

# CHANGES IN NEUTRINO OSCILLATIONS DUE TO POSSIBLE NON-STANDARD INTERACTIONS WITH MATTER

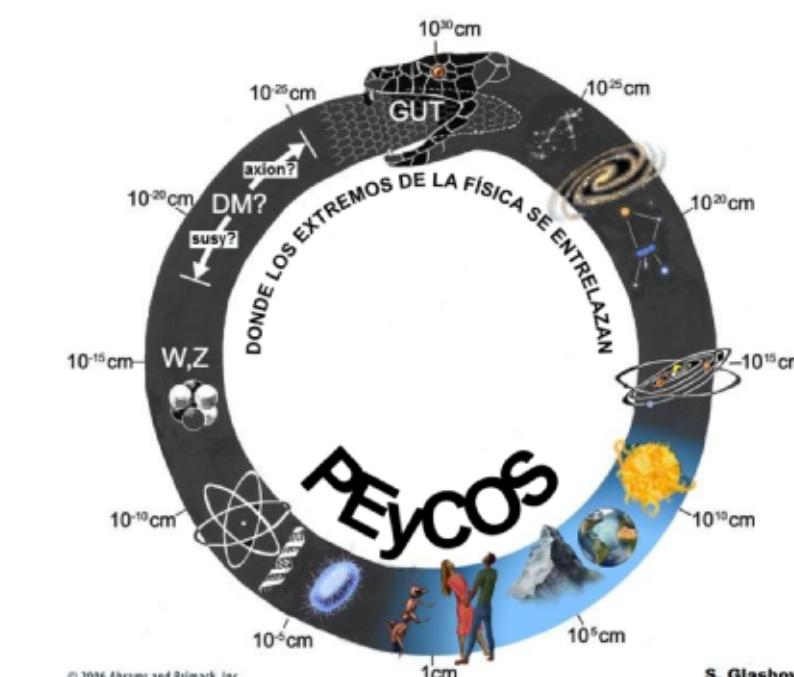
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Faculty of Basic Sciences  
Physics Program  
2020



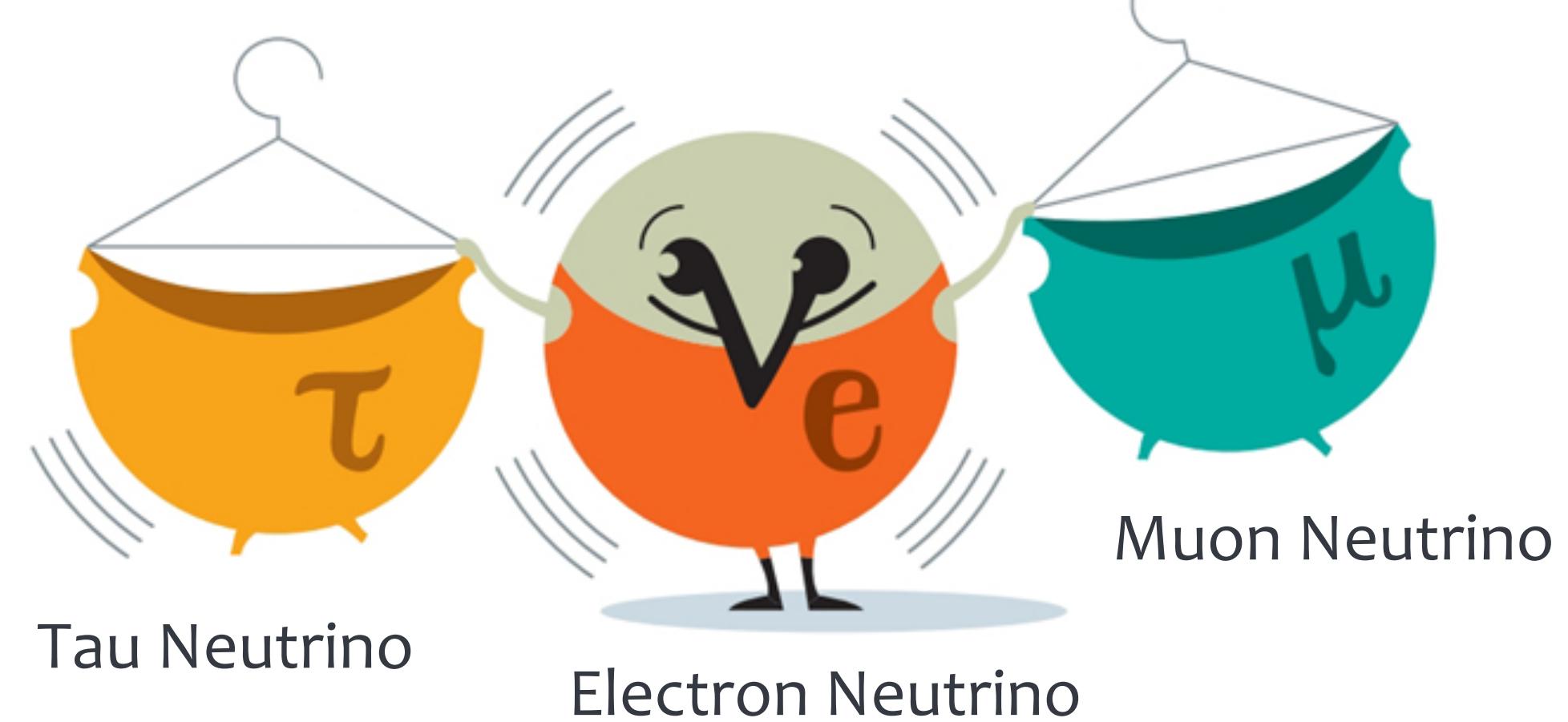
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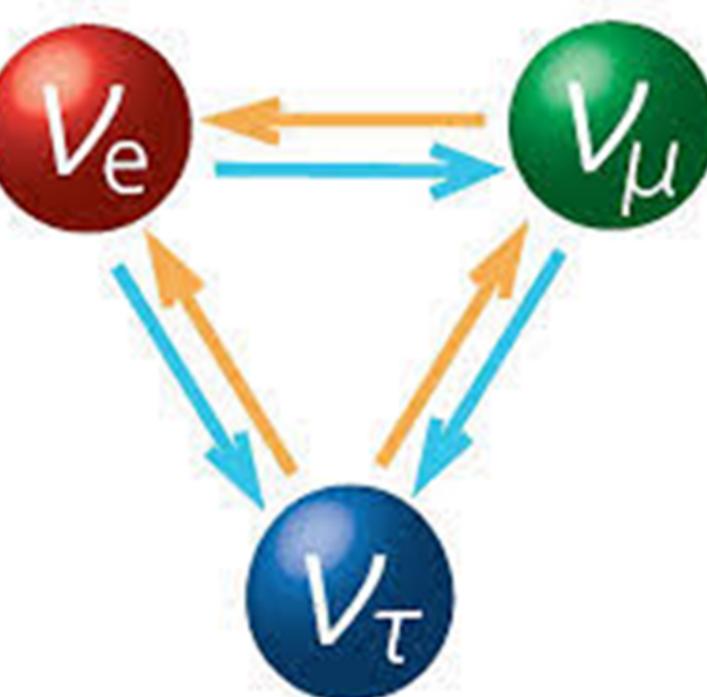


$$\nu_e = m_1 \nu_1 + m_2 \nu_2 + m_3 \nu_3$$

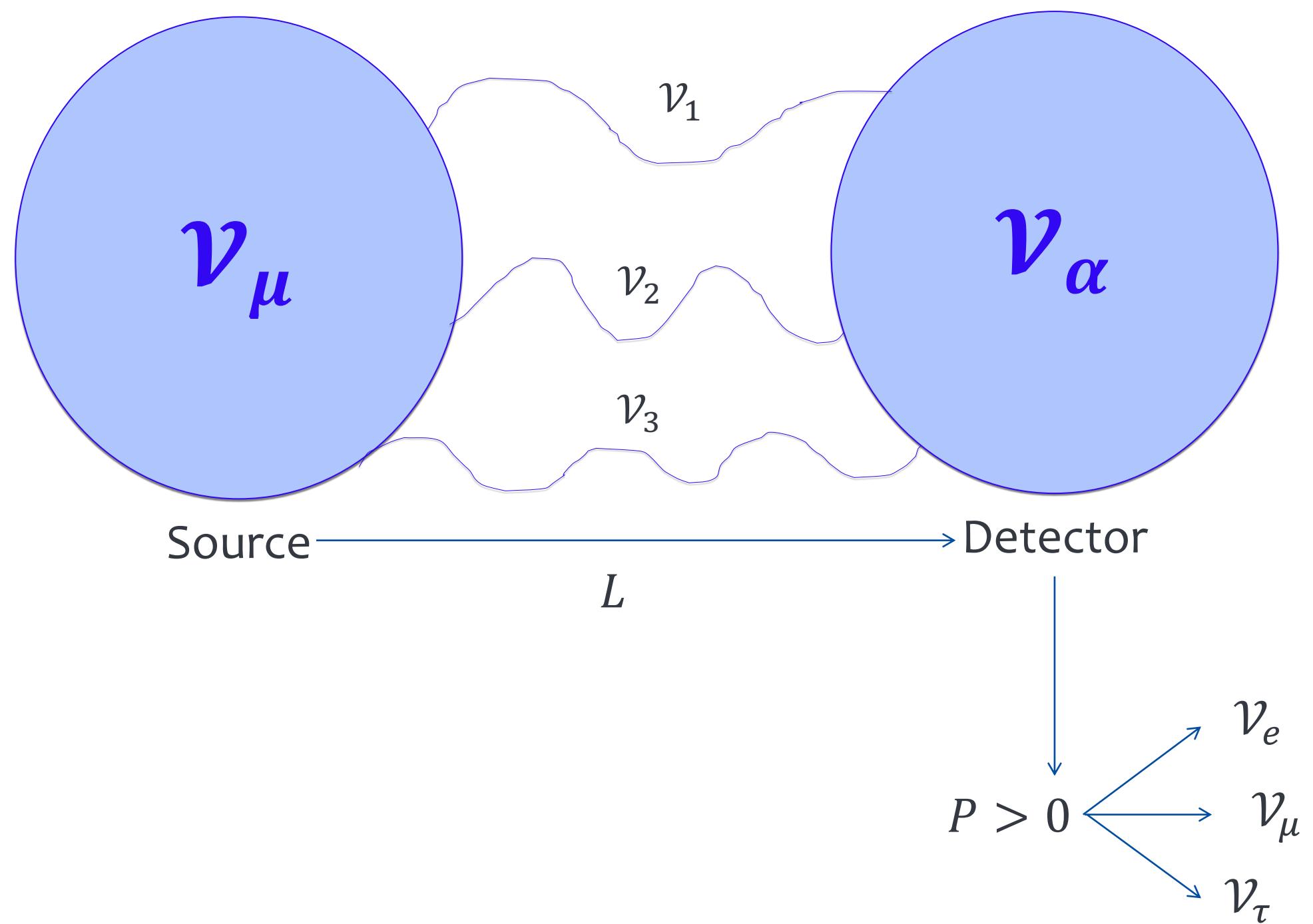
$$\nu_\mu = \nu_1 + \nu_2 + \nu_3$$

$$\nu_\tau = \nu_1 + \nu_2 + \nu_3$$

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & C_{23} & S_{23} \\ 0 & -S_{23} & C_{23} \end{pmatrix} \begin{pmatrix} C_{13} & 0 & S_{13} e^{i\delta_{cp}} \\ 0 & 1 & 0 \\ -S_{13} e^{i\delta_{cp}} & 0 & C_{13} \end{pmatrix} \begin{pmatrix} C_{12} & S_{12} & 0 \\ -S_{13} & C_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$



# Phenomenon of Oscillation



The flavor states  $|\nu_\alpha\rangle$  and the mass states  $|\nu_k\rangle$  are related:

$$|\nu_\alpha(t = 0)\rangle = \sum_k U_{\alpha k}^* |\nu_k\rangle$$

- $\alpha = e, \mu, \tau$
- $k = 1, 2, 3$

$$|\nu_\mu\rangle = U_{\mu 1}^* |\nu_1\rangle + U_{\mu 2}^* |\nu_2\rangle + U_{\mu 3}^* |\nu_3\rangle$$

$$t > 0$$

$$|\nu_\mu(t)\rangle = U_{\mu 1}^* e^{-iE_1 t} |\nu_1\rangle + U_{\mu 2}^* e^{-iE_2 t} |\nu_2\rangle + U_{\mu 3}^* e^{-iE_3 t} |\nu_3\rangle$$

- $U_{\alpha k}$  represents the lepton mixing matrix

$$P_{\nu_\alpha \rightarrow \nu_\beta}(E, L) = \sum_{kj} U_{\alpha k}^* U_{\alpha k} U_{\alpha k} U_{\beta j}^* e^{-i \left( \frac{\Delta m_{kj}^2 L}{2E} \right)}$$

