

D Mixing and Decay

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for the Belle Collaboration

XXX. PHYSICS IN COLLISION

September 1st, 2010



Charm as a probe of New Physics in

- ① $D - \bar{D}$ mixing
- ② CP violation
- ③ Rare decays

Mixing Phenomena

Mixing is a process

- in which **particle** changes to its **anti-particle** and vice versa
- possible only in flavored neutral **particle–anti-particle** systems

Mixing observed in all neutral meson systems:

Meson M	Flavors	Particle discovered	Mixing discovered	Implication
K^0	$\bar{s}d$	1950 (Caltech)	1956 (Columbia)	m_c
B_d^0	$\bar{b}d$	1983 (CESR)	1987 (Desy)	m_t
B_s^0	$\bar{b}s$	1992 (LEP)	2006 (Fermilab)	??
D^0	$c\bar{u}$	1976 (SLAC)	2007 (KEK, SLAC)	??

Mixing is not possible in π^0 system since $\pi^0 \equiv \bar{\pi}^0$;
 t quark decays before it could form a hadron.

Uniqueness of Charm:

- 1 the only Up-type neutral meson allowing full range of probes for New Physics

Mixing Phenomenology - Time evolution

- Time evolution of $D^0 - \bar{D}^0$ system given by time-dependent Schrödinger Eq.

$$i \frac{\partial}{\partial t} \begin{pmatrix} |D^0\rangle \\ |\bar{D}^0\rangle \end{pmatrix} = [\mathbf{M} - \frac{i}{2}\mathbf{\Gamma}] \begin{pmatrix} |D^0\rangle \\ |\bar{D}^0\rangle \end{pmatrix}$$

- Eigenstates of $[\mathbf{M} - \frac{i}{2}\mathbf{\Gamma}]$ are mass eigenstates $D_{1,2}$ with $m_{1,2}$ and $\Gamma_{1,2}$
 $\hookrightarrow \neq$ flavor eigenstates D^0 and \bar{D}^0

$$|D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle \quad p^2 + q^2 = 1$$

- time evolution of flavor eigenstate

$$|D^0(t)\rangle = \left[|D^0\rangle \cosh\left(\frac{ix+y}{2}t\right) + \frac{q}{p}|\bar{D}^0\rangle \sinh\left(\frac{ix+y}{2}t\right) \right] \times e^{-\frac{1}{2}(1+\frac{im}{\Gamma})t}$$

Mixing parameters:

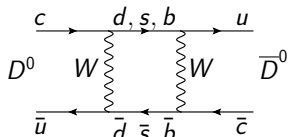
$$\mathbf{x} = \frac{m_1 - m_2}{\Gamma}, \quad \mathbf{y} = \frac{\Gamma_1 - \Gamma_2}{2\Gamma}, \quad \Gamma = \frac{1}{2}(\Gamma_1 + \Gamma_2)$$

Contributions to x and y

Standard Model

Burdman, Shipsey, Ann.Rev.Nucl.Part.Sci.53,431; Falk et al., PRD65, 054034; Bigi, Uraltsev, Nucl. Phys. B592, 92;

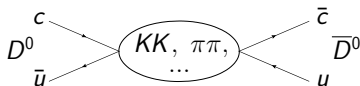
Short distance



Effective CKM and GIM suppression

$$|x|, |y| \leq 10^{-3}$$

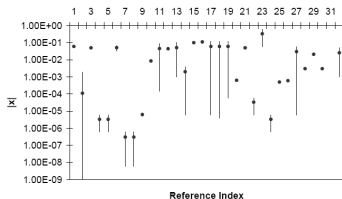
Long distance



Contribution from hadronic intermediate states

$$x, y \sim \text{up to } 1\%$$

New Physics predictions for $|x|$



- Large uncertainty in SM mixing rate
 \hookrightarrow difficult to identify New Physics contributions (except if $x \gg y$)
- however, measurements of x and y still provide useful constraints on many New Physics models

CP Violation in Charm

Q: If $D - \bar{D}$ mixing can't reveal New Physics, what can?

A: CP violation!

- Source of CP violation in the Standard Model
↪ single complex phase (η) in the quark mixing matrix

$$\mathbf{V}_{\text{CKM}} = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\lambda^3(\rho - i\eta + \frac{1}{2}\eta\lambda^2) \\ -\lambda & 1 - \frac{1}{2}\lambda^2 - i\eta A^2\lambda^4 & A\lambda^2(1 + i\eta\lambda^2) \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

- Charmed meson processes
↪ CP violation in Standard Model is CKM suppressed: $\sim \mathcal{O}(10^{-3})$
↪ Possible only in Singly Cabibbo suppressed decays (tree + penguin amplitudes)
↪ CP violation in New Physics models: **up to 1%**
Grossman, Kagan, Nir, PRD75, 036008; Bigi, hep-ph/0104008
↪ Current experimental sensitivity: **few 0.1%**

Observation of *large* $\mathcal{O}(1\%)$ CPV in charm decays would be a sign for New Physics!

CP Violation Phenomenology

- Classification of CP-violating effects:

$$\hookrightarrow \mathbf{A}_{CP}^f = \frac{\Gamma(D \rightarrow f) - \Gamma(\bar{D} \rightarrow \bar{f})}{\Gamma(D \rightarrow f) + \Gamma(\bar{D} \rightarrow \bar{f})} \approx \mathbf{a}_d^f + \mathbf{a}_m^f + \mathbf{a}_i^f$$

- \mathbf{a}_d^f : CP violation in decay

$$\hookrightarrow |\mathcal{A}_f| \neq |\bar{\mathcal{A}}_{\bar{f}}| \quad \mathcal{A}_f = \langle f | D \rangle, \quad \bar{\mathcal{A}}_{\bar{f}} = \langle \bar{f} | \bar{D} \rangle$$

- \mathbf{a}_m^f : CP violation in mixing

$$\hookrightarrow |\mathbf{q}/\mathbf{p}| \neq 1 \quad |D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle$$

- \mathbf{a}_i^f : CP violation in interference

of decays with and without mixing ($f = \bar{f}$)

$$\hookrightarrow \phi \neq 0 \text{ or } \pi \quad \phi = \arg\left(\frac{q}{p} \frac{\bar{\mathcal{A}}_{\bar{f}}}{\mathcal{A}_f}\right)$$

Experimental observables

Time-integrated measurements:

$$A_{CP}^f = \frac{N(D \rightarrow f) - N(\bar{D} \rightarrow \bar{f})}{N(D \rightarrow f) + N(\bar{D} \rightarrow \bar{f})}$$

Time-dependent measurements:

$$A_{\Gamma} = \frac{\tau(D \rightarrow f_{CP}) - \tau(\bar{D} \rightarrow f_{CP})}{\tau(D \rightarrow f_{CP}) + \tau(\bar{D} \rightarrow f_{CP})} = -(a_m + a_i)$$

Available Charm Samples

B-factories:

- continuum production @ $\Upsilon(4S)$:
 $\sigma(c\bar{c}) \approx 1.3 \text{ nb}$
- Belle: $\sim 1.3 \cdot 10^9$ $c\bar{c}$ pairs
- Babar: $\sim 0.7 \cdot 10^9$ $c\bar{c}$ pairs

Tevatron:

- $p\bar{p}$ @ $\sim 2 \text{ TeV}$
- CDF: $\sim 70 \cdot 10^9$ D^0 's

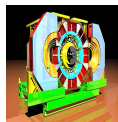
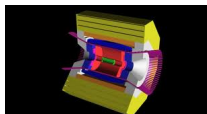
Charm factories:

- $\psi(3770) \rightarrow D^0\bar{D}^0, D^+D^-$
- CLEO: $\sim 2.8 \cdot 10^6$ $D^0\bar{D}^0$ pairs
- BESIII: $\sim 3.4 \cdot 10^6$ $D^0\bar{D}^0$ pairs

LHC:

- pp @ 7 TeV
- LHCb: *has only started*

Diverse exp. conditions!



Mixing measurements

Decay time distribution sensitive to mixing parameters x and y and depends on the final state:

$$\frac{dN(D^0 \rightarrow f)}{dt} \propto \left| \langle f | D^0 \rangle + \frac{q}{p} \left(\frac{ix+y}{2} \langle f | \bar{D}^0 \rangle \right) \right|^2$$

Final state	Belle	BaBar	CDF	Cleo	E791	Focus
$K^+ \pi^-$	✓	★	★	✓	✓	✓
$KK, \pi\pi$	★	★		✓	✓	✓
$K_S^0 \pi\pi$	✓	✓		✓		
$K_S^0 KK$	✓	✓				
$K^+ \pi^- \pi^0$		★				
$K^+ \pi^- \pi^- \pi^+$		✓				
$K^+ \ell^- \nu_\ell$	✓	✓		✓	✓	
quantum corr. in $\psi(3770) \rightarrow D^0 \bar{D}^0$				✓		

✓ – measurement performed; ★ – evidence for mixing

Full list of all $D^0 - \bar{D}^0$ mixing measurements is available at:
<http://www.slac.stanford.edu/xorg/hfag/charm/index.html>

Mixing and CPV in decays to CP eigenstates ($KK, \pi\pi$)

