

# Photon-induced processes

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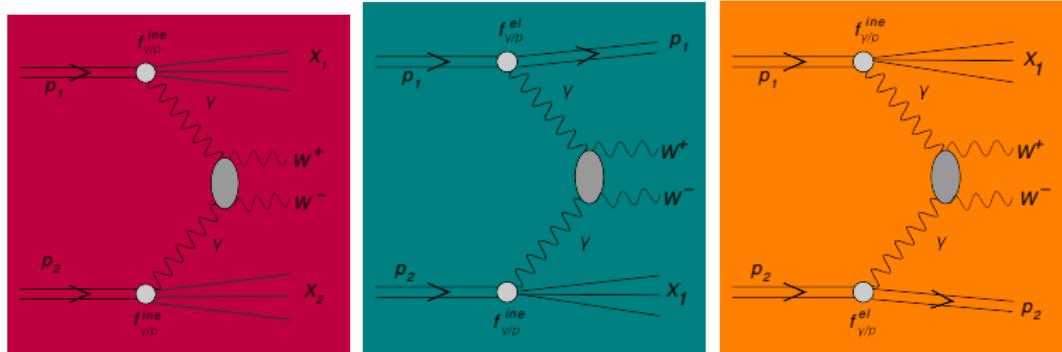
June 8, 2021

# Introduction ( $p + p$ collisions)

- Precise calculations of various electroweak reactions in  **$p p$  collisions** at the LHC need to account for, on top of the higher-order corrections, the effects of photon-induced processes.
- **production of lepton pairs**
  - M. Luszczak, W. Schafer and A. Szczurek,  
*Phys. Rev. D93 (2016) 074018*
  - B. Linek, M. Luszczak and A. Szczurek,  
paper in preparation
- **pairs of electroweak bosons**
  - M. Luszczak, A. Szczurek and Ch. Royon,  
*JHEP 1502 (2015) 098*
  - M. Luszczak, W. Schafer and A. Szczurek,  
*JHEP 1805 (2018) 064*
  - L. Forthomme, M. Luszczak, W. Schafer and A. Szczurek, *Phys.Lett. B789 (2019) 300-307*
- **production of  $t\bar{t}$  pairs**
  - M. Luszczak, L. Forthomme, W. Schafer and A. Szczurek,  
*JHEP 02 (2019) 100*

# Inclusive $\gamma\gamma \rightarrow W^+W^-$ mechanism

- $\gamma\gamma$  processes contribute also to inclusive cross section



$$\frac{d\sigma^{\gamma_{in}\gamma_{in}}}{dy_1 dy_2 d^2 p_t} = \frac{1}{16\pi^2 \hat{s}^2} x_1 \gamma_{in}(x_1, \mu^2) x_2 \gamma_{in}(x_2, \mu^2) |\mathcal{M}_{\gamma\gamma \rightarrow W^+W^-}|^2$$

$$\frac{d\sigma^{\gamma_{el}\gamma_{in}}}{dy_1 dy_2 d^2 p_t} = \frac{1}{16\pi^2 \hat{s}^2} x_1 \gamma_{el}(x_1, \mu^2) x_2 \gamma_{in}(x_2, \mu^2) |\mathcal{M}_{\gamma\gamma \rightarrow W^+W^-}|^2$$

$$\frac{d\sigma^{\gamma_{in}\gamma_{el}}}{dy_1 dy_2 d^2 p_t} = \frac{1}{16\pi^2 \hat{s}^2} x_1 \gamma_{in}(x_1, \mu^2) x_2 \gamma_{el}(x_2, \mu^2) |\mathcal{M}_{\gamma\gamma \rightarrow W^+W^-}|^2$$

# QED parton distributions

## • MRST-QED parton distributions

- QED-corrected evolution equations for the parton distributions of the proton

$$\begin{aligned}\frac{\partial \mathbf{q}_i(x, \mu^2)}{\partial \log \mu^2} &= \frac{\alpha_S}{2\pi} \int_x^1 \frac{dy}{y} \left\{ P_{qq}(y) \mathbf{q}_i\left(\frac{x}{y}, \mu^2\right) + P_{qg}(y) \mathbf{g}\left(\frac{x}{y}, \mu^2\right) \right\} \\ &\quad + \frac{\alpha}{2\pi} \int_x^1 \frac{dy}{y} \left\{ \tilde{P}_{qq}(y) e_i^2 \mathbf{q}_i\left(\frac{x}{y}, \mu^2\right) + P_{q\gamma}(y) e_i^2 \gamma\left(\frac{x}{y}, \mu^2\right) \right\} \\ \frac{\partial \mathbf{g}(x, \mu^2)}{\partial \log \mu^2} &= \frac{\alpha_S}{2\pi} \int_x^1 \frac{dy}{y} \left\{ P_{gq}(y) \sum_j \mathbf{q}_j\left(\frac{x}{y}, \mu^2\right) + P_{gg}(y) \mathbf{g}\left(\frac{x}{y}, \mu^2\right) \right\} \\ \frac{\partial \gamma(x, \mu^2)}{\partial \log \mu^2} &= \frac{\alpha}{2\pi} \int_x^1 \frac{dy}{y} \left\{ P_{\gamma q}(y) \sum_j e_j^2 \mathbf{q}_j\left(\frac{x}{y}, \mu^2\right) + P_{\gamma\gamma}(y) \gamma\left(\frac{x}{y}, \mu^2\right) \right\}\end{aligned}$$