$\Delta m_{kj}^2 \equiv m_k^2 - m_j^2$

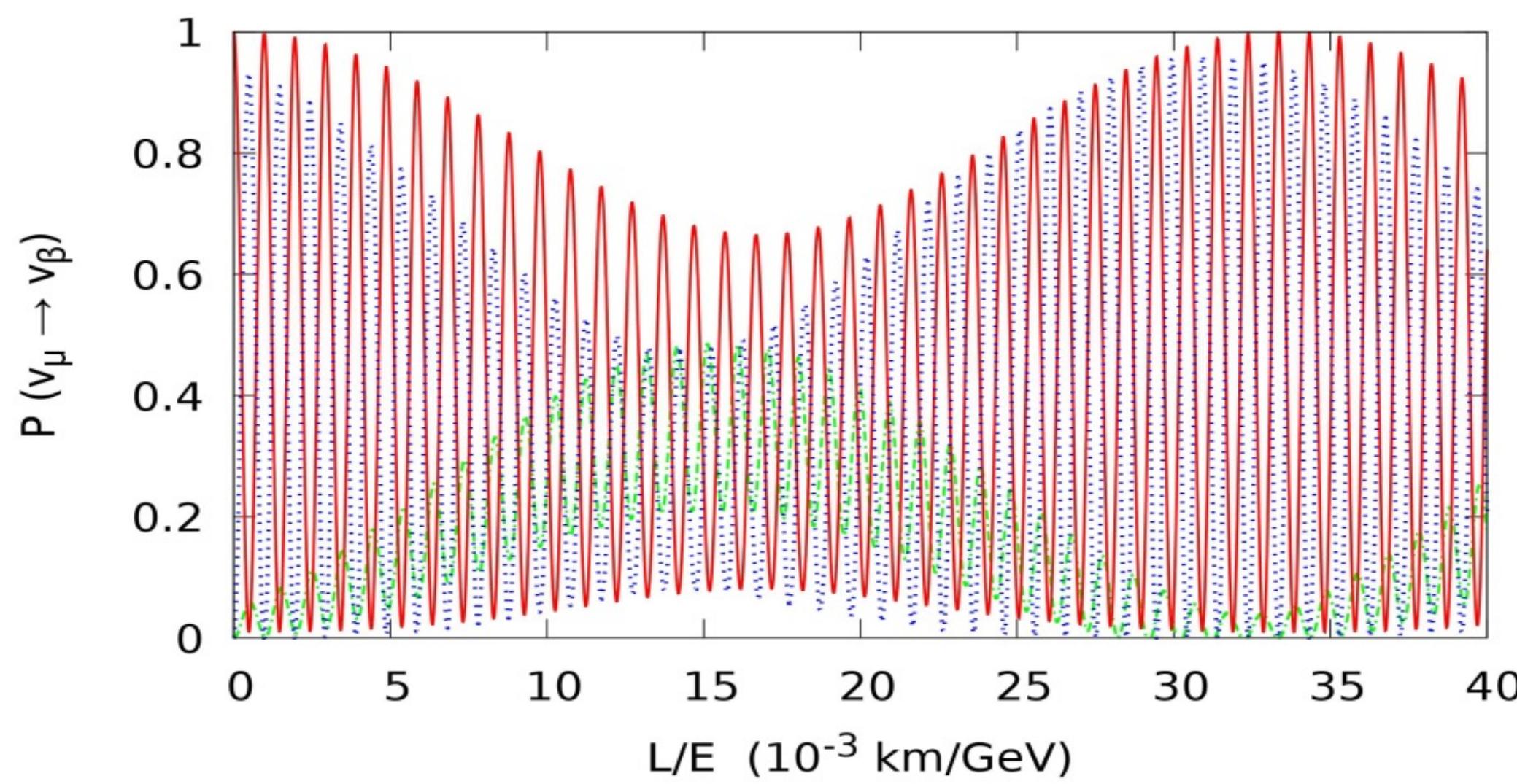
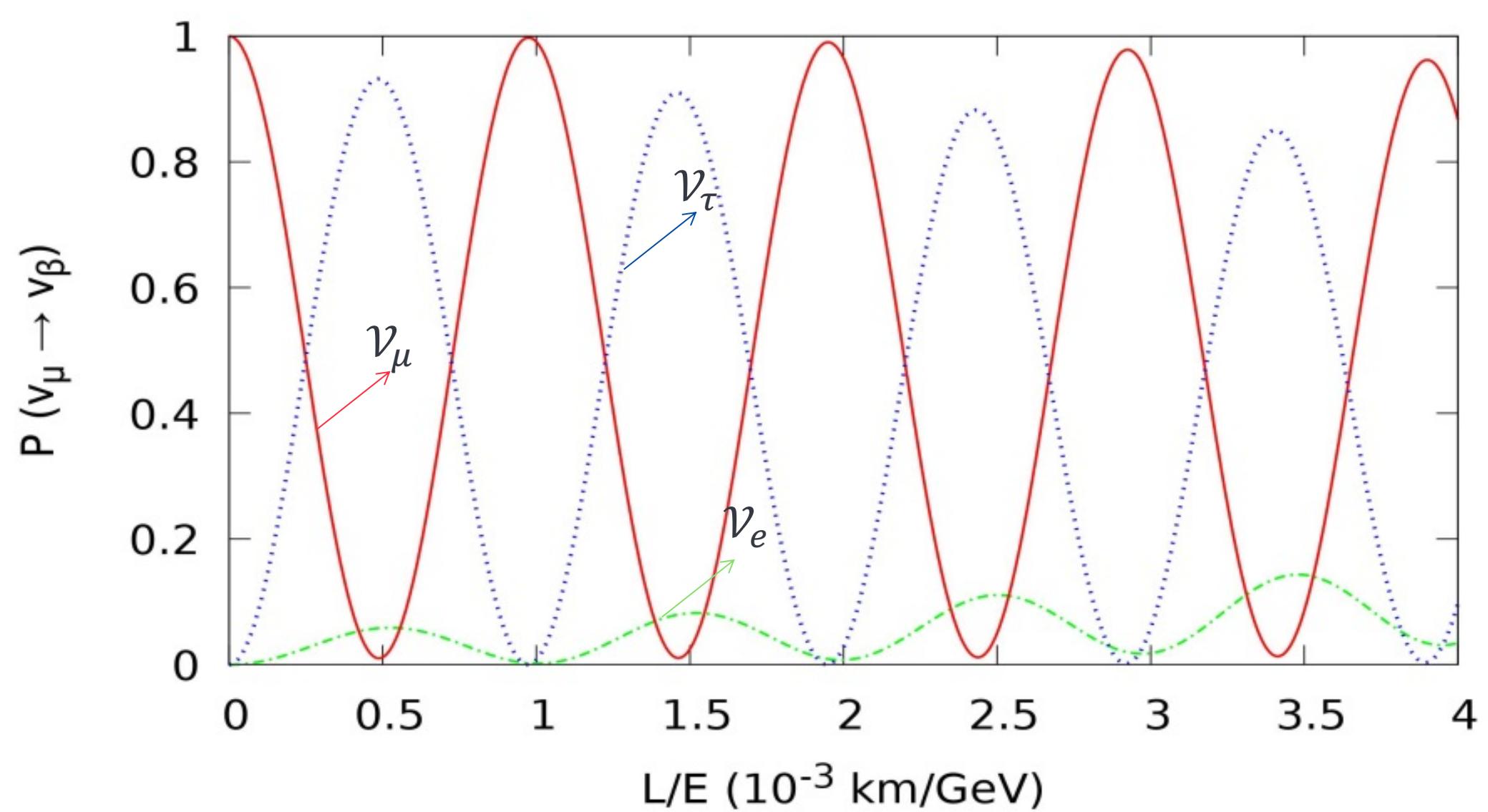
### Transition probability

$$P_{\nu_\alpha \rightarrow \nu_\beta} = \delta_{\alpha\beta} - 4 \sum_{k>j} \Re(U_{\alpha k}^* U_{\alpha k} U_{\alpha k} U_{\beta j}^*) \sin^2 \left( \frac{\Delta m_{kj}^2 L}{4E} \right) + 2 \sum_{k>j} \Im(U_{\alpha k}^* U_{\alpha k} U_{\alpha k} U_{\beta j}^*) \sin \left( \frac{\Delta m_{kj}^2 L}{2E} \right)$$

### Disappearance Probability

$$P_{\nu_\alpha \rightarrow \nu_\alpha} = 1 - 4 \sum_{k>j} |U_{\alpha k}|^2 |U_{\alpha k}|^2 \sin^2 \left( \frac{\Delta m_{kj}^2 L}{4E} \right)$$

Parámetro	Valores $\pm 1\sigma$	$3\sigma$
$\theta_{12}$ ( $^\circ$ )	$33.82^{+0.78}_{-0.76}$	$31.61 \rightarrow 36.27$
$\theta_{23}$ ( $^\circ$ )	$48.6^{+1.0}_{-1.4}$	$41.1 \rightarrow 51.3$
$\theta_{13}$ ( $^\circ$ )	$8.6^{+0.13}_{-0.13}$	$8.22 \rightarrow 8.98$
$\delta_{cp}$ ( $^\circ$ )	$221^{+39}_{-28}$	$144 \rightarrow 357$
$\frac{\Delta m_{21}^2}{10^{-5} \text{eV}^2}$	$7.39^{+0.21}_{-0.20}$	$6.79 \rightarrow 8.01$
$\frac{\Delta m_{31}^2}{10^{-3} \text{eV}^2}$	$2.528^{+0.029}_{-0.031}$	$2.436 \rightarrow 2.618$



# Oscillation probability in matter

When neutrinos travel through a dense medium, they experience a forward scattering of the particles that they encounter along the way

In a material medium:

$$H = H_0 + H_1$$

$$H_1 |\mathcal{V}_\alpha \rangle = V_\alpha |\mathcal{V}_\alpha \rangle$$



It is an effective potential due to  
coherent interactions in the medium

$H_E$  is the effective Hamiltonian in matrix form

$$H_E = \frac{1}{2E} (U \mathbb{M}^2 U^\dagger + \mathbb{A})$$

$$\mathbb{M}^2 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 \\ 0 & 0 & \Delta m_{31}^2 \end{pmatrix}$$

$$\mathbb{A} = \begin{pmatrix} A & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$A = 2EV_{CC} = 2\sqrt{2}EG_F N_e$$

## Two – Neutrinos Mixing

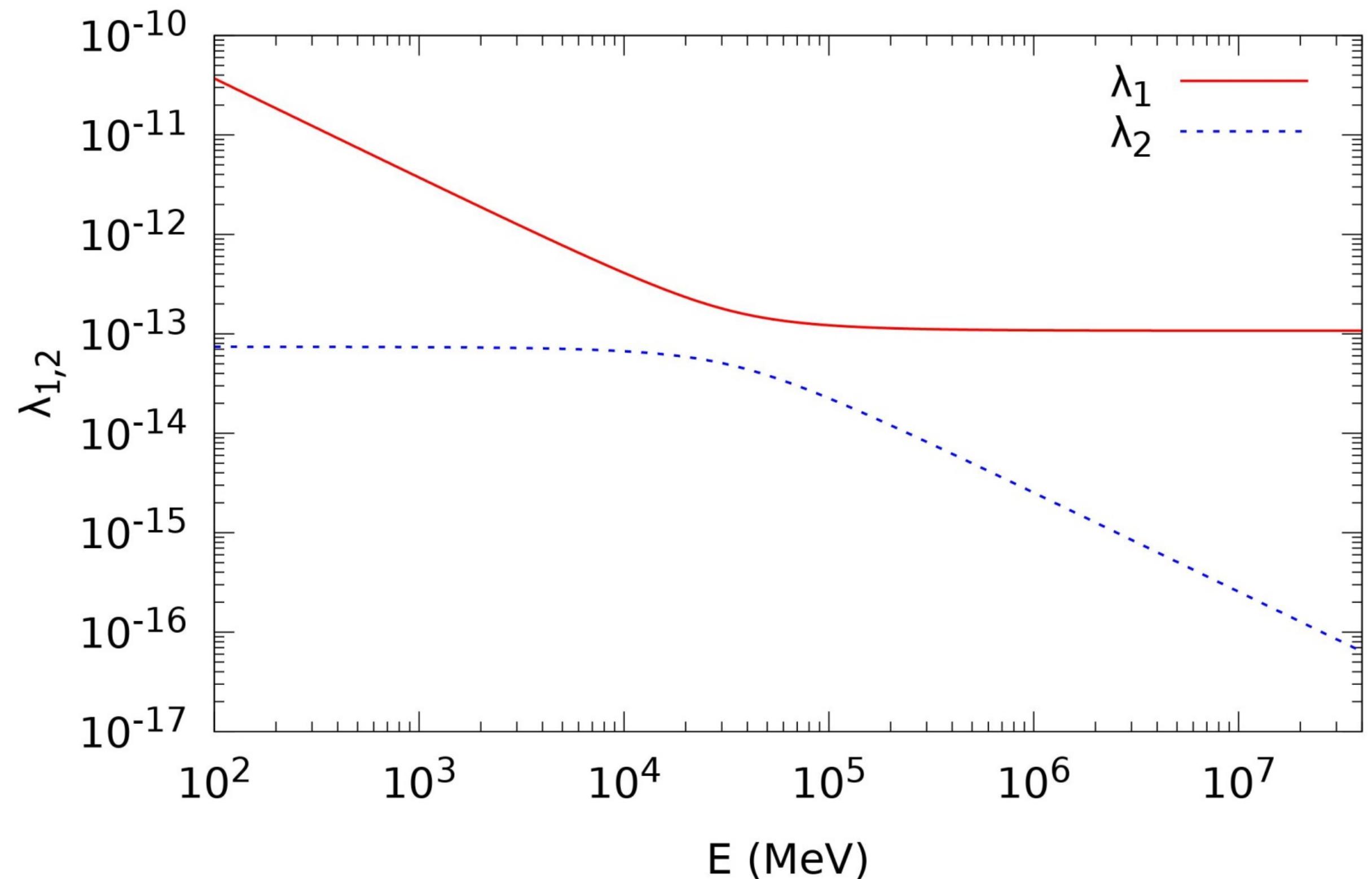
The two-neutrino effective mixing matrix

