

9th Edition of the Large Hadron Collider Physics Conference
7th–12th June 2021

Jet Substructure + Correlations in Hadronic Final States from ATLAS

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On behalf of the ATLAS Collaboration



THE UNIVERSITY
OF BRITISH COLUMBIA

ATLAS

$\sqrt{s} = 13 \text{ TeV}, 139 \text{ fb}^{-1}, p_{T,1} > 675 \text{ GeV}$

$\ln(1/z)$

$z = p_{\text{emission}}^- / (p_{\text{emission}}^- + p_{\text{core}}^-)$

$\ln(R/\Delta R)$

$\Delta R = \Delta R(\text{emission, core})$

$(1/N_{\text{jets}}) d^2N_{\text{emissions}} / (\ln(1/z) d\ln(R/\Delta R))$

Coming soon

Hadronic event shapes

Event Shapes

Class of observables describing energy flow in multijet events

A good probe for strong-interaction processes

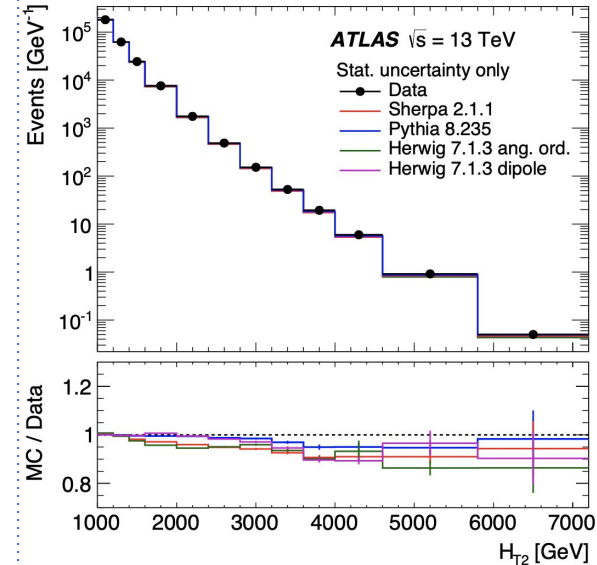
Great testing ground for multijet simulation

This measurement improves upon ATLAS Run-1 analysis ([arXiv:1206.2135](https://arxiv.org/abs/1206.2135))

- 139 fb⁻¹ of 13 TeV Run 2 data (>4000 x more!)
- High- p_T particle-flow jets
- Improved generators ([ATL-PHYS-PUB-2019-017](https://arxiv.org/abs/1901.01717))

Analysis

- Single-jet trigger $p_T > 460$ GeV
- Particle-flow, anti- k_t jets, $R = 0.4$
 - $p_T > 100$ GeV
 - $|\eta| < 2.4$
- Events
 - ≥ 2 jets with $H_{T2} > 1$ TeV
 - $H_{T2} = p_{T1} + p_{T2}$
- Unfolding:
 - Unfolded to particle-level using iterative Bayesian unfolding



Scalar sum of transverse momenta of the two leading jets + MC predictions

Hadronic event shapes

[Detailed definitions
in extra materials](#)

