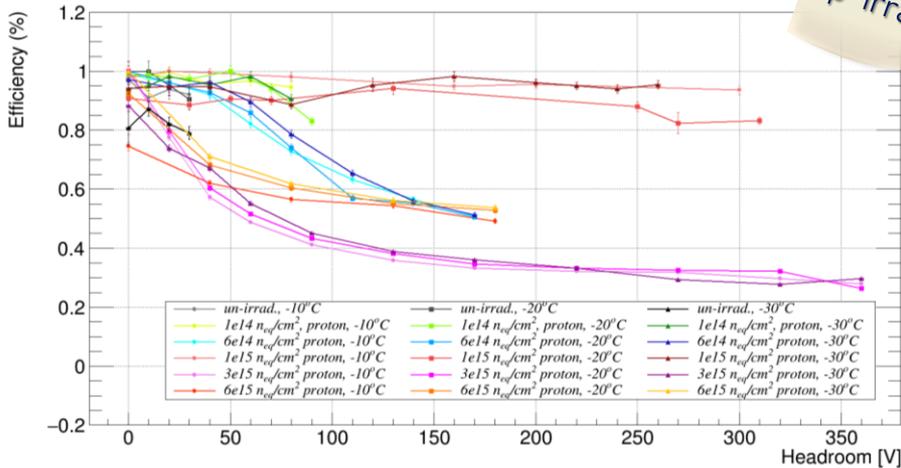
Boron Implanted Gain Layer - Efficiency - Neutron Irradiated



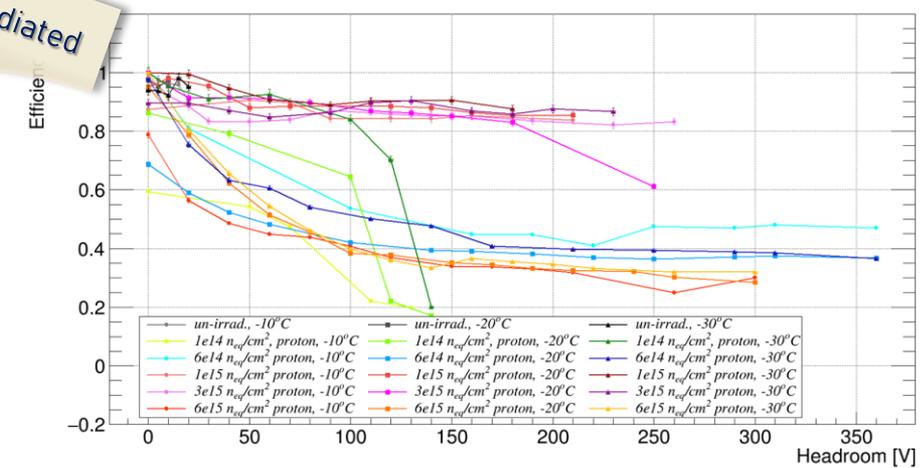
Gallium Implanted Gain Layer - Efficiency - Neutron Irradiated



Boron Implanted Gain Layer - Efficiency - Proton Irradiated



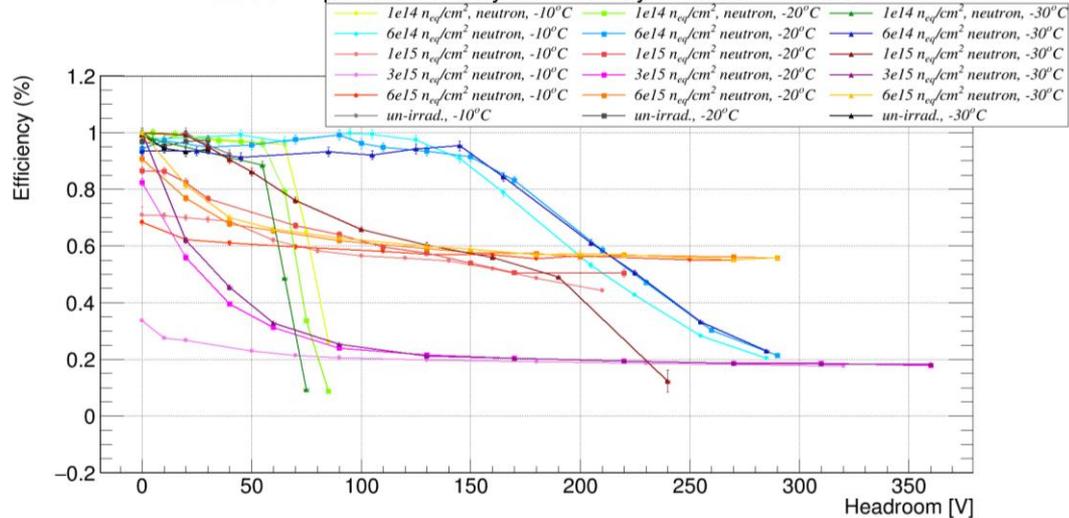
Gallium Implanted Gain Layer - Efficiency - Proton Irradiated



