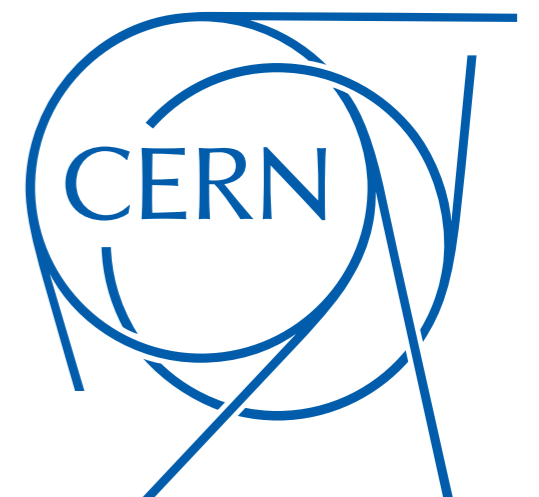


# Theory Predictions: HH and Combinations with Single Higgs

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Stephen Jones



# The Higgs self-coupling

Standard Model Higgs Lagrangian:

$$\mathcal{L} \supset -V(\phi), \quad V(\Phi) = -\mu^2(\Phi^\dagger\Phi) + \lambda(\Phi^\dagger\Phi)^2$$



EW symmetry breaking

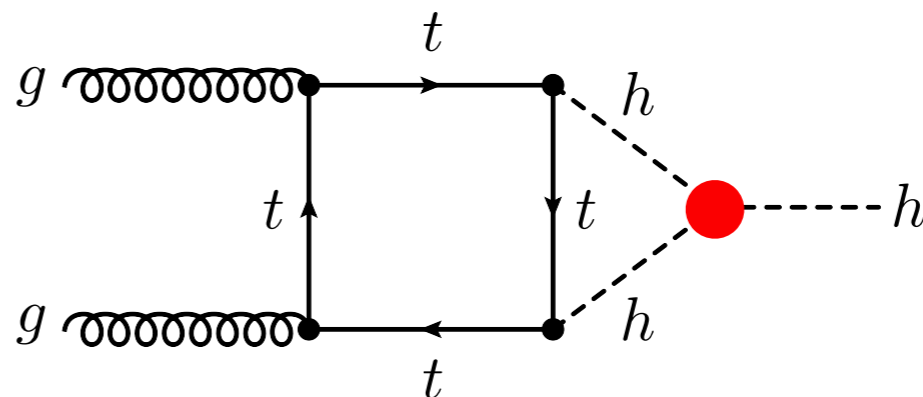
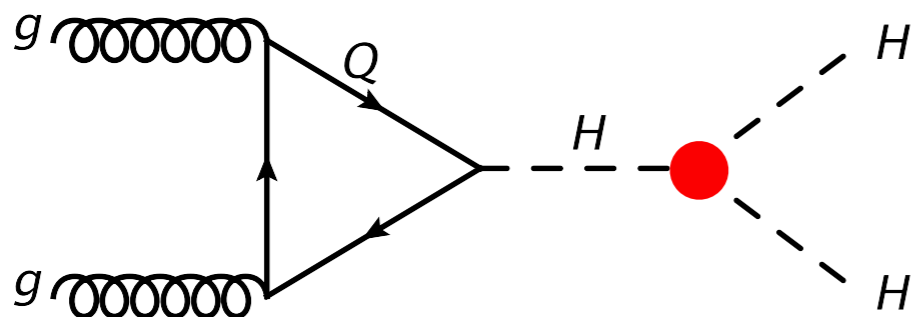
$$V(H) = \frac{1}{2}m_H^2 H^2 + \boxed{\lambda v H^3} + \frac{\lambda}{4} H^4, \quad \begin{array}{l} \mu^2 = \lambda v^2 \\ m_H^2 = 2\lambda v^2 \end{array} \quad \begin{array}{l} \text{SM: self-couplings} \\ \text{determined by } m_H, v \end{array}$$



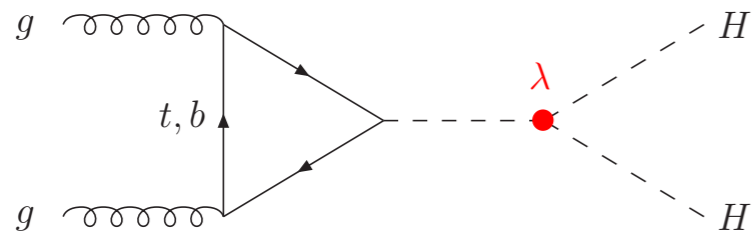
TH: coupling known in SM

EXP: need to find and measure

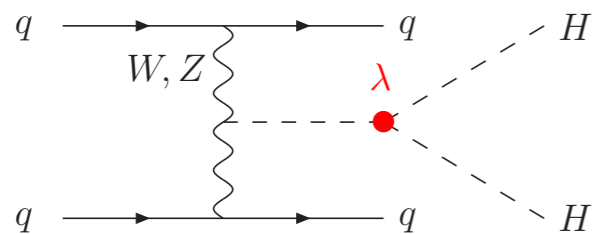
processes involving Higgs self couplings



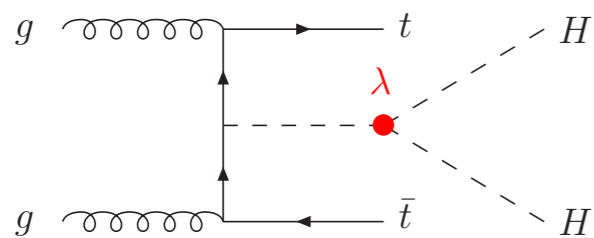
# HH Production Channels at the LHC



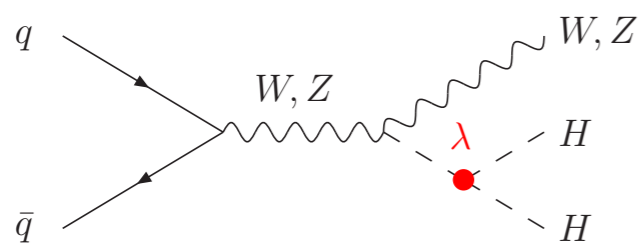
**Gluon Fusion**



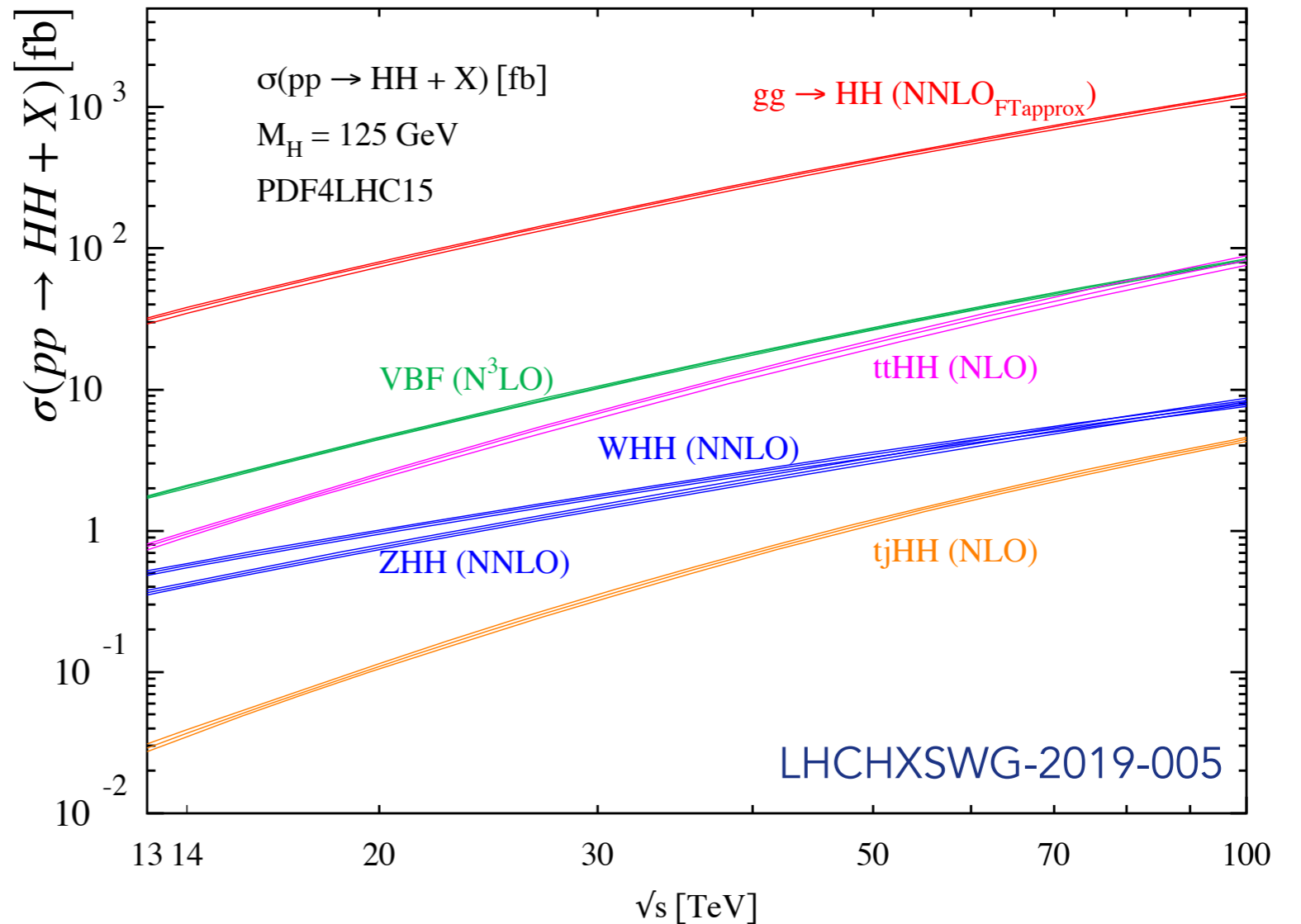
**Vector Boson Fusion**



**Associated Production ( $t\bar{t}$ )**



**Associated Production (W,Z)**

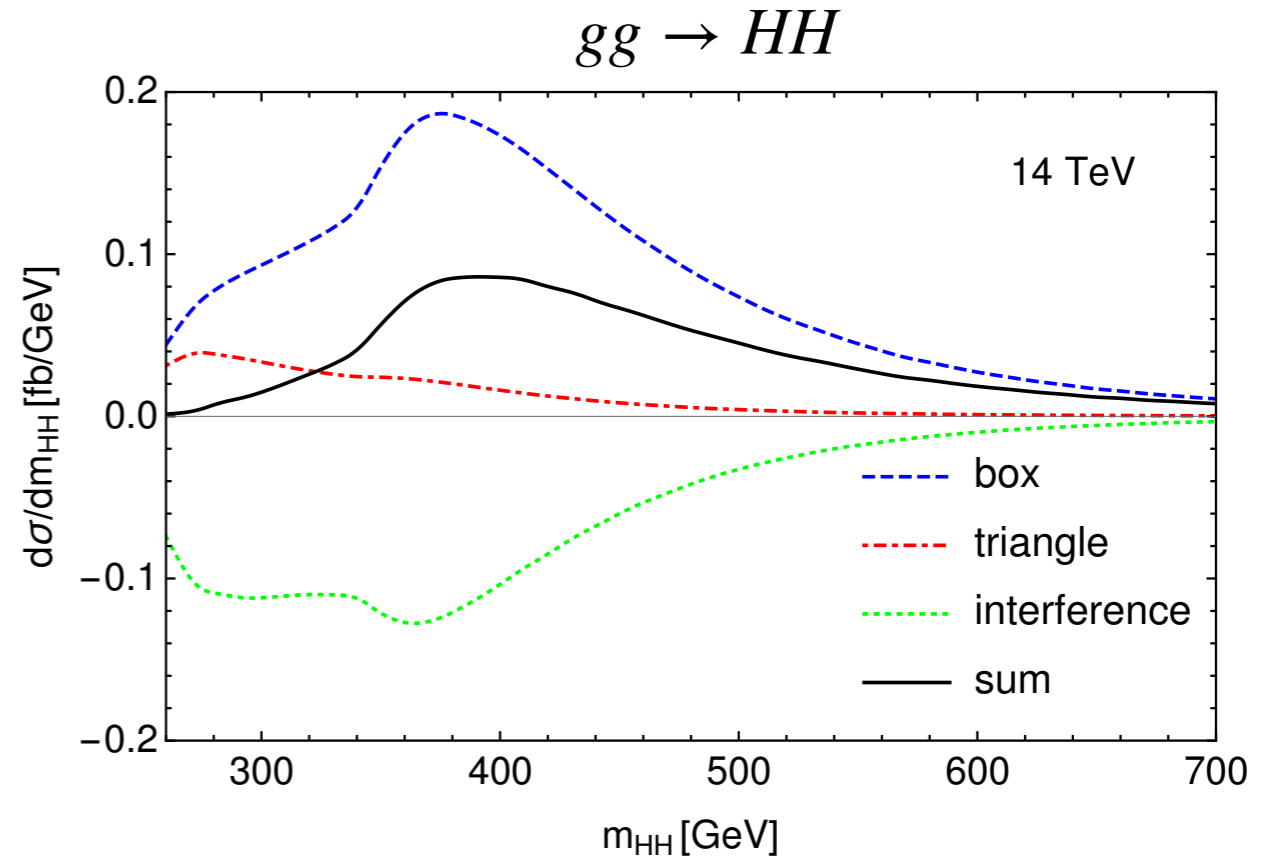
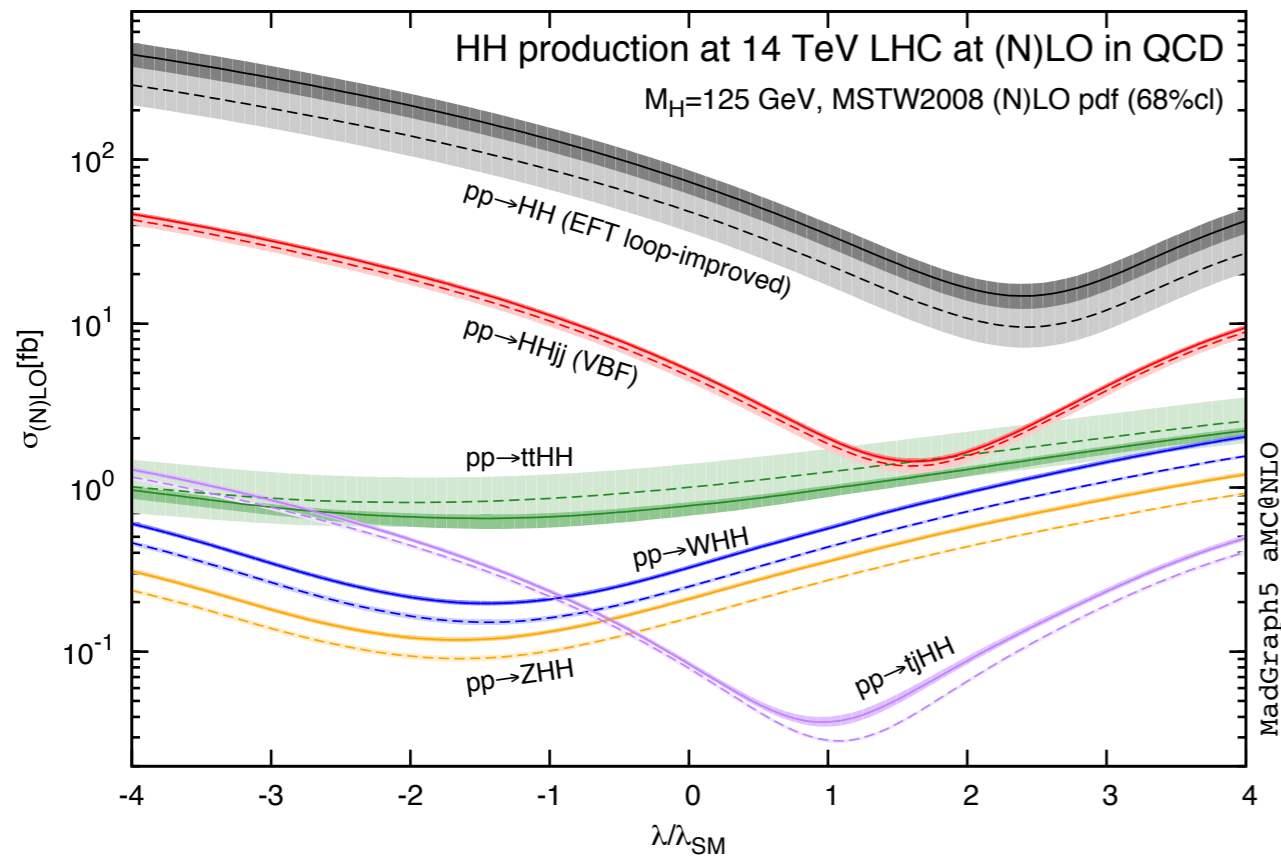


