

# Charm Physics Confronts High- $p_T$ Lepton Tails

Admir Greljo

2003.12421

BSM Forum, 16.04.2020

# Introduction

## QUARKS

$$c \quad I(J^P) = 0(1/2^+)$$

Charge =  $\frac{2}{3} e$  Charm = +1

- '70 The GIM mechanism
- '74 November revolution  $J/\psi$
- '19 CP violation

- Charm is a cornerstone of the SM
- A unique arena for QCD and Flavor physics

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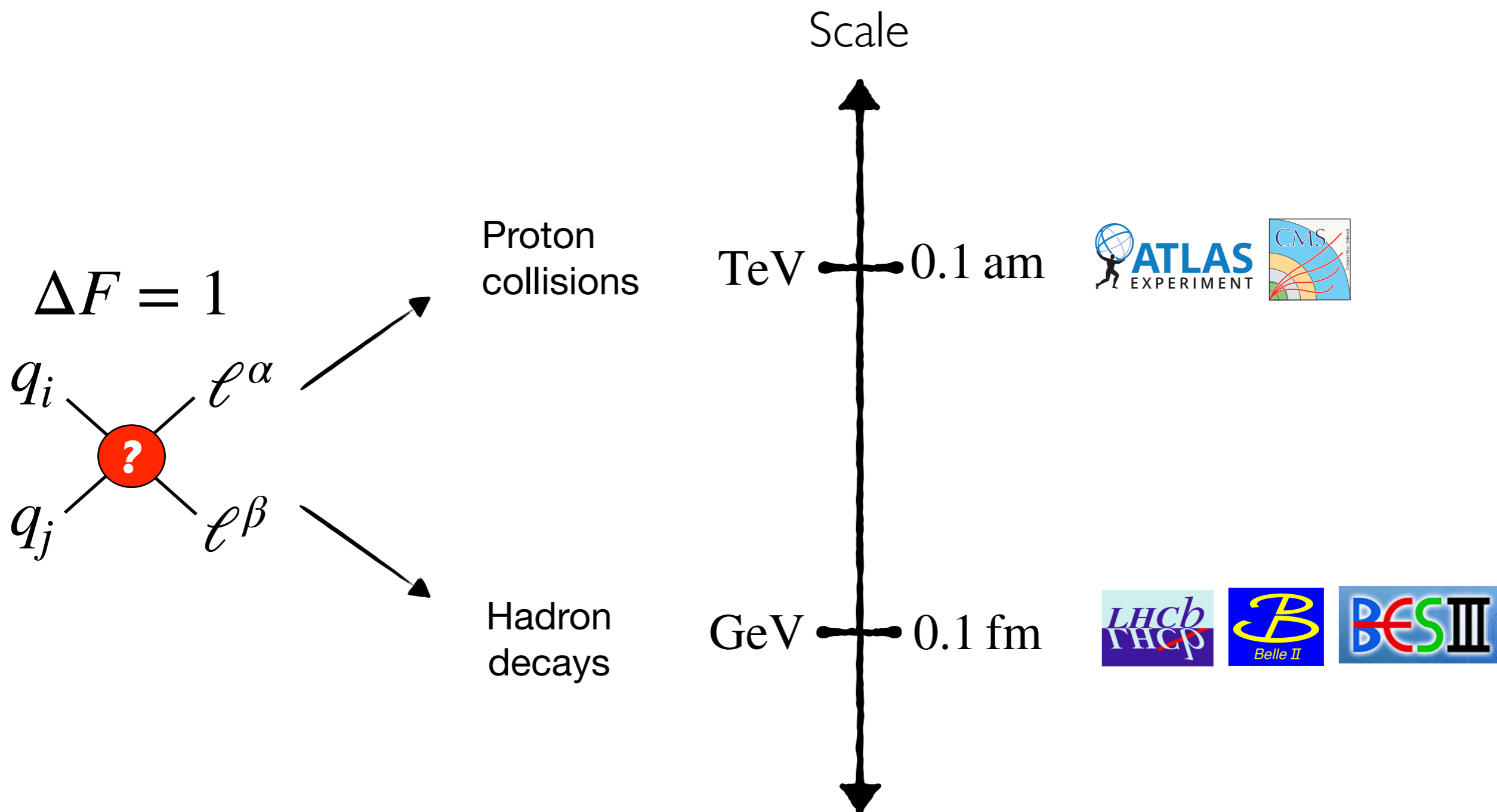
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Q: How unique is the charm sector as a probe of NP within the zoo of flavor and collider phenomenology?

Q: What is the role of charm in a broader quest for a microscopic theory beyond the SM?

# Opportunities across the scales



# Contemporary experiments

## High-energy Frontier



TeV

3 x more luminosity by '23  
20 x by '35

Harvesting large statistics!

## High-intensity Frontier



GeV

5 x more  
by '30

'19 - '25  
50 x Belle

10 x more

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Javier Fuentes-Martin, Admir Greljo, Jorge Martin Camalich, Jose David Ruiz-Alvarez

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# 2003.12421: *The highlight*

## Rare FCNC $c \rightarrow u l^+ l^-$ transition

- Tiny SM rates
- short-distance contribution negligible, efficient
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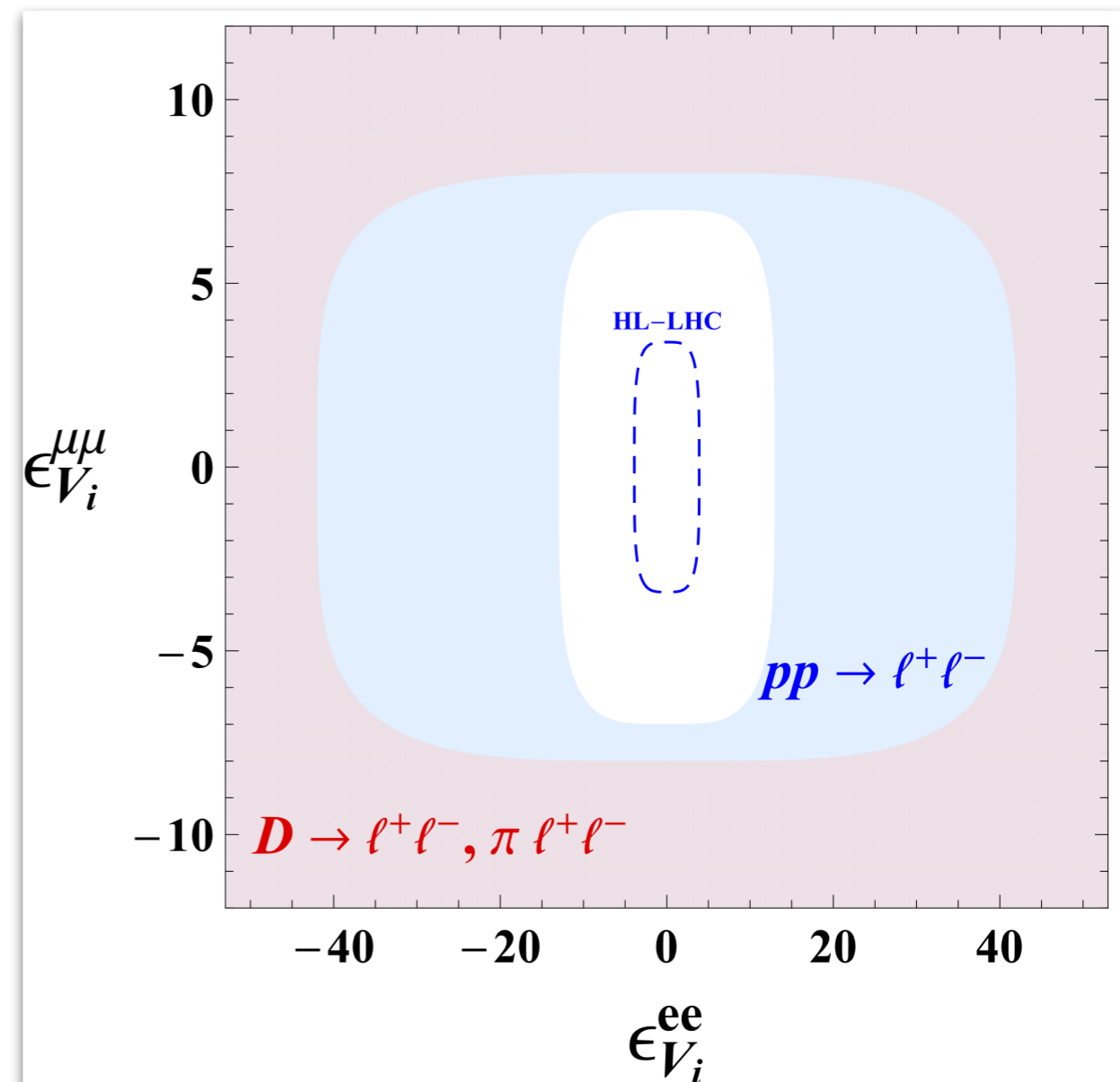
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## ***Charged currents***

$$c \rightarrow d^i \bar{e}^\alpha \nu^\beta$$

# Theoretical framework

## 2.2 The low-energy effective theory

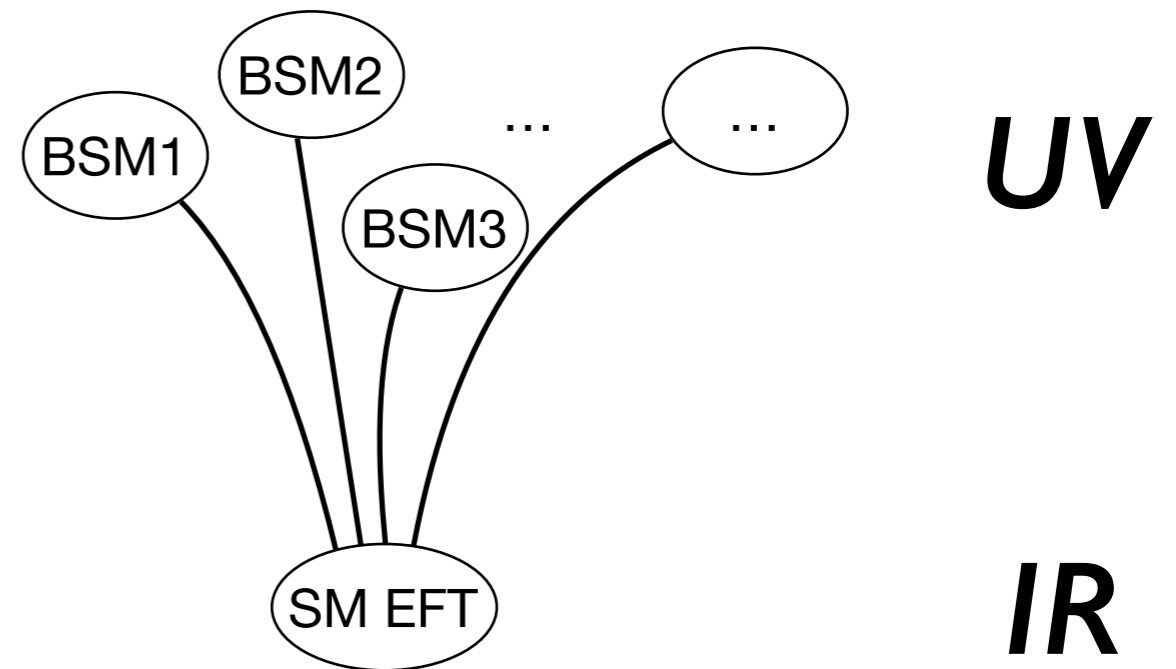
$$\mathcal{L}_{\text{CC}} = -\frac{4G_F}{\sqrt{2}} V_{ci} \left[ (1 + \epsilon_{V_L}^{\alpha\beta i}) \mathcal{O}_{V_L}^{\alpha\beta i} + \epsilon_{V_R}^{\alpha\beta i} \mathcal{O}_{V_R}^{\alpha\beta i} + \epsilon_{S_L}^{\alpha\beta i} \mathcal{O}_{S_L}^{\alpha\beta i} + \epsilon_{S_R}^{\alpha\beta i} \mathcal{O}_{S_R}^{\alpha\beta i} + \epsilon_T^{\alpha\beta i} \mathcal{O}_T^{\alpha\beta i} \right] + \text{h.c.},$$

$$\begin{aligned} \epsilon_{X,SM}^{\alpha\beta i} = 0 \text{ for all } X \quad & \mathcal{O}_{V_L}^{\alpha\beta i} = (\bar{e}_L^\alpha \gamma_\mu \nu_L^\beta) (\bar{c}_L \gamma^\mu d_L^i), & \mathcal{O}_{V_R}^{\alpha\beta i} &= (\bar{e}_L^\alpha \gamma_\mu \nu_L^\beta) (\bar{c}_R \gamma^\mu d_R^i), \\ & \mathcal{O}_{S_L}^{\alpha\beta i} = (\bar{e}_R^\alpha \nu_L^\beta) (\bar{c}_R d_L^i), & \mathcal{O}_{S_R}^{\alpha\beta i} &= (\bar{e}_R^\alpha \nu_L^\beta) (\bar{c}_L d_R^i), \\ & \mathcal{O}_T^{\alpha\beta i} = (\bar{e}_R^\alpha \sigma_{\mu\nu} \nu_L^\beta) (\bar{c}_R \sigma^{\mu\nu} d_L^i). \end{aligned}$$

