



axion like particles at colliders and beyond

Yotam Soreq

PBC meets theory: informal discussion about PBC selected topics
11 June, 2020



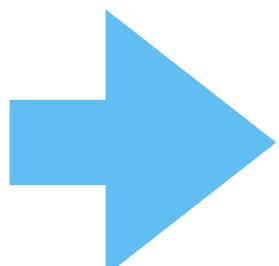


axion like particles

- * originally - the Axion propose as a solution to the strong CP problem
- * appear in many BSM scenarios
- * portal to dark matter and/or dark sector
- * if very light, it is a dark matter candidate
- * predicted by string theory

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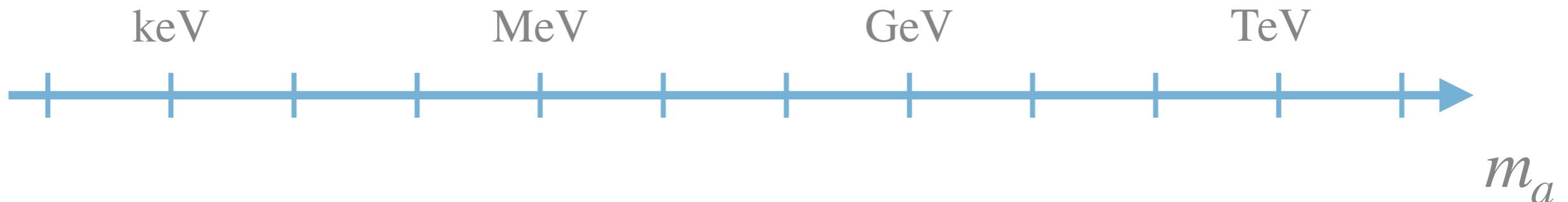
well motivated BSM scenario

axion like particles

pseudo-scalar and pNGB

$$\mathcal{L}_{\text{eff}} = - \frac{4\pi\alpha_s c_g}{\Lambda} a G^{\mu\nu} \tilde{G}_{\mu\nu} + \frac{c_\gamma}{4\Lambda} a F^{\mu\nu} \tilde{F}_{\mu\nu}$$

$\Lambda \gg m_a$

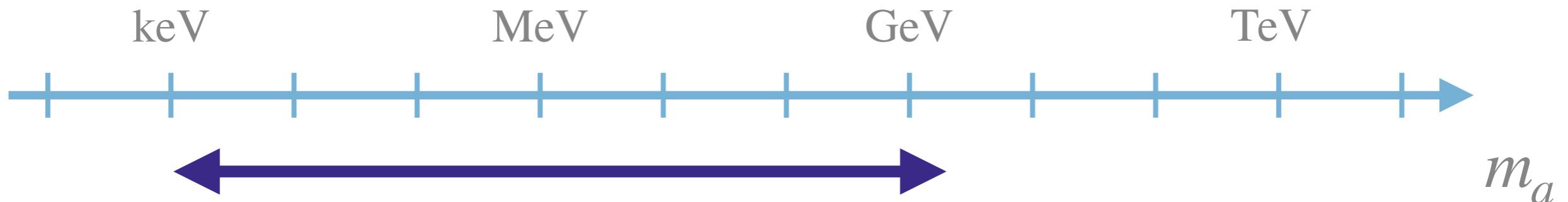


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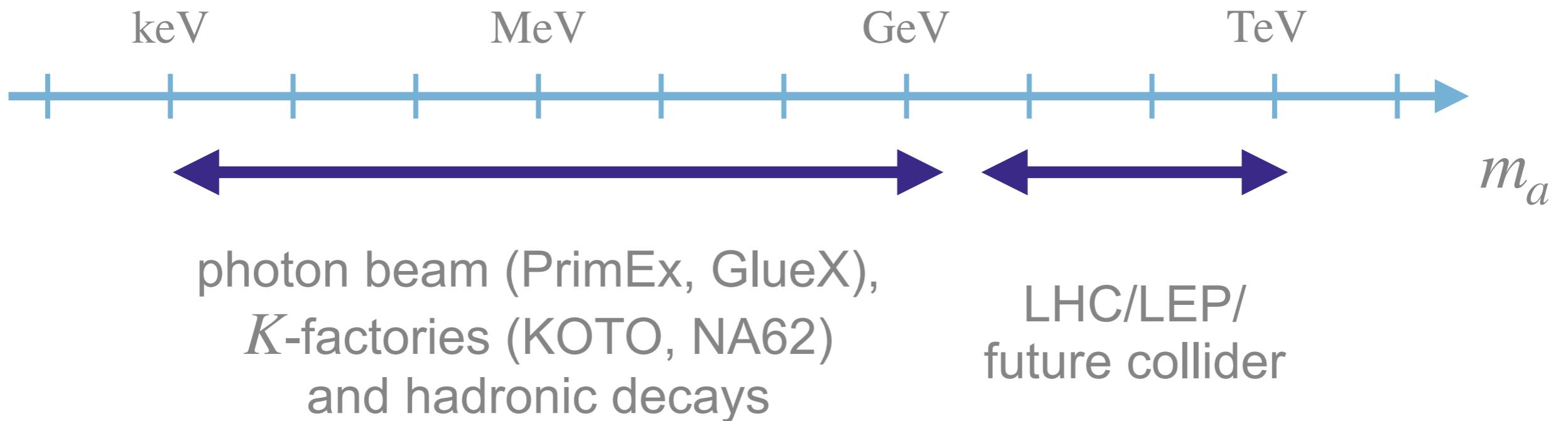
photon beam (PrimEx, GlueX),
 K -factories (KOTO, NA62)
and hadronic decays

axion like particles

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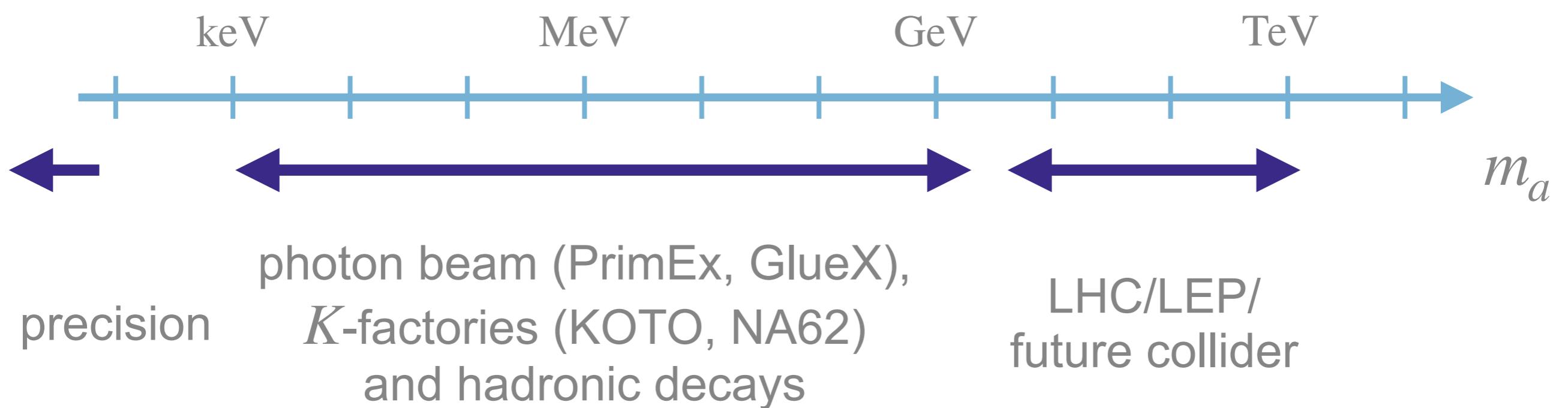


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ALPs at the MeV to the GeV scale

Aloni, YS, Williams - 1811.03474
Aloni, Fanelli,YS, Williams - 1903.03586

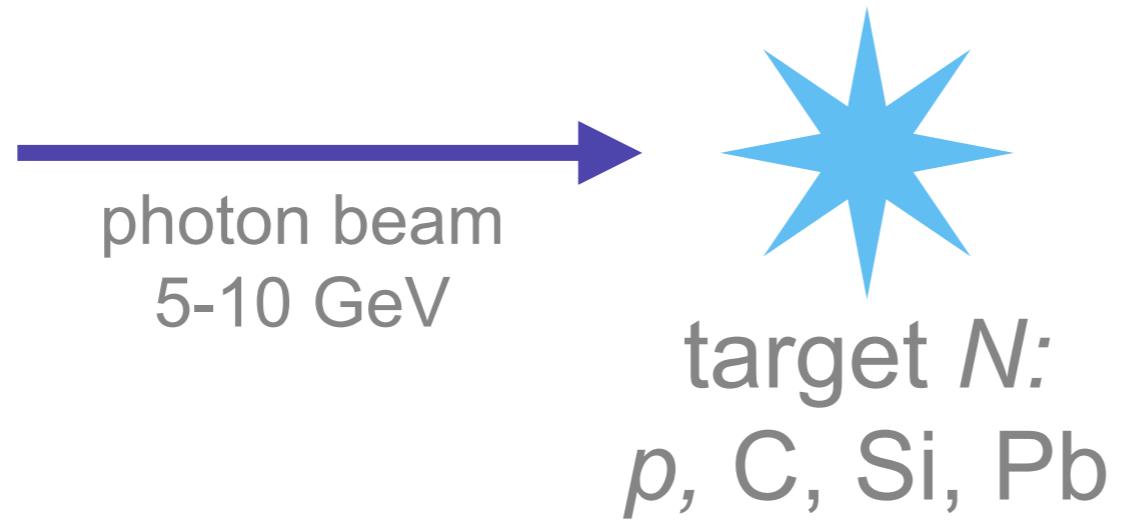
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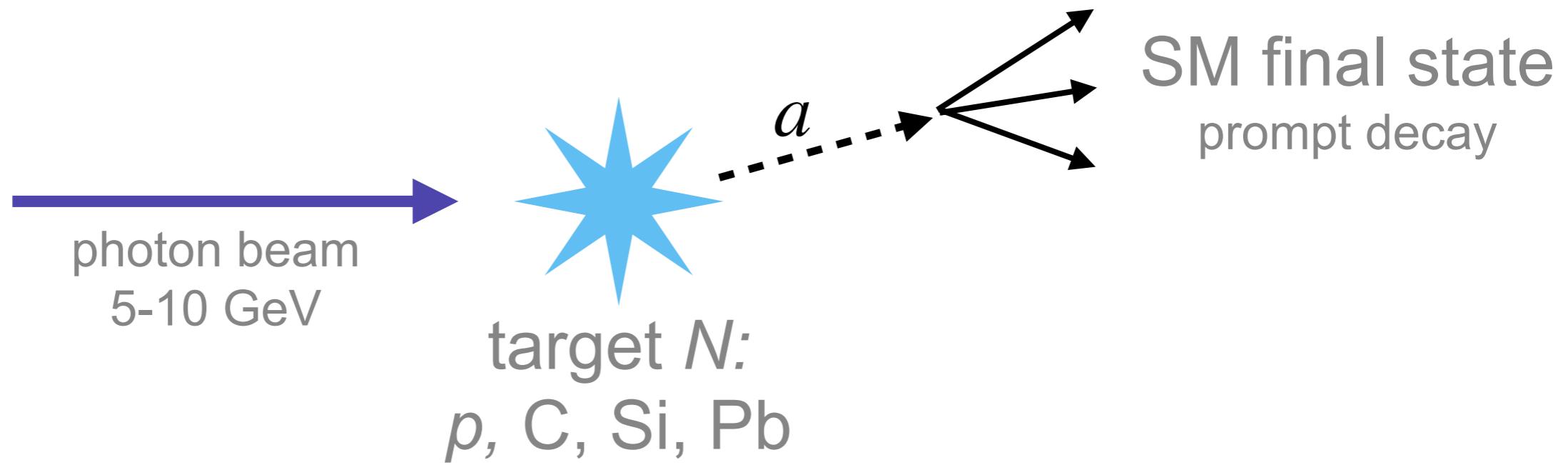
$$c_g \neq 0 \text{ or } c_\gamma \neq 0$$

- * probing at photon beam (Primakoff like) experiments
- * estimate of hadronic decay rates

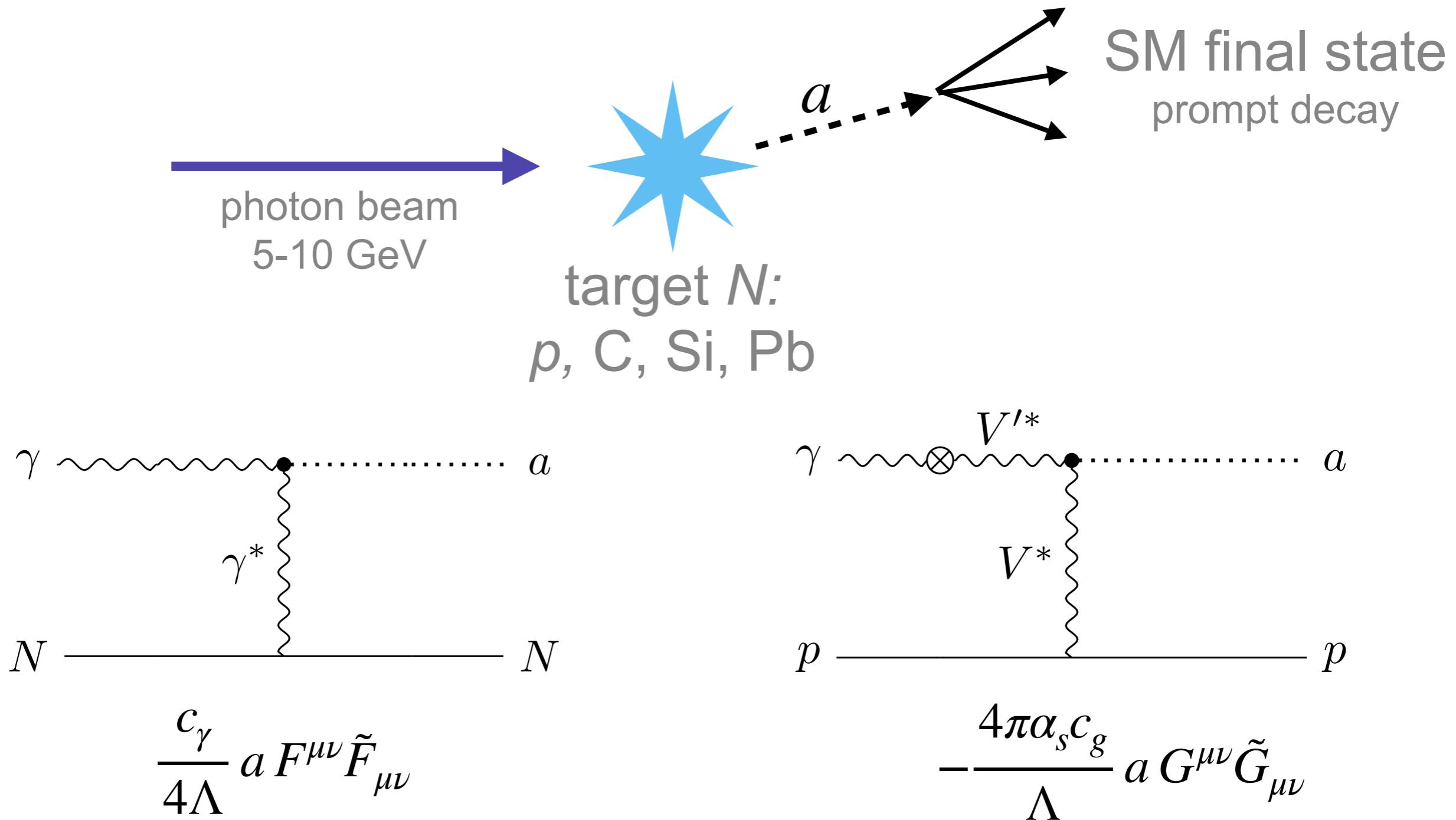
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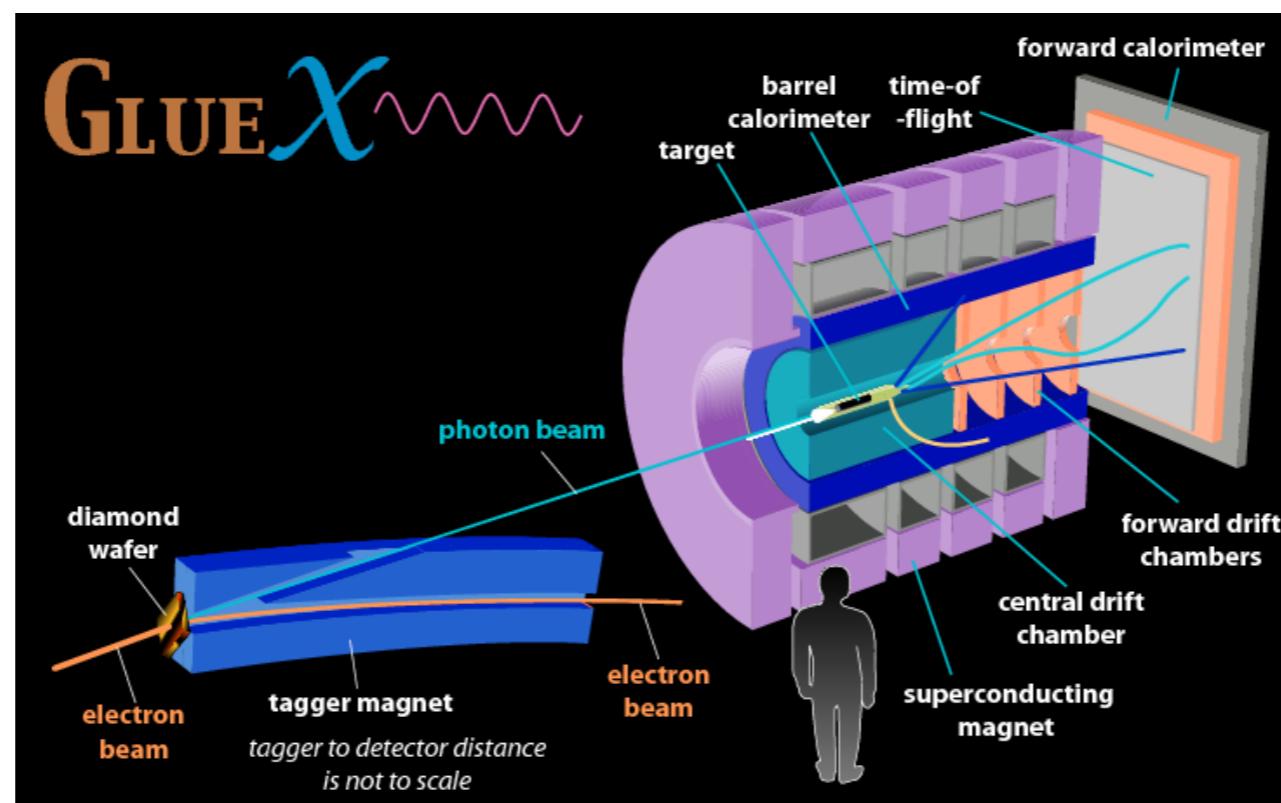
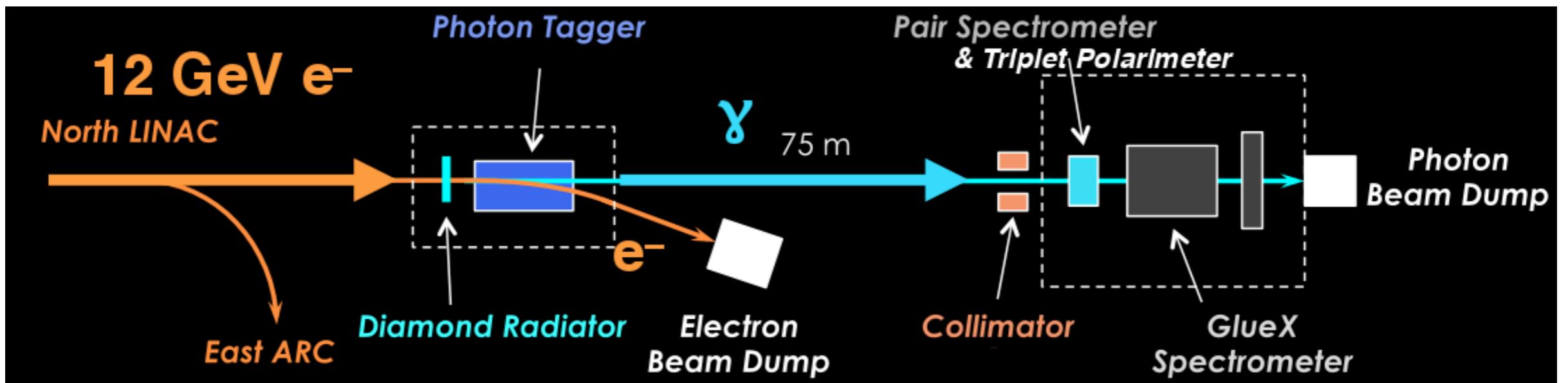