- Measurement of lifetime difference between $D^0 \rightarrow K^- \pi^+$ (CP -mixed) and $D^0 \rightarrow K^+ K^-, \pi^+ \pi^-$ (CP -even) decays (tagged and untagged samples)

$$\hookrightarrow \Gamma(D^0 \rightarrow K^- \pi^+) \propto e^{-t/\tau_{D^0}} \quad y_{CP} = \frac{\tau_{KK, \pi\pi}}{\tau_{KK, \pi\pi}} - 1$$

$$\hookrightarrow \Gamma(D^0 \rightarrow K^+ K^-, \pi^+ \pi^-) \propto e^{-(1+y_{CP})t/\tau_{D^0}} \quad A_\Gamma = \frac{\tau(\bar{D}^0 \rightarrow f_{CP}) - \tau(D^0 \rightarrow f_{CP})}{\tau(\bar{D}^0 \rightarrow f_{CP}) + \tau(D^0 \rightarrow f_{CP})}$$

- In case of no CP violation: $y_{CP} = y$ and $A_\Gamma = 0$

Mixing and CPV in decays to CP eigenstates ($KK, \pi\pi$)

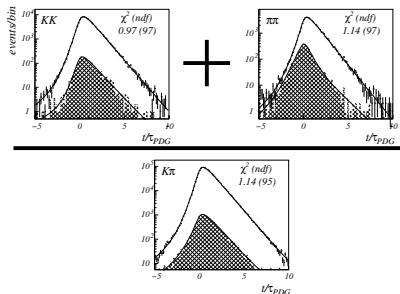
- Measurement of lifetime difference between $D^0 \rightarrow K^- \pi^+$ (CP -mixed) and $D^0 \rightarrow K^+ K^-, \pi^+ \pi^-$ (CP -even) decays (tagged and untagged samples)

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$$\hookrightarrow \Gamma(D^0 \rightarrow K^+ K^-, \pi^+ \pi^-) \propto e^{-(1+y_{CP})t/\tau_{D^0}} \quad A_{\Gamma} = \frac{\tau(\bar{D}^0 \rightarrow f_{CP}) - \tau(D^0 \rightarrow f_{CP})}{\tau(\bar{D}^0 \rightarrow f_{CP}) + \tau(D^0 \rightarrow f_{CP})}$$

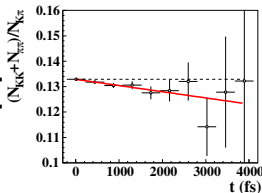
- In case of no CP violation: $y_{CP} = y$ and $A_{\Gamma} = 0$

Belle [PRL98, 211803 (2007)]



$$y_{CP} = (1.31 \pm 0.32 \pm 0.25)\%$$

First evidence for mixing!

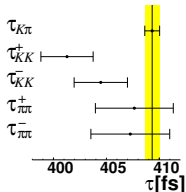


$$A_{\Gamma} = (0.01 \pm 0.30 \pm 0.15)\%$$

Mixing and CPV in decays to CP eigenstates ($KK, \pi\pi$)

BaBar performed measurements of y_{CP} using:

- 1 Tagged Sample: require D^0 to originate in $D^{*+} \rightarrow D^0\pi^+$ decay



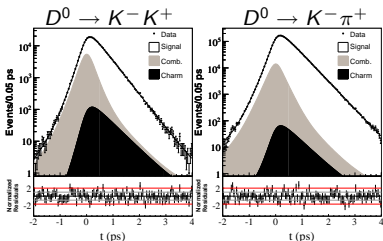
PRD78, 011105 (2008)

$$y_{CP} = (1.24 \pm 0.39 \pm 0.13)\%$$

$$\Delta Y = -(0.26 \pm 0.36 \pm 0.08)\%$$

$$\Delta Y = (1 + y_{CP})A_{\Gamma}$$

- 2 Untagged Sample: take all D^0 candidates (except from the tagged sample)



PRD80, 071103 (2009)

$$y_{CP} = (1.12 \pm 0.26 \pm 0.22)\%$$

Combined: tagged + untagged

$$y_{CP} = (1.16 \pm 0.22 \pm 0.18)\%$$

4.1 σ significance!

Time dependent Dalitz analyses

- Many quasi 2-body intermediate states, e.g. in $D^0 \rightarrow K_S^0 \pi^+ \pi^-$ decays:
 - ↪ CF: $D^0 \rightarrow K^{*-} \pi^+$
 - ↪ DCS: $D^0 \rightarrow K^{*+} \pi^-$
 - ↪ CP: $D^0 \rightarrow \rho^0 K_S^0$

$$D^0 : \mathcal{A}(m_-^2, m_+^2) = \sum_r a_r e^{i\phi_r} \mathcal{A}_r(m_-^2, m_+^2) + a_{nr} e^{i\phi_{nr}}$$

$$\bar{D}^0 : \bar{\mathcal{A}}(m_-^2, m_+^2) = \sum_r \bar{a}_r e^{i\bar{\phi}_r} \bar{\mathcal{A}}_r(m_-^2, m_+^2) + a_{nr} e^{i\phi_{nr}}$$

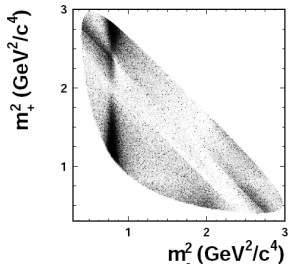
If $f = \bar{f} \Rightarrow$ relative phases determined
(unlike $D^0 \rightarrow K^+ \pi^- (\pi^0)$)

- Time dependent decay rate ($\mathcal{A}_{1,2} = \frac{1}{2}(\mathcal{A} \pm \bar{\mathcal{A}})$)

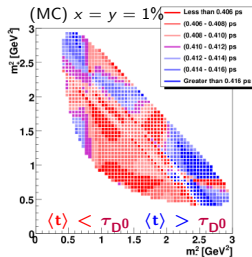
$$\Gamma(m_-^2, m_+^2, t) = e^{-\Gamma t} (|\mathcal{A}_1|^2 e^{-y\Gamma t} + |\mathcal{A}_2|^2 e^{y\Gamma t} + 2\mathcal{R}[\mathcal{A}_1 \mathcal{A}_2^*] \cos(x\Gamma t) + 2\mathcal{I}[\mathcal{A}_1 \mathcal{A}_2^*] \sin(x\Gamma t))$$

Simultaneous determination of x and y!

Dalitz plot for $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

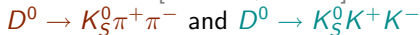


$\langle t \rangle$ across Dalitz plot

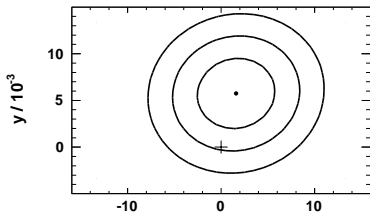


Mixing and CPV $D^0 \rightarrow K_S^0 \pi^+ \pi^-$, $D^0 \rightarrow K_S^0 K^+ K^-$ decays

BaBar [PRL105,081803]



68%, 95% and 99.9% confidence level contours



Conserved CP symmetry ($|q/p| = 1$ & $\phi = 0$)

$$x = (0.16 \pm 0.23 \pm 0.14)\%$$

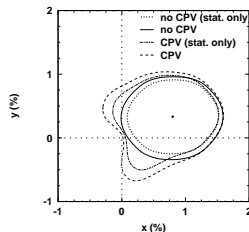
$$y = (0.57 \pm 0.20 \pm 0.15)\%$$

Measurements are consistent and together provide the most accurate determination of x and y !

Belle [PRL99,131803]



95% confidence level contours



Conserved CP symmetry ($|q/p| = 1$ & $\phi = 0$)

$$x = (0.80 \pm 0.29^{+0.13}_{-0.16})\%$$

$$y = (0.33 \pm 0.24^{+0.10}_{-0.14})\%$$

CPV allowed ($|q/p|$ & ϕ free parameters of the fit)

$$|q/p| = 0.86 \pm 0.30 \pm 0.09$$

$$\phi = -0.24 \pm 0.30 \pm 0.09$$

Consistent with no CPV!

Mixing and CPV in WS hadronic decays ($D^0 \rightarrow K^+ \pi^-$)

- Right sign (RS) charge combination

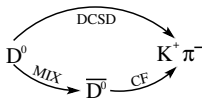
$$D^{*+} \rightarrow D^0(K^- \pi^+) \pi^+$$

$$\Gamma_{RS} \propto e^{-t/\tau_{D^0}}$$

- Wrong sign (WS) charge combination

$$D^{*+} \rightarrow D^0(K^+ \pi^-) \pi^+$$

↪ DCS or mixing



$$\Gamma_{WS} \propto [R_D + y' \sqrt{R_D} (\Gamma t) + \frac{x'^2 + y'^2}{4} (\Gamma t)^2] e^{-\Gamma t}$$

- DCS ● interference ● mixing

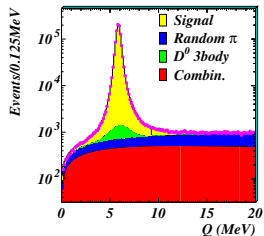
↪ R_D : DCS/CF rate

$$\hookrightarrow \mathbf{x}' = \mathbf{x} \cos \delta + \mathbf{y} \sin \delta$$

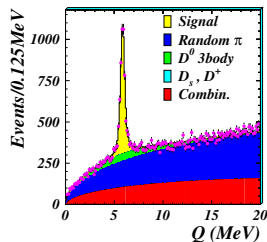
$$\hookrightarrow \mathbf{y}' = \mathbf{y} \cos \delta - \mathbf{x} \sin \delta$$

↪ δ strong phase between DCS and CF

RS events



WS events

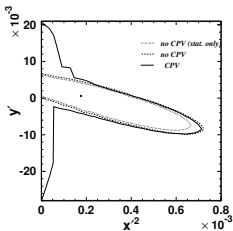
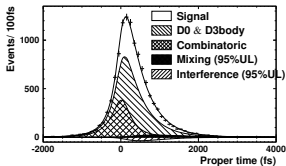


$$Q = M_{K\pi\pi} - M_{K\pi} - m_{\pi}$$

Mixing and CPV in WS hadronic decays $D^0 \rightarrow K^+ \pi^-$

Belle [400 fb⁻¹]

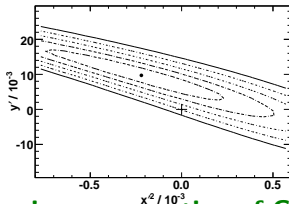
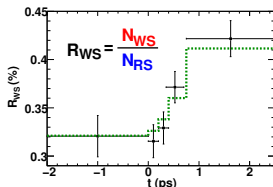
PRL96, 151801 (2006).