# Theoretical framework

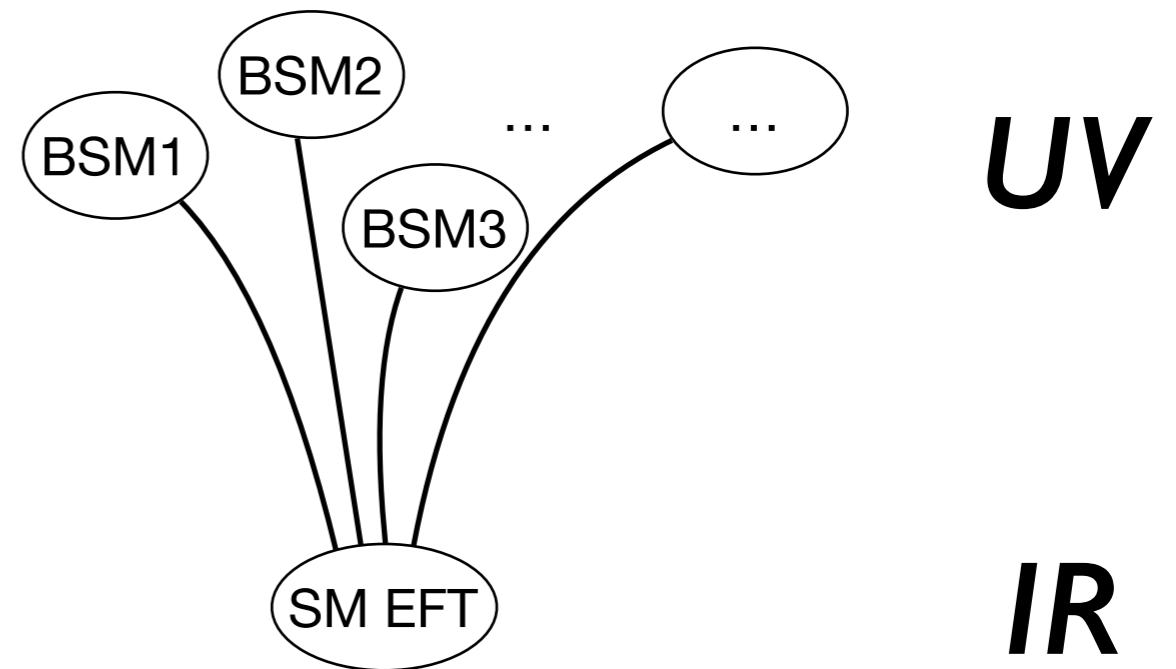
## 2.1 The high-energy effective theory

$$\mathcal{L}_{\text{SM EFT}} \supset \frac{1}{v^2} \sum_k C_k \mathcal{O}_k$$



# Theoretical framework

## 2.1 The high-energy effective theory



$$\mathcal{L}_{\text{SMEFT}} \supset \frac{1}{v^2} \sum_k C_k \mathcal{O}_k$$

- The full list of 4F operators <sup>(\*) Warsaw basis</sup>

$$\mathcal{O}_{lq}^{(3)} = (\bar{l}_L \gamma_\mu \tau^I l_L) (\bar{q}_L \gamma^\mu \tau^I q_L),$$

$$\mathcal{O}_{lequ}^{(1)} = (\bar{l}_L^p e_R) \epsilon_{pr} (\bar{q}_L^r u_R),$$

$$\mathcal{O}_{ledq} = (\bar{l}_L e_R) (\bar{d}_R q_L),$$

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- W vertex correction

$$(\phi^\dagger \overset{\leftrightarrow}{D}_\mu^I \phi) (\bar{q}_L \gamma^\mu \tau^I q_L)$$

$$(\tilde{\phi}^\dagger i D_\mu \phi) (\bar{u}_R \gamma^\mu d_R)$$



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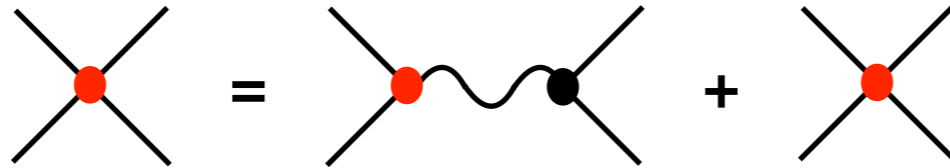
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## Matching



$$\mathcal{O}_{V_L}^{\alpha\beta i} = (\bar{e}_L^\alpha \gamma_\mu \nu_L^\beta) (\bar{c}_L \gamma^\mu d_L^i),$$

$$\mathcal{O}_{S_L}^{\alpha\beta i} = (\bar{e}_R^\alpha \nu_L^\beta) (\bar{c}_R d_L^i),$$

$$\mathcal{O}_T^{\alpha\beta i} = (\bar{e}_R^\alpha \sigma_{\mu\nu} \nu_L^\beta) (\bar{c}_R \sigma^{\mu\nu} d_L^i).$$

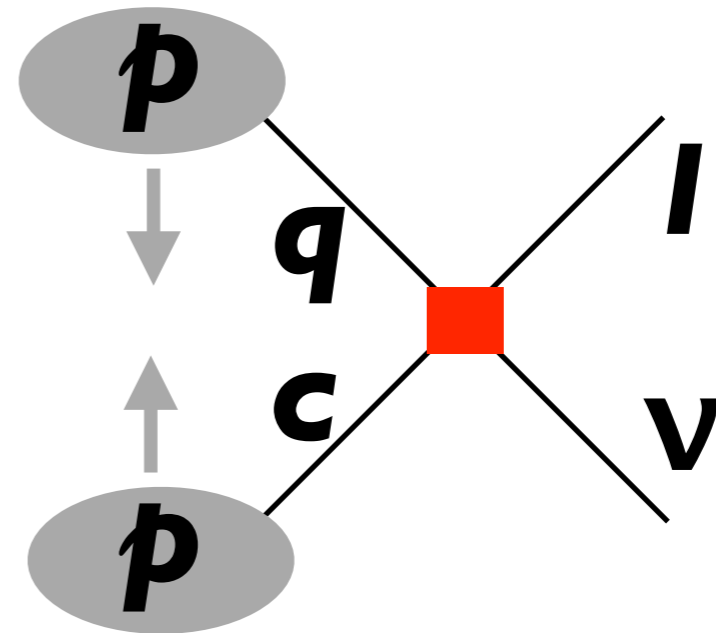
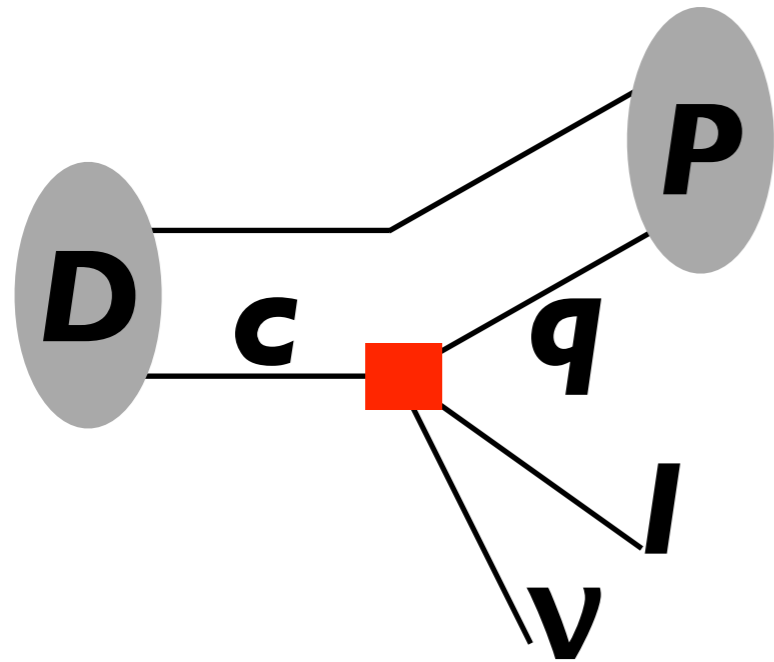
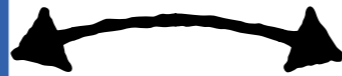
$$\mathcal{O}_{V_R}^{\alpha\beta i} = (\bar{e}_L^\alpha \gamma_\mu \nu_L^\beta) (\bar{c}_R \gamma^\mu d_R^i),$$

$$\mathcal{O}_{S_R}^{\alpha\beta i} = (\bar{e}_R^\alpha \nu_L^\beta) (\bar{c}_L d_R^i),$$

- SMEFT 4F operators match to  $V_L, S_R, S_L, T$  but not to  $V_R$
- $V_L$  and  $V_R$  receive chirality-preserving  $W$  vertex corrections
- Effects from chirality-flipping vertex corrections are beyond dim-6  $\bar{\psi} \sigma^{\mu\nu} \psi \phi F_{\mu\nu}$
- SMEFT effects in leptonic  $W$  couplings,  $G_F$ , and CKM determination neglected
- RGEs allow to connect low and high  $p_T$
- RGE effects sizeable for scalar and tensor operators

Caveats beyond this setup will be discussed later

**Crossing symmetry**



**Charmed  
meson decays**

# Charmed meson decays

$$c \rightarrow d^i \bar{e}^\alpha \nu^\beta$$

---

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- QCD invariant under Lorentz symmetry and Parity =>

$$\langle 0 | \bar{q} \sigma^{\mu\nu} q | D \rangle = 0, \quad \langle 0 | \bar{q} \gamma^\mu q | D \rangle = 0, \quad \langle 0 | \bar{q} q | D \rangle = 0$$

- Leptonic decays sensitive only to axial vector and pseudo scalar operators

$$\epsilon_A^{\alpha\beta i} = \epsilon_{V_R}^{\alpha\beta i} - \epsilon_{V_L}^{\alpha\beta i} \quad \epsilon_P^{\alpha\beta i} = \epsilon_{S_R}^{\alpha\beta i} - \epsilon_{S_L}^{\alpha\beta i}$$

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$$\text{BR}(D^+ \rightarrow \bar{e}^\alpha \nu^\alpha) = \tau_{D^+} \frac{m_{D^+} m_\alpha^2 f_D^2 G_F^2 |V_{cd}|^2 \beta_\alpha^4}{8\pi} \left| 1 - \epsilon_A^{\alpha d} + \frac{m_D^2}{m_\alpha(m_c + m_u)} \epsilon_P^{\alpha d} \right|^2$$

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■ LQCD: Precise decay constants

$$f_D = 212.0(7) \text{ MeV}$$

$$f_{D_s} = 249.9(5) \text{ MeV}$$

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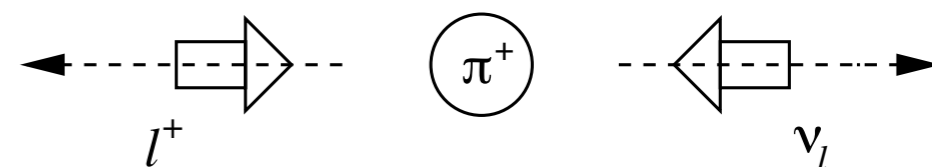
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■ LQCD: Precise decay constants

■ Chirality suppression for the axial vector

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$$A : \bar{e}_L \gamma^\mu \nu_L, \quad P : \bar{e}_R \nu_L$$

# Charmed meson decays

$$c \rightarrow d^i \bar{e}^\alpha \nu^\beta$$

● Leptonic decays:  $D_{(s)} \rightarrow \bar{e}^\alpha \nu$

$i$	$\alpha$	Branching ratios, see PDG
$d$	$e$	(*) upper limit, CLEO
	$\mu$	BES3
	$\tau$	BES3
$s$	$e$	(*) upper limit, BELLE
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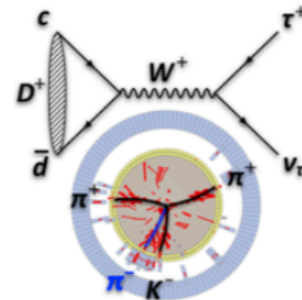
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Editors' Suggestion

## Observation of the Leptonic Decay $D^+ \rightarrow \tau^+ \nu_\tau$

M. Ablikim *et al.* (BESIII Collaboration)

Phys. Rev. Lett. **123**, 211802 (2019) – Published 22 November 2019



The first observation of the two-body decay of a charm meson into a tau and its neutrino allow for a new probe of lepton flavor universality.

[Show Abstract +](#)

# Charmed meson decays

$$c \rightarrow d^i \bar{e}^\alpha \nu^\beta$$

Leptonic decays:  $D_{(s)} \rightarrow \bar{e}^\alpha \nu$

$i$	$\alpha$	$\epsilon_V^{\alpha i}$	$\epsilon_A^{\alpha i}$	$\epsilon_S^{\alpha i}$	$\epsilon_P^{\alpha i}$	$\epsilon_T^{\alpha i}$
$d$	$e$		$[-32, 34]$		$[-0.005, 0.005]$	
	$\mu$		$[-0.013, 0.07]$		$[-0.0024, 0.0004]$	
	$\tau$		$[-0.27, 0.21]$		$[-0.11, 0.15]$	
$s$	$e$		$[-27, 29]$		$[-0.005, 0.004]$	
	$\mu$		$[-0.07, 0.02]$		$[-0.0007, 0.0022]$	
	$\tau$		$[-0.07, 0.014]$		$[-0.008, 0.04]$	

95% CL ranges on WCs at 2 GeV (one parameter fit).

- Stringent limits on P operators
- Limits on A depend strongly on the lepton flavour

# Charmed meson decays

$$c \rightarrow d^i \bar{e}^\alpha \nu^\beta$$

- Semileptonic decays:  $D \rightarrow \pi(K) \bar{\ell} \nu$

- QCD invariant under Lorentz symmetry and Parity =>

$$\langle P_i | \bar{q} \gamma^\mu \gamma^5 q | D \rangle = 0, \quad \langle P_i | \bar{q} \gamma^5 q | D \rangle = 0$$

- Semileptonic decays sensitive to vector, scalar and tensor operators

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$$\frac{\text{BR}(D \rightarrow P_i \bar{\ell}^\alpha \nu^\alpha)}{\text{BR}_{\text{SM}}} = |1 + \epsilon_V^{\alpha i}|^2 + 2 \text{Re} [(1 + \epsilon_V^{\alpha i})(x_S \epsilon_S^{\alpha i*} + x_T \epsilon_T^{\alpha i*})] + y_S |\epsilon_S^{\alpha i}|^2 + y_T |\epsilon_T^{\alpha i}|^2$$

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■ LQCD: Form factors

$P$	$\alpha$	$\text{BR}_{\text{SM}}$	$x_S$	$x_T$	$y_S$	$y_T$
$\pi^-$	$e$	$2.65(18) \cdot 10^{-3}$	$1.12(10) \cdot 10^{-3}$	$1.21(15) \cdot 10^{-3}$	2.74(22)	1.14(21)
	$\mu$	$2.61(17) \cdot 10^{-3}$	0.228(19)	0.23(3)	2.73(18)	1.15(22)
$K^-$	$e$	$3.48(26) \cdot 10^{-2}$	$1.29(8) \cdot 10^{-3}$	$1.18(11) \cdot 10^{-3}$	2.00(11)	0.69(8)
	$\mu$	$3.39(25) \cdot 10^{-2}$	0.251(16)	0.224(20)	2.00(11)	0.71(8)

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- The largest available phase space  $m_{D^+} - m_{\pi^0} \simeq 1.735 \text{ GeV}$ .
- No limits on tauonic V, S, T operators  
[Caveat: Excited resonances or  $D_{(s)} \rightarrow \tau \nu \gamma$  ]

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- Semileptonic decays:  $D \rightarrow \pi(K) \bar{\ell} \nu$

$i$	$\alpha$	$\epsilon_V^{\alpha i}$	$\epsilon_A^{\alpha i}$	$\epsilon_S^{\alpha i}$	$\epsilon_P^{\alpha i}$	$\epsilon_T^{\alpha i}$
$d$	$e$	$[-0.02, 0.11]$		$[-0.29, 0.29]$		$[-0.5, 0.5]$
	$\mu$	$[-0.06, 0.07]$		$[-0.33, 0.17]$		$[-0.6, 0.22]$
	$\tau$	—		—		—
$s$	$e$	$[-0.07, 0.08]$		$[-0.29, 0.29]$		$[-0.5, 0.5]$
	$\mu$	$[-0.09, 0.06]$		$[-0.4, 0.16]$		$[-0.9, 0.22]$
	$\tau$	—		—		—

95% CL ranges on WCs at 2 GeV (one parameter fit).

- Limits on scalar and tensor operators are weak, dominated by the quadratic contribution.
- Vector operators constrained at the few percent level. Form factor errors relevant.
- Future improvements  $\sim 3x$  on the rates at BESIII. Challenge for LQCD to keep up.