# • Efficiency

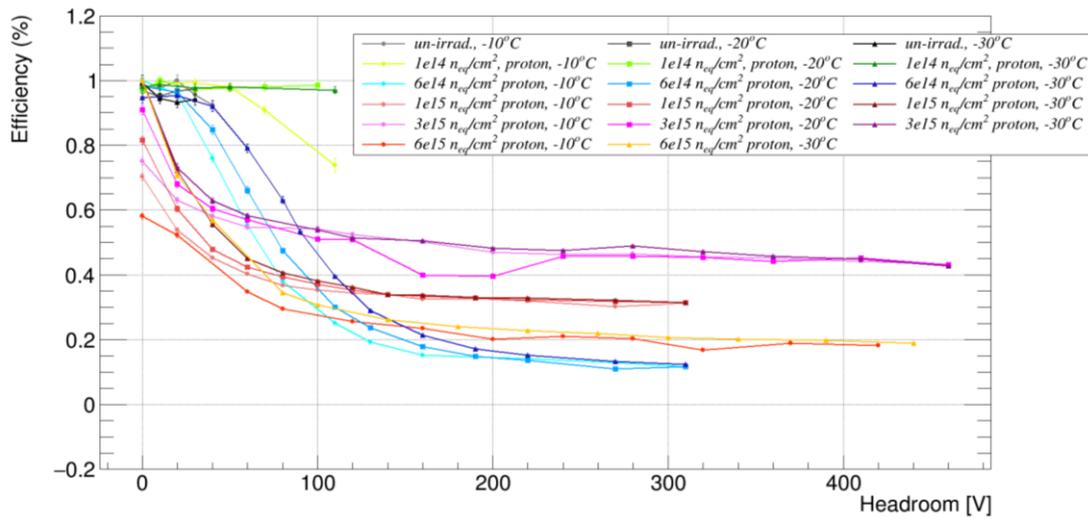
## Efficiency vs Headroom – Carbon

Carbon Implanted Gain Layer - Efficiency - Neutron Irradiated



n irradiated

Carbon Implanted Gain Layer - Efficiency - Proton Irradiated



p irradiated

# • Efficiency

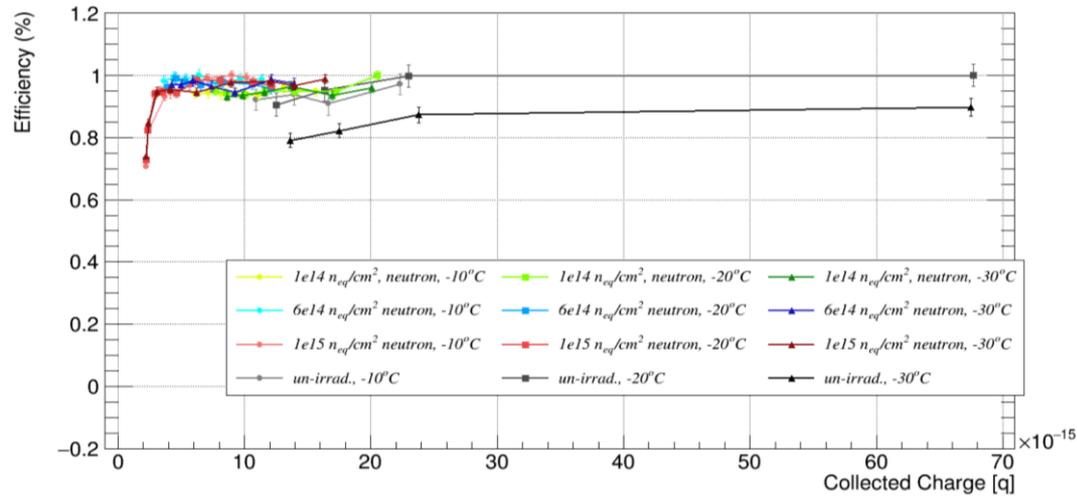
## Head room & efficiency conclusions

- We can achieve  $\sim 100\%$  efficiency for Carbon + Boron and Boron only for up to  $1e15$  at neutron irradiation
- For proton irradiation we achieve  $100\%$  efficiency at  $1e15$  only for boron only sensors
- It seems that boron only at  $3e15$  neutron is close to a  $100\%$ , more study is needed
- Boron only sensors provide larger headroom at  $100\%$  efficiency than boron + carbon combination
- Proton irradiation is more damaging than neutrons if correct scaling factors are applied, reality is somewhere in the middle
- In best case scenario (boron at  $3e15$  neutrons) no safety factor is present