BaBar [384 fb⁻¹]

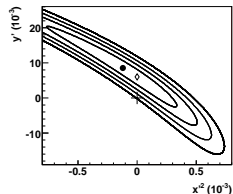
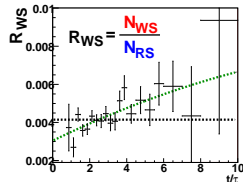
PRL98, 211802 (2007).

First Evidence!



CDF [1.5 fb⁻¹]

PRL100, 121802 (2008).



Results assuming conservation of CP symmetry

Experiment	$R_D (10^{-3})$	$y' (10^{-3})$	$x^2 (10^{-3})$	Signif.
CDF	3.04 ± 0.55	8.5 ± 7.6	-0.12 ± 0.35	3.8
BaBar	3.03 ± 0.19	9.7 ± 5.4	-0.22 ± 0.37	3.9
Belle	3.64 ± 0.17	$0.6^{+4.0}_{-3.9}$	$0.18^{+0.21}_{-0.23}$	2.0

Mixing in WS $D^0 \rightarrow K^+\pi^-\pi^0$ decays (BaBar)

PRL103, 211801

Analysis similar to the WS $D^0 \rightarrow K^+\pi^-$ analysis, however the strong phase δ varies across the Dalitz plot.

● DCS ● interference ● mixing

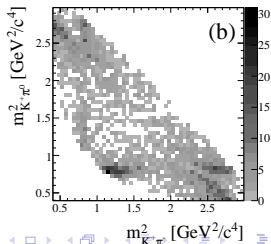
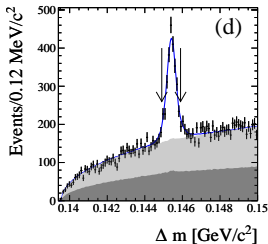
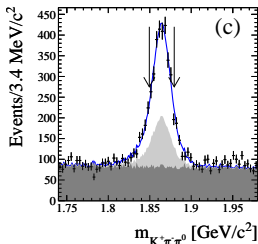
$$\frac{dN_{\bar{f}}(s_0, s_+, t)}{ds_0 ds_+ dt} = e^{-\Gamma t} \left\{ |A_{\bar{f}}|^2 + |A_{\bar{f}}| |\bar{A}_{\bar{f}}| [y'' \cos \delta_{\bar{f}} - x'' \sin \delta_{\bar{f}}] (\Gamma t) + \frac{x''^2 + y''^2}{4} |\bar{A}_{\bar{f}}|^2 (\Gamma t)^2 \right\}$$

$$s_0 = m_{K^+\pi^-}^2; s_+ = m_{K^+\pi^0}^2$$

● Mixing parameters

↪

$$x'' = x \cos \delta_{K\pi\pi^0} + y \sin \delta_{K\pi\pi^0} \quad \text{and} \quad y'' = y \cos \delta_{K\pi\pi^0} - x \sin \delta_{K\pi\pi^0}$$



Mixing in WS $D^0 \rightarrow K^+\pi^-\pi^0$ decays (BaBar)

Assuming no CPV

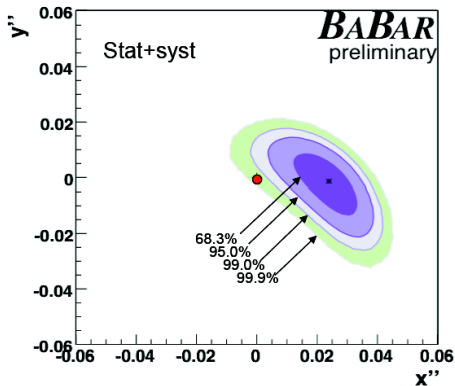
$$\begin{aligned} x'' &= (2.61_{-0.68}^{+0.57} \pm 0.39)\% \\ y'' &= -(0.05_{-0.64}^{+0.55} \pm 0.34)\% \\ R_M &= (2.9 \pm 1.6) \times 10^{-4} \end{aligned}$$

Allowing CPV

$$\begin{aligned} x''^+ &= (2.53_{-0.63}^{+0.54} \pm 0.39)\% \\ y''^+ &= -(0.05_{-0.67}^{+0.63} \pm 0.50)\% \end{aligned}$$

$$\begin{aligned} x''^- &= (3.55_{-0.83}^{+0.73} \pm 0.65)\% \\ y''^- &= -(0.54_{-1.16}^{+0.40} \pm 0.41)\% \end{aligned}$$

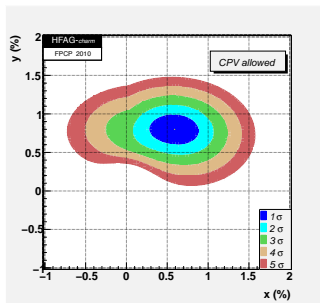
Results consistent with no CPV.



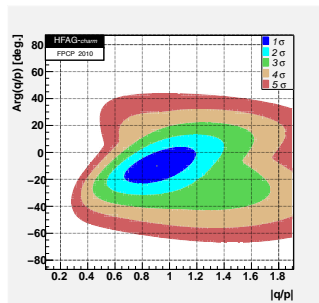
No mixing is excluded at 99% confidence level.

World average of mixing parameters

Heavy Flavor Averaging Group (HFAG) performs an average of 8 underlying physics parameters from currently 30 observables. [www.slac.stanford.edu/xorg/hfag/]



$$x = (0.59 \pm 0.20)\%$$
$$y = (0.80 \pm 0.13)\%$$



$$|q/p| = 0.91^{+0.19}_{-0.16}$$
$$\phi(^{\circ}) = -10.0^{+9.3}_{-8.7}$$

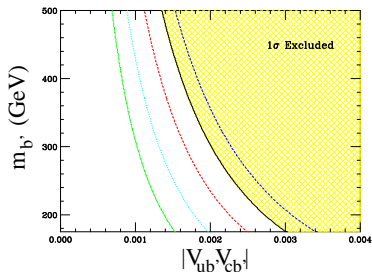
No mixing point $(x, y) = (0, 0)$ is excluded at 10.2σ , while no CP violation point $(|q/p|, \phi) = (1, 0)$ is consistent within 1σ .

Impact – Constraints on new physics models from mixing

E. Golowich *et al.*, PRD76,095009

- Constraints on new physics models from $D^0 - \bar{D}^0$ complementary to those obtained in B and K sector
 \hookrightarrow FCNC transitions with *down-like* quarks in charm sector (unique feature)
- 21 NP models considered \rightarrow 17 with useful constraints

Example: quark b' from 4th generation

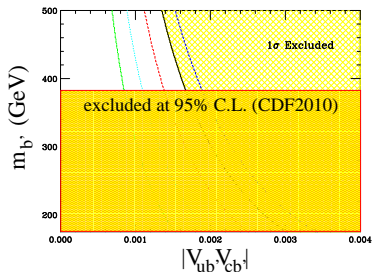


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- 21 NP models considered \rightarrow 17 with useful constraints

Example: quark b' from 4th generation



$|V_{ub'} V_{cb'}| < 0.002$
order of magnitude stronger constraint
as from CKM unitarity

Providing complementary and improved
constraints!

Time-integrated searches of CP Violation

- Searches for direct CP violation performed in total over 30 D^0 , D^+ and D_s^+ decay modes in past 15 years
 - ↪ Belle, BaBar, Cleo, CDF, FOCUS, E796, E687
- No evidence for CP violation found so far
 - ↪ Sensitivity is in some cases reaching 0.2%
- Measurements statistical limited
 - ↪ All measurements can be significantly improved!

