# QCD and Electroweak physics at Upgrade II

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Science & Technology Facilities Council

#### **UK Research** and Innovation

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# The success of the SM



Overall extremely good experiment-theory agreement

# Differential SM measurements



# Differential SM measurements



# SM physics at HL-LHC/LHCb Upgrade II

# Precision EW/QCD V+jets



Rare processes VBS



$$\begin{split} & \mathcal{L}_{SM} = -\frac{1}{2} \partial_{\nu} g_{\mu}^{\alpha} \partial_{\sigma} g_{\mu}^{\alpha} - g_{\mu}^{\alpha} d^{\alpha} \partial_{\mu} g_{\mu}^{\alpha} g_{\mu}^{\alpha} - \frac{1}{2} \partial_{\mu} A_{\nu} \partial_{\mu} A_{\nu} - \frac{1}{2} (\partial_{\nu} Z_{\mu}^{\alpha} (W_{\mu}^{+} W_{\nu}^{-} - M^{2} W_{\mu}^{+} W_{\mu}^{-}) - Z_{\nu}^{\beta} (W_{\mu}^{+} \partial_{\nu} W_{\mu}^{-} - W_{\mu}^{-} \partial_{\nu} W_{\mu}^{+}) + \mathcal{L}^{\beta} (W_{\nu}^{+} \partial_{\nu} W_{\mu}^{-} - W_{\mu}^{-} \partial_{\nu} W_{\mu}^{+}) - A_{\nu} (W_{\mu}^{+} \partial_{\nu} W_{\mu}^{-} - W_{\mu}^{-} \partial_{\nu} W_{\mu}^{+}) + A_{\mu} (W_{\nu}^{+} \partial_{\nu} W_{\mu}^{-} - W_{\mu}^{-} \partial_{\nu} W_{\mu}^{+}) + \frac{1}{2} g^{2} W_{\mu}^{+} W_{\nu}^{-} W_{\mu}^{-} \partial_{\nu} W_{\mu}^{+}) + A_{\mu} (W_{\nu}^{+} \partial_{\nu} W_{\mu}^{-} - Z_{\mu}^{\mu} \partial_{\nu} \partial_{\mu} W_{\nu}^{+} W_{\nu}^{-}) + g^{2} S_{\omega}^{\mu} (M_{\mu}^{\mu} Z_{\nu}^{W} W_{\nu}^{-} - Z_{\mu}^{\mu} \partial_{\mu} \partial_{\mu} D_{\nu} D_{\mu}^{\mu} - 2M^{2} \partial_{\mu} A_{\mu}^{\mu} \partial_{\nu} \partial_{\mu} - 2M^{2} \partial_{\mu} A_{\mu}^{\mu} \partial_{\mu} \partial_{\mu} - 2M^{2} \partial_{\mu} A_{\mu}^{\mu} \partial_{\mu} \partial_{\mu} - 2M^{2} \partial_{\mu} \partial_{\mu} \partial_{\mu} \partial_{\mu} \partial_{\mu} - 2M^{2} \partial_{\mu} \partial_{\mu} \partial_{\mu} - 2M^{2} \partial_{\mu} \partial_{\mu} \partial_{\mu} \partial_{\mu} - 2M^{2} \partial_{\mu} \partial_{\mu} \partial_{\mu} \partial_{\mu} - 2M^{2} \partial_{\mu} \partial_$$

 $|\mathcal{M}|^2 - \sigma$ 



$$\begin{split} & \mathcal{L}_{SM} = -\frac{1}{2} \partial_{\nu} g_{\mu}^{2} \partial_{\nu} g_{\mu}^{a} - g_{\mu} f^{abc} \partial_{\mu} g_{\nu}^{a} g_{\mu}^{b} g_{\nu}^{c} f^{abc} f^{abc} g_{\mu}^{b} g_{\nu}^{c} g_{\mu}^{c} g_{\nu}^{c} - \partial_{\nu} W_{\mu}^{+} \partial_{\nu} W_{\mu}^{-} - \\ & W_{\mu}^{+} W_{\mu}^{-} - Z_{\nu}^{0} (W_{\mu}^{+} \partial_{\nu} W_{\mu}^{-} - W_{\mu}^{-} \partial_{\nu} W_{\mu}^{+}) + Z_{\mu}^{0} (W_{\nu}^{+} \partial_{\nu} W_{\mu}^{-} - W_{\nu}^{-} \partial_{\nu} W_{\mu}^{+}) - \\ & W_{\nu}^{+} \partial_{\nu} W_{\mu}^{+} ) - \frac{1}{2} g^{2} W_{\mu}^{+} W_{\mu}^{-} W_{\mu}^{-} \partial_{\nu} W_{\mu}^{+}) + Z_{\mu}^{0} (W_{\nu}^{+} \partial_{\nu} W_{\mu}^{-} - W_{\nu}^{-} \partial_{\nu} W_{\mu}^{+}) - \\ & W_{\nu}^{-} \partial_{\nu} W_{\mu}^{+} ) - \frac{1}{2} g^{2} W_{\mu}^{+} W_{\nu}^{-} W_{\mu}^{-} + \frac{1}{2} g^{2} W_{\mu}^{+} W_{\nu}^{-} W_{\mu}^{+} g^{2} \partial_{\nu} (W_{\mu}^{+} W_{\nu}^{-} - \\ & Z_{\mu}^{+} Z_{\mu}^{0} W_{\nu}^{+} W_{\nu}^{-} ) + g^{2} z_{\mu}^{i} (A_{\mu} W_{\nu}^{+} A_{\nu} W_{\nu}^{-} - A_{\mu} A_{\mu} W_{\nu}^{+} W_{\mu}^{-}) + g^{2} s_{wca} (A_{\mu} Z_{\nu}^{0} (W_{\mu}^{+} W_{\nu}^{-} - \\ & Z_{\mu}^{+} Z_{\mu}^{0} W_{\nu}^{+} W_{\nu}^{-}) + \frac{1}{2} \partial_{\mu} (W_{\mu}^{+} W_{\nu}^{-} - \\ & Z_{\mu}^{+} Z_{\mu}^{0} W_{\nu}^{+} W_{\nu}^{-}) + \frac{1}{2} \partial_{\mu} (W_{\mu}^{+} A_{\nu}^{-} - \\ & g_{\mu} (W_{\mu}^{+} W_{\nu}^{-}) - \\ & A_{\mu}^{+} (W_{\mu}^{+} D_{\nu}^{-}) + \frac{1}{2} g_{\mu}^{+} Z_{\mu}^{+} (W_{\nu}^{+} D_{\nu}^{-}) + \\ & g_{\mu} (W_{\mu}^{+} (H_{\mu}^{+} + (\phi^{0})^{4} + 4(\phi^{+} \phi^{-})^{2} + 4(\phi^{0})^{2} \phi^{+} \phi^{+} + H^{+} \phi^{+} \phi^{+} - \\ & g_{\mu} (W_{\mu}^{+} (W_{\mu}^{+} \phi^{-}) - \\ & \frac{1}{2} g^{2} (W_{\mu}^{+} (\Phi^{0} \partial_{\mu} \phi^{-} - \phi^{-} \partial_{\mu} \theta^{+}) - \\ & W_{\mu}^{-} (H_{\mu}^{-} - \phi^{-} \partial_{\mu} H) + W_{\mu}^{-} (H \partial_{\mu} \phi^{+} - \phi^{+} \partial_{\mu} H)) + \frac{1}{2} g_{\nu}^{-} Z_{\mu}^{0} (Z_{\mu}^{0} (W_{\mu}^{+} \phi^{-}) \\ & \frac{1}{2} g^{2} (W_{\mu}^{+} (\Phi^{0} \partial_{\mu}^{-} - W_{\mu}^{0} \phi^{+}) - \\ & g_{\mu}^{-} (W_{\mu}^{+} (\Phi^{0} - 2^{-} \partial_{\mu} \phi^{+}) - \\ & W_{\mu}^{-} \phi^{+}) + \\ & \frac{1}{2} g^{2} (W_{\mu}^{+} (W_{\mu}^{+} \Phi^{-} + W_{\mu}^{-} \partial_{\mu} \phi^{+}) - \\ & \frac{1}{2} g^{2} Z_{\mu}^{0} (W_{\mu}^{+} \Phi^{-} + W_{\mu}^{-} \partial_{\mu} \phi^{+}) - \\ & \frac{1}{2} g^{2} Z_{\mu}^{0} (W_{\mu}^{+} \Phi^{-} + \\ & W_{\mu}^{-} (\Phi^{+} - U_{\mu}^{-} \phi^{+}) - \\ & \frac{1}{2} g^{2} (W_{\mu}^{-} (W_{\mu}^{+} \Phi^{-} - W_{\mu}^{-} \phi^{+}) + \\ & \frac{1}{2} g^{2} Z_{\mu}^{0} (W_{\mu}^{+} \Phi^{+} + \\ & W_{\mu}^$$

 $|\mathcal{M}|^2 - \sigma$ 







# Hard (perturbative) scattering process N(N)LO QCD + EW



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# Hard (perturbative) scattering process N(N)LO QCD + EW