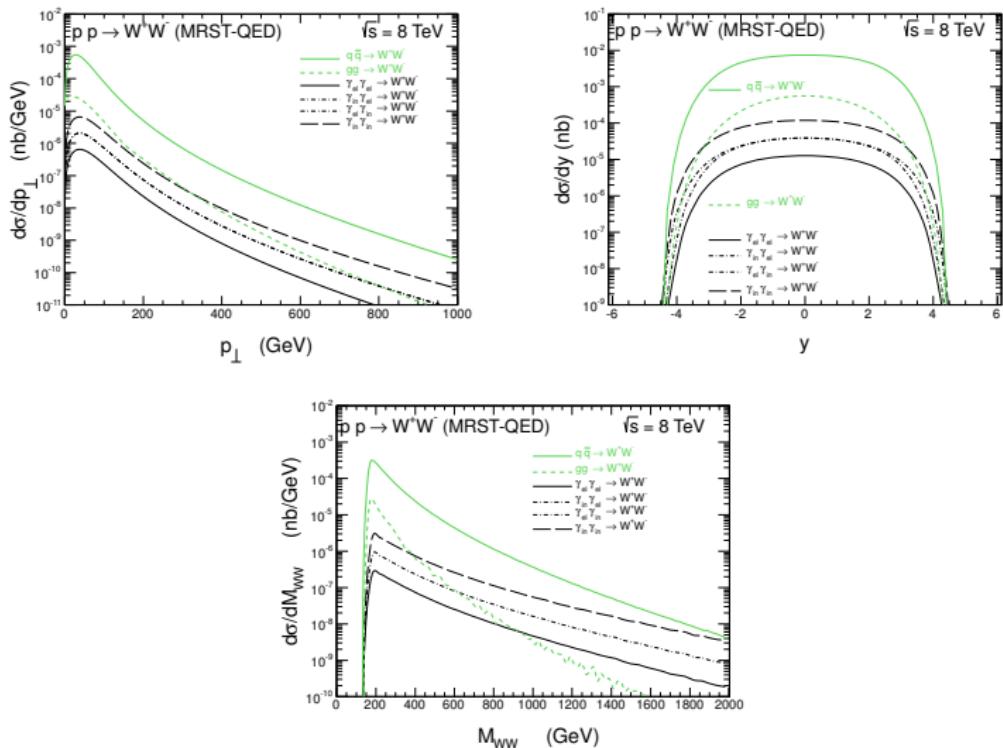
## • NNPDF2.3 parton distributions

- fit to deep-inelastic scattering (DIS) and Drell-Yan data

## • LUXqed17 parton distributions

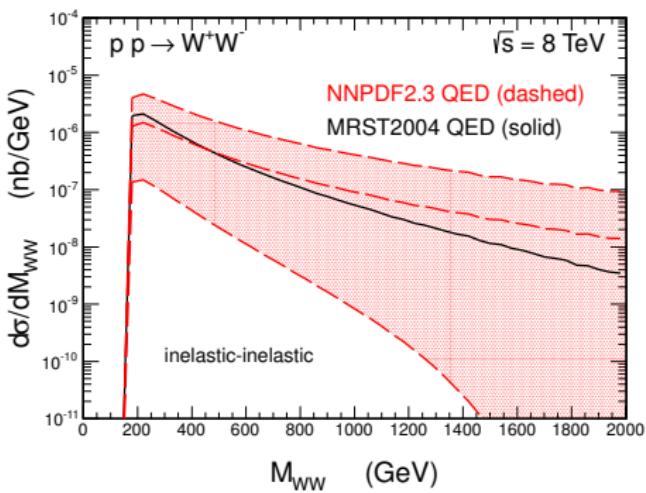
- integral over proton structure functions  $F_2(x, Q^2)$  and  $F_L(x, Q^2)$

# Results for MRSTQ parton distributions



M. Luszczak, A. Szczurek and Ch. Royon, JHEP 1502 (2015) 098

# NNPDF2.3 QED photon distributions



big uncertainties for large  $WW$  invariant masses

- very difficult to obtain the photon distributions from fits to experimental data

M. Łuszczak, A. Szczurek and Ch. Royon, JHEP 1502 (2015) 098

# $k_T$ -factorization approach

- the unintegrated photon fluxes can be expressed in terms of the hadronic tensor

$$\mathcal{F}_{\gamma^* \leftarrow A}^{\text{in,el}}(z, \mathbf{q}) = \frac{\alpha_{\text{em}}}{\pi} (1-z) \left( \frac{\mathbf{q}^2}{\mathbf{q}^2 + z(M_X^2 - m_A^2) + z^2 m_A^2} \right)^2 \cdot \frac{p_B^\mu p_B^\nu}{s^2} W_{\mu\nu}^{\text{in,el}}(M_X^2, Q^2) dM_X^2$$