# Charmed meson decays

$$c \rightarrow d^i \bar{e}^\alpha \nu^\beta$$

- Leptonic decays:  $D_{(s)} \rightarrow \bar{e}^\alpha \nu$
- Semileptonic decays:  $D \rightarrow \pi(K) \bar{\ell} \nu$

$i$	$\alpha$	$\epsilon_V^{\alpha i}$	$\epsilon_A^{\alpha i}$	$\epsilon_S^{\alpha i}$	$\epsilon_P^{\alpha i}$	$\epsilon_T^{\alpha i}$
$d$	$e$	$[-0.02, 0.11]$	$[-32, 34]$	$[-0.29, 0.29]$	$[-0.005, 0.005]$	$[-0.5, 0.5]$
	$\mu$	$[-0.06, 0.07]$	$[-0.013, 0.07]$	$[-0.33, 0.17]$	$[-0.0024, 0.0004]$	$[-0.6, 0.22]$
	$\tau$	—	$[-0.27, 0.21]$	—	$[-0.11, 0.15]$	—
$s$	$e$	$[-0.07, 0.08]$	$[-27, 29]$	$[-0.29, 0.29]$	$[-0.005, 0.004]$	$[-0.5, 0.5]$
	$\mu$	$[-0.09, 0.06]$	$[-0.07, 0.02]$	$[-0.4, 0.16]$	$[-0.0007, 0.0022]$	$[-0.9, 0.22]$
	$\tau$	—	$[-0.07, 0.014]$	—	$[-0.008, 0.04]$	—

95% CL ranges on WCs at 2 GeV (one parameter fit).

# Charmed meson decays

$$c \rightarrow d^i \bar{e}^\alpha \nu^\beta$$

- Leptonic decays:  $D_{(s)} \rightarrow \bar{e}^\alpha \nu$
- Semileptonic decays:  $D \rightarrow \pi(K) \bar{\ell} \nu$
- Not considered / future directions
  - $D > V$ , no lattice QCD predictions
  - Baryonic  $\Lambda_c$  decays, data not precise
  - Kinematic distributions

# ***Charmed meson decays***

- In the UV, the relevant operator basis is the “chiral basis” not the “parity basis”

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**Vector**  $\epsilon_{VL}^{\alpha\beta i}$

$$\mathcal{O}_{lq}^{(3)} = (\bar{l}_L \gamma_\mu \tau^I l_L) (\bar{q}_L \gamma^\mu \tau^I q_L)$$

- Electron: Semileptonic
- Muon: Semileptonic and leptonic comparable
- Tau: Leptonic

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## Scalar, Tensor

$$\mathcal{O}_{ledq} = (\bar{l}_L e_R) (\bar{d}_R q_L),$$

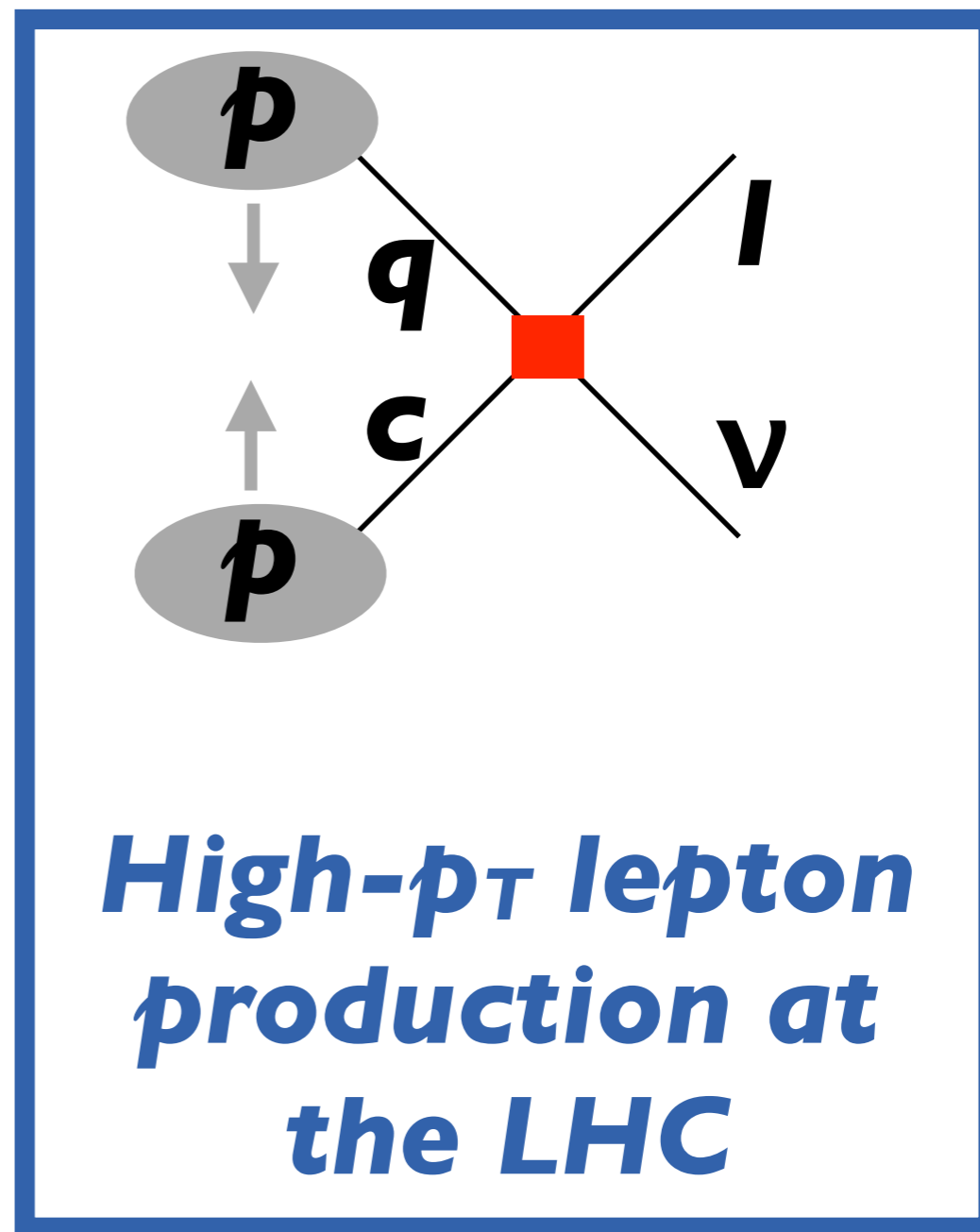
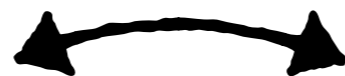
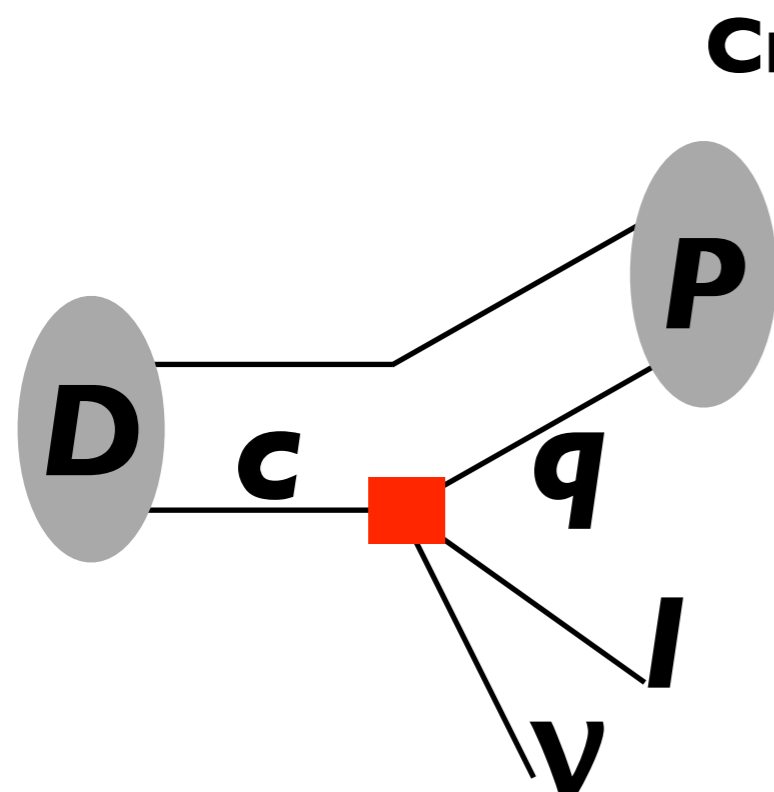
$$\mathcal{O}_{lequ}^{(3)} = (\bar{l}_L^p \sigma_{\mu\nu} e_R) \epsilon_{pr} (\bar{q}_L^r \sigma^{\mu\nu} u_R),$$

$$\mathcal{O}_{lequ}^{(1)} = (\bar{l}_L^p e_R) \epsilon_{pr} (\bar{q}_L^r u_R),$$

$i$	$\alpha$	$\epsilon_{S_L}^{\alpha i} (-\epsilon_{S_R}^{\alpha i}) \times 10^3$	$\epsilon_T^{\alpha i} \times 10^2$
$d$	$e$	$[-2.5, 2.7]$	$[-1.6, 1.5]$
	$\mu$	$[-0.2, 1.2]$	$[-0.7, 0.13]$
	$\tau$	$[-70, 60]$	$[-33, 44]$
$s$	$e$	$[-2.0, 2.2]$	$[-1.3, 1.2]$
	$\mu$	$[-1.1, 0.3]$	$[-0.2, 0.6]$
	$\tau$	$[-19, 4.0]$	$[-2.0, 12]$

95% CL ranges on WCs at 1 TeV (one parameter fit).

- RGE flow to P operator at low energies



# High- $p_T$ lepton production at the LHC

In the high-energy limit  $\sqrt{s} \gg m_W$

## W-vertex

Chirality preserving:  $\frac{1}{\Lambda^2} \psi^2 \phi D \phi$

$$4F \frac{1}{\Lambda^2} \psi^4$$

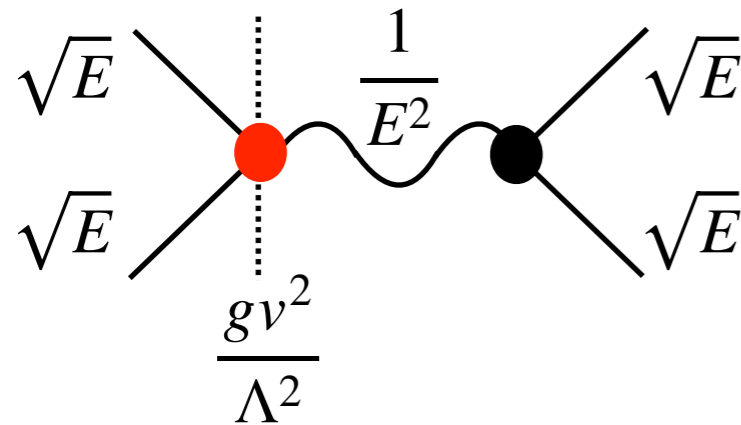
Chirality flipping:  $\frac{1}{\Lambda^2} \psi^2 \phi F$

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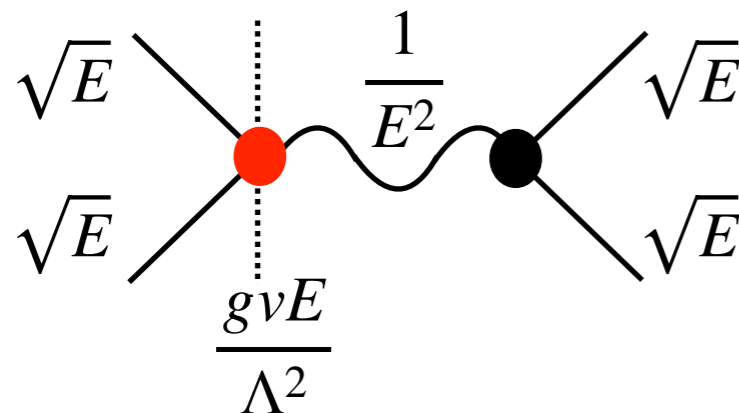


$$\mathcal{A} \sim \frac{m_W^2}{\Lambda^2}$$

$(\mathcal{A}_{SM} \sim g^2)$

$$4F \frac{1}{\Lambda^2} \psi^4$$

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$$\mathcal{A} \sim \frac{g\sqrt{s}}{\Lambda^2}$$

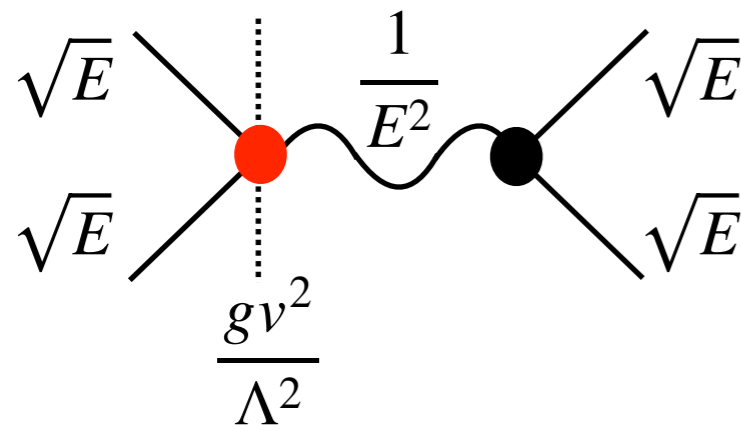


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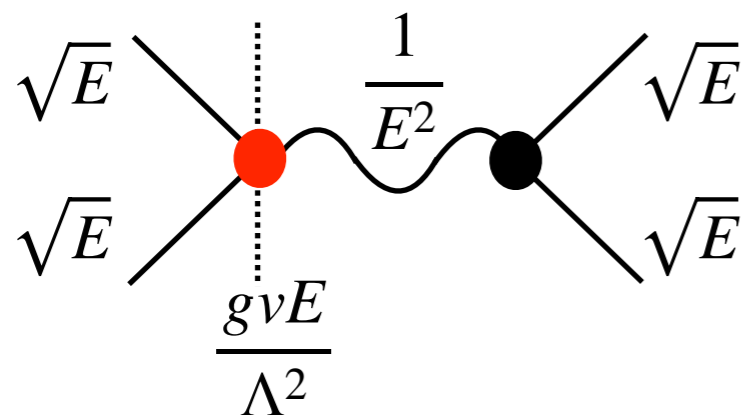
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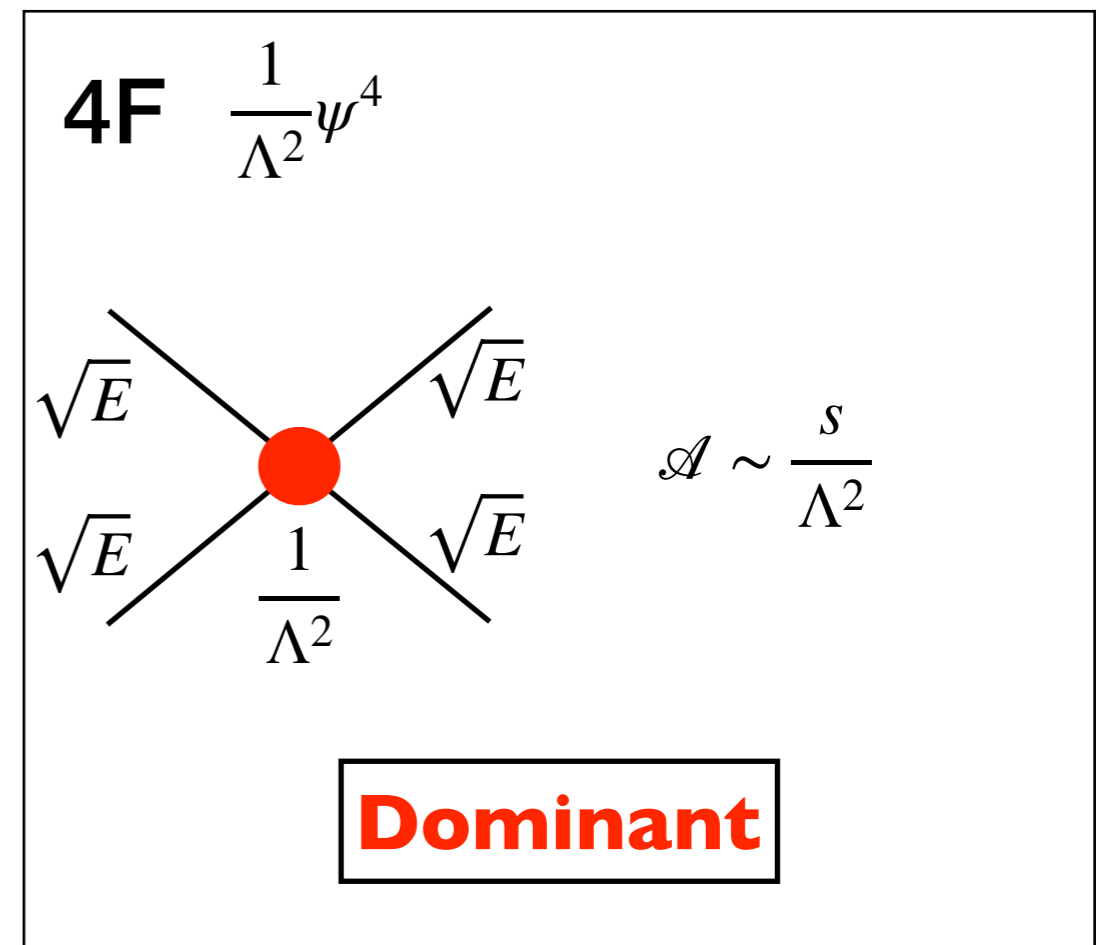
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Chirality flipping:  $\frac{1}{\Lambda^2} \psi^2 \phi F$



$$\mathcal{A} \sim \frac{g\sqrt{s}}{\Lambda^2}$$



Scattering amplitudes induced by 4F contact interactions grow with energy before the completion kicks in to insure unitarity.