Thrust

T_{\perp} : transverse

T_m : minor component

Measures back-to-back
(dijet-like) configuration

Sphericity

S : spherical isotropic

S_{\perp} : transverse isotropic

Measures isotropic
distribution of radiation

Aplanarity

A

Measures the containment
of the radiation in a plane

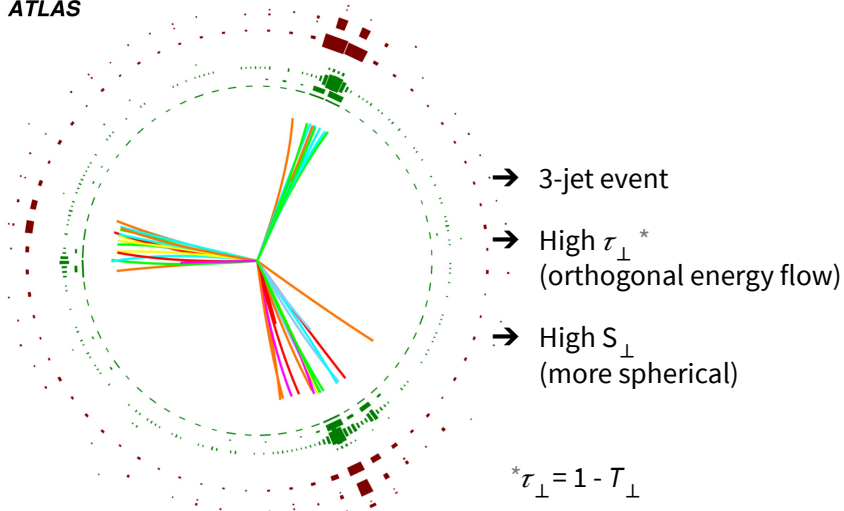
C & D

C : quadratic combination

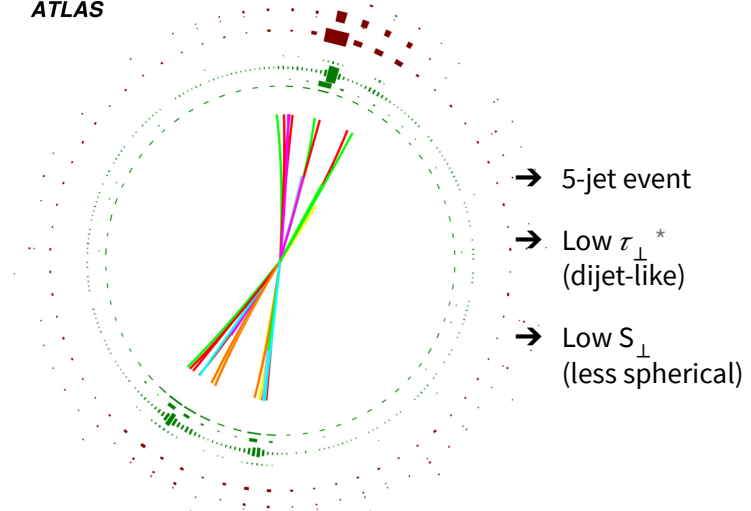
D : cubic combination

Quantities for 3+ and
4+ jet events

ATLAS

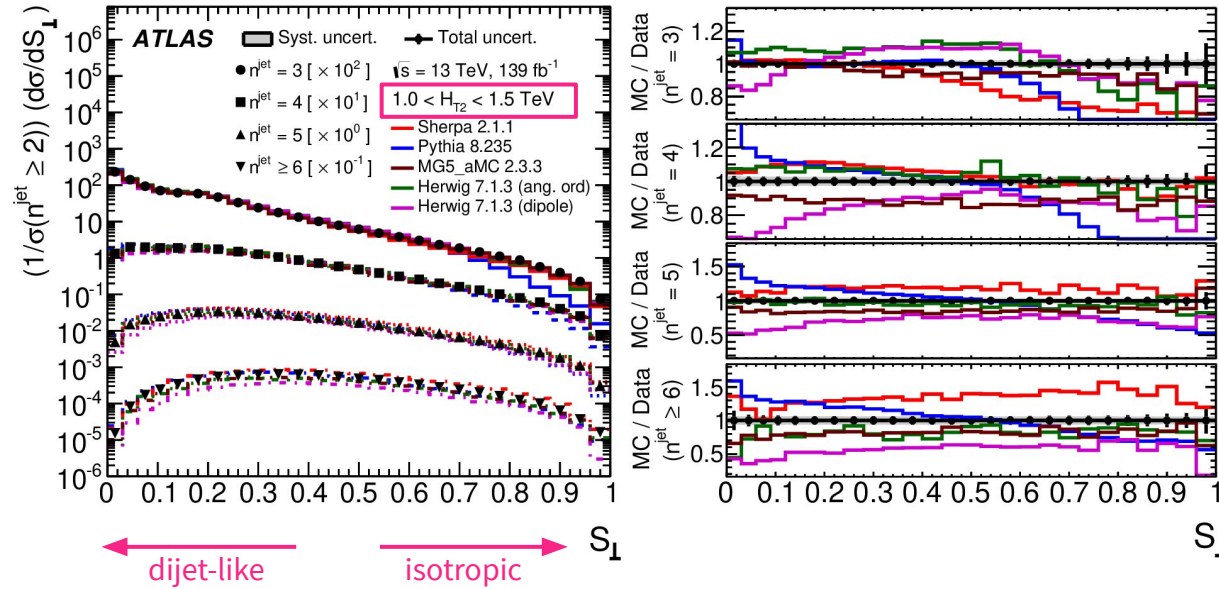


ATLAS



Hadronic event shapes

S_{\perp} : Transverse sphericity



Low n^{jet} :

Pythia and Sherpa agree in the dijet-like limit, but underestimate for isotropic events.

Herwig7 and MG5_aMC are closer.

Higher n^{jet} :

Shapes are improved, but overall cross section disagreement

Hadronic event shapes

Uncertainties

- **Modelling** and **Jet Energy Scale and Jet Energy Resolution** are dominant uncertainties
- **JES/JER** becomes more prominent for higher n^{jet} bins
 - Dominant JES/JER uncertainty is MC mis-modelling ([2007.02645](#))
- Total syst. uncertainty from ~1% to ~6% depending on n^{jet}

Observations

No MC predictions studied provide a good description in all regions of phase space

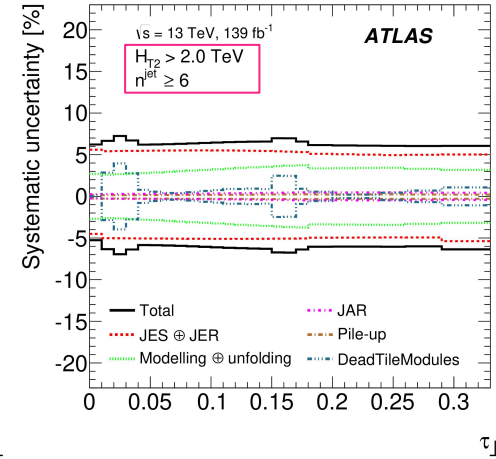
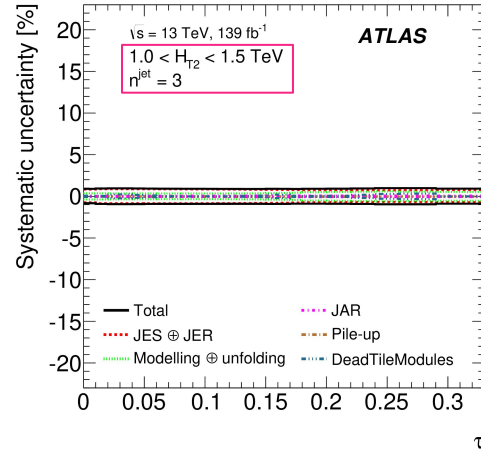
At low n^{jet} , **Pythia** and **Sherpa** underestimate measurements at high values of event-shape distributions.

- i.e. events in data appear to be more isotropic than predicted by simulation
- Parton shower models have trouble simulating hard and wide-angle radiation

Based on **Herwig7** simulation, angle-ordered parton showers perform better than dipole-based parton showers

MG5_aMC gives best overall shape agreement

- Includes up to 4 final-state partons
- Highlights importance of ME terms beyond LO for high- p_T multijet dynamics



Lund jet plane

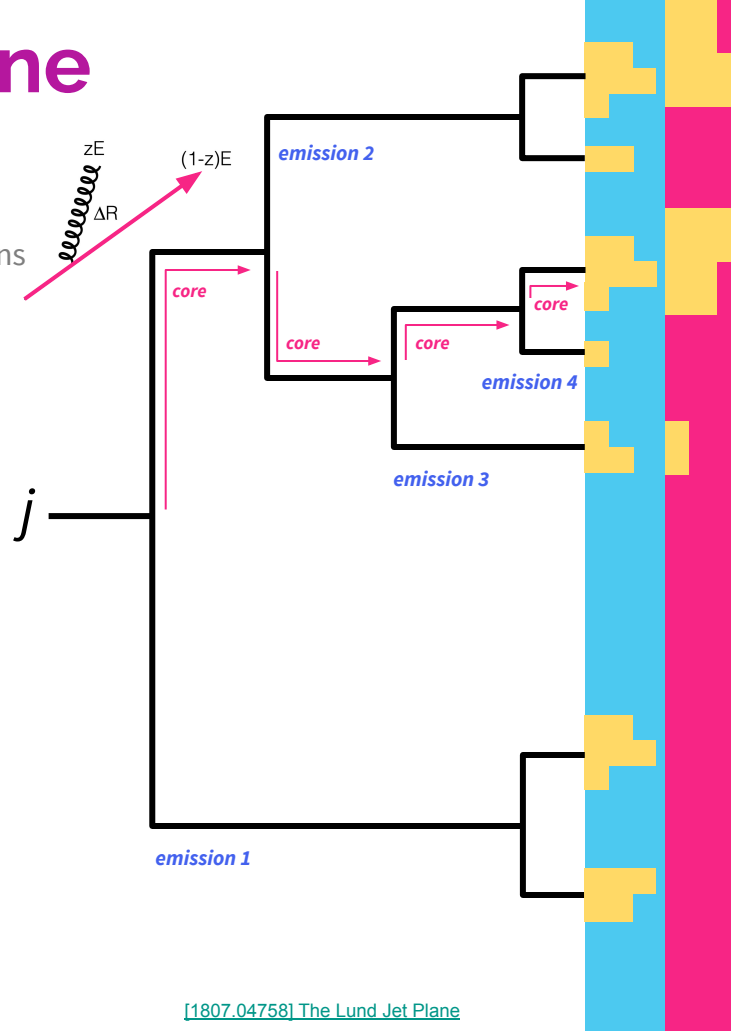
Jets can be approximated as a **core** parton **emitting** lower-energy gluons

→ The Cambridge/Aachen (C/A) reclustering algorithm combines **closest pairs** of deposits

← “Declustering” the jet in reverse populates the Lund Jet Plane (LJP) with the **widest-angle emission** at each node.