- they enter the cross section for  $W^+W^-$  production

$$\frac{d\sigma^{(i,j)}}{dy_1 dy_2 d^2\mathbf{p}_1 d^2\mathbf{p}_2} = \int \frac{d^2\mathbf{q}_1}{\pi q_1^2} \frac{d^2\mathbf{q}_2}{\pi q_2^2} \mathcal{F}_{\gamma^*/A}^{(i)}(x_1, \mathbf{q}_1) \mathcal{F}_{\gamma^*/B}^{(j)}(x_2, \mathbf{q}_2) \frac{d\sigma^*(p_1, p_2; \mathbf{q}_1, \mathbf{q}_2)}{dy_1 dy_2 d^2\mathbf{p}_1 d^2\mathbf{p}_2}$$

- the longitudinal momentum fractions of  $W^+W^-$  are obtained from the rapidities and transverse momenta of final state

$$x_1 = \sqrt{\frac{\mathbf{p}_1^2 + m_W^2}{s}} e^{y_W} + \sqrt{\frac{\mathbf{p}_2^2 + m_W^2}{s}} e^{y_W},$$
$$x_2 = \sqrt{\frac{\mathbf{p}_1^2 + m_W^2}{s}} e^{-y_W} + \sqrt{\frac{\mathbf{p}_2^2 + m_W^2}{s}} e^{-y_W}$$

# Unintegrated photon fluxes

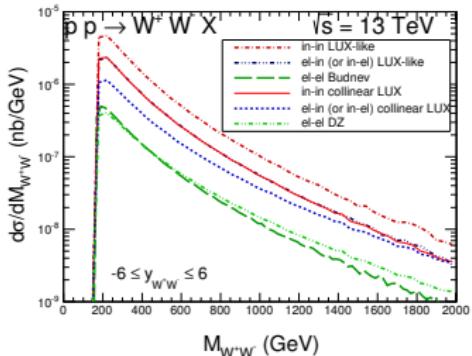
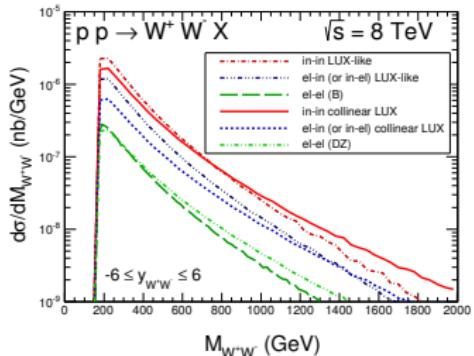
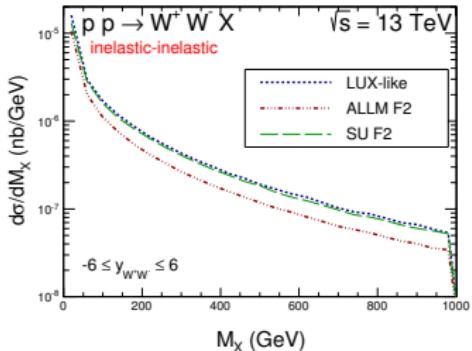
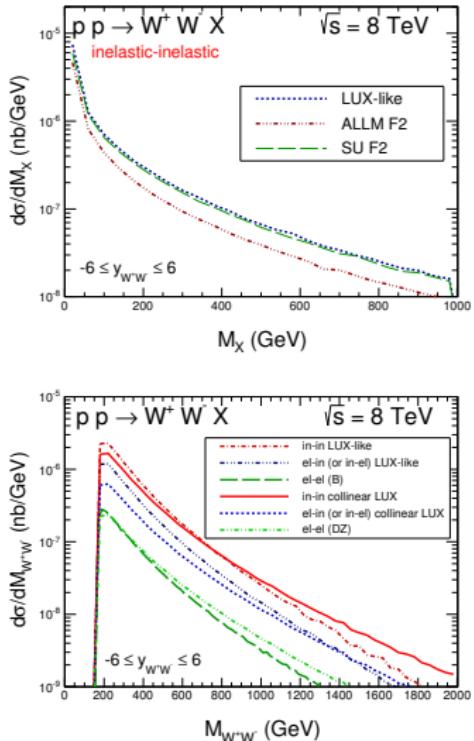
- the inelastic fluxes need the proton structure functions  $F_2(Bj, Q^2)$  and  $F_L(Bj, Q^2)$ .