# • Efficiency

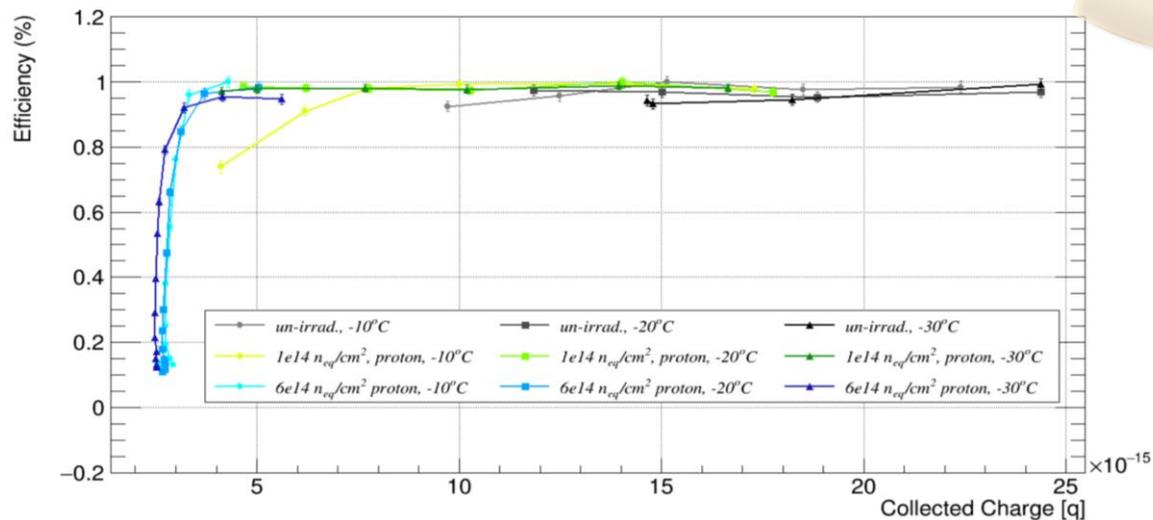
## Efficiency vs Charge – Boron

Boron Implanted Gain Layer - Trigger Frequency - Neutron Irradiated



n irradiated

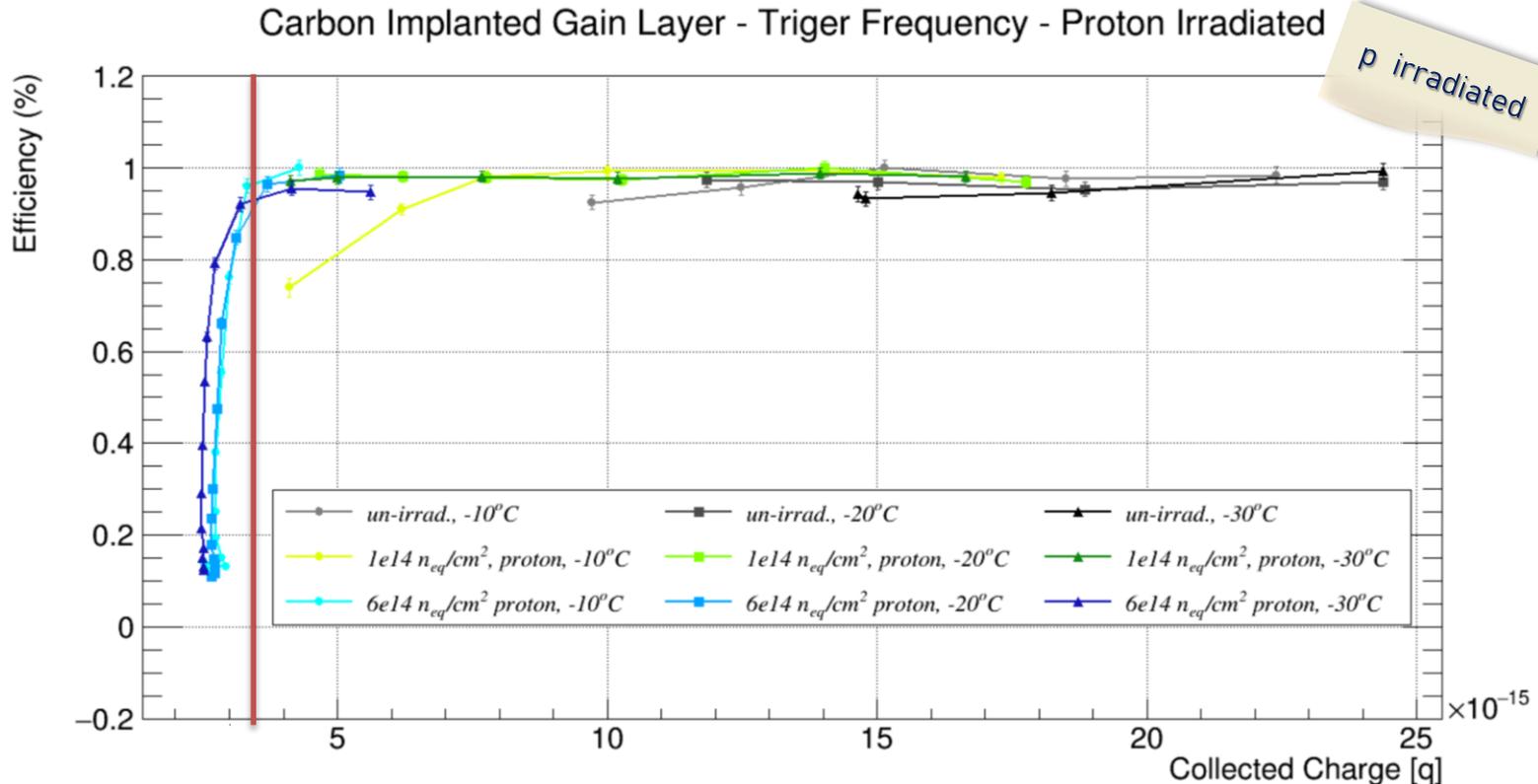
Carbon Implanted Gain Layer - Trigger Frequency - Proton Irradiated



p irradiated