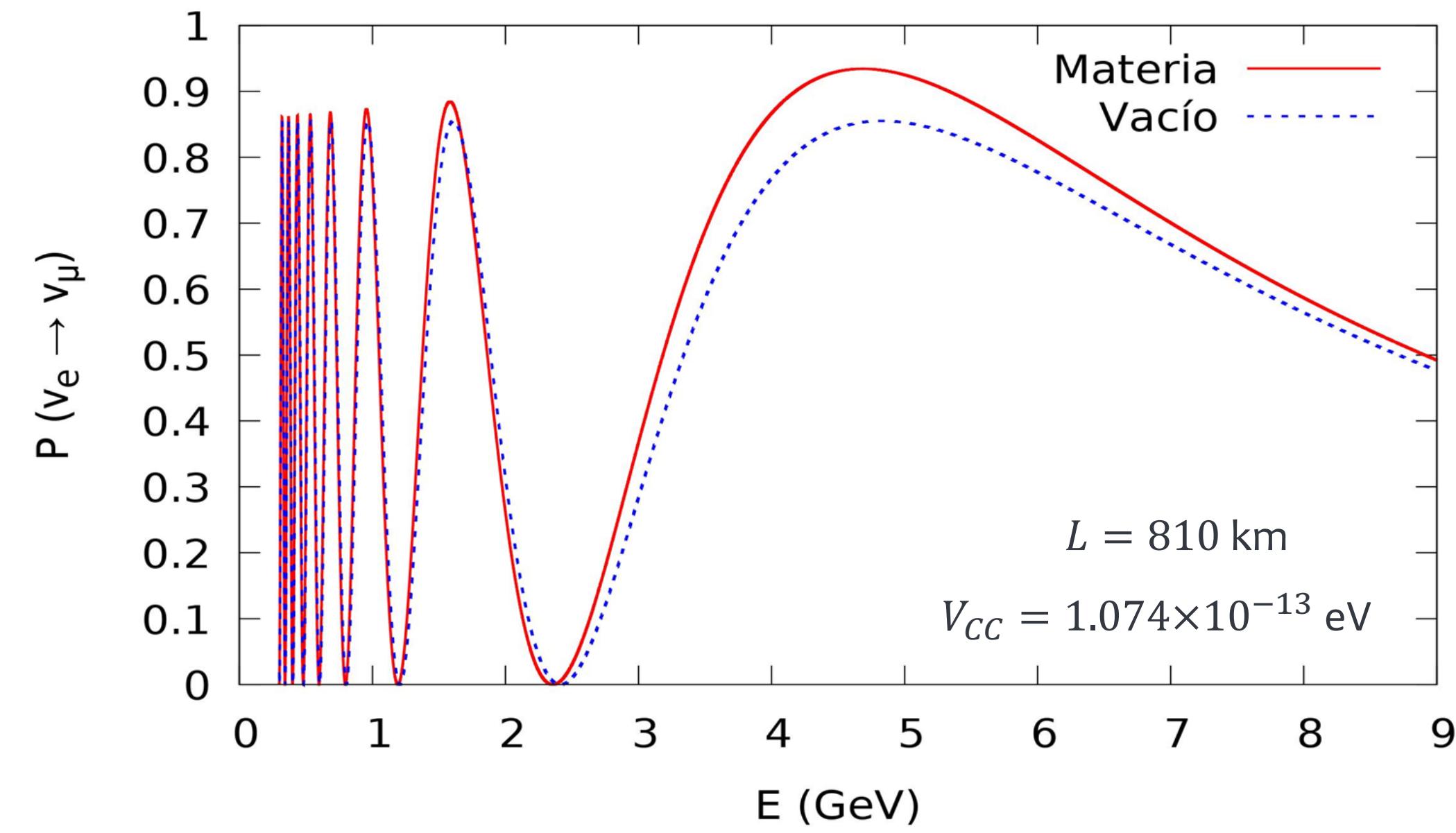
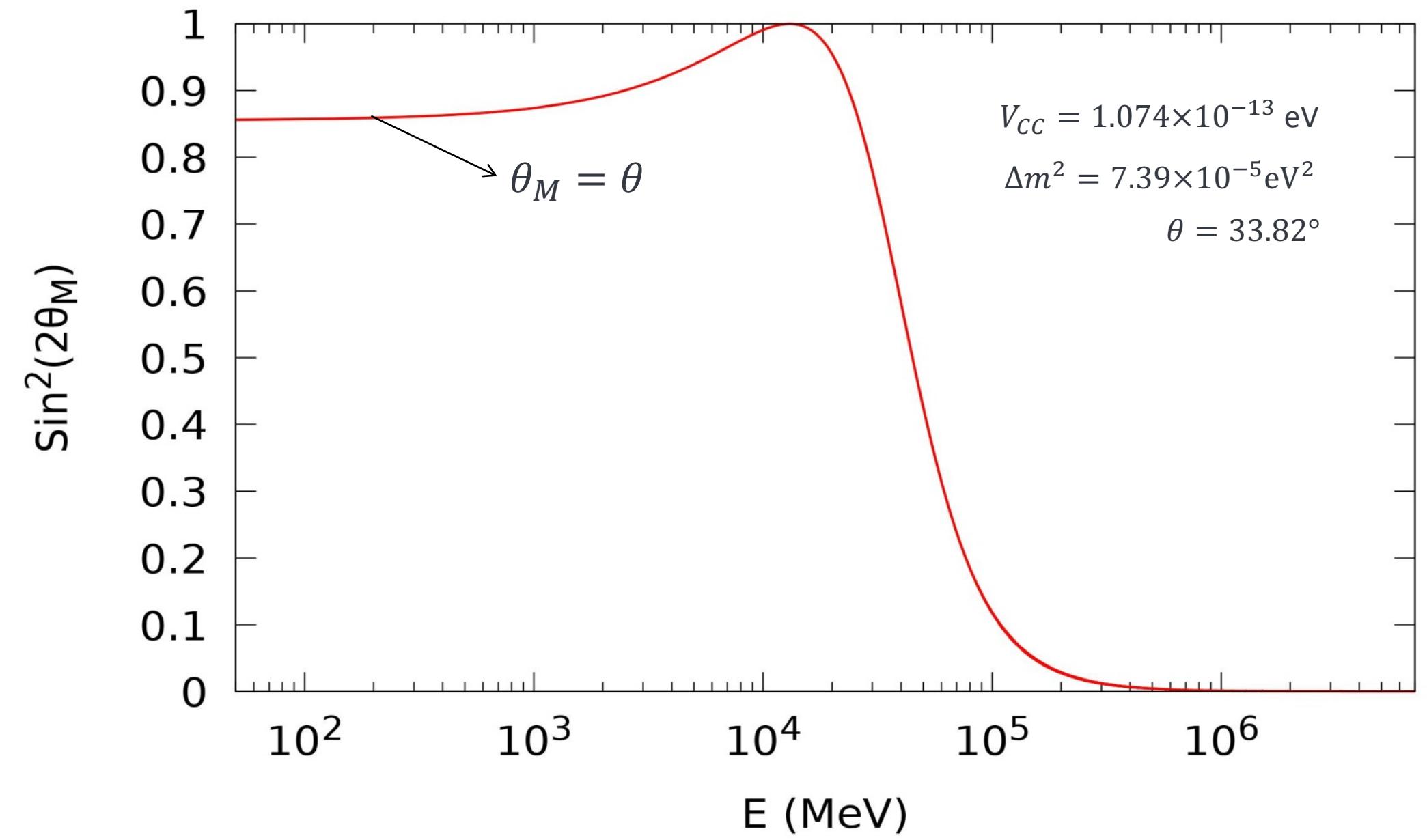
$$U = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix}$$

Making the matrixial producto we can get

$$H_E = \frac{1}{2E} \begin{pmatrix} A + \Delta m^2 \sin \theta^2 & \Delta m^2 \sin(2\theta) \\ \Delta m^2 \sin(2\theta) & A - \Delta m^2 \cos \theta^2 \end{pmatrix},$$

$$\lambda_{1,2} = \frac{\Delta m^2 + A}{4E} \pm \frac{\sqrt{(\Delta m^2 \sin 2\theta)^2 + (\Delta m^2 \cos 2\theta - A)^2}}{4E}$$





$$\sin 2\theta_M = \frac{\sin 2\theta}{\sqrt{(\sin 2\theta)^2 + \left(\cos 2\theta - \frac{A}{\Delta m^2}\right)^2}} \rightarrow \Delta m_M^2$$

$$A = 2EV_{CC} = 2\sqrt{2}EG_F N_e$$

$E \ll ,$	$\sin^2 2\theta_M \longrightarrow \sin^2 2\theta$
$E \gg ,$	$\sin^2 2\theta_M \longrightarrow 0$

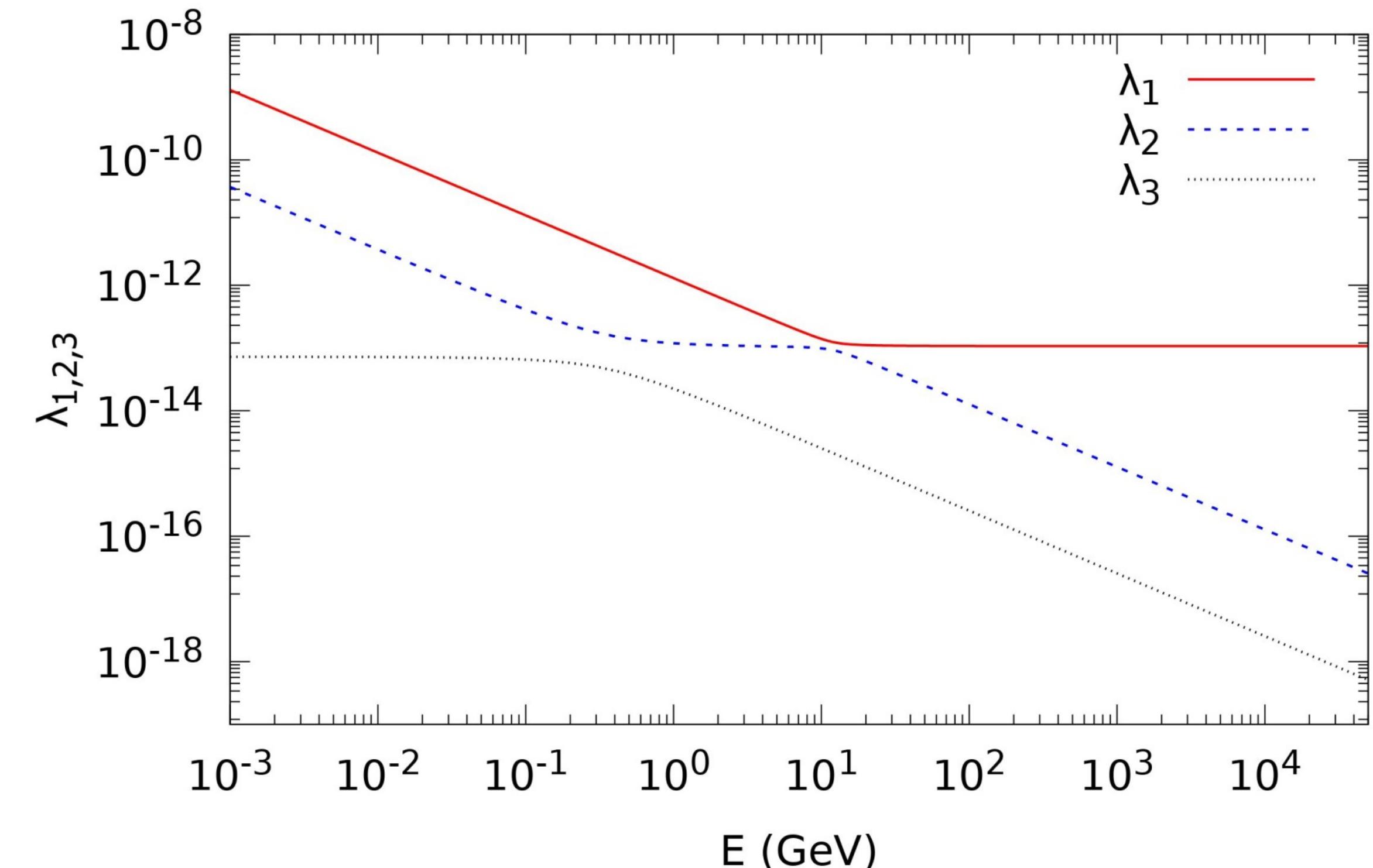
$$P_{\nu_e \rightarrow \nu_\mu} = \sin^2 2\theta_M \sin^2 \left( 1.27 \frac{\Delta m_M^2 L}{E} \right)$$