$$\begin{aligned}\mathcal{F}_{\gamma^* \leftarrow A}^{\text{in}}(z, \mathbf{q}) &= \frac{\alpha_{\text{em}}}{\pi} \left\{ (1-z) \left( \frac{\mathbf{q}^2}{\mathbf{q}^2 + z(M_X^2 - m_A^2) + z^2 m_A^2} \right)^2 \frac{F_2(x_{Bj}, Q^2)}{Q^2 + M_X^2 - m_p^2} \right. \\ &+ \left. \frac{z^2}{4x_{Bj}^2} \frac{\mathbf{q}^2}{\mathbf{q}^2 + z(M_X^2 - m_A^2) + z^2 m_A^2} \frac{2x_{Bj} F_1(x_{Bj}, Q^2)}{Q^2 + M_X^2 - m_p^2} \right\}\end{aligned}$$

- elastic pieces only require the standard electromagnetic form factors of a proton

$$\begin{aligned}\mathcal{F}_{\gamma^* \leftarrow A}^{\text{el}}(z, \mathbf{q}) &= \frac{\alpha_{\text{em}}}{\pi} \left\{ (1-z) \left( \frac{\mathbf{q}^2}{\mathbf{q}^2 + z(M_X^2 - m_A^2) + z^2 m_A^2} \right)^2 \frac{4m_p^2 G_E^2(Q^2) + Q^2 G_M^2(Q^2)}{4m_p^2 + Q^2} \right. \\ &+ \left. \frac{z^2}{4} \frac{\mathbf{q}^2}{\mathbf{q}^2 + z(M_X^2 - m_A^2) + z^2 m_A^2} G_M^2(Q^2) \right\}\end{aligned}$$

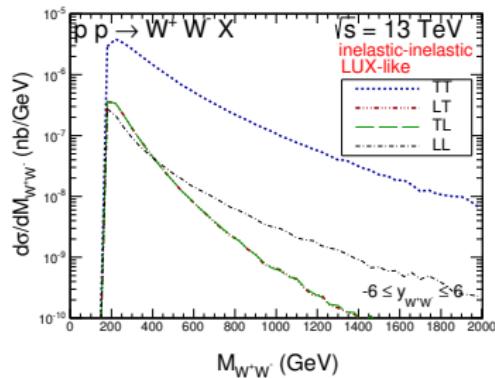
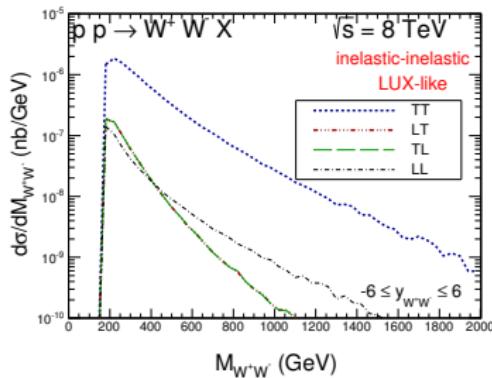
# Results for $k_T$ -factorization approach



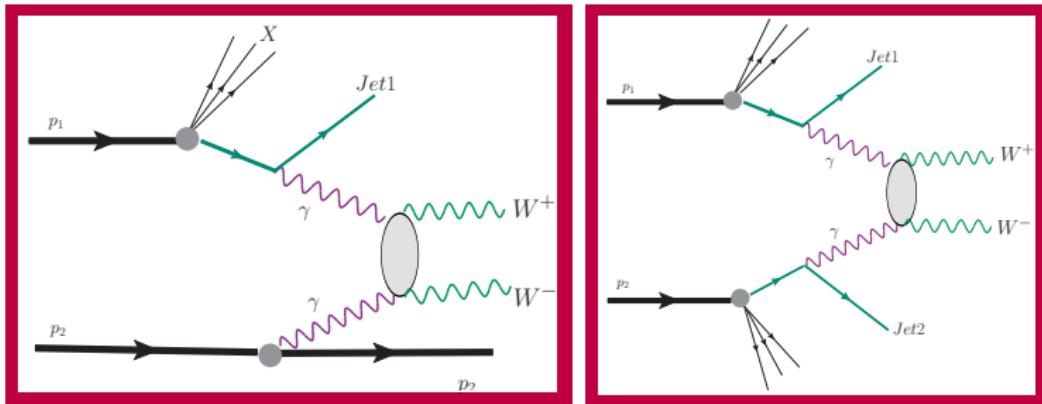
# Results, spin decompositions

contribution	8 TeV	13 TeV
TT	0.405	0.950
LL	0.017	0.046
LT + TL	$0.028 + 0.028$	$0.052 + 0.052$
SUM	0.478	1.090

Table: Contributions of different polarizations of  $W$  bosons for the inelastic-inelastic component for the LUX-like structure function. The cross sections are given in  $pb$ .