#### **QCD** Bremsstrahlung

- ▶ parton shower
- matched to NLO matrix elements

#### **QED** Bremsstrahlung

- ▶ parton shower
- matched to NLO matrix elements







# Theoretical Predictions for the LHC

Hard (pertudo  $d\sigma = d\sigma_{LO}$ 

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u Z^0_\mu W^+_\mu W^+_\mu W^+$  $\begin{array}{c} W_{\nu}^{+}W_{\mu}^{-}) - Z_{\nu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})) - \\ igs_{w}(\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-} - W_{\nu}^{+}W_{\mu}^{-}) - A_{\nu}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + A_{\mu}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}W_{\mu}^{-}) \\ \end{array}$  $W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})) - \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{+}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}\tilde{W}_{\nu}^{-}W_{\mu}^{+}\tilde{W}_{\nu}^{-} + g^{2}c_{w}^{2}(Z_{\mu}^{0}W_{\mu}^{+}Z_{\nu}^{0}W_{\nu}^{-} - C_{\mu}^{0}W_{\mu}^{-}))$  $\begin{array}{c} Z_{\mu}^{0} Z_{\mu}^{0} W_{\nu}^{+} W_{\nu}^{-}) + g^{2} s_{w}^{2} (A_{\mu} W_{\mu}^{+} A_{\nu} W_{\nu}^{-} - A_{\mu} A_{\mu} W_{\nu}^{+} W_{\nu}^{-}) + g^{2} s_{w} c_{w} (A_{\mu} Z_{\nu}^{0} (W_{\mu}^{+} W_{\nu}^{-} - W_{\nu}^{+} W_{\mu}^{-}) - 2A_{\mu} Z_{\mu}^{0} W_{\nu}^{+} W_{\nu}^{-}) - \frac{1}{2} \partial_{\mu} H \partial_{\mu} H - 2M^{2} \alpha_{h} H^{2} - \partial_{\mu} \phi^{+} \partial_{\mu} \phi^{-} - \frac{1}{2} \partial_{\mu} \phi^{0} \partial_{\mu} \phi^{0} - \frac{1}{2} \partial$  $eta_h \left( rac{2M^2}{a^2} + rac{2M}{a} H + rac{1}{2} (H^2 + \phi^0 \phi^0 + 2\phi^+ \phi^-) 
ight) + rac{2M^4}{a^2} lpha_h \frac{1}{8}g^{2}\alpha_{h}\left(H^{4}+(\phi^{0})^{4}+4(\phi^{+}\phi^{-})^{2}+4(\phi^{0})^{2}\phi^{+}\phi^{-}+4H^{2}\phi^{+}\phi^{-}+2(\phi^{0})^{2}H^{2}\right)$  $g M W^+_\mu W^-_\mu H - rac{1}{2} g rac{M}{c_{e\mu}^2} Z^0_\mu Z^0_\mu H$  –  $rac{1}{2}ig\left(W^+_\mu(\phi^0\partial_\mu\phi^--\phi^-\partial_\mu\phi^0)-W^-_\mu(\phi^0\partial_\mu\phi^+-\phi^+\partial_\mu\phi^0)
ight)+$  $\frac{1}{2}g\left(W^+_{\mu}(H\partial_{\mu}\phi^- - \phi^-\partial_{\mu}H) + W^-_{\mu}(H\partial_{\mu}\phi^+ - \phi^+\partial_{\mu}H)\right) + \frac{1}{2}g\frac{1}{c_w}(Z^0_{\mu}(H\partial_{\mu}\phi^0 - \phi^0\partial_{\mu}H) + \frac{1}{2}g\frac{1}{c_w}(Z^0_{\mu}H)$  $M\left(\frac{1}{c_{w}}Z_{\mu}^{0}\partial_{\mu}\phi^{0}+W_{\mu}^{+}\partial_{\mu}\phi^{-}+W_{\mu}^{-}\partial_{\mu}\phi^{+}\right)-ig\frac{s_{w}^{2}}{c_{w}}MZ_{\mu}^{0}(W_{\mu}^{+}\phi^{-}-W_{\mu}^{-}\phi^{+})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W$  $W^{-}_{\mu}\phi^{+}) - igrac{1-2c_{w}^{2}}{2c_{w}}Z^{0}_{\mu}(\phi^{+}\partial_{\mu}\phi^{-} - \phi^{-}\partial_{\mu}\phi^{+}) + igs_{w}A_{\mu}(\phi^{+}\partial_{\mu}\phi^{-} - \phi^{-}\partial_{\mu}\phi^{+}) \frac{1}{4}g^2 W^+_\mu W^-_\mu \left(H^2 + (\phi^0)^2 + 2\phi^+\phi^-\right) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z^0_\mu Z^0_\mu \left(H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2\phi^+\phi^-\right) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z^0_\mu Z^0_\mu \left(H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2\phi^+\phi^-\right) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z^0_\mu Z^0_\mu \left(H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2\phi^+\phi^-\right) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z^0_\mu Z^0_\mu \left(H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2\phi^+\phi^-\right) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z^0_\mu Z^0_\mu \left(H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2\phi^+\phi^-\right) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z^0_\mu Z^0_\mu \left(H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2\phi^+\phi^-\right) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z^0_\mu Z^0_\mu \left(H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2\phi^+\phi^-\right) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z^0_\mu Z^0_\mu \left(H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2\phi^+\phi^-\right) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z^0_\mu Z^0_\mu \left(H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2\phi^+\phi^-\right) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z^0_\mu Z^0_\mu \left(H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2\phi^+\phi^-\right) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z^0_\mu Z^0_\mu \left(H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2\phi^+\phi^-\right) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z^0_\mu Z^0_\mu \left(H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2\phi^+\phi^-\right) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z^0_\mu Z^0_\mu \left(H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2\phi^+\phi^-\right) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z^0_\mu Z^0_\mu \left(H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2\phi^+\phi^-\right) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z^0_\mu Z^0_\mu \left(H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2\phi^+\phi^-\right) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z^0_\mu Z^0_\mu Z^0_\mu \left(H^2 + (\phi^0)^2 + 2(2s_w^2 - 1)^2\phi^+\phi^-\right) - \frac{1}{8}g^2 \frac{1}{c_w^2} Z^0_\mu Z$  $\frac{1}{2}g^2 \frac{s_{\mu}^2}{c} Z^0_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) - \frac{1}{2}ig^2 \frac{s_{\mu}^2}{c} Z^0_{\mu} H(W^+_{\mu} \phi^- - W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^+) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^-) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^-) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^-) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^-) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^-) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^-) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^-) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^-) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^-) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^-) + \frac{1}{2}g^2 s_w A_{\mu} \phi^-) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^- + W^-_{\mu} \phi^-) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^-) + \frac{1}{2}g^2 s_w A_{\mu} \phi^-) + \frac{1}{2}g^2 s_w A_{\mu} \phi^0(W^+_{\mu} \phi^-) + \frac{1}{2}g^2 s_w A_{\mu} \phi^-) +$  $W^{-}_{\mu}\phi^{+}) + \frac{1}{2}ig^{2}s_{w}A_{\mu}H(W^{+}_{\mu}\phi^{-}-W^{-}_{\mu}\phi^{+}) - g^{2}\frac{s_{w}}{c_{w}}(2c_{w}^{2}-1)Z^{0}_{\mu}A_{\mu}\phi^{+}\phi^{-} - 1)$  $\begin{array}{l} g^2 s_w^2 A_\mu A_\mu \phi^+ \phi^- + \frac{1}{2} i g_s \lambda_{ij}^a (\bar{q}_i^a \gamma^\mu q_j^\sigma) g_\mu^a - \bar{e}^{\lambda} (\gamma \partial + m_e^{\lambda}) e^{\lambda} - \bar{\nu}^{\lambda} (\gamma \partial + m_\nu^{\lambda}) \nu^{\lambda} - \bar{u}_j^{\lambda} (\gamma \partial + m_u^{\lambda}) u_j^{\lambda} - \bar{d}_j^{\lambda} (\gamma \partial + m_d^{\lambda}) d_j^{\lambda} + i g s_w A_\mu \left( -(\bar{e}^{\lambda} \gamma^\mu e^{\lambda}) + \frac{2}{3} (\bar{u}_j^{\lambda} \gamma^\mu u_j^{\lambda}) - \frac{1}{3} (\bar{d}_j^{\lambda} \gamma^\mu d_j^{\lambda}) \right) + \\ \frac{i g}{4 c_w} Z_\mu^0 \left\{ (\bar{\nu}^{\lambda} \gamma^\mu (1 + \gamma^5) \nu^{\lambda}) + (\bar{e}^{\lambda} \gamma^\mu (4 s_w^2 - 1 - \gamma^5) e^{\lambda}) + (\bar{d}_j^{\lambda} \gamma^\mu (\frac{4}{3} s_w^2 - 1 - \gamma^5) d_j^{\lambda}) + \\ \end{array} \right.$  $(\bar{u}_{j}^{\lambda}\gamma^{\mu}(1-\frac{8}{3}s_{w}^{2}+\gamma^{5})u_{j}^{\lambda})\}+\frac{ig}{2\sqrt{2}}W_{\mu}^{+}\left((\bar{\nu}^{\lambda}\gamma^{\mu}(1+\gamma^{5})U^{lep}_{\lambda\kappa}e^{\kappa})+(\bar{u}_{j}^{\lambda}\gamma^{\mu}(1+\gamma^{5})C_{\lambda\kappa}d_{j}^{\kappa})\right)+$  $\frac{ig}{2\sqrt{2}}W^{-}_{\mu}\left((\bar{e}^{\kappa}U^{lep}_{\ \kappa\lambda}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda})+(\bar{d}^{\kappa}_{j}C^{\dagger}_{\kappa\lambda}\gamma^{\mu}(1+\gamma^{5})u^{\lambda}_{j})\right)+$  $\frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{e}^{\kappa}(\bar{\nu}^{\lambda}U^{lep}_{\lambda\kappa}(1-\gamma^{5})e^{\kappa})+m_{\nu}^{\lambda}(\bar{\nu}^{\lambda}U^{lep}_{\lambda\kappa}(1+\gamma^{5})e^{\kappa}\right)+$  $\frac{ig}{2M\sqrt{2}}\phi^{-}\left(m_{e}^{\lambda}(\bar{e}^{\lambda}U^{lep}_{\ \lambda\kappa}^{\dagger}(1+\gamma^{5})\nu^{\kappa})-m_{\nu}^{\kappa}(\bar{e}^{\lambda}U^{lep}_{\ \lambda\kappa}^{\dagger}(1-\gamma^{5})\nu^{\kappa}\right)-\frac{g}{2}\frac{m_{\nu}^{\lambda}}{M}H(\bar{\nu}^{\lambda}\nu^{\lambda}) \frac{g}{2}\frac{m_{\epsilon}^{\lambda}}{M}H(\bar{e}^{\lambda}e^{\lambda}) + \frac{ig}{2}\frac{m_{\nu}^{\lambda}}{M}\phi^{0}(\bar{\nu}^{\lambda}\gamma^{5}\nu^{\lambda}) - \frac{ig}{2}\frac{m_{\epsilon}^{\lambda}}{M}\phi^{0}(\bar{e}^{\lambda}\gamma^{5}e^{\lambda}) - \frac{1}{4}\bar{\nu}_{\lambda}M_{\lambda\kappa}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa} \frac{1}{4}\overline{\nu_{\lambda}}\frac{M_{\lambda\kappa}^{R}\left(1-\gamma_{5}\right)\dot{\nu_{\kappa}}}{m_{\lambda\kappa}^{R}\left(1-\gamma_{5}\right)\dot{\nu_{\kappa}}}+\frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1-\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_$  $\frac{ig}{2M\sqrt{2}}\phi^{-}\left(m_d^{\lambda}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^5)u_j^{\kappa})-m_u^{\kappa}(\bar{d}_j^{\lambda}C_{\lambda\kappa}^{\dagger}(1-\gamma^5)u_j^{\kappa}\right)-\frac{g}{2}\frac{m_u^{\lambda}}{M}H(\bar{u}_j^{\lambda}u_j^{\lambda}) \frac{g}{2}\frac{m_{\dot{d}}^{\lambda}}{M}H(\bar{d}_{j}^{\lambda}d_{j}^{\lambda}) + \frac{ig}{2}\frac{m_{u}^{\lambda}}{M}\phi^{0}(\bar{u}_{j}^{\lambda}\gamma^{5}u_{j}^{\lambda}) - \frac{ig}{2}\frac{m_{\dot{d}}^{\lambda}}{M}\phi^{0}(\bar{d}_{j}^{\lambda}\gamma^{5}d_{j}^{\lambda}) + \bar{G}^{a}\partial^{2}G^{a} + g_{s}f^{abc}\partial_{\mu}\bar{G}^{a}G^{b}g_{\mu}^{c} + \bar{X}^{+}(\partial^{2}-M^{2})X^{+} + \bar{X}^{-}(\partial^{2}-M^{2})X^{-} + \bar{X}^{0}(\partial^{2}-\frac{M^{2}}{c_{v}^{2}})X^{0} + \bar{Y}\partial^{2}Y + igc_{w}W_{\mu}^{+}(\partial_{\mu}\bar{X}^{0}X^{-} - \bar{X}^{0})X^{-} + \bar{X}^{-}(\partial^{2}-M^{2})X^{-} + \bar{X}^{0}(\partial^{2}-\frac{M^{2}}{c_{v}^{2}})X^{0} + \bar{Y}\partial^{2}Y + igc_{w}W_{\mu}^{+}(\partial_{\mu}\bar{X}^{0}X^{-} - \bar{X}^{0})X^{-} + \bar{X}^{-}(\partial^{2}-M^{2})X^{-} + \bar{X}^{-}(\partial^{2}-M^{2}$  $\partial_{\mu}ar{X}^{+}X^{0})+igs_{w}W^{+}_{\mu}(\partial_{\mu}ar{Y}X^{-}-\partial_{\mu}ar{X}^{+}Y)+igc_{w}W^{-}_{\mu}(\partial_{\mu}ar{X}^{-}X^{0}-\partial_{\mu}ar{X}^{0}X^{+})+igs_{w}W^{-}_{\mu}(\partial_{\mu}ar{X}^{-}Y-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+}-\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{X}^{+}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{Y}X^{+})+igc_{w}Z^{0}_{\mu}(\partial_{\mu}ar{Y}X^{+})+igc_{w$  $\partial_\mu ar{X}^- X^-) + igs_w A_\mu (\partial_\mu ar{X}^+ X^+ \partial_{\mu} ar{X}^{-} X^{-}) - rac{1}{2} g M \left( ar{X}^{+} X^{+} H + ar{X}^{-} X^{-} H + rac{1}{c_{w}^{2}} ar{X}^{0} X^{0} H 
ight) + rac{1 - 2c_{w}^{2}}{2c_{w}} i g M \left( ar{X}^{+} X^{0} \phi^{+} - ar{X}^{-} X^{0} \phi^{-} 
ight) +$ 