$D^0 \rightarrow$	A_{CP} [%]	$D^+ \rightarrow$	A_{CP} [%]	$D_s^+ \rightarrow$	A_{CP} [%]
K^+K^-	-0.16 ± 0.23	$K_S^0\pi^+$	-0.72 ± 0.26	$K_S^0K^+$	-0.28 ± 0.41
$\pi^+\pi^-$	$+0.22 \pm 0.37$	$K_S^0K^+$	-0.09 ± 0.63	$K_S^0\pi^+$	$+6.5 \pm 2.5$
$\pi^+\pi^-\pi^0$	-0.23 ± 0.42	$K^+K^-\pi^+$	$+0.39 \pm 0.61$	$K^+K^-\pi^+$	$+0.3 \pm 1.4$
$K^-\pi^+\pi^0$	$+0.16 \pm 0.89$	$K^-\pi^+\pi^+$	-0.5 ± 1.0	$\pi^+\pi^-\pi^+$	$+2.0 \pm 4.7$
$K_S^0\pi^0$	$+0.10 \pm 1.3$	$K^-\pi^+\pi^+$	-0.5 ± 1.0	$K^+\pi^-\pi^+$	$+11.2 \pm 7.1$
$K^+K^-\pi^0$	$+1.00 \pm 1.7$	$K_S^0\pi^+\pi^0$	$+0.3 \pm 0.9$	$\pi^+\eta$	-8.2 ± 5.3
$\pi^0\pi^0$	$+0.10 \pm 4.8$	$\pi^+\pi^-\pi^+$	-1.7 ± 4.2	$\pi^+\eta'$	-5.5 ± 3.9
⋮	⋮	⋮	⋮	⋮	⋮

Full list of all CPV measurements is available at:
<http://www.slac.stanford.edu/xorg/hfag/charm/index.html>

Time-integrated searches of CP Violation

Key is to distinguish possible CPV asymmetry from detector effects and production asymmetry in reconstructed asymmetry

$$A^{\text{reco}} = \frac{N_D^{\text{reco}} - N_{\bar{D}}^{\text{reco}}}{N_D^{\text{reco}} + N_{\bar{D}}^{\text{reco}}}$$

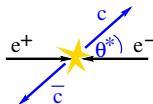
$$N_D^{\text{reco}} = N_D^{\text{prod}} \cdot \mathcal{B}(D \rightarrow f) \cdot \epsilon_f \implies \text{if } A_i \ll 1 \implies A^{\text{reco}} = A_{\text{FB}}^D + A_{\text{CP}}^f + A_{\epsilon}^f$$

A_{CP}
CP asymmetry

independent of any kinematic variable

A_{FB}
Production asymmetry

due to γ/Z interference in $e^+e^- \rightarrow C\bar{C}$ (only at e^+e^- coll.)



(anti-symmetric in $\cos\theta_D^*$)

A_{ϵ}^f
Reconstruction asymmetry

h^\pm reconstruction efficiency asymmetry

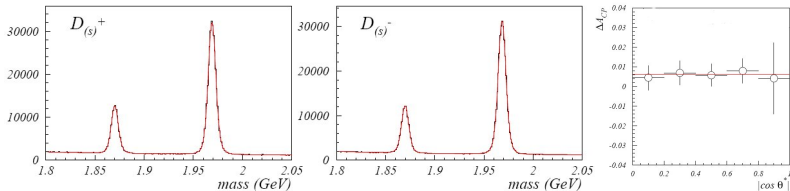


(p^{lab} , $\cos\theta^{\text{lab}}$)

In order to control systematics A_i 's are estimated on real data sample!

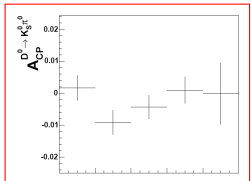
ΔA_{CP} between $D^+ \rightarrow \phi\pi^+$ and $D_s^+ \rightarrow \phi\pi^+$ and A_{CP} in $D^0 \rightarrow K_S^0 P^0$ (Belle preliminary)

- ΔA_{CP} between $D^+ \rightarrow \phi\pi^+$ and $D_s^+ \rightarrow \phi\pi^+$

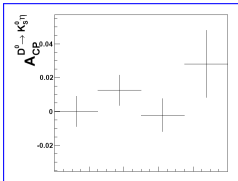


$$\Delta A_{CP} = (+0.62 \pm 0.30 \pm 0.15)\%$$

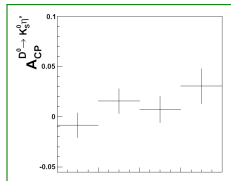
- A_{CP} in $D^0 \rightarrow K_S^0 \pi^0$, $D^0 \rightarrow K_S^0 \eta$ (★) and $D^0 \rightarrow K_S^0 \eta'$ (★) ★ – first measurement



$$A_{CP} = (-0.28 \pm 0.19 \pm 0.10)\%$$



$$(+0.54 \pm 0.51 \pm 0.13)\%$$



$$(+0.90 \pm 0.67 \pm 0.15)\%$$

Search for CP Violation with T -odd correlations

Assuming CPT invariance: T violation $\Rightarrow CP$ violation

- Possible only in ≥ 4 -body decay

$$\hookrightarrow D^0 \rightarrow K^- K^+ \pi^- \pi^+$$

- T -odd quantity:

$$C_T \equiv \langle \vec{p}_{K^+} \cdot (\vec{p}_{\pi^+} \times \vec{p}_{\pi^-}) \rangle$$

- T violating asymmetry A_T

$$D^0: A_T = \frac{\Gamma(C_T > 0) - \Gamma(C_T < 0)}{\Gamma(C_T > 0) + \Gamma(C_T < 0)}$$

$$\bar{D}^0: \bar{A}_T = \frac{\Gamma(-\bar{C}_T > 0) - \Gamma(-\bar{C}_T < 0)}{\Gamma(-\bar{C}_T > 0) + \Gamma(-\bar{C}_T < 0)}$$

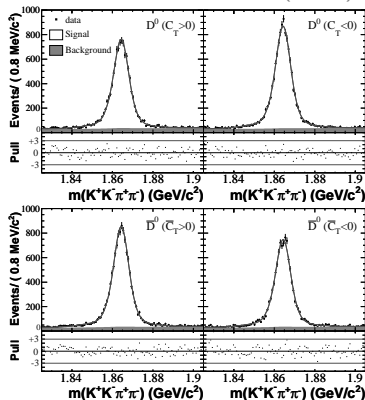
$$A_T = \frac{1}{2} (A_T - \bar{A}_T)$$

Bigi, hep-ph/0107102 (2001)

Bensalem et al., PRD66, 094004 (2002)

A_T can be different from zero due to final state interactions, but $A_T \neq 0$ represents CP violation.

BaBar PRD81, 111103 (2010)



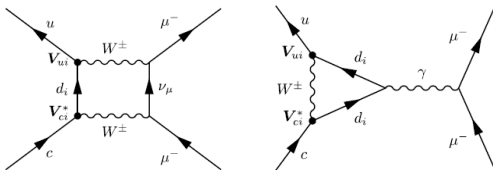
$$A_T = (-68.5 \pm 7.3 \pm 4.5) \times 10^{-3}$$

$$\bar{A}_T = (-70.5 \pm 7.3 \pm 3.9) \times 10^{-3}$$

$$A_T = (1.0 \pm 5.1 \pm 4.4) \times 10^{-3}$$

Charm rare decays: $D^0 \rightarrow \ell^+ \ell^-$ (Motivation)

- **Standard Model:**



↔ Flavor Changing Neutral Current decays ($D^0 \rightarrow \ell^+ \ell^-$) are highly suppressed

↔ with long distance contributions $\mathcal{B} \sim 10^{-13}$

↔ Lepton Flavor Violating decays ($D^0 \rightarrow e^\pm \mu^\mp$) are forbidden

- **New Physics:**

↔ Flavor Changing Neutral Current transitions may be enhanced by many orders of magnitude

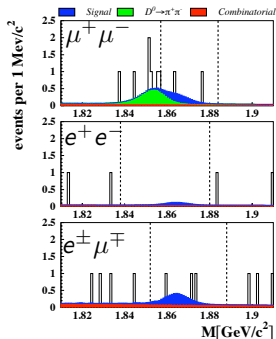
↔ R-parity violating SUSY: $\mathcal{B}(\mu^+ \mu^-)$ up to 10^{-8}

↔ Leptoquarks: $\mathcal{B}(\mu^+ \mu^-) \sim 8 \cdot 10^{-8}$

Golowich et. al., PRD79 114030 (2009); Dorsner et. al. PLB682 67 (2009)

Search for $D^0 \rightarrow \ell^+ \ell^-$ at Belle and CDF

Belle [PRD81 091102 (2010)]

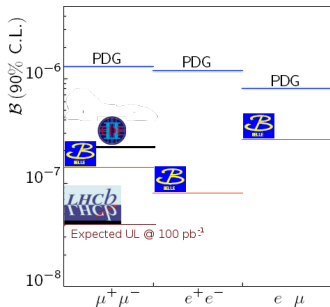


CDF [arXiv:1008.5077]

↪ used less than 10% of available sample

$D^0 \rightarrow \pi^+ \pi^-$ used as normalization channel:

$$\mathcal{B}(D^0 \rightarrow \ell^+ \ell^-) = \frac{N_{\ell\ell}}{N_{\pi\pi}} \frac{\epsilon_{\pi\pi}}{\epsilon_{\ell\ell}} \mathcal{B}(D^0 \rightarrow \pi^+ \pi^-)$$



Channel	$N_{\ell\ell}$	N_{bkg}	90% C.L. UL
$\mathcal{B} e^+ e^-$	0	1.7 ± 0.2	7.9×10^{-8}
$\mathcal{B} e^\pm \mu^\mp$	3	2.6 ± 0.2	2.6×10^{-7}
$\mathcal{B} \mu^+ \mu^-$	2	3.1 ± 0.1	1.4×10^{-7}
$\mathcal{B} \mu^+ \mu^-$	4	9 ± 2	2.1×10^{-7}

UL in $D^0 \rightarrow \ell^+ \ell^-$ disfavors leptoquark contribution as explanation of f_D anomaly.



Conclusions

- Collective evidence for $D^0 - \bar{D}^0$ mixing are compelling
 - No single measurement exceeds 5σ
 - The no-mixing point is excluded at around 10σ
 - The WA of x and y seem consistent with SM expectations
 - Providing strong constraints for some New Physics models
- No evidence of CP violation (at the level of 0.3%)
- Still room for improvements using existing data sets
 - exploiting the entire data sets and covering all the sensitive measurements (Belle, BaBar, CDF)
- Is the best yet to come?