Emissions are parameterized in relative momentum fraction (z) and relative emission angle (ΔR)

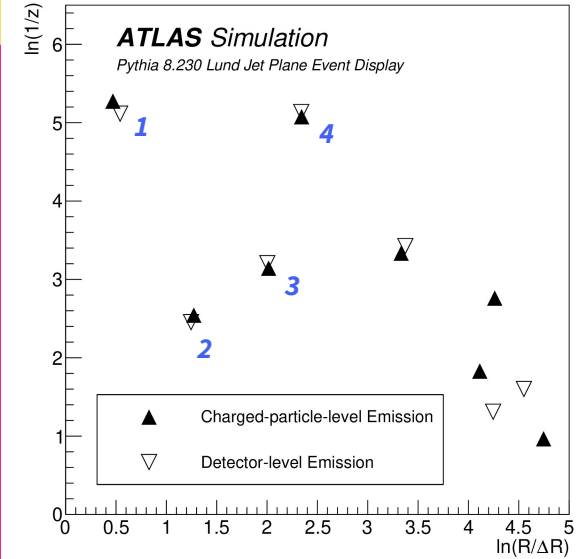
A single jet can be mapped to the LJP as a set of coordinates



[1807.04758] The Lund Jet Plane

y-axis: $\ln(1/z)$

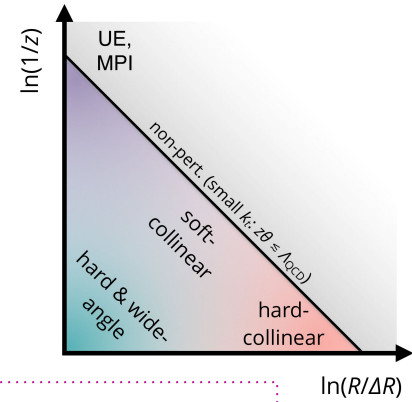
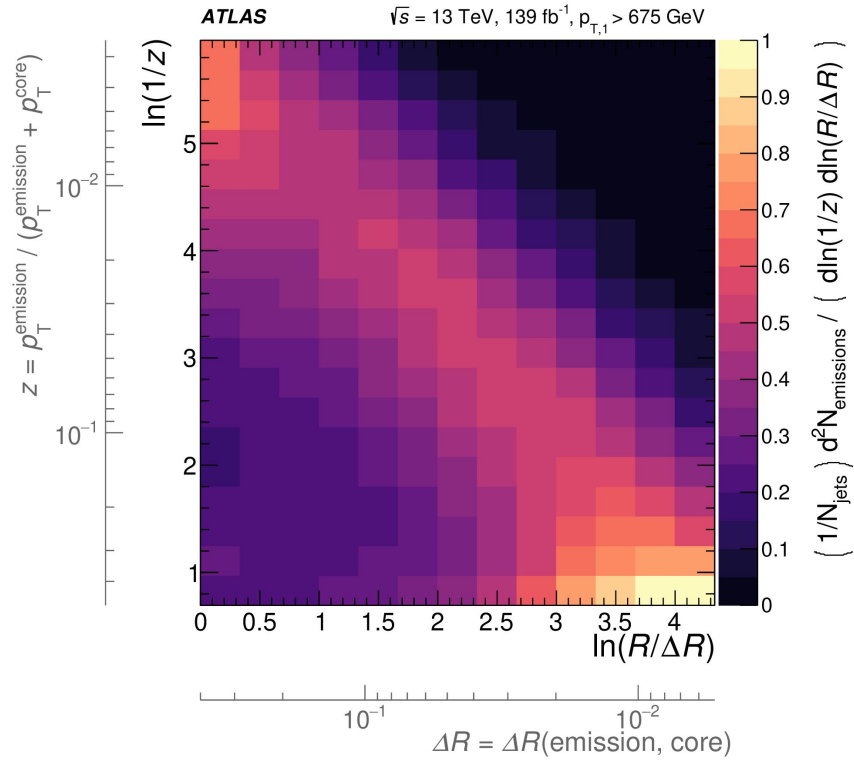
z = momentum fraction of emitted gluon relative to core



x-axis: $\ln(R/\Delta R)$

ΔR = angular separation of emitted gluon relative to core

Lund jet plane



An ensemble of jets can be plotted on the LJP and compared to simulation

~ 29.5 million (unfolded) jets collected by ATLAS are selected and plotted

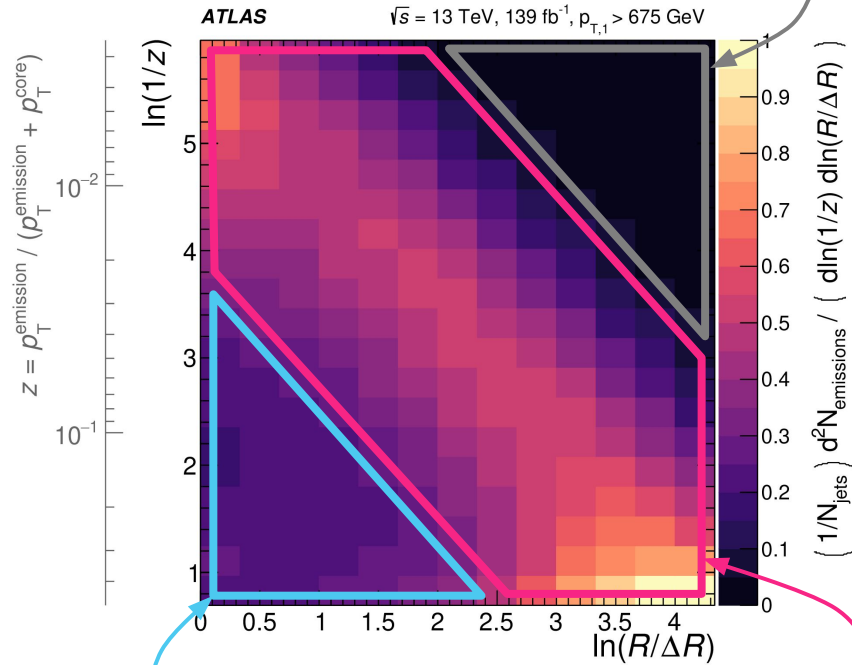
Jet selection:

- Single-jet triggered
- $|\eta| < 2.1$
- $p_{T, \text{leading}} > 675 \text{ GeV}$
- $p_{T, \text{leading}} / p_{T, \text{subleading}} < 1.5$

To simplify 2→2 interpretation of final state

Lund jet plane

very suppressed in NP region

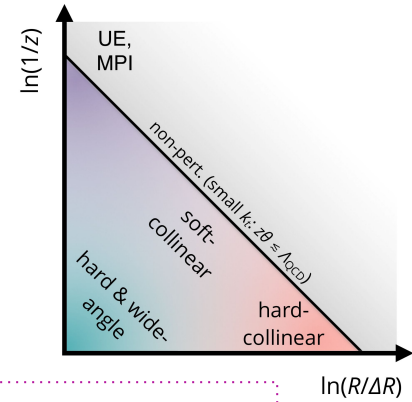


populated nearly uniformly by perturbative emissions

$$\Delta R = \Delta R(\text{emission, core})$$

$$\frac{1}{N_{\text{jets}}} \frac{d^2 N_{\text{emissions}}}{d \ln(1/z) d \ln(R/\Delta R)} \propto \text{constant}$$

large number of emissions found at the transition to the nonperturbative regime.
 α_s is enhanced for small values of k_t