# Rapidity gap survival factors caused by remnant fragmentation



implementation of the above process

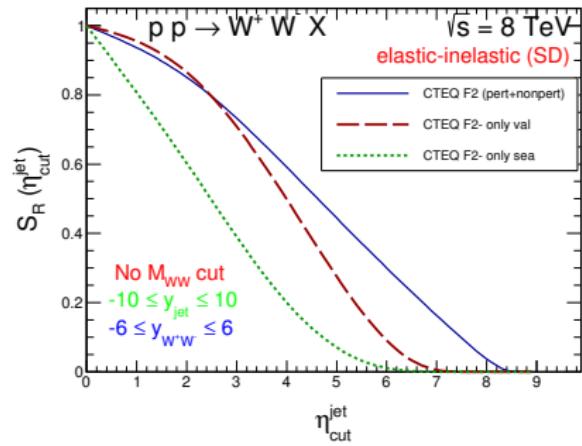
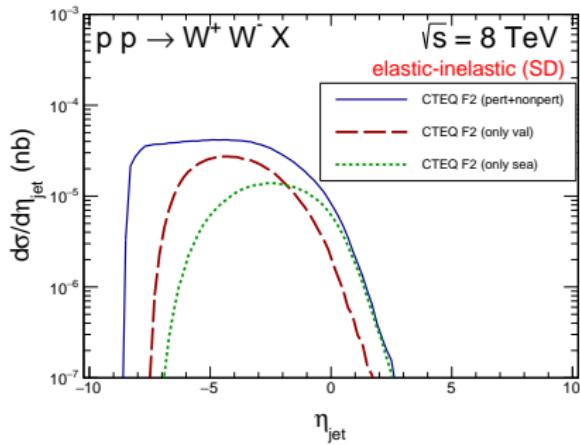
in CepGen for the Monte-Carlo generation of unweighted events

the hadronisation of remnant states  $X$  and/or  $Y$  systems

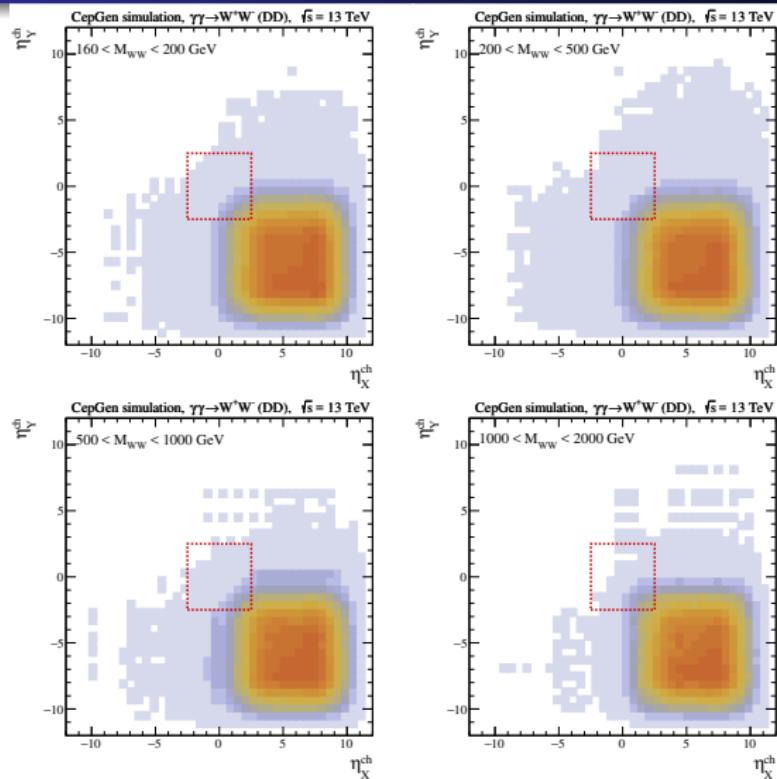
is performed using the Lund fragmentation algorithm implemented in Pythia8, and interfaced to CepGen.

# Parton level approach for single dissociation

$$S_R(\eta_{\text{cut}}) = 1 - \frac{1}{\sigma} \int_{-\eta_{\text{cut}}}^{\eta_{\text{cut}}} \frac{d\sigma}{d\eta_{\text{jet}}} d\eta_{\text{jet}}$$

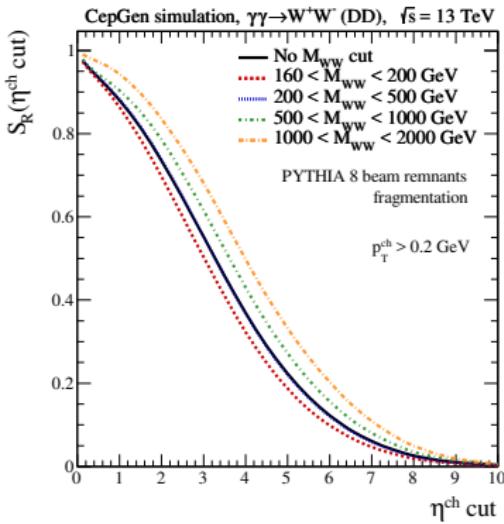
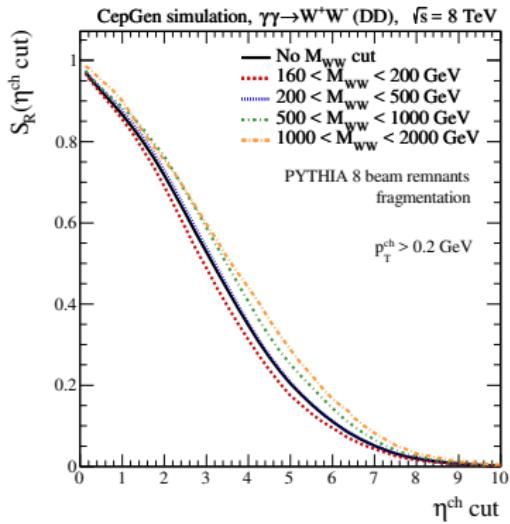