Production channels similar to H

A very important difference:

$$\sigma(pp \rightarrow HH) \sim \frac{\sigma(pp \rightarrow H)}{1000}$$

# HH Self Coupling Dependence



Frederix, Frixione, Hirschi, Maltoni, Mattelaer,  
Torrielli, Vryonidou, M. Zaro 14

LHCHSWG-2019-005

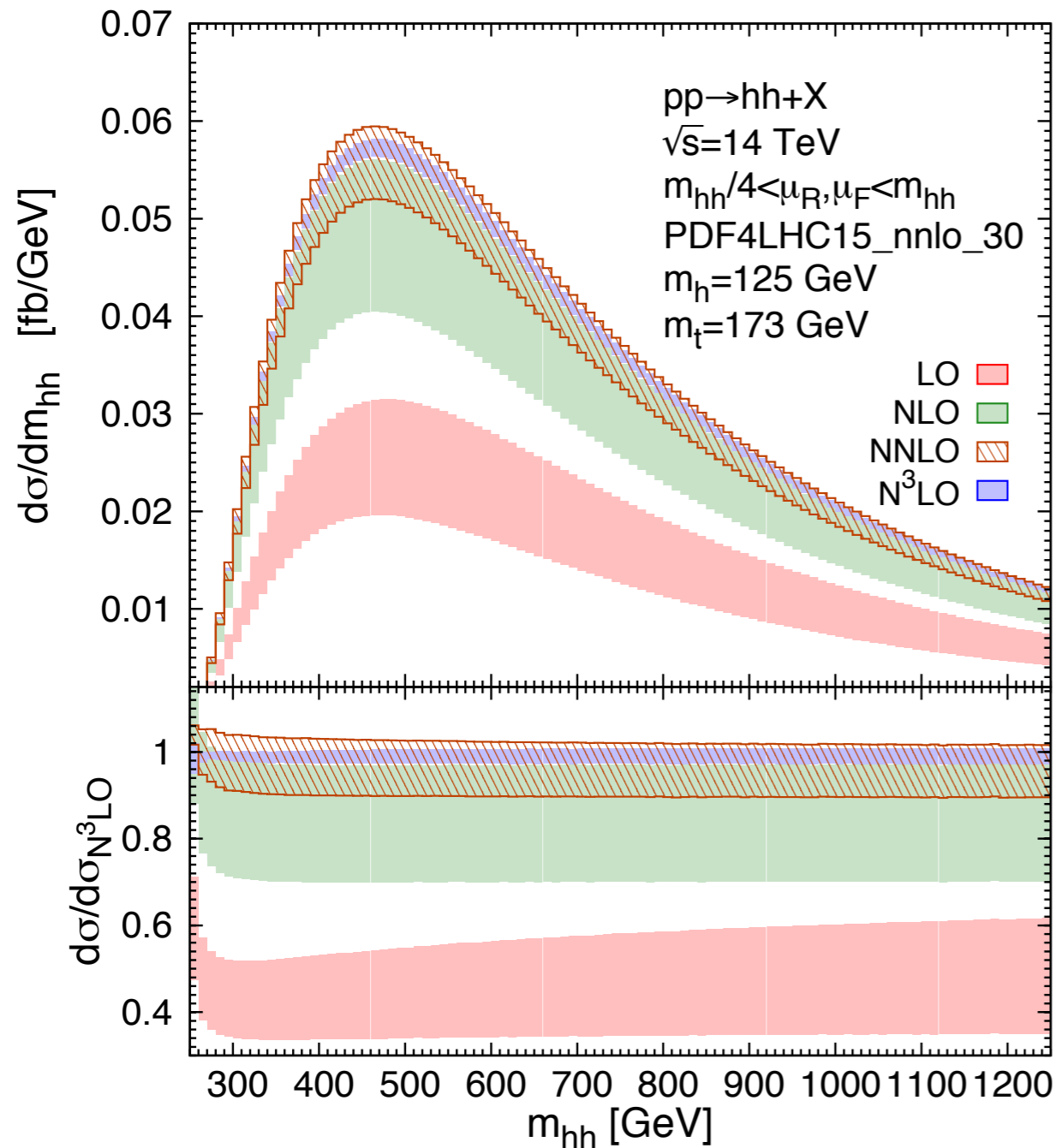
Theory uncertainties on cross section translate into uncertainties on the self-coupling extraction:

For  $gg \rightarrow HH$  close to SM  $\lambda_{hhh}$  we observe  $\frac{\Delta\sigma}{\sigma} \sim -\frac{\Delta\lambda}{\lambda}$

Differential measurements provide additional information and break degeneracies present at total cross-section level

# HH Gluon Fusion: N<sup>3</sup>LO HTL

N<sup>3</sup>LO results for Gluon fusion in the  $m_T \rightarrow \infty$  were recently obtained



order \ $\sqrt{s}$	13 TeV	14 TeV	27 TeV	100 TeV
LO	13.80 <sup>+31%</sup> <sub>-22%</sub>	17.06 <sup>+31%</sup> <sub>-22%</sub>	98.22 <sup>+26%</sup> <sub>-19%</sub>	2015 <sup>+19%</sup> <sub>-15%</sub>
NLO	25.81 <sup>+18%</sup> <sub>-15%</sub>	31.89 <sup>+18%</sup> <sub>-15%</sub>	183.0 <sup>+16%</sup> <sub>-14%</sub>	3724 <sup>+13%</sup> <sub>-11%</sub>
NNLO	30.41 <sup>+5.3%</sup> <sub>-7.8%</sub>	37.55 <sup>+5.2%</sup> <sub>-7.6%</sub>	214.2 <sup>+4.8%</sup> <sub>-6.7%</sub>	4322 <sup>+4.2%</sup> <sub>-5.3%</sub>
N <sup>3</sup> LO	31.31 <sup>+0.66%</sup> <sub>-2.8%</sub>	38.65 <sup>+0.65%</sup> <sub>-2.7%</sub>	220.2 <sup>+0.53%</sup> <sub>-2.4%</sub>	4438 <sup>+0.51%</sup> <sub>-1.8%</sub>



Very mild scale dependence

Take  $\hat{\sigma}^a$  part of result from known single Higgs calculation

Anastasiou, Duhr, Dulat, Herzog, Mistlberger 15;  
 Dulat, Lazopoulos, Mistlberger 18

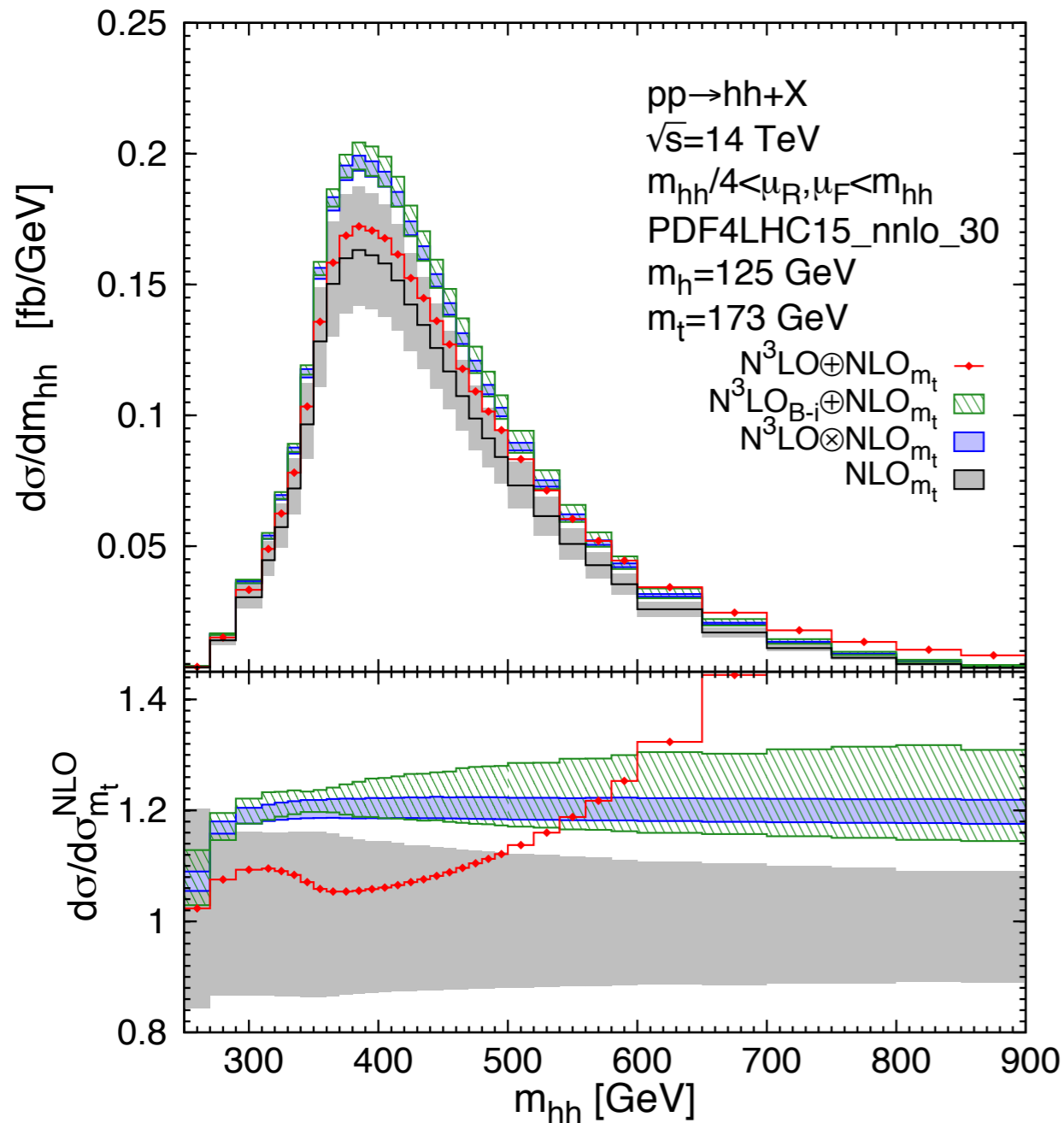
2-loop box piece of  $\hat{\sigma}^b$  first computed earlier

Banerjee, Borowka, Dhani, Gehrmann, Ravindran 18

Chen, Li, Shao, Wang 19

# HH Gluon Fusion: N<sup>3</sup>LO HTL + NLO SM

Top quark mass effects (known up to NLO) have also been included



$\sqrt{s}$	13 TeV	14 TeV	27 TeV	100 TeV
$\text{NLO}_{m_t}$	$27.56^{+14\%}_{-13\%}$	$32.64^{+14\%}_{-12\%}$	$126.2^{+12\%}_{-10\%}$	$1119^{+13\%}_{-13\%}$
$\text{NNLO} \oplus \text{NLO}_{m_t}$	$32.16^{+5.9\%}_{-5.9\%}$	$38.29^{+5.6\%}_{-5.5\%}$	$157.3^{+3.0\%}_{-4.7\%}$	$1717^{+5.8\%}_{-12\%}$
$\text{NNLO}_{B-i} \oplus \text{NLO}_{m_t}$	$33.08^{+5.0\%}_{-4.9\%}$	$39.16^{+4.9\%}_{-5.0\%}$	$150.8^{+4.6\%}_{-5.7\%}$	$1330^{+4.0\%}_{-7.2\%}$
$\text{NNLO} \otimes \text{NLO}_{m_t}$	$32.47^{+5.3\%}_{-7.8\%}$	$38.42^{+5.2\%}_{-7.6\%}$	$147.6^{+4.8\%}_{-6.7\%}$	$1298^{+4.2\%}_{-5.3\%}$
$N^3\text{LO} \oplus \text{NLO}_{m_t}$	$33.06^{+2.1\%}_{-2.9\%}$	$39.40^{+1.7\%}_{-2.8\%}$	$163.3^{+4.0\%}_{-8.3\%}$	$1833^{+14\%}_{-20\%}$
$N^3\text{LO}_{B-i} \oplus \text{NLO}_{m_t}$	$34.17^{+1.9\%}_{-4.6\%}$	$40.44^{+1.9\%}_{-4.7\%}$	$155.5^{+2.3\%}_{-5.0\%}$	$1372^{+2.8\%}_{-5.0\%}$
$N^3\text{LO} \otimes \text{NLO}_{m_t}$	$33.43^{+0.66\%}_{-2.8\%}$	$39.56^{+0.64\%}_{-2.7\%}$	$151.7^{+0.53\%}_{-2.4\%}$	$1333^{+0.51\%}_{-1.8\%}$

Very mild scale dependence persists also after including top mass effects up to NLO

Results agree with  $\text{NNLO}_{\text{FTapprox}}$  result (which retains  $m_T$  effects in real radiation) but with reduced scale uncertainty

Grazzini, Heinrich, SJ, Kallweit, Kerner, Lindert, Mazzitelli 18; (+NNLL) de Florian, Mazzitelli 18;