 $\mathcal{L}_{SM} = -\frac{1}{2} \partial_{\nu} g^a_{\mu} \partial_{\nu} g^a_{\mu} - g_s f^{abc} \partial_{\mu} g^a_{\nu} g^b_{\mu} g^c_{\nu} - \frac{1}{4} g^2_s f^{abc} f^{ade} g^b_{\mu} g^c_{\nu} g^d_{\mu} g^e_{\nu} - \partial_{\nu} W^+_{\mu} \partial_{\nu} W^-_{\mu} - \frac{1}{4} g^2_s f^{abc} f^{ade} g^b_{\mu} g^c_{\nu} g^d_{\mu} g^e_{\nu} - \frac{1}{4} g^2_s f^{abc} f^{ade} g^b_{\mu} g^c_{\nu} g^d_{\mu} g^e_{\nu} - \frac{1}{4} g^2_s f^{abc} f^{ade} g^b_{\mu} g^c_{\nu} g^d_{\mu} g^e_{\nu} - \frac{1}{4} g^2_s f^{abc} f^{ade} g^b_{\mu} g^c_{\nu} g^d_{\mu} g^e_{\nu} - \frac{1}{4} g^2_s f^{abc} f^{ade} g^b_{\mu} g^c_{\nu} g^d_{\mu} g^e_{\nu} - \frac{1}{4} g^2_s f^{abc} f^{ade} g^b_{\mu} g^c_{\nu} g^d_{\mu} g^e_{\nu} - \frac{1}{4} g^2_s f^{abc} f^{abc} g^b_{\mu} g^c_{\nu} g^d_{\mu} g^e_{\nu} - \frac{1}{4} g^2_s f^{abc} f^{abc} g^b_{\mu} g^c_{\nu} g^d_{\mu} g^e_{\nu} - \frac{1}{4} g^2_s f^{abc} f^{abc} g^b_{\mu} g^c_{\nu} g^d_{\mu} g^e_{\nu} - \frac{1}{4} g^2_s f^{abc} f^{abc} g^b_{\mu} g^c_{\nu} g^d_{\mu} g^e_{\nu} - \frac{1}{4} g^2_s f^{abc} g^b_{\mu} g^c_{\nu} g^d_{\mu} g^e_{\nu} - \frac{1}{4} g^2_s g^a_{\mu} g^b_{\nu} g^c_{\mu} g^e_{\nu} g^d_{\mu} g^e_{\nu} - \frac{1}{4} g^2_s g^a_{\mu} g^e_{\nu} g^d_{\mu} g^e_{\nu} g^e_{\mu} g^e_{\mu} g^e_{\nu} g^e_{\mu} g$ 

 $\frac{1}{2c_w} igM \left( ar{X}^0 X^- \phi^+ - ar{X}^0 X^+ \phi^- 
ight) + igMs_w \left( ar{X}^0 X^- \phi^+ - ar{X}^0 X^+ \phi^- 
ight) + rac{1}{2} igM \left( ar{X}^+ X^+ \phi^0 - ar{X}^- X^- \phi^0 
ight) \,.$ 

Hard (perturbative) scattering process:

 $d\sigma = d\sigma_{\rm LO} + \alpha_{S} \, d\sigma_{\rm NLO} + \alpha_{\rm EW} \, d\sigma_{\rm NLO \, EW}$ 

 $+\alpha_{S}^{2} d\sigma_{\rm NNLO} + \alpha_{\rm EW}^{2} d\sigma_{\rm NNLO\,EW} + \alpha_{S} \alpha_{\rm EW} d\sigma_{\rm NNLO\,QCDxEW}$ 

