

*Towards a precise theoretical determination  
of the  $B_s$  lifetime*

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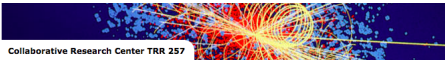
Annual meeting of the German LHCb groups

Bonn

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Based on ArXiv:2004.09527

In collaboration with A. Lenz and A. Rusov



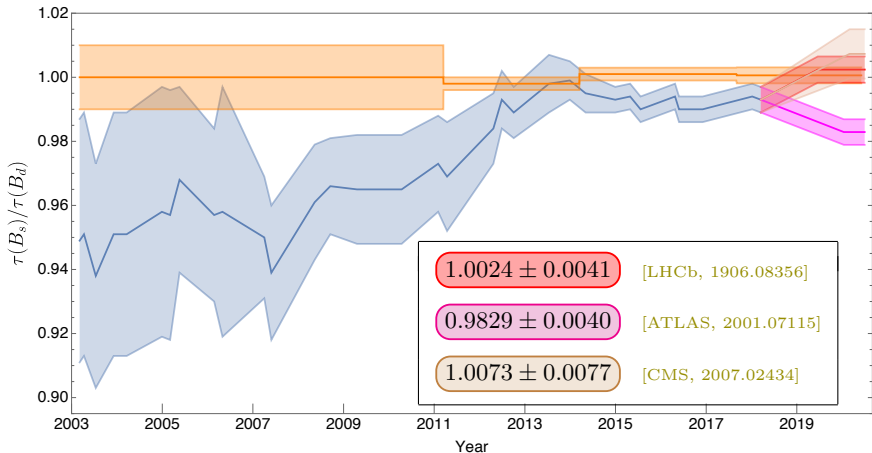


# *Motivation*

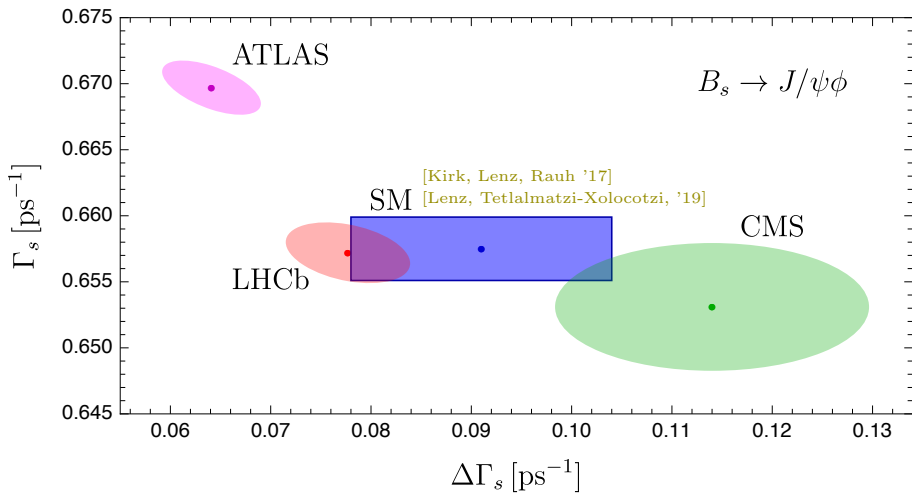
# $\tau(B_s)/\tau(B_d)$ - Experimental status

SM HFLAV

Credit M. Kirk



# Closer look ...



## $\tau(B_s)/\tau(B_d)$ - Theoretical status

- ◇ Use Heavy Quark Expansion (HQE) [Shifman, Voloshin '85]

$$\frac{\tau(B_s)}{\tau(B_d)} = \frac{\Gamma_b + \delta\Gamma_{B_d}}{\Gamma_b + \delta\Gamma_{B_s}} = 1 + \underbrace{\tau(B_s) (\delta\Gamma_{B_d} - \delta\Gamma_{B_s})}_{0.0007 \pm 0.0025} \quad [\text{Kirk, Lenz, Rauh '17}]$$