# Double dissociation



- distributions in pseudorapidity of particles from  $X$  ( $\eta_X^{\text{ch}}$ ) and  $Y$  ( $\eta_Y^{\text{ch}}$ )

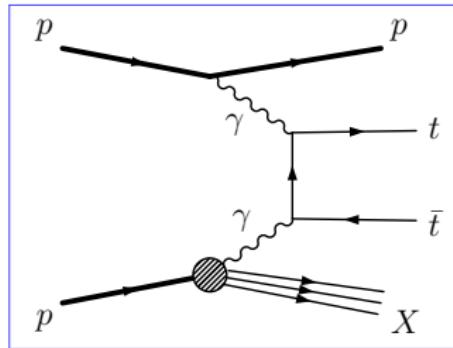
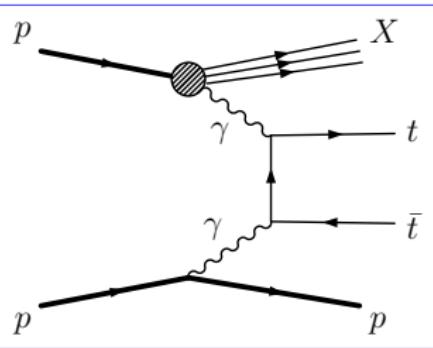
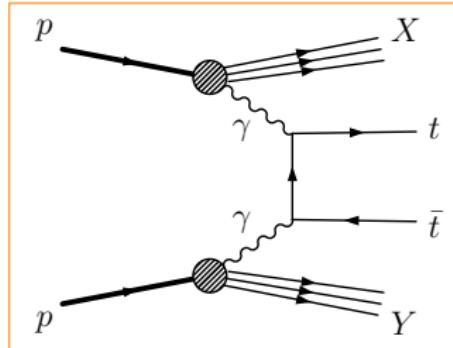
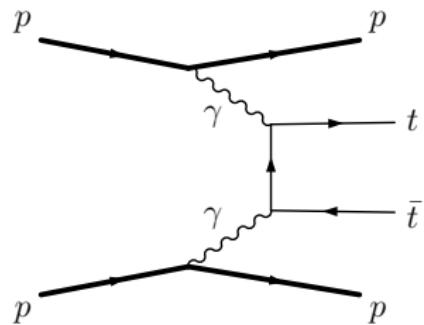
# Double dissociation



we predict a strong dependence on  $\eta_{\text{cut}}$

- it would be valuable to perform experimental measurements with different  $\eta_{\text{cut}}$

# Production of $t\bar{t}$ pairs



# Production of $t\bar{t}$ pairs

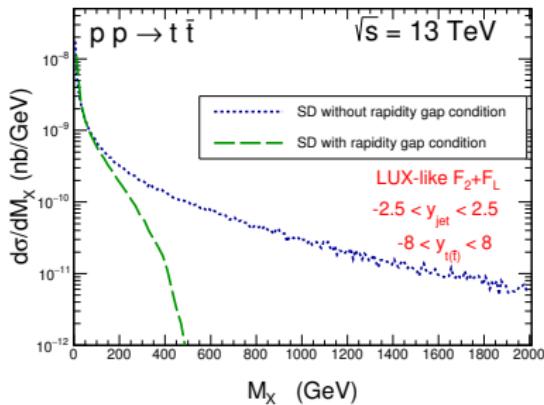
Contribution	No cuts	$y_{jet}$ cut
elastic-elastic	0.292	0.292
elastic-inelastic	0.544	0.439
inelastic-elastic		
inelastic-inelastic	0.983	0.622
all contributions	2.36	1.79

Table: Cross section in fb at  $\sqrt{s} = 13$  TeV for different components (left column) and the same when the extra condition on the outgoing jet  $|y_{jet}| > 2.5$  is imposed.

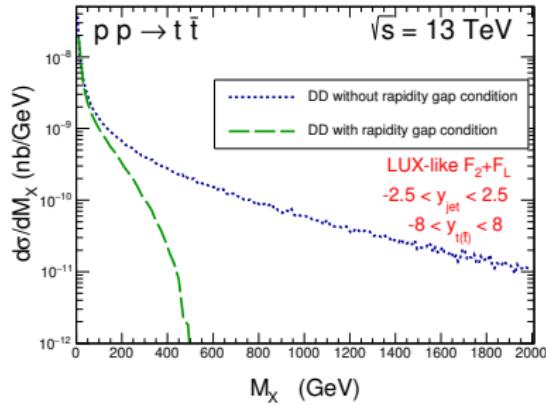
**right panel** → results when a rapidity gap (that means no additional particle production except the  $t$  or  $\bar{t}$ ) in the central region, for  $-2.5 < y < 2.5$  is required in addition