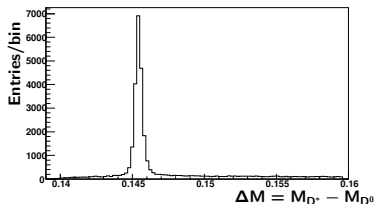
Backup slides

Common steps in $D^0 - \bar{D}^0$ mixing and CPV measurements

- 1 Tag the flavor of the produced neutral D meson
- 2 Measure proper decay time

Flavor tagging

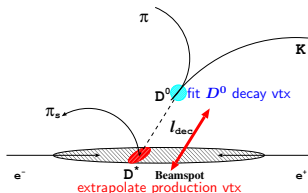
- require $D^{*+} \rightarrow D^0 \pi^+$
 - ↪ flavor tagging with π 's charge
 - ↪ background suppression with $\Delta M = M_{D^{*+}} - M_{D^0}$



eliminate D^0 s from $b \rightarrow c$ with $p_{\text{CMS}}^{D^{*+}} > 2.5 \text{ GeV}/c^2$ (B-fact.) or use impact parameter (hadron col.)

Proper decay time

- Vertexing with beam point constraint



$$t = \frac{l_{\text{dec}}}{c\beta\gamma}, \quad \beta\gamma = \frac{p_{D^0}}{M_{D^0}}$$

σ_t uncertainty of the measurement typically between $1/6\tau_{D^0}$ and $1/2\tau_{D^0}$

Mixing probability

- probability to observe an initial M^0 as M^0 or \bar{M}^0 after time t

$$\mathcal{P}_{\text{non-mix}}(t) = |\langle M^0(t) | M^0 \rangle|^2 = \frac{1}{2} e^{-\Gamma t} [\cosh(y\Gamma t) + \cos(x\Gamma t)]$$

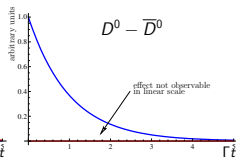
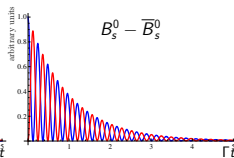
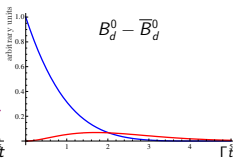
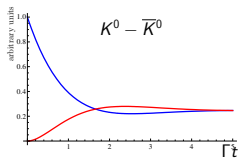
$$\mathcal{P}_{\text{mix}}(t) = |\langle M^0(t) | \bar{M}^0 \rangle|^2 = \frac{1}{2} e^{-\Gamma t} [\cosh(y\Gamma t) - \cos(x\Gamma t)]$$

- time integrated mixing rate

$$R_M = \frac{\int_0^\infty \mathcal{P}_{\text{mix}}(t) dt}{\int_0^\infty \mathcal{P}_{\text{non-mix}}(t) dt} = \frac{x^2 + y^2}{2 + x^2 - y^2}$$

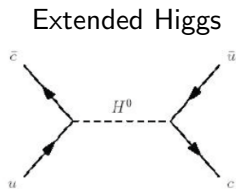
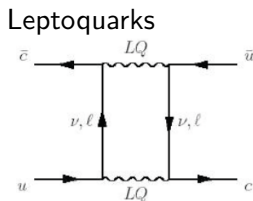
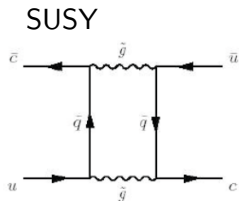
M^0	x	y	R_M
K^0	0.946	0.997	0.994
B_d^0	0.776	< 0.01	0.23
B_s^0	26.1	0.15	0.997
D^0	0.01	0.01	10^{-4}

1 out of 10^4 D^0 mesons oscillates before it decays



Large sample of D^0 mesons needed to observe $D^0 - \bar{D}^0$ mixing

New Physics in Charm Mixing

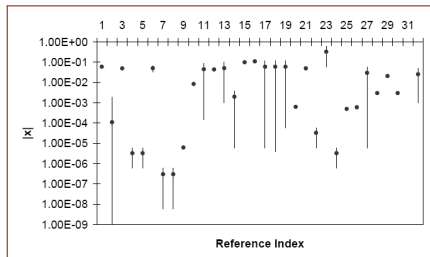
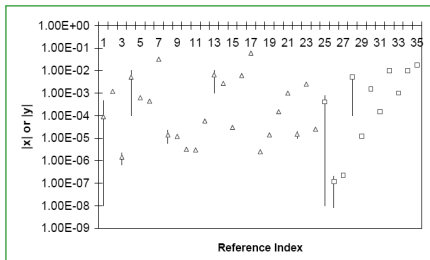


- Possible New Physics contributions can increase x , while y is mostly unaffected

$\hookrightarrow |x| \gg |y|$ would be a hint of New Physics

Compilation of predictions for x and y

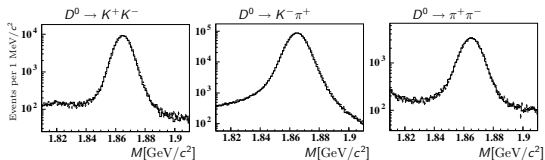
Compilation of SM predictions for $|x|$ (\triangle) and $|y|$ (\square)
and New Physics predictions for $|x|$ (\bullet)



A. Petrov, Int.J.Mod.Phys.A21, 5686;

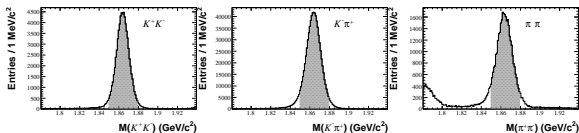
Mixing and CPV in $D^0 \rightarrow K^+K^-$, $\pi^+\pi^-$ decays

- Belle tagged analysis (540 fb^{-1}): PRL98, 211803 (2007)



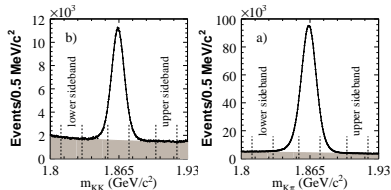
$D^0 \rightarrow$	Sig. yield	Purity
$K^- \pi^+$	1.22M	99%
$K^+ K^-$	111k	98%
$\pi^+ \pi^-$	49k	92%

- BaBar tagged analysis (384 fb^{-1}): PRD78, 011105 (2008)



$D^0 \rightarrow$	Sig. yield	Purity
$K^- \pi^+$	731k	99.9%
$K^+ K^-$	70k	99.6%
$\pi^+ \pi^-$	31k	98%

- BaBar untagged analysis (384 fb^{-1}): arXiv:0908.0761



$D^0 \rightarrow$	Sig. yield	Purity
$K^- \pi^+$	2.71M	94.2%
$K^+ K^-$	264k	80.9%

4x the size of the tagged sample and independent

Mixing in $D^0 \rightarrow K_S^0 K^+ K^-$ decays (Belle)

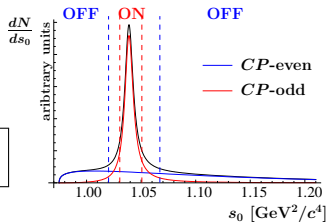
arXiv:0905.4185 (PRD accepted) [673 fb⁻¹]

Measurement of lifetime difference between CP -even and CP -odd eigenstates

- $\sqrt{s_0} = m_{K^+ K^-}$ dependent CP mixture
 - ↪ **ON** region: mainly CP -odd ($\phi(1020)K_S^0$)
 - ↪ **OFF** region: mainly CP -even ($a_0(980)^0 K_S^0$)

$$\frac{d^2 N(s_0, t)}{ds_0 dt} \propto a_1(s_0) e^{-(1+y_{CP})t/\tau_{D^0}} + a_2(s_0) e^{-(1-y_{CP})t/\tau_{D^0}}$$

$$a_{1,2}(s_0) = \int |\mathcal{A}_{1,2}(s_0, s_+)|^2 ds_+; \sqrt{s_+} = m_{K_S^0 K^+}; \mathcal{A}_{1,2} = \frac{1}{2}(\mathcal{A} \pm \bar{\mathcal{A}})$$



- Effective lifetimes in **ON** and **OFF** regions

$$\tau_{\text{ON,OFF}} = [1 + (1 - 2f_{\text{ON,OFF}})y_{CP}] \tau_{D^0} \Rightarrow y_{CP} = \frac{1}{f_{\text{ON}} - f_{\text{OFF}}} \left(\frac{\tau_{\text{OFF}} - \tau_{\text{ON}}}{\tau_{\text{OFF}} + \tau_{\text{ON}}} \right)$$

↪ $f_{\text{ON}}, f_{\text{OFF}}$ are CP -even fractions in **ON** and **OFF** regions, determined using 8-resonant Dalitz model (REF!!!)

$$y_{CP} = +(0.11 \pm 0.61(\text{stat.}) \pm 0.52(\text{syst.}))\%$$

Mixing parameters in $D^0 \rightarrow K_S^0 K^+ K^-$ and $D^0 \rightarrow K_S^0 \pi^+ \pi^-$

TABLE I: Results from the mixing fits. The first uncertainty is statistical, the second systematic and the third systematic from the amplitude model. For the nominal fit, the corresponding correlation coefficients between x and y are 3.5%, 16.0% and -2.7% , respectively.