# Theoretical Predictions for the LHC

Hard (perturbative) scattering process:  $d\sigma = d\sigma_{\rm LO} + \alpha_S \, d\sigma_{\rm NLO} + \alpha_{\rm EW} \, d\sigma_{\rm NLO \, EW}$ 

$$\mathrm{d}\sigma_{\mathrm{NLO}} = \frac{1}{2s}$$

 $\mathcal{M}_{\rm NLO,V}$  $\mathcal{M}_{\mathrm{NLO,R}}$ 

- •soft/collinear cancellations+PDF renormalisation  $\Rightarrow$  reduction of  $\mu_F$  dependence

 $\mathcal{L}_{SM} = -\frac{1}{2} \partial_{\nu} g^{a}_{\mu} \partial_{\nu} g^{a}_{\mu} - g_{s} f^{abc} \partial_{\mu} g^{a}_{\nu} g^{b}_{\mu} g^{c}_{\nu} - \frac{1}{4} g^{2}_{s} f^{abc} f^{abc} g^{b}_{\mu} g^{c}_{\nu} g^{d}_{\mu} g^{e}_{\nu} - \partial_{\nu} W^{+}_{\mu} \partial_{\nu} W^{-}_{\mu} - M^{2} W^{+}_{\mu} W^{-}_{\mu} - \frac{1}{2} \partial_{\nu} Z^{0}_{\mu} \partial_{\nu} Z^{0}_{\mu} - \frac{1}{2c^{2}_{w}} M^{2} Z^{0}_{\mu} Z^{0}_{\mu} - \frac{1}{2} \partial_{\mu} A_{\nu} \partial_{\mu} A_{\nu} - igc_{w} (\partial_{\nu} Z^{0}_{\mu} (W^{+}_{\mu} W^{-}_{\nu} - M^{2}_{\nu} G^{0}_{\nu} ) - \frac{1}{2c^{2}_{w}} M^{2} Z^{0}_{\mu} Z^{0}_{\mu} - \frac{1}{2} \partial_{\mu} A_{\nu} \partial_{\mu} A_{\nu} - igc_{w} (\partial_{\nu} Z^{0}_{\mu} (W^{+}_{\mu} W^{-}_{\nu} - M^{2}_{\nu} ) - \frac{1}{2c^{2}_{w}} M^{2} Z^{0}_{\mu} Z^{0}_{\mu} - \frac{1}{2} \partial_{\mu} Z^{0}_{\mu} \partial_{\nu} Z^{0}_{\mu} - \frac{1}{2c^{2}_{w}} M^{2} Z^{0}_{\mu} Z^{0}_{\mu} - \frac{1}{2} \partial_{\mu} Z^{0}_{\mu} \partial_{\nu} Z^{0}_{\mu} - \frac{1}{2c^{2}_{w}} M^{2}_{\mu} - \frac{1}{2c^{2}_{w$  $\begin{array}{l} W_{\nu}^{+}W_{\mu}^{-})-Z_{\nu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-}-W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+})+Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-}-W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+}))-igs_{w}(\partial_{\nu}A_{\mu}(W_{\mu}^{+}W_{\nu}^{-}-W_{\nu}^{+}W_{\mu}^{-})-A_{\nu}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-}-W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+})+A_{\mu}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-}-W_{\nu}^{-}W_{\nu}^{-}) \end{array}$  $\widetilde{W_{\nu}^{-}\partial_{\nu}W_{\mu}^{-}})) - \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-}W_{\nu}^{+}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\nu}^{-}W_{\mu}^{+}W_{\nu}^{-} + g^{2}c_{w}^{2}(Z_{\mu}^{0}W_{\mu}^{+}Z_{\nu}^{0}W_{\nu}^{-} - C_{\mu}^{0}W_{\mu}^{-})) - \frac{1}{2}g^{2}W_{\mu}^{+}W_{\nu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\nu}^{-}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\mu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+} + \frac{1}{2}g^{2}$  $\begin{array}{c} Z_{\mu}^{0} Z_{\mu}^{0} W_{\nu}^{+} W_{\nu}^{-}) + g^{2} s_{w}^{2} (A_{\mu} W_{\mu}^{+} A_{\nu} W_{\nu}^{-} - A_{\mu} A_{\mu} W_{\nu}^{+} W_{\nu}^{-}) + g^{2} s_{w} c_{w} (A_{\mu} Z_{\nu}^{0} (W_{\mu}^{+} W_{\nu}^{-} - W_{\nu}^{+} W_{\mu}^{-}) - 2A_{\mu} Z_{\mu}^{0} W_{\nu}^{+} W_{\nu}^{-}) - \frac{1}{2} \partial_{\mu} H \partial_{\mu} H - 2M^{2} \alpha_{h} H^{2} - \partial_{\mu} \phi^{+} \partial_{\mu} \phi^{-} - \frac{1}{2} \partial_{\mu} \phi^{0} \partial_{\mu} \phi^{0} - \frac{1}{2} \partial_{\mu} \partial_{\mu} \partial_{\mu} \partial_{\mu} \partial_{\mu} \phi^{0} - \frac{1}{2} \partial_{\mu} \partial_{$  $\beta_h \left( \frac{2M^2}{a^2} + \frac{2M}{a}H + \frac{1}{2}(H^2 + \phi^0\phi^0 + 2\phi^+\phi^-) \right) + \frac{2M^4}{a^2}\alpha_h$  $g \alpha_h M (H^3 + H \phi^0 \phi^0 + 2H \phi^+ \phi^-) {\textstyle \frac{1}{8}} g^2 \alpha_h \left( H^4 + (\phi^0)^4 + 4(\phi^+\phi^-)^2 + 4(\phi^0)^2 \phi^+ \phi^- + 4 H^2 \phi^+ \phi^- + 2(\phi^0)^2 H^2 \right)$  $gMW^+_\mu W^-_\mu H - rac{1}{2}grac{M}{c_w^2}Z^0_\mu Z^0_\mu H$   $rac{1}{2} ig \left( W^+_\mu (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - W^-_\mu (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0) 
ight) +$  $\frac{1}{2}g\left(W^+_\mu(H\partial_\mu\phi^- - \phi^-\partial_\mu H) + W^-_\mu(H\partial_\mu\phi^+ - \phi^+\partial_\mu H)\right) + \frac{1}{2}g\frac{1}{c_w}(Z^0_\mu(H\partial_\mu\phi^0 - \phi^0\partial_\mu H) +$  $M\left( \tfrac{1}{c_{w}} Z_{\mu}^{0} \partial_{\mu} \phi^{0} + W_{\mu}^{+} \partial_{\mu} \phi^{-} + W_{\mu}^{-} \partial_{\mu} \phi^{+} \right) - ig \tfrac{s_{w}^{2}}{c_{w}} M Z_{\mu}^{0} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{-}) + ig s_{w} M A_{\mu} (W_{\mu}^{+} \phi^{-}) + ig s_{w} ($  $W^-_\mu \phi^+) - ig rac{1-2c_w^2}{2c_w} Z^0_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) - ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^+ \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w A_\mu (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^-) + ig s_w (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^+) + ig s_w (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^-) + ig s_w (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^-) + ig s_w (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^-) + ig s_w (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^-) + ig s_w (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^-) + ig s_w (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^-) + ig s_w (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^-) + ig s_w (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^-) + ig s_w (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^-) + ig s_w (\phi^- \partial_\mu \phi^- - \phi^- \partial_\mu \phi^-) + ig s_w (\phi^- \partial_\mu \phi^- - \phi^-$  $\frac{1}{4}g^2W_{\mu}^{-}W_{\mu}^{-}\left(H^2+\widetilde{(\phi^0)^2}+2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)$  $\frac{1}{2}g^2\frac{s_w^2}{c_w}Z^0_{\mu}\phi^0(W^+_{\mu}\phi^- + W^-_{\mu}\phi^+) - \frac{1}{2}ig^2\frac{s_w^2}{c_w}Z^0_{\mu}H(W^+_{\mu}\phi^- - W^-_{\mu}\phi^+) + \frac{1}{2}g^2s_wA_{\mu}\phi^0(W^+_{\mu}\phi^- + W^-_{\mu}\phi^-) + \frac{1}{2}g^2s_wA_{\mu}\phi^-) + \frac{1}{2}g^2s_wA_{\mu}\phi^- + \frac{1}{2}g^2s_wA_{\mu}\phi^-) + \frac{1}{2}g^2s_wA_{\mu}\phi^- + \frac{1}{2}g^2s_wA_{\mu}\phi^-) + \frac{1}{2}g^2s_wA_{\mu}\phi^-) + \frac{1}{2}g^2s_wA_{\mu}\phi^- + \frac{1}{2}g^2s_wA_{\mu}\phi^-) + \frac{1}{2}g^2s_wA_{\mu}\phi^-) + \frac{1}{2}g^2s_wA_{\mu}\phi^-) + \frac{1}{2}g^2s_wA_{\mu}\phi^-) + \frac{1}{2}g^2s_wA_{\mu}\phi^-) + \frac{1}{2}g^$  $\begin{array}{l} \frac{1}{2g} g_{\frac{1}{cw}} Z_{\mu} \varphi \left( \psi_{\mu} \varphi + \psi_{\mu} \varphi \right) - \frac{1}{2} i g_{\frac{1}{cw}} Z_{\mu} \Pi \left( \psi_{\mu} \varphi - \psi_{\mu} \varphi \right) + \frac{1}{2} g_{\frac{1}{2w}} S_{w} A_{\mu} \varphi \left( \psi_{\mu} \varphi + \psi_{\mu} \varphi \right) + \frac{1}{2} g_{\frac{1}{2}} S_{w} A_{\mu} \varphi \left( \psi_{\mu} \varphi + \psi_{\mu} \varphi \right) + \frac{1}{2} g_{\frac{1}{2}} S_{w} A_{\mu} \varphi \left( \psi_{\mu} \varphi + \psi_{\mu} \varphi \right) + \frac{1}{2} g_{\frac{1}{2}} S_{w} A_{\mu} \varphi \left( \psi_{\mu} \varphi + \psi_{\mu} \varphi \right) + \frac{1}{2} g_{\frac{1}{2}} S_{w} A_{\mu} \varphi \left( \psi_{\mu} \varphi + \psi_{\mu} \varphi \right) + \frac{1}{2} g_{\frac{1}{2}} S_{w} A_{\mu} \varphi \left( \psi_{\mu} \varphi + \psi_{\mu} \varphi \right) + \frac{1}{2} g_{\frac{1}{2}} S_{w} A_{\mu} \varphi \left( \psi_{\mu} \varphi + \psi_{\mu} \varphi \right) + \frac{1}{2} g_{\frac{1}{2}} S_{w} A_{\mu} \varphi \left( \psi_{\mu} \varphi + \psi_{\mu} \varphi \right) + \frac{1}{2} g_{\frac{1}{2}} S_{w} A_{\mu} \varphi \left( \psi_{\mu} \varphi + \psi_{\mu} \varphi \right) + \frac{1}{2} g_{\frac{1}{2}} g_{\frac{1}{2}} (\gamma \partial + \psi_{\mu} \partial + \psi_{\mu}$  $\frac{ig}{2\sqrt{2}}W^{-}_{\mu}\left((\bar{e}^{\kappa}U^{lep^{\dagger}}_{\kappa\lambda}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda})+(\bar{d}^{\kappa}_{j}C^{\dagger}_{\kappa\lambda}\gamma^{\mu}(1+\gamma^{5})u^{\lambda}_{j})\right)+$  $\frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{e}^{\kappa}(\bar{\nu}^{\lambda}U^{lep}{}_{\lambda\kappa}(1-\gamma^{5})e^{\kappa})+m_{\nu}^{\lambda}(\bar{\nu}^{\lambda}U^{lep}{}_{\lambda\kappa}(1+\gamma^{5})e^{\kappa})+\right.$  $\frac{ig}{2M\sqrt{2}}\phi^{-}\left(m_{e}^{\lambda}(\bar{e}^{\lambda}U^{lep}_{\lambda\kappa}^{\dagger}(1+\gamma^{5})\nu^{\kappa})-m_{\nu}^{\kappa}(\bar{e}^{\lambda}U^{lep}_{\lambda\kappa}^{\dagger}(1-\gamma^{5})\nu^{\kappa}\right)-\frac{g}{2}\frac{m_{\lambda}^{\lambda}}{M}H(\bar{\nu}^{\lambda}\nu^{\lambda}) \frac{g}{2}\frac{m_{e}^{\lambda}}{M}H(\bar{e}^{\lambda}e^{\lambda}) + \frac{ig}{2}\frac{m_{\nu}^{\lambda}}{M}\phi^{0}(\bar{\nu}^{\lambda}\gamma^{5}\nu^{\lambda}) - \frac{ig}{2}\frac{m_{e}^{\lambda}}{M}\phi^{0}(\bar{e}^{\lambda}\gamma^{5}e^{\lambda}) - \frac{1}{4}\bar{\nu}_{\lambda}M_{\lambda\kappa}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa} - \frac{ig}{2}\frac{m_{e}^{\lambda}}{M}\phi^{0}(\bar{\nu}^{\lambda}\gamma^{5}\nu^{\lambda}) - \frac{ig}{2}\frac{m_{e}^{\lambda}}{M}\phi^{0}(\bar{\nu}^{\lambda}\gamma^{\lambda}) - \frac{ig}{2}\frac{m_{e}^{\lambda}}{M}\phi^{0}($  $\frac{1}{4}\overline{\nu_{\lambda}}\frac{M_{\lambda\kappa}^{R}\left(1-\gamma_{5}\right)\dot{\nu_{\kappa}}}{m_{\lambda\kappa}^{R}\left(1-\gamma_{5}\right)\dot{\nu_{\kappa}}}+\frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1-\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa})+m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_$  $\frac{ig}{2M\sqrt{2}}\phi^{-}\left(m_{d}^{\lambda}(\bar{d}_{j}^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^{5})u_{j}^{\kappa})-m_{u}^{\kappa}(\bar{d}_{j}^{\lambda}C_{\lambda\kappa}^{\dagger}(1-\gamma^{5})u_{j}^{\kappa})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\right.$  $\frac{g}{2}\frac{m_{d}^{\lambda}}{M}H(\bar{d}_{j}^{\lambda}d_{j}^{\lambda}) + \frac{ig}{2}\frac{m_{u}^{\lambda}}{M}\phi^{0}(\bar{u}_{j}^{\lambda}\gamma^{5}u_{j}^{\lambda}) - \frac{ig}{2}\frac{m_{d}^{\lambda}}{M}\phi^{0}(\bar{d}_{j}^{\lambda}\gamma^{5}d_{j}^{\lambda}) + \bar{G}^{a}\partial^{2}G^{a} + g_{s}f^{abc}\partial_{\mu}\bar{G}^{a}G^{b}g_{\mu}^{c} + \bar{X}^{+}(\partial^{2}-M^{2})X^{+} + \bar{X}^{-}(\partial^{2}-M^{2})X^{-} + \bar{X}^{0}(\partial^{2}-\frac{M^{2}}{c_{v}^{2}})X^{0} + \bar{Y}\partial^{2}Y + igc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-} - \bar{X}^{0})X^{-} + \bar{X}^{0}(\partial^{2}-M^{2})X^{-} + \bar{X}^{0}(\partial^{2}-M^{2})X^{-} + \bar{X}^{0}(\partial^{2}-M^{2})X^{0} + \bar{Y}\partial^{2}Y + igc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-} - \bar{X}^{0})X^{0} + \bar{X}^{0}(\partial^{2}-M^{2})X^{0} + \bar{X}^{0}(\partial^$  $\begin{array}{l} \partial_{\mu}\bar{X}^{+}X^{0} + igs_{w}W^{+}_{\mu}(\partial_{\mu}\bar{Y}X^{-} - \partial_{\mu}\bar{X}^{+}Y) + igc_{w}W^{-}_{\mu}(\partial_{\mu}\bar{X}^{-}X^{0} - \partial_{\mu}\bar{X}^{0}X^{+}) + igs_{w}W^{-}_{\mu}(\partial_{\mu}\bar{X}^{-}Y - \partial_{\mu}\bar{Y}X^{+}) + igc_{w}Z^{0}_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+} - \partial_{\mu}\bar{Y}X^{+}) + igc_{w}Z^{0}_{\mu}(\partial_{\mu}\bar{X}^{+}X^{+}) + igc_{w}Z^{0}_{\mu}(\partial_{\mu}\bar{X}^{-}X^{-}) + igc_{w}Z^{0}_{\mu}(\partial_{\mu}\bar{X}^{-}) + igc_{w}Z^{0}_{\mu}(\partial_{\mu}\bar{X}^{-}X^{-}) + igc_{w}Z^{0}_{\mu}(\partial_{\mu}\bar{X}^{-}) + igc_$  $\partial_\mu ar X^- X^-) {+} igs_w A_\mu (\partial_\mu ar X^+ X^+ \partial_{\mu}\bar{X}^{-}X^{-}) - \frac{1}{2}gM\left(\bar{X}^{+}X^{+}H + \bar{X}^{-}X^{-}H + \frac{1}{c_{w}^{2}}\bar{X}^{0}X^{0}H\right) + \frac{1-2c_{w}^{2}}{2c_{w}}igM\left(\bar{X}^{+}X^{0}\phi^{+} - \bar{X}^{-}X^{0}\phi^{-}\right) + \frac{1}{2}gM\left(\bar{X}^{+}X^{0}\phi^{+} - \bar{X}^{0}\phi^{+}\right) + \frac$  $\frac{1}{2c_w} igM(ar{X}^0 X^- \phi^+ - ar{X}^0 X^+ \phi^-) + igMs_w(ar{X}^0 X^- \phi^+ - ar{X}^0 X^+ \phi^-) +$ 