\*  $\Gamma_b$  - leading contribution, free b-quark decay      \*  $\delta\Gamma_{B_q}$  - subleading terms

- ◇ Multiple **cancellations** arise
- ◇ Unique possibility
  - \* to compete with increasing experimental precision
  - \* to validate HQE
  - \* to test for BSM scenarios and search for invisible decays

# $\tau(B_s)/\tau(B_d)$ - *New Physics*

- ◇ BSM contributions appear in the lifetime ratio as:

$$\underbrace{\frac{\tau(B_s)}{\tau(B_d)}}_{\text{exp.}} \approx 1 + \underbrace{\tau(B_s) (\delta\Gamma_{B_d}^{\text{SM}} - \delta\Gamma_{B_s}^{\text{SM}})}_{\text{theory}} + \underbrace{[\text{BR}(B_d \rightarrow X)^{\text{BSM}} - \text{BR}(B_s \rightarrow X)^{\text{BSM}}]}_{\text{indirectly constrained}}$$

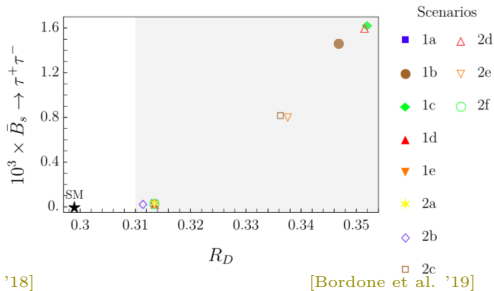
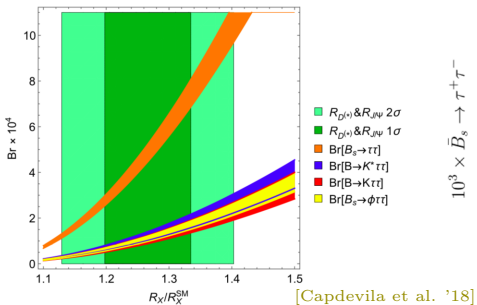
- \* NP could affect differently  $b \rightarrow s$  and  $b \rightarrow d$  transitions
- \* Possibility to constrain BSM contributions at permille level
- \* Hints for NP in  $b \rightarrow s\mu^+\mu^-$  and  $b \rightarrow c\tau^-\bar{\nu}_\tau$  processes might point towards large effects in  $b \rightarrow s\tau^+\tau^-$  [Capdevila et al. '18; Bordone et al. '19]

# The $B_s \rightarrow \tau^+ \tau^-$ decay

- ◇ Suppressed in the SM and experimentally very challenging:

$$\text{Br}(B_s \rightarrow \tau^+ \tau^-) \begin{cases} =_{\text{th.}} (7.73 \pm 0.49) \times 10^{-7} & [\text{Bobeth et al. '14}] \\ <_{\text{exp.}} 6.8 \times 10^{-3} & [\text{LHCb, 1703.02508}] \end{cases}$$

- ◇ Correlations between  $R_{D^{(*)}}$ ,  $R_{J/\psi}$  and  $B_s \rightarrow \tau^+ \tau^-$ , ...



- ◇ These big effects might be visible in  $\tau(B_s)/\tau(B_d)$



*The Heavy Quark Expansion*



# The theoretical framework

- ◇ From the optical theorem:

$$\Gamma_{B_q} = \frac{1}{2m_{B_q}} \text{Im} \langle B_q | i \int d^4x \mathcal{T} \{ \mathcal{L}_{\text{eff}}(x), \mathcal{L}_{\text{eff}}(0) \} | B_q \rangle$$