## 4.1 Short-distance new physics in high- $p_T$ tails

- Partonic level cross section

$$\hat{\sigma}(s) = \frac{G_F^2 |V_{ij}|^2}{18\pi} s \left[ \left| \delta^{\alpha\beta} \frac{m_W^2}{s} - \epsilon_{V_L}^{\alpha\beta ij} \right|^2 + \frac{3}{4} (|\epsilon_{S_L}^{\alpha\beta ij}|^2 + |\epsilon_{S_R}^{\alpha\beta ij}|^2) + 4 |\epsilon_T^{\alpha\beta ij}|^2 \right]$$

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- In the relativistic limit, chiral fermions act as independent particles with definite helicity.
- Therefore, the interference among operators is achieved only when the operators match the same flavor and chirality for all four fermions.
- The lack of interference tends to increase the cross section in the high- $p_T$  tails, and allows to **set bounds on several NP operators simultaneously**.
- Different / complementary to charm decays.

Most of the bounds from  $D_{(S)}$  mesons decays depend on interference terms among different WCs, and it becomes difficult to break flat directions without additional observables.

## 4.1 Short-distance new physics in high- $p_T$ tails

- Five quark flavors accessible in the incoming proton PDFs

$$\mathcal{L}_{q_i \bar{q}_j}(\tau, \mu_F) = \int_{\tau}^1 \frac{dx}{x} f_{q_i}(x, \mu_F) f_{\bar{q}_j}(\tau/x, \mu_F)$$

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- The relative correction to the x-section in the tail

$$\frac{\Delta\sigma}{\sigma} \approx R_{ij} \times \frac{d_X \epsilon_X^2}{(m_W^2/s)^2}$$

$$R_{ij} \equiv \frac{(\mathcal{L}_{u_i \bar{d}_j} + \mathcal{L}_{d_j \bar{u}_i}) \times |V_{ij}|^2}{(\mathcal{L}_{u \bar{d}} + \mathcal{L}_{d \bar{u}}) \times |V_{ud}|^2}$$

$$d_X = 1, \frac{3}{4}, 4 \text{ for } X = V, S, T$$

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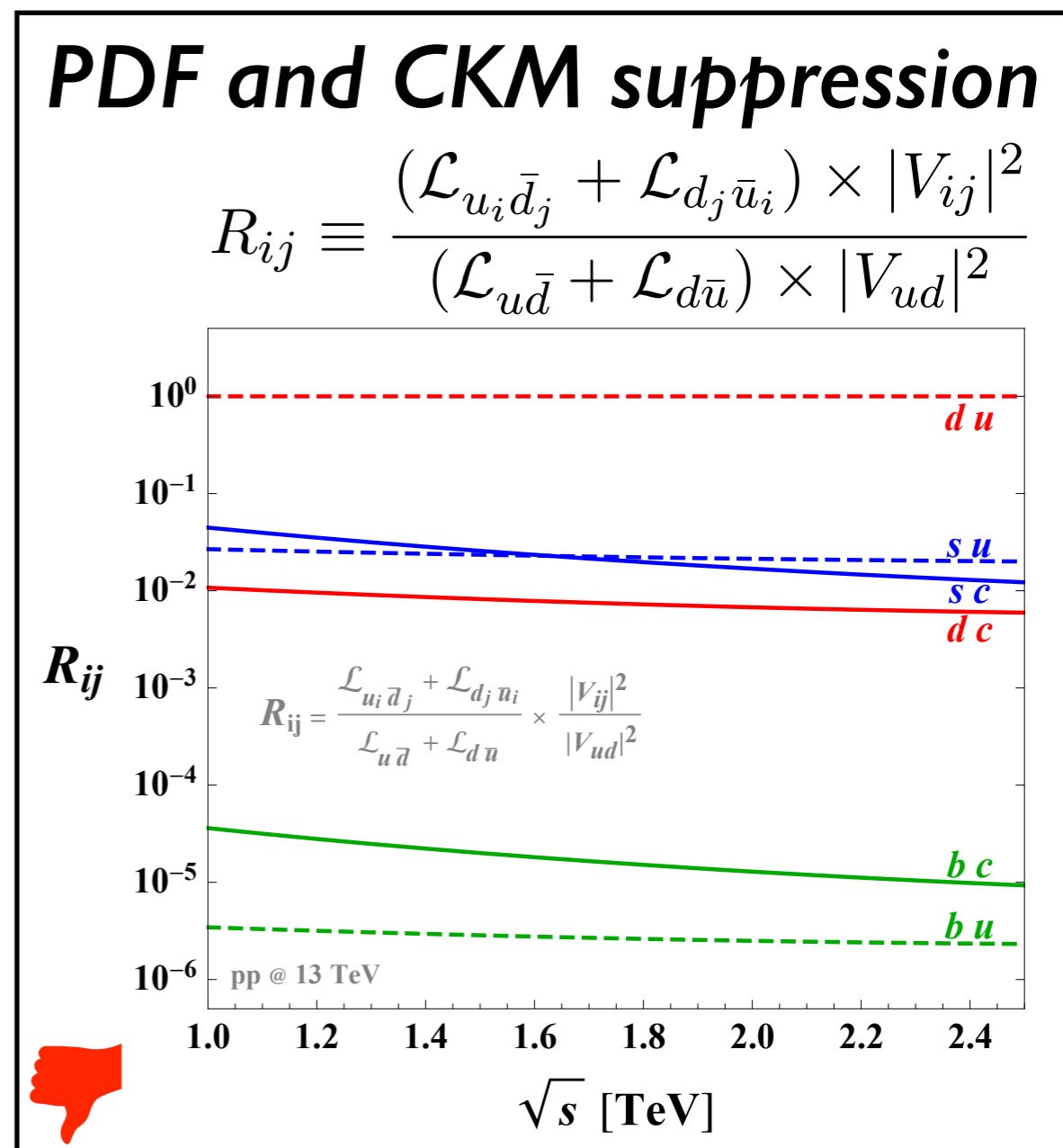
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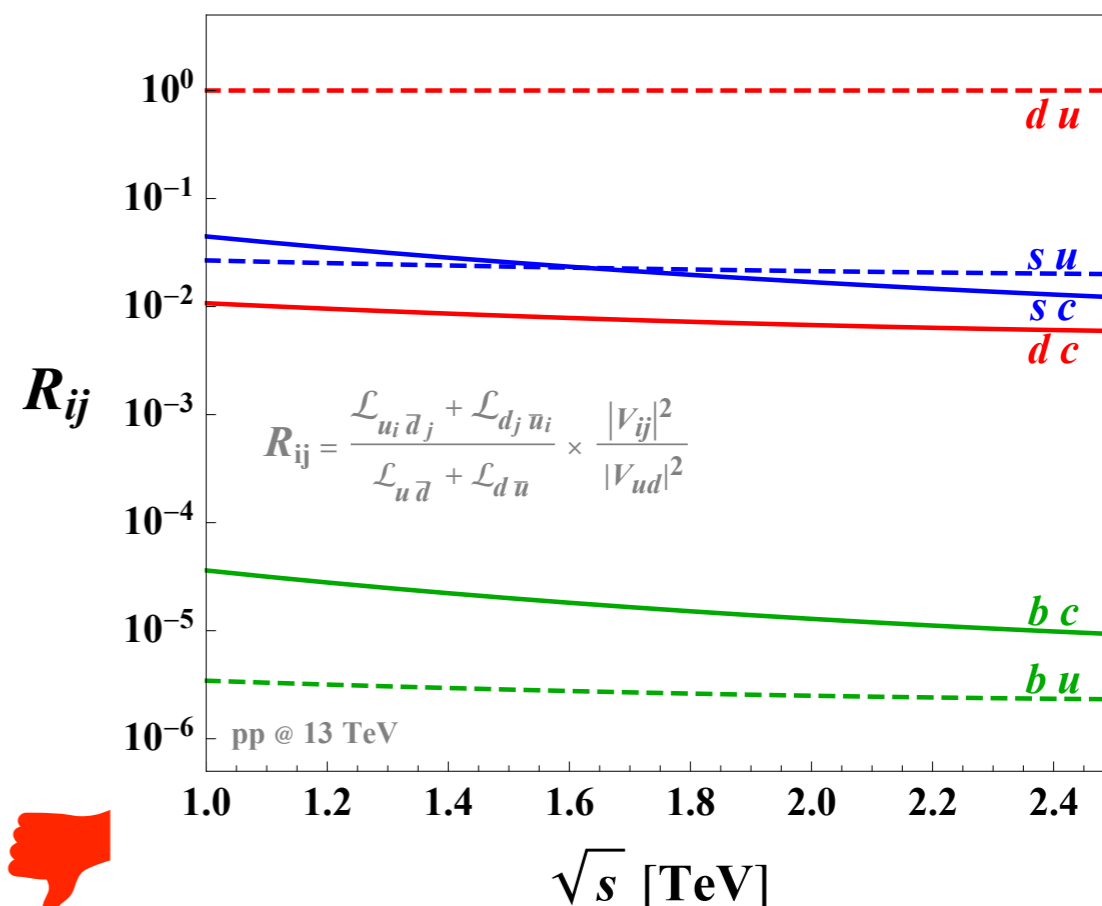
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**Energy enhancement**

  $(s/m_W^2)^2 \sim \mathcal{O}(10^5)$

**PDF and CKM suppression**

$$R_{ij} \equiv \frac{(\mathcal{L}_{u_i \bar{d}_j} + \mathcal{L}_{d_j \bar{u}_i}) \times |V_{ij}|^2}{(\mathcal{L}_{u \bar{d}} + \mathcal{L}_{d \bar{u}}) \times |V_{ud}|^2}$$



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$$d_X = 1, \frac{3}{4}, 4 \text{ for } X = V, S, T$$

$$\left| \frac{\Delta\sigma}{\sigma} \right|_{\text{tails}} \lesssim \mathcal{O}(0.1)$$

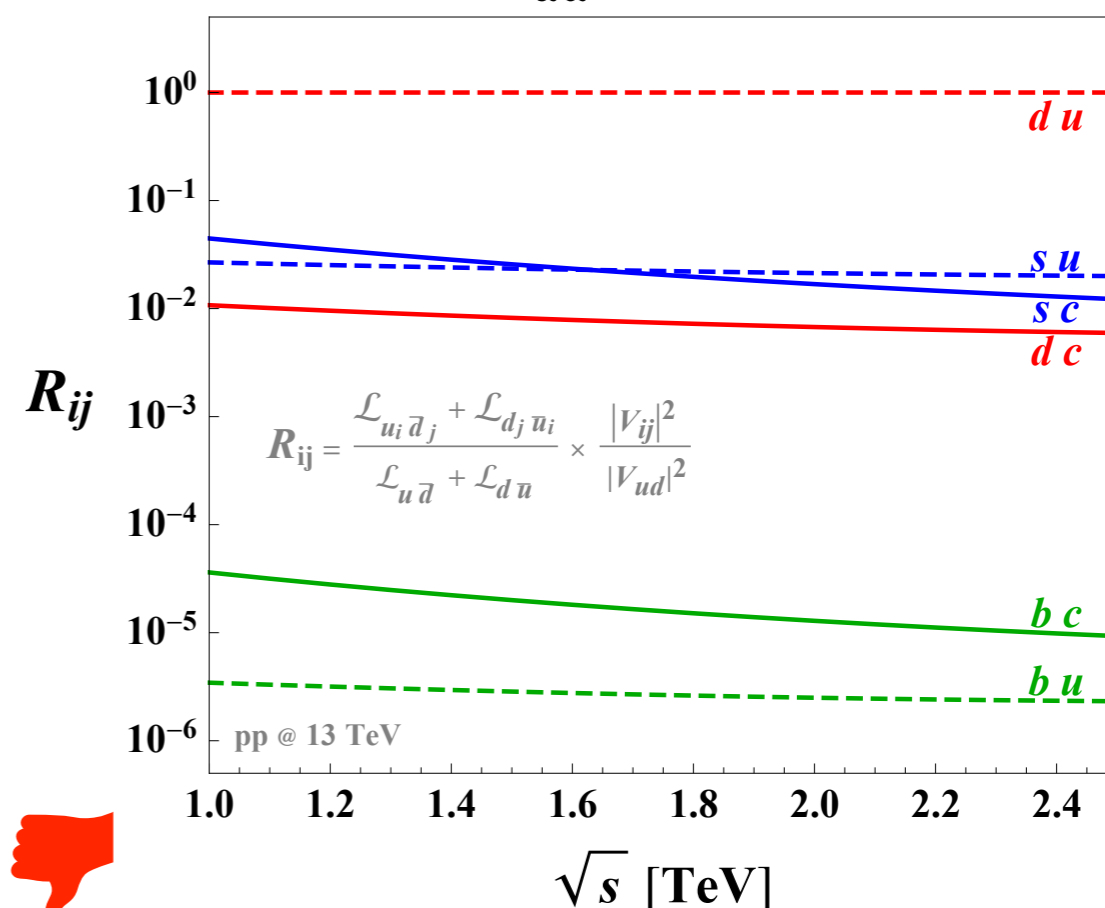
e.g.  $\rightarrow \epsilon_L^{CS} \lesssim \mathcal{O}(0.01)$