# • Efficiency

## Efficiency vs Charge – Carbon

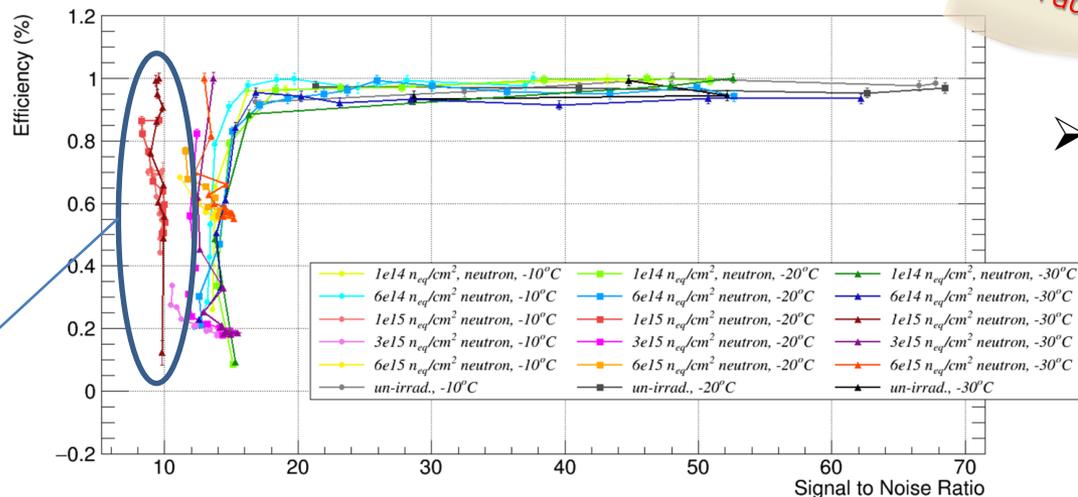


- Regardless of radiation, temperature or implant, for  $Q > 3.5$  fQ sensors are 100 efficient
- Similar behavior on neutron and proton irradiated sensors
- On a fixed threshold trigger  $3.5$  fQ  $\rightarrow$  20mV with an amplification of 100