- ◇ OPE in inverse power of  $m_b$ :  $p^\mu = m_b v^\mu + k^\mu$

$$\Gamma_{B_q} = \underbrace{\Gamma_3 \langle \mathcal{O}_3 \rangle}_{\Gamma_b} + \underbrace{\Gamma_5 \frac{\langle \mathcal{O}_5 \rangle}{m_b^2} + \Gamma_6 \frac{\langle \mathcal{O}_6 \rangle}{m_b^3} + \dots + 16\pi^2 \left[ \tilde{\Gamma}_6 \frac{\langle \tilde{\mathcal{O}}_6 \rangle}{m_b^3} + \tilde{\Gamma}_7 \frac{\langle \tilde{\mathcal{O}}_7 \rangle}{m_b^4} + \dots \right]}_{\delta\Gamma_{B_q}}$$

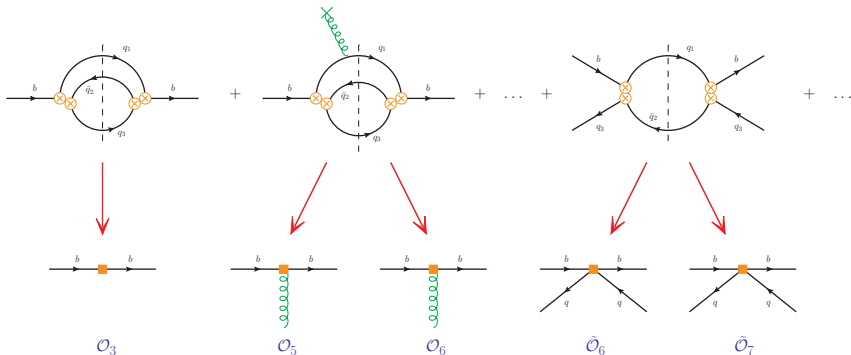
- \*  $\Gamma_i, \tilde{\Gamma}_i$  - short distance coefficients

- \*  $\mathcal{O}_d, \tilde{\mathcal{O}}_d$  - local quark operator of dimension  $d$

- \*  $\frac{\delta\Gamma_{B_q}^{(d)}}{\Gamma_b} \sim \left( \frac{k}{m_b} \right)^{d-3} \sim \left( \frac{1 \text{ GeV}}{4.5 \text{ GeV}} \right)^{d-3}$  - small parameter

# The theoretical framework

$$\Gamma_{B_q} = \Gamma_3 \langle \mathcal{O}_3 \rangle + \Gamma_5 \frac{\langle \mathcal{O}_5 \rangle}{m_b^2} + \Gamma_6 \frac{\langle \mathcal{O}_6 \rangle}{m_b^3} + \dots + 16\pi^2 \left[ \tilde{\Gamma}_6 \frac{\langle \tilde{\mathcal{O}}_6 \rangle}{m_b^3} + \tilde{\Gamma}_7 \frac{\langle \tilde{\mathcal{O}}_7 \rangle}{m_b^4} + \dots \right]$$



# The theoretical framework

◇ What has been included so far ...

”Two – loop” contributions

”One – loop” contributions

	$\mathcal{O}(1)$	$\mathcal{O}(\alpha_s)$	$\mathcal{O}(1)$	$\mathcal{O}(\alpha_s)$
$\mathcal{O}(1)$	✓	✓	–	–
$\mathcal{O}\left(\frac{1}{m_b^2}\right)$	✓	✗	–	–
$\mathcal{O}\left(\frac{1}{m_b^3}\right)$	✗	✗	✓	✓
$\mathcal{O}\left(\frac{1}{m_b^4}\right)$	✗	✗	✓	✗

## Some peculiarities

◇ **Suppression** of  $1/m_b^2$  contributions

◇ "One-loop"  $1/m_b^3$  corrections expected to be dominant, but

$q = d, s$

$$\delta\tilde{\Gamma}_{B_q}^{(6)} \sim \left\{ \underbrace{\left( \frac{C_1^2}{3} + 2C_1C_2 + 3C_2^2 \right)}_{\approx 10^{-2}} \left( \underbrace{(B_2^q)}_{\approx 1} - \underbrace{(B_1^q)}_{\approx 1} \right) + \underbrace{\mathcal{O}\left(\frac{m_c^2}{m_b^2}\right)}_{\approx 0.05} + \underbrace{2C_1^2}_{\approx 2} \underbrace{f(\epsilon_2, \epsilon_1)}_{\text{color suppr.}} \right\}$$