Chen, Li, Shao, Wang 19

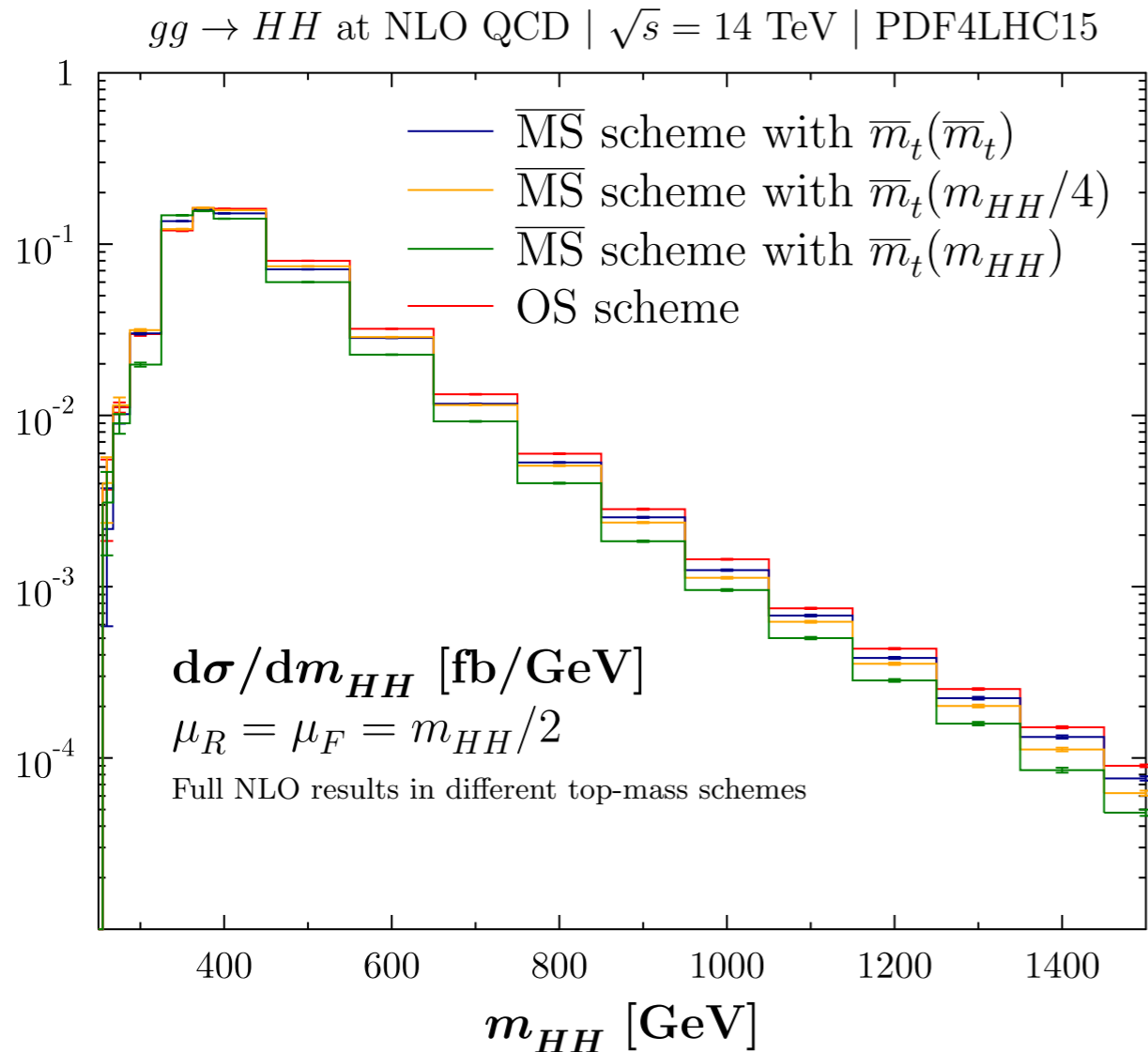
# HH Gluon Fusion: Mass Scheme Uncertainties

With such a tiny scale uncertainty, other sources of uncertainty become relevant

HH@NLO:  $m_T$  in the OS and  $\overline{\text{MS}}$  scheme

Baglio, Campanario, Glaus, Mühlleitner, (+Ronca), Spira, Streicher 18, (20)

See talk of Seraina Glaus on Tue



Top quark mass scheme unc:

$$\left. \frac{d\sigma(gg \rightarrow HH)}{dQ} \right|_{Q=300 \text{ GeV}} = 0.0312(5)^{+9\%}_{-23\%} \text{ fb/GeV},$$

$$\left. \frac{d\sigma(gg \rightarrow HH)}{dQ} \right|_{Q=400 \text{ GeV}} = 0.1609(4)^{+7\%}_{-7\%} \text{ fb/GeV},$$

$$\left. \frac{d\sigma(gg \rightarrow HH)}{dQ} \right|_{Q=600 \text{ GeV}} = 0.03204(9)^{+0\%}_{-26\%} \text{ fb/GeV},$$

$$\left. \frac{d\sigma(gg \rightarrow HH)}{dQ} \right|_{Q=1200 \text{ GeV}} = 0.000435(4)^{+0\%}_{-30\%} \text{ fb/GeV},$$

Large uncertainty obtained comparing OS scheme with  $\overline{\text{MS}}$  scheme at scale  $m_{HH}$

Such mass scheme uncertainties will show up in other processes (e.g. HJ, ZH)

Jones, Spira (Les Houches 19)

See talks of Daniel de Florian on Mon & Jonas Lindert on Tue

# HH Gluon Fusion: Mass Scheme Uncertainties (II)

Combination of scale ( $\mu_R, \mu_F$ ) and top mass scheme (OS /  $\overline{\text{MS}}$ ) studied very recently Baglio, Campanario, Glaus, Mühlleitner, Ronca, Spira 20

If we wish to take the **envelope** of the predictions as the uncertainty, then the two uncertainties should be added **linearly** (validated at NLO)

Above authors advocate use of NNLO<sub>FTapprox</sub> with (NLO) mass scheme errors added

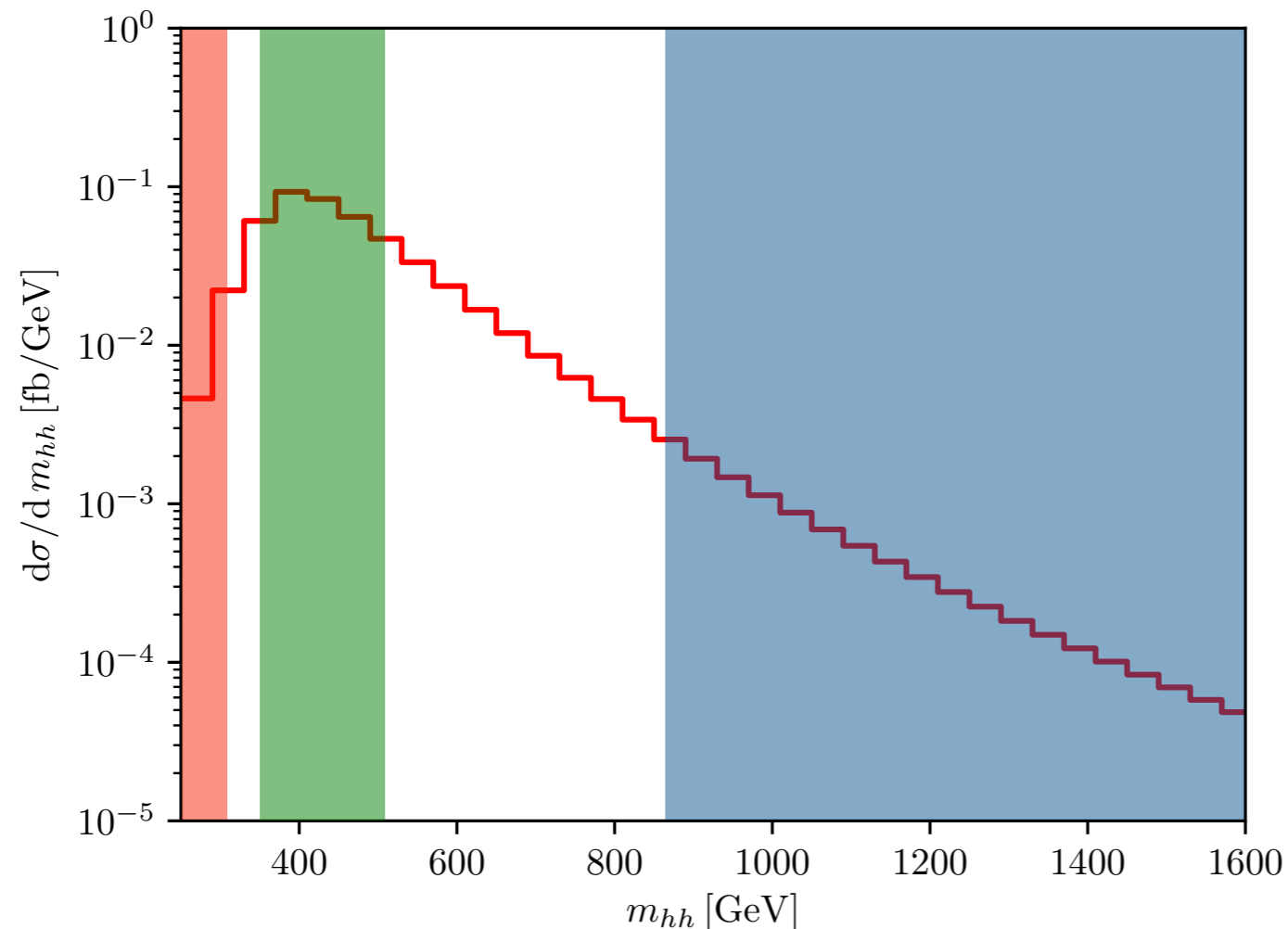
Scale ( $\mu_R, \mu_F$ )	NLO Mass Scheme Unc.	Proposed Combination
$\kappa_\lambda = -10 : \sigma_{tot} = 1680_{-7.7\%}^{+3.0\%} \text{ fb},$	$\kappa_\lambda = -10 : \sigma_{tot} = 1438(1)_{-6\%}^{+10\%} \text{ fb},$	$\kappa_\lambda = -10 : \sigma_{tot} = 1680_{-14\%}^{+13\%} \text{ fb},$
$\kappa_\lambda = -5 : \sigma_{tot} = 598.9_{-7.5\%}^{+2.7\%} \text{ fb},$	$\kappa_\lambda = -5 : \sigma_{tot} = 512.8(3)_{-7\%}^{+10\%} \text{ fb},$	$\kappa_\lambda = -5 : \sigma_{tot} = 598.9_{-15\%}^{+13\%} \text{ fb},$
$\kappa_\lambda = -1 : \sigma_{tot} = 131.9_{-6.7\%}^{+2.5\%} \text{ fb},$	$\kappa_\lambda = -1 : \sigma_{tot} = 113.66(7)_{-9\%}^{+8\%} \text{ fb},$	$\kappa_\lambda = -1 : \sigma_{tot} = 131.9_{-16\%}^{+11\%} \text{ fb},$
$\kappa_\lambda = 0 : \sigma_{tot} = 70.38_{-6.1\%}^{+2.4\%} \text{ fb},$	$\kappa_\lambda = 0 : \sigma_{tot} = 61.22(6)_{-12\%}^{+6\%} \text{ fb},$	$\kappa_\lambda = 0 : \sigma_{tot} = 70.38_{-18\%}^{+8\%} \text{ fb},$
$\kappa_\lambda = 1 : \sigma_{tot} = 31.05_{-5.0\%}^{+2.2\%} \text{ fb},$	$\kappa_\lambda = 1 : \sigma_{tot} = 27.73(7)_{-18\%}^{+4\%} \text{ fb},$	$\kappa_\lambda = 1 : \sigma_{tot} = 31.05_{-23\%}^{+6\%} \text{ fb},$
$\kappa_\lambda = 2 : \sigma_{tot} = 13.81_{-4.9\%}^{+2.1\%} \text{ fb},$	$\kappa_\lambda = 2 : \sigma_{tot} = 13.2(1)_{-23\%}^{+1\%} \text{ fb},$	$\kappa_\lambda = 2 : \sigma_{tot} = 13.81_{-28\%}^{+3\%} \text{ fb},$
$\kappa_\lambda = 2.4 : \sigma_{tot} = 13.10_{-5.1\%}^{+2.3\%} \text{ fb},$	$\kappa_\lambda = 2.4 : \sigma_{tot} = 12.7(1)_{-22\%}^{+4\%} \text{ fb},$	$\kappa_\lambda = 2.4 : \sigma_{tot} = 13.10_{-27\%}^{+6\%} \text{ fb},$
$\kappa_\lambda = 3 : \sigma_{tot} = 18.67_{-7.3\%}^{+2.7\%} \text{ fb},$	$\kappa_\lambda = 3 : \sigma_{tot} = 17.6(1)_{-15\%}^{+9\%} \text{ fb},$	$\kappa_\lambda = 3 : \sigma_{tot} = 18.67_{-22\%}^{+12\%} \text{ fb},$
$\kappa_\lambda = 5 : \sigma_{tot} = 94.82_{-8.8\%}^{+4.9\%} \text{ fb},$	$\kappa_\lambda = 5 : \sigma_{tot} = 83.2(3)_{-4\%}^{+13\%} \text{ fb},$	$\kappa_\lambda = 5 : \sigma_{tot} = 94.82_{-13\%}^{+18\%} \text{ fb},$
$\kappa_\lambda = 10 : \sigma_{tot} = 672.2_{-8.5\%}^{+4.2\%} \text{ fb}$	$\kappa_\lambda = 10 : \sigma_{tot} = 579(1)_{-4\%}^{+12\%} \text{ fb}$	$\kappa_\lambda = 10 : \sigma_{tot} = 672.2_{-13\%}^{+16\%} \text{ fb}$

See talk of Seraina Glaus on Tue



# Mass Uncertainties: Where do we go from here?

1) Just keep calculating, but NNLO with full  $m_T$  is very challenging



**Low invariant mass:**

expand in  $1/m_T^2$

known to NNLO

Grigo, Hoff, Steinhauser 15;

**Around Peak:**

threshold expansion

Gröber, Maier, Rauh 17

**High energy:**

small- $m_T$  expansion

known at NLO

Davies, Mishima, Steinhauser,  
Wellmann 18, 19

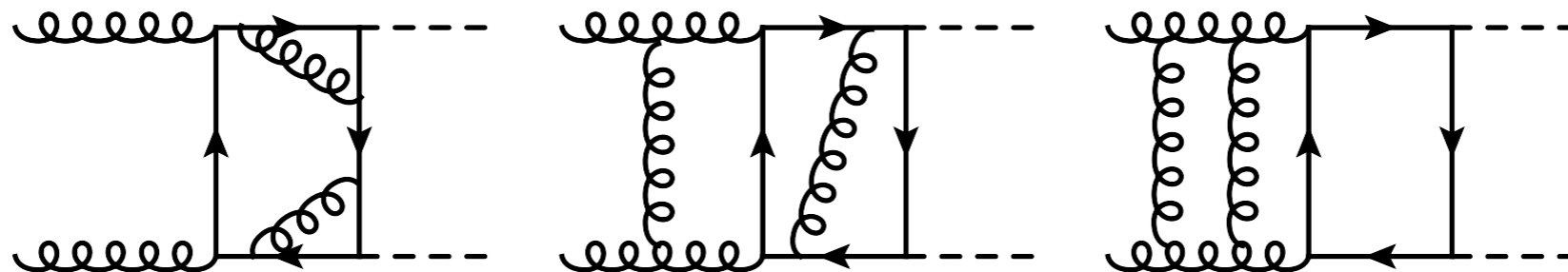
See also: Davies, Steinhauser 19; Davies, Herren, Mishima, Steinhauser 19; Davies, Gröber, Maier, Rauh, Steinhauser 19; Giardino, Gröber 18;

2) Understand structure of mass logarithms Liu, Penin 17, 18

3) Choose preferred scales/schemes? (Threshold: OS, HE:  $\overline{\text{MS}}$  ?)