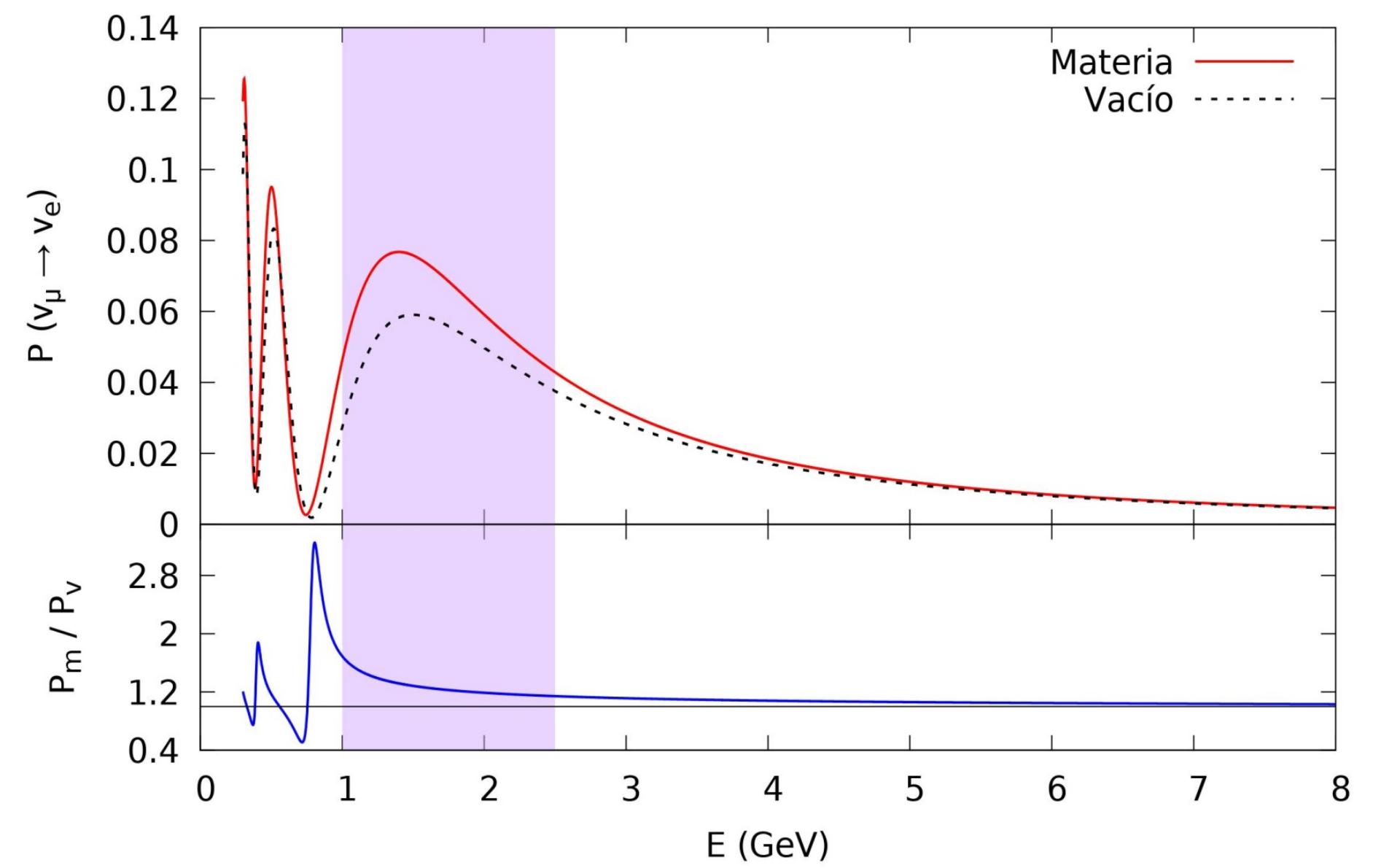
# Three Neutrinos Oscillation in Matter

In this case  $U$  get the form:

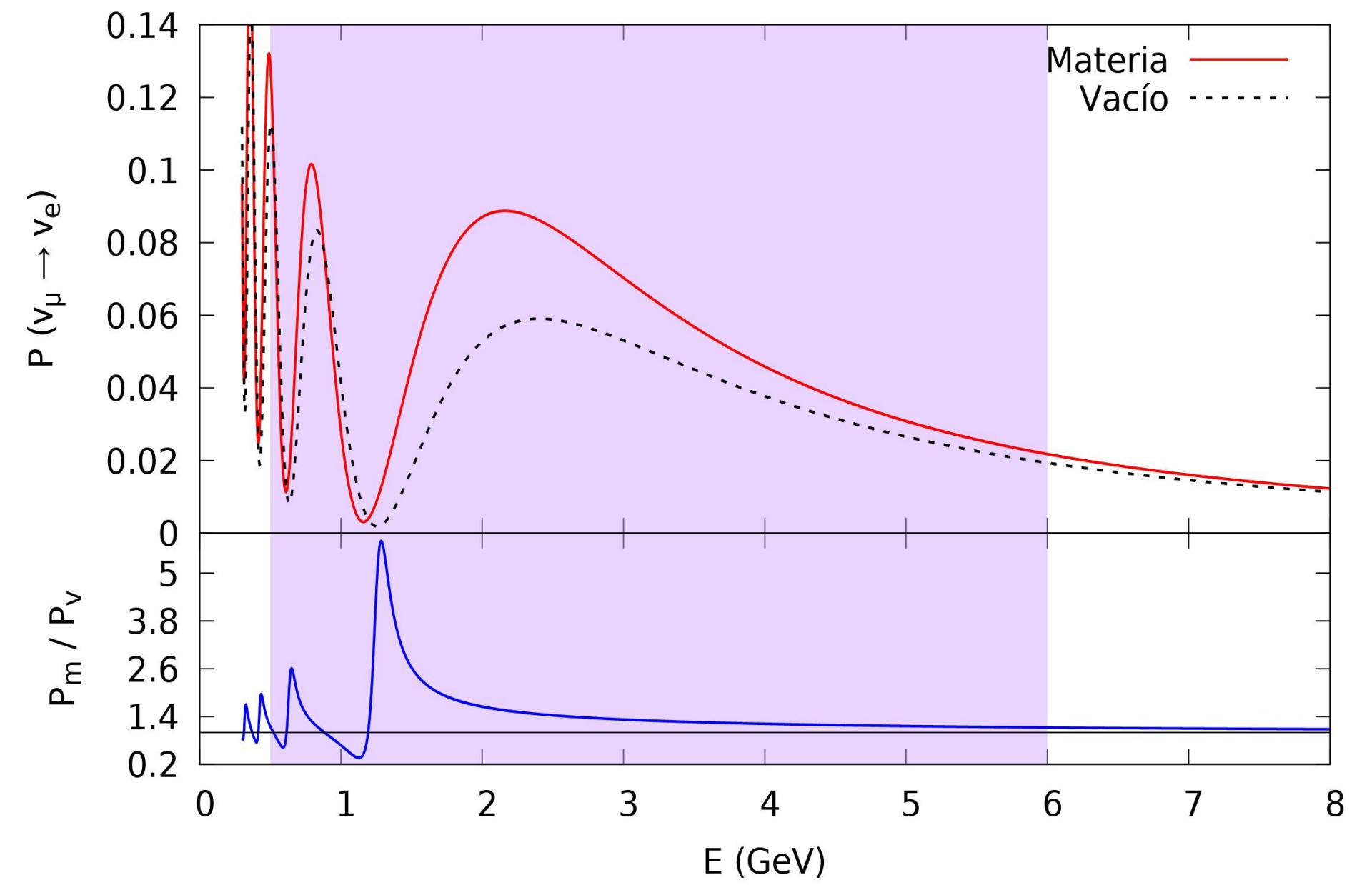
$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & C_{23} & S_{23} \\ 0 & -S_{23} & C_{23} \end{pmatrix} \begin{pmatrix} C_{13} & 0 & S_{13} e^{i\delta_{cp}} \\ 0 & 1 & 0 \\ -S_{13} e^{i\delta_{cp}} & 0 & C_{13} \end{pmatrix} \begin{pmatrix} C_{12} & S_{12} & 0 \\ -S_{13} & C_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Valores de parámetros		
Experimento	L (km)	$\rho$ (g cm $^{-3}$ )
DUNE	1300	2.8
NO $\nu$ A	810	2.8

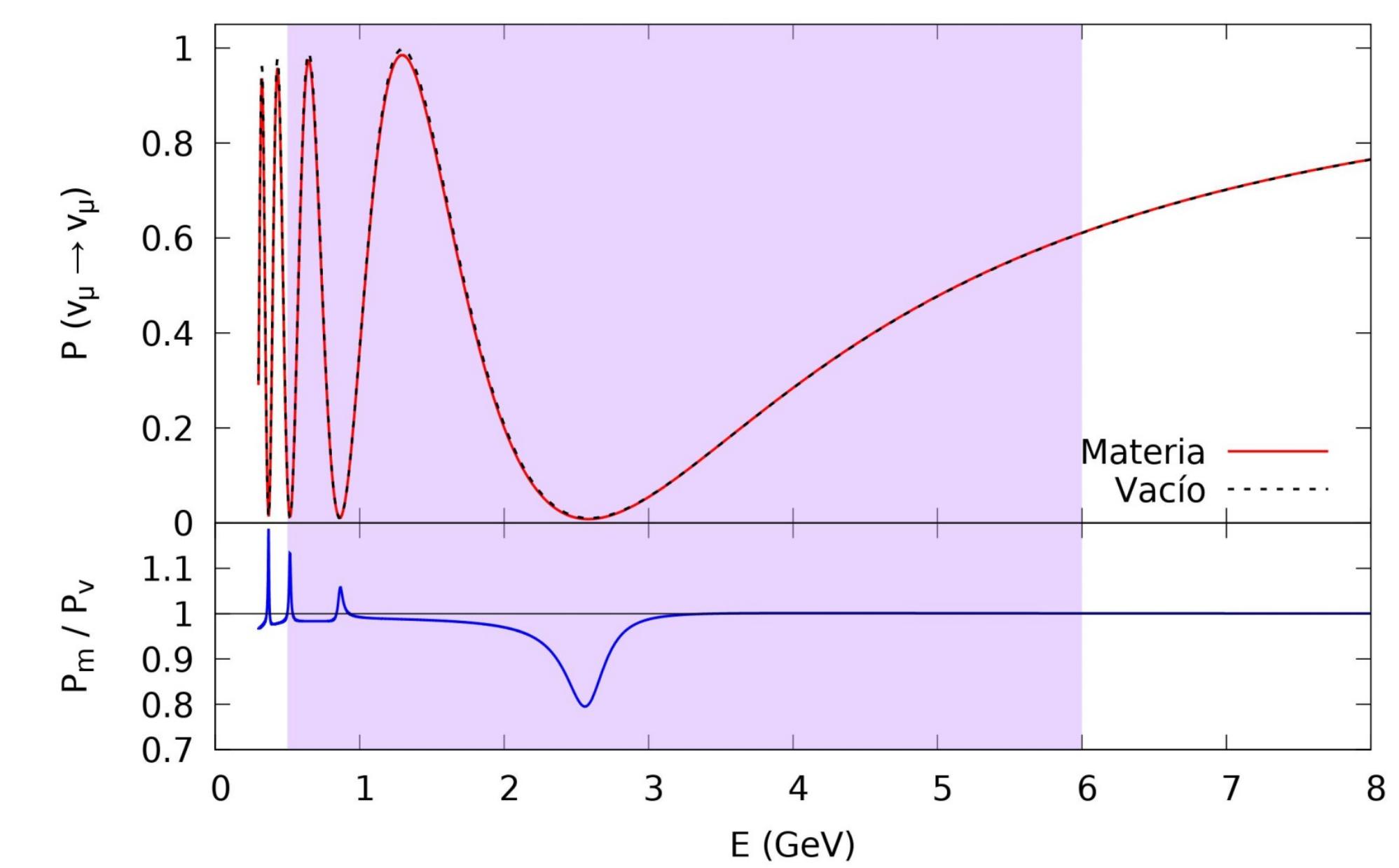
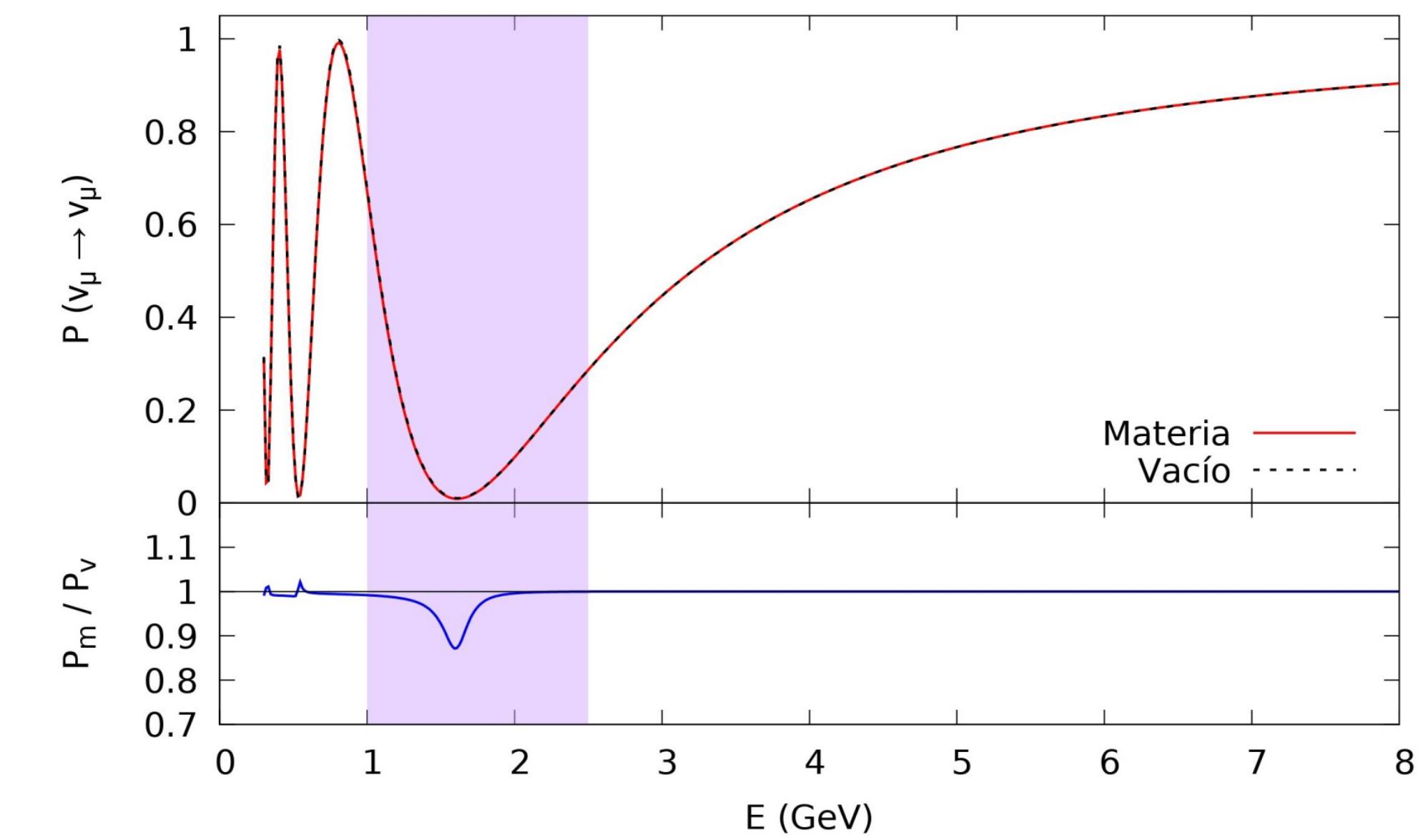




NOvA



DUNE



# Oscillation Probability in Matter with NSI

The physics of neutrino oscillation as we have seen, has made remarkable progress as the main description of neutrino flavor transitions in recent time.