ALPs at Primakoff like experiments

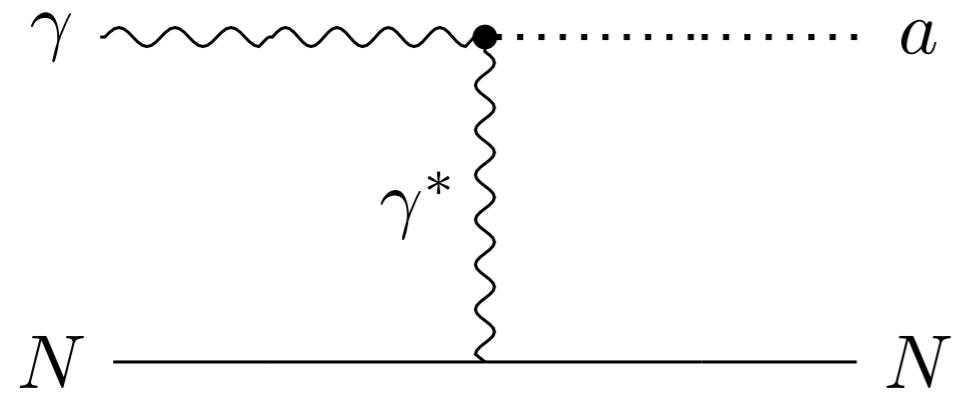


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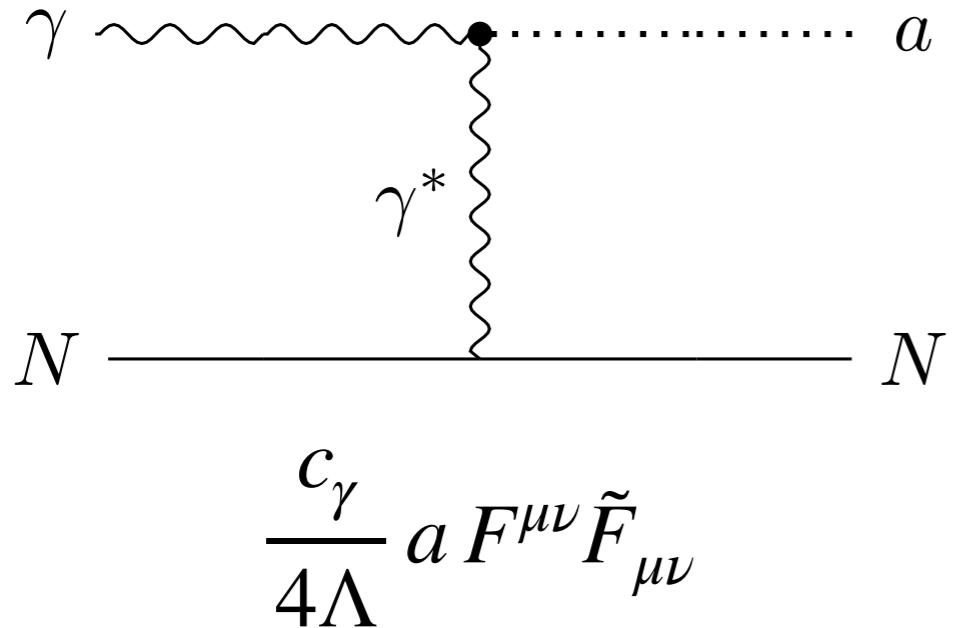


ALP photons coupling



$$\frac{c_\gamma}{4\Lambda} a F^{\mu\nu} \tilde{F}_{\mu\nu}$$

ALP photons coupling



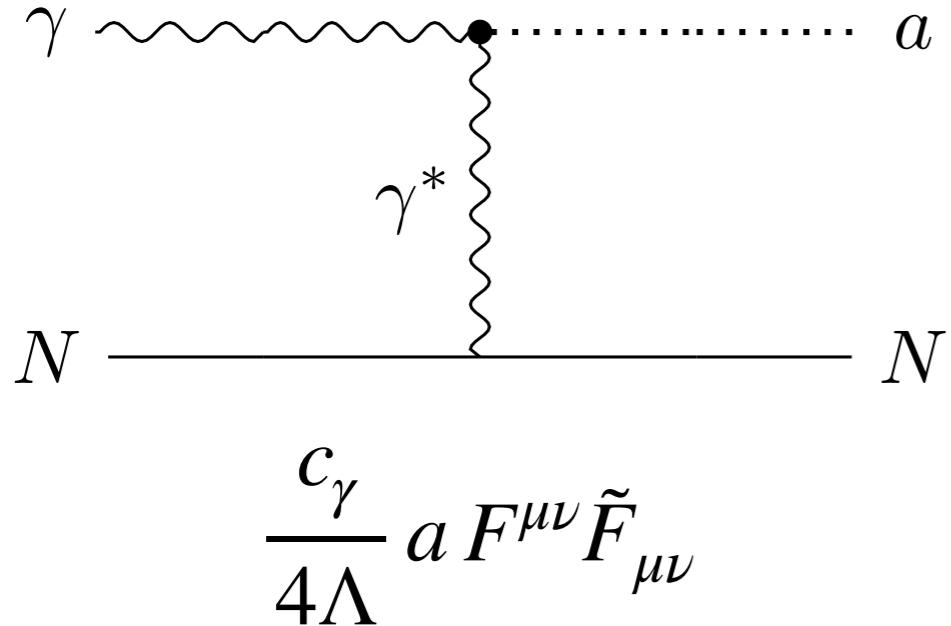
$$\frac{d\sigma_{\gamma N \rightarrow aN}^{\text{elastic}}}{dt} = \alpha Z_N^2 F_N^2(t) \Gamma_{a \rightarrow \gamma\gamma} \mathcal{H}(m_N, m_a, s, t)$$

target
charge

form
factor

kinematical
function

ALP photons coupling



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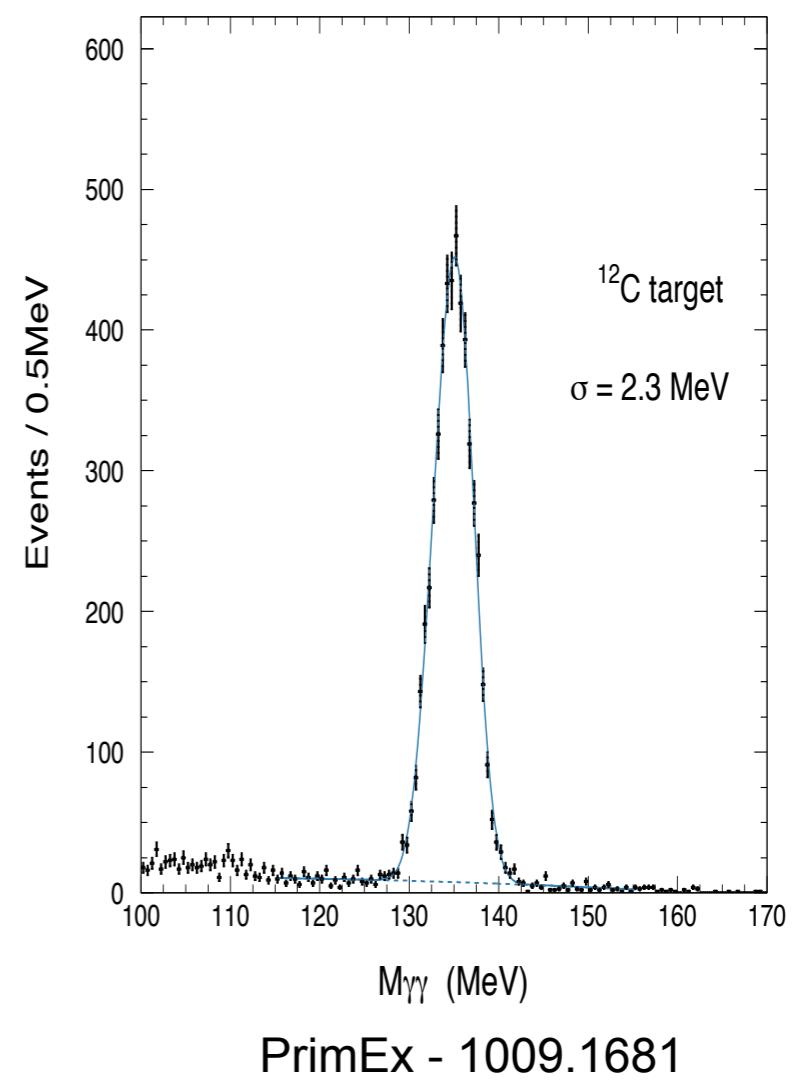
Primakoff production of ALPs and $P = \pi^0, \eta$ are similar

$$\frac{d\sigma_{\gamma N \rightarrow aN}^{\text{elastic}}}{dt} = \frac{\Gamma_{a \rightarrow \gamma\gamma} \mathcal{H}(m_N, m_a, s, t)}{\Gamma_{P \rightarrow \gamma\gamma} \mathcal{H}(m_N, m_p, s, t)} \frac{d\sigma_{\gamma N \rightarrow PN}^{\text{elastic}}}{dt}$$

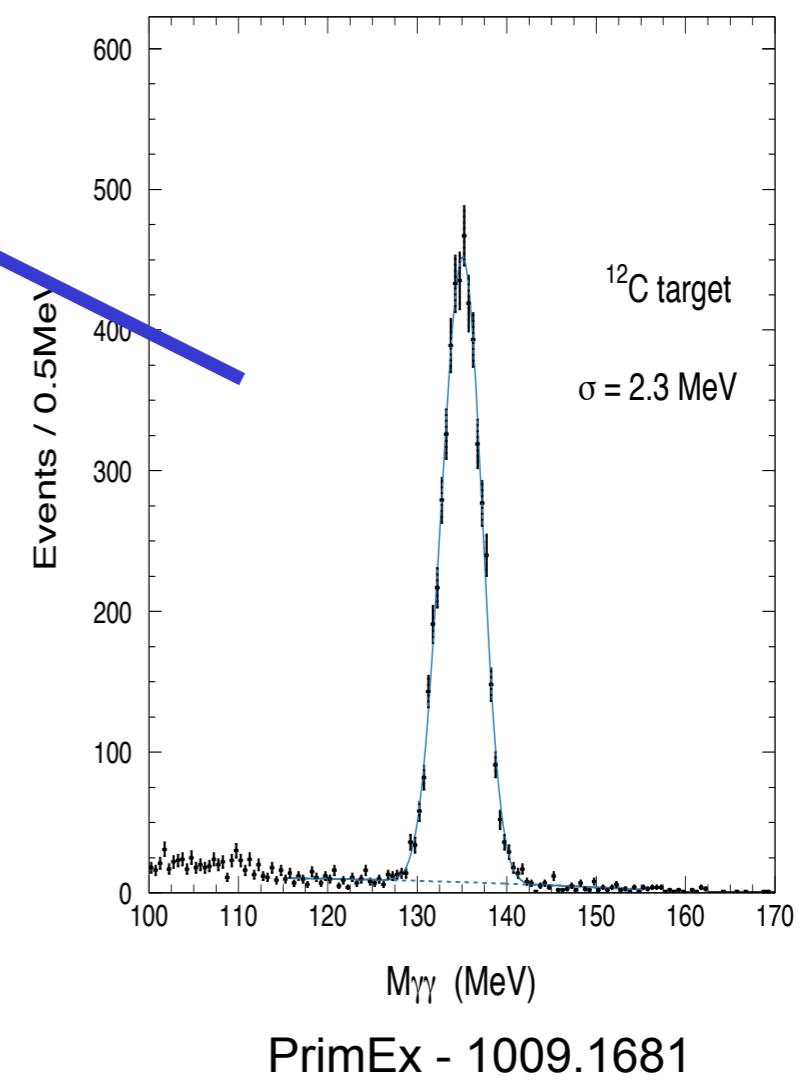
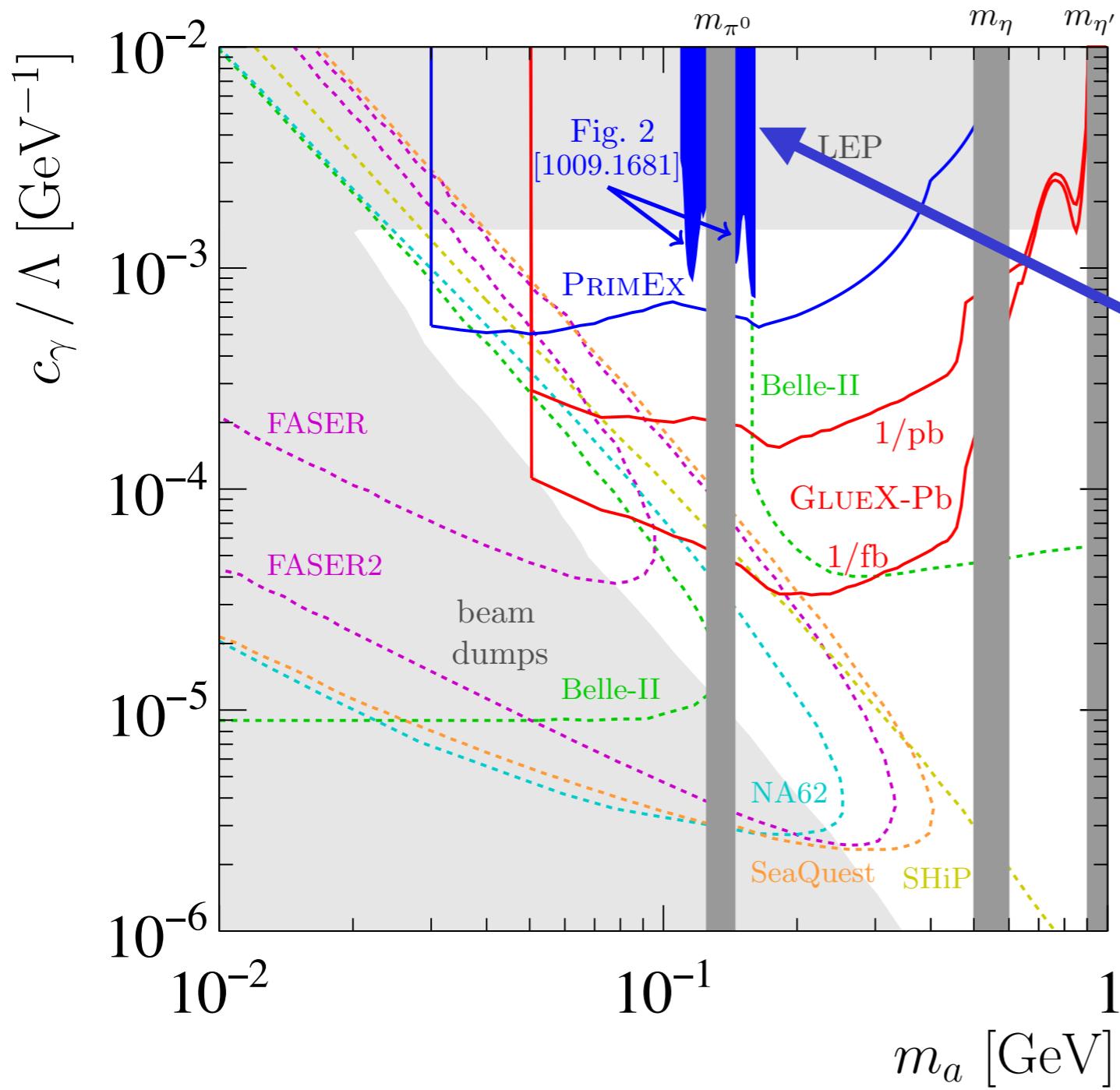
at the forward region

data-driven signal normalization
(cancel form-factor and flux dependence)