# Expansions beyond NLO

## NNLO Virtual:



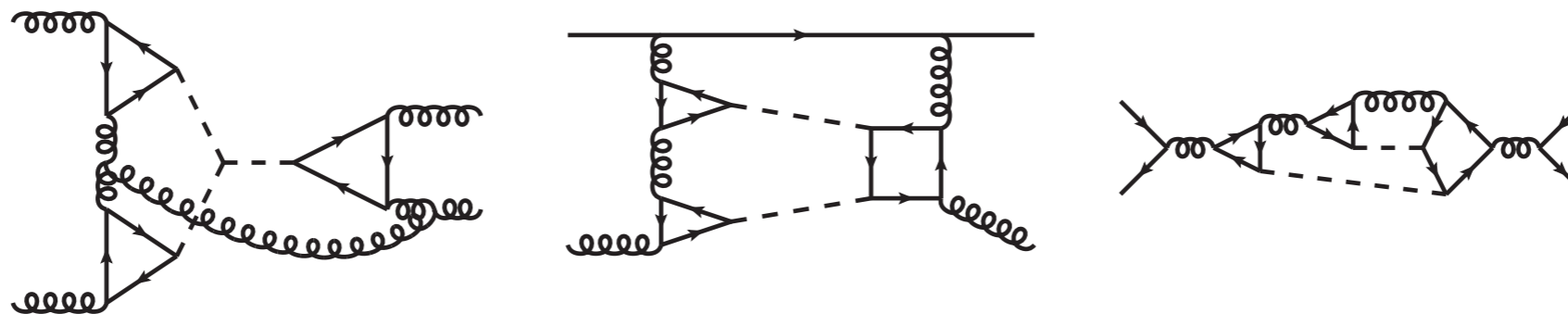
Computed 3-loop virtual piece in large- $m_T$  expansion:

Boxes up to  $1/m_T^8$

Davies, Steinhauser 19

Triangles up to  $1/m_T^{14}$

## NNLO Real-Virtual (Partial):



Davies, Herren,

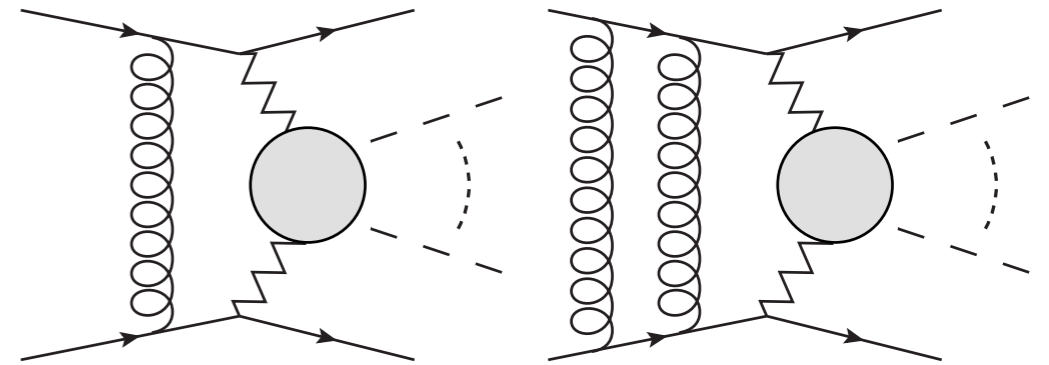
Mishima, Steinhauser 19

5-loop forward scattering amplitudes

Calculation restricted to diagrams with 3 closed top quark loops ( $n_h^3$ )

# VBF HH: Non-factorisable contribution

VBF Approximation/structure function approach:  
neglect the (colour suppressed) exchange of particles between the quark lines



Non-factorisable contributions recently studied using the eikonal approximation

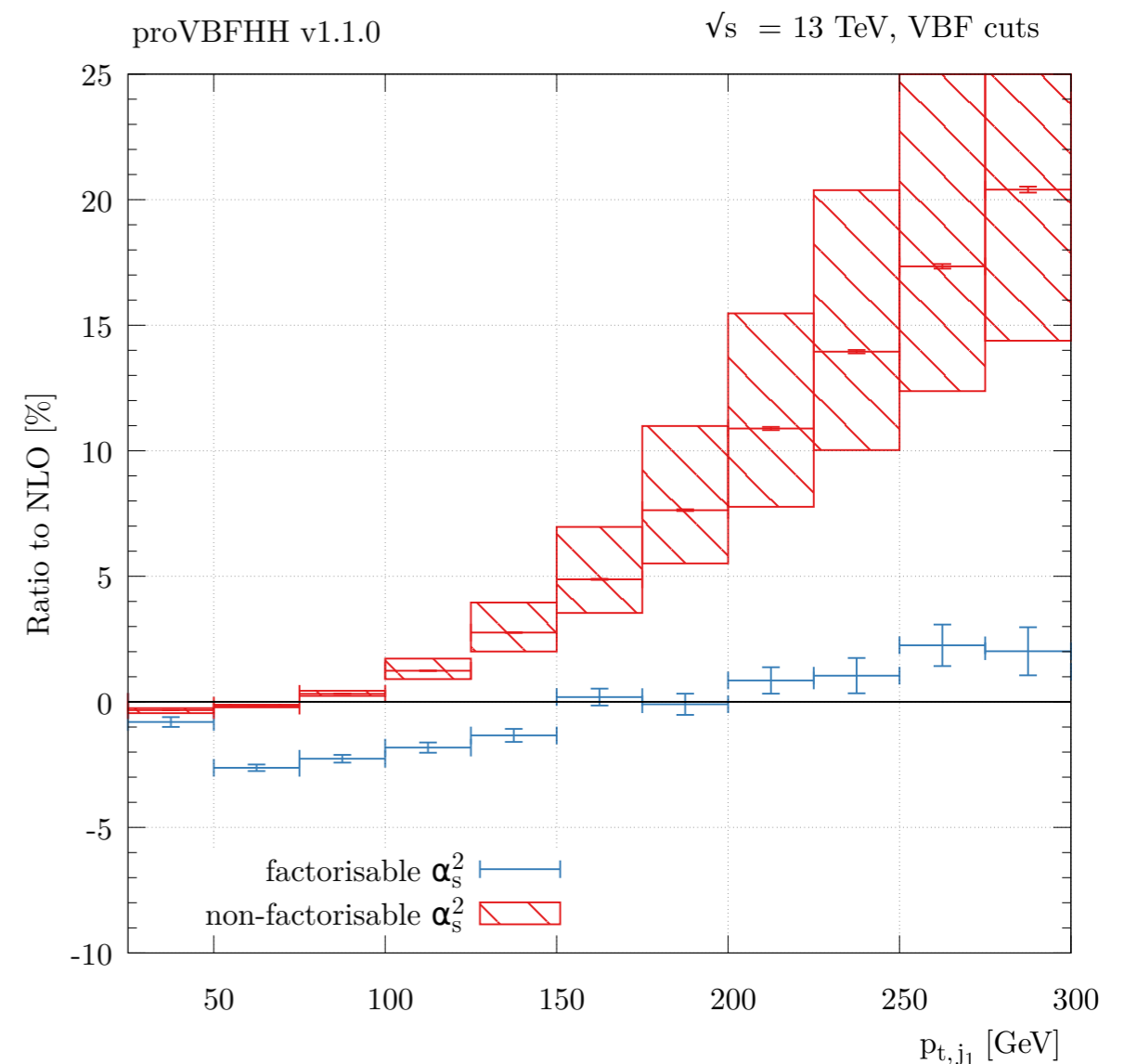
Liu, Melnikov, Penin 19

Dreyer, Karlberg, Tancredi 20

**Delicate cancellations between “box” and “triangle” ( $\lambda_3$ ) diagrams spoiled, giving rise to a large corrections**

$$d\sigma_{HH,nf}^{NNLO} \sim \tilde{\alpha}_s^2 \left[ \left(1 - \frac{\pi^2}{3}\right) (d\sigma_{TT}^{LO} + d\sigma_{TB}^{LO}) + \left(\frac{5}{4} - \frac{\pi^2}{3}\right) d\sigma_{BB}^{LO} \right].$$

**Note:** (As pointed out by authors) Eikonal approximation not trustworthy for too high  $p_{t,j}$



# HH VBF: NNLO QCD + NLO EW

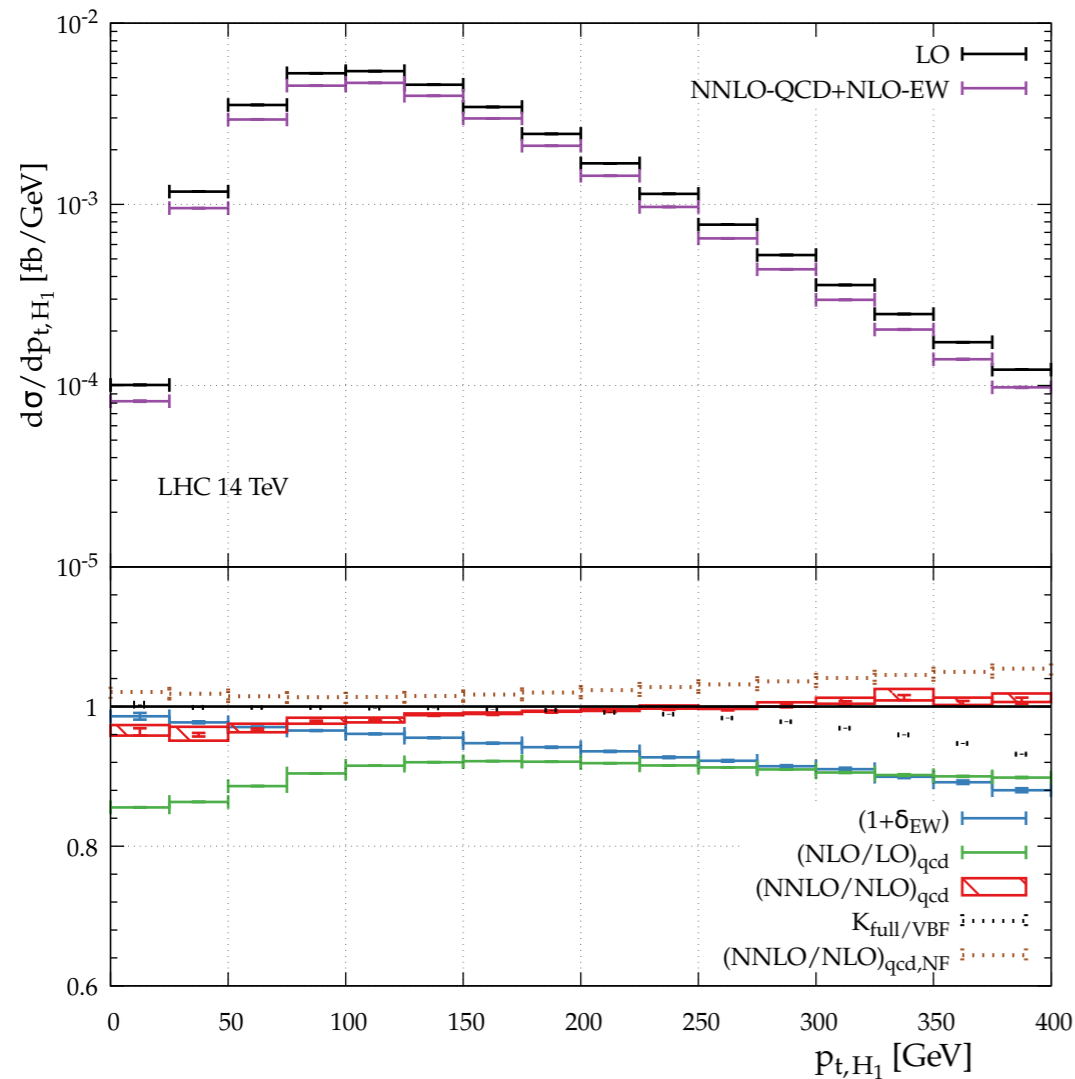
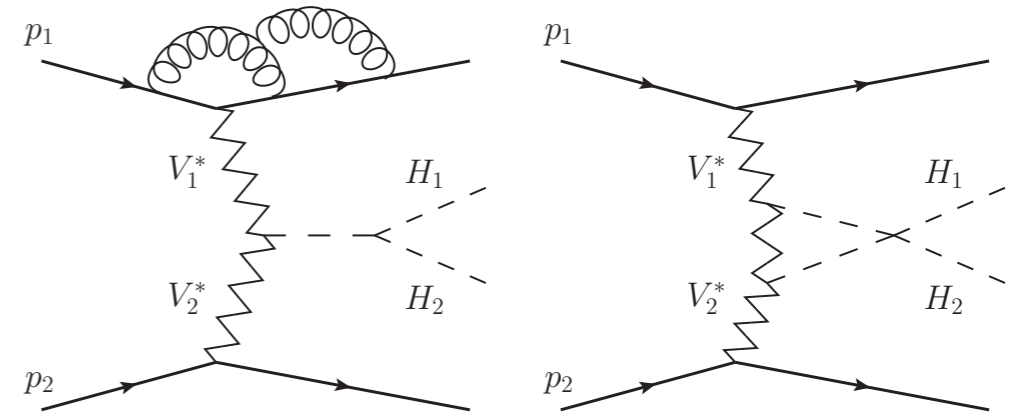
Inclusive known to N<sup>3</sup>LO QCD

Dreyer, Karlberg 18

New state of the art for differential predictions

NNLO QCD Dreyer, Karlberg 18

+ NLO EW Dreyer, Karlberg, Lang, Pellen 20



$\sigma_{\text{LO}}^{\text{full}}$	$\delta_{\text{NLO QCD}}^{\text{full}}$	$\delta_{\text{NNLO QCD}}^{\text{VBF}}$	$\delta_{\text{NLO EW}}^{\text{full}}$	$\sigma_{\text{NNLO QCD} \times \text{NLO EW}}$	$\delta_{\text{NNLO QCD}}^{\text{NF}}$ [fb]
$0.78444(9)^{+0.0825}_{-0.0694}$	$-0.07110(13)$	$-0.0115(5)$	$-0.0476(2)$	$0.6684(5)^{+0.002}_{-0.0004}$	$0.01237(2)$
$+10.5\%$ $-8.8\%$	$-9.1\%$	$-1.5\%$	$-6.1\%$	$-14.8\%^{+0.3\%}_{-0.06\%}$	$+1.7\%$



EW corrections similar in size to NLO QCD corrections and to those in single Higgs case

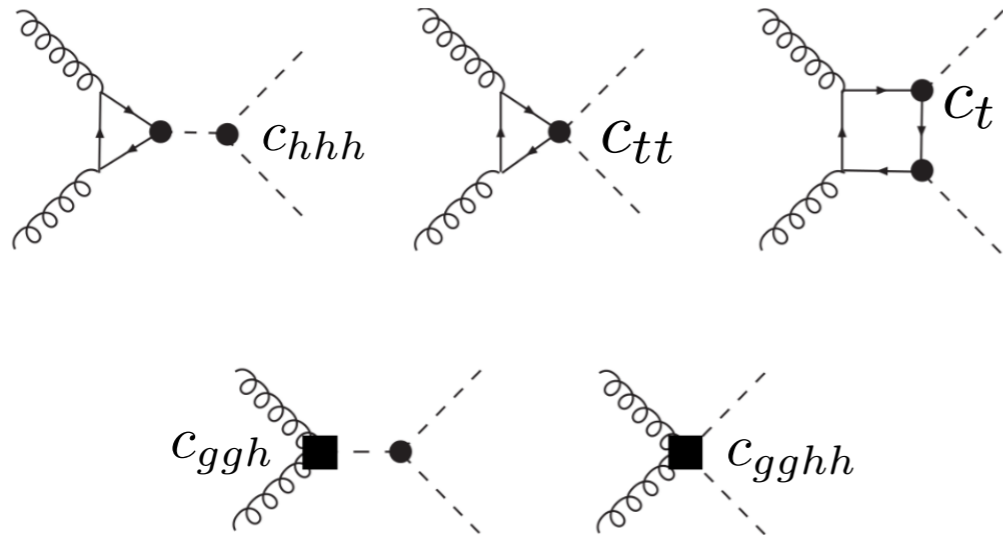
Non-factorisable contribution similar to NNLO QCD factorisable contribution but with opposite sign