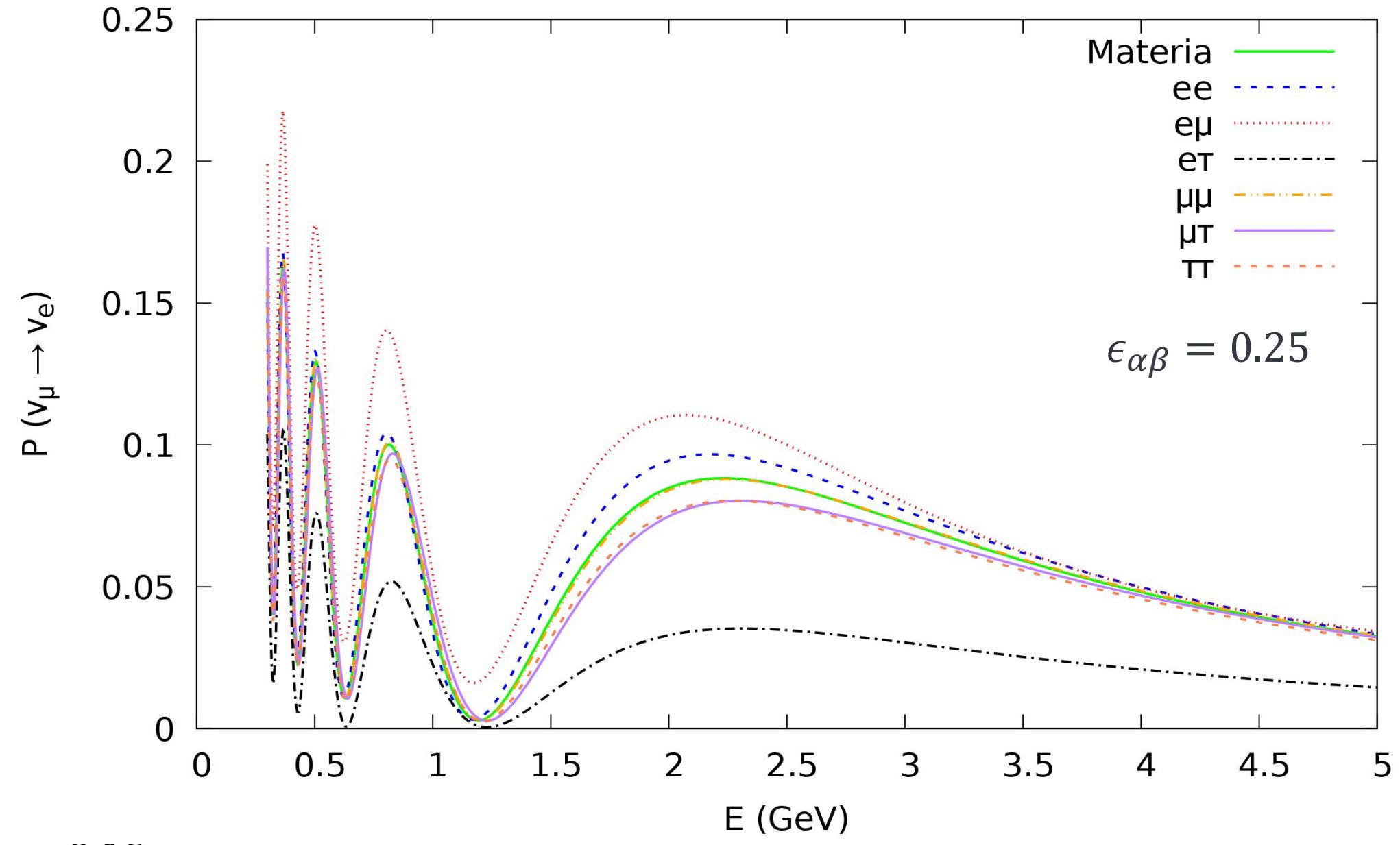
$$H_{\text{NSI}} = \frac{1}{2E} (U \mathbb{M}^2 U^\dagger + \mathbb{V} \epsilon^m)$$

$$\epsilon^m = \begin{pmatrix} 1 + \epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon^*_{e\mu} & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon^*_{e\tau} & \epsilon^*_{\mu\tau} & \epsilon_{\tau\tau} \end{pmatrix}$$

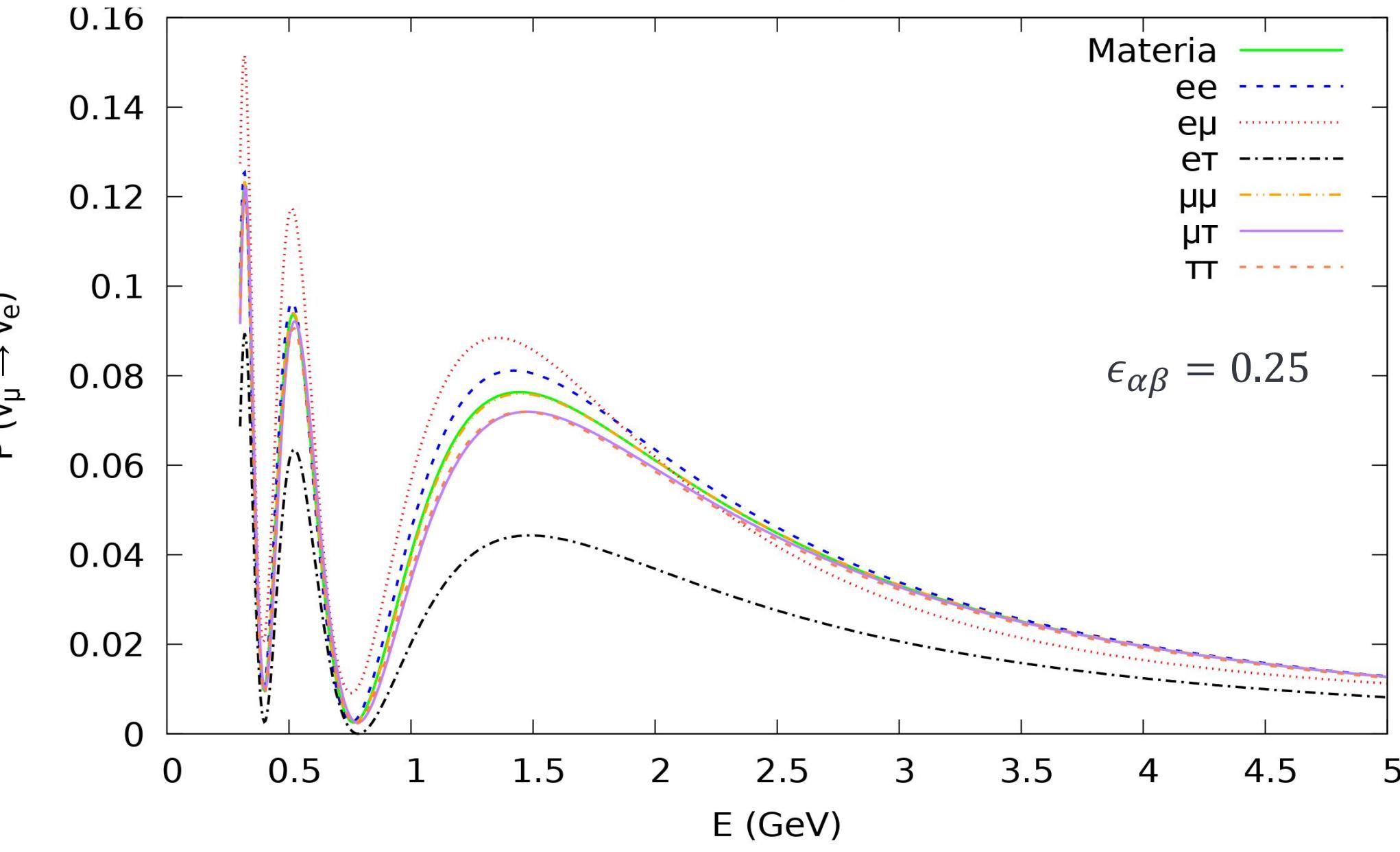
$$\epsilon_{\alpha\beta} \equiv \sum_{f=e,u,d} \epsilon_{\alpha\beta}^f \frac{N_f}{N_e}$$

- $\alpha, \beta = e, \mu, \tau$

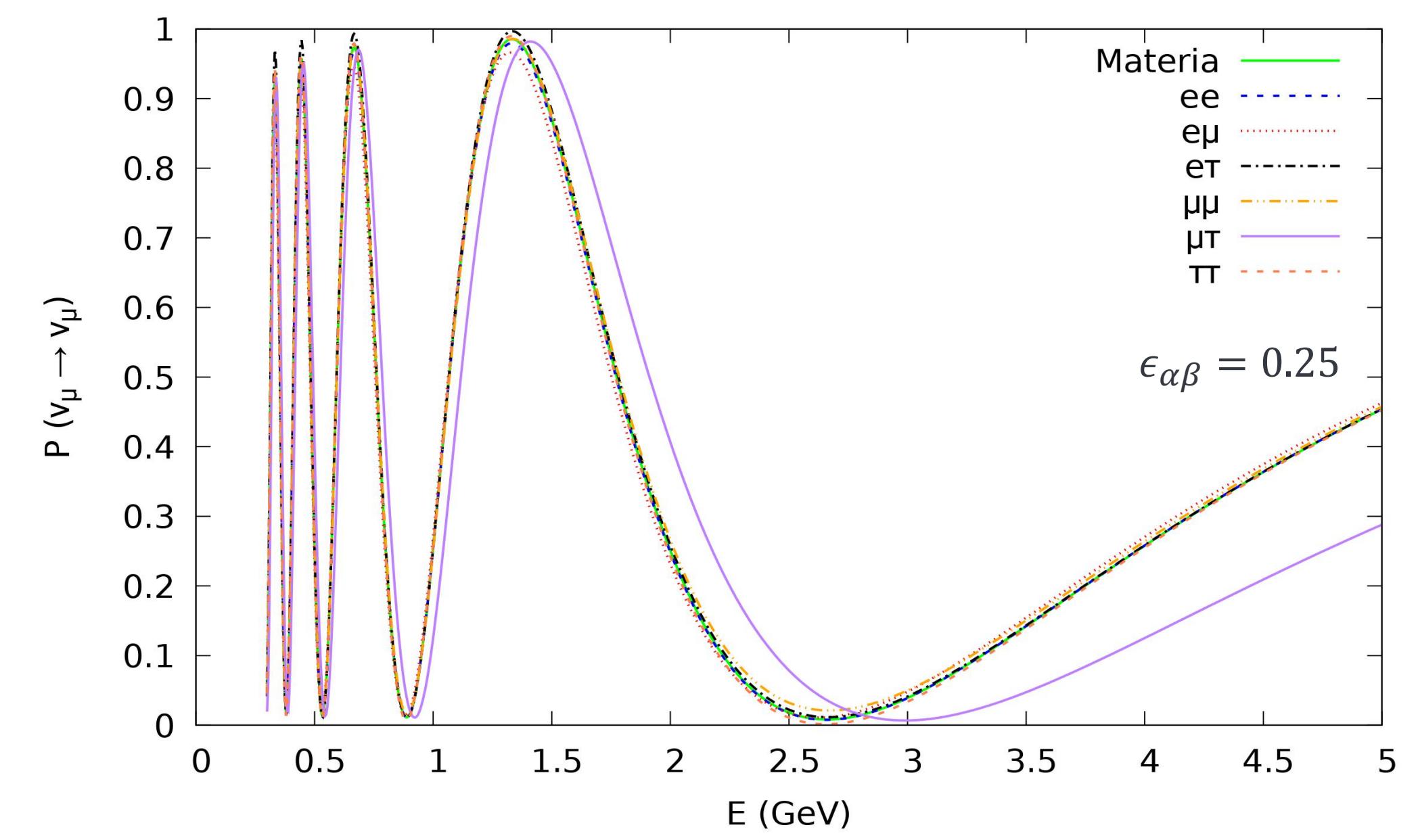
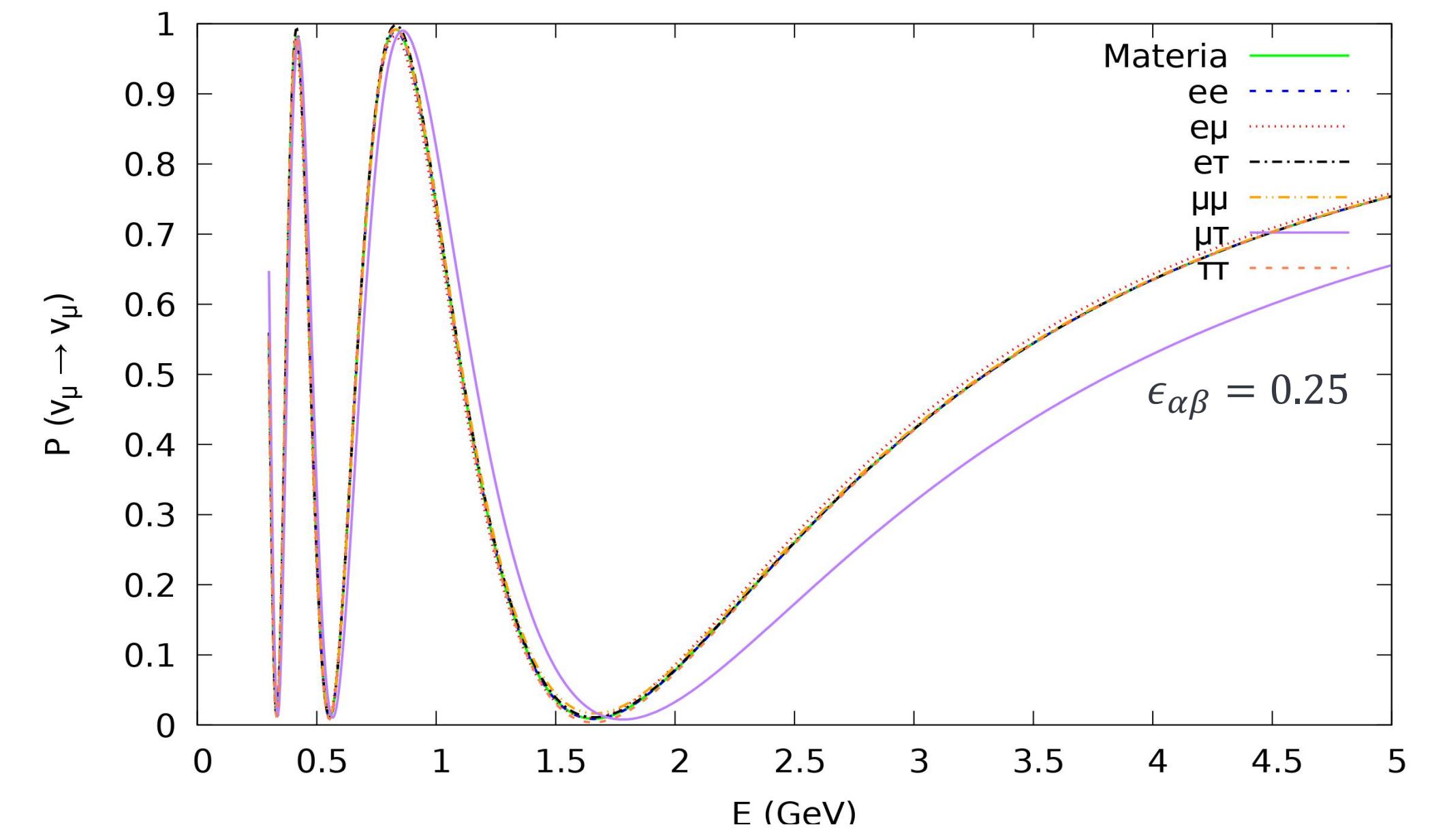
- $\epsilon_{\alpha\beta}$  are complex to  $\alpha \neq \beta$
- $\epsilon_{\alpha\beta}$  are real to  $\alpha = \beta$