$$|\mathcal{M}|^2 - \sigma$$

 $\frac{1}{2}igM\left(\bar{X}^{+}X^{+}\phi^{0}-\bar{X}^{-}X^{-}\phi^{0}
ight)$  .

- $+\alpha_{S}^{2} d\sigma_{\rm NNLO} + \alpha_{\rm EW}^{2} d\sigma_{\rm NNLO\,EW} + \alpha_{S} \alpha_{\rm EW} d\sigma_{\rm NNLO\,QCDxEW}$





# Theoretical Predictions for the LHC

Hard (perturbative) scattering process:  $d\sigma = d\sigma_{\rm LO} + \alpha_S \, d\sigma_{\rm NLO} + \alpha_{\rm EW} \, d\sigma_{\rm NLO \, EW}$ 

 $d\hat{\sigma}_{\rm NNLO} = \frac{1}{2s}$ 



 $\mathcal{L}_{SM} = -rac{1}{2}\partial_
u g^a_\mu \partial_
u g^a_\mu - g_s f^{abc} \partial_\mu g^a_
u g^b_
u g^c_
u - rac{1}{4}g^2_s f^{abc} f^{ade} g^b_\mu g^c_
u g^d_\mu g^e_
u - \partial_
u W^+_\mu \partial_
u W^-_\mu$  $M^{2}W_{\mu}^{+}W_{\mu}^{-} - \frac{1}{2}\partial_{\nu}Z_{\mu}^{0}\partial_{\nu}Z_{\mu}^{0} - \frac{1}{2c_{w}^{2}}M^{2}Z_{\mu}^{0}Z_{\mu}^{0} - \frac{1}{2}\partial_{\mu}A_{\nu}\partial_{\mu}A_{\nu} - igc_{w}(\partial_{\nu}Z_{\mu}^{0}(W_{\mu}^{+}W_{\nu}^{-}$  $W_{\nu}^{+}W_{\mu}^{-}) - Z_{\nu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})) - Z_{\nu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-} - W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-}) + Z_{\mu}^{0}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-}) + Z_{\mu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-}) + Z_{\mu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-}) + Z_{\mu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-}) + Z_{\mu}^{0}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-}) + Z_{\mu}^{0}(W_{\mu}^{+}) + Z_{\mu}^{0}(W_{\mu$  $igs_{w}(\partial_{\nu}A_{\mu}^{\mu}(W_{\mu}^{+}W_{\nu}^{-}-W_{\nu}^{+}W_{\mu}^{-})-A_{\nu}(W_{\mu}^{+}\partial_{\nu}W_{\mu}^{-}-W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+})+A_{\mu}(W_{\nu}^{+}\partial_{\nu}W_{\mu}^{-}-W_{\mu}^{-}\partial_{\nu}W_{\mu}^{+})$  $W_{\nu}^{-}\partial_{\nu}W_{\mu}^{+})) - \frac{1}{2}g^{2}W_{\mu}^{+}W_{\nu}^{-}W_{\nu}^{+}W_{\nu}^{-} + \frac{1}{2}g^{2}W_{\mu}^{+}W_{\nu}^{-}W_{\mu}^{+}W_{\nu}^{-} + g^{2}c_{w}^{2}(Z_{\mu}^{0}W_{\mu}^{+}Z_{\nu}^{0}W_{\nu}^{-} - C_{\mu}^{0}W_{\mu}^{-}))$  $\beta_h \left( \frac{2M^2}{a^2} + \frac{2M}{a}H + \frac{1}{2}(H^2 + \phi^0\phi^0 + 2\phi^+\phi^-) \right) + \frac{2M^4}{a^2}\alpha_h - \frac{1}{2}(H^2 + \phi^0\phi^0 + 2\phi^+\phi^-)$  $g \alpha_h M (H^3 + H \phi^0 \phi^0 + 2H \phi^+ \phi^-) \frac{1}{8}g^2\alpha_h\left(H^4+(\phi^0)^4+4(\phi^+\phi^-)^2+4(\phi^0)^2\phi^+\phi^-+4H^2\phi^+\phi^-+2(\phi^0)^2H^2\right)$  $gMW^+_\mu W^-_\mu H - rac{1}{2}grac{M}{c_w^2}Z^0_\mu Z^0_\mu H$   $rac{1}{2} ig \left( W^+_\mu (\phi^0 \partial_\mu \phi^- - \phi^- \partial_\mu \phi^0) - W^-_\mu (\phi^0 \partial_\mu \phi^+ - \phi^+ \partial_\mu \phi^0) 
ight) +$  $\frac{1}{2}g\left(W^+_\mu(H\partial_\mu\phi^- - \phi^-\partial_\mu H) + W^-_\mu(H\partial_\mu\phi^+ - \phi^+\partial_\mu H)\right) + \frac{1}{2}g\frac{1}{c_w}(Z^0_\mu(H\partial_\mu\phi^0 - \phi^0\partial_\mu H) +$  $M\left(\frac{1}{c_{w}}Z_{\mu}^{0}\partial_{\mu}\phi^{0}+W_{\mu}^{+}\partial_{\mu}\phi^{-}+W_{\mu}^{-}\partial_{\mu}\phi^{+}\right)-ig\frac{s_{w}^{2}}{c_{w}}MZ_{\mu}^{0}(W_{\mu}^{+}\phi^{-}-W_{\mu}^{-}\phi^{+})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}MA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W_{\mu}^{+}\phi^{-})+igs_{w}WA_{\mu}(W$  $W^{-}_{\mu}\phi^{+}) - igrac{1-2c^{2}_{w}}{2c_{w}}Z^{0}_{\mu}(\phi^{+}\partial_{\mu}\phi^{-} - \phi^{-}\partial_{\mu}\phi^{+}) + igs_{w}A_{\mu}(\phi^{+}\partial_{\mu}\phi^{-} - \phi^{-}\partial_{\mu}\phi^{+}) \frac{1}{4}g^2W_{\mu}^{+}W_{\mu}^{-}\left(H^2+\tilde{(\phi^0)}^2+2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)-\frac{1}{8}g^2\frac{1}{c_w^2}Z_{\mu}^0Z_{\mu}^0\left(H^2+(\phi^0)^2+2(2s_w^2-1)^2\phi^+\phi^-\right)$  $\frac{1}{2}g^2 \frac{s_w^2}{c_w} Z^0_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) - \frac{1}{2}ig^2 \frac{s_w^2}{c_w} Z^0_\mu H(W^+_\mu \phi^- - W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^+) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^-) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^-) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^-) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^-) + \frac{1}{2}g^2 s_w A_\mu \phi^-) + \frac{1}{2}g^2 s_w A_\mu \phi^0(W^+_\mu \phi^- + W^-_\mu \phi^-) + \frac{1}{2}g^2 s_w A_\mu \phi^-) + \frac{1}{2}g^2 s_w A_\mu \phi^-) + \frac{1}{2}g^2 s_w A_\mu \phi^- + \frac{1}{2}g^2 s_w A_\mu \phi^-) + \frac{1}{2}g^2$  $\begin{array}{c} & 2g \ c_w \ \mathcal{L}_{\mu} \phi \ (\mathcal{V}_{\mu} \ \phi \ ) + \mathcal{V}_{\mu} \phi \ ) - 2g \ \mathcal{L}_{w} \mathcal{L}_{\mu} (\mathcal{V}_{\mu} \ \phi \ ) + 2g \ \mathcal{L}_{w} \mathcal{L}_{\mu} \phi \ (\mathcal{V}_{\mu} \ \phi \ ) + 2g \ \mathcal{L}_{w} \mathcal{L}_{\mu} \phi \ ) \\ & W_{\mu}^{-} \phi^{+} ) + \frac{1}{2} i g^{2} s_{w} \mathcal{A}_{\mu} \mathcal{H} (W_{\mu}^{+} \phi^{-} - W_{\mu}^{-} \phi^{+}) - g^{2} \frac{s_{w}}{c_{w}} (2c_{w}^{2} - 1) \mathcal{Z}_{\mu}^{0} \mathcal{A}_{\mu} \phi^{+} \phi^{-} - g^{2} s_{w}^{2} \mathcal{L}_{\mu} \mathcal{A}_{\mu} \phi^{+} \phi^{-} - \frac{1}{2} i g_{s} \lambda_{ij}^{a} (q_{i}^{a} \gamma^{\mu} q_{j}^{a}) g_{\mu}^{a} - \bar{e}^{\lambda} (\gamma \partial + m_{e}^{\lambda}) e^{\lambda} - \bar{\nu}^{\lambda} (\gamma \partial + m_{\nu}^{\lambda}) \nu^{\lambda} - \bar{u}_{i}^{\lambda} (\gamma \partial + m_{u}^{\lambda}) u_{j}^{\lambda} - \bar{d}_{j}^{\lambda} (\gamma \partial + m_{d}^{\lambda}) d_{j}^{\lambda} + i g s_{w} \mathcal{A}_{\mu} \left( -(\bar{e}^{\lambda} \gamma^{\mu} e^{\lambda}) + \frac{2}{3} (\bar{u}_{j}^{\lambda} \gamma^{\mu} u_{j}^{\lambda}) - \frac{1}{3} (\bar{d}_{j}^{\lambda} \gamma^{\mu} d_{j}^{\lambda}) \right) + \frac{i g}{4c_{w}} \mathcal{L}_{\mu}^{0} \left\{ (\bar{\nu}^{\lambda} \gamma^{\mu} (1 + \gamma^{5}) \nu^{\lambda}) + (\bar{e}^{\lambda} \gamma^{\mu} (4s_{w}^{2} - 1 - \gamma^{5}) e^{\lambda}) + (d_{j}^{\lambda} \gamma^{\mu} (\frac{4}{3} s_{w}^{2} - 1 - \gamma^{5}) d_{j}^{\lambda}) + \end{array} \right.