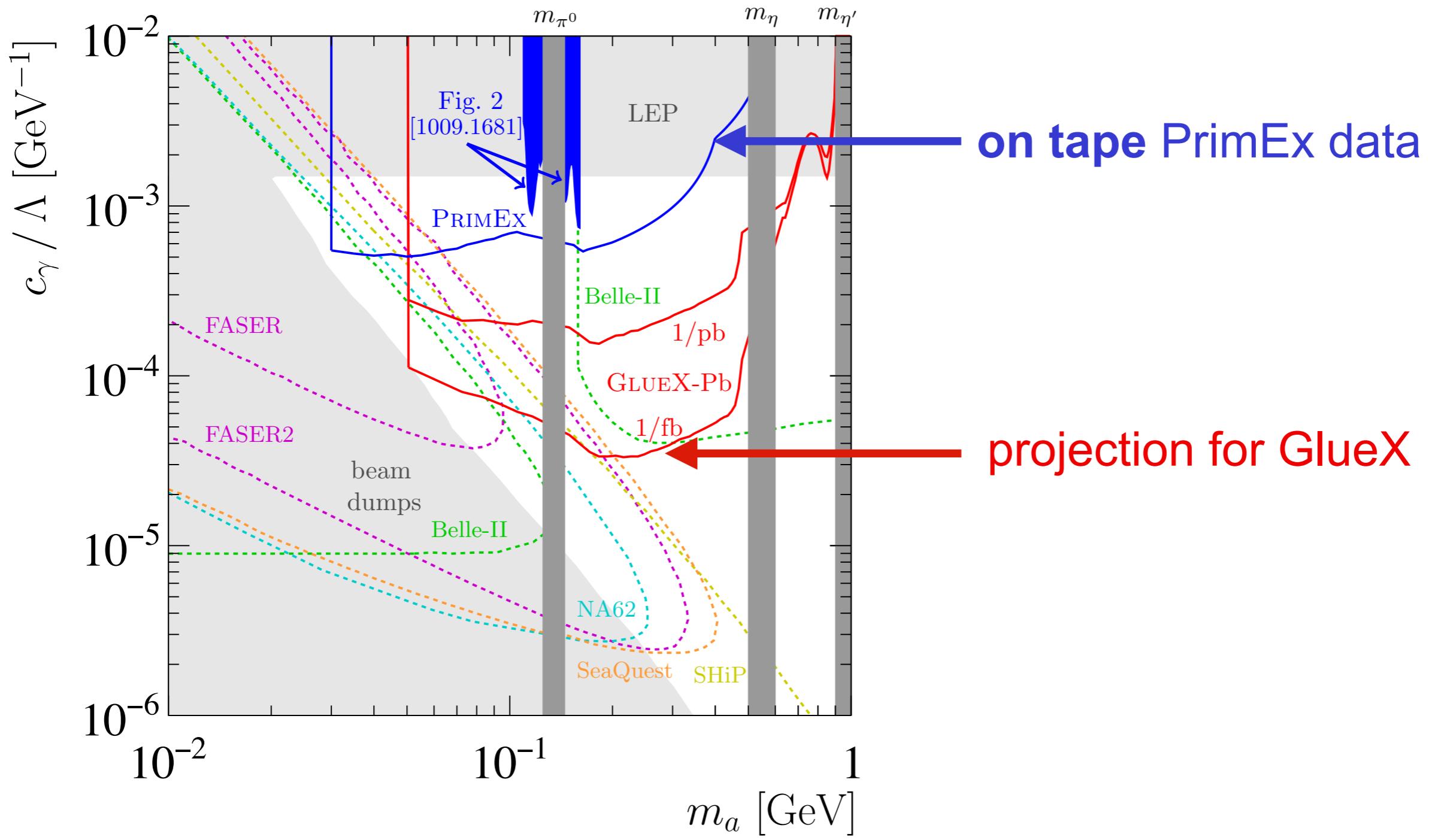
ALP photons coupling



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ALP gluons coupling

$$-\frac{4\pi\alpha_s c_g}{\Lambda} a G^{\mu\nu} \tilde{G}_{\mu\nu}$$

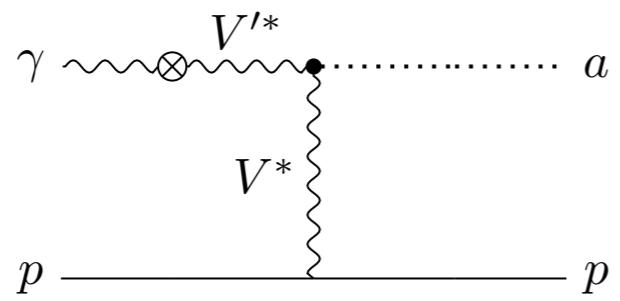
$$F_a = |\Lambda/(32\pi^2 c_g)|$$

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GlueX
p target

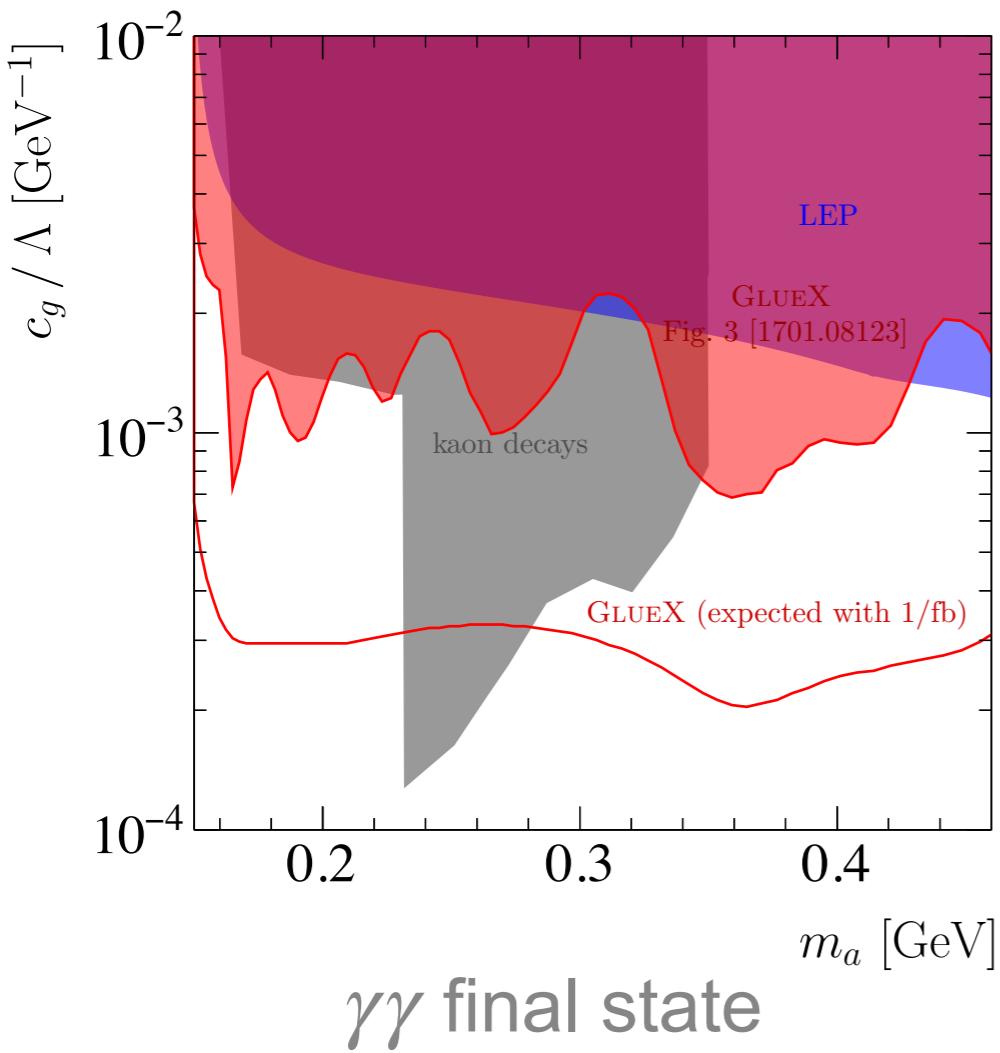
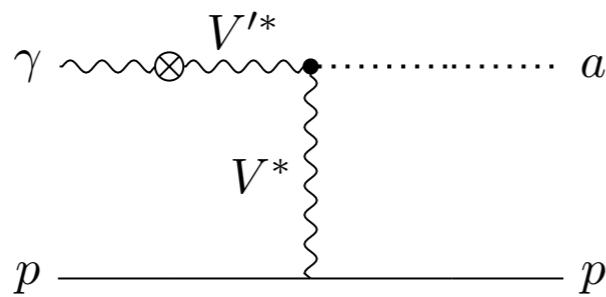


$$\frac{d\sigma_{\gamma p \rightarrow ap}}{dt} \approx \left(\frac{f_\pi}{F_a} \right)^2 \left[|\langle a\pi^0 \rangle|^2 \frac{d\sigma_{\gamma p \rightarrow \pi^0 p}}{dt} + |\langle a\eta \rangle|^2 \frac{d\sigma_{\gamma p \rightarrow \eta p}}{dt} \right]$$

\uparrow \uparrow
 $a - \pi^0, \eta$ mixing

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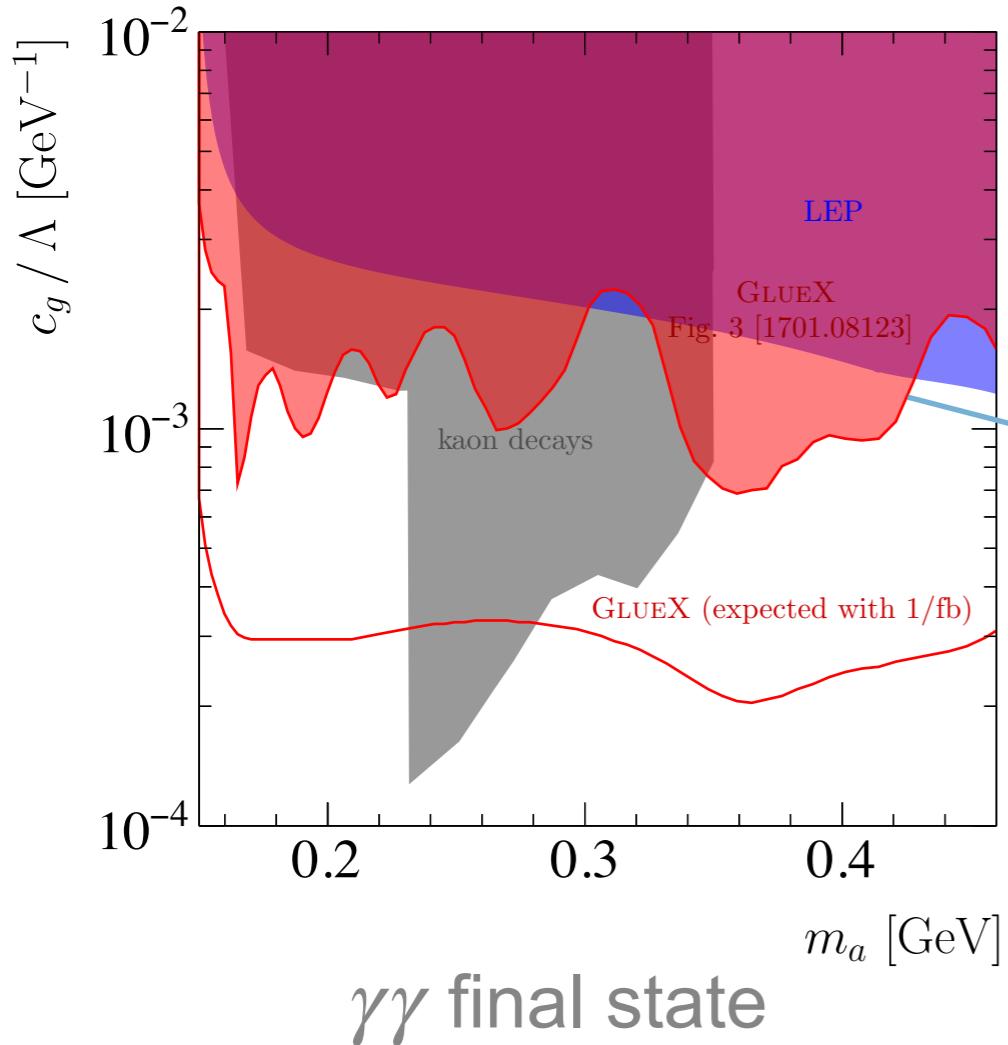
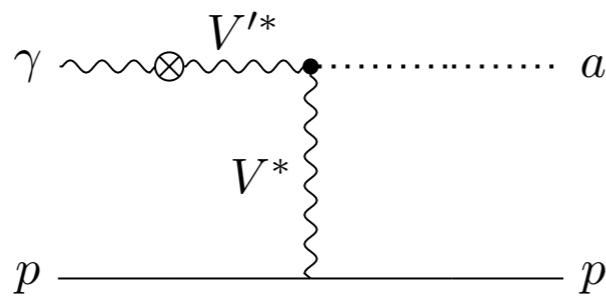
↑ *a - π^0, η mixing* ↑

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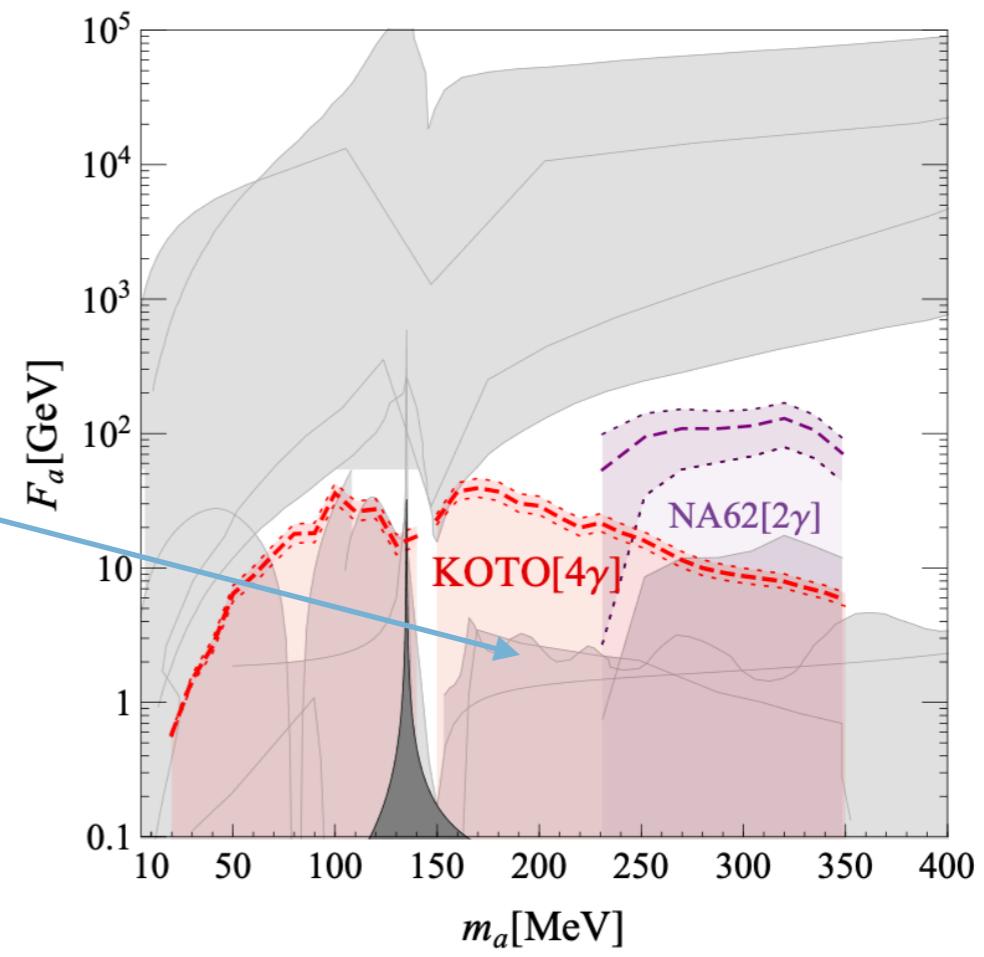
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KOTO
 $K_L \rightarrow \pi^0 a \rightarrow 4\gamma$



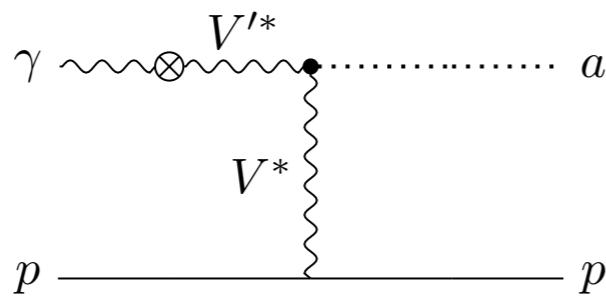
Gori, Perez, Tobioka - 2005.05170

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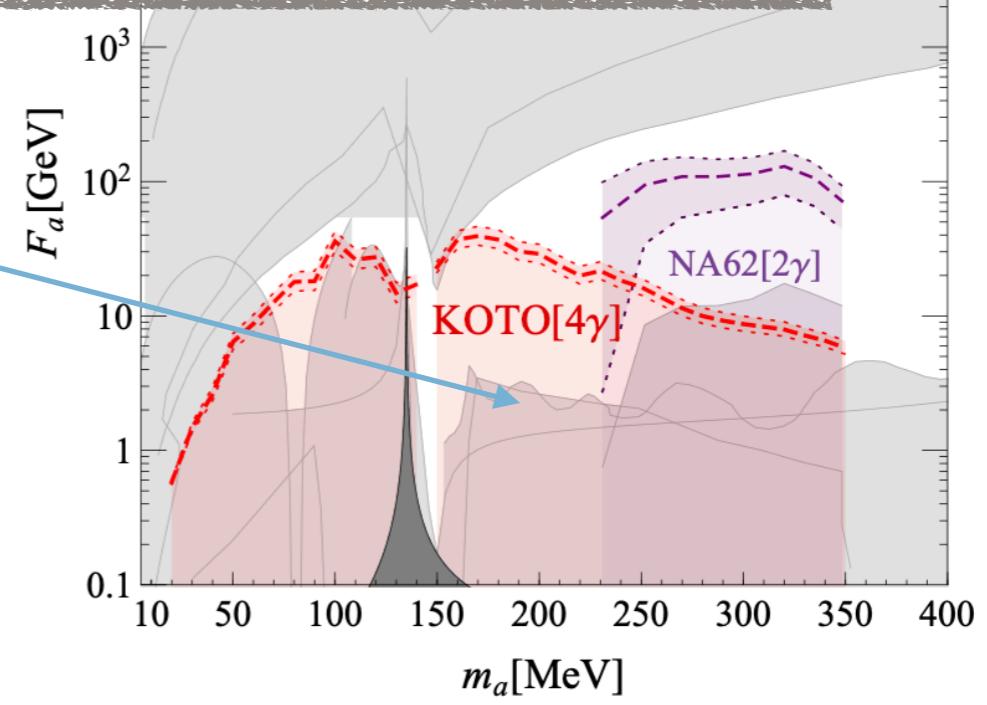
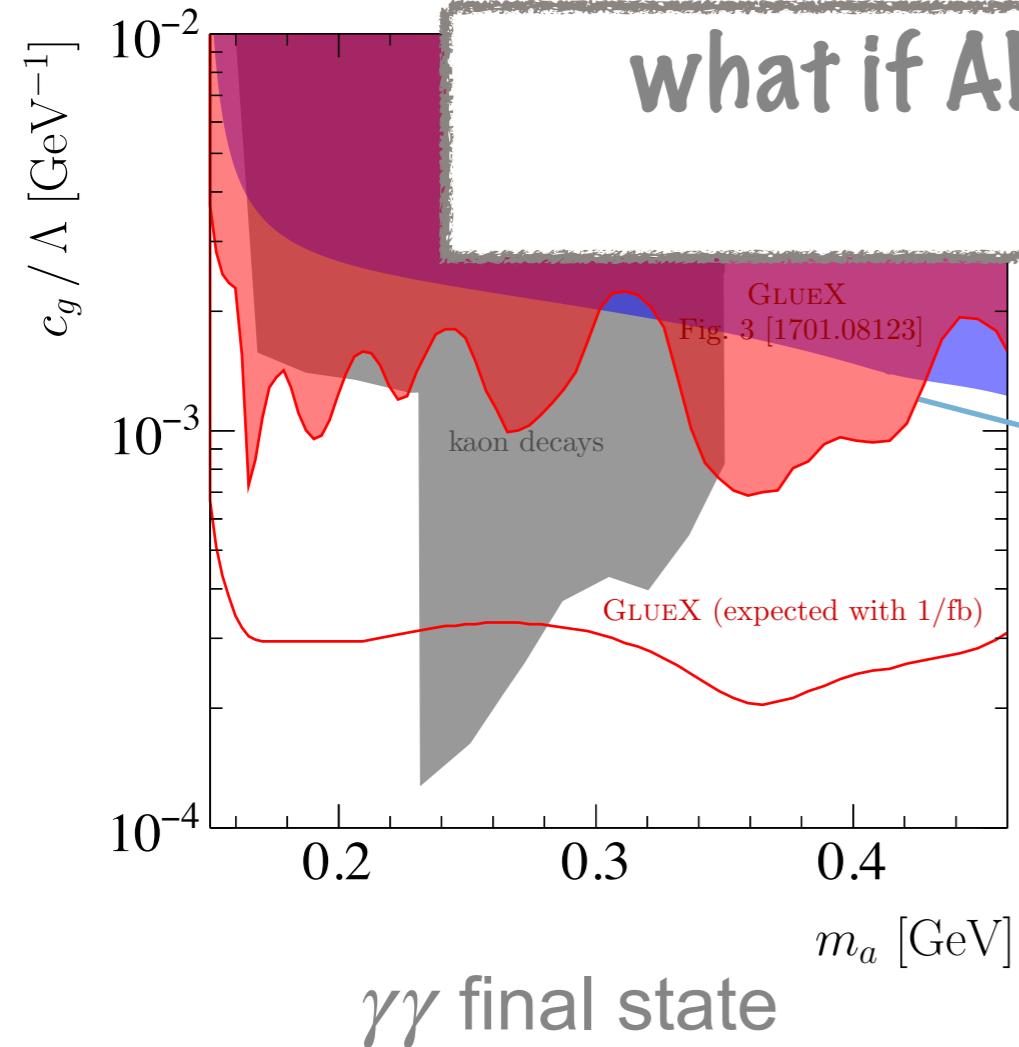
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How to estimate hadronic rates for ALPs with
QCD scale mass?