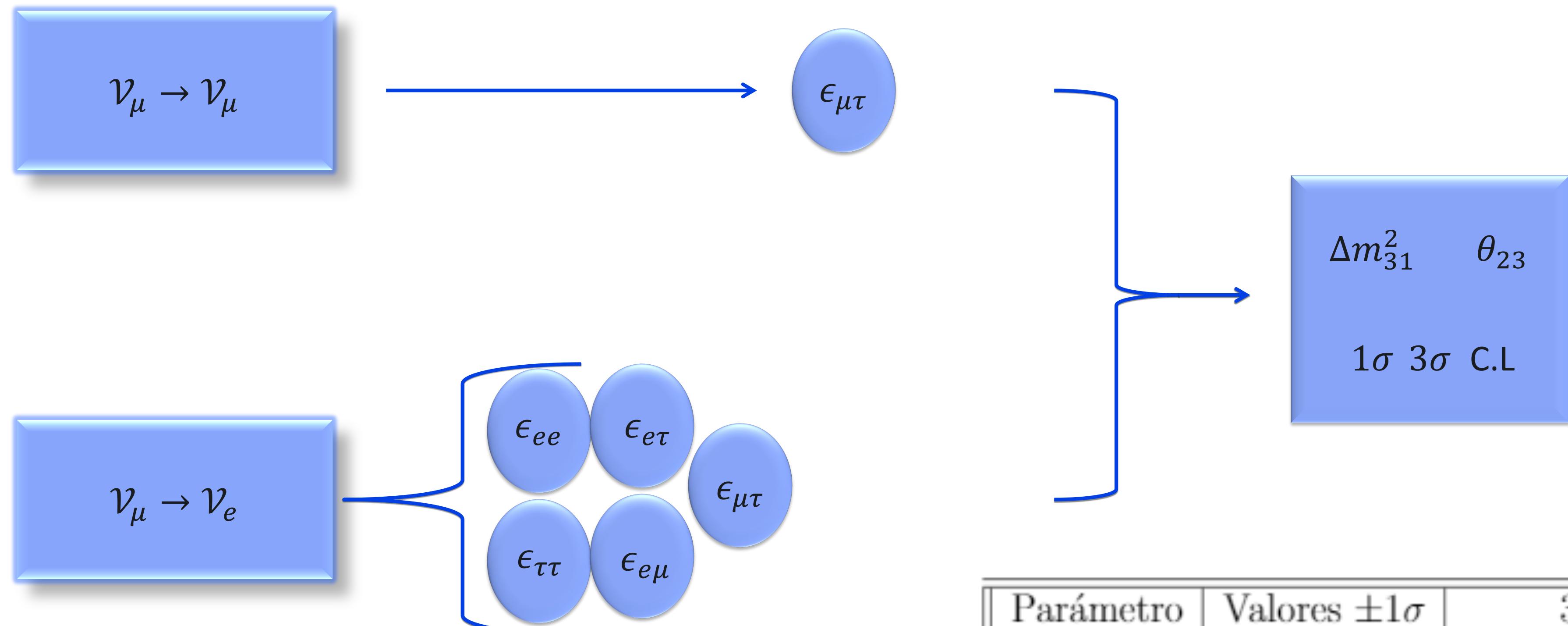


NOVA

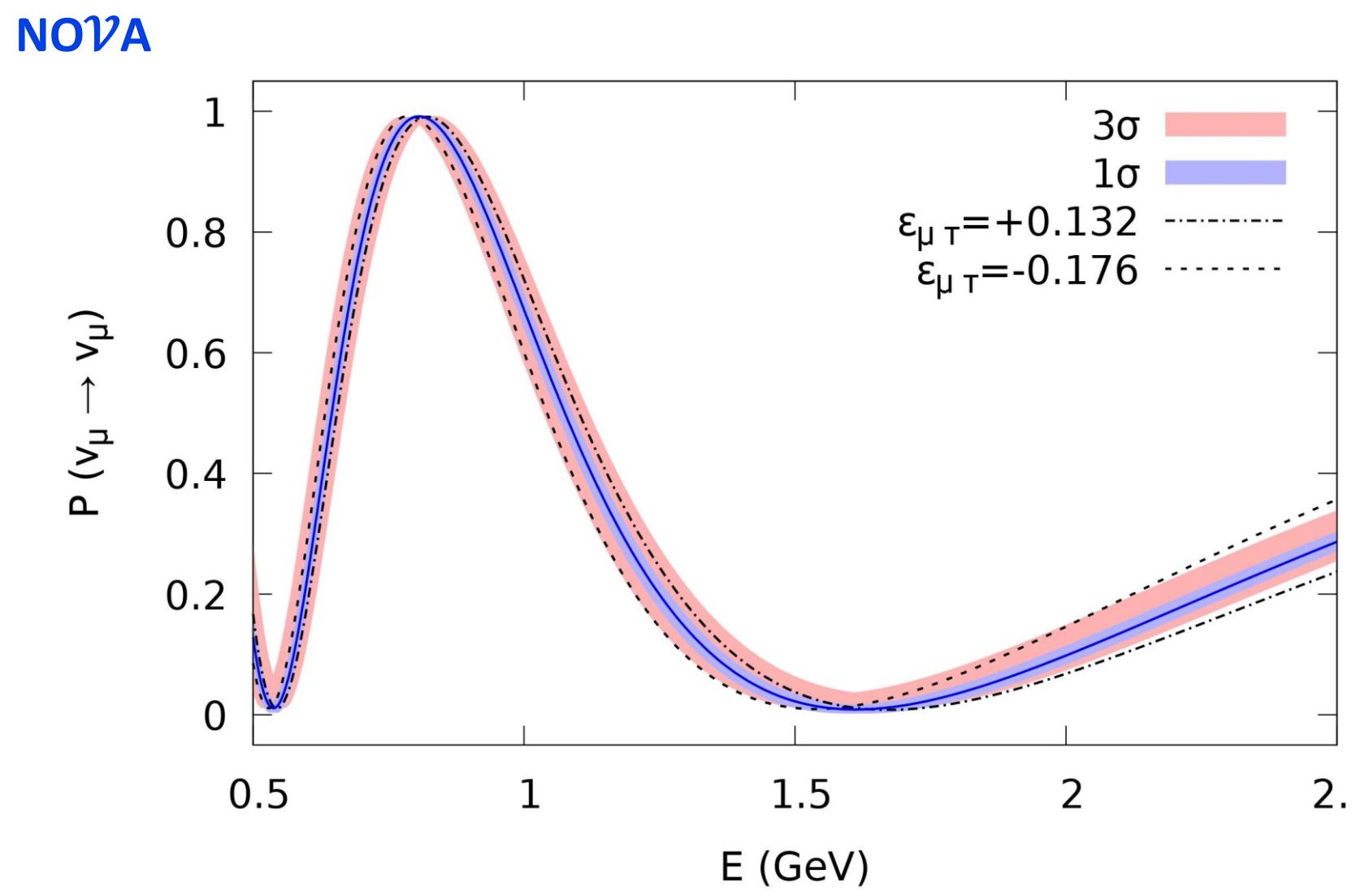
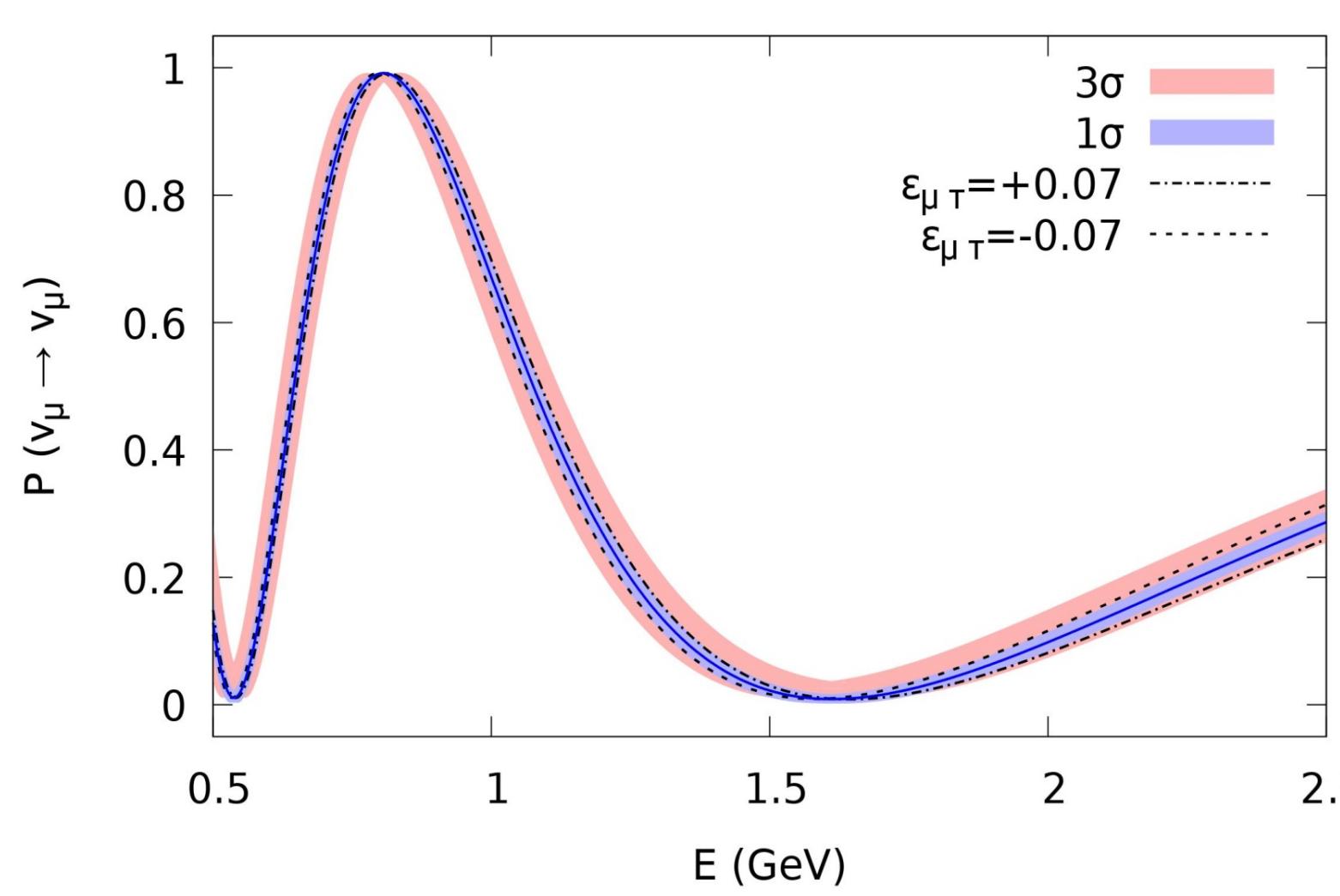