An ensemble of jets can be plotted on the LJP and compared to simulation

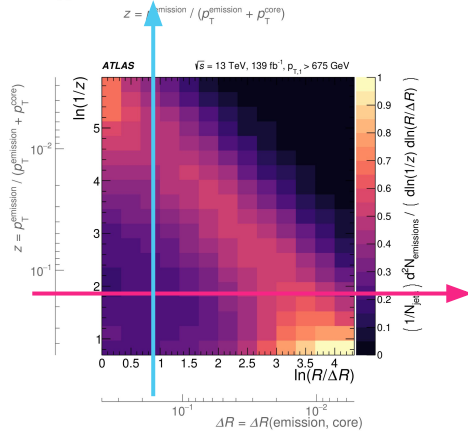
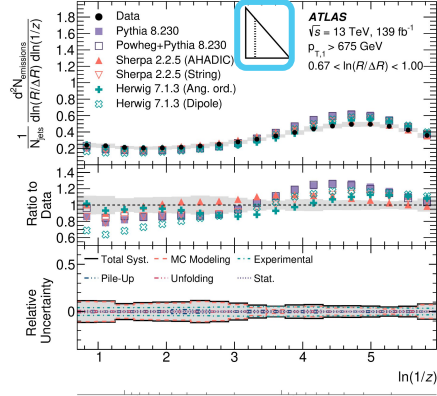
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To simplify 2→2 interpretation of final state

Lund jet plane

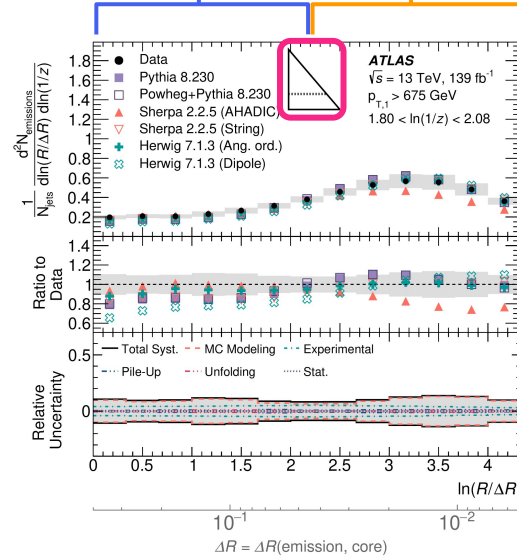


- + Herwig 7.1.3 (Ang. ord.)
- ⊗ Herwig 7.1.3 (Dipole)

Different **parton shower models** differ most significantly for **hard emissions** at **wide angles** (large values of k_t)

- ▲ Sherpa 2.2.5 (AHADIC)
- ▼ Sherpa 2.2.5 (String)

Different **hadronization models** differ most significantly for **soft collinear splittings**, at **transition to NP region** (small values of k_t)



Slices of the LJP are plotted and compared to MC generators with different **parton shower** and **hadronization** models.

No single model is found to be in agreement with the measured data across the entire plane

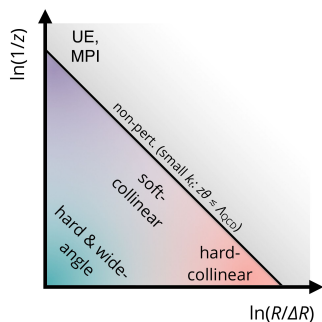
Can be useful for tuning NP models and for constraining the parameters of advanced parton shower programs

Lund jet plane

Ratios of the LJP using different hadronization or showering algorithms **can factorize physical effects**

Parton shower ratio shows difference in harder wider-angle emissions

Hadronization ratio shows where hadronization effects are isolated

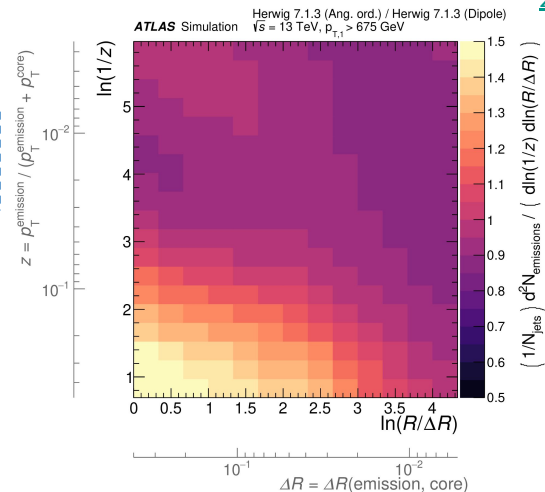


Herwig 7.1.3 +



Angle-ordered parton shower

Dipole parton shower

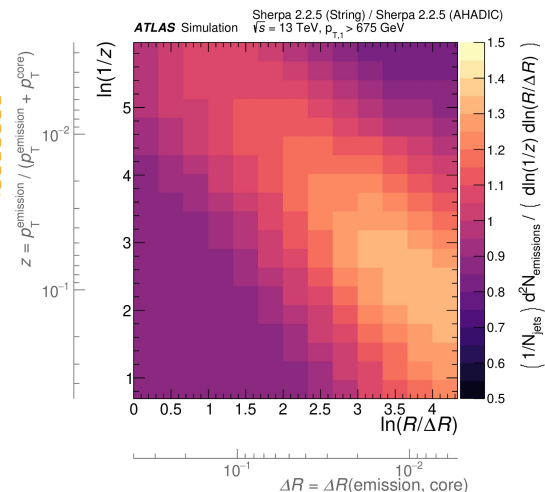


Sherpa 2.2.5 +



AHADIC cluster-based hadronization

LUND string-based hadronization



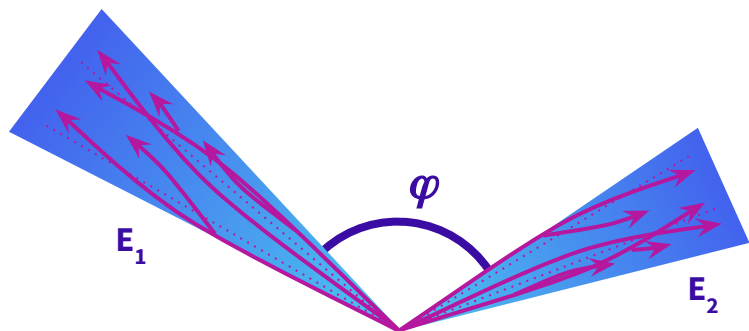
α_s measurement using (A)TEEC

Measurement of strong coupling

Uses full Run-2 dataset to measure α_s via evolution of TEEC/ATEEC with varying hard scale

Both observables are sensitive to QCD radiation and present a clear dependence with the strong coupling

Tests asymptotic freedom **beyond TeV scale** at NLO accuracy



Analysis

Jets:

Particle-flow, anti- k_t , $R = 0.4$
 $p_T > 60$ GeV, $|\eta| < 2.4$

Events:

≥ 2 jets with $H_{T2} > 1$ TeV
 $H_{T2} = p_{T1} + p_{T2}$ is proxy for hard interaction scale Q

[1006.2144](#)

Unfolding:

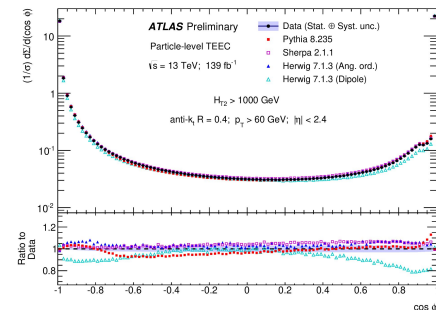
Unfolded to particle-level using iterative Bayesian unfolding

Calculation of α_s :

(A)TEEC distributions measured inclusively and in bins of H_{T2}
 $\alpha_s(m_Z)$ determined by fitting theor. predictions to distributions

TEEC — Transverse energy-energy correlation

ATEEC — Its associated azimuthal angular asymmetry



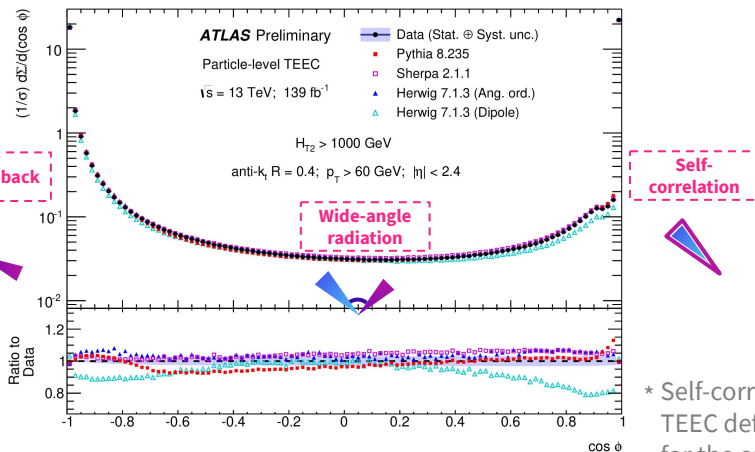
TEEC

Azimuthal distance between
any two jets

$$\frac{1}{\sigma} \frac{d\Sigma}{d \cos \phi} = \frac{1}{\sigma} \sum_{i,j} \int d\sigma \frac{E_{T,i} E_{T,j}}{(E_{T,i} + E_{T,j})^2} \delta(\cos \Delta\varphi_{ij} - \cos \phi)$$

TEEC function in multi-jet events defined as the **transverse energy-weighted azimuthal angular distribution of jet pairs in the final state**

- Peaks at $\cos(\phi) \approx -1$: **back to back** two-jet events and $\cos(\phi) \approx +1$: **self correlation***
- **Central plateau** : dominated by wide-angle radiation
- MC generators match data depending on $\cos(\phi)$ region



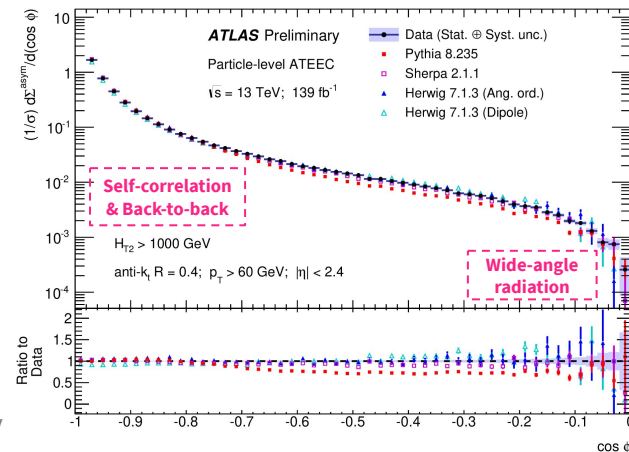
* Self-correlations are included in TEEC definition and are necessary for the correct normalization

ATEEC

$$\frac{1}{\sigma} \frac{d\Sigma^{\text{asymm}}}{d \cos \phi} = \frac{1}{\sigma} \left(\left. \frac{\Sigma}{d \cos \phi} \right|_{\phi} - \left. \frac{\Sigma}{d \cos \phi} \right|_{\pi-\phi} \right)$$

Measures the **difference between the forward** ($\cos \phi > 0$) **and the backward** ($\cos \phi < 0$) **TEEC**

- Eliminates uncertainties symmetric in $\cos(\phi)$
- Peaks at $\cos(\phi) \approx -1$ and drops off several orders of magnitude



α_s measurement using (A)TEEC

A(TEEC) binned in H_{T2} and $\alpha_s(m_Z)$ is determined by fitting theoretical predictions to the observed data

Fit is done per-bin and globally

For each bin, $\alpha_s(m_Z)$ is evolved to $\alpha_s(Q)$ using NLO solutions to the renormalization group equation

Extends $\alpha_s(Q)$ measurement to $Q > 1$ TeV

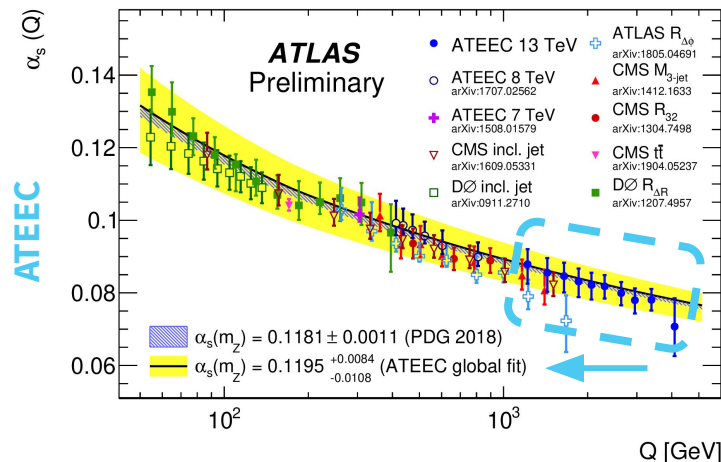
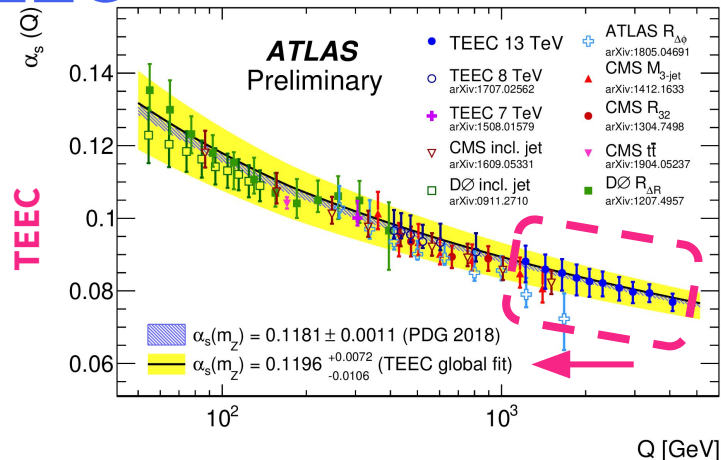
Tests RGE predictions at the highest energy scales ever!