◇ Strong **suppression** despite loop enhancement

◇ "Two-loop"  $1/m_b^3$  corrections found sizeable in the SL case

[Gremm, Kapustin, '96]

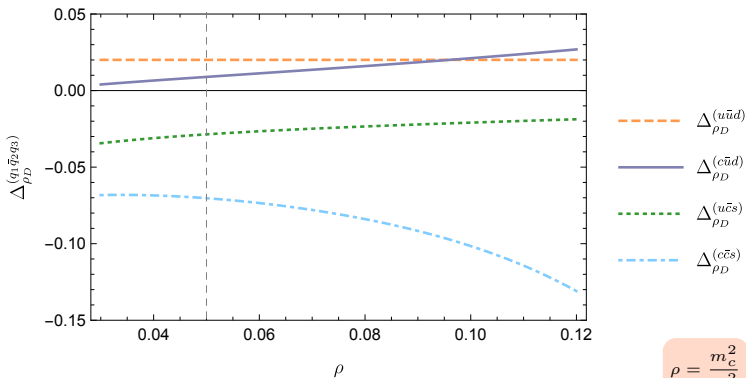
\* What about the NL case?



*Contribution  
of the Darwin term  
for NL decays*

# Result

- ◇ Computation done by **two independent** groups [Lenz, Piscopo, Rusov, '20]  
[Mannel, Moreno, Pivovarov, '20]  
[Moreno, '20]
- ◇ Large relative size of **2 – 7%**



# Conclusion

- Large coefficient of the Darwin operator, but

$$\frac{\tau(B_s)}{\tau(B_d)} = 1 + \left\{ \underbrace{\Gamma_5 \left( \langle \mathcal{O}_5 \rangle_{B_d} - \langle \mathcal{O}_5 \rangle_{B_s} \right)}_{\checkmark} \frac{1}{m_b^2} + \underbrace{\Gamma_6}_{\checkmark} \underbrace{\left( \langle \mathcal{O}_6 \rangle_{B_d} - \langle \mathcal{O}_6 \rangle_{B_s} \right)}_{\times} \frac{1}{m_b^3} \right.$$

$$\left. + \left[ \underbrace{\left( \tilde{\Gamma}_6^{B_d} - \tilde{\Gamma}_6^{B_s} \right) \langle \tilde{\mathcal{O}}_6 \rangle_{B_d}}_{\checkmark} - \tilde{\Gamma}_6^{B_s} \underbrace{\left( \langle \tilde{\mathcal{O}}_6 \rangle_{B_s} - \langle \tilde{\mathcal{O}}_6 \rangle_{B_d} \right)}_{\times} \right] \frac{1}{m_b^3} + \dots \right\} \tau(B_s)$$

- $SU(3)_f$  violation effects crucial

Further steps:

- \* Determination of  $\left( \langle \mathcal{O}_6 \rangle_{B_d} - \langle \mathcal{O}_6 \rangle_{B_s} \right)$  [Lenz, Piscopo, Rusov]
- \* Computation of  $\langle \tilde{\mathcal{O}}_6 \rangle_{B_s}$  [King, Lenz, Rauh, Witzel]  
HQET SumRules    Lattice

## Final remarks on $B_s \rightarrow J/\psi \phi$

### ◇ $\phi_s$

- \* Quite precisely measured ( $-21 \pm 31$ ) mrad [HFLAV '19]
- \* In the SM ( $-37 \pm 1$ ) mrad if **penguin pollution** neglected ( $\pm 17$  mrad)
- \* Originally very promising BSM observable, but experimental precision approaching penguin size
- \* Not clear how to improve theory from first-principles