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$m_a \lesssim$ GeV

chiral PT

?????

$m_a \gtrsim 2$ GeV

pQCD

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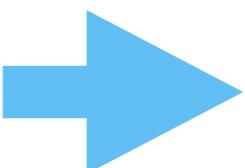
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$e^+e^- \rightarrow$ hadrons



information on specific
 $U(3)_{\text{flavor}}$ combinations

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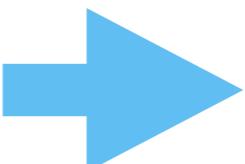
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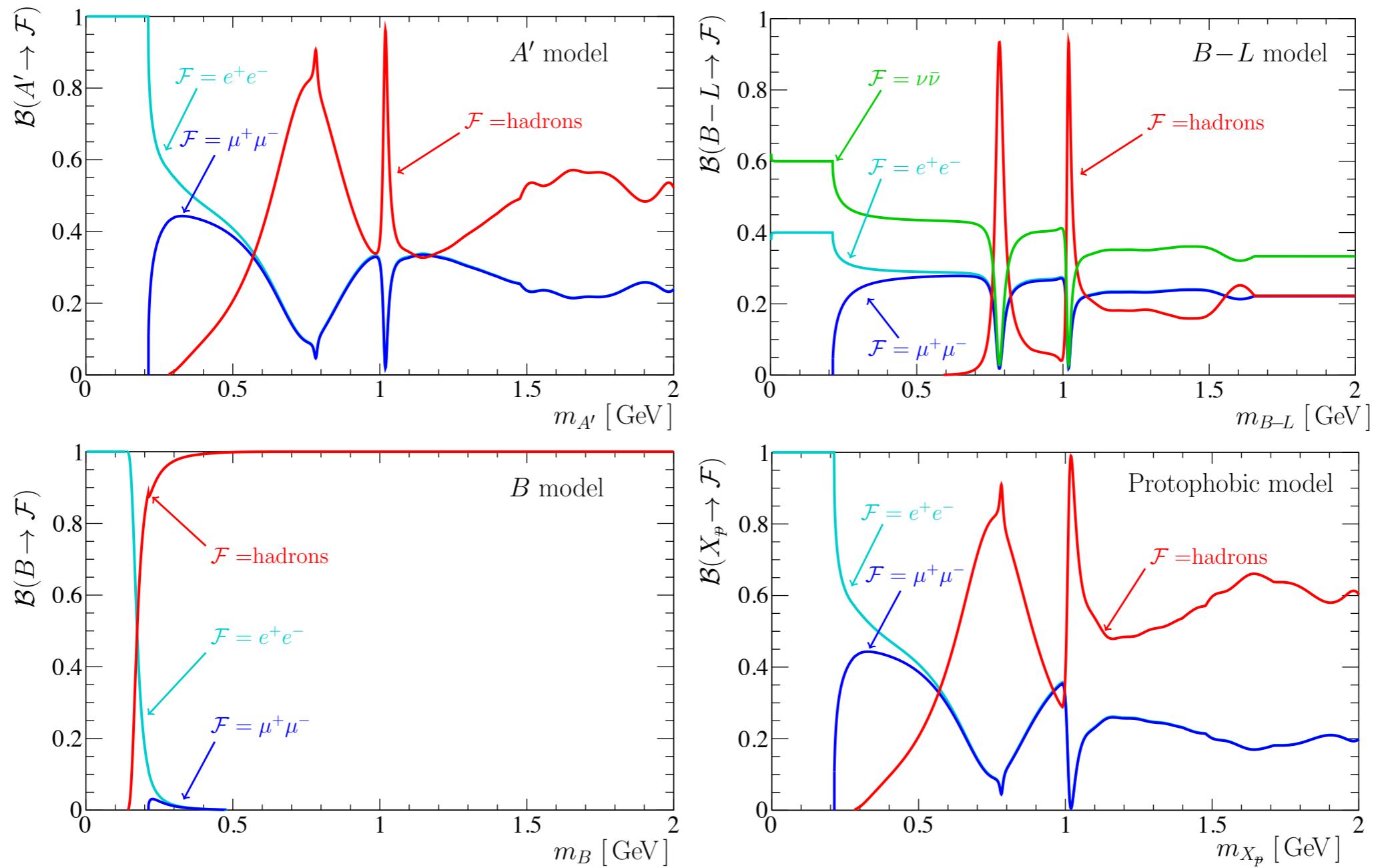
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directly deduce the hadronic rates of vectors

ALP gluons coupling

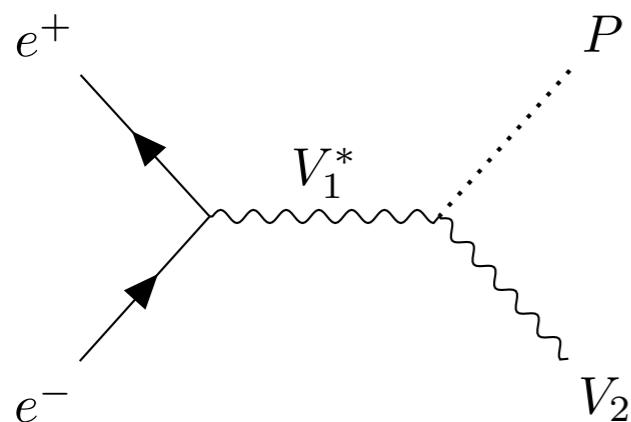


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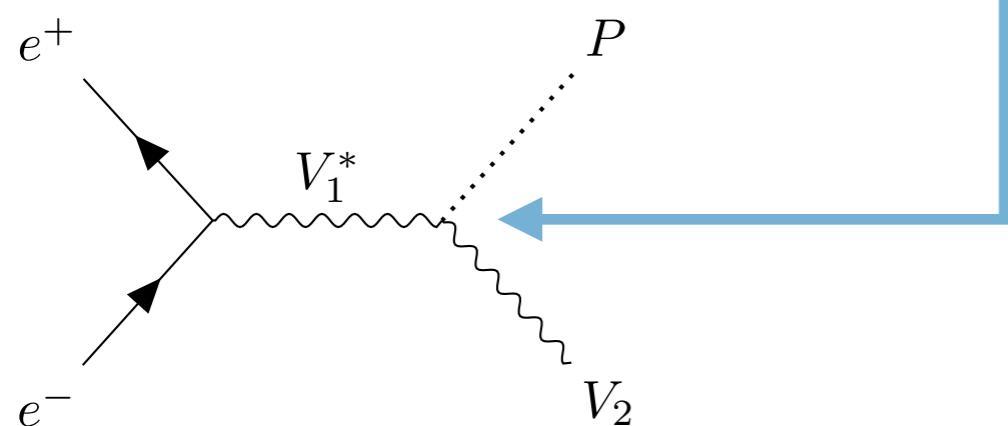


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$$\mathcal{A}(V_1 \rightarrow V_2 P) = \epsilon_{\mu\nu\alpha\beta} \epsilon_1^\mu \epsilon_2^{*\nu} p_1^\alpha p_2^\beta \mathcal{F}(p_1^2, p_2^2, q^2) \times \frac{3g^2}{4\pi^2 f_\pi} \langle V_1 V_2 P \rangle$$

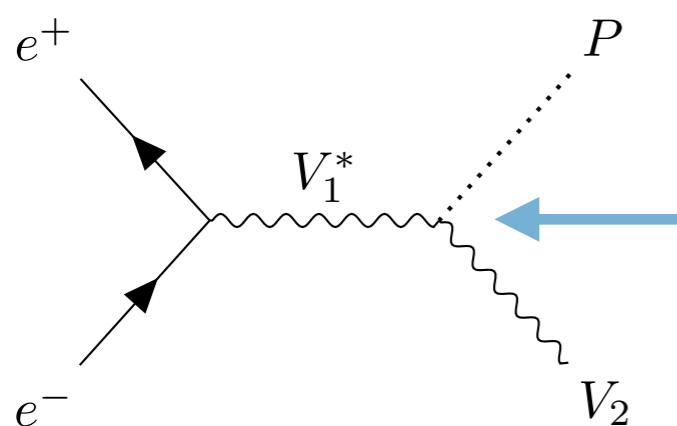
one Lorentz structure

modified VMD

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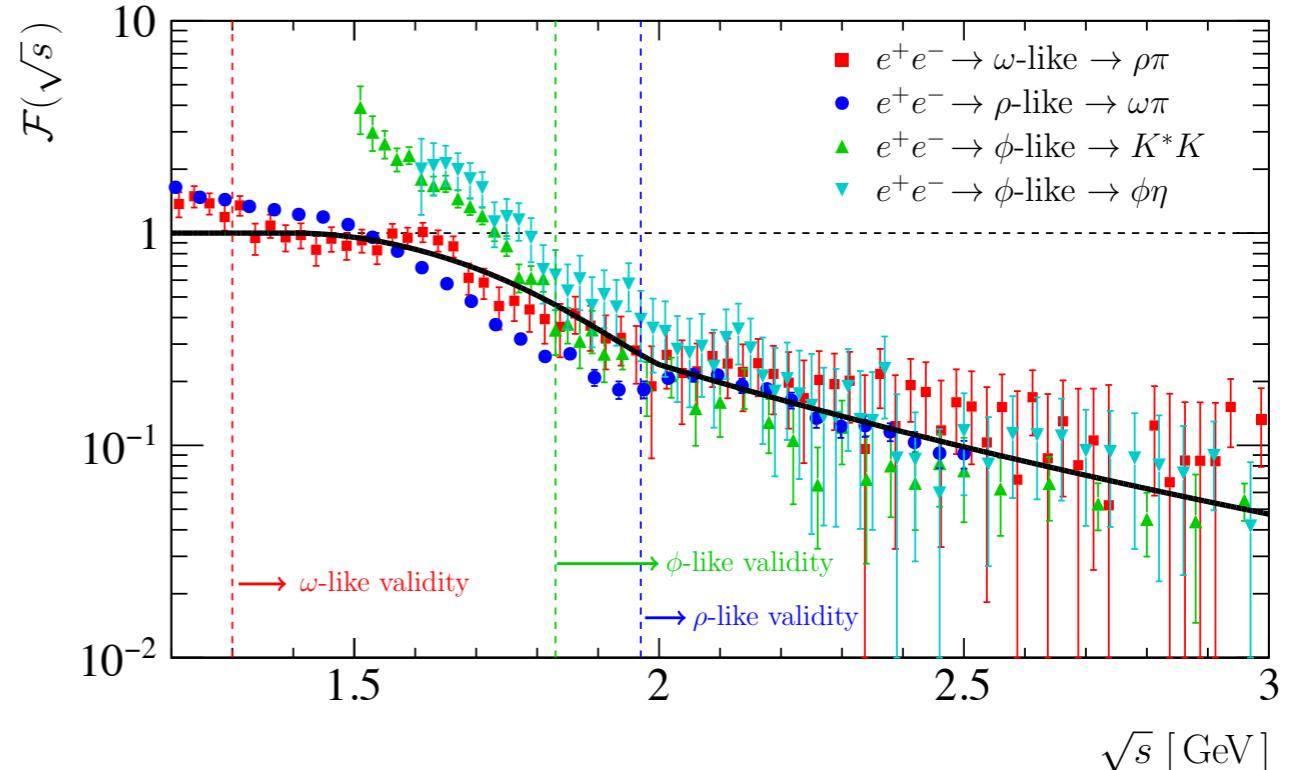


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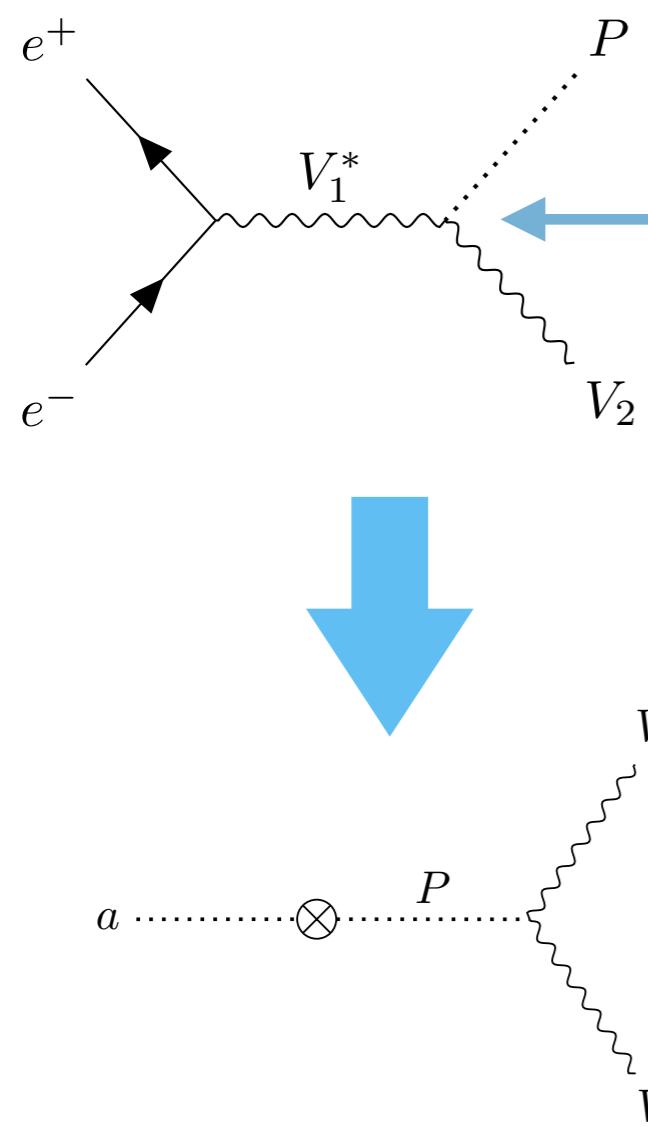
from data

$$\mathcal{F}(m) = \begin{cases} 1 & \text{for } m < 1.4 \text{ GeV} \\ \text{interpolation} & \text{for } 1.4 \leq m \leq 2 \text{ GeV} \\ \left[\frac{\beta_{\mathcal{F}}}{m} \right]^4 & \text{for } m > 2 \text{ GeV} \end{cases}$$

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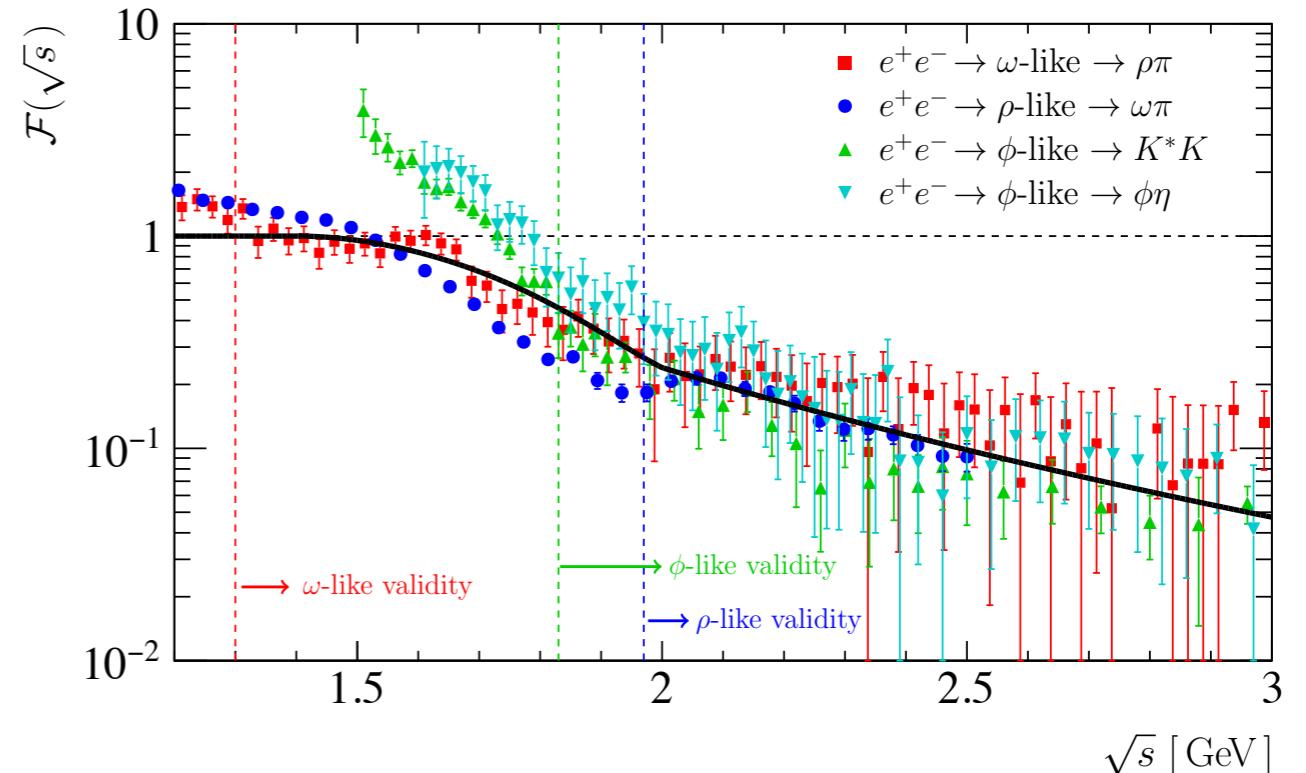