All corrections available in public code:  
**proVBFHH v1.1.0**

# HH Gluon Fusion: EFT Results

Just varying  $\lambda$ : one "direction" in EFT parameter space

Parametrise **non-resonant** new physics with EFT:



NLO QCD corrections with full top-quark mass dependence known (non-linear EFT framework)

Buchalla, Capozzi, Celis, Heinrich, Scyboz 18

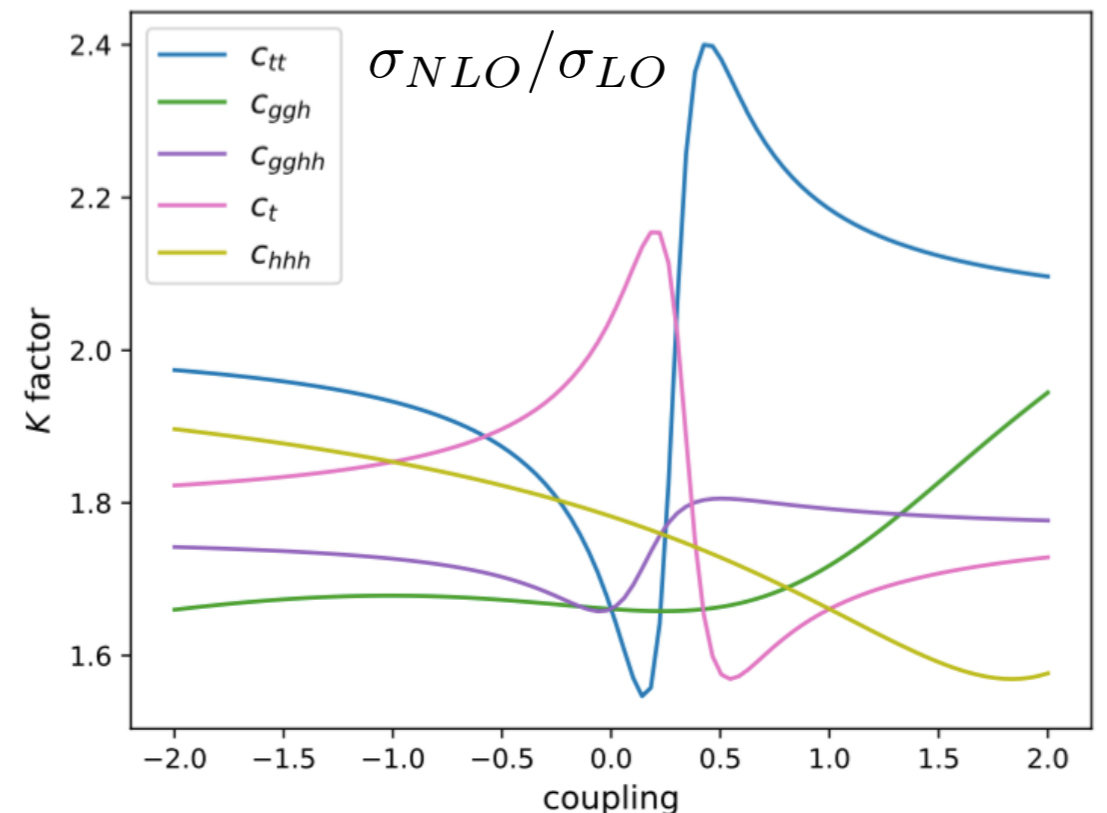
- Results for 12 BSM "clusters"/benchmarks
- Coefficients for reconstructing  $\sigma_{\text{tot}}, m_{hh}$  for arbitrary values of the couplings
- K-factors show significant dependence on the couplings

See also:

(B.I. NLO HTL) Gröber, Mühlleitner, Spira, Streicher 15;

(B.I. NNLO HTL) de Florian, Fabre, Mazzitelli 17;

Dall'Osso, Dorigo, Gottardo, Oliveira, Tosi, Goertz 15; Carvalho, Manzano, Dorigo, Gouzevich 16;



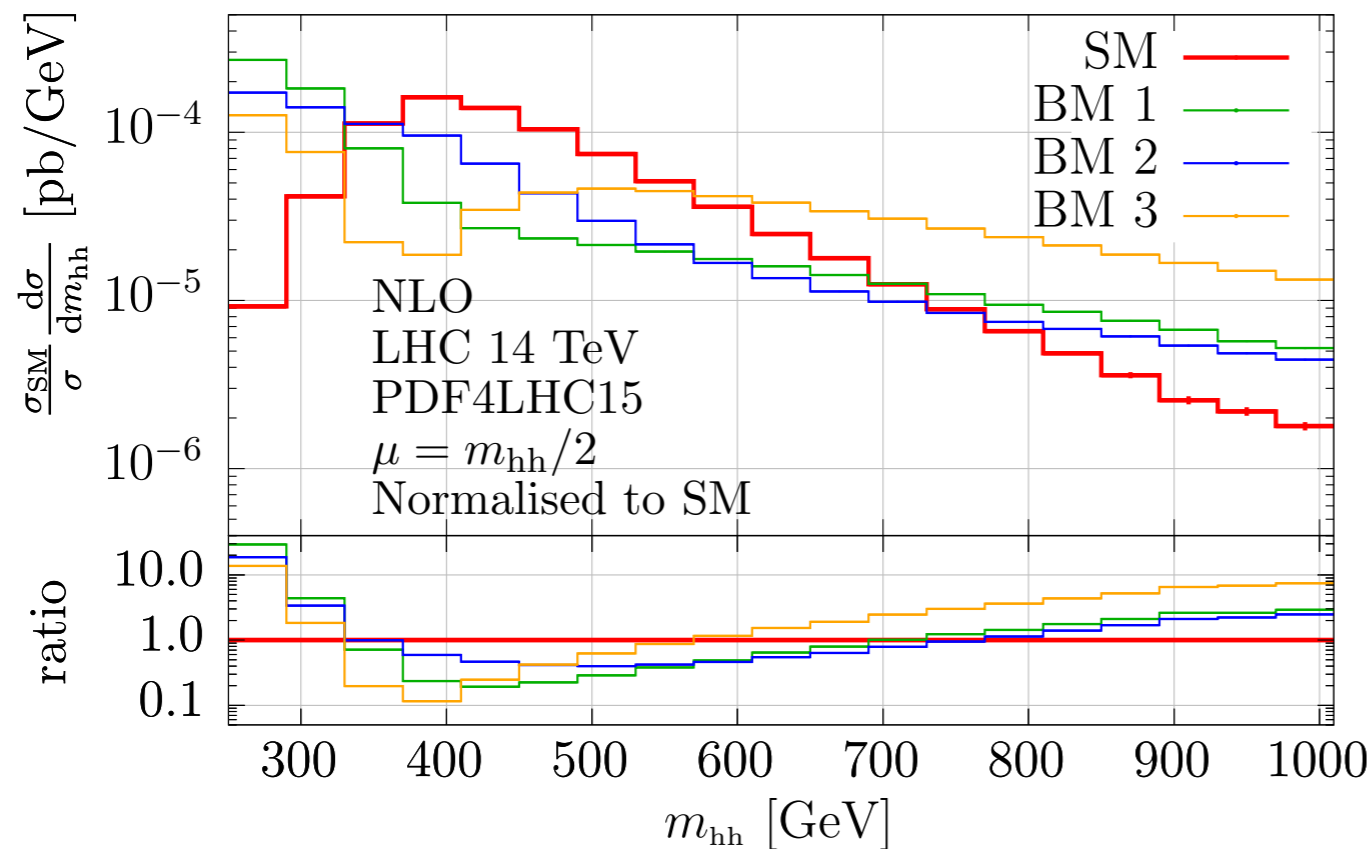
# HH Gluon Fusion: EFT Results (II)

Results in non-linear EFT framework for  $gg \rightarrow HH$  @ NLO (2-loop) with full  $m_T$  are now publicly available in POWHEG-BOX (See /User-Processes-V2/ggHH)

Heinrich, SJ, Kerner, Scyboz 20

$$\begin{aligned}
 |\mathcal{M}_{\text{BSM}}|^2 = & a_1 c_t^4 + a_2 c_{tt}^2 + a_3 c_t^2 c_{hhh}^2 + a_4 c_{ggh}^2 c_{hhh}^2 + a_5 c_{ggh}^2 + a_6 c_{tt} c_t^2 + a_7 c_t^3 c_{hhh} \\
 & + a_8 c_{tt} c_t c_{hhh} + a_9 c_{tt} c_{ggh} c_{hhh} + a_{10} c_{tt} c_{ggh} + a_{11} c_t^2 c_{ggh} c_{hhh} + a_{12} c_t^2 c_{ggh} \\
 & + a_{13} c_t c_{hhh}^2 c_{ggh} + a_{14} c_t c_{hhh} c_{ggh} + a_{15} c_{ggh} c_{hhh} c_{ggh} + a_{16} c_t^3 c_{ggh} \\
 & + a_{17} c_t c_{tt} c_{ggh} + a_{18} c_t c_{ggh}^2 c_{hhh} + a_{19} c_t c_{ggh} c_{ggh} + a_{20} c_t^2 c_{ggh}^2 \\
 & + a_{21} c_{tt} c_{ggh}^2 + a_{22} c_{ggh}^3 c_{hhh} + a_{23} c_{ggh}^2 c_{ggh} .
 \end{aligned}$$

Born-virtual interference term parametrised with 23 linearly independent sets of couplings, grids generated for each interference term, combined at run time

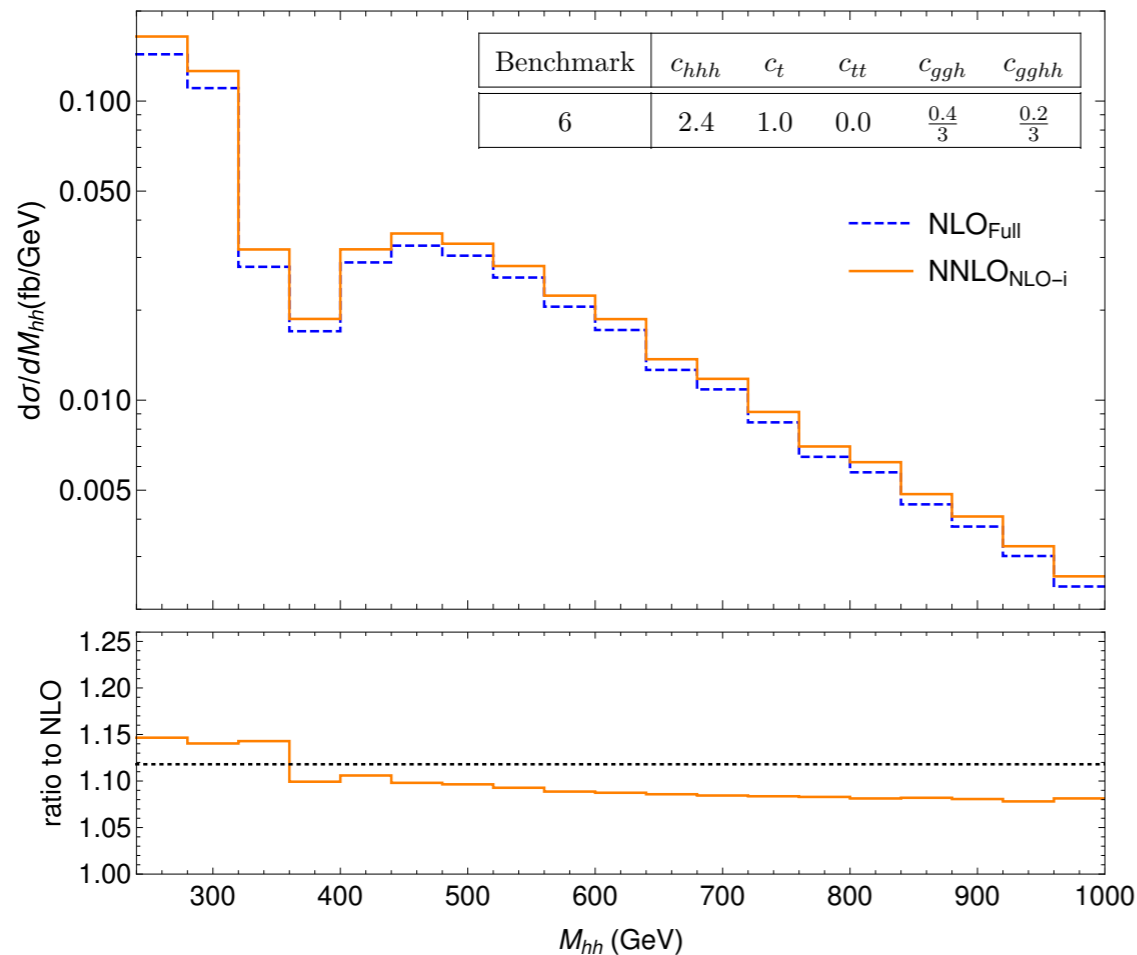


Allows user to specify EFT couplings in a completely flexible manner

**Note:** Chromo-magnetic operator not included here (suppressed depending on EFT counting)

# HH Gluon Fusion: NNLO HTL + NLO SM with EFT

NNLO (Born-improved) HTL limit results known including dim-6 operators  
de Florian, Fabre, Mazzitelli 17



Can apply bin-by-bin reweighting to obtain NLO improved results including EFT effects

$$\Delta\sigma(\text{NNLO}_{\text{NLO-i}}) = \Delta\sigma(\text{NNLO}_{\text{B-i}}) \times \frac{\Delta\sigma(\text{NLO}_{\text{Full}})}{\Delta\sigma(\text{NLO}_{\text{B-i}})}$$

de Florian, Fabre, Heinrich, Mazzitelli (Les Houches 19)

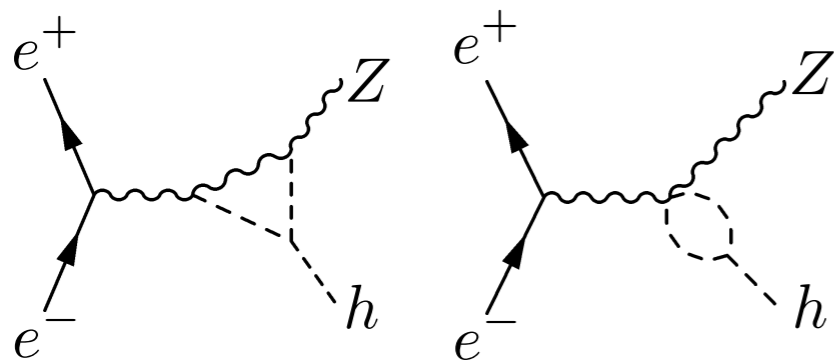
$c_{hhh}$	-1	0	1	2	2.4	3	5
$\sigma$ [fb]	$131.9^{+2.5\%}_{-6.7\%}$	$70.38^{+2.4\%}_{-6.1\%}$	$31.05^{+2.2\%}_{-5.0\%}$	$13.81^{+2.1\%}_{-4.9\%}$	$13.1^{+2.3\%}_{-5.1\%}$	$18.67^{+2.7\%}_{-7.3\%}$	$94.82^{+4.9\%}_{-8.8\%}$
$\sigma/\sigma^{\text{SM}}$	4.25	2.27	1	0.445	0.422	0.601	3.05
$\sigma/\sigma_{\text{NLO}}$	1.13	1.13	1.12	1.11	1.12	1.15	1.16