# • Efficiency

## Efficiency vs SNR – Boron

Carbon Implanted Gain Layer - Efficiency vs SNR - Neutron Irradiated



➤ SNR > 18 is 100 % efficient

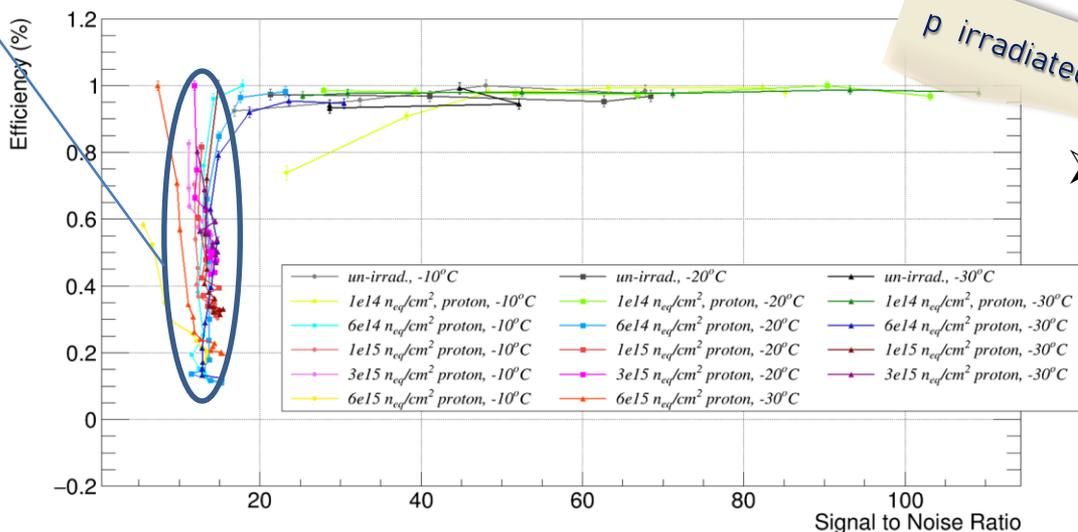
➤ This is a result but not a guarantee!!

➤ One way relationship SNR > 18 → 100 eff,

➤ 100 % efficiency does not guarantee SNR

They never get 100% efficient

Carbon Implanted Gain Layer - Efficiency vs SNR - Proton Irradiated



# •Conclusions on Efficiency

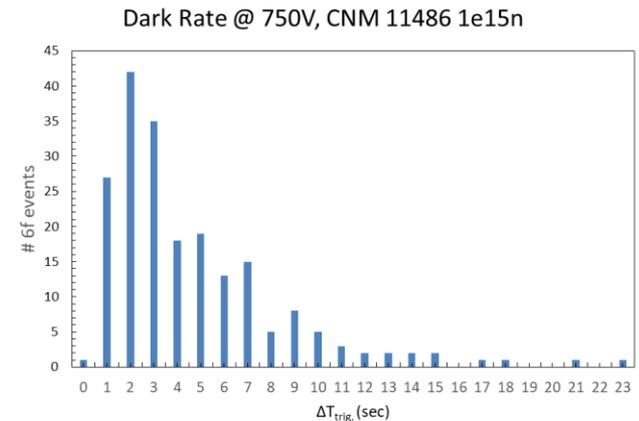
## Charge and SMR

- Independently of implant, irradiation type and temperature all sensors seem to follow the same trend
- More fitting necessary to distinguish possible minute differences (at the level of statistical uncertainties)
- Once an SNR of  $\sim 18$  is reached, a 100% efficiency is expected
- At a charge of  $\sim 4fq$  also a 100% efficiency is to be expected
- Because of the direct relation between SNR and collected charge, assuming a noise of  $0.2fq$ , a 100% efficiency should be reached at  $3,6 fq$

# •Stability

## Concept and measurement

- ✓ Sensors with gain present dark rate at high bias voltage values
- ✓ Dark rate events are result of thermal Brownian electron movement
- ✓ At high fields, these events can get amplified and induce pulses
- ✓ Effect follows the Poisson distribution



### *Dark Rate Estimation Method*

- ✓ **For each bias point:**
  - ✓ Set a fixed threshold unilateral trigger
  - ✓ Remove any external stimuli
  - ✓ Record 4 consecutive events
  - ✓ For each event calculate trigger time distance from first event
  - ✓ Record mean of  $3\Delta t$  values to reject background (cosmics, noise)
  - ✓ Reject values  $< 0.01$  Hz
  - ✓ Calculate the median and the uncertainty of all (500) accepted values
- ✓ **Repeat process for all voltage points until breakdown**
- ✓ **Repeated the process for different temperatures**
- ✓ **Scan constant threshold trigger if required**