Fit type	$x/10^{-3}$	$y/10^{-3}$
Nominal	$1.6 \pm 2.3 \pm 1.2 \pm 0.8$	$5.7 \pm 2.0 \pm 1.3 \pm 0.7$
$K_S^0 \pi^+ \pi^-$	2.6 ± 2.4	6.0 ± 2.1
$K_S^0 K^+ K^-$	-13.6 ± 9.2	4.4 ± 5.7
D^0	0.0 ± 3.3	5.5 ± 2.8
\bar{D}^0	3.3 ± 3.3	5.9 ± 2.8

Mixing in semileptonic decays $D^0 \rightarrow K^{(*)-} \ell^+ \nu_\ell$

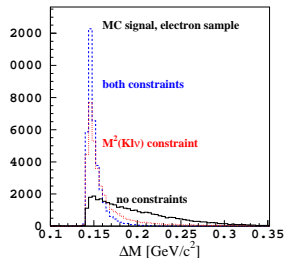
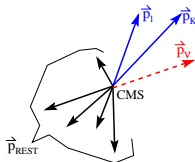
U. Bitenc *et al.* [Belle Collaboration], PRD77, 112003 (2008). [$\mathcal{L} = 492 \text{ fb}^{-1}$]

- Wrong sign (WS) charge combination accessible only via mixing

	Flavor at production		Flavor at decay	
without mixing	$D^{*+} \rightarrow D^0 \pi^+$		$D^0 \rightarrow K^- \ell^+ \nu_\ell$	RS
with mixing	$D^{*+} \rightarrow D^0 \pi^+$	$D^0 - \bar{D}^0$	$\bar{D}^0 \rightarrow K^+ \ell^- \nu_\ell$	WS

Neutrino reconstruction:

- $P_\nu = P_{\text{CMS}} - P_{K\ell} - P_{\text{rest}}$
- $M_{K\ell\nu}^2 = m_{D^0}^2 \text{ \& } (P_\nu^*)^2 = 0$

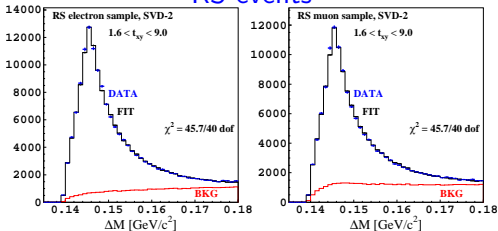


Time integrated mixing rate:

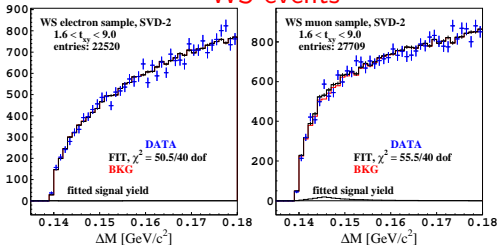
$$R_M \simeq \frac{x^2 + y^2}{2} = \frac{N_{\text{WS}}}{N_{\text{RS}}}$$

Mixing in semileptonic decays $D^0 \rightarrow K^{(*)-} \ell^+ \nu_\ell$

RS events



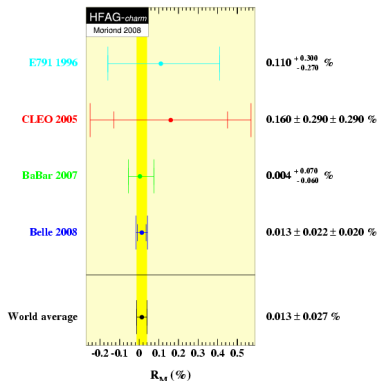
WS events



No WS charge combinations observed.

$$R_M = (1.3 \pm 2.2 \pm 2.0) \times 10^{-4}$$

$$R_M < 6.1 \times 10^{-4} @ 90\% \text{ C.L.}$$



<http://www.slac.stanford.edu/xorg/hfag/>

Future Prospects

TABLE V: Expected precision (σ) on the measured quantities using methods described in the text for SuperB with an integrated luminosity of 75 ab^{-1} at SuperB at 10 GeV, 300 fb^{-1} (\sim two months) running at charm threshold with SuperB, and LHCb with 10 fb^{-1} [13].

Mode	Observable	$\Upsilon(4S)$ (75 ab^{-1})	$\psi(3770)$ (300 fb^{-1})	LHCb (10 fb^{-1})
$D^0 \rightarrow K^+ \pi^-$	x'^2	3×10^{-5}		6×10^{-5}
	y'	7×10^{-4}		9×10^{-4}
$D^0 \rightarrow K^+ K^-$	y_{CP}	5×10^{-4}		5×10^{-4}
$D^0 \rightarrow K_S^0 \pi^+ \pi^-$	x	4.9×10^{-4}		
	y	3.5×10^{-4}		
	$ q/p $	3×10^{-2}		
	ϕ	2°		
$\psi(3770) \rightarrow D^0 \bar{D}^0$	x^2		$(1-2) \times 10^{-5}$	
	y		$(1-2) \times 10^{-3}$	
	$\cos \delta$		$(0.01-0.02)$	

arXiv:0810.1312

Table 5.23: Expected number of reconstructed $D^{*+} \rightarrow D^0 \pi^+$, $D^0 \rightarrow K^- \pi^+$ decays at different facilities (projected using [292], [293], [294], [295]). [†]For charm factory the expected yield of $\Psi(3770) \rightarrow D^0 \bar{D}^0$, $D^0 \rightarrow K^- \pi^+$, $\bar{D}^0 \rightarrow K^+ \pi^-$ is quoted.

Facility	num. of $D^{*+} \rightarrow D^0 \pi^+$, $D^0 \rightarrow K^- \pi^+$	int. luminosity [fb^{-1}]	Comment
existing B factories	2.5×10^6	1000	final data set
Super-KEKB	14×10^6	5000	purity $\sim 99\%$
Charm factory [†]	4×10^4	20	both D^0 's reconstructed; $D^0 \bar{D}^0$ in coherent state
Tevatron	0.5×10^6	0.35	
LHCb	15×10^6	2	

<http://belle2.kek.jp/physics.html>

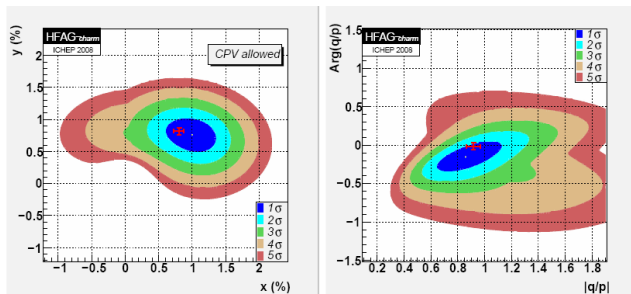


Figure 5.67: Left: The probability contours for the current world average values of the mixing parameters x and y [338]. The error bars denote the expected accuracy on the parameters with 50 ab^{-1} following from the extrapolation of results using K^+K^- , $\pi^+\pi^-$, $K^+\pi^-$ and $K_S\pi^+\pi^-$ final states. Right: The probability contours for the current world average values of the CPV parameters $|q/p|$ and ϕ [338]. The error bars denote the expected accuracy with the same assumptions as above.

<http://belle2.kek.jp/physics.html>

World average

$$R_M = \frac{1}{2}(x^2 + y^2)$$

$$2y_{CP} = (|q/p| + |p/q|)y \cos \phi - (|q/p| - |p/q|)x \sin \phi$$

$$2A_\Gamma = (|q/p| - |p/q|)y \cos \phi - (|q/p| + |p/q|)x \sin \phi$$

$$\begin{aligned} x_{K^0\pi\pi} &= x \\ y_{K^0\pi\pi} &= y \\ |q/p|_{K^0\pi\pi} &= |q/p| \\ \text{Arg}(q/p)_{K^0\pi\pi} &= \phi \end{aligned}$$

$$\begin{pmatrix} x'' \\ y'' \end{pmatrix}_{K^+\pi^-} = \begin{pmatrix} \cos \delta_{K\pi\pi} & \sin \delta_{K\pi\pi} \\ -\sin \delta_{K\pi\pi} & \cos \delta_{K\pi\pi} \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

$$\begin{pmatrix} x' \\ y' \end{pmatrix} = \begin{pmatrix} \cos \delta & \sin \delta \\ -\sin \delta & \cos \delta \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix}$$

$$A_M = \frac{|q/p|^2 - |p/q|^2}{|q/p|^2 + |p/q|^2}$$

$$x'^{\pm} = \left(\frac{1 \pm A_M}{1 \mp A_M} \right)^{1/4} (x' \cos \phi \pm y' \sin \phi)$$

$$y'^{\pm} = \left(\frac{1 \pm A_M}{1 \mp A_M} \right)^{1/4} (y' \cos \phi \mp x' \sin \phi)$$

$$\frac{1}{2} [R(D^0 \rightarrow K^+\pi^-) + \overline{R}(\overline{D}^0 \rightarrow K^-\pi^+)] = R_D$$

$$\frac{R(D^0 \rightarrow K^+\pi^-) - \overline{R}(\overline{D}^0 \rightarrow K^-\pi^+)}{R(D^0 \rightarrow K^+\pi^-) + \overline{R}(\overline{D}^0 \rightarrow K^-\pi^+)} = A_D$$

HFAG: arXiv:0808.1297 or

<http://www.slac.stanford.edu/xorg/hfag/>

χ^2 fit of **8 underlying parameters** using all measured quantities (**30 observables**) including correlations between them

Parameter	Value
x	$(0.59 \pm 20)\%$
y	$(0.80 \pm 0.13)\%$
δ	$(27.8^{+11.2}_{-13.2})^\circ$
$\delta_{K\pi\pi}$	$(23.2^{+22.3}_{-23.3})^\circ$
R_D	$(0.3319 \pm 0.0081)\%$
A_D	$(-2.0 \pm 2.4)\%$
$ q/p $	$0.91^{+0.19}_{-0.16}$
ϕ	$(-10.0^{+9.3}_{-8.7})^\circ$