$\text{NNLO}_{\text{NLO-i}}$  corrections show rather mild dependence on  $\lambda_3$

# Higgs Self-Coupling from Single Higgs Production

So far focused on HH production where  $\lambda_3$  appears at LO

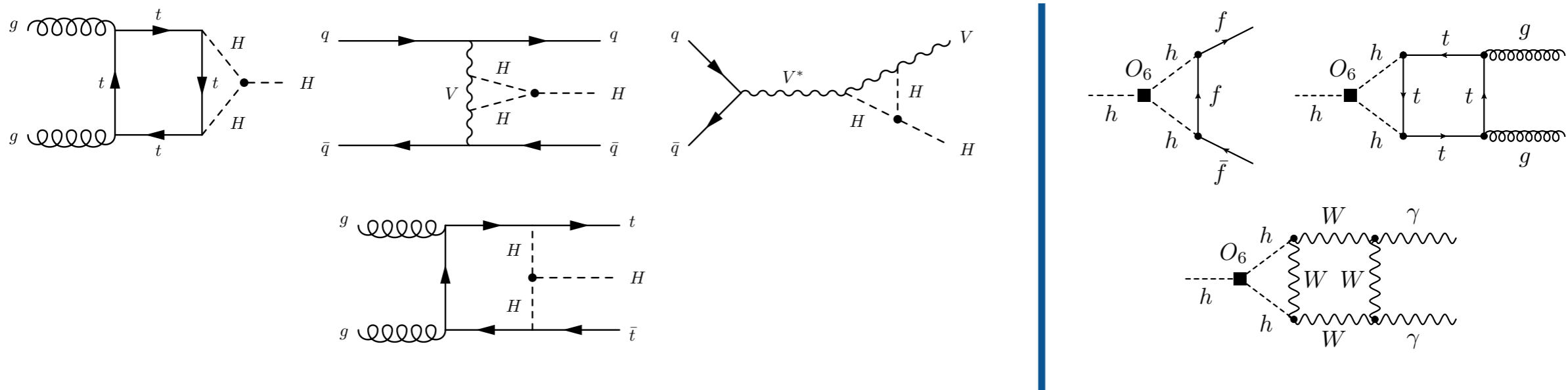
Can also constrain this coupling from high-order effects in single Higgs production



E.g. can constrain  $\lambda_3$  below HH threshold from EW corrections to  $e^+e^- \rightarrow ZH$

McCullough 13

At LHC,  $\lambda_3$  appears in main Higgs production and decay channels

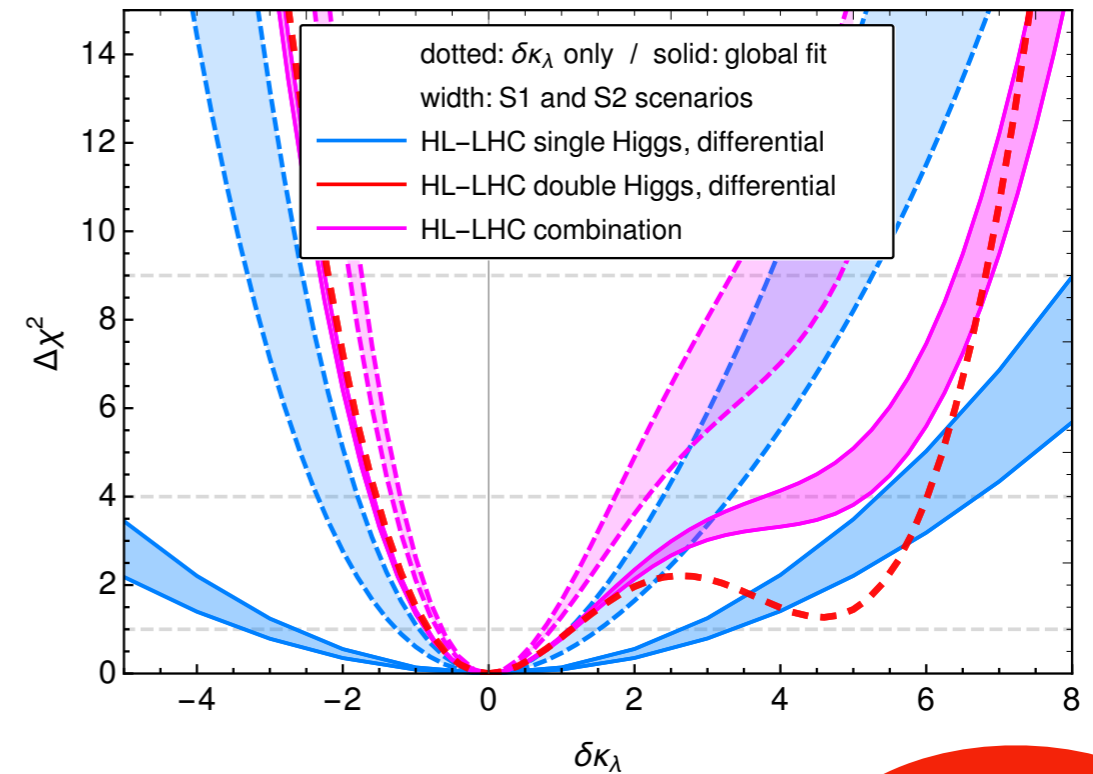
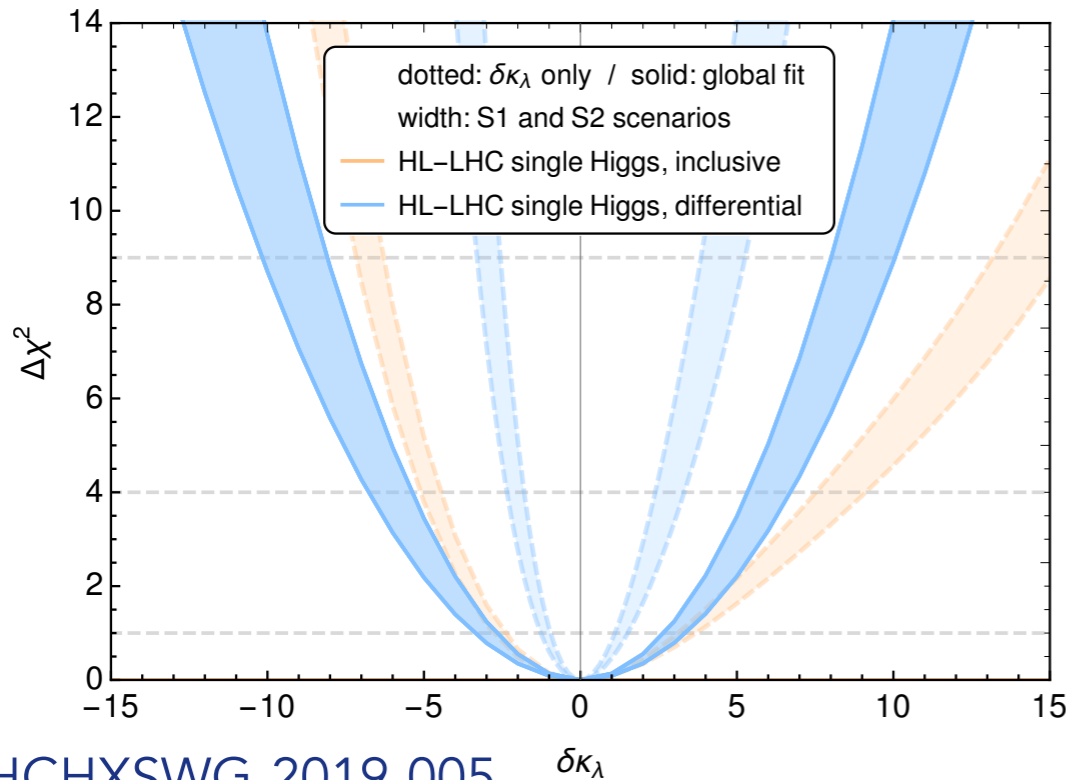


Gorbahn, Haisch 16, 19; Bizon, Gorbahn, Haisch, Zanderighi 16; Degraasi, Giardino, Maltoni, Pagani 16; Maltoni, Pagani, Shivaji, Zhao 17; Di Vita, Grojean, Panico, Riemann, Vantalon 17



# Single Higgs Constraints

Assuming that only  $\lambda_3$  is modified single Higgs can provide very useful constraints



LHCHSWG-2019-005

Impressive results have already been obtained with current data

**Warning:**  
see EXP talks for updates

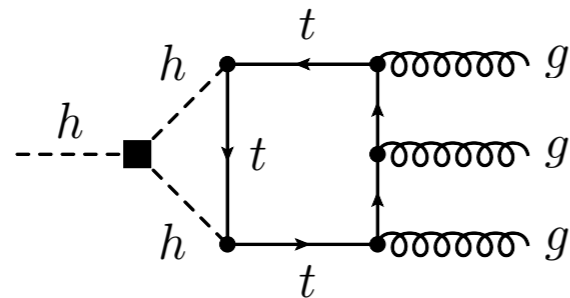
Limits on  $\lambda_3$  from HH production (ATLAS  $b\bar{b}b\bar{b}$ ,  $b\bar{b}\tau^+\tau^-$ ,  $b\bar{b}\gamma\gamma$ )  
 $\sigma_{\text{tot}} \leq 6.9\sigma_{\text{SM}}$  (95% CL) and  $-5.0 < \kappa_\lambda < 12.0$  CERN-EP-2019-099



Complementary limits on  $\lambda_3$  from single Higgs:  $-3.2 < \kappa_\lambda < 11.9$   
**Combination:**  $-2.3 < \kappa_\lambda < 10.3$  ATL-PHYS-PUB-2019-009  
 ATLAS-CONF-2019-049

# Higgs Self-Coupling from Single Higgs Production

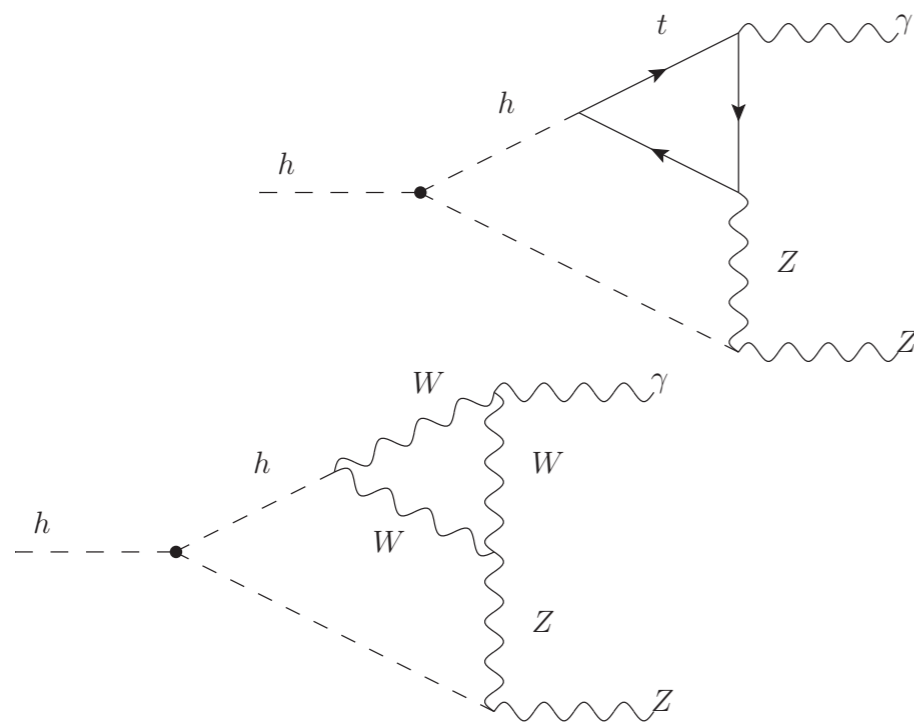
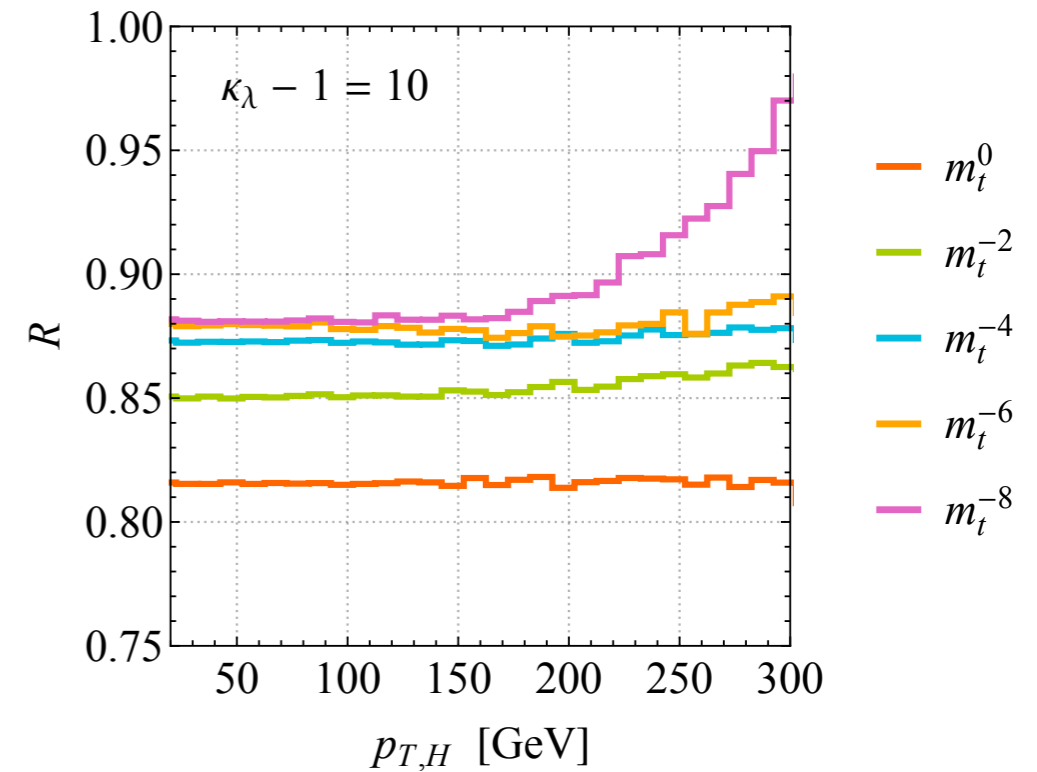
Desirable to have differential effects for gluon fusion: need 2-loop EW diagrams for  $pp \rightarrow HJ$



Computed in  $1/m_T^2$  expansion (valid for  $p_{T,H} < m_T$ )  
 Gorbahn, Haisch 19

Ratio to SM rather flat below top threshold

Interesting to explore  $\lambda_3$  effects above threshold (?)