X 500



# •Sensor Stability

## Concept and measurement

**Self-trigger time:**

$$\Delta T_{trig}^i = \frac{\sum_{j=1}^{n-1} (T_{j+1}^{trig} - T_j^{trig})}{n}$$

**Self-trigger Rate:**

$$R_{trig}^i = \frac{1}{\Delta T_{trig}^i}$$

X 500

**Median of several rate measurements**

$$\widetilde{R}_{trig} = \frac{R_{trig} \lfloor (\#k+1) \div 2 \rfloor + R_{trig} \lceil (\#k+1) \div 2 \rceil}{2}$$

**Uncertainty on trigger rate:**

$$\delta \widetilde{R}_{trig} (\%) = \sqrt{\frac{(N_{over} + 1) \times (N_{over} + 2)}{(N + 2) \times (N + 3)} - \frac{(N_{over} + 1)^2}{(N + 2)^2}}$$

Efficiency is a binary magnitude, Bayesian approach implemented

**Sigmoid Dark rate Fit:**

$$R_{Dark Rate} = \frac{R_{max}}{1 + e^{C \times (V_{50\%} - V)}} + R_{BaseLine}$$

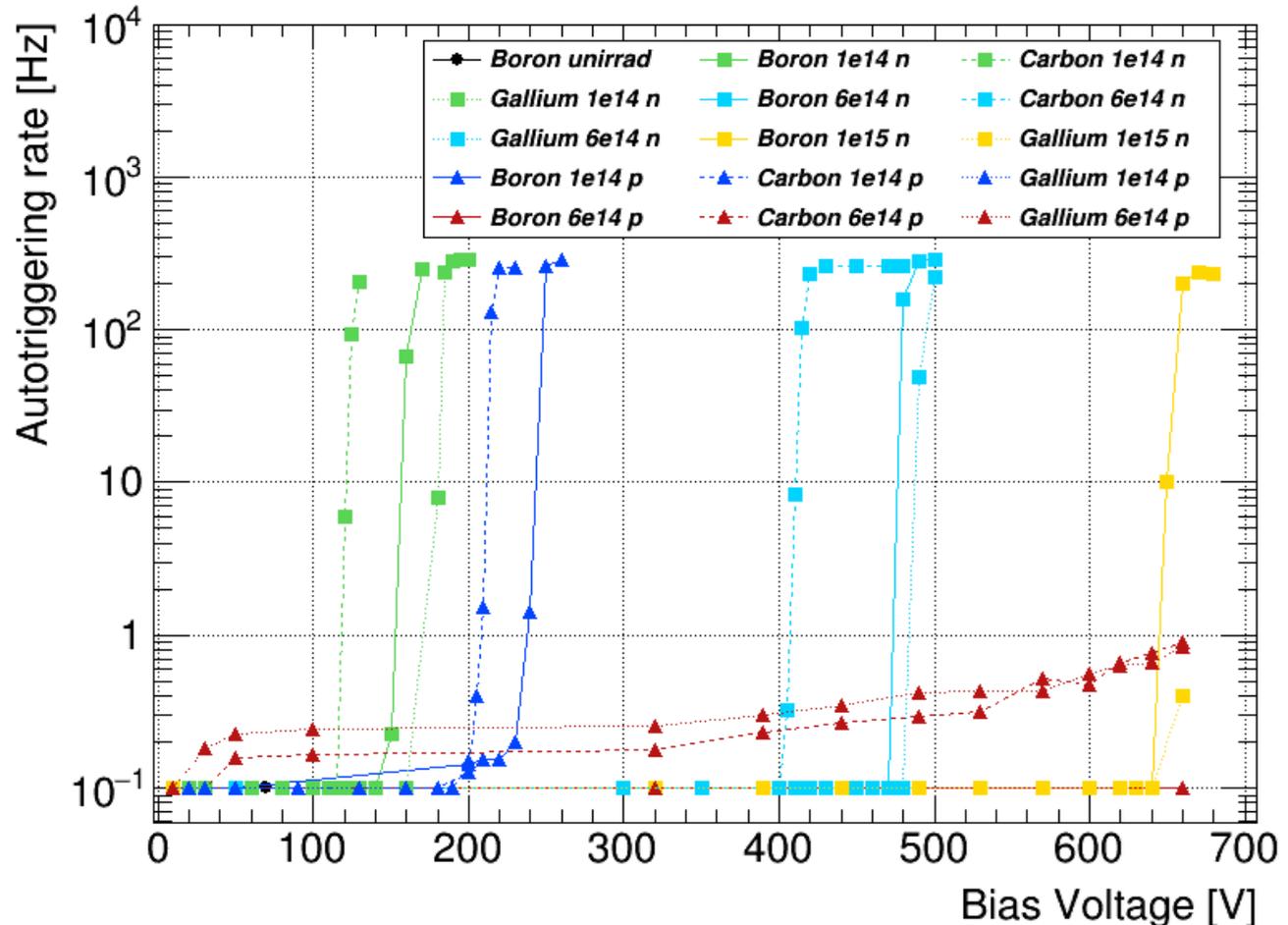
Max, recordable rate  
Inst. saturation point