### ◇ $\Gamma_s, \Delta\Gamma_s$

- \* Quite precisely measured but **experimental discrepancy**
- \* Theory can be systematically improved - hard but doable
- \* Huge effort going into perturbative QCD and non-perturbative methods (HQET Sum Rules, lattice)





*Thanks for the attention*

*Backup slides*

# Dimension-six operator basis

## Two-quark operators

$$\mathcal{O}_{\rho D} = \bar{b}_v (iD_\mu) (iv \cdot D) (iD^\mu) b_v$$

$$\mathcal{O}_{\rho LS} = \bar{b}_v (iD_\mu) (iv \cdot D) (iD_\nu) (-i\sigma^{\mu\nu}) b_v$$

## Four-quark operators

$$\tilde{\mathcal{O}}_{6,1}^{(q)} = (\bar{b}_v^i \gamma_\mu (1 - \gamma_5) q^i) (\bar{q}^j \gamma^\mu (1 - \gamma_5) b_v^j) \quad \tilde{\mathcal{O}}_{6,2}^{(q)} = (\bar{b}_v^i \not{\psi} (1 - \gamma_5) q^i) (\bar{q}^j \not{\psi} (1 - \gamma_5) b_v^j)$$

$$\tilde{\mathcal{O}}_{6,3}^{(q)} = (\bar{b}_v^i \gamma_\mu (1 - \gamma_5) q^j) (\bar{q}^j \gamma^\mu (1 - \gamma_5) b_v^i) \quad \tilde{\mathcal{O}}_{6,4}^{(q)} = (\bar{b}_v^i \not{\psi} (1 - \gamma_5) q^j) (\bar{q}^j \not{\psi} (1 - \gamma_5) b_v^i)$$

## Parametrisation of four-quark operators matrix elements

$$\langle B_{q'} | \tilde{\mathcal{O}}_{6,i}^{(q)} | B_{q'} \rangle = A_i m_B^2 f_B^2 \left( \mathcal{B}_i^{(q)}(B) \delta_{qq'} + \tau_i^{(q)}(B) \right)$$

with  $A_1 = A_3 = 1$ ,  $A_2 = A_4 = (m_B / (m_b + m_q))^2$ ,  $q = u, d, s$

# Quark Hadron Duality

Experiment at hadron level, calculation at quark-gluon level

$$\text{QHD violation} \equiv \begin{cases} 1/m_Q \text{ corrections in } \Gamma \\ \text{oscillatory terms in } \Gamma \end{cases}$$

★ In the '90s appears discrepancy:

$$\frac{\tau(\Lambda_b)}{\tau(B_d)} = \begin{cases} \sim 0.96 & [\text{Shifman, Voloshin '86}] \\ 0.798 \pm 0.034 & [\text{HFAG '03}] \end{cases}$$

★ 2019 status:

$$\frac{\tau(\Lambda_b)}{\tau(B_d)} = \begin{cases} 0.935 \pm 0.054 & [\text{Lenz '14}] \\ 0.969 \pm 0.006 & [\text{HFLAV '19}] \end{cases}$$

◇ Shift of  $4.9\sigma$

# Quark Hadron Duality

Experiment at hadron level, calculation at quark-gluon level

★ Compare HQE with experiments:

◇ No sign of any significant deviation

◇  $\Delta\Gamma_s$  highly sensitive (fewer states, smaller phase space)

\* Good agreement

★ Simplified models of QCD:

◇ SV limit: no duality violation for SL and NL decays

[Boyd, Grinstein, Manohar '95; Grinstein, Savrov '03]

◇ 'tHooft model: no  $1/m_Q$  corrections, tiny oscillatory terms

[Grinstein, Lebed '97, '98, '01]

[Bigi, Shifman, Uraltsev, Vainshtein '98, '99, '00]