**Energy enhancement**

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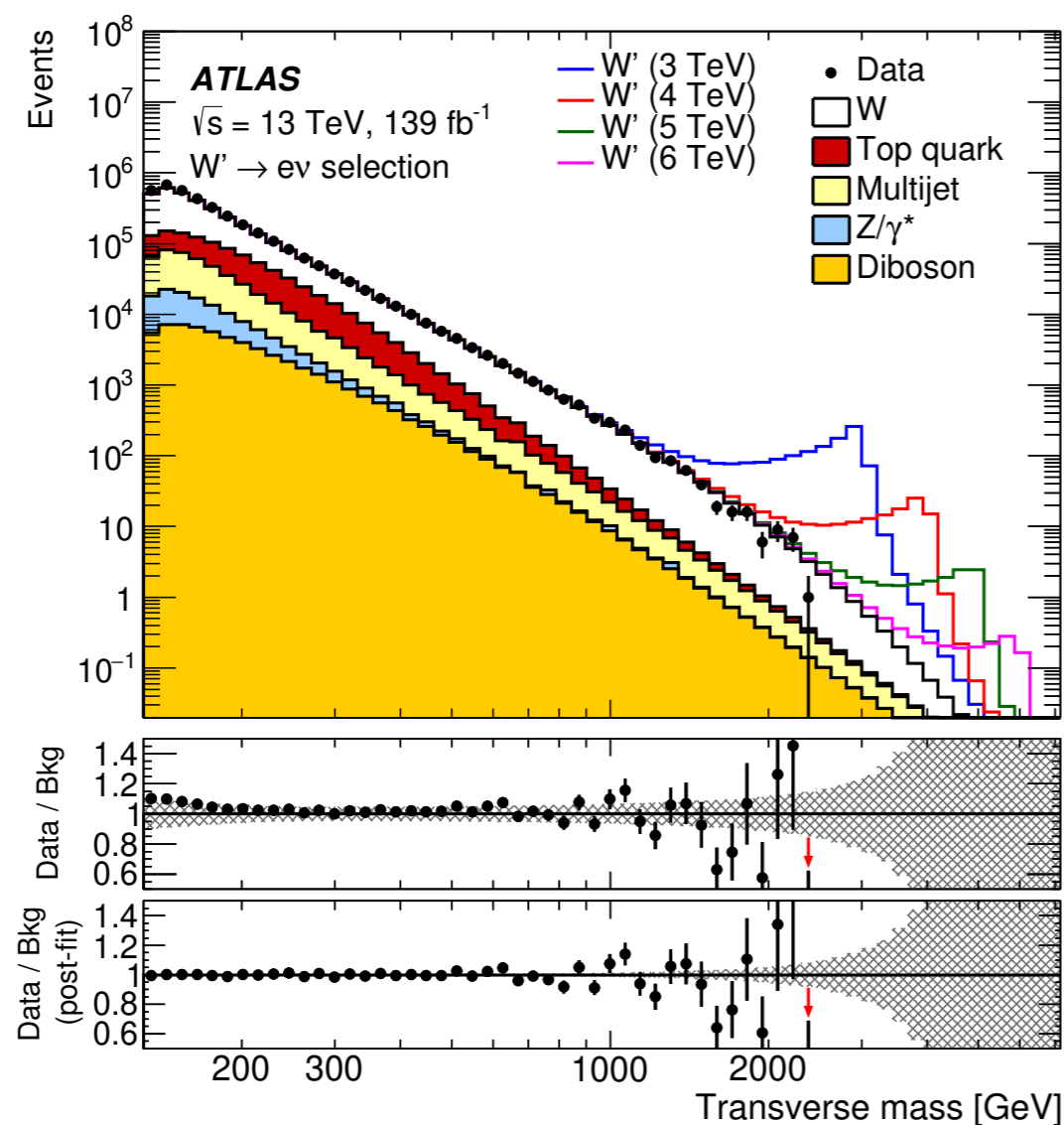
$$R_{ij} \equiv \frac{(\mathcal{L}_{u_i \bar{d}_j} + \mathcal{L}_{d_j \bar{u}_i}) \times |V_{ij}|^2}{(\mathcal{L}_{u \bar{d}} + \mathcal{L}_{d \bar{u}}) \times |V_{ud}|^2}$$





## 4.2 Recast of the existing experimental searches

- Charged (and neutral) Drell-Yan is extremely well measured at the LHC.
- We recast the available searches fitting the transverse mass distribution at the reco level.



Channel	Statistics [ $\text{fb}^{-1}$ ]	Experiment
$\tau\nu$	36	CMS
$e\nu, \mu\nu$	36	ATLAS
	139	ATLAS
	36	ATLAS
	36	CMS
$\tau\tau$	36	ATLAS
$\tau\tau, e\mu, e\tau, \mu\tau$	2.2	CMS
$ee, \mu\mu$	139	ATLAS
	140	CMS
$e\mu, e\tau, \mu\tau$	36	CMS
	36	ATLAS
	36	ATLAS

[Available data]

- Full-fledged simulations validated by reproducing the official SM prediction. The SM background systematics included conservatively. The modified frequentist CLs method used.

**4.2 Recast of the existing experimental searches**

$i$	$\alpha$	$\epsilon_{V_L}^{\alpha\alpha i} \times 10^2$	$ \epsilon_{V_L}^{\alpha\beta i}  \times 10^2$ ( $\alpha \neq \beta$ )	$ \epsilon_{S_{L,R}}^{\alpha\beta i}(\mu)  \times 10^2$		$ \epsilon_T^{\alpha\beta i}(\mu)  \times 10^3$	
				$\mu = 1 \text{ TeV}$	$\mu = 2 \text{ GeV}$	$\mu = 1 \text{ TeV}$	$\mu = 2 \text{ GeV}$
$d$	$e$	$[-0.52, 0.86]$	0.67 (0.42)	0.72 (0.46)	1.5 (0.96)	4.3 (2.7)	3.4 (2.2)
	$\mu$	$[-0.85, 1.2]$	1.0 (0.38)	1.1 (0.42)	2.3 (0.86)	6.6 (2.4)	5.2 (1.9)
	$\tau$	$[-1.4, 1.8]$	1.6 (0.68)	1.5 (0.55)	3.1 (1.1)	8.7 (3.1)	6.9 (2.5)
$s$	$e$	$[-0.28, 0.59]$	0.42 (0.26)	0.43 (0.28)	0.91 (0.57)	2.8 (1.5)	2.2 (1.2)
	$\mu$	$[-0.46, 0.78]$	0.63 (0.23)	0.68 (0.25)	1.4 (0.52)	4.0 (1.4)	3.1 (1.1)
	$\tau$	$[-0.65, 1.2]$	0.93 (0.40)	0.87 (0.31)	1.8 (0.65)	5.2 (1.8)	4.1 (1.5)

95% CL ranges on WCs. Naive HL-LHC projection in ().

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95% CL ranges on WCs. Naive HL-LHC projection in ().

- Similar results for **d** and **s** - strange PDF versus Cabibo squared.
- Approx all limits  $\mathcal{O}(0.01)$ .
- $\epsilon_{V_L}^{\alpha\beta i} : \epsilon_{S_{L,R}}^{\alpha\beta i} : \epsilon_T^{\alpha\beta i} \approx 1 : \frac{2}{\sqrt{3}} : \frac{1}{2}$
- Quadratic terms dominates the limits also for  $V_L$ .
- The most sensitive bins fall in the range  $[1 - 1.5] \text{ TeV}$
- Dedicated future analysis: angular dependence, lepton charge asymmetry, etc.

## 4.1 Short-distance new physics in high- $p_T$ tails

How well do we know the bckg?

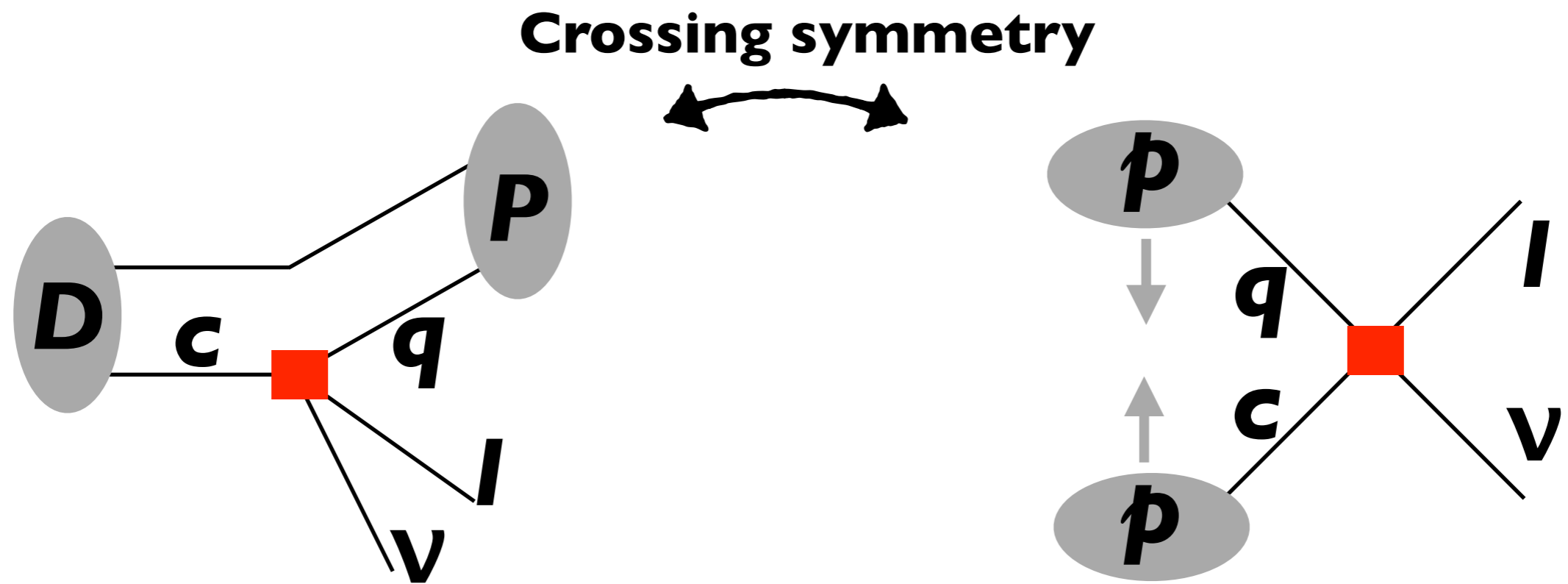
- The SM prediction (NNLO QCD + NLO EW) suffices the experimental precision.

How well do we know the signal?

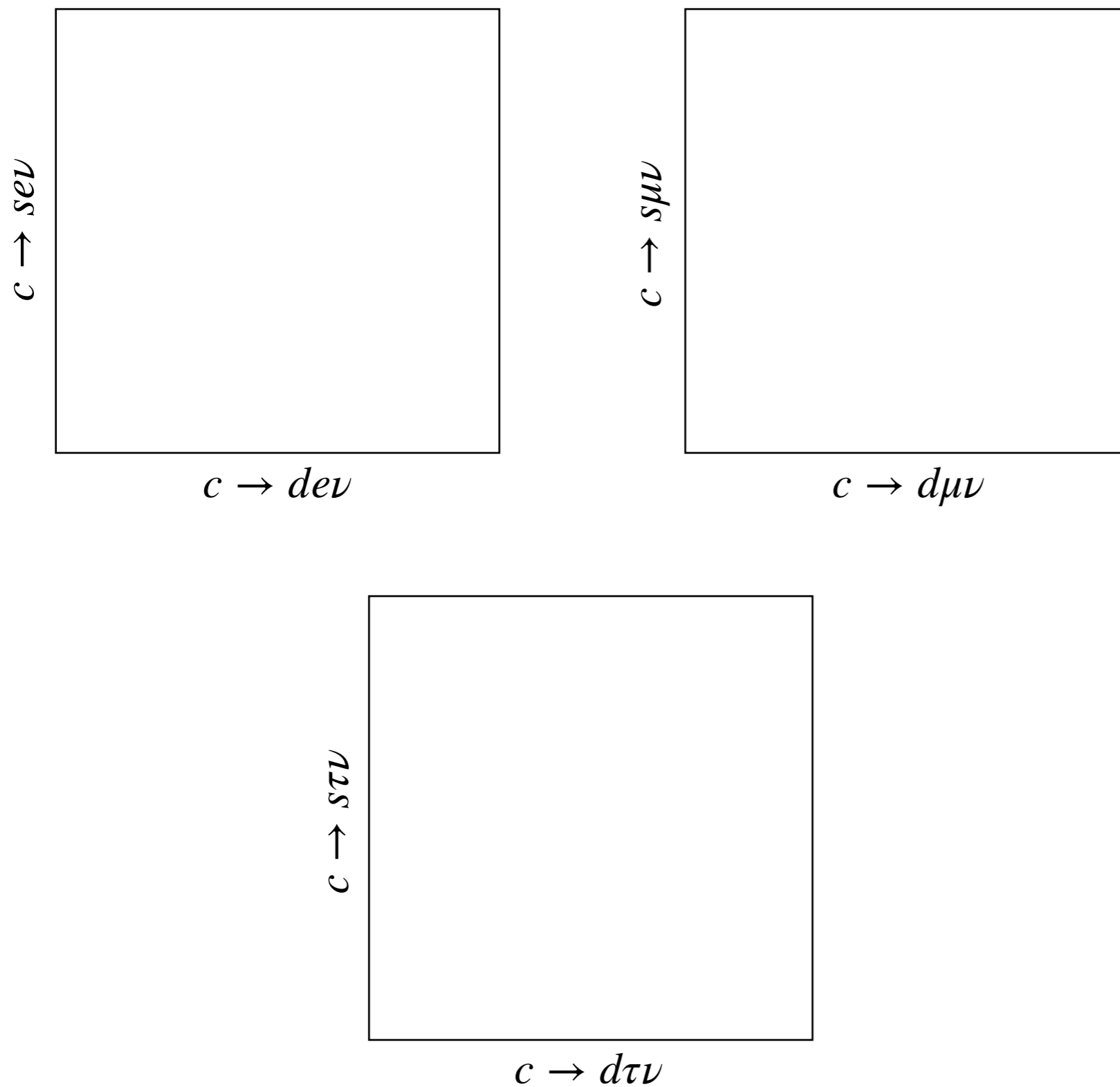
- The uncertainty on the signal prediction from the missing higher order radiative corrections and PDF replicas estimated to be  $\sim 10\%$  on the rate in the most sensitive bin.  $\Delta\epsilon_X/\epsilon_X \approx 0.5 \Delta\sigma/\sigma$

How well do we know PDFs?

- The PDF determination assumes the SM. The impact of the Drell-Yan data in the global PDF fit is small at the moment. The issue is there in the future.