50% of maximum  
voltage point

Baseline trigger rate  
(noise, radioactivity)

# •Sensor Stability

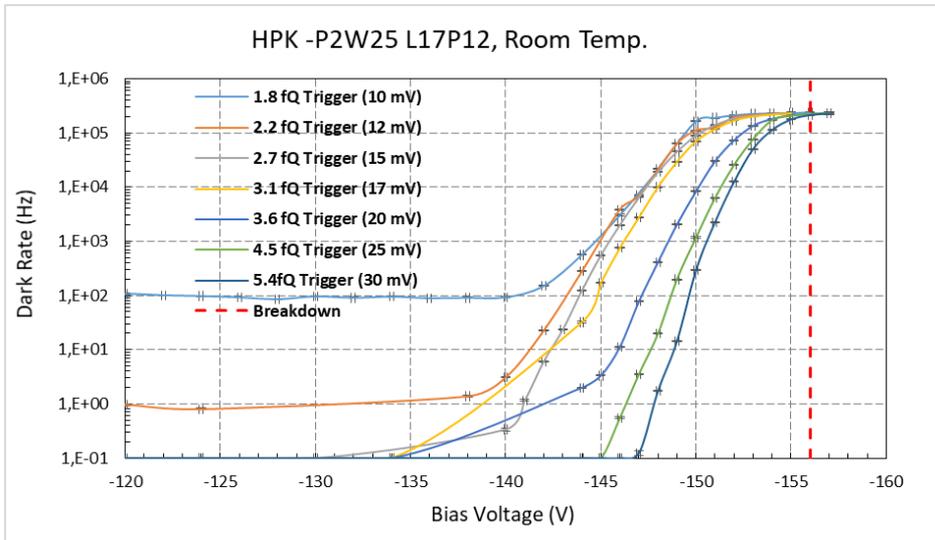
Boron, Gallium, Carbon @ -30°C



- ✓ Carbon presents the most unstable implementation with respect to dark rate
- ✓ Boron is the better solution across the board with higher stability points