$  $(\bar{u}_{j}^{\lambda}\gamma^{\mu}(1-\frac{8}{3}s_{w}^{2}+\gamma^{5})u_{j}^{\lambda})\}+\frac{ig}{2\sqrt{2}}W_{\mu}^{+}\left((\bar{\nu}^{\lambda}\gamma^{\mu}(1+\gamma^{5})U^{lep}_{\lambda\kappa}e^{\kappa})+(\bar{u}_{j}^{\lambda}\gamma^{\mu}(1+\gamma^{5})C_{\lambda\kappa}d_{j}^{\kappa})\right)+$  $\frac{ig}{2\sqrt{2}}W^{-}_{\mu}\left((\bar{e}^{\kappa}U^{lep}_{\kappa\lambda}\gamma^{\mu}(1+\gamma^{5})\nu^{\lambda})+(\bar{d}^{\kappa}_{j}C^{\dagger}_{\kappa\lambda}\gamma^{\mu}(1+\gamma^{5})u^{\lambda}_{j})\right)+$  $\frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{e}^{\kappa}(\bar{\nu}^{\lambda}U^{lep}{}_{\lambda\kappa}(1-\gamma^{5})e^{\kappa})+m_{\nu}^{\lambda}(\bar{\nu}^{\lambda}U^{lep}{}_{\lambda\kappa}(1+\gamma^{5})e^{\kappa}\right)+$  $\frac{ig}{2M\sqrt{2}}\phi^{-}\left(m_{e}^{\lambda}(\bar{e}^{\lambda}U^{lep}_{\ \lambda\kappa}^{\dagger}(1+\gamma^{5})\nu^{\kappa})-m_{\nu}^{\kappa}(\bar{e}^{\lambda}U^{lep}_{\ \lambda\kappa}^{\dagger}(1-\gamma^{5})\nu^{\kappa}\right)-\frac{g}{2}\frac{m_{\nu}^{\lambda}}{M}H(\bar{\nu}^{\lambda}\nu^{\lambda}) \frac{g}{2}\frac{m_{e}^{\lambda}}{M}H(\bar{e}^{\lambda}e^{\lambda}) + \frac{ig}{2}\frac{m_{\nu}^{\lambda}}{M}\phi^{0}(\bar{\nu}^{\lambda}\gamma^{5}\nu^{\lambda}) - \frac{ig}{2}\frac{m_{e}^{\lambda}}{M}\phi^{0}(\bar{e}^{\lambda}\gamma^{5}e^{\lambda}) - \frac{1}{4}\bar{\nu}_{\lambda}M_{\lambda\kappa}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa} \frac{1}{4}\overline{\bar{\nu}_{\lambda}}\frac{M_{\lambda\kappa}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}}{M_{\lambda\kappa}^{R}(1-\gamma_{5})\hat{\nu}_{\kappa}} + \frac{ig}{2M\sqrt{2}}\phi^{+}\left(-m_{d}^{\kappa}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1-\gamma^{5})d_{j}^{\kappa}) + m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^{\kappa}) + m_{u}^{\lambda}(\bar{u}_{j}^{\lambda}C_{\lambda\kappa}(1+\gamma^{5})d_{j}^$  $\frac{ig}{2M\sqrt{2}}\phi^{-}\left(m_{d}^{\lambda}(\bar{d}_{j}^{\lambda}C_{\lambda\kappa}^{\dagger}(1+\gamma^{5})u_{j}^{\kappa})-m_{u}^{\kappa}(\bar{d}_{j}^{\lambda}C_{\lambda\kappa}^{\dagger}(1-\gamma^{5})u_{j}^{\kappa})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{j}^{\lambda})-\frac{g}{2}\frac{m_{u}^{\lambda}}{M}H(\bar{u}_{j}^{\lambda}u_{\lambda$  $\frac{g}{2}\frac{m_{d}^{\lambda}}{M}H(\bar{d}_{j}^{\lambda}d_{j}^{\lambda}) + \frac{ig}{2}\frac{m_{u}^{\lambda}}{M}\phi^{0}(\bar{u}_{j}^{\lambda}\gamma^{5}u_{j}^{\lambda}) - \frac{ig}{2}\frac{m_{d}^{\lambda}}{M}\phi^{0}(\bar{d}_{j}^{\lambda}\gamma^{5}d_{j}^{\lambda}) + \bar{G}^{a}\partial^{2}G^{a} + g_{s}f^{abc}\partial_{\mu}\bar{G}^{a}G^{b}g_{\mu}^{c} + \bar{X}^{+}(\partial^{2}-M^{2})X^{+} + \bar{X}^{-}(\partial^{2}-M^{2})X^{-} + \bar{X}^{0}(\partial^{2}-\frac{M^{2}}{c_{v}^{2}})X^{0} + \bar{Y}\partial^{2}Y + igc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-} - \bar{X}^{0})X^{-} + \bar{X}^{0}(\partial^{2}-M^{2})X^{-} + \bar{X}^{0}(\partial^{2}-M^{2})X^{-} + \bar{X}^{0}(\partial^{2}-M^{2})X^{0} + \bar{Y}\partial^{2}Y + igc_{w}W^{+}_{\mu}(\partial_{\mu}\bar{X}^{0}X^{-} - \bar{X}^{0})X^{0} + \bar{X}^{0}(\partial^{2}-M^{2})X^{0} + \bar{X}^{0}(\partial^$  $\begin{array}{l} \partial_{\mu}\bar{X}^{+}X^{0}) + igs_{w}W_{\mu}^{+}(\partial_{\mu}\bar{Y}X^{-} - \partial_{\mu}\bar{X}^{+}\bar{Y}) + igc_{w}W_{\mu}^{-}(\partial_{\mu}\bar{X}^{-}X^{0} - \partial_{\mu}\bar{X}^{0}X^{+}) + igs_{w}W_{\underline{\mu}}^{-}(\partial_{\mu}\bar{X}^{-}Y - \partial_{\mu}\bar{Y}X^{+}) + igc_{w}Z_{\mu}^{0}(\partial_{\mu}\bar{X}^{+}X^{+} - \partial_{\mu}\bar{Y}X^{+}) + igc_{w}Z_{\mu}^{0}(\partial_{\mu}\bar{X}^{-}X^{0} - \partial_{\mu}\bar{Y}X^{+}) + igc_{w}Z_{\mu}^{0}(\partial_{\mu}\bar{X}^{-}X^{-}) + igc_{w}Z_{\mu}^{0}(\partial_{\mu}\bar{X}^{-}X^{0} - \partial_{\mu}\bar{Y}X^{+}) + igc_{w}Z_{\mu}^{0}(\partial_{\mu}\bar{X}^{-}X^{-}) + i$  $\partial_\mu ar X^- X^-) {+} igs_w A_\mu (\partial_\mu ar X^+ X^+ \partial_{\mu}\bar{X}^{-}X^{-}) - \frac{1}{2}gM\left(\bar{X}^{+}X^{+}H + \bar{X}^{-}X^{-}H + \frac{1}{c_{w}^{2}}\bar{X}^{0}\bar{X}^{0}H\right) + \frac{1-2c_{w}^{2}}{2c_{w}}igM\left(\bar{X}^{+}X^{0}\phi^{+} - \bar{X}^{-}X^{0}\phi^{-}\right) + \frac{1}{2}gM\left(\bar{X}^{+}H + \bar{X}^{-}\bar{X}^{-}H + \frac{1}{c_{w}^{2}}\bar{X}^{0}\bar{X}^{0}H\right) + \frac{1-2c_{w}^{2}}{2c_{w}}igM\left(\bar{X}^{+}\bar{X}^{0}\phi^{+} - \bar{X}^{-}\bar{X}^{0}\phi^{-}\right) + \frac{1}{2}gM\left(\bar{X}^{+}\bar{X}^{0}\bar{X}^{0}\bar{X}^{0}H + \bar{X}^{-}\bar{X}^{0}\bar{X}^{0}\bar{X}^{0}H\right) + \frac{1}{2}gM\left(\bar{X}^{+}\bar{X}^{0}\bar{X}^{0}\bar{X}^{0}\bar{X}^{0}H\right) + \frac{1}{2}gM\left(\bar{X}^{+}\bar{X}^{0}\bar{X}^$  $\sum_{w} \sum_{w} \sum_{w$ 