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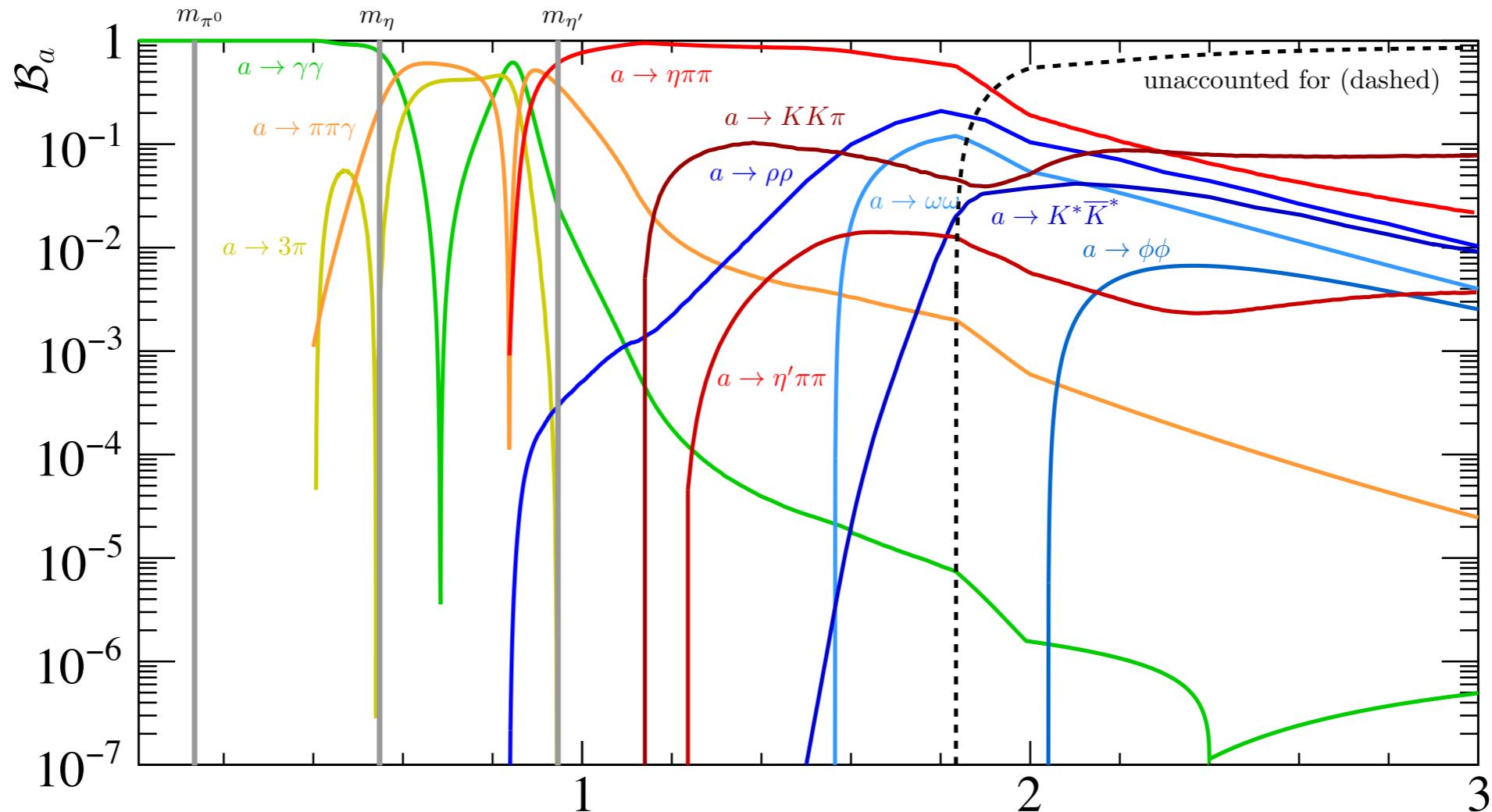
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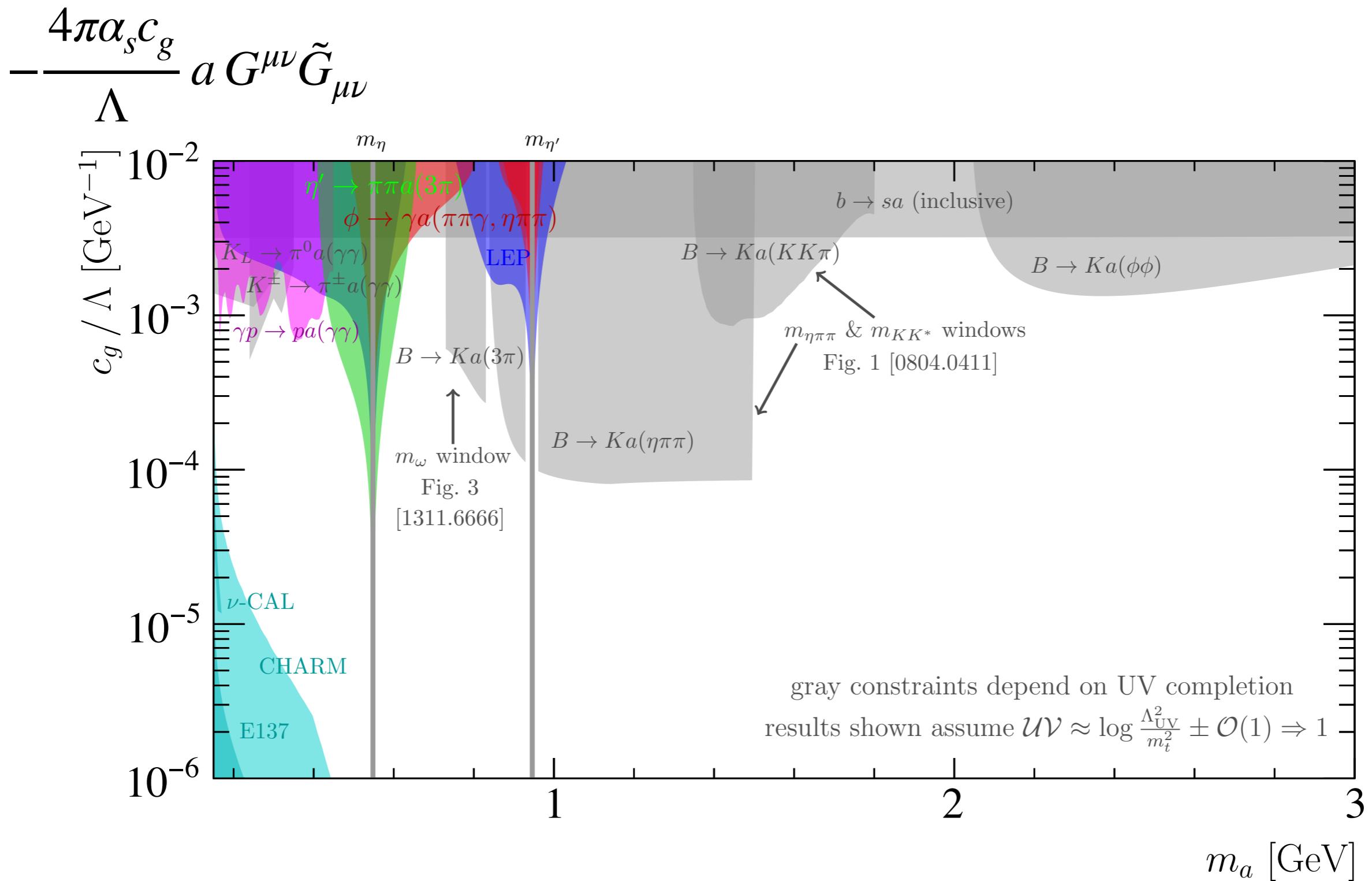
replace P by $P - a$ mixing



cross check: η_c

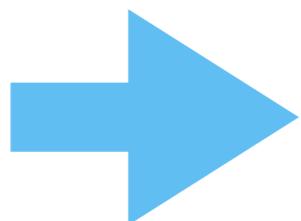
	This Work VMD $\times \mathcal{F}(m) ^2$	Experiment Average	Experiment $SU(3)$	m_a [GeV]
$\mathcal{B}(\eta_c \rightarrow \rho\rho)$	1.0%	$1.8 \pm 0.5\%$	$1.10 \pm 0.14\%$	
$\mathcal{B}(\eta_c \rightarrow \omega\omega)$	0.40%	$0.20 \pm 0.10\%$	$0.44 \pm 0.06\%$	
$\mathcal{B}(\eta_c \rightarrow \phi\phi)$	0.25%	$0.28 \pm 0.04\%$	$0.28 \pm 0.04\%$	
$\mathcal{B}(\eta_c \rightarrow K^*\bar{K}^*)$	0.91%	$0.91 \pm 0.26\%$	$1.00 \pm 0.13\%$	

ALP gluons coupling

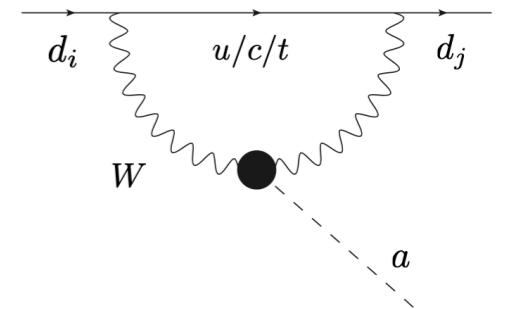


a_{WW} and rare Kaon decays

$$-\frac{g_{aW}}{4} a W_{\mu\nu} \tilde{W}^{\mu\nu}$$

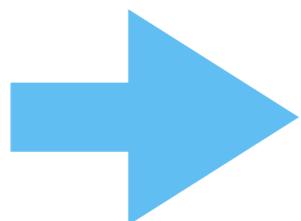


$K \rightarrow \pi a$ by the
SM FCNC loop

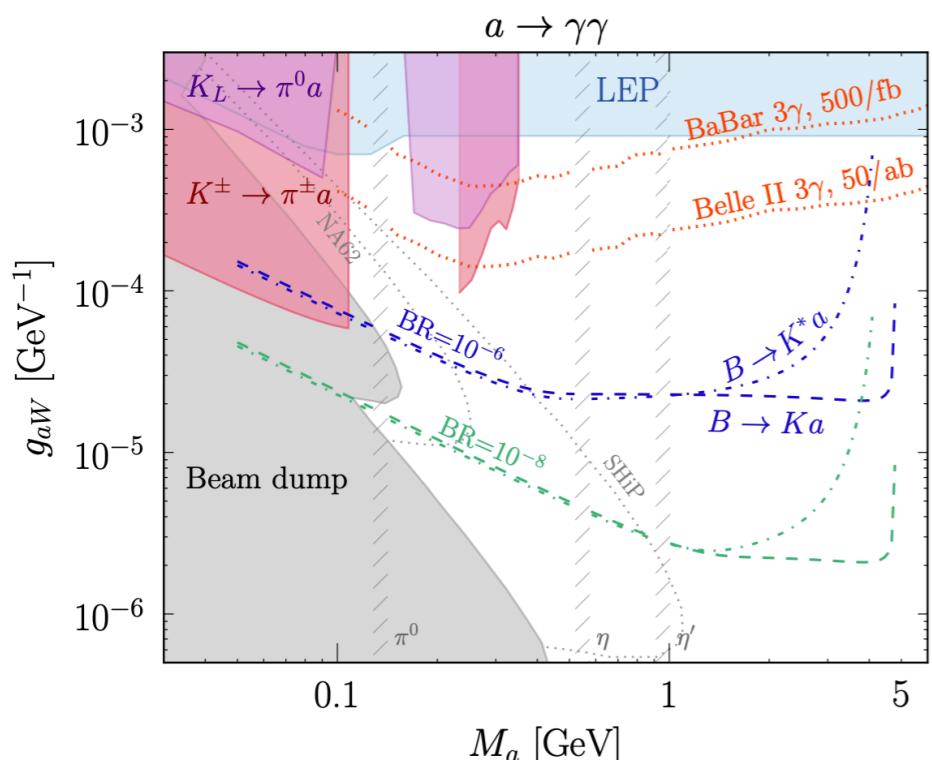
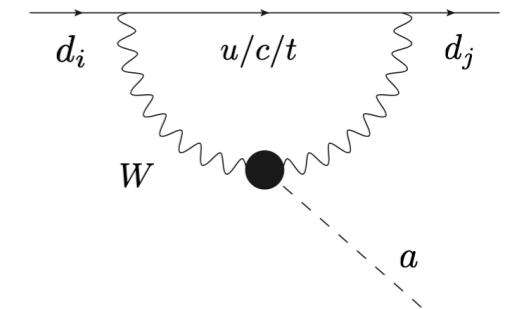


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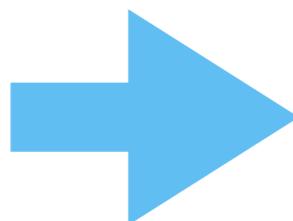
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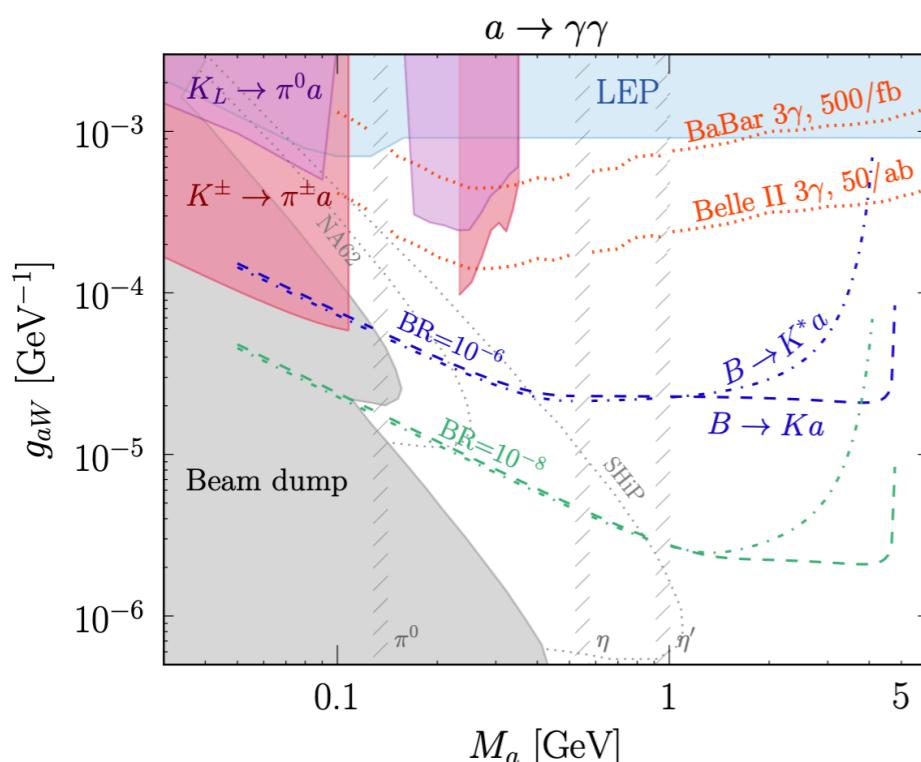
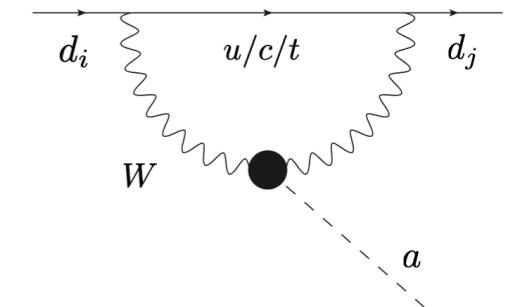
Izaguirre, Lin, Shuve - 1611.09355

aWW and rare Kaon decays

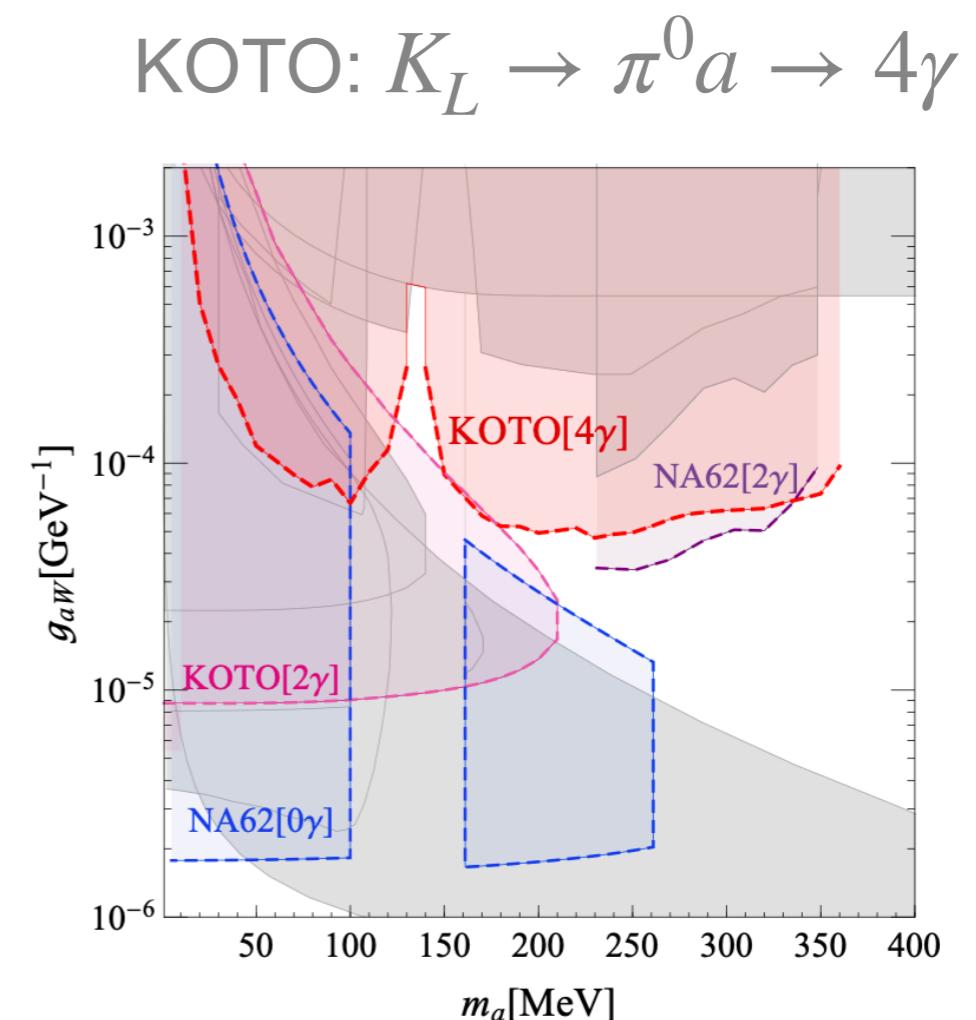
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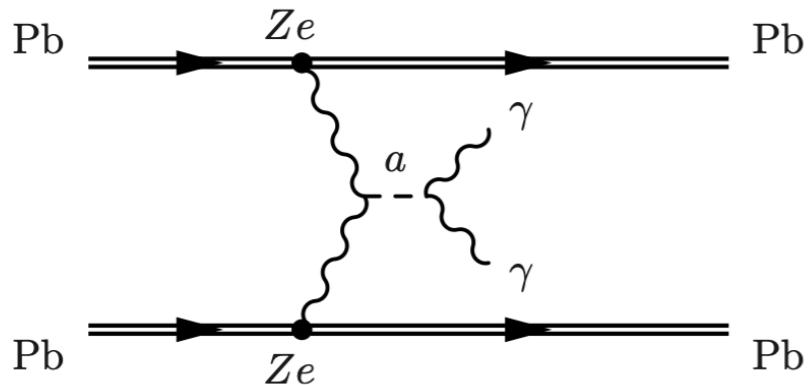
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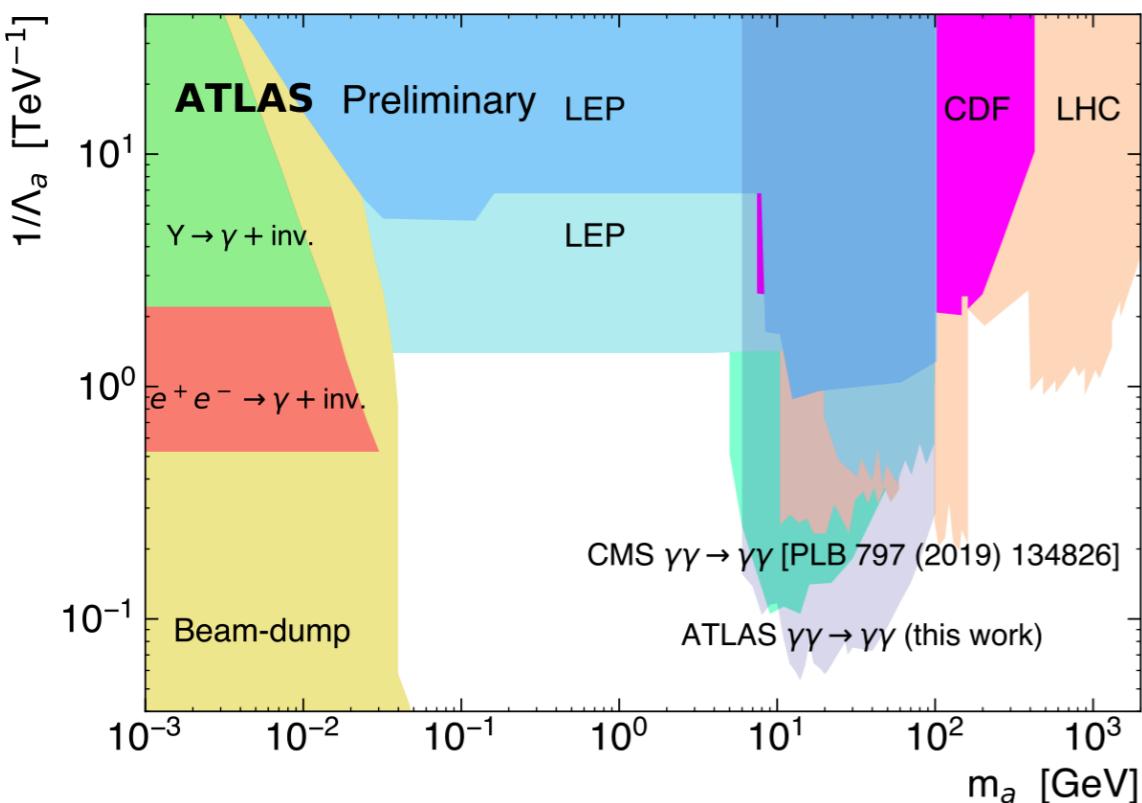
Gori, Perez, Tobioka - 2005.05170

higher ALP masses

heavy ion collisions at the LHC



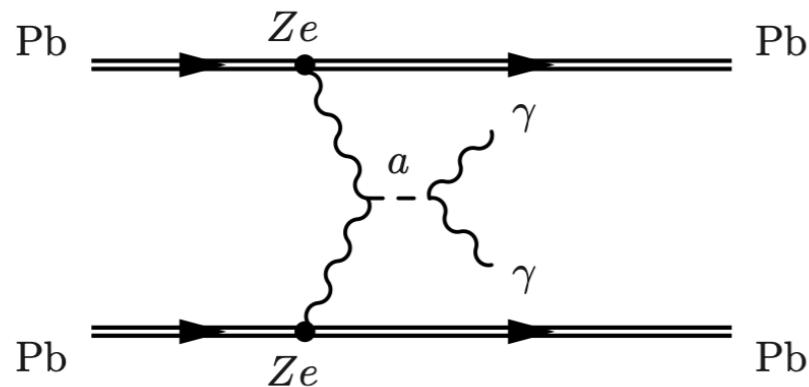
Existing constraints from JHEP 1712 (2017) 044