DUNE

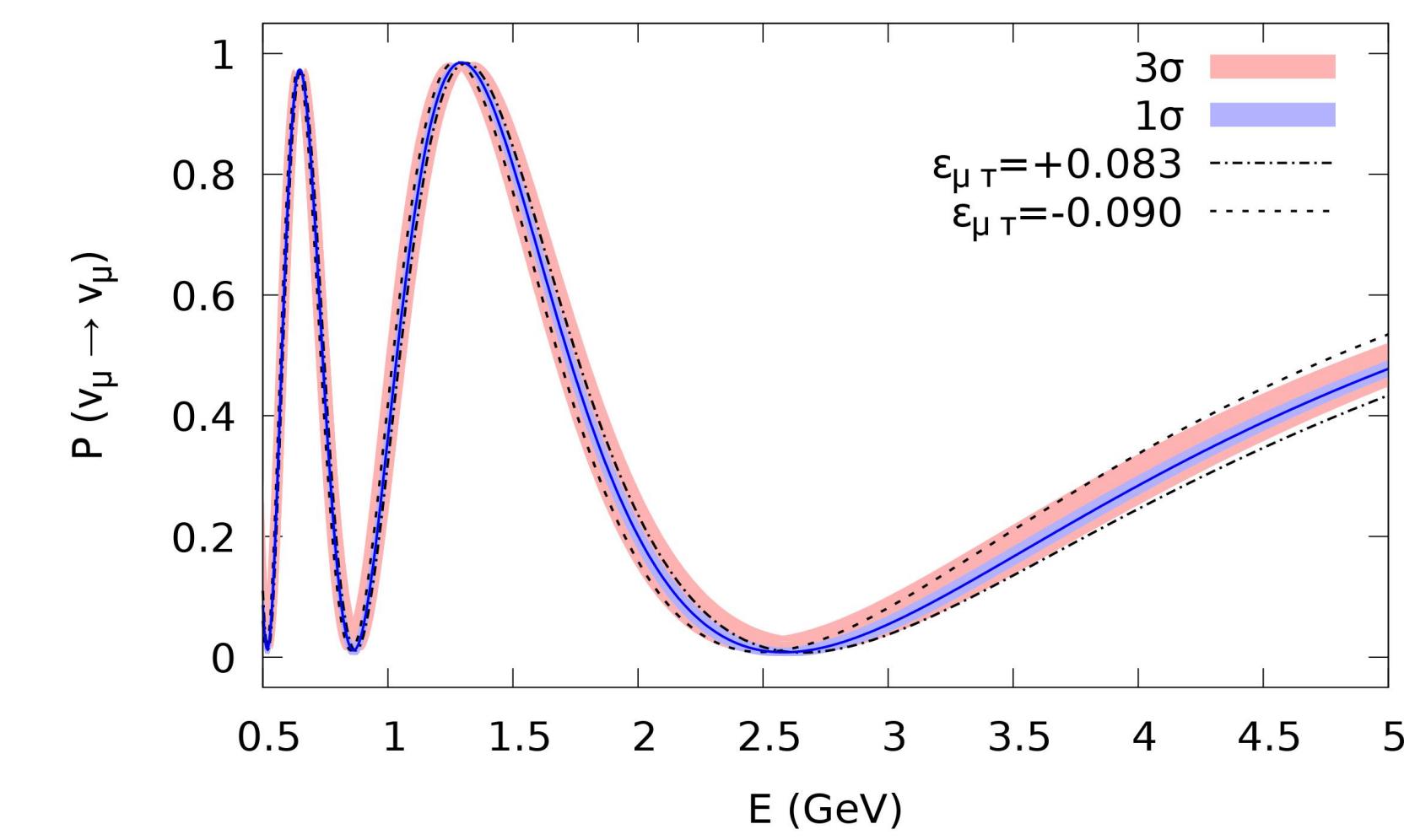
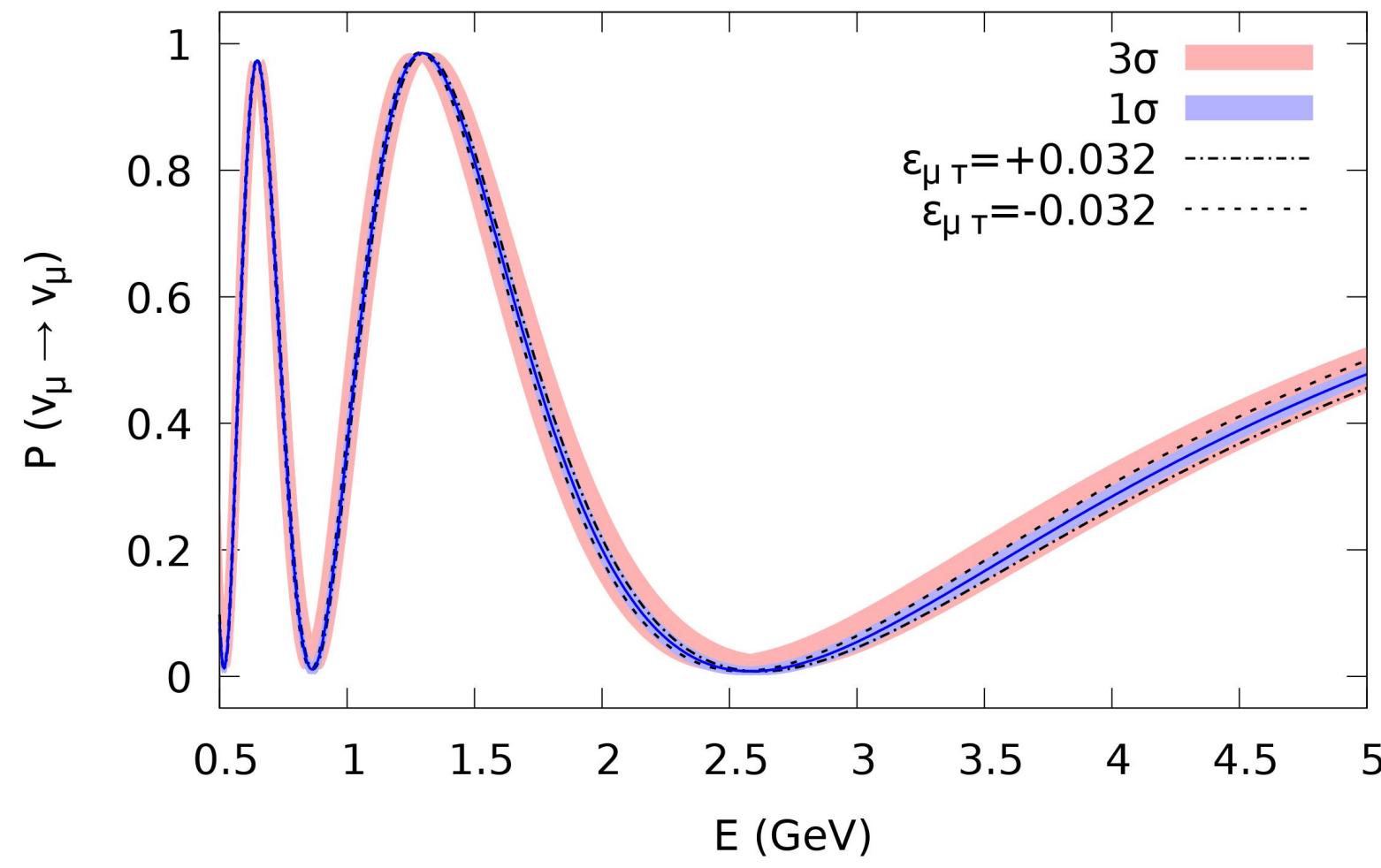


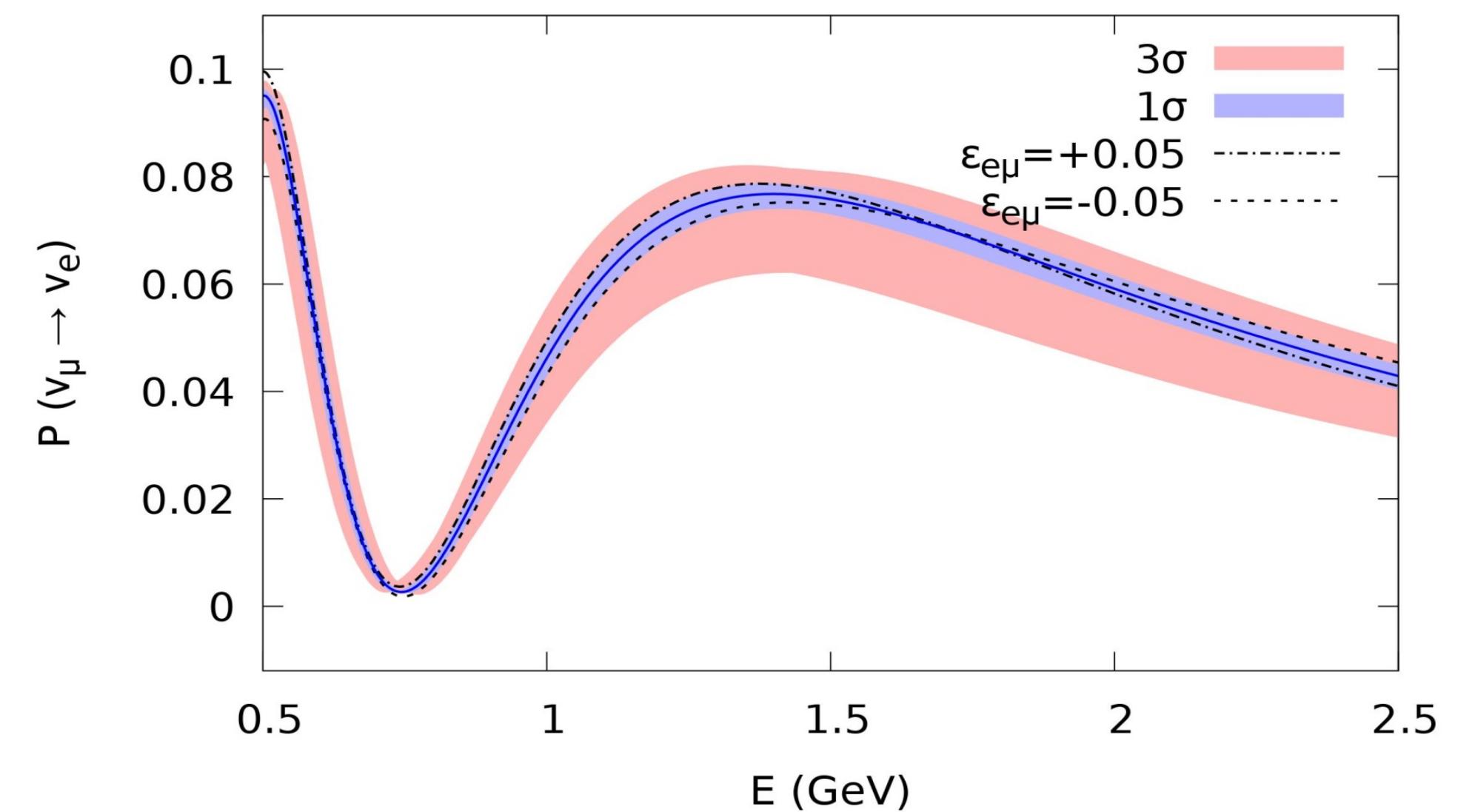


Parámetro	Valores $\pm 1\sigma$	$3\sigma$
$\theta_{23}$ ( $^\circ$ )	$48.6^{+1.0}_{-1.4}$	$41.1 \rightarrow 51.3$
$\frac{\Delta m_{31}^2}{10^{-3} \text{ eV}^2}$	$2.528^{+0.029}_{-0.031}$	$2.436 \rightarrow 2.618$