$(x, y) = (0, 0)$ excluded at 10.2σ

No CPV within 1σ

Number of reconstructed decays:

$$N^{reco} = N_{D^{*+}}^{prod} \cdot \mathcal{B}(D^{*+} \rightarrow D^0 \pi^+) \cdot \mathcal{B}(D^0 \rightarrow h^+ h^-) \cdot \epsilon_{hh} \cdot \epsilon_{\pi}$$

- Contributions to asymmetry in N^{reco} :
 - production (A_{FB})
 - branching fractions (A_{CP})
 - efficiencies (A_{ϵ})
- If asymmetries are small ($A_{FB}, A_{CP}, A_{\epsilon} \ll 1$) it is easy to see, that the asymmetry in N^{reco} is:

$$A^{reco} = A_{FB}^{D^{*+}} + A_{CP}^{D^0 \pi} + A_{CP}^{hh} + A_{\epsilon}^{hh} + A_{\epsilon}^{\pi}$$

- Some are zero: $A_{CP}^{D^0 \pi} = 0$ (strong decay), $A_{\epsilon}^{hh} = 0$ (same final state)

- Production asymmetry (A_{FB}) is due to interference in $e^+e^- \rightarrow c\bar{c}$ (mediated by virtual γ or Z^0)
 - anti-symmetric function of $\cos\theta^*$ (follows from CP conservation)

$$A_{FB}(\cos\theta^*) = -A_{FB}(-\cos\theta^*)$$

- Measured asymmetry:

$$A^{reco} = A_{FB}^{D^{*+}}(\cos\theta^*) + A_{CP}^{hh} + A_{\epsilon}^{\pi}(\theta, p)$$

- Asymmetry in π_{slow} efficiency $A_{\epsilon}^{\pi}(\theta, p)$ can be measured in $D^0 \rightarrow K^-\pi^+$ by using tagged and untagged decays
- Corrected asymmetry

$$A_{corr}^{reco} = A^{reco} - A_{\epsilon}^{\pi}(\theta, p)$$

$$A_{corr}^{reco}(\cos\theta^*) = A_{FB}^{D^{*+}}(\cos\theta^*) + A_{CP}^{KK}$$

Number of reconstructed tagged and untagged $D^0 \rightarrow K^- \pi^+$ decays:

$$N^{\text{untag}} = N_{D^0}^{\text{prod}} \cdot \mathcal{B}(D^0 \rightarrow K^- \pi^+) \cdot \epsilon_{K\pi}$$

$$N^{\text{tag}} = N_{D^{*+}}^{\text{prod}} \cdot \mathcal{B}(D^{*+} \rightarrow D^0 \pi_S^+) \cdot \mathcal{B}(D^0 \rightarrow K^- \pi^+) \cdot \epsilon_{K\pi} \cdot \epsilon_{\pi}$$

Measured asymmetry:

$$A^{\text{untag}} = A_{FB}^{D^0} + A_{CP}^{K\pi} + A_{\epsilon}^{K\pi}$$

$$A^{\text{tag}} = A_{FB}^{D^0} + A_{CP}^{K\pi} + A_{\epsilon}^{K\pi} + A_{\epsilon}^{\pi}$$

Assuming $A_{FB}^{D^0} = A_{FB}^{D^{*+}}$:

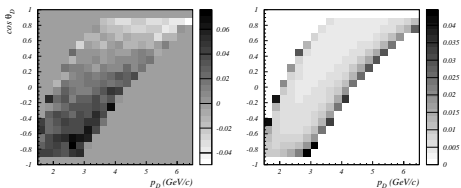
$$A_{\epsilon}^{\pi} = A^{\text{tag}} - A^{\text{untag}}$$

$A_{\epsilon}^{K\pi}$ and A_{ϵ}^{π} are functions of corresponding phase spaces.

CPV in $D^0 \rightarrow K^- K^+, \pi^- \pi^+$ decays backup (time-integrated)

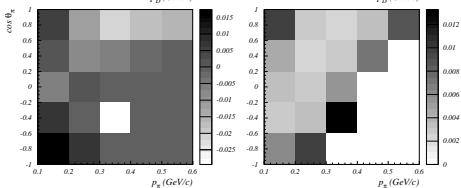
Determination of soft pion π_s asymmetry:

- using tagged and untagged $D^0 \rightarrow K^- \pi^+$ decays



\Rightarrow asymmetry map of the untagged $K\pi$ sample (left)
with uncertainty (right)

\hookrightarrow weight D^0 candidates in the π_s tagged $K\pi$ sample

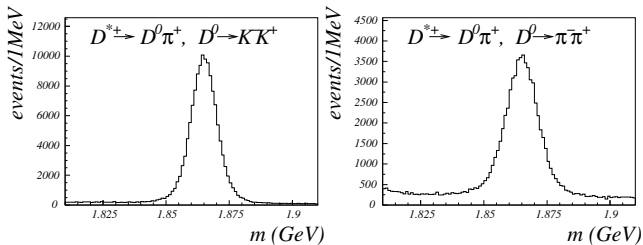


\Rightarrow asymmetry map of the slow pion efficiency (left)
with uncertainty (right)

\hookrightarrow weight D^0 yields to correct for tagging asymmetry

Averaging over the phase space the correction due to the π_s efficiency is found to be $(0.76 \pm 0.09\%)$.

CPV in $D^0 \rightarrow K^-K^+, \pi^-\pi^+$ decays backup (time-integrated)



The signal counting was performed by the mass-sideband subtraction.

Systematics:

Signal counting

	KK	$\pi\pi$
Signal shape diff.	0.02%	0.04%
Sideband position	0.01%	0.03%
Random π_{slow} bkg.	0.03%	0.03%
Total	0.04%	0.06%

π_S eff. correction

	KK	$\pi\pi$
Statistics of $K\pi$	0.09%	0.09%
Binning	0.03%	0.02%
Min. num. events/bin	0.04%	0.03%
Total	0.10%	0.10%

A_{CP} extraction

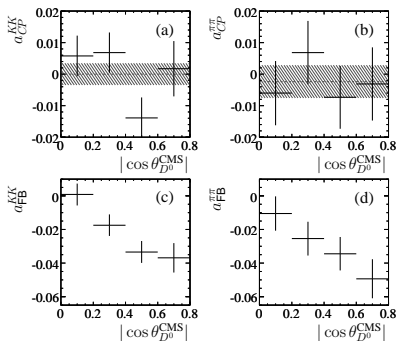
	KK	$\pi\pi$
Binning	0.03%	0.03%
SVD1/2	0.03%	0.00%
Total	0.04%	0.03%

Time integrated CPV in $D^0 \rightarrow K^+K^-, \pi^+\pi^-$ decays

$$A_{\text{corr}}^{\text{reco}}(\cos\theta^*) = \frac{N(D^0) - N(\bar{D}^0)}{N(D^0) + N(\bar{D}^0)}$$

$$= A_{FB}^{D^{*+}} + A_{CP}^{hh}$$

BaBar



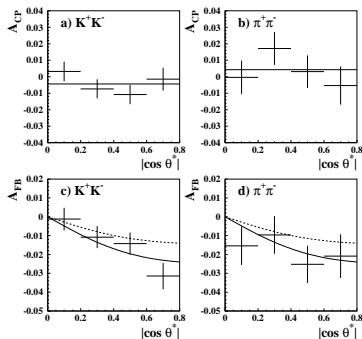
PRL100, 061803

$$A_{CP}^{KK} = (0.00 \pm 0.34(\text{stat}) \pm 0.13(\text{syst}))\%$$

$$A_{CP}^{\pi\pi} = (-0.24 \pm 0.52(\text{stat}) \pm 0.22(\text{syst}))\%$$

- $A_{CP} = \frac{A_{\text{corr}}^{\text{reco}}(\cos\theta^*) + A_{\text{corr}}^{\text{reco}}(-\cos\theta^*)}{2}$
- $A_{FB} = \frac{A_{\text{corr}}^{\text{reco}}(\cos\theta^*) - A_{\text{corr}}^{\text{reco}}(-\cos\theta^*)}{2}$

Belle



PLB670, 190

$$A_{CP}^{KK} = (-0.41 \pm 0.30(\text{stat}) \pm 0.11(\text{syst}))\%$$

$$A_{CP}^{\pi\pi} = (+0.41 \pm 0.52(\text{stat}) \pm 0.12(\text{syst}))\%$$

What is so special about $D_{(s)}^+ \rightarrow K_S h^+$ decays?