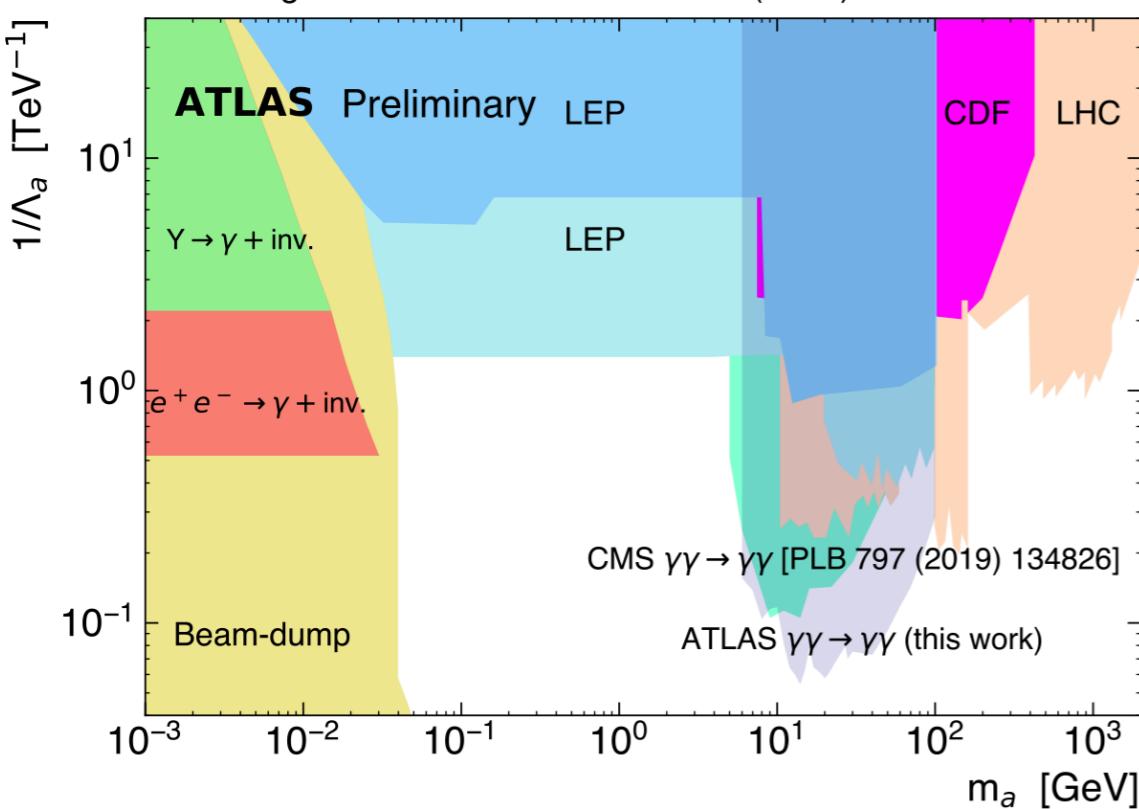
Knapen, Lin, Lou, Melia - 1607.06083
ALTAS, CMS

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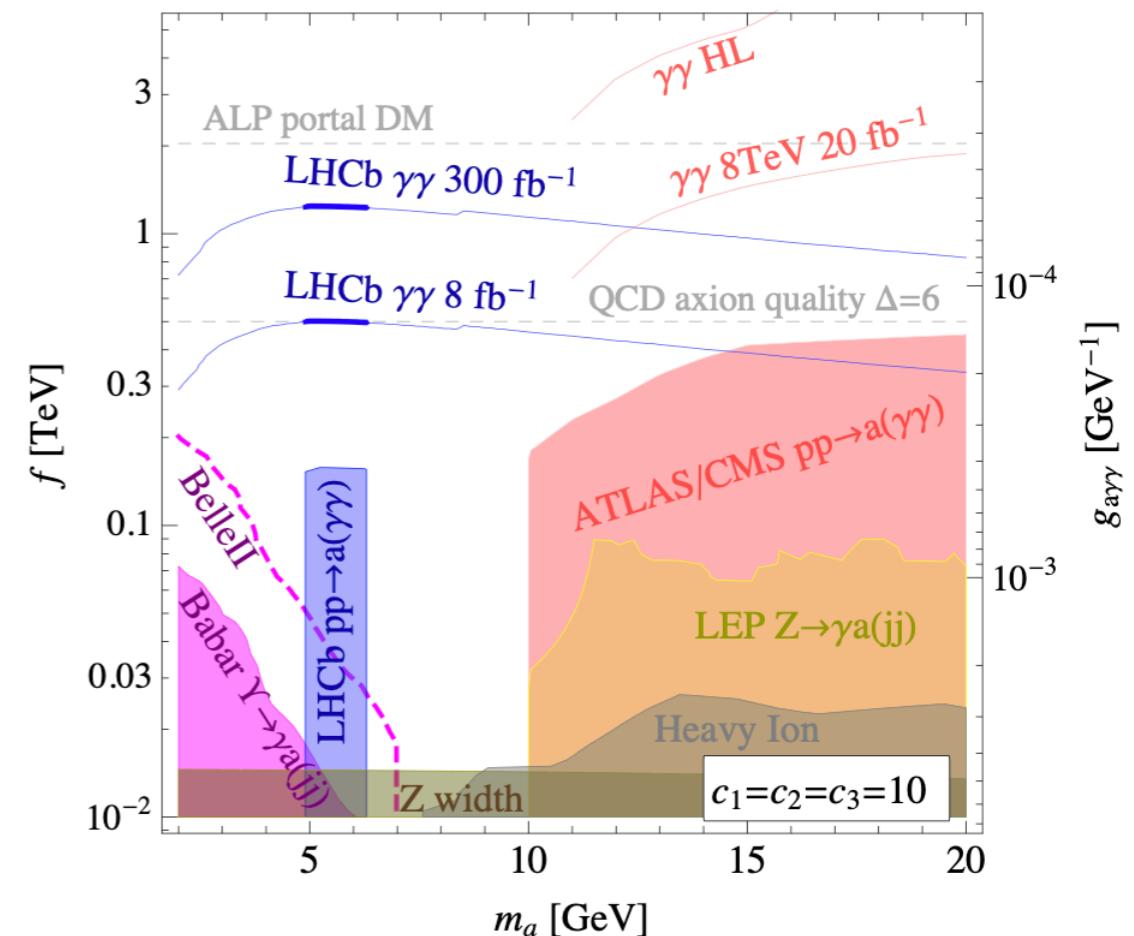
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$\gamma\gamma$ resonance at the LHC

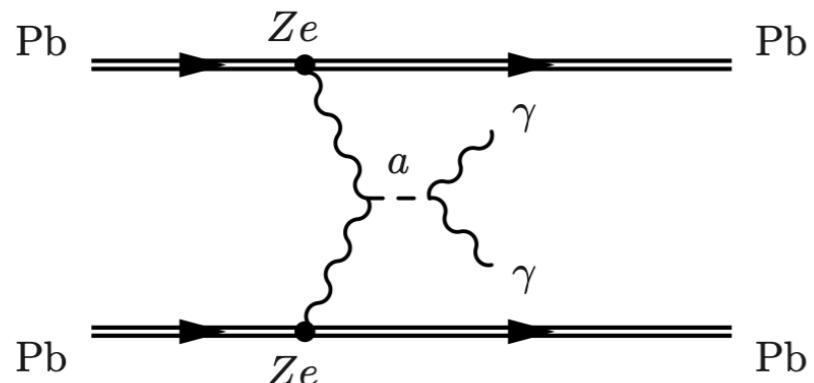


Mariotti, Redigolo, Sala, Tobioka - 1710.01743
 Vidal, Mariotti, Redigolo, Sala, Tobioka - 1810.09452

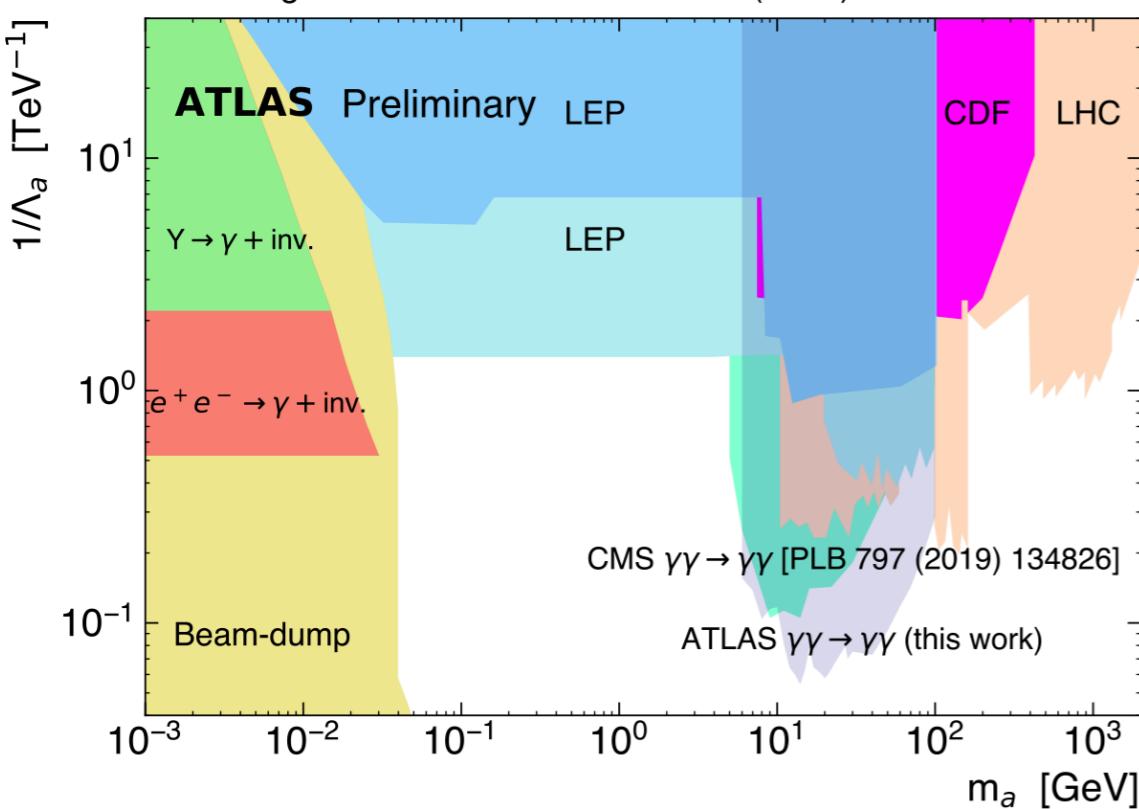
Knapen, Lin, Lou, Melia - 1607.06083
 ALTAS, CMS

higher ALP masses

heavy ion collisions at the LHC

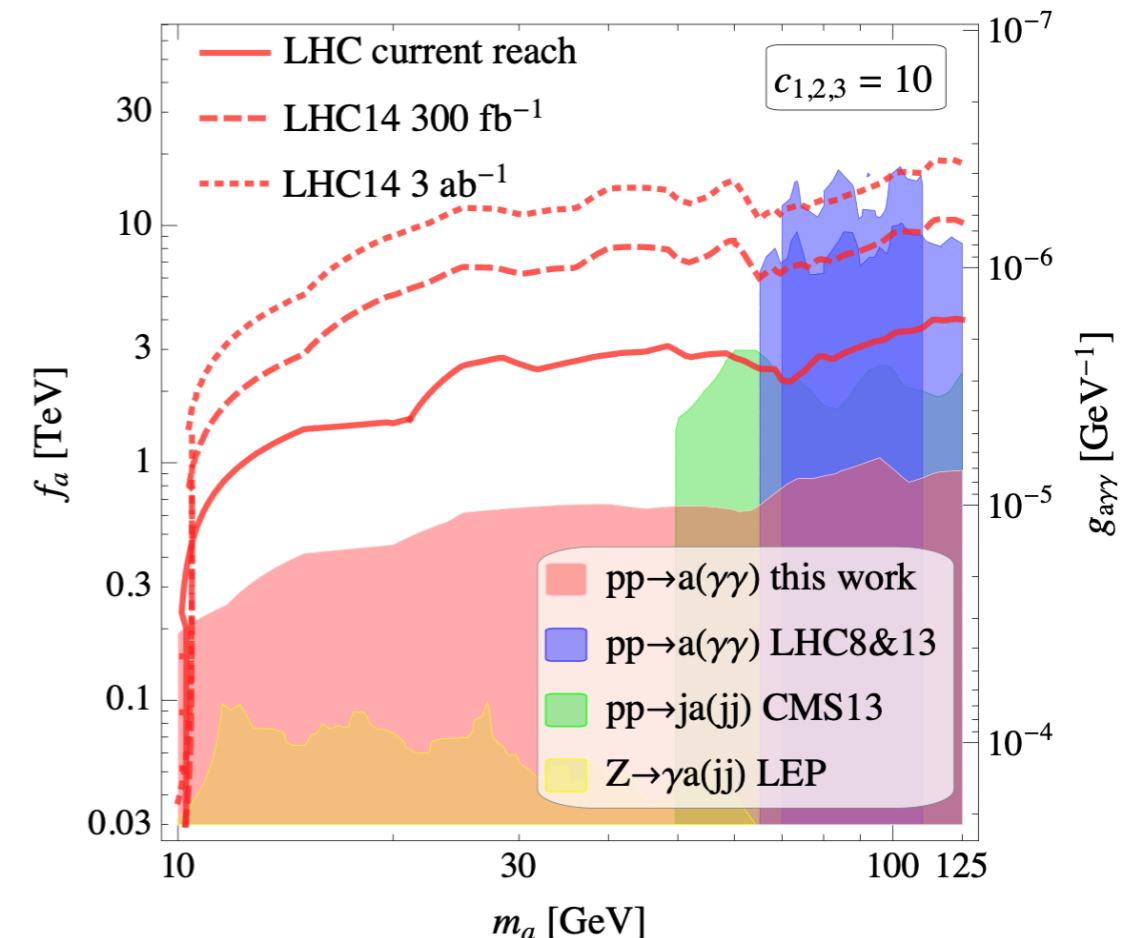


Existing constraints from JHEP 1712 (2017) 044



Knapen, Lin, Lou, Melia - 1607.06083
ALTAS, CMS

$\gamma\gamma$ resonance at the LHC



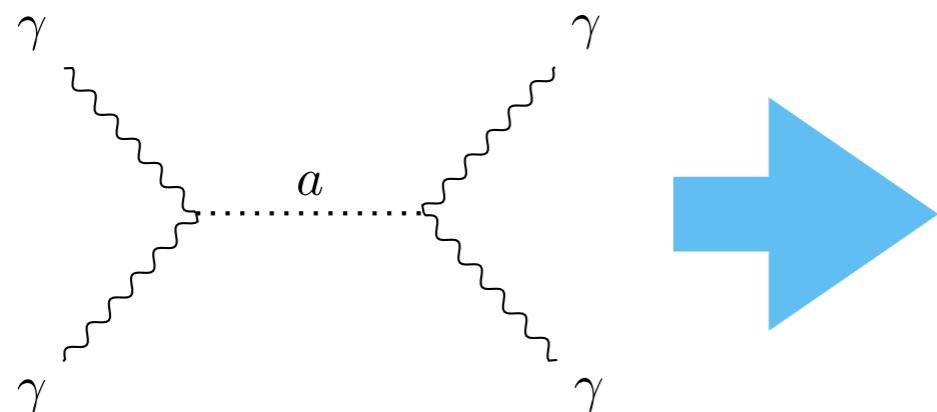
Mariotti, Redigolo, Sala, Tobioka - 1710.01743
Vidal, Mariotti, Redigolo, Sala, Tobioka - 1810.09452