Agrees well with PDG world average

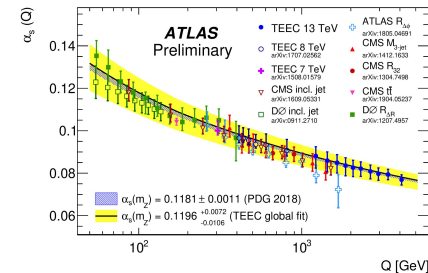
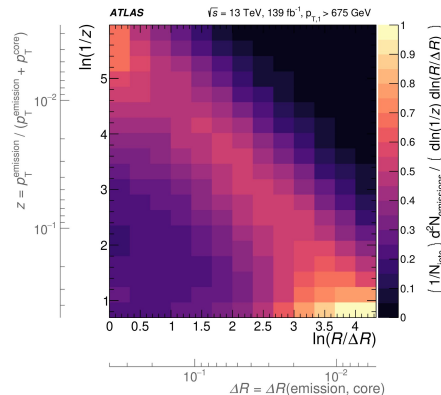
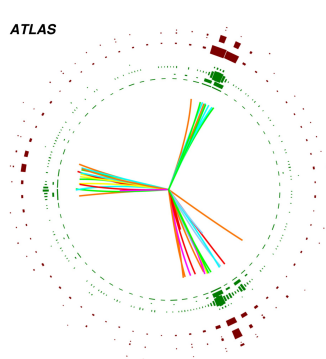
Comparison to previous analysis (8 TeV) [arXiv:1707.02562](https://arxiv.org/abs/1707.02562)

Uncertainties: Stat. 1.5% \rightarrow 0.5% — Syst. 5% \rightarrow 2%

Increase Q reach from .8 TeV \rightarrow 4 TeV



Conclusions



- Jet substructure and correlation measurements are used to understand and improve the performance of simulation, and to probe QCD
- Modelling uncertainties are dominant in many regions and no one generator performs well in all phase spaces
- The large quantity of events in the Run 2 dataset allows for multi-differential measurements, and precisions measurements of physical parameters

More jets & QCD in ATLAS at LHCP 2021

[Nucleon Structure and Soft QCD from ATLAS](#)

Andre Sopczak (Monday - *Nucleon Structure and Soft QCD*)

[Flavour-tagging / Jet / Met performance in ATLAS and CMS](#)

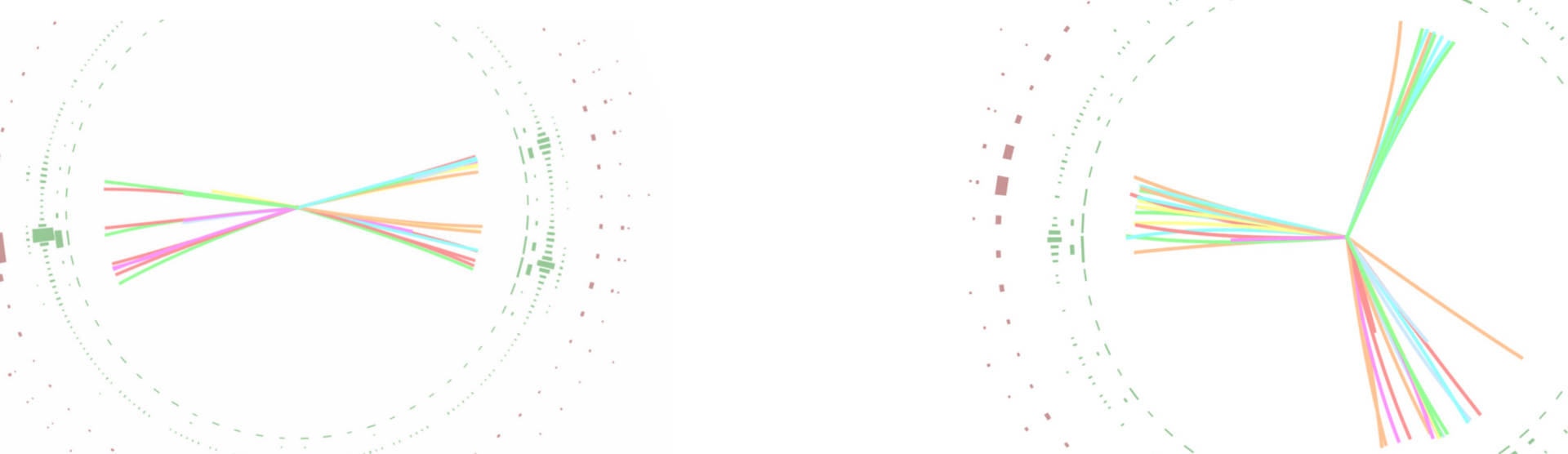
Jonathan Bossio (Thursday - *Detector performance*)

[Precision QCD Measurements from ATLAS](#)

Tibor Zenis (Thursday - *QCD: Precision Measurements*)

[Results on soft QCD at LHC and Tevatron](#)

Leszek Adamczyk (Friday - *Plenary VII: QCD Physics*)



Thank you for your attention!

Additional material

Hadronic event shapes

Thrust

Measures back-to-back dijet-like configuration

$$T_{\perp} = \frac{\sum_i |\vec{p}_{T,i} \cdot \hat{n}_T|}{\sum_i |\vec{p}_{T,i}|}$$

$$T_m = \frac{\sum_i |\vec{p}_{T,i} \times \hat{n}_T|}{\sum_i |\vec{p}_{T,i}|}$$

\hat{n}_T thrust axis – direction where jet momentum projection is maximized

$$\tau_{\perp} = 1 - T_{\perp}$$

Sphericity tensor

$$\mathcal{M}_{xyz} = \frac{1}{\sum_i |\vec{p}_i|} \sum_i \frac{1}{|\vec{p}_i|} \begin{pmatrix} p_{x,i}^2 & p_{x,i}p_{y,i} & p_{x,i}p_{z,i} \\ p_{y,i}p_{x,i} & p_{y,i}^2 & p_{y,i}p_{z,i} \\ p_{z,i}p_{x,i} & p_{z,i}p_{y,i} & p_{z,i}^2 \end{pmatrix} \quad \text{eigenvalues } \{\lambda_k\}$$

Transverse sphericity tensor

$$\mathcal{M}_{xy} = \frac{1}{\sum_i |\vec{p}_i|} \sum_i \frac{1}{|\vec{p}_i|} \begin{pmatrix} p_{x,i}^2 & p_{x,i}p_{y,i} \\ p_{y,i}p_{x,i} & p_{y,i}^2 \end{pmatrix} \quad \text{eigenvalues } \{\mu_k\}$$

Sphericity

$$S = \frac{3}{2}(\lambda_2 + \lambda_3)$$

Measures spherical isotropy

$$S_{\perp} = \frac{2\mu_2}{\mu_1 + \mu_2}$$

Measures planar isotropy

Aplanarity

$$A = \frac{3}{2}\lambda_3$$

Measures the containment of the radiation in a plane

C & D

Quadratic and cubic combinations of the eigenvalues

$$C = 3(\lambda_1\lambda_2 + \lambda_1\lambda_3 + \lambda_2\lambda_3)$$

3+ jet event shape

$$D = 27(\lambda_1\lambda_2\lambda_3)$$

4+ jet event shapes

Hadronic event shapes

Event shape definitions:

S_{\perp} : Alice Collaboration, **Transverse sphericity of primary charged particles**, [arXiv:1205.3963](https://arxiv.org/abs/1205.3963)

A , C and D : CMS Collaboration, **Study of the UE in top quark pair production**, [arXiv:1807.02810](https://arxiv.org/abs/1807.02810)

τ_{\perp} , T_m : CMS Collaboration, **First measurement of hadronic event shapes**, [arXiv:1102.0068](https://arxiv.org/abs/1102.0068)

τ_{\perp} : CMS Collaboration, **Event shapes and azimuthal correlations in Z + jets events**, [arXiv:1301.1646](https://arxiv.org/abs/1301.1646)

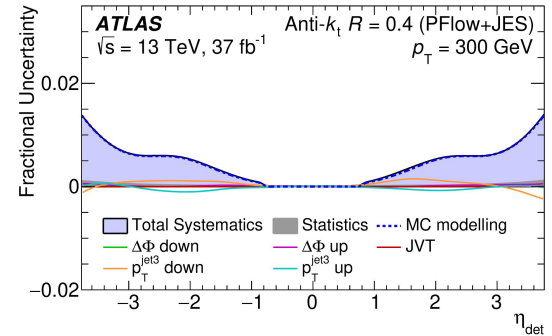
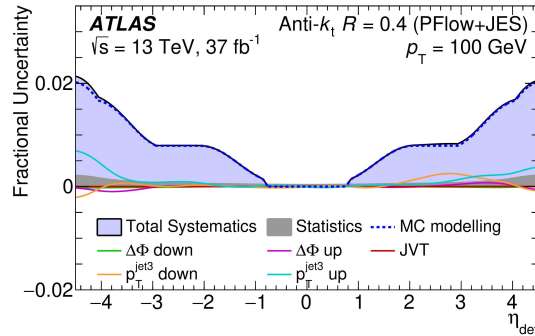
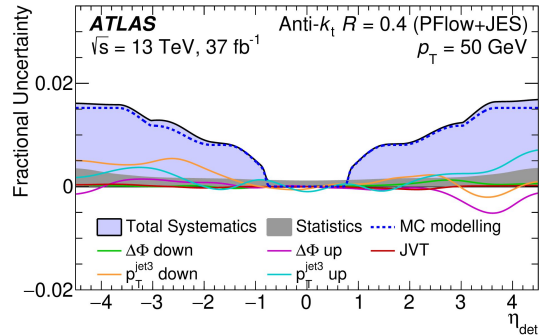
τ_{\perp} : CMS Collaboration, **Event shapes variables measured using multijet final states**, [arXiv:1811.00588](https://arxiv.org/abs/1811.00588)

A , T_m , $S_{\alpha,\beta}$: C. Chen, **New approach to identifying boosted hadronically decaying particles using jet substructure**, [arXiv:1112.2567](https://arxiv.org/abs/1112.2567)

Hadronic event shapes

The dominant uncertainty is in MC mis-modelling and is taken to be the difference between the smoothed calibration curves derived from the Powheg+Pythia8 and Sherpa dijet samples.

<https://arxiv.org/abs/2007.02645> (Sec. 5.2.1)



Lund jet plane

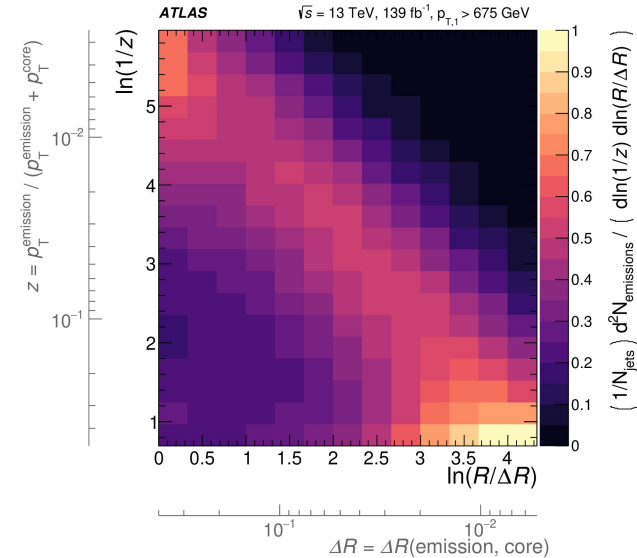
Why this choice of axes?

The LJP is sometimes depicted with the y-axis representing $\ln(k_t)$.

The choice of using z instead of k_t is to decouple the angular (x-axis) and momentum (y-axis) measurements as the resolution of each can differ substantially.

Historically, both choices of axes have been used.

$$k_t \sim z^* \Delta R$$



Discussion of variables: [arXiv:1807.04758](https://arxiv.org/abs/1807.04758) Sec. 2.1

α_s measurement using (A)TEEC

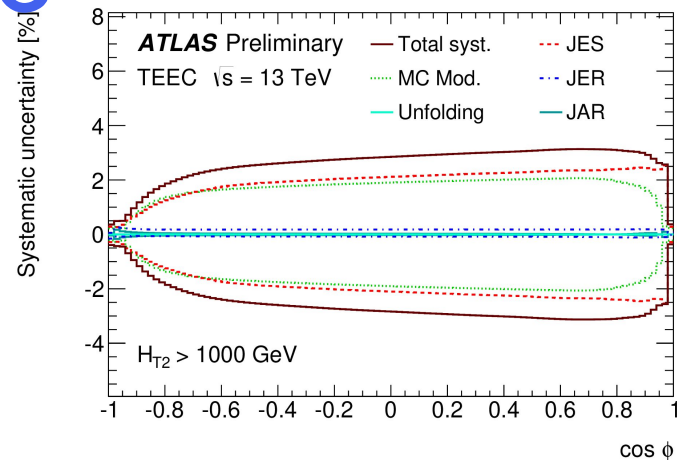
Dominant systematics

TEEC systematic uncertainties are dominated by
Jet Energy Scale (< 2%) and
modelling of the strong interaction (< 2%)

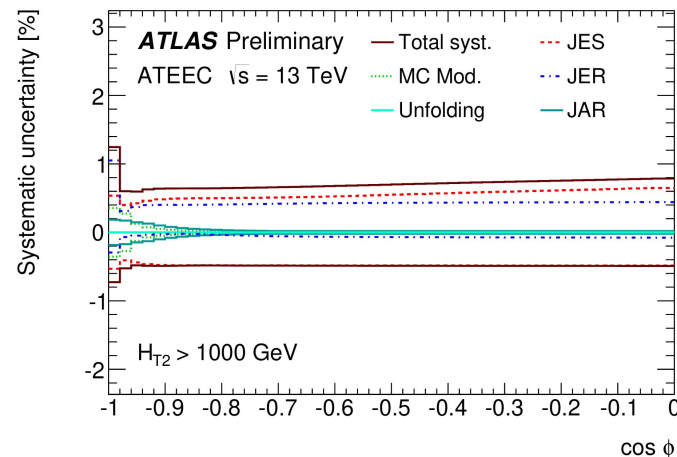
ATEEC systematic uncertainties are dominated by
Jet Energy Scale (< 1%) and
Jet Energy Resolution (< 1%)

Other sources of systematic uncertainty include:
 Jet Angular Resolution (< 0.5%) and
 Unfolding uncertainty (negligible)

TEEC



ATEEC



α_s measurement using (A)TEEC

The values of $\alpha_s(m_Z)$ determined from fits to the (A)TEEC functions, in inclusive and exclusive H_{T2} bins, and global fit.