**Self-coupling dependent contributions to  $h \rightarrow \gamma Z$  now known** Degrassi, Vitti 19

2-loop diagrams computed in a small external momentum expansion

Sensitivity of  $\Gamma(h \rightarrow \gamma Z)$  & BR to  $\lambda_3$  found to be similar to  $h \rightarrow WW$

# Higgs Self-Coupling from Single Higgs Production

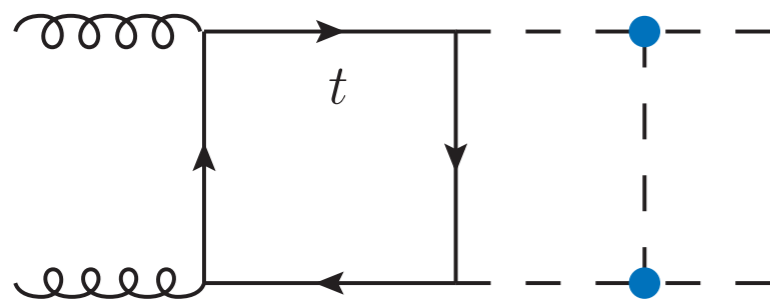
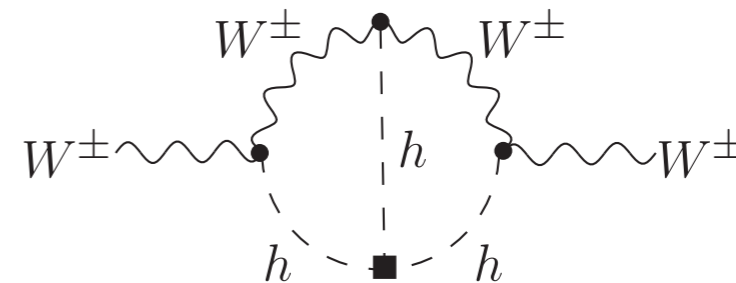
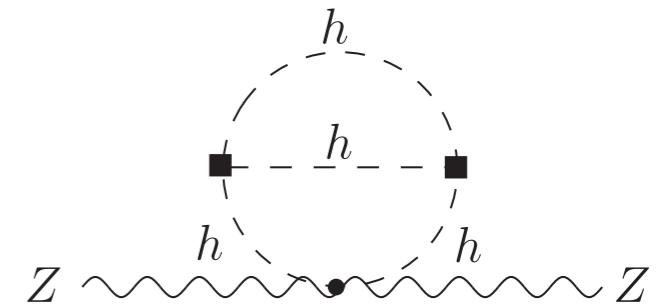
Can also constrain  $\lambda_3$  by considering the modification of precision EW observables (EW oblique corrections)  $S, T$

Weaker bounds than single Higgs production:

$$-14.0 \leq \kappa_\lambda \leq 17.4 \text{ (but complementary)}$$

Degrassi, Fedele, Giardino 17;

Kribs, Maier, Rzehak, Spannowsky, Waite 17;



Aside: can play similar games with HH to set indirect limits on  $\lambda_4$  from (partial) EW corrections to HH

Bizon, Haisch, Rottoli 18; Borowka, Duhr, Maltoni, Pagani, Shivaji, Zhao 18

**Important caveat:** If  $\lambda_3$  is modified by BSM physics we may expect other Higgs couplings to be affected, can have drastic effects on indirect constraints, need to be careful how we interpret deviations (+global EFT approach motivated)

Di Vita, Grojean, Panico, Riemann, Vantalon 17

# Summary

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## **Incredible progress in HH theory over the last few years**

- Gluon fusion - Full SM result: NLO
- Gluon fusion - HTL result: N<sup>3</sup>LO (also differential)
- Vector Boson Fusion - N<sup>3</sup>LO inclusive, NNLO differentially + NLO EW
- Progress matched by amazing work from the experiments

## **Uncertainties beyond scale variations are becoming relevant**

- Mass scheme uncertainties at the level of >10% percent @ NLO
- Motivates studies of  $m_T$  dependence beyond 2-loop

**Combination with constraints from single Higgs production & EW precision observables can improve  $\lambda_3$  determination**

**Many other fascinating developments were not covered in this talk**

**(e.g. prospects at future collider prospects, EFT fits, ...)**

**See talks of Konstantinos Nikolopoulos, Michele Selvaggi & Shankha Banerjee from this morning**

**Thank you for listening**

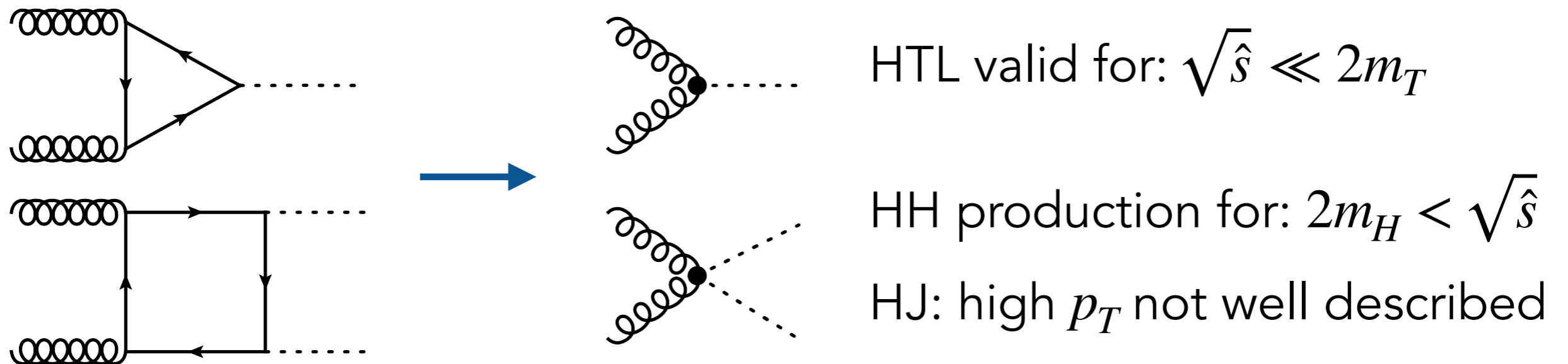
Backup

# Heavy Top Limit

Heavy Top Limit (HTL):  $m_T \rightarrow \infty$

Effective tree-level couplings between gluons and Higgs

Lowers number of loops by 1



**Born improved NLO HTL:**

$$d\sigma_{\text{NLO}}(m_T) \approx d\bar{\sigma}_{\text{NLO}}(m_T) \equiv \underbrace{\frac{d\sigma_{\text{LO}}(m_T)}{d\sigma_{\text{LO}}(m_T \rightarrow \infty)}}_{\text{N}} d\sigma_{\text{NLO}}(m_T \rightarrow \infty)$$

Spira et al. (HPAIR)

# HH Approximations @ NLO (Schematically)

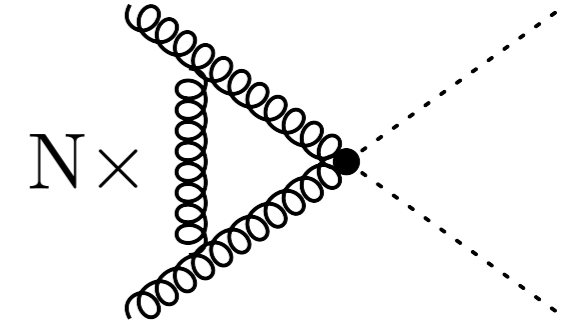
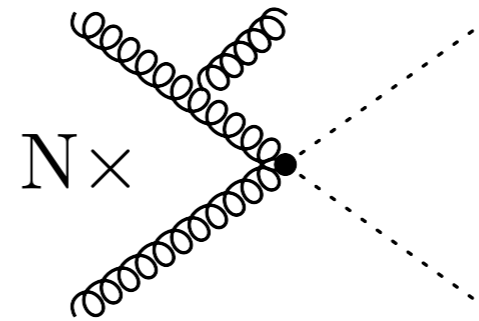
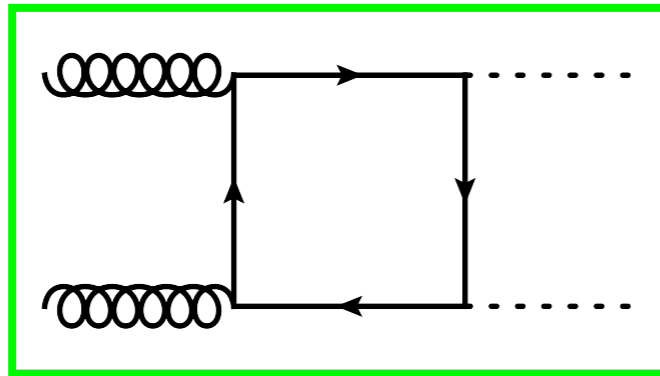
$B$

$R$

$V$

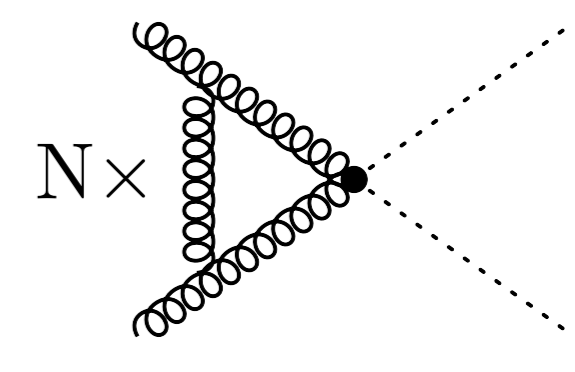
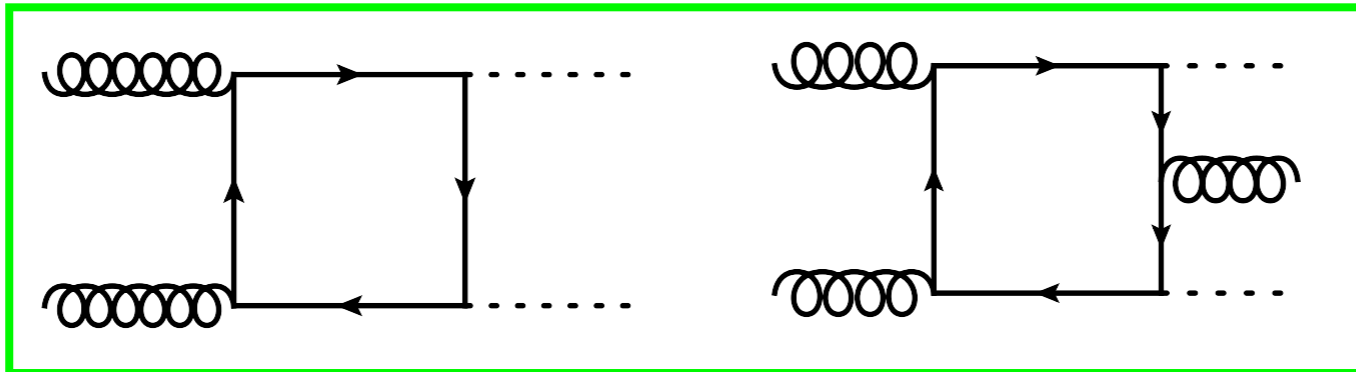
## B-i HTL:

Dawson,  
Dittmaier, Spira 98

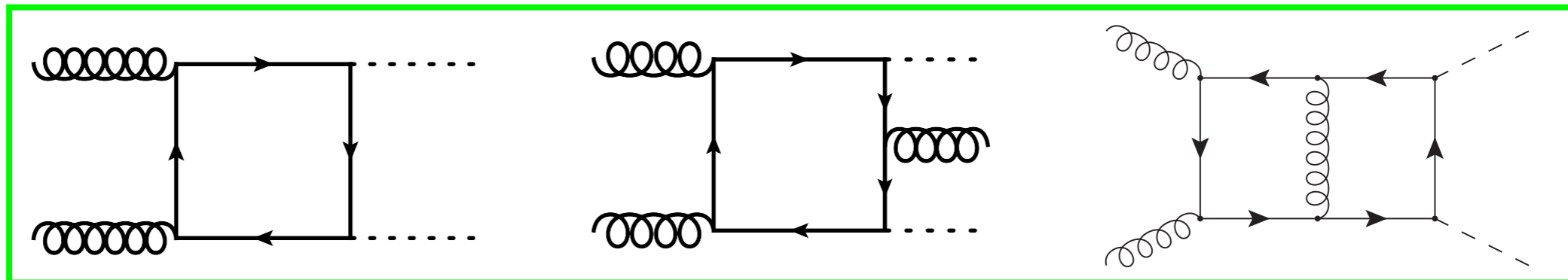


## FTapprox:

Maltoni, Vryonidou,  
Zaro 14



## Full Theory:



Borowka, Greiner, Heinrich, SPJ, Kerner, Schlenk, Schubert, Zirke 16;

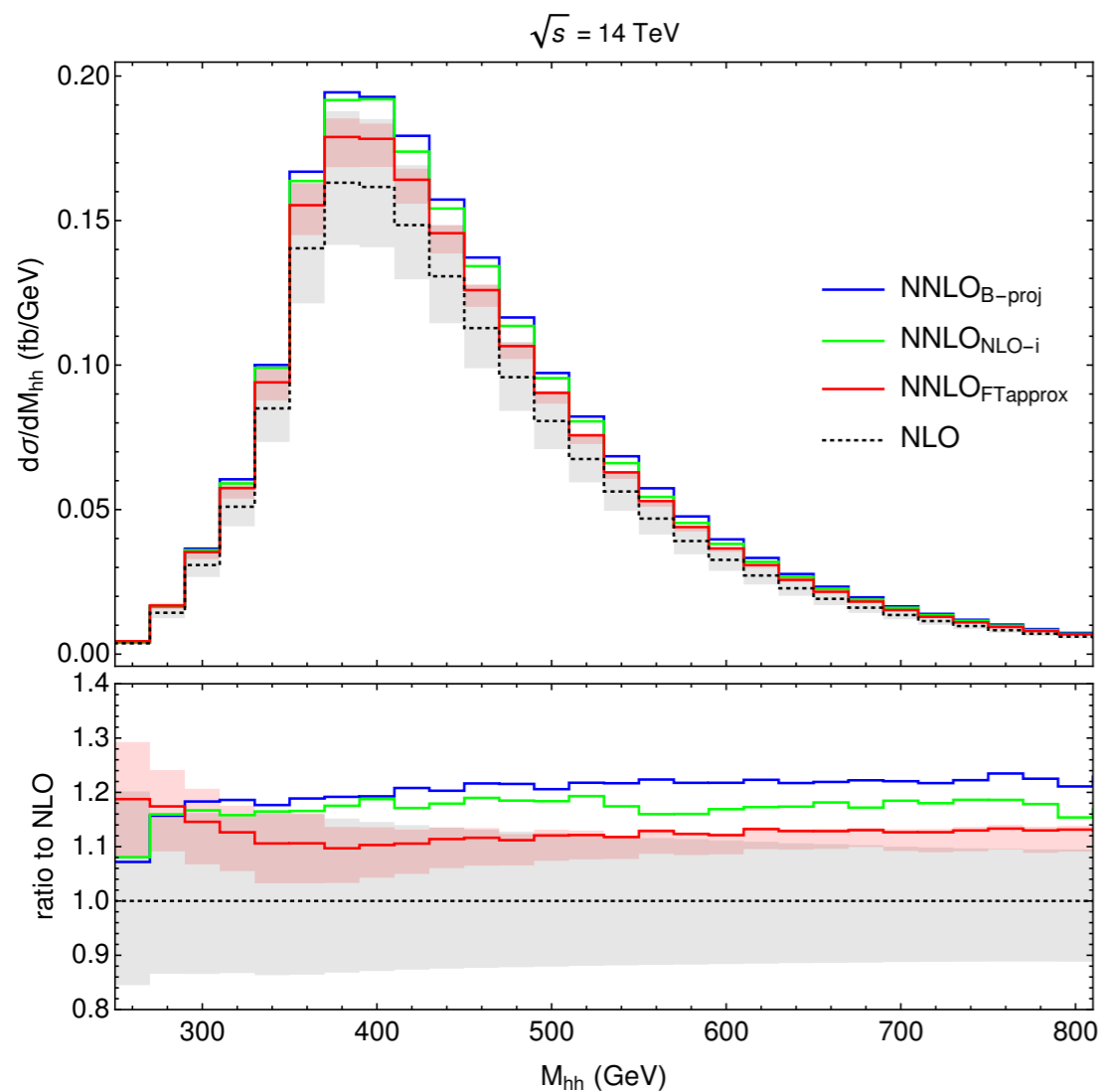
Borowka, Greiner, Heinrich, SPJ, Kerner, Schlenk, Zirke 16;