Probing ALPs and the Axiverse with Superconducting Radiofrequency Cavities

Bogorad, Hook, Kahn, YS - 1902.01418

the idea

probing off-shell ALPs via non-linear QED in a cavity

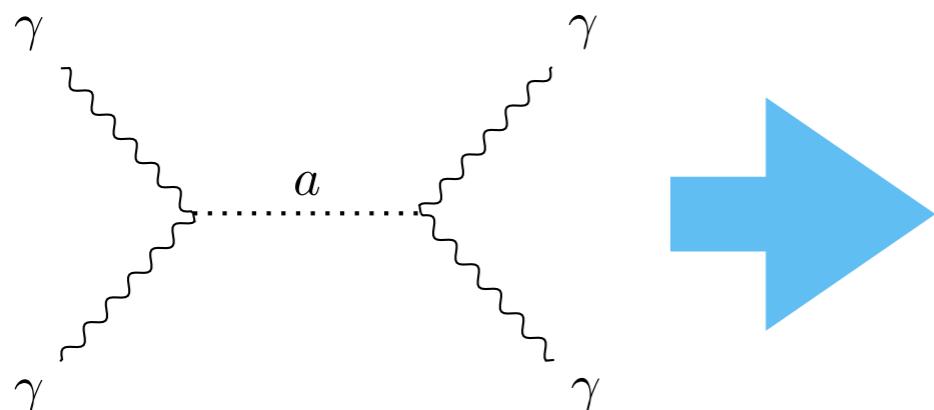


$$\propto (F^{\mu\nu}\tilde{F}_{\mu\nu})^2 \propto (E \cdot B)^2$$

non-linear Maxwell equations

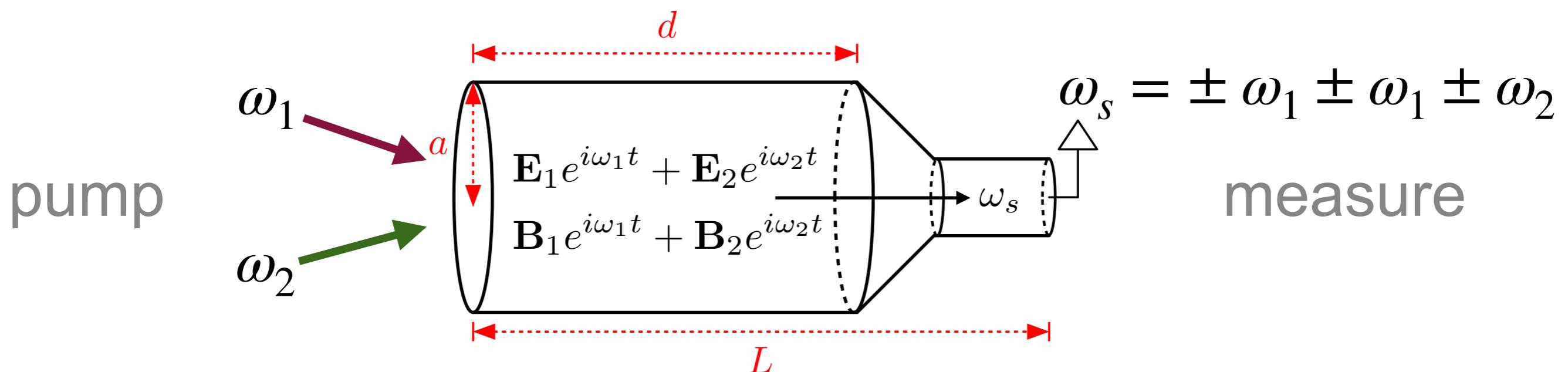
the idea

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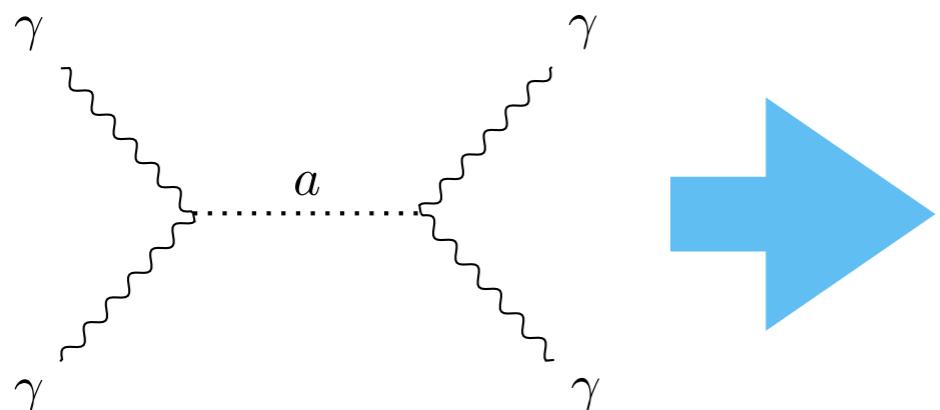
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non-linear Maxwell equations



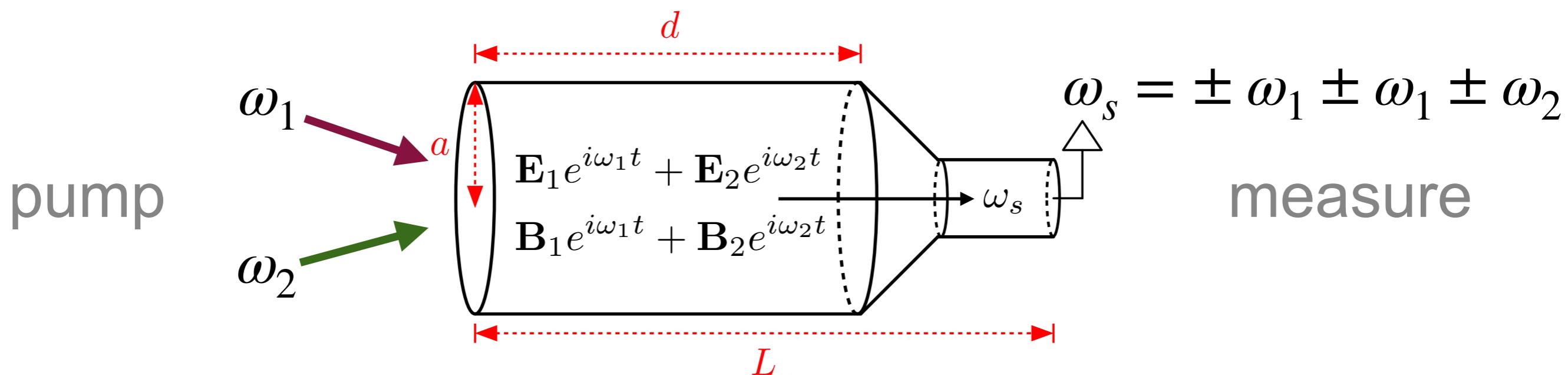
the idea

probing off-shell ALPs via non-linear QED in a cavity



$$\propto (F^{\mu\nu}\tilde{F}_{\mu\nu})^2 \propto (E \cdot B)^2$$

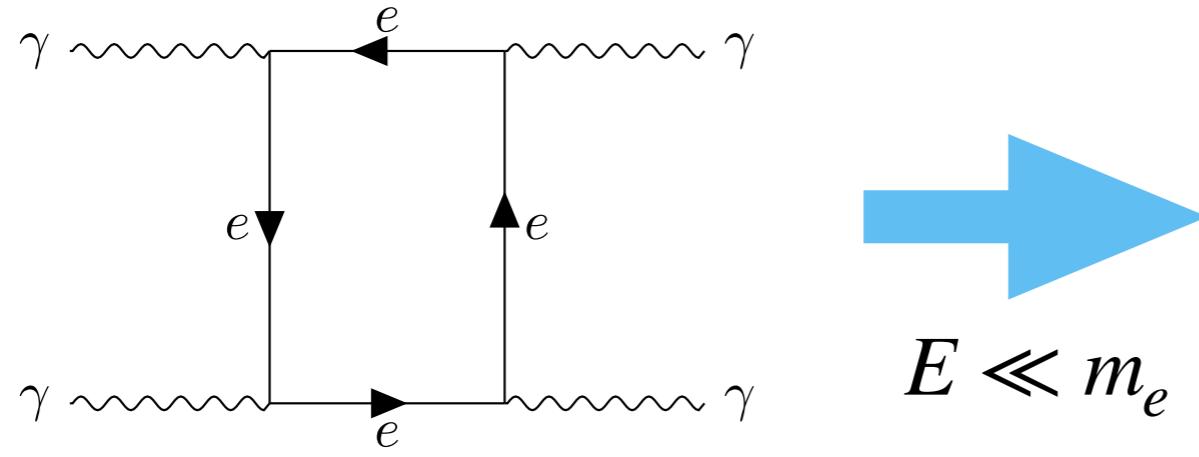
non-linear Maxwell equations



advantages:

- * probes large range of masses - broadband
- * does not rely on ALP been dark matter

the Euler Heisenberg effect



non-linear QED

$$\propto c_1(F^{\mu\nu}F_{\mu\nu})^2 + c_2(F^{\mu\nu}\tilde{F}_{\mu\nu})^2$$

Hiesenberg Euler, 1936
Schwinger, 1951

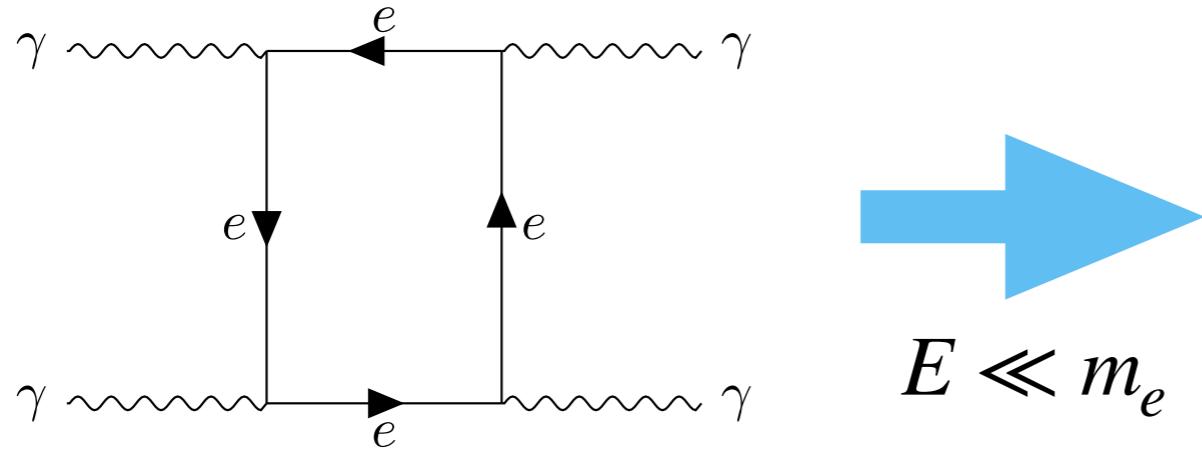
$$E \ll m_e$$

never been measured below the electron mass!

measured at high energies
(light by light scattering)

ATLAS, 2017

the Euler Heisenberg effect



non-linear QED

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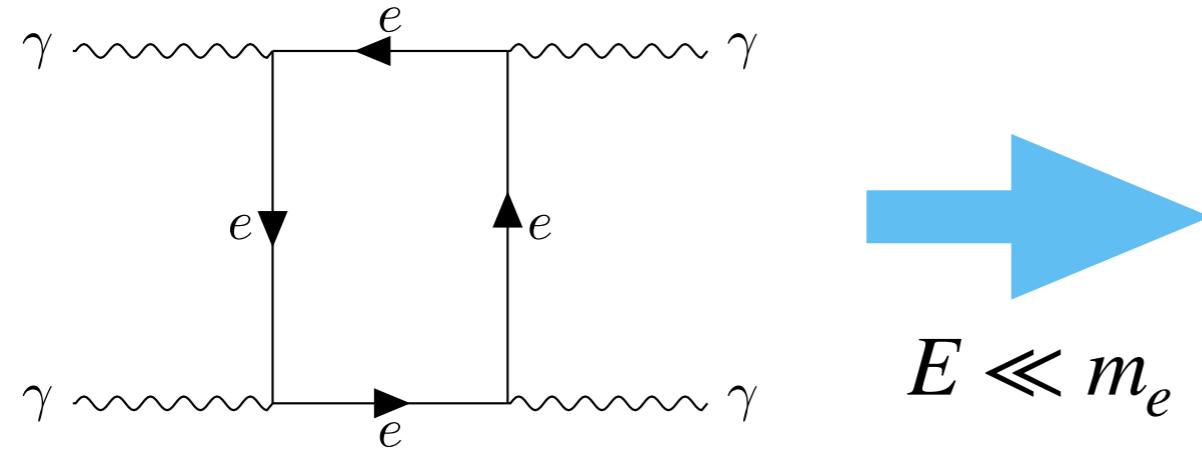
measured at high energies
(light by light scattering)

ATLAS, 2017

ALP vs EH $\frac{c_\gamma/\Lambda}{m_a} \gtrsim \mathcal{O}(1) \times \frac{\alpha}{m_e^2} \simeq \frac{10^{-10} \text{ GeV}^{-1}}{10^{-6} \text{ eV}}$

comparable to the current limit on ALPs (by CAST)
Evans and Rafelski, 1810.06717

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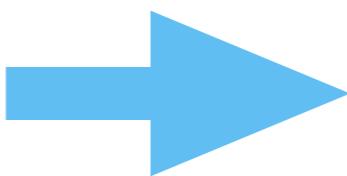
ALP vs EH

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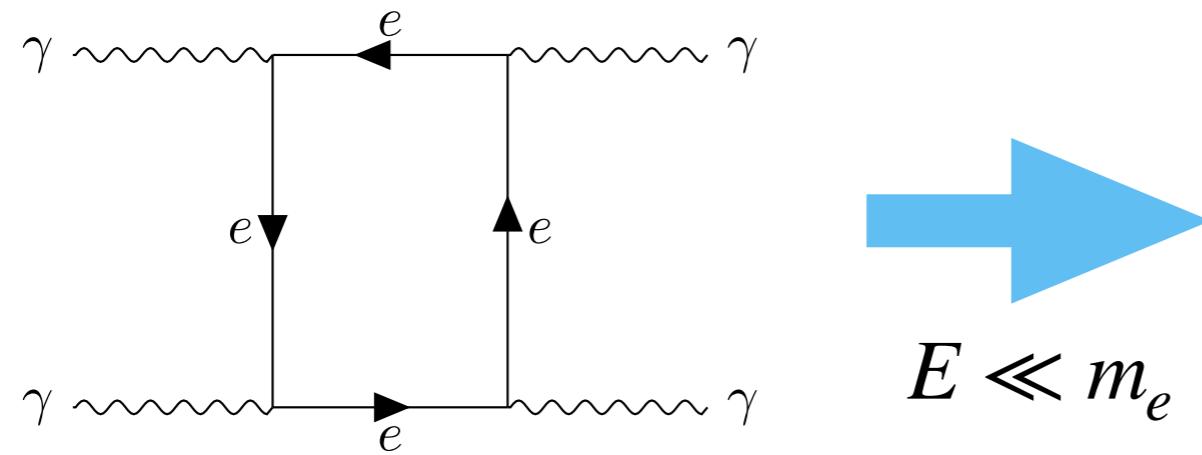
Evans and Rafelski, 1810.06717

improve current bounds



sensitivity to EH

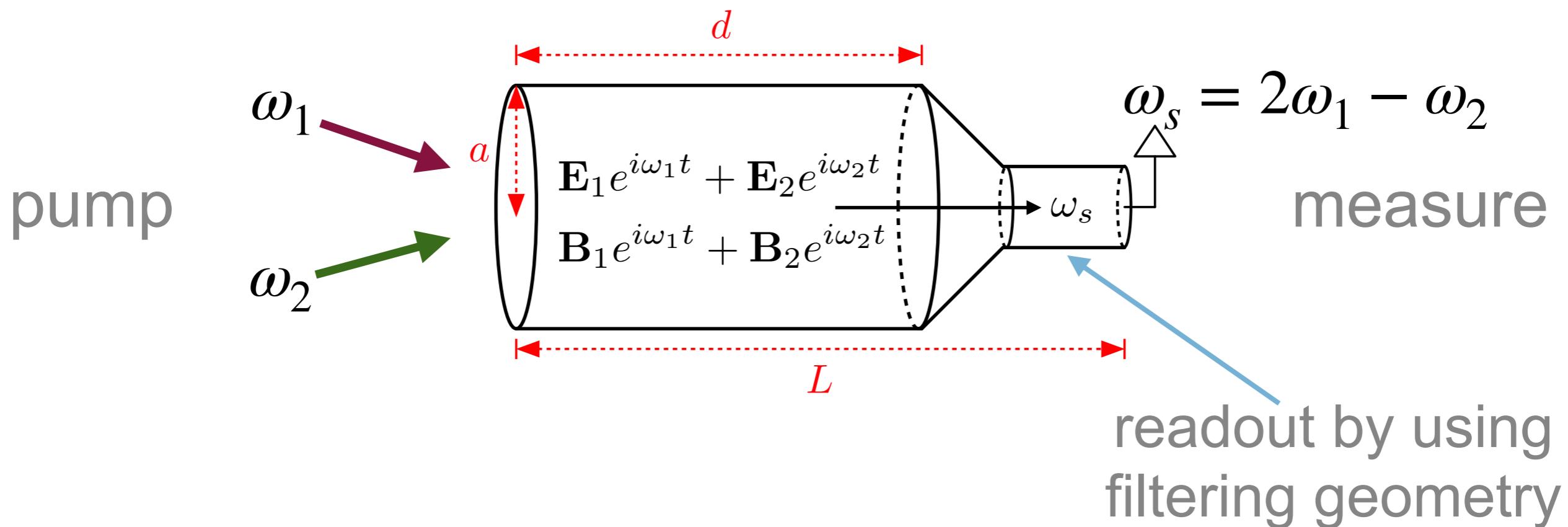
detecting the EH effect by superconducting radiofrequency cavities



non-linear QED in the SM

$$\propto c_1(F^{\mu\nu}F_{\mu\nu})^2 + c_2(F^{\mu\nu}\tilde{F}_{\mu\nu})^2$$

Hiesenberg Euler, 1936
Schwinger, 1951



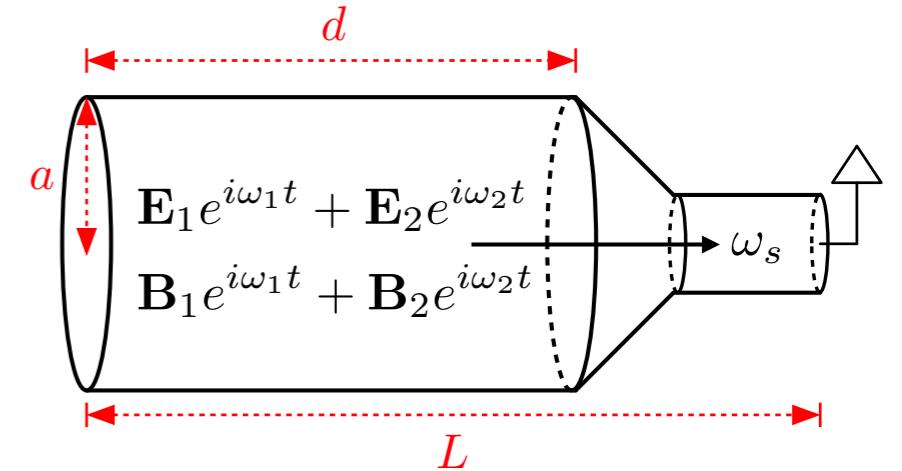
Brodin, Marklund, Stenflo, PRL, 2001
Eriksson, Brodin, Marklund, Stenflo, PRA, 2004

$$\omega_s > \omega_1, \omega_2$$

sensitivity to ALPs

$$\frac{c_\gamma}{\Lambda} = \begin{cases} \left(\frac{4TL}{Q_s V E_0^6 K_0^2} \sqrt{\frac{B}{t}} \text{SNR} \right)^{1/4} \omega_s & m_a \ll \omega_s \\ \left(\frac{4TL}{Q_s V E_0^6 K_\infty^2} \sqrt{\frac{B}{t}} \text{SNR} \right)^{1/4} m_a & m_a \gg \omega_s \end{cases}$$