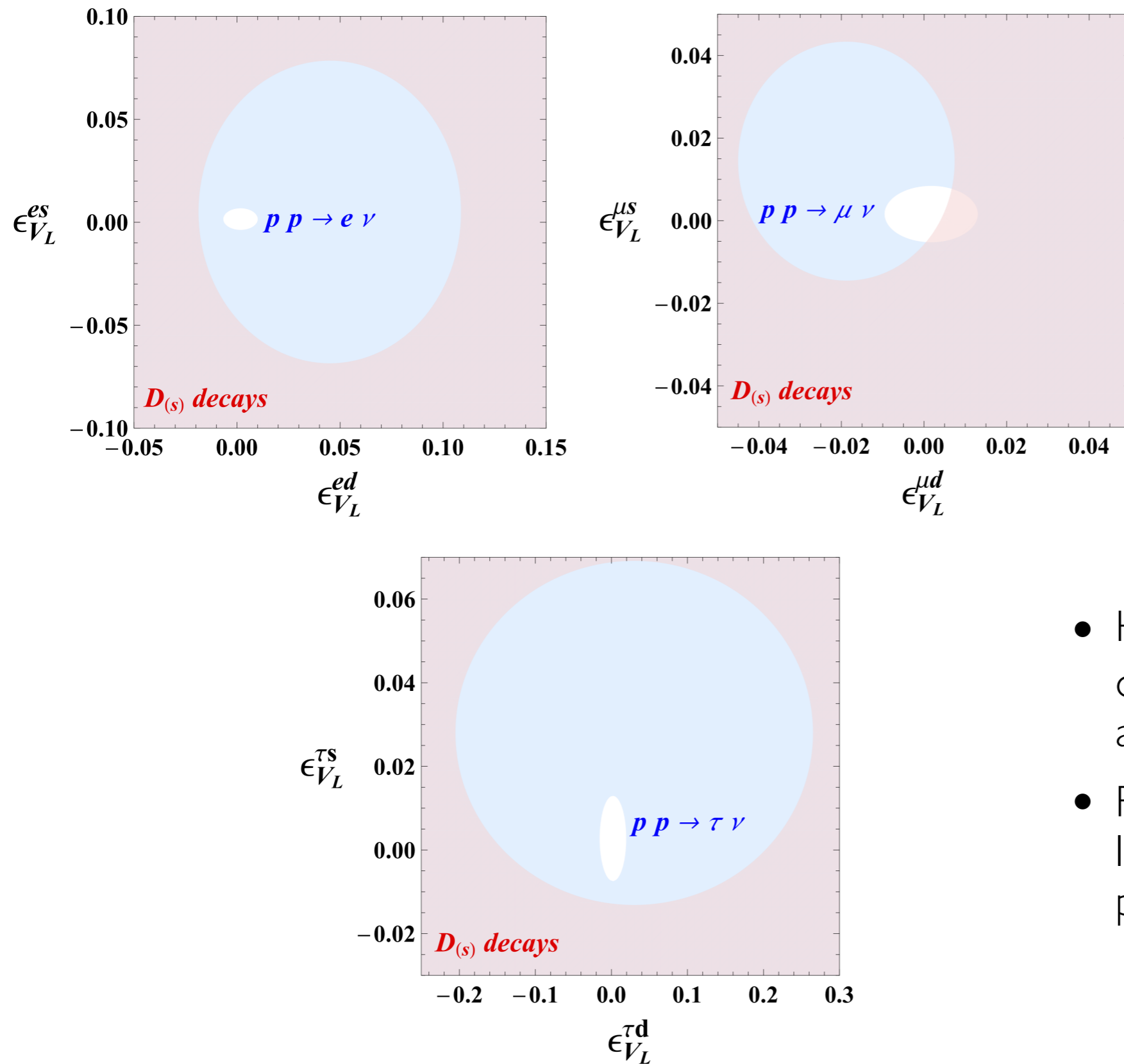


***Interplay between low and high energy***



**Figure 2.** Exclusion limits at 95% CL on  $c \rightarrow d(s)\bar{e}^\alpha \nu^\alpha$  transitions in  $(\epsilon_{V_L}^{\alpha\alpha d}, \epsilon_{V_L}^{\alpha\alpha s})$  plane were  $\alpha = e$  (top left),  $\alpha = \mu$  (top right), and  $\alpha = \tau$  (bottom). The region colored in pink is excluded by  $D_{(s)}$  meson decays, while the region colored in blue is excluded by high- $p_T$  LHC.

$$\mathcal{O}_{lq}^{(3)} = (\bar{l}_L \gamma_\mu \tau^I l_L)(\bar{q}_L \gamma^\mu \tau^I q_L)$$



- High- $p_T$  limits are almost an order of magnitude stronger for all transitions
- Future projections from BESIII likely not competitive with future projections from the HL-LHC

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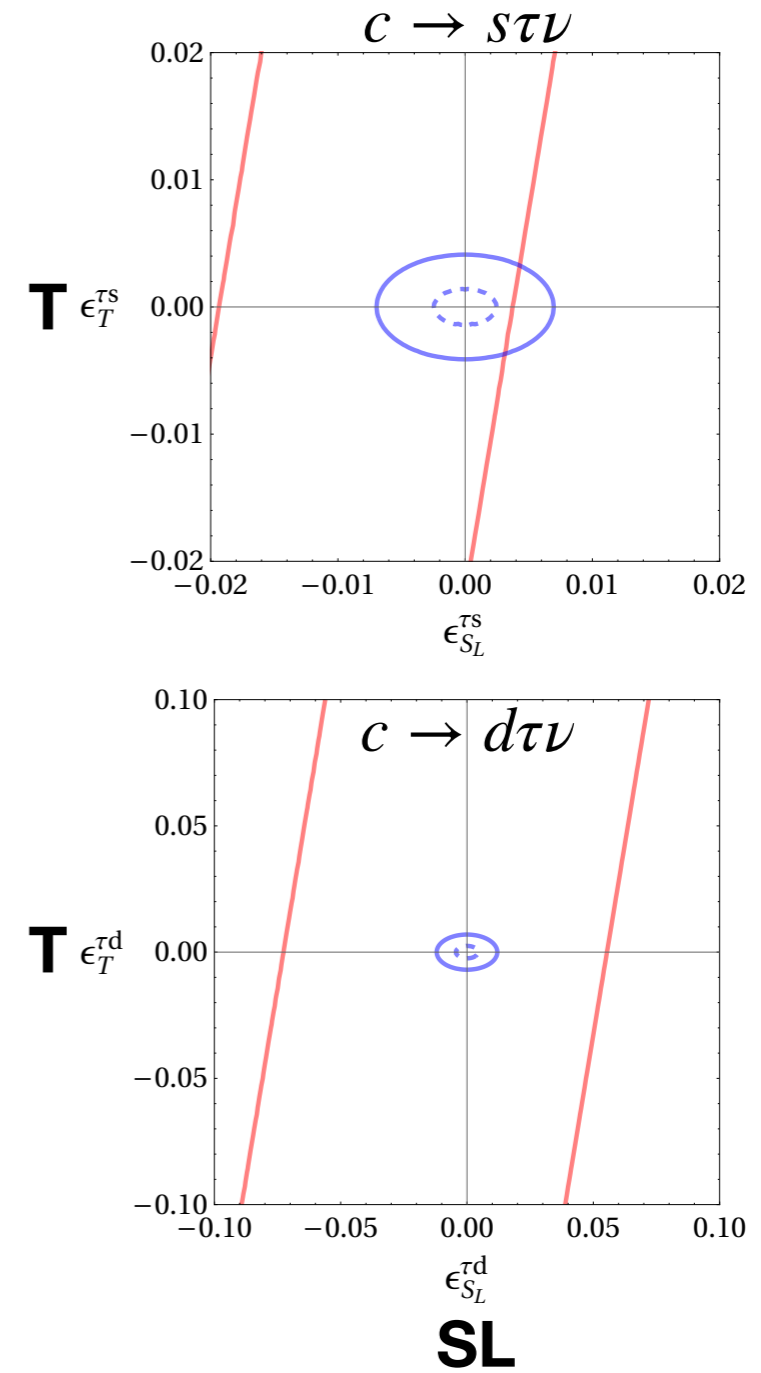
$$\mathcal{O}_{lq}^{(3)} = (\bar{l}_L \gamma_\mu \tau^I l_L)(\bar{q}_L \gamma^\mu \tau^I q_L)$$

**Figure 3.** 95% CL regions for the combined fits of  $\epsilon_{S_L}^{\alpha\beta i}$  and  $\epsilon_T^{\alpha\beta i}$  to the charmed-meson decay data with  $\beta = \alpha$  (red solid line) or  $\beta \neq \alpha$  (light-red dash-dotted line) and to monolepton LHC data (blue solid line). Projections for the high-luminosity phase of the LHC ( $3 \text{ ab}^{-1}$ ), obtained by rescaling the expected limits with luminosity, are represented by dashed ellipses.

$$\begin{aligned} \mathcal{O}_{lequ}^{(1)} &= (\bar{l}_L^p e_R) \epsilon_{pr} (\bar{q}_L^r u_R) \\ \mathcal{O}_{lequ}^{(3)} &= (\bar{l}_L^p \sigma_{\mu\nu} e_R) \epsilon_{pr} (\bar{q}_L^r \sigma^{\mu\nu} u_R) \end{aligned}$$

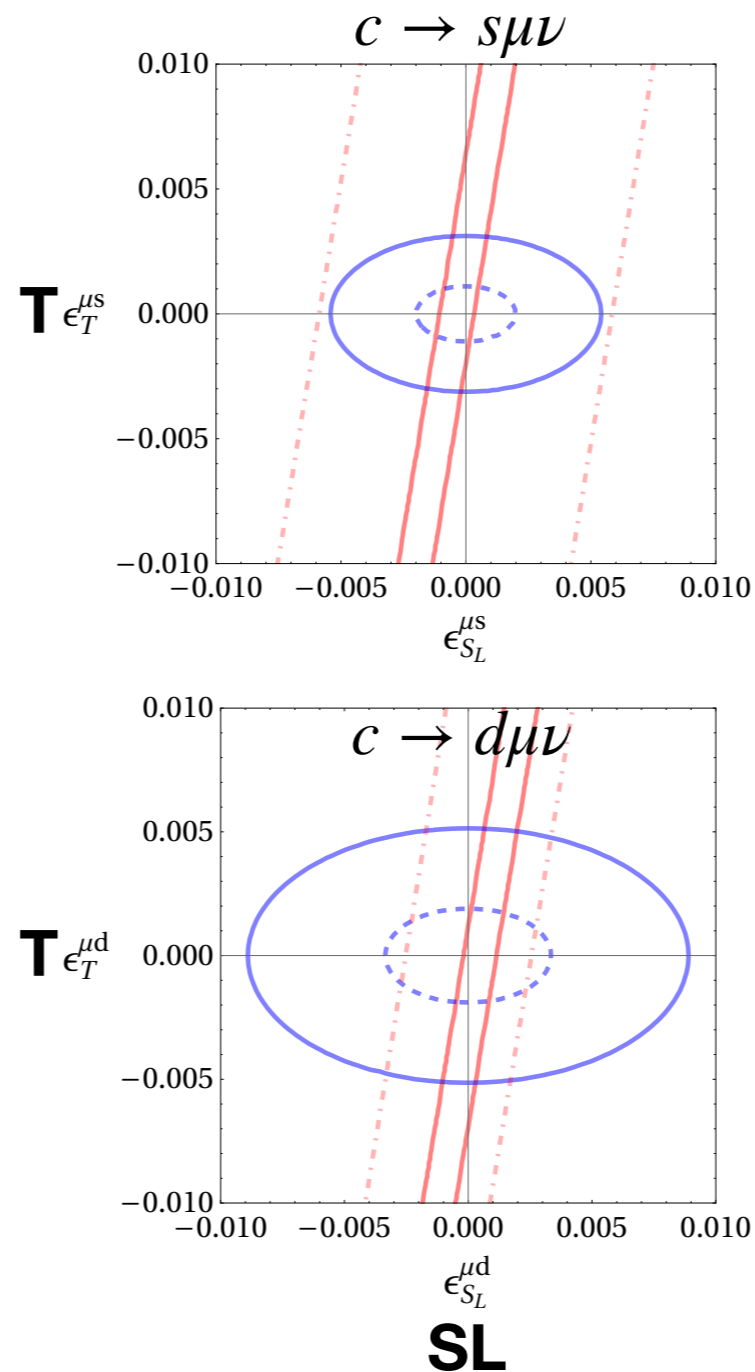


- Tau: High- $p_T$  more sensitive



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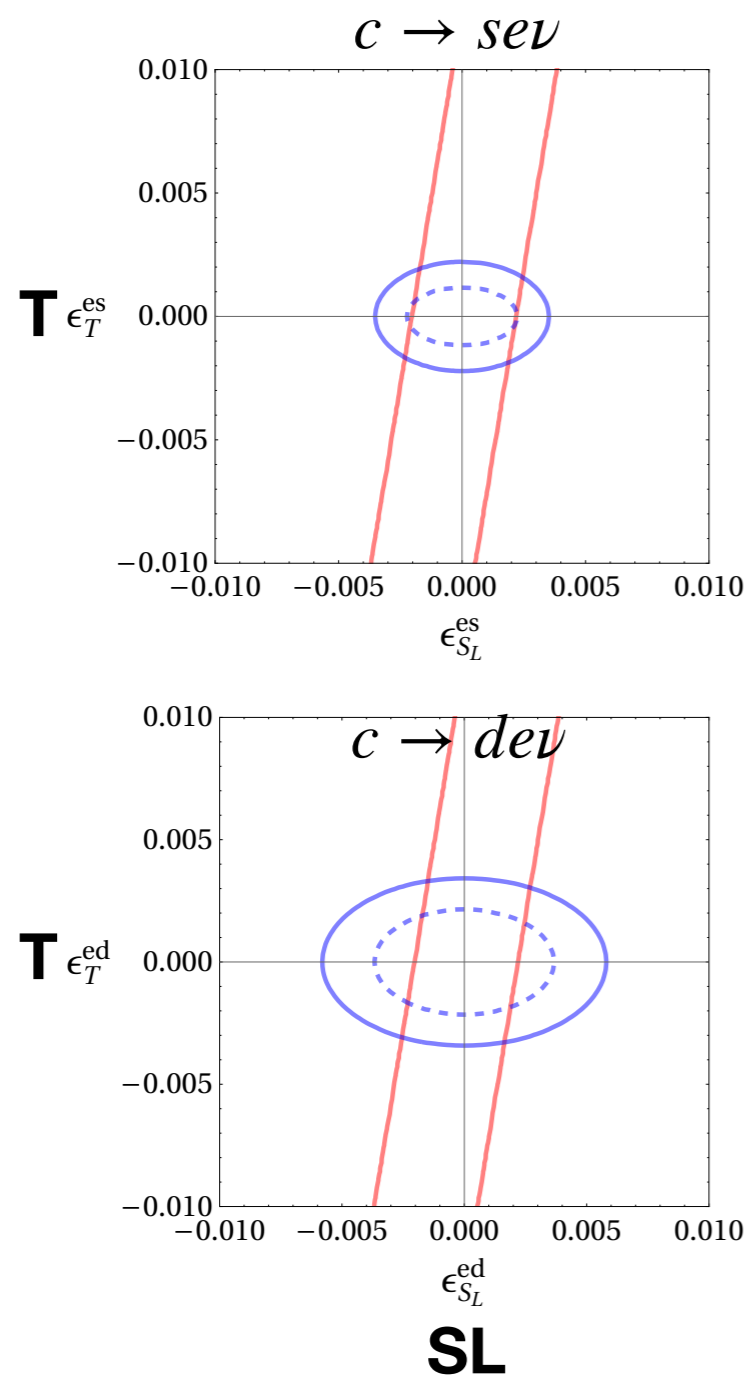


- Muon: P low-pT, S high-pT

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- Electron: P competitive

**Figure 3.** 95% CL regions for the combined fits of  $\epsilon_{S_L}^{\alpha\beta i}$  and  $\epsilon_T^{\alpha\beta i}$  to the charmed-meson decay data with  $\beta = \alpha$  (red solid line) or  $\beta \neq \alpha$  (light-red dash-dotted line) and to monolepton LHC data (blue solid line). Projections for the high-luminosity phase of the LHC ( $3 \text{ ab}^{-1}$ ), obtained by rescaling the expected limits with luminosity, are represented by dashed ellipses.