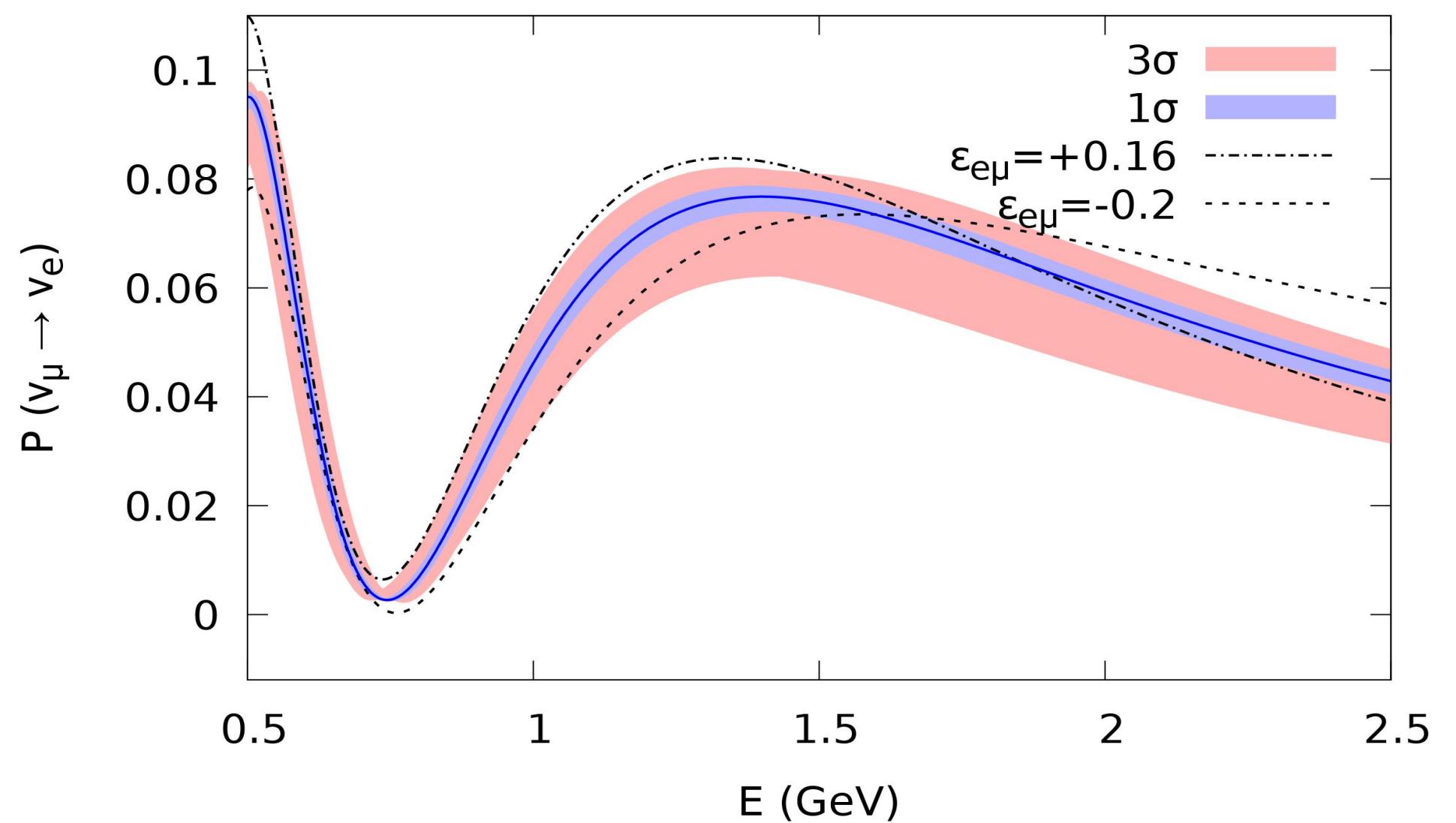


	$1\sigma$	$3\sigma$
NO $\nu$ A	$-0.07 \leq \epsilon_{\mu\tau} \leq 0.07$	$-0.176 \leq \epsilon_{\mu\tau} \leq 0.132$
DUNE	$-0.032 \leq \epsilon_{\mu\tau} \leq 0.032$	$-0.090 \leq \epsilon_{\mu\tau} \leq 0.083$

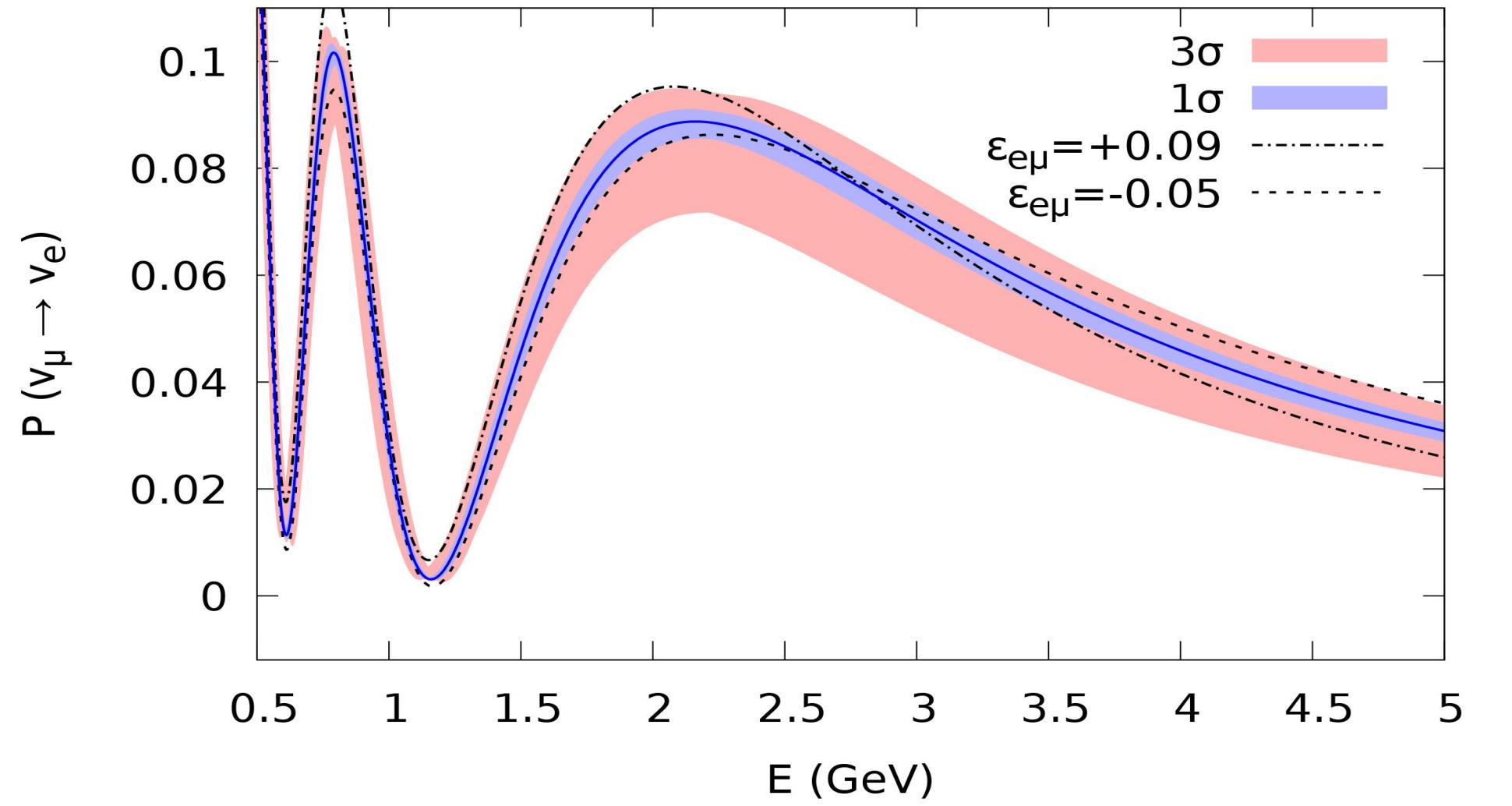
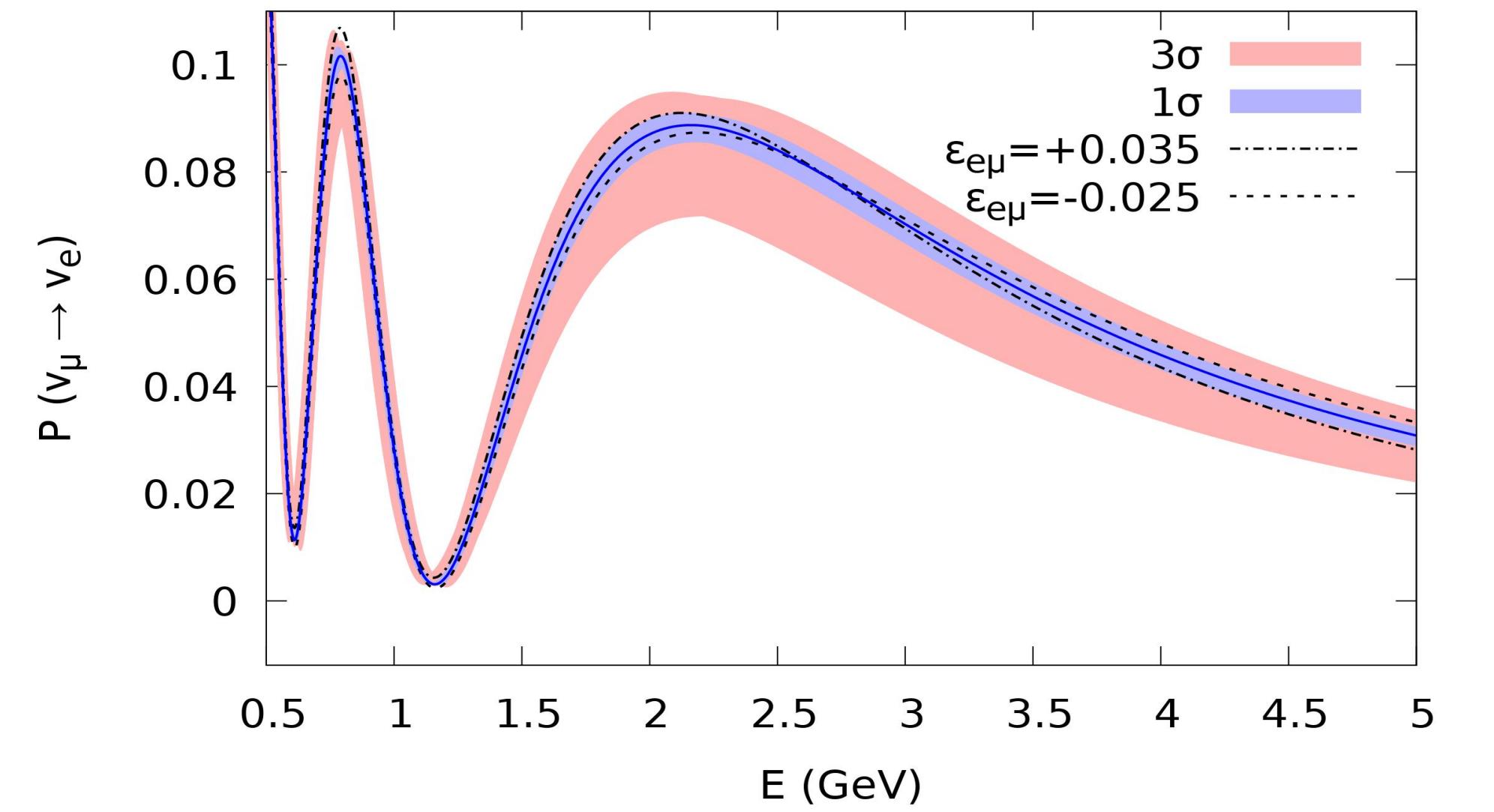




NOVA



DUNE



Parámetros NSI	$1\sigma$	$3\sigma$
$\epsilon_{ee}$	$-0.23 \leq \epsilon_{ee} \leq 0.18$	$-0.6 \leq \epsilon_{ee} \leq 0.4$
$\epsilon_{e\mu}$	$-0.05 \leq \epsilon_{e\mu} \leq 0.05$	$-0.2 \leq \epsilon_{e\mu} \leq 0.16$
$\epsilon_{e\tau}$	$-0.02 \leq \epsilon_{e\tau} \leq 0.02$	$-0.07 \leq \epsilon_{e\tau} \leq 0.13$
$\epsilon_{\mu\tau}$	$-0.16 \leq \epsilon_{\mu\tau} \leq 0.18$	$-0.4 \leq \epsilon_{\mu\tau} \leq 0.5$
$\epsilon_{\tau\tau}$	$-0.28 \leq \epsilon_{\tau\tau} \leq 0.34$	$-0.4 \leq \epsilon_{\tau\tau} \leq 0.8$

**NO $\nu$ A**

Parámetros NSI	$1\sigma$	$3\sigma$
$\epsilon_{ee}$	$-0.24 \leq \epsilon_{ee} \leq 0.24$	$-0.45 \leq \epsilon_{ee} \leq 0.35$
$\epsilon_{e\mu}$	$-0.025 \leq \epsilon_{e\mu} \leq 0.035$	$-0.05 \leq \epsilon_{e\mu} \leq 0.09$
$\epsilon_{e\tau}$	$-0.02 \leq \epsilon_{e\tau} \leq 0.02$	$-0.05 \leq \epsilon_{e\tau} \leq 0.1$
$\epsilon_{\mu\tau}$	$-0.1 \leq \epsilon_{\mu\tau} \leq 0.1$	$-0.35 \leq \epsilon_{\mu\tau} \leq 0.35$
$\epsilon_{\tau\tau}$	$-0.22 \leq \epsilon_{\tau\tau} \leq 0.22$	$-0.42 \leq \epsilon_{\tau\tau} \leq 0.48$

**DUNE**

	$1\sigma$	$3\sigma$
NO $\nu$ A	$-0.07 \leq \epsilon_{\mu\tau} \leq 0.07$	$-0.176 \leq \epsilon_{\mu\tau} \leq 0.132$
DUNE	$-0.032 \leq \epsilon_{\mu\tau} \leq 0.032$	$-0.090 \leq \epsilon_{\mu\tau} \leq 0.083$

# Conclusions and Perspectives

- The distance of source to detector of a neutrino experiment varies the probability oscillation and results in a change in the energy range.
- The interaction of charge current with electrons in the medium affects noticeably the oscillation channel  $\mathcal{V}_\mu \rightarrow \mathcal{V}_e$ .
- The fact that the NSI parameters have values other than zero may somehow be interfering with the measurement of the parameters that govern the neutrino oscillation.
- The NSI parameters have an effect that seems to mix both changes in amplitude and frequency.
- For future projects, it is considered that the other standard parameters will be varied in order to obtain a more precise estimate of these NSI parameters.



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