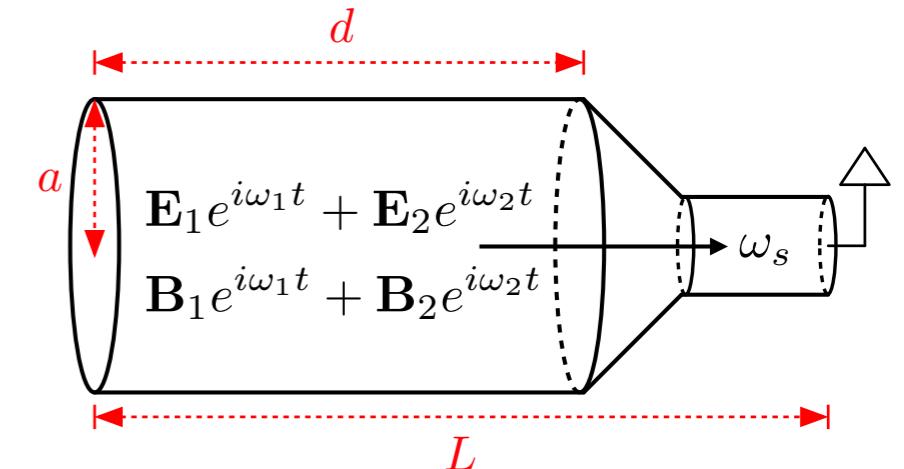
SNR = 5



sensitivity to ALPs

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SNR = 5



$$a = 0.5 \text{ m}, d = 1.56 \text{ m}, V = 1.23 \text{ m}^3$$

$$\omega_1 = \text{TE}_{011}, \omega_2 = \text{TM}_{010}, \omega_s = \text{TM}_{020}$$

$$\omega_s/(2\pi) = 527 \text{ MHz}$$

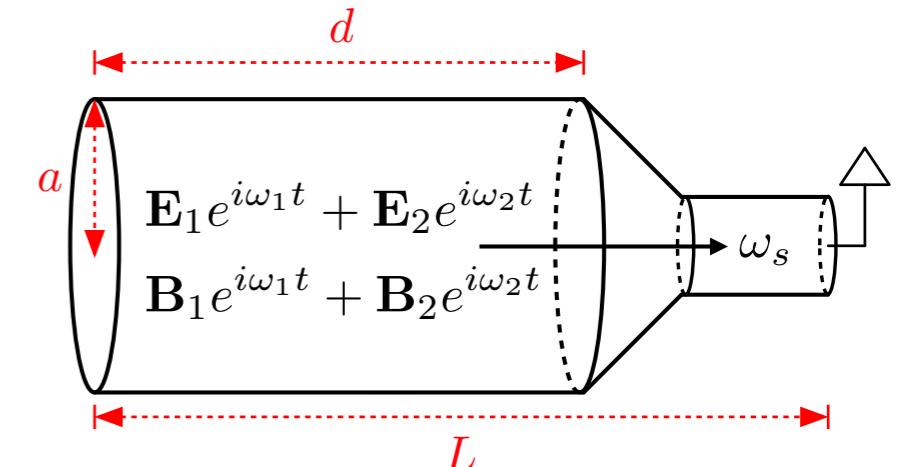
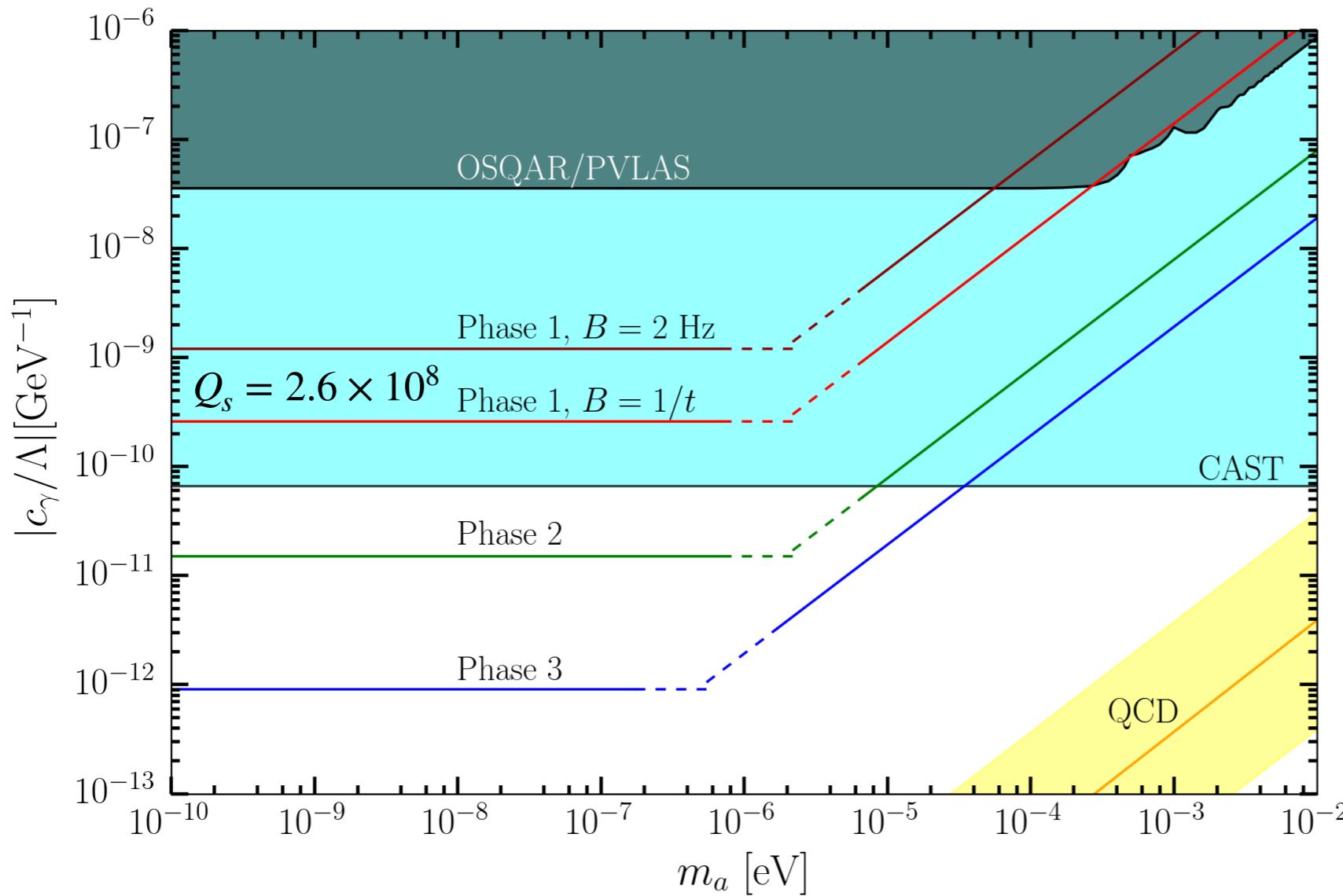
$$K_0 = 0.4, K_\infty = 0.18$$

$$E_0 = 45 \text{ MV/m} \quad T = 1.5 \text{ K}$$

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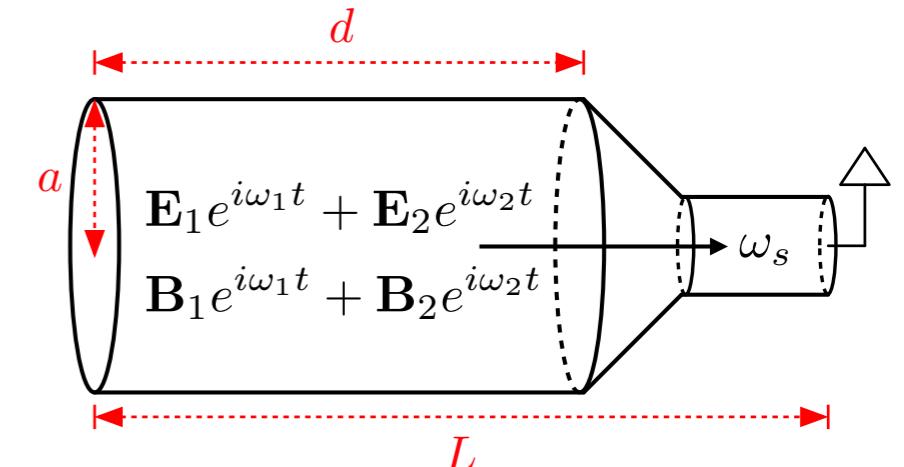
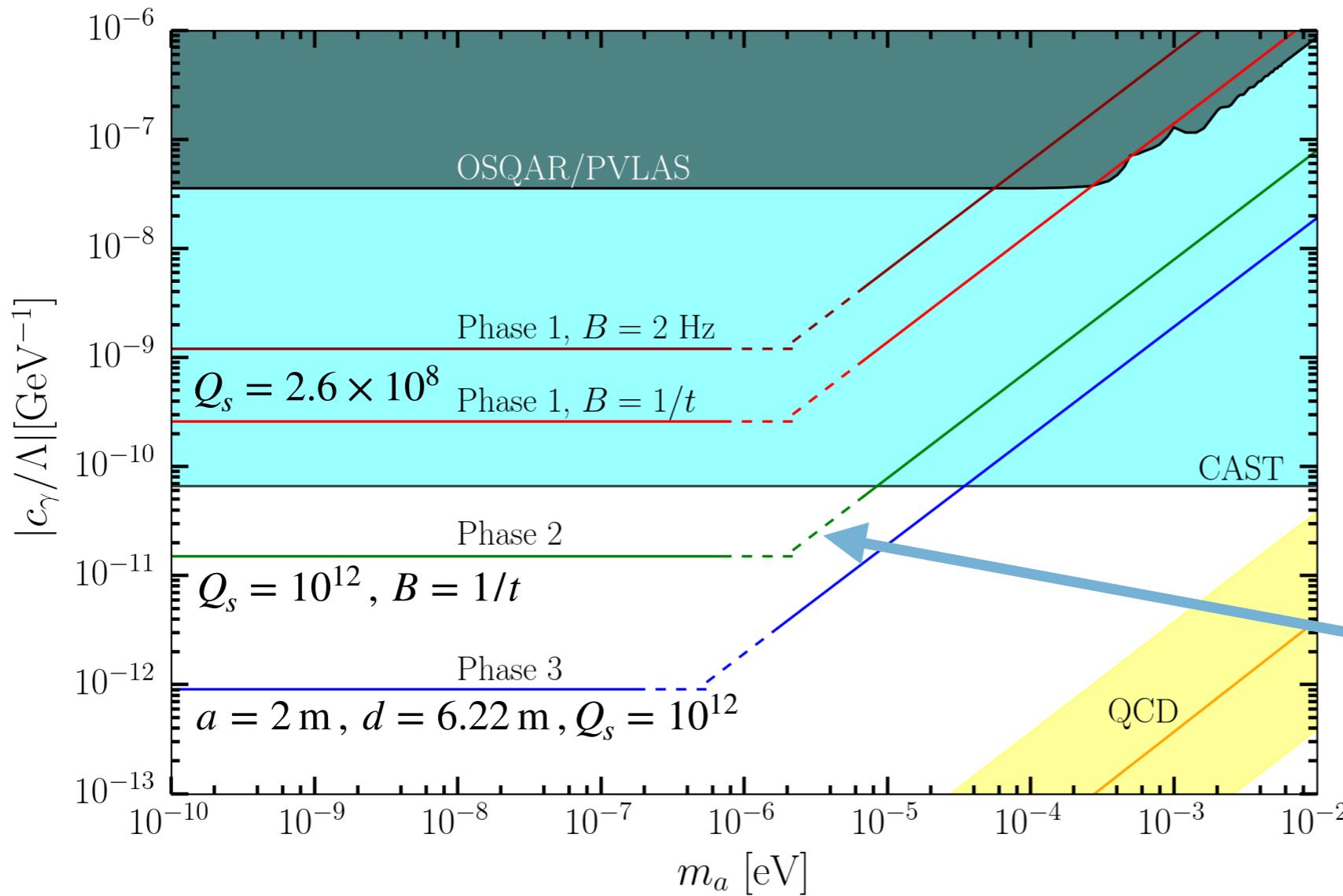
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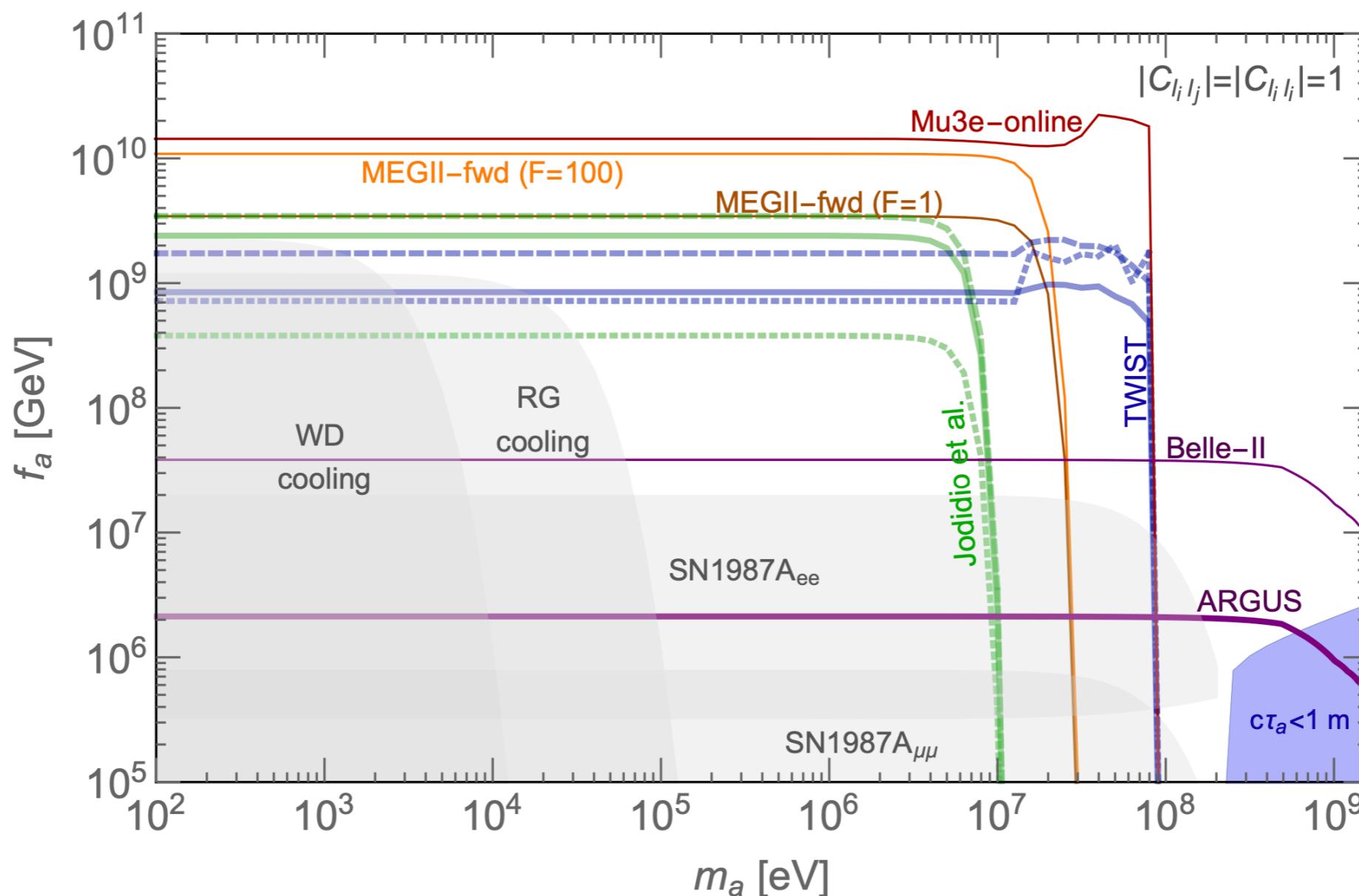
20 days run to
detect EH!

Outlook

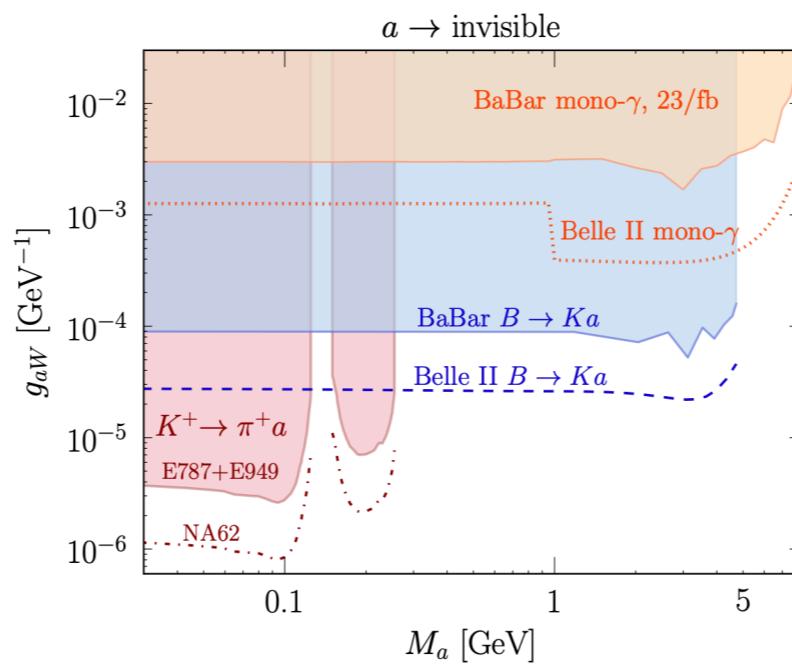
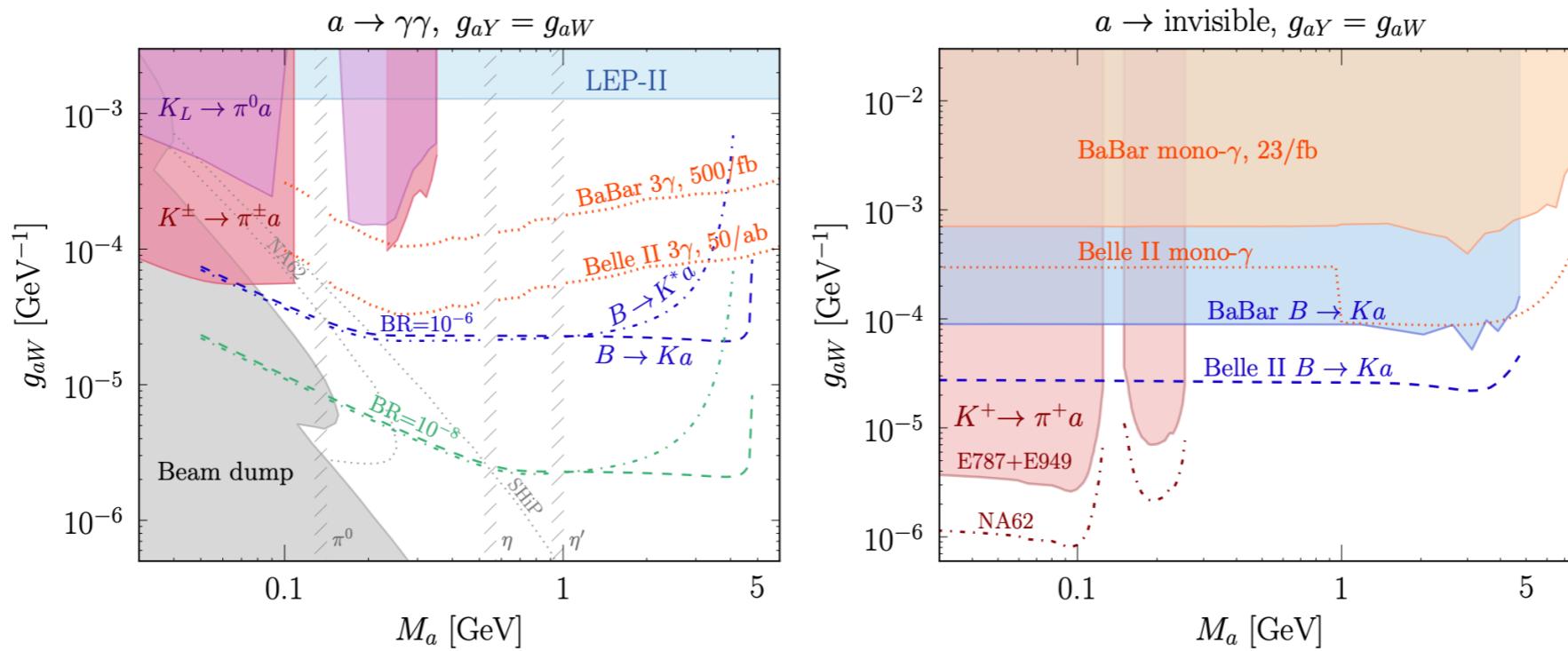
- * on tape PrimEx data can improve the sensitive to ALP with QCD mass scale, future GlueX data will improve it by order of magnitude
- * ALPs hadronic rates can be estimated from data
- * future rare kaon decay is a promising channel to probe ALPs
- * higher ALPs masses can be probed by LHC searches (heavy ion/ $\gamma\gamma$ resonances)