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### 4.3 Possible caveats within and beyond the EFT

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 Dominant term

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**A significant cancellation would require a peculiar NP scenario.**

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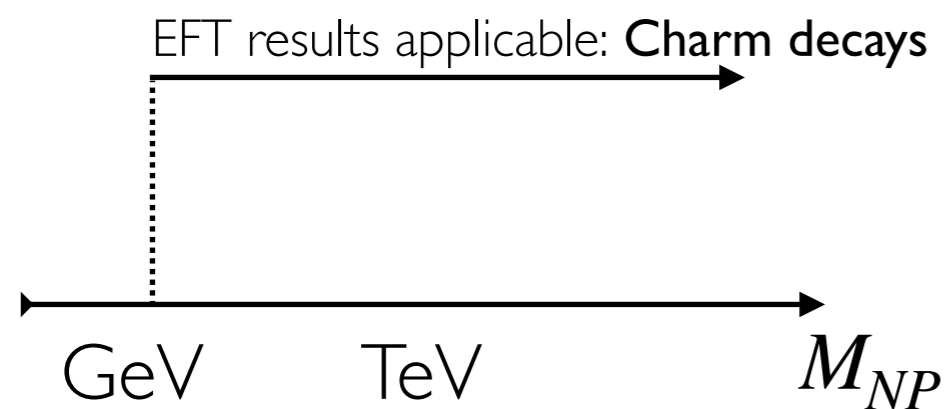
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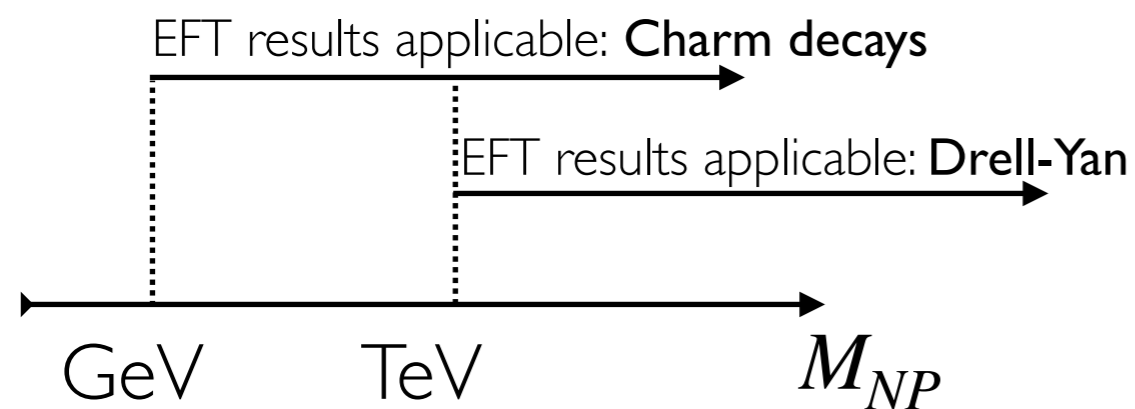


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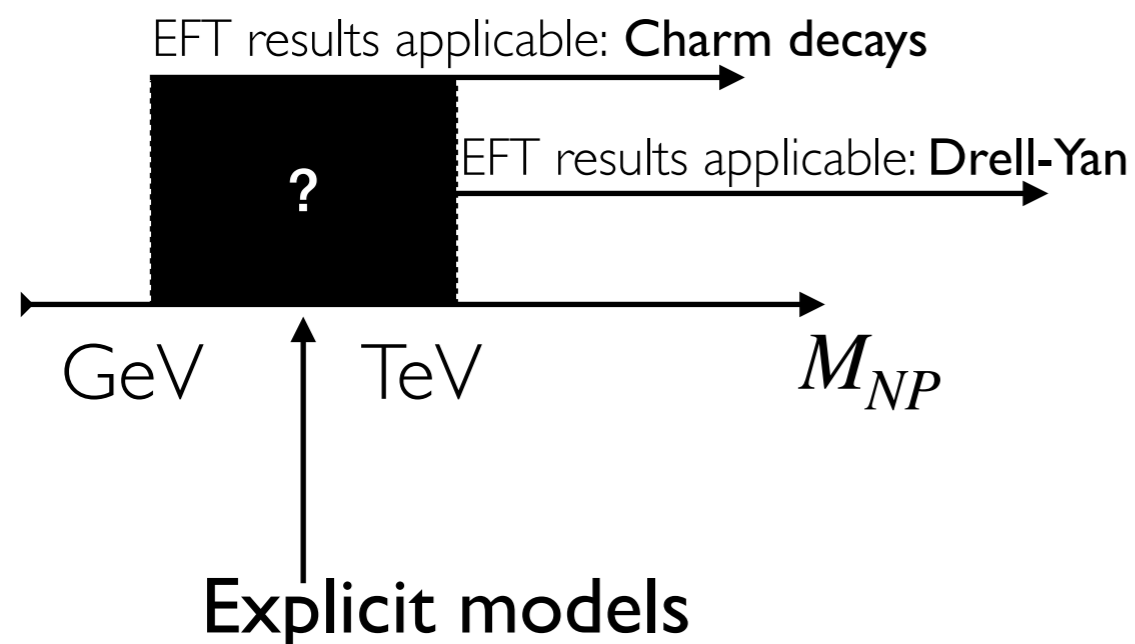


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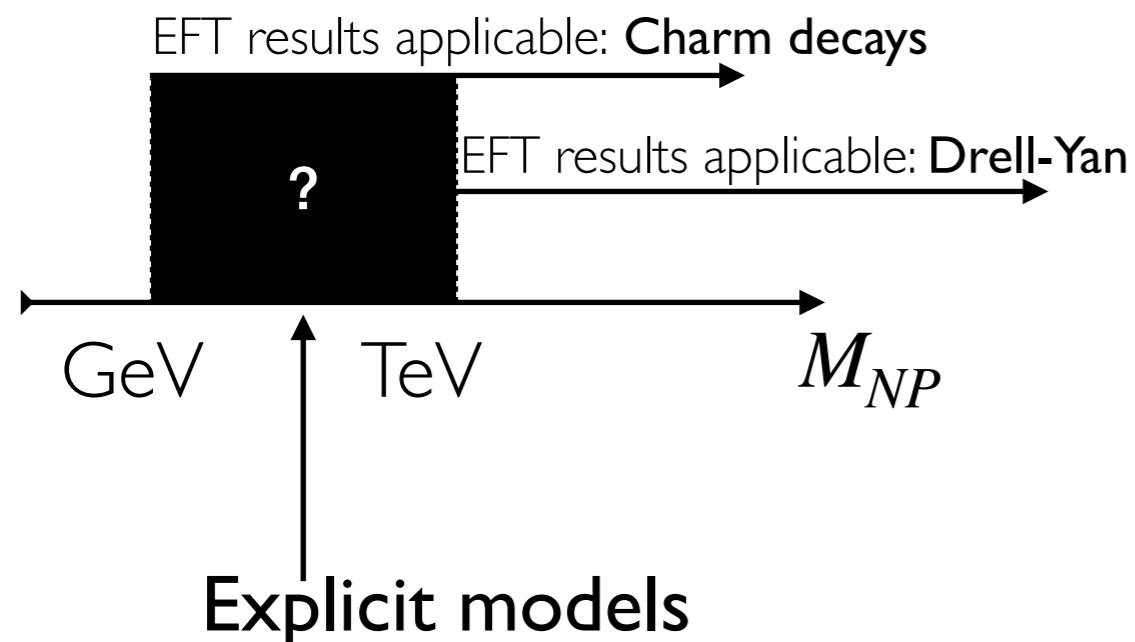


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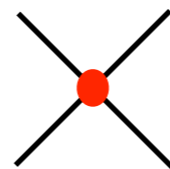
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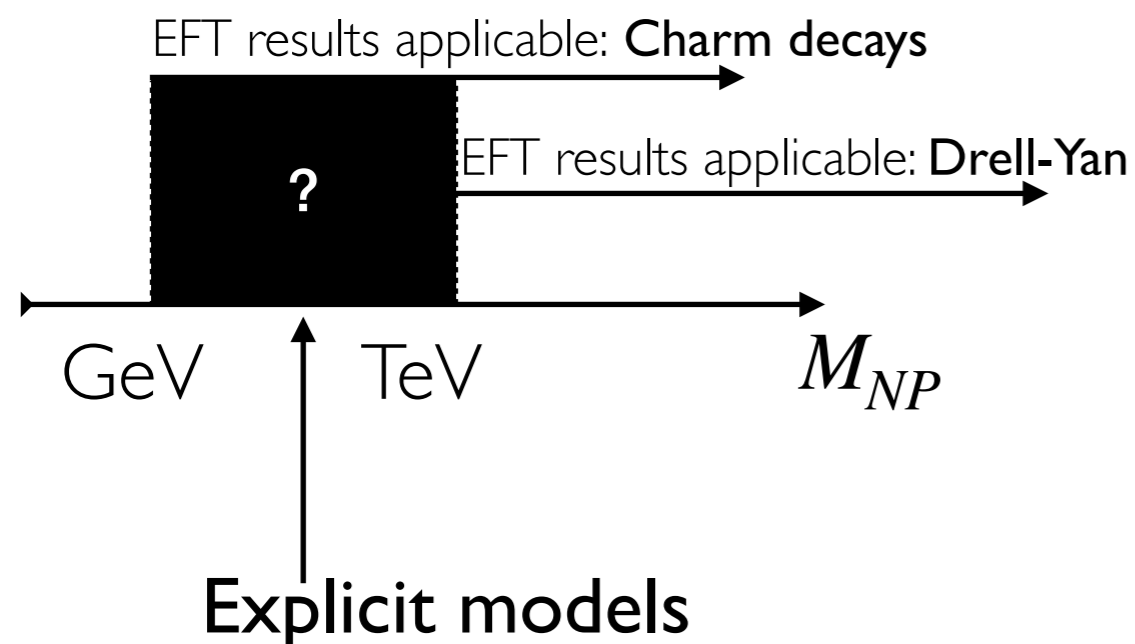


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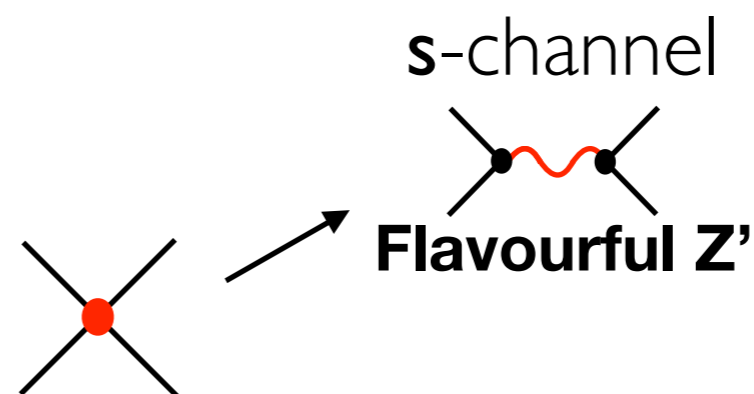
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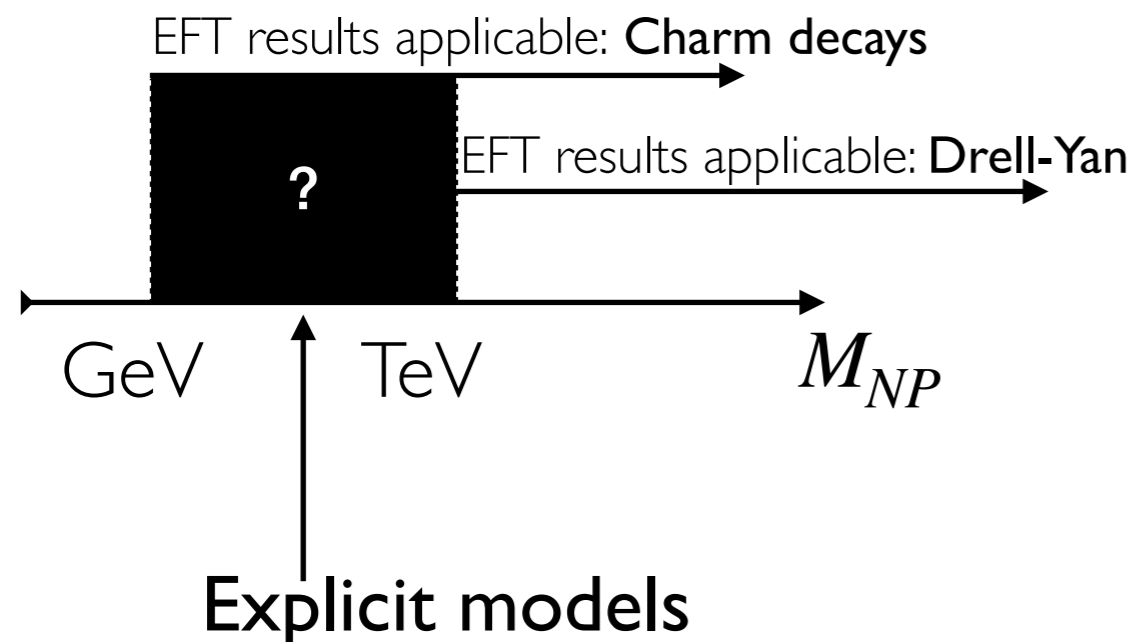
- EFT bounds are overly conservative