TEEC

$\langle Q \rangle$ [GeV]	$\alpha_s(m_Z)$ value (MMHT 2014)			χ^2/N_{dof}
Global	0.1196 ± 0.0001 (stat.) ± 0.0004 (syst.) $^{+0.0071}_{-0.0104}$ (scale) ± 0.0011 (PDF) ± 0.0002 (NP)			235.8 / 347
Inclusive	0.1208 ± 0.0002 (stat.) ± 0.0006 (syst.) $^{+0.0081}_{-0.0101}$ (scale) ± 0.0009 (PDF) ± 0.0002 (NP)			42.7 / 91
1219	0.1206 ± 0.0002 (stat.) ± 0.0006 (syst.) $^{+0.0083}_{-0.0105}$ (scale) ± 0.0009 (PDF) ± 0.0003 (NP)			18.6 / 51
1434	0.1191 ± 0.0003 (stat.) ± 0.0007 (syst.) $^{+0.0080}_{-0.0101}$ (scale) ± 0.0010 (PDF) ± 0.0002 (NP)			18.0 / 51
1647	0.1195 ± 0.0002 (stat.) ± 0.0007 (syst.) $^{+0.0077}_{-0.0094}$ (scale) ± 0.0011 (PDF) ± 0.0002 (NP)			38.2 / 51
1856	0.1186 ± 0.0003 (stat.) ± 0.0008 (syst.) $^{+0.0076}_{-0.0094}$ (scale) ± 0.0011 (PDF) ± 0.0004 (NP)			25.9 / 51
2064	0.1183 ± 0.0004 (stat.) ± 0.0010 (syst.) $^{+0.0071}_{-0.0084}$ (scale) ± 0.0012 (PDF) ± 0.0005 (NP)			22.4 / 27
2300	0.1192 ± 0.0004 (stat.) ± 0.0011 (syst.) $^{+0.0066}_{-0.0075}$ (scale) ± 0.0012 (PDF) ± 0.0004 (NP)			21.3 / 27
2636	0.1185 ± 0.0004 (stat.) ± 0.0012 (syst.) $^{+0.0064}_{-0.0072}$ (scale) ± 0.0012 (PDF) ± 0.0001 (NP)			22.0 / 27
2952	0.1179 ± 0.0005 (stat.) ± 0.0014 (syst.) $^{+0.0059}_{-0.0064}$ (scale) ± 0.0013 (PDF) ± 0.0003 (NP)			25.0 / 27
3383	0.1194 ± 0.0007 (stat.) ± 0.0014 (syst.) $^{+0.0052}_{-0.0052}$ (scale) ± 0.0013 (PDF) ± 0.0002 (NP)			15.3 / 13
4095	0.1167 ± 0.0010 (stat.) ± 0.0014 (syst.) $^{+0.0050}_{-0.0053}$ (scale) ± 0.0015 (PDF) ± 0.0003 (NP)			13.5 / 13

Table 2: Values of the strong coupling constant at the Z boson mass scale, $\alpha_s(m_Z)$, obtained from fits to the TEEC function using MMHT 2014 parton distribution functions. The values of the average interaction scale $\langle Q \rangle$ are shown in the first column, while the values of the χ^2 function at the minimum are shown in the third column. The uncertainty referred to as NP is the one related to the non-pQCD corrections.

Scale:

The renormalisation scale is set for each event to the scalar sum of the transverse momenta of all final-state partons, $\mu_R = \hat{H}_T$, while the factorisation scale is set to half this scale, $\mu_F = \hat{H}_T/2$.

[[arXiv:1807.03692](https://arxiv.org/abs/1807.03692), [arXiv:2007.02645](https://arxiv.org/abs/2007.02645)]

ATEEC

$\langle Q \rangle$ [GeV]	$\alpha_s(m_Z)$ value (MMHT 2014)			χ^2/N_{dof}
Global	0.1195 ± 0.0002 (stat.) ± 0.0006 (syst.) $^{+0.0084}_{-0.0106}$ (scale) ± 0.0009 (PDF) ± 0.0003 (NP)			254.1 / 173
Inclusive	0.1198 ± 0.0002 (stat.) ± 0.0006 (syst.) $^{+0.0078}_{-0.0095}$ (scale) ± 0.0010 (PDF) ± 0.0002 (NP)			46.3 / 45
1219	0.1202 ± 0.0003 (stat.) ± 0.0006 (syst.) $^{+0.0079}_{-0.0098}$ (scale) ± 0.0010 (PDF) ± 0.0002 (NP)			25.7 / 25
1434	0.1184 ± 0.0003 (stat.) ± 0.0007 (syst.) $^{+0.0078}_{-0.0098}$ (scale) ± 0.0011 (PDF) ± 0.0002 (NP)			35.6 / 25
1647	0.1188 ± 0.0004 (stat.) ± 0.0007 (syst.) $^{+0.0073}_{-0.0087}$ (scale) ± 0.0012 (PDF) ± 0.0001 (NP)			41.9 / 25
1856	0.1177 ± 0.0006 (stat.) ± 0.0008 (syst.) $^{+0.0072}_{-0.0083}$ (scale) ± 0.0013 (PDF) ± 0.0006 (NP)			24.6 / 25
2064	0.1174 ± 0.0008 (stat.) ± 0.0009 (syst.) $^{+0.0069}_{-0.0078}$ (scale) ± 0.0013 (PDF) ± 0.0007 (NP)			18.7 / 13
2300	0.1185 ± 0.0009 (stat.) ± 0.0010 (syst.) $^{+0.0063}_{-0.0067}$ (scale) ± 0.0014 (PDF) ± 0.0005 (NP)			22.5 / 13
2636	0.1166 ± 0.0016 (stat.) ± 0.0012 (syst.) $^{+0.0062}_{-0.0066}$ (scale) ± 0.0015 (PDF) ± 0.0000 (NP)			21.7 / 13
2952	0.1141 ± 0.0029 (stat.) ± 0.0013 (syst.) $^{+0.0062}_{-0.0069}$ (scale) ± 0.0018 (PDF) ± 0.0003 (NP)			15.2 / 13
3383	0.1164 ± 0.0043 (stat.) ± 0.0015 (syst.) $^{+0.0050}_{-0.0044}$ (scale) ± 0.0017 (PDF) ± 0.0001 (NP)			6.3 / 6
4095	0.1029 ± 0.0163 (stat.) ± 0.0014 (syst.) $^{+0.0066}_{-0.0012}$ (scale) ± 0.0010 (PDF) ± 0.0003 (NP)			5.9 / 6

Table 3: Values of the strong coupling constant at the Z boson mass scale, $\alpha_s(m_Z)$, obtained from fits to the ATEEC function using MMHT 2014 parton distribution functions. The values of the average interaction scale $\langle Q \rangle$ are shown in the first column, while the values of the χ^2 function at the minimum are shown in the third column. The uncertainty referred to as NP is the one related to the non-pQCD corrections.