# Production of $t\bar{t}$ pairs

SD (left)

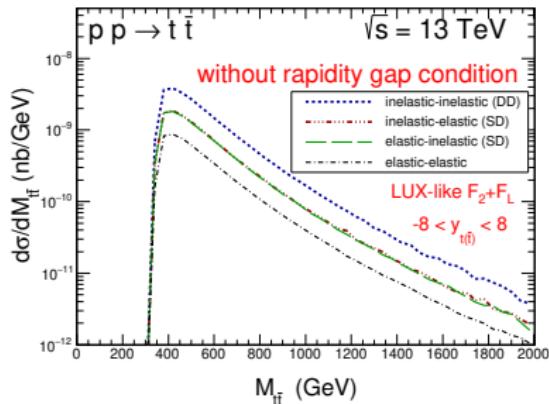


DD (right)

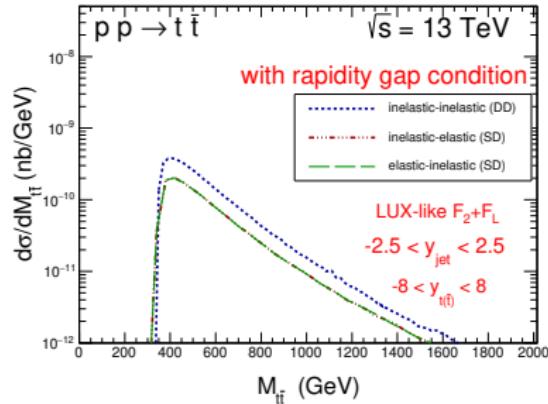


# Production of $t\bar{t}$ pairs

without rapidity gap condition



with rapidity gap condition



# Central dilepton production with rapidity gap and with forward protons

The ATLAS collaboration analysis impose the consistency requirements:

$$\xi_1 = \xi_{\parallel}^{+}, \quad \xi_2 = \xi_{\parallel}^{-}$$

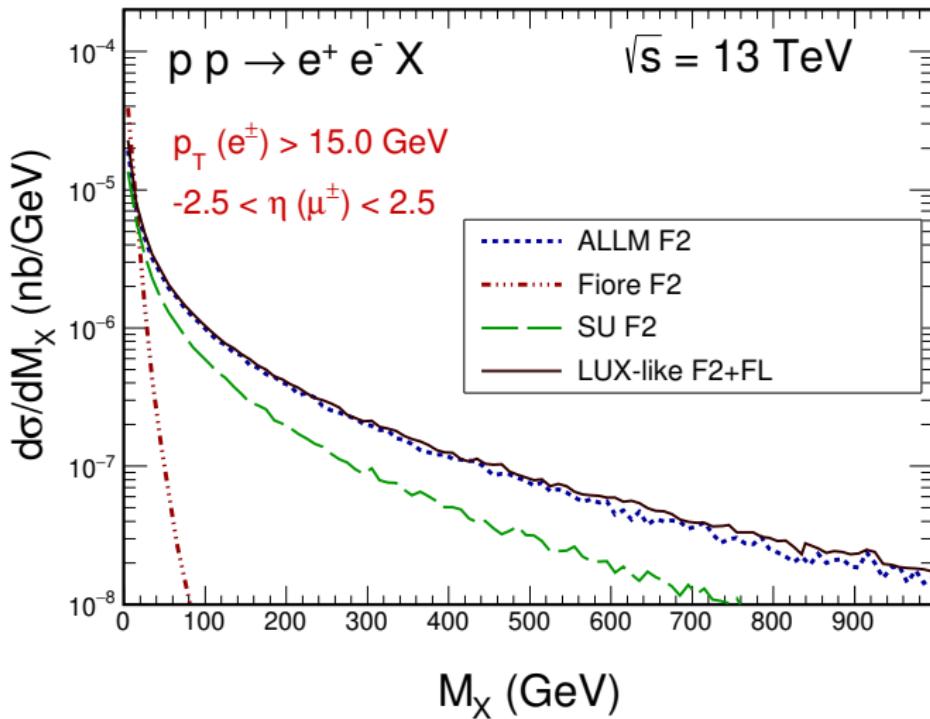
- The longitudinal momentum fractions of the photons were recalculated in the ATLAS analysis as:

$$\begin{aligned}\xi_{\parallel}^{+} &= \left( M_{\parallel} / \sqrt{s} \right) \exp(+Y_{\parallel}), \\ \xi_{\parallel}^{-} &= \left( M_{\parallel} / \sqrt{s} \right) \exp(-Y_{\parallel}).\end{aligned}$$