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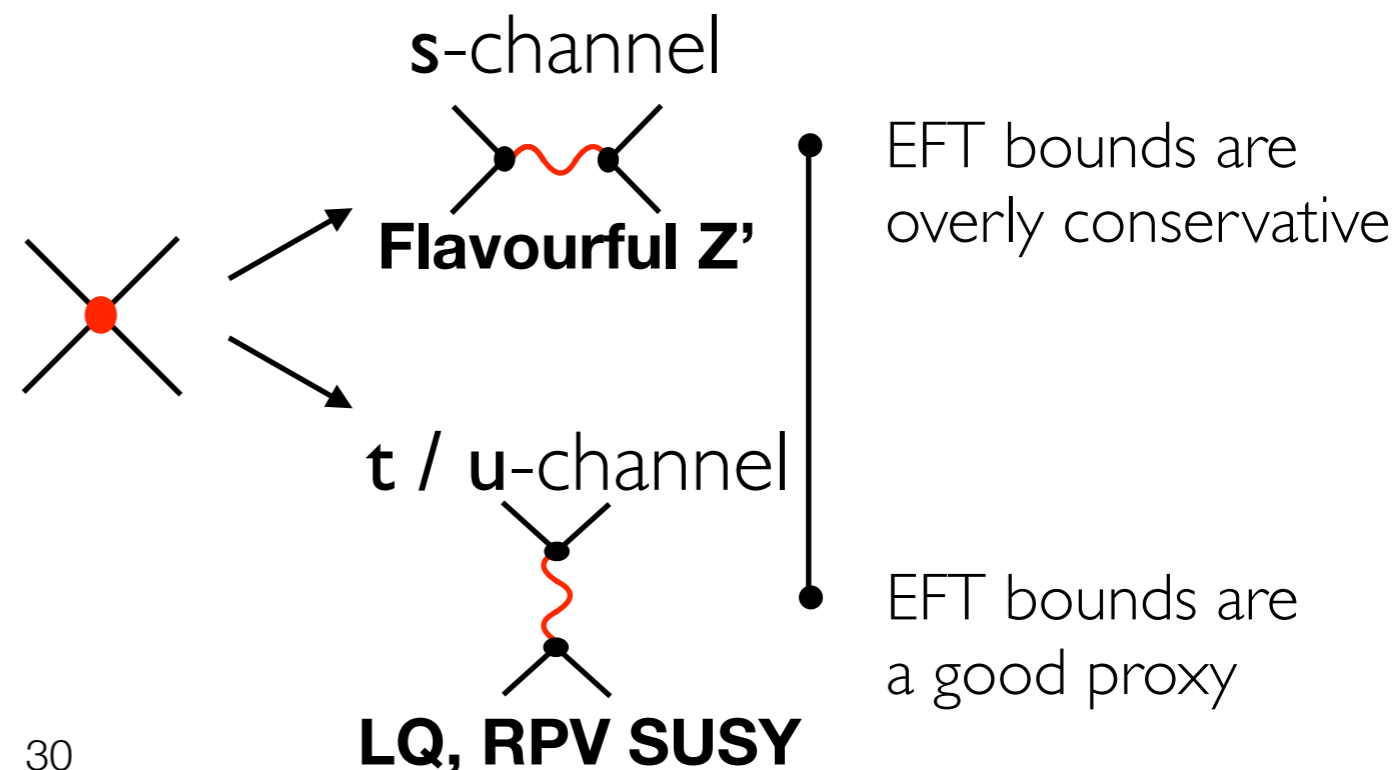
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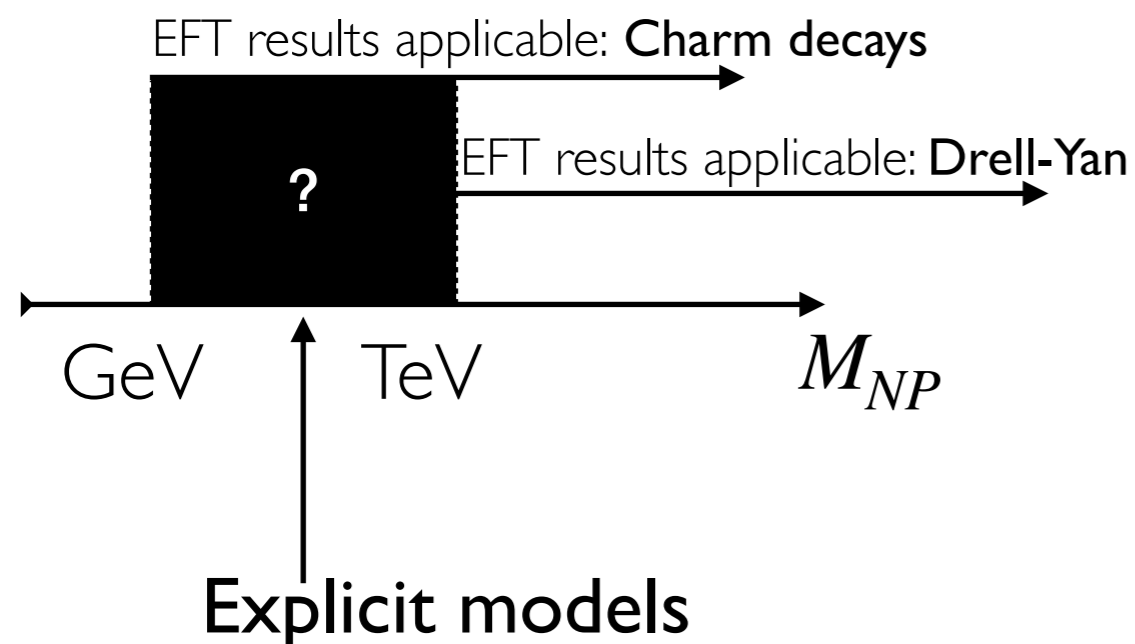


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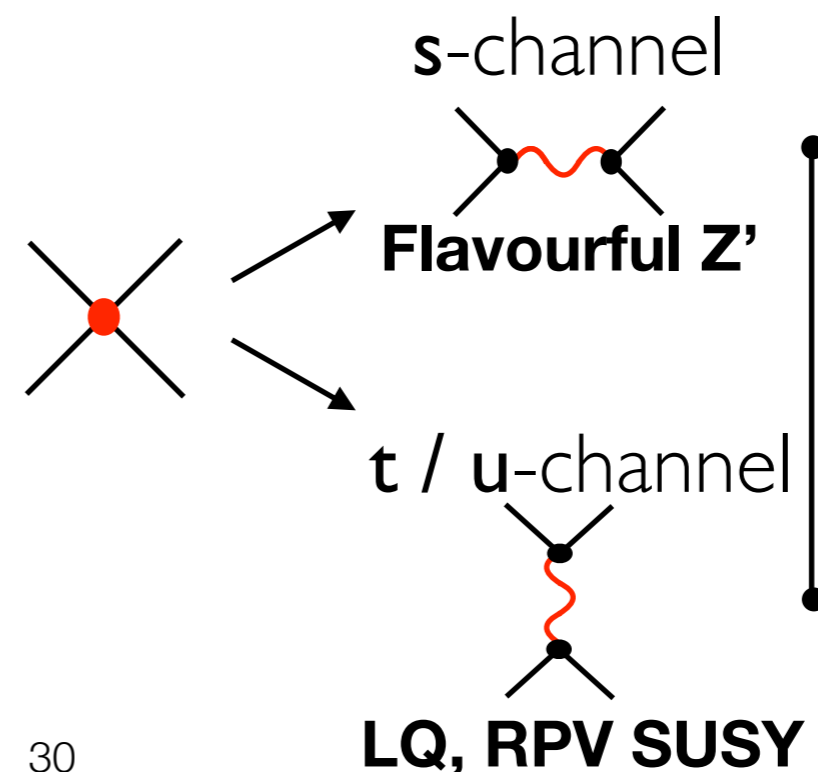


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#### Tree-level UV completions



Charged mediators  
 $M_{NP} \gtrsim \mathcal{O}(100 \text{ GeV})$   
 Coloured mediators  
 even more

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EFT bounds are  
 a good proxy

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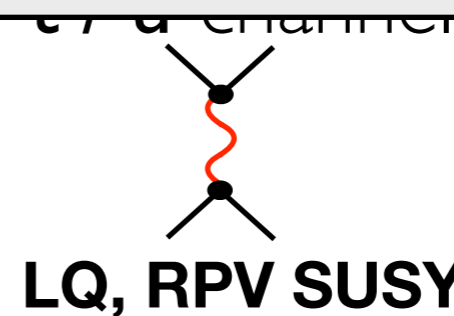


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- *To conclude, the comparison of low- and high- $p_T$  data within an EFT framework is a useful exercise even if the EFT validity is not guaranteed.*
- *If high- $p_T$  provides stronger limits relative to the ones derived from low- $p_T$ , this will also hold in a generic NP model barring tuned cancellations.*

Explicit models



EFT bounds are a good proxy

## ***Neutral currents***

$$c \rightarrow u e^\alpha \bar{e}^\beta$$

- Exercise repeated,  
see 2003.12421

# Constraints from $SU(2)$ gauge invariance

$$q_L^i = \begin{pmatrix} V_u^{ij} u_L^j \\ V_d^{ij} d_L^j \end{pmatrix}, \quad V = V_u^\dagger V_d \quad l_L^\alpha = \begin{pmatrix} \nu_L^\alpha \\ e_L^\alpha \end{pmatrix},$$

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## Example

$$\mathcal{O}_{lq}^{(3)} = (\bar{l}_L \gamma_\mu \tau^I l_L) (\bar{q}_L \gamma^\mu \tau^I q_L)$$

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- i) Charged-current  $d_i \rightarrow u l \nu$  and  $\tau \rightarrow d_i u \nu$  transitions (1st line),
- ii) Neutral-current  $c \rightarrow u l l^{(\prime)}$ ,  $\tau \rightarrow l u u$  decays and  $\mu u \rightarrow e u$  conversion (2nd line),
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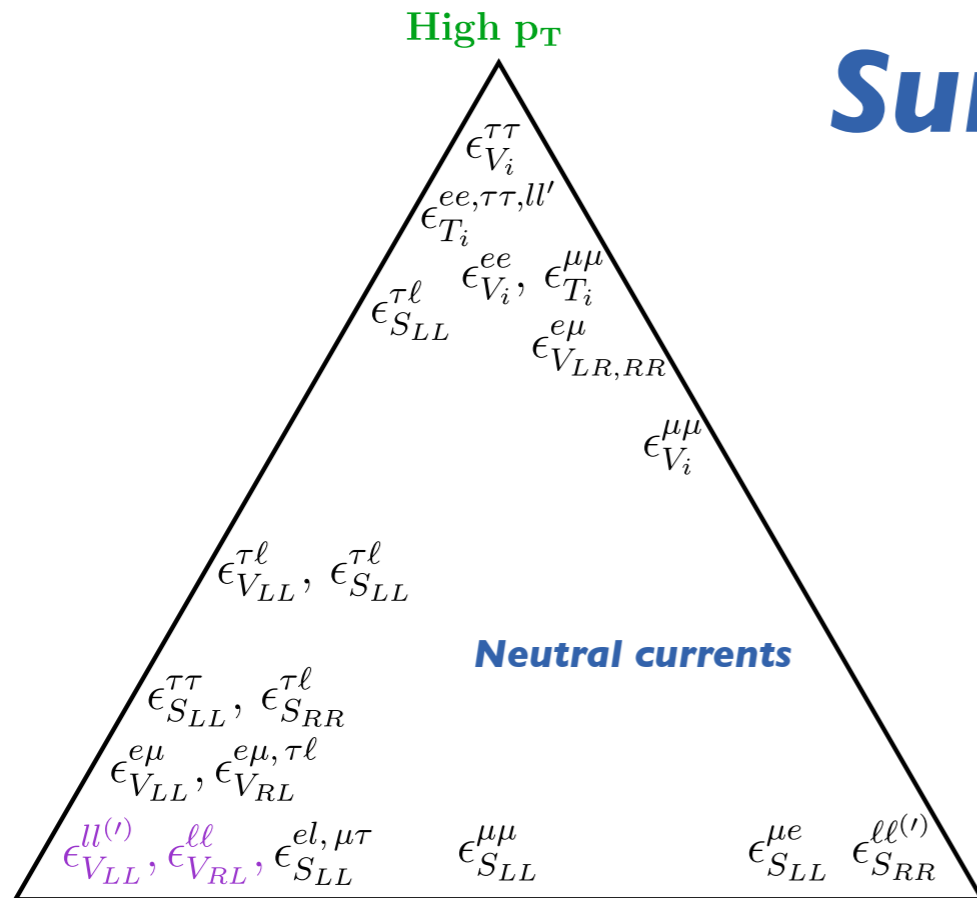
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## Counterexample

$$\mathcal{O}_{eu} = (\bar{e}_R \gamma^\mu e_R) (\bar{u}_R \gamma^\mu u_R)$$

# Summary

$SU(2)_L$   
relations



$D$  physics

We systematically went through all options

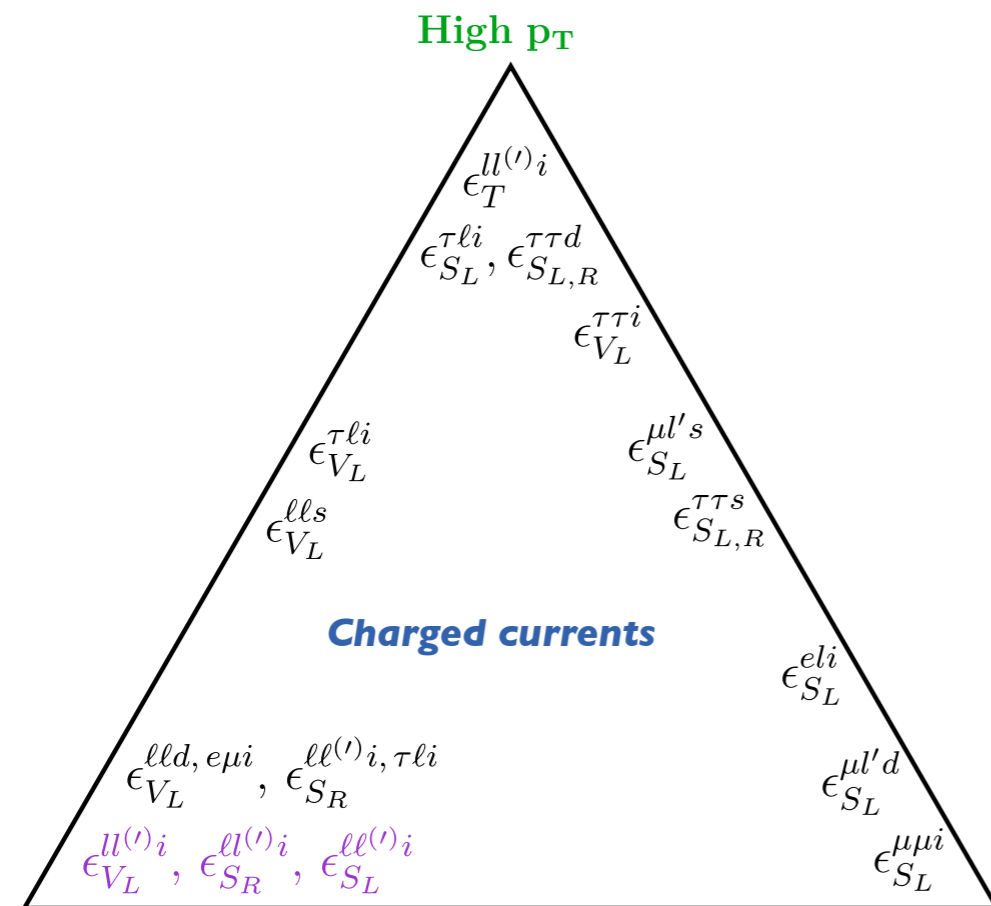
$$\mathcal{O}_{LQ}^{(1)} = (\bar{L}\gamma_\mu L)(Q\gamma^\mu Q), \quad \mathcal{O}_{LQ}^{(3)} = (\bar{L}\gamma_\mu\tau^I L)(Q\gamma^\mu\tau^I Q),$$

$$\mathcal{O}_{eu} = (\bar{e}\gamma_\mu e)(\bar{u}\gamma^\mu u), \quad \mathcal{O}_{Lu} = (\bar{L}\gamma_\mu L)(\bar{u}\gamma^\mu u),$$

$$\mathcal{O}_{Qe} = (\bar{Q}\gamma^\mu Q)(\bar{e}\gamma_\mu e), \quad \mathcal{O}_{LedQ} = (\bar{L}\gamma_\mu e)(\bar{d}\gamma^\mu Q),$$

$$\mathcal{O}_{LeQu}^{(1)} = (\bar{L}^p e)\epsilon_{pr}(\bar{Q}^r u), \quad \mathcal{O}_{LeQu}^{(3)} = (\bar{L}^p\sigma_{\mu\nu}e)\epsilon_{pr}(\bar{Q}^r\sigma^{\mu\nu}u),$$

$SU(2)_L$   
relations



$D_{(s)}$  physics

$D(s)$  decays, high- $p_T$  lepton tails and  $SU(2)_L$  relations chart the space of the SMEFT affecting semi(leptonic) charm flavor transitions.

***The end***

I apologise for missing citations, see the reference list of 2003.12421