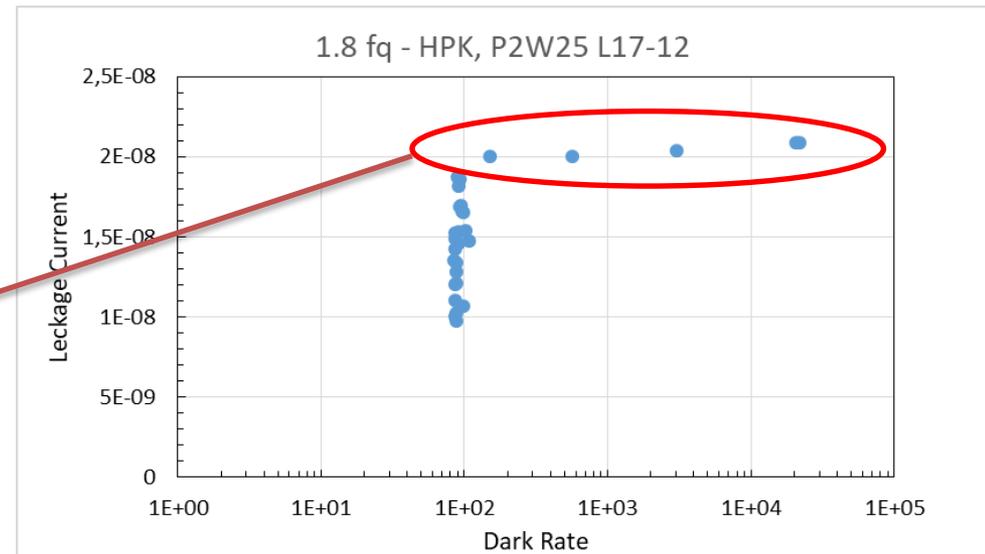
# • Sensor Stability

## HPK P2 @ Room Temp



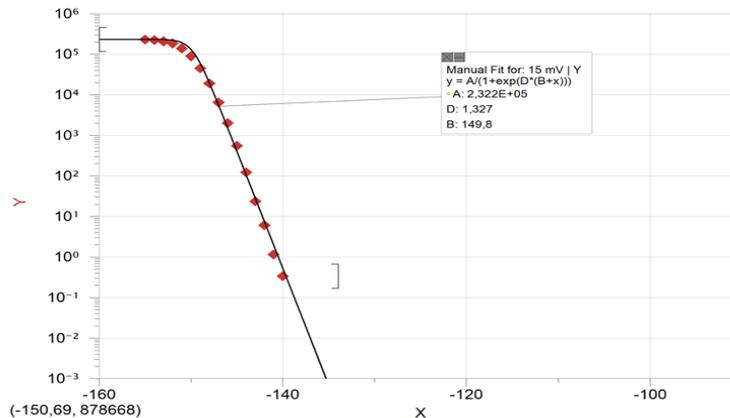
- ✓ Uneradicated HPK P2
- ✓ Breakdown  $\sim 156$ V
- ✓ Measured at room temp
- ✓ Different Constant threshold triggers (1.8 – 5.4 fQ) applied
- ✓ Uncertainties using Bayesian approximation
- ✓ Max saturation rate 230 kHz

- ✓ Sensor far from breakdown
- ✓ Leakage current not demonstrate significant variation
- ✓ Stationary lockage current at exponential rate increase

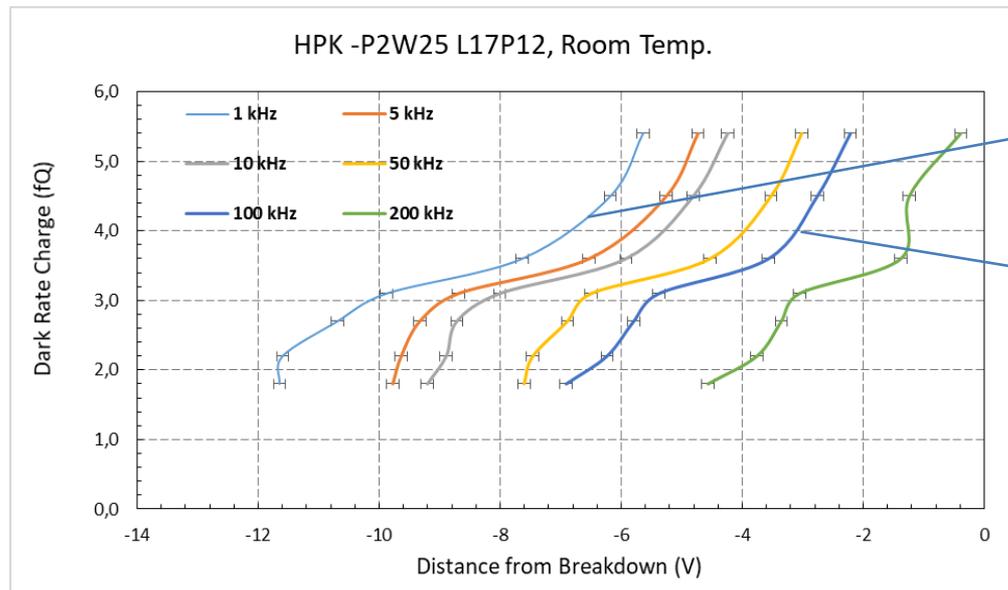


# •Sensor Stability

## HPK P2 @ Room Temp



- ✓ Analytical expressions derived from sigmoid fits in each threshold
- ✓ Estimate expected voltage point for a given dark rate
- ✓ Calculate distance from breakdown voltage per given rate and threshold trigger



- ✓ Depending on dark rate requirements, operation has to stay on the left of the curve
- ✓ For a 4 fQ sensitive ASIC, maxim operating voltage is 3.5V less than breakdown for a 05 % dark rate (assuming full 20 MHz)
- ✓ Dark rate not synchronous

# •Conclusions

---

## Stability and Dark rate

- ✓ Dark rate is an intrinsic characteristic of all gain sensors
- ✓ The effect present itself close to breakdown but clearly before
- ✓ It is common on all producers, productions and implants
- ✓ Carbon is more unstable with respect to Boron
- ✓ Moderate dark rate might be accepted with respect to application
- ✓ On a 4 fq sensitive ASIC one can operate no closer to 4 V below the breakdown to maintain 1% occupancy at 20 MHz
- ✓ Qualification has to be carried out in every producer
- ✓ Strongly depends on gain layer gradient