- $D^+ \rightarrow K_S \pi^+$ appears to be a CF mode, however the same final state can be reached through a DCS amplitude

$$\hookrightarrow D^+ \rightarrow \bar{K}^0 \pi^+ / K^0 \pi^+ \rightarrow K_S \pi^+$$

★ two interfering amplitudes generate asymmetry $\sim \mathcal{O}(10^{-4})$

- The CP impurity in the K_S wave function induces larger asymmetry

$$\star A_{CP}(D^+ \rightarrow K_S \pi^+) \simeq \frac{|q_K|^2 - |p_K|^2}{|q_K|^2 + |p_K|^2} \simeq -(0.332 \pm 0.006)\%$$

$D_{(s)}^+ \rightarrow K_S \pi^+$ channels

Use $D_s^+ \rightarrow \phi \pi^+$ decays to correct for:

- production asymmetry A_{FB}
- reconstruction asymmetry $A_\epsilon^{\pi^+}$
- no asymmetry due to $\phi \rightarrow K^+ K^-$ reconstruction

Method

In each $(p_\pi^{\text{lab}}, \cos\theta_\pi^{\text{lab}}, \cos\theta_D^*)$ bin

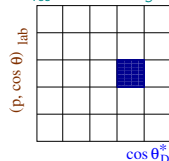
① Measure $A_{rec}^{D_{(s)}^+ \rightarrow K_S \pi^+} = A_{FB}^{D_{(s)}} + A_\epsilon^{\pi^+} + A_{CP}^{D_{(s)}^+ \rightarrow K_S^0 \pi^+}$

② Measure $A_{rec}^{D_s^+ \rightarrow \phi \pi^+} = A_{FB}^{D_s} + A_\epsilon^{\pi^+}$

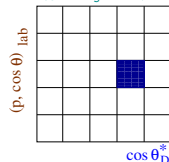
③ Subtract measured asymmetries

$$A_{CP}^{D^+ \rightarrow K_S \pi^+} = A_{rec}^{D^+ \rightarrow K_S \pi^+} - A_{rec}^{D_s^+ \rightarrow \phi \pi^+}$$

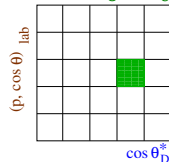
1. A_{rec} in $D^+ \rightarrow K_S \pi^+$



2. A_{rec} in $D_s^+ \rightarrow \phi \pi^+$

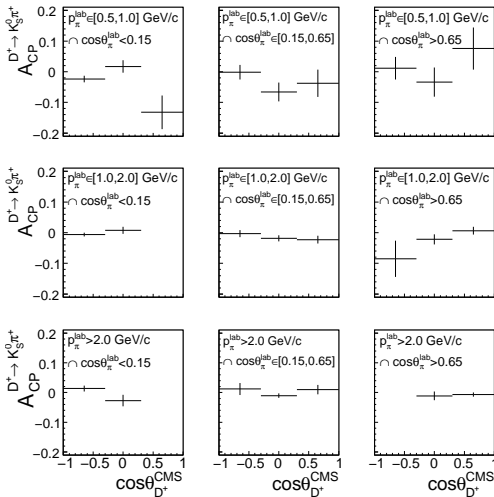


3. Subtraction gives A_{CP}



$D_{(s)}^+ \rightarrow K_S \pi^+$ channels

Measured $A_{CP}^{D^+ \rightarrow K_S \pi^+}$ in bins of $(p_{\pi}^{\text{lab}}, \cos\theta_{\pi}^{\text{lab}}, \cos\theta_{D^+}^{\text{CMS}})$



$$A_{CP}^{D^+ \rightarrow K_S \pi^+} = -(0.71 \pm 0.26)\%$$

$$A_{CP}^{D_s^+ \rightarrow K_S \pi^+} = (5.45 \pm 2.50)\%$$

$D_{(s)}^+ \rightarrow K_S K^+$ channels

Use $D_s^+ \rightarrow \phi\pi^+$ and $D^0 \rightarrow K^-\pi^+$ decays to correct for:

- production asymmetry A_{FB}
- reconstruction asymmetry $A_\epsilon^{K^+}$

Method

In each $(p_\pi^{\text{lab}}, \cos\theta_\pi^{\text{lab}}, \cos\theta_D^*)$ bin

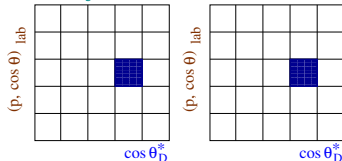
- 1 Measure $A_{rec}^{D_s^+ \rightarrow \phi\pi^+} = A_{FB}^{D_s} + A_\epsilon^\pi$
- 2 Measure $A_{rec}^{D^0 \rightarrow K^-\pi^+} = A_{FB}^{D^0} + A_\epsilon^\pi + A_\epsilon^{K^+}$

In each $(p_K^{\text{lab}}, \cos\theta_K^{\text{lab}})$ bin

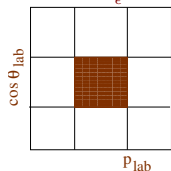
- 1 Obtain $A_\epsilon^{K^+} = A_{rec}^{D^0 \rightarrow K^-\pi^+} - A_{rec}^{D_s^+ \rightarrow \phi\pi^+}$
- 2 Measure $A_{rec}^{D_{(s)}^+ \rightarrow K_S K^+} = A_{FB}^{D_{(s)}} + A_\epsilon^{K^+} + A_{CP}^{D_{(s)} \rightarrow K_S^0 K^+}$
- 3 Obtain

$$A_{K_{corr.}}^{D^+ \rightarrow K_S \pi^+} = A_{rec}^{D^+ \rightarrow K_S \pi^+} - A_{\pi_{corr.}}^{D^0 \rightarrow K^-\pi^+} = A_{CP}^{D^+ \rightarrow K_S \pi^+} + A_{FB}^{D_{(s)}}$$

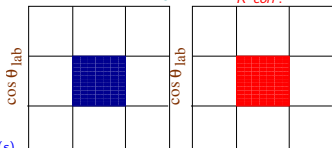
1. A_{rec} in $D_s^+ \rightarrow \phi\pi^+$
2. A_{rec} in $D^0 \rightarrow K^-\pi^+$



3. Fill $A_\epsilon^{K^+}$



4. A_{rec} in $D^+ \rightarrow K_S K^+$
5. $A_{K_{corr.}}^{D^+ \rightarrow K_S \pi^+}$

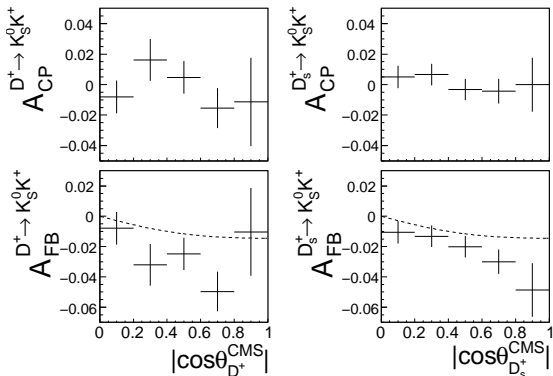


$D_{(s)}^+ \rightarrow K_S K^+$ channels

Using (anti-)symmetric properties of A_{CP} (A_{FB}) in $\cos\theta_D^{\text{CMS}}$

$$A_{CP}^D = \frac{1}{2} [A_{K \text{ corr}}^D(\cos\theta_D^{\text{CMS}}) + A_{K \text{ corr}}^D(-\cos\theta_D^{\text{CMS}})]$$

$$A_{FB}^D = \frac{1}{2} [A_{\pi \text{ corr}}^D(\cos\theta_D^{\text{CMS}}) - A_{\pi \text{ corr}}^D(-\cos\theta_D^{\text{CMS}})]$$



$$A_{CP}^{D^+ \rightarrow K_S K^+} = -(0.16 \pm 0.58)\%$$
$$A_{CP}^{D_s^+ \rightarrow K_S K^+} = (0.12 \pm 0.36)\%$$

Source		$D^+ \rightarrow K_S \pi^+$	$D_s^+ \rightarrow K_S \pi^+$	$D^+ \rightarrow K_S K^+$	$D_s^+ \rightarrow K_S K^+$
$A_{\text{rec}}^{D_s^+ \rightarrow \phi \pi^+}$	$D_s^+ \rightarrow \phi \pi^+$ statistics	0.18	0.18	-	-
	$A_{\text{rec}}^{D_s^+ \rightarrow \phi \pi^+}$ binning	0.03	0.03	-	-
	$M(K^+ K^-)$ window	0.03	0.03	-	-
$A_\epsilon^{K^-}$	$D_s^+ \rightarrow \phi \pi^+$ statistics	-	-	0.18	0.18
	$A_{\text{rec}}^{D_s^+ \rightarrow \phi \pi^+}$ binning	-	-	0.03	0.03
	$M(K^+ K^-)$ window	-	-	0.03	0.03
	$D^0 \rightarrow K^- \pi^+$ statistics	-	-	0.06	0.06
	$A_\epsilon^{K^-}$ binning	-	-	0.04	0.04
Possible $A_{CP}^{D^0 \rightarrow K^- \pi^+}$	-	-	0.01	0.01	
$\cos \theta_{D^+}^{\text{CMS}}$ binning		-	-	0.06	0.06
Fitting		0.04	0.27	0.12	0.05
K^0/\bar{K}^0 -material effects		0.06	0.06	0.06	0.06
Total		0.20	0.33	0.25	0.22

Table of systematic uncertainty in A_{CP} (%).

CPV in $D_{(s)}^+ \rightarrow K_S h^+$ decays: Results

A_{CP} in	Belle (%)	Cleo (%)	HFAG WA (%)	A_{CP}^{SM} (%)
$D^+ \rightarrow K_S \pi^+$	$-0.71 \pm 0.19 \pm 0.20$	$-1.3 \pm 0.7 \pm 0.3$	-0.72 ± 0.26	-0.332^\dagger
$D_s^+ \rightarrow K_S \pi^+$	$+5.45 \pm 2.50 \pm 0.33$	$+16.3 \pm 7.3 \pm 0.3$	$+6.5 \pm 2.5$	$+0.332$
$D^+ \rightarrow K_S K^+$	$-0.16 \pm 0.58 \pm 0.25$	$-0.2 \pm 1.5 \pm 0.9$	-0.09 ± 0.63	-0.332
$D_s^+ \rightarrow K_S K^+$	$+0.12 \pm 0.36 \pm 0.22$	$+4.7 \pm 1.8 \pm 0.9$	$+0.28 \pm 0.41$	-0.332^\dagger

\dagger Interference of CF and DCS amplitudes is neglected.

- Major source of systematics is due to h^\pm reconstruction asymmetry correction (limited sample sizes of $D_s^+ \rightarrow \phi \pi^+$ and $D^0 \rightarrow K^- \pi^+$)
 - Scales with luminosity!