 $\frac{1}{2}igM\left(\bar{X}^{+}X^{+}\phi^{0}-\bar{X}^{-}X^{-}\phi^{0}
ight)$ 

 $+\alpha_{\rm S}^2 \, {\rm d}\sigma_{\rm NNLO} + \alpha_{\rm EW}^2 \, {\rm d}\sigma_{\rm NNLO\,EW} + \alpha_{\rm S}\alpha_{\rm EW} \, {\rm d}\sigma_{\rm NNLO\,QCDxEW}$ 



- $d\Phi_{n(+1)}$ n, n+1, n+2 particle phase space
  - virtual one-loop matrix element
  - real tree-level matrix element
- $M_{\rm NNLO,V}$  double-virtual two-loop matrix element
  - $M_{\rm NNLO,RV}$  real-virtual one-loop matrix element
- $\mathcal{M}_{\text{NNLO,RR}}$ double-real tree-level matrix element





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Decomposition	in ter	ms of sj
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 ${}^{\mathrm{p}} k_{1}^{\mu_{2}} = \frac{\sqrt{q^{2}}}{2}$ 

$\mathrm{d}\sigma^{\mathrm{unp}}$	_ 3	$\mathrm{d}\sigma$
$d^4q$	$-\frac{16\pi}{16\pi}$	$\overline{\mathrm{d}^4 q  \mathrm{d} \cos \theta  \mathrm{d} \phi}$
$\sin(2t)$	$+A_{1}$	
$\sin  heta$	$+A_{3}$	
$\sin(2\theta$	$+A_{6}$	

dominant angular coefficients:  $A_{0,...,4}$ 

### V+jets

•very important standard-candle (very clean and large x-sections) • crucial background in many BSM searches •allows for Mw and  $sin^2\theta^{eff}$  measurements

lepton plane Sematics in the  ${
m Z}/\gamma^{*}$  (lepton-pair) rest frame:  $(1, \pm \sin\theta\cos\phi, \pm \sin\theta\sin\phi, \pm \cos\theta)^{\mathrm{T}}$ pherical harmonics:  $Y_{lm}(\theta, \phi)$ , l = 0, 1, 2 $\frac{1}{2} = \left\{ (1 + \cos^2 \theta) + \frac{1}{2} A_0 (1 - 3\cos^2 \theta) \right\}$  $(\theta)\cos\phi + \frac{1}{2} A_2 \sin^2\theta \cos(2\phi)$  $\cos \phi + A_4 \ \cos \theta + A_5 \ \sin^2 \theta \ \sin(2\phi)$  $(\theta) \sin \phi + A_7 \sin \theta \sin \phi \Big\},$  $\rightsquigarrow$  probed by  $\gamma^*$  & Z exchange parity even:  $A_{0,1,2}$  $\rightsquigarrow$  sensitive to  $\sin^2 \theta_{\rm w}$ ,  $A_4 \leftrightarrow A_{\rm FB}$ parity odd:  $A_{3,4}$ 







[Gauld, Gehrmann-De Ridder, Gehrmann, Glover, Huss, 1708.00008]



#### V+jets

 $\checkmark @ \mathcal{O}(\alpha_{s}^{0}) \quad \text{spin-}\frac{1}{2} \text{ nature of quarks } \leftrightarrow \text{ Callan-Gross } (F_{2} = 2xF_{1})$  $\checkmark @ \mathcal{O}(\alpha_{s}^{1}) \quad \text{vector coupling of spin-1 gluon}$ 

 $\checkmark \otimes \mathcal{O}(\alpha_s^2) \longrightarrow \mathsf{DY} \otimes \mathsf{NNLO}$  only **LO** prediction in  $(A_0 - A_2)!$ 

→V+jet @ NNLO yields  $\mathcal{O}(\alpha_S^3)$ , i.e. (A<sub>0</sub>-A<sub>2</sub>) at NLO





Dominant uncertainty = Scale variation +/- 10%



 $\overline{Q}$ 



- QCD always dominant  $\bullet$
- $\bullet$
- Proper treatment of FSR corrections important lacksquare

EW and QCD-EW contributions typically (1-10)%



#### HF hadroproduction: ratio [Gauld, Haisch, Pecjak, 1901.0757]



#### Continuum

- Mass effects (mb = 4.75 GeV, mc = 1.5 GeV)
- QED effects (Qc=2/3, Qb=1/3)

#### Z-boson Resonance

• Weak effects (Zbb vs Zcc couplings)



# HF hadroproduction: asymmetry

[Gauld, Haisch, Pecjak, 1901.0757]





$$-1 \left( \frac{\mathrm{d}\sigma_A}{\mathrm{d}m_{Q\bar{Q}}} \bigg|_{\Delta y > 0} - \frac{\mathrm{d}\sigma_A}{\mathrm{d}m_{Q\bar{Q}}} \bigg|_{\Delta y < 0} \right)$$

 $\Delta y = y_Q - y_{\bar{Q}}$ 





#### HF hadroproduction: asymmetry [Gauld, Haisch, Pecjak, 1901.0757]



Sensitivity on Zbb and Zcc couplings! →Could this even compete with  $A^{b}_{FB, LEP}$  (long-lasting 3 $\sigma$  deviation)? →Percent level precision required.... →This requires NNLO QCD and good control of exp. systematics. →Feasible!





# Top quark production in the forward region



[HL/HE Report	'19]
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Final state	$300 \text{ fb}^{-1}$	$\langle x \rangle$
$\ell b$	830k	0.295
$\ell b \overline{b}$	130k	0.368
$\mu eb$	12k	0.348
$\mu ebar{b}$	1.5k	0.415

➡ measurements at sub-percent level feasible

➡ measurements at percent level feasible

#### Significant constraints on gluon PDF in forward region possible

• Only partial reconstruction of decay products possible

• Complementary information to ATLAS and CMS









■Sufficient sensitivity for non-zero charge asymmetry at HL-LHC







- direct access to quartic EW gauge couplings
- •VBS: longitudinal gauge bosons at high energies
- •window to electroweak symmetry breaking via off-shell Higgs exchange











 $d\sigma = d\sigma(\alpha_S^2 \alpha^4) + d\sigma(\alpha_S \alpha^5) + d\sigma(\alpha^6) + \dots$ LO

QCD-background interference



**VBS-signal** 





QCD-background interference



#### $d\sigma = d\sigma(\alpha_S^2 \alpha^4) + d\sigma(\alpha_S \alpha^5) + d\sigma(\alpha^6) + \dots$ L()

**VBS-signal** 

 $\cdots + d\sigma(\alpha_S^3 \alpha^4) + d\sigma(\alpha_S^2 \alpha^5) + d\sigma(\alpha_S \alpha^6) + \sigma(\alpha^7)$ NLO









![](_page_25_Picture_6.jpeg)

![](_page_26_Figure_1.jpeg)

➡separation meaningless at NLO

![](_page_26_Picture_4.jpeg)

![](_page_26_Picture_7.jpeg)

Signature:  $\ell^+ \ell^+ j$ 

pp 
$$\rightarrow \mu^+ \nu_\mu \mu^+ \nu_\mu jj$$
 (ss WW),  
pp  $\rightarrow \mu^+ \nu_\mu \mu^+ \mu^- jj$  (WZ),  
pp  $\rightarrow \mu^+ \mu^- \mu^+ \mu^- jj$  (ZZ),

Channel	$\sigma_{\rm EW}$ [fb]	$\sigma_{ m QCD}$
ss WW	0.0185(1)	0.010
WZ	0.0071(1)	0.295
ZZ	0.0003(1)	0.016
Sum	0.0258(1)	0.321

![](_page_27_Figure_4.jpeg)

![](_page_27_Figure_5.jpeg)

![](_page_27_Figure_6.jpeg)

 $\mathcal{Y}_{\mu_1^+}$ 

3.5

4.5

4

![](_page_27_Picture_8.jpeg)

### Conclusions

- SM is in excellent shape
- Important complementarity in phase-space accessible by LHCb
- (N)NLO QCD + NLO EW is the new standard:V+jets, tt, HF,VBS
- Explore the unknown

New theoretical, mathematical, and computational concepts

Possible technical developments towards HL/HE-LHC • NNLO QCD + PS

- NNLO QCD for  $2 \rightarrow 3(4)$
- NNLO QCDxEVV & NNLO EVV

precision for HL-LHC

• High-precision (Theo + Exp) allows to push limits to unprecedented levels (LHC completes LEP)

• PS matching and multi-jet merging @ NLO QCD+EW

• N3LO QCD for  $2 \rightarrow 2$ 

![](_page_28_Picture_17.jpeg)

![](_page_28_Picture_18.jpeg)

![](_page_28_Picture_19.jpeg)

# Backup

![](_page_29_Picture_2.jpeg)

# Relevance of EW higher-order corrections I

Numerically  $\mathcal{O}(\alpha) \sim \mathcal{O}(\alpha_s^2) \Rightarrow | \text{NLO EW} \sim \text{NNLO QCD}$ 

![](_page_30_Figure_3.jpeg)

 $\rightarrow$  overall large effect in the tails of distributions:  $p_T$ ,  $m_{inv}$ ,  $H_T$ ,... (relevant for BSM searches!)

#### I. Possible large (negative) enhancement due to soft/collinear logs from virtual EW gauge bosons:

[Ciafaloni, Comelli,'98; Lipatov, Fadin, Martin, Melles, '99; Kuehen, Penin, Smirnov, '99; Denner, Pozzorini, '00]

![](_page_30_Picture_8.jpeg)

$$_{+\text{NLL}}^{\text{loop}} = \frac{\alpha}{4\pi} \sum_{k=1}^{n} \left\{ \frac{1}{2} \sum_{l \neq k} \sum_{a=\gamma, Z, W^{\pm}} I^{a}(k) I^{\bar{a}}(l) \ln^{2} \frac{\hat{s}_{kl}}{M^{2}} + \gamma^{\text{ew}}(k) \ln \frac{\hat{s}}{M^{2}} \right\}$$

![](_page_30_Picture_11.jpeg)

2. Possible large enhancement due to soft/collinear logs from photon radiation  $\sim \alpha \log \left(\frac{m_f^2}{Q^2}\right)$ in sufficiently exclusive observables.

![](_page_31_Figure_2.jpeg)

 $\rightarrow$  important for various precision observables, e.g. for determination of M<sub>W</sub> in DY

![](_page_31_Figure_4.jpeg)

![](_page_31_Figure_5.jpeg)

![](_page_31_Picture_6.jpeg)