Only lepton variables enter the formula

- We use the same formula in our analysis

# Single-dissociative contribution



# Results: $\xi_{\parallel}^+$ or $\xi_{\parallel}^-$ cuts

contribution	c.s. in fb without $\xi$ -cuts	c.s. in fb with $\xi$ -cuts
elastic-elastic, cut on proton 1	358.68	5.4591
elastic-elastic, cut on proton 2	.....	5.4592
elastic-inelastic, cut on proton 1, SU, 0-100 GeV	427.8949	10.0190 (3.3492)
inelastic-elastic, cut on proton 2 SU, 0-100 GeV	427.0130	10.0186 (3.3491)
elastic-inelastic, VDM (no $\Omega$ ), 0-100 GeV	98.0215 (2UN)	
inelastic-elastic, VDM (no $\Omega$ ), 0-100 GeV	98.0297 (2UN)	
elastic-inelastic SU partonic	449.1076 (2UN)	
inelastic-elastic SU partonic	449.0985 (2UN)	
elastic-inelastic, cut on proton 1, ALLM	468.6102 (2UN)	11.8292
inelastic-elastic, cut on proton 2, ALLM	468.6102 (2UN)	11.8294
elastic-inelastic, new Szczurek	461.5330 (2UN)	12.6046 [14.1823] (5.9311)
inelastic-elastic, new Szczurek	461.5750 (2UN)	12.6032 [14.1806] (5.9309)
elastic-inelastic, ALLM	571.871 (GEN)	9.711
inelastic-elastic, ALLM	571.562 (GEN)	9.621
elastic-inelastic, LUX-like, $F_2 + F_L$	635.215 (GEN)	19.894
inelastic-elastic, LUX-like, $F_2 + F_L$	635.102 (GEN)	19.831
elastic-inelastic, LUX-like, $F_2$ only	..... (GEN)	.....
inelastic-elastic, LUX-like, $F_2$ only	656.702 (GEN)	.....
elastic-inelastic, cut on proton 1, resonances	38.6709 (2UN)	0.57872
inelastic-elastic, cut on proton 2 resonances	38.6639 (2UN)	0.57872
elastic-inelastic, cut on proton 1, $\Delta^+$	28.5844 (2UN)	0.42755
inelastic-elastic, cut on proton 2 $\Delta^+$	28.5814 (2UN)	0.42763

**Tablica:** Integrated cross section for  $\mu^+ \mu^-$  with one p in 0.035  $< \xi_{\parallel}^{\pm} < 0.08$ . Here  $p_{1t}, p_{2t} > 15$  GeV and  $-2.5 < y_1, y_2 < 2.5$ . In the parenthesis result with  $p_{t,sum} < 5$  GeV. 2UN – doubly unintegrated photon distribution and GEN – generator version.

# SUPERCHIC analysis: $\xi_{||}^+$ or $\xi_{||}^-$ cuts

reaction	no soft $S_G$	with soft $S_G$	$< S_G >$
$-2.5 < Y_{  } < 2.5$			
elastic-elastic	0.54438	0.50402	0.926
inelastic-elastic	0.89595	0.64283	0.717
elastic-inelastic	0.89587	0.64254	0.717
inelastic-inelastic	1.62859	0.24172	0.15
$-2.5 < y_1, y_2 < 2.5$ in addition			
elastic-elastic	0.42268	0.39355	0.931
inelastic-elastic	0.69241	0.51092	0.738
elastic-inelastic	0.69246	0.51087	0.738
$\xi$ cut in addition			
elastic-elastic, cut on $\xi_1$	0.00762	0.00675	0.886
elastic-elastic, cut on $\xi_2$	0.00762	0.00675	0.886
inelastic-elastic, cut on $\xi_2$	0.02718	0.01416	0.521
elastic-inelastic, cut on $\xi_1$	0.02717	0.01416	0.521
$p_{t,pair} < 5$ GeV in addition			
elastic-elastic	.....	.....	....
inelastic-elastic, cut on $\xi_2$	0.008035 (2000)	0.00435	0.541
elastic-inelastic, cut on $\xi_1$	0.008056 (2000)	0.00436	0.541

**Tablica:** Integrated cross section for  $\mu^+ \mu^-$  production in pb for  $\sqrt{s} = 13$  TeV using SUPERCHIC program.  $0.035 < \xi_{||}^\pm < 0.08$ . To calculate absorption effects we used model no 4 as implemented in the SUPERCHIC generator.

# Conclusions

- We use a recent formalism developed for the inclusive case which includes **transverse momenta of incoming photons**.
- We have found that the hadronisation only mildly modifies **the gap survival factor calculated on the parton level**. This may justify approximate treatment of hadronisation of remnants.
- We have also made calculations with the popular **SUPERCHIC generator** and compared corresponding results to the results of our code(s). In general, the results are almost identical.
- We have calculated also **soft rapidity gap survival factor**(probability of no hadron emission in the range of the main (ATLAS, CMS) detector) as a function of  $M_{\parallel}$ , transverse momentum of the dilepton pair, mass of the proton remnant and  $Y_{\parallel}$ .
- The soft gap survival factor for single dissociative contribution **strongly depends on whether proton is measured or not**. It is significantly smaller when proton is measured.
- We have also calculated gap survival factor due to mini(jet) emission by checking whether the minijet enters or not the main detector.