Baglio, Campanario, Glaus, Mühlleitner, Spira, Streicher 18;

# HH: NNLO HTL Combined with NLO SM

Differential NNLO HTL + NLO SM

Top quark mass effects studied using 3 different approximations



Grazzini, Heinrich, SJ, Kallweit, Kerner, Lindert, Mazzitelli 18; (+NNLL) de Florian, Mazzitelli 18;

$\sqrt{s}$	13 TeV	14 TeV	27 TeV	100 TeV
NLO [fb]	27.78 $^{+13.8\%}_{-12.8\%}$	32.88 $^{+13.5\%}_{-12.5\%}$	127.7 $^{+11.5\%}_{-10.4\%}$	1147 $^{+10.7\%}_{-9.9\%}$
NLO <sub>FTapprox</sub> [fb]	28.91 $^{+15.0\%}_{-13.4\%}$	34.25 $^{+14.7\%}_{-13.2\%}$	134.1 $^{+12.7\%}_{-11.1\%}$	1220 $^{+11.9\%}_{-10.6\%}$
NNLO <sub>NLO-i</sub> [fb]	32.69 $^{+5.3\%}_{-7.7\%}$	38.66 $^{+5.3\%}_{-7.7\%}$	149.3 $^{+4.8\%}_{-6.7\%}$	1337 $^{+4.1\%}_{-5.4\%}$
NNLO <sub>B-proj</sub> [fb]	33.42 $^{+1.5\%}_{-4.8\%}$	39.58 $^{+1.4\%}_{-4.7\%}$	154.2 $^{+0.7\%}_{-3.8\%}$	1406 $^{+0.5\%}_{-2.8\%}$
NNLO <sub>FTapprox</sub> [fb]	31.05 $^{+2.2\%}_{-5.0\%}$	36.69 $^{+2.1\%}_{-4.9\%}$	139.9 $^{+1.3\%}_{-3.9\%}$	1224 $^{+0.9\%}_{-3.2\%}$
$M_t$ unc. NNLO <sub>FTapprox</sub>	$\pm 2.6\%$	$\pm 2.7\%$	$\pm 3.4\%$	$\pm 4.6\%$
NNLO <sub>FTapprox</sub> /NLO	1.118	1.116	1.096	1.067

## 1) NNLO<sub>NLO-i</sub>

Rescale NLO by  $K_{\text{NNLO}} = \text{NNLO}_{\text{HTL}}/\text{NLO}_{\text{HTL}}$

## 2) NNLO<sub>B-proj</sub>

Project real radiation contributions to Born configurations, rescale by  $\text{LO}/\text{LO}_{\text{HTL}}$

## 3) NNLO<sub>FTapprox</sub>

NNLO HTL correction rescaled for each multiplicity by:

$$\mathcal{R}(ij \rightarrow HH + X) = \frac{\mathcal{A}_{\text{Full}}^{\text{Born}}(ij \rightarrow HH + X)}{\mathcal{A}_{\text{HEFT}}^{(0)}(ij \rightarrow HH + X)}$$



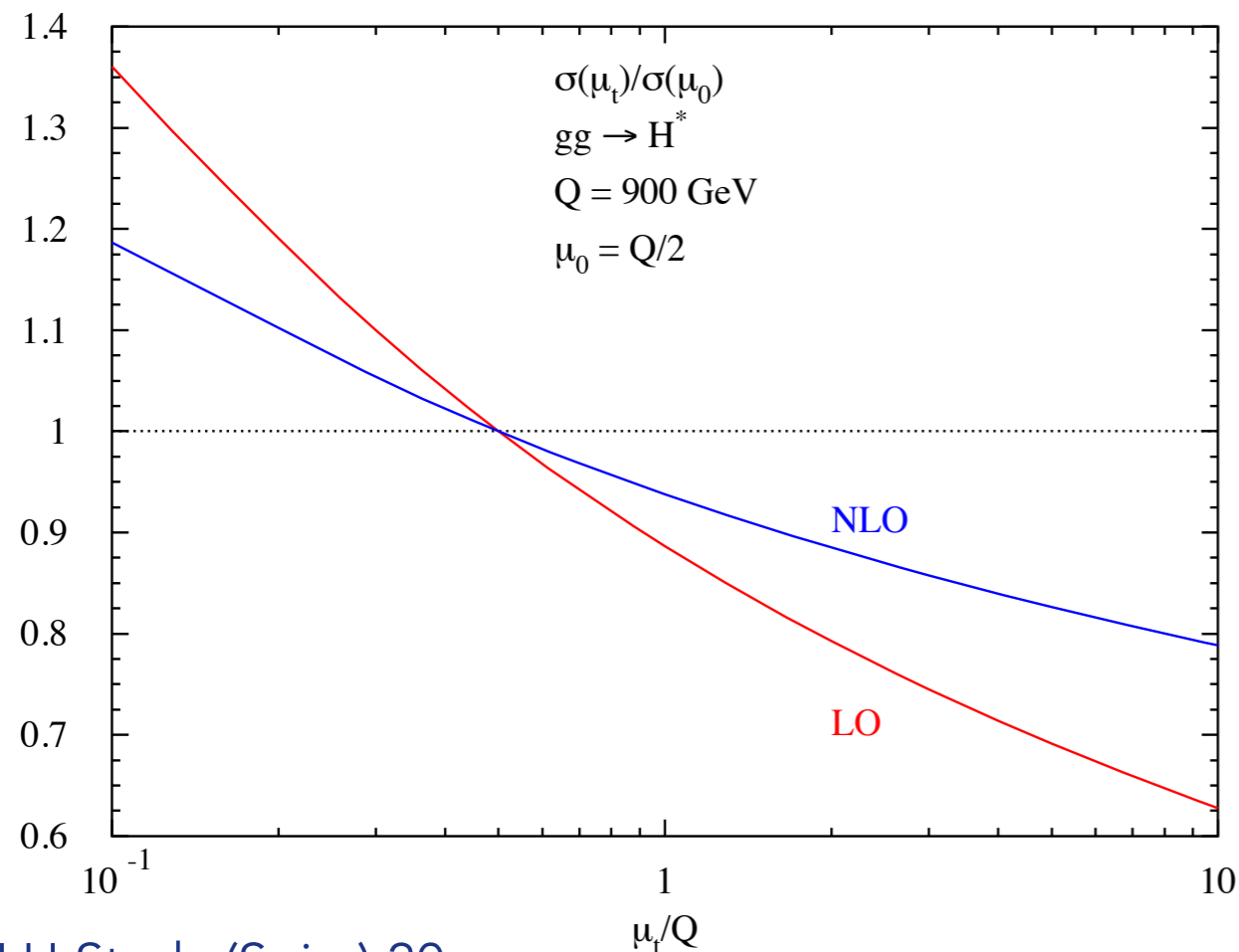
# Mass Scheme Dependence

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# H\* Mass Scheme Uncertainties

LH study of mass scheme dependence currently being finalised, attempts to highlight the issue by examining: H\*, HH, HJ, ZZ

Consider  $gg \rightarrow H^*$  @  $Q = 900$  GeV:



LH Study (Spira) 20

Suggests that mass scheme uncertainties could be quite sizeable for many (loop-induced) Higgs processes with scales  $\gtrsim m_T$

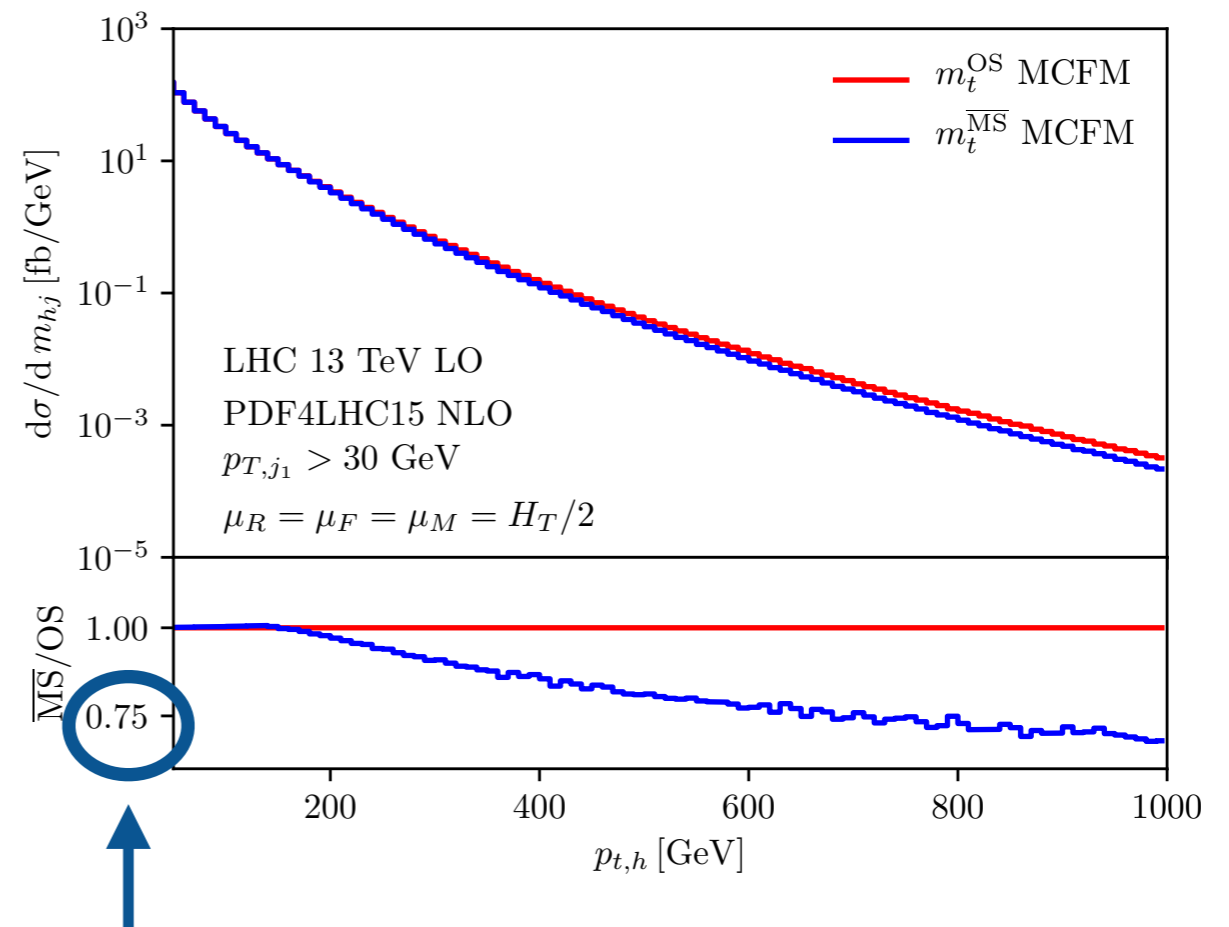
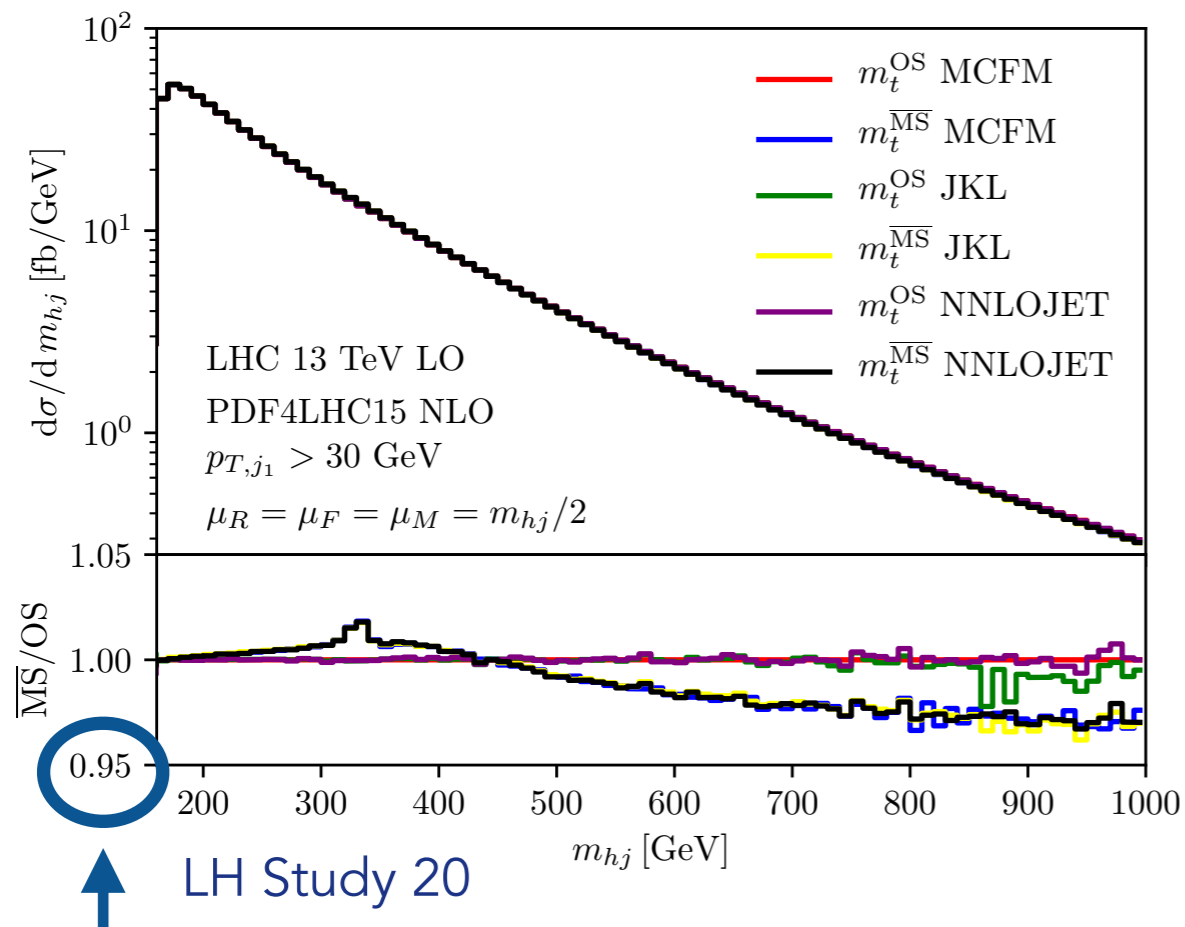
$\sigma(gg \rightarrow H^*)$ [pb]	$Q = 125$ GeV	$Q = 900$ GeV
LO	$18.43^{+0.8\%}_{-1.1\%}$	$0.139^{+0.0\%}_{-36.0\%}$
NLO	$42.17^{+0.4\%}_{-0.5\%}$	$0.230^{+0.0\%}_{-22.3\%}$



Similarly to HH production,  $m_T$  scheme dependence reduced by "only" factor  $\sim 2$

**Note:** For on-shell  $H(125)$  production uncertainty is tiny

# HJ Mass Scheme Uncertainties



Mass scheme uncertainty hugely different for each distribution

Suspicion:  $m_{h_j}$  is mostly not probing the top quark loop above threshold, smaller sensitivity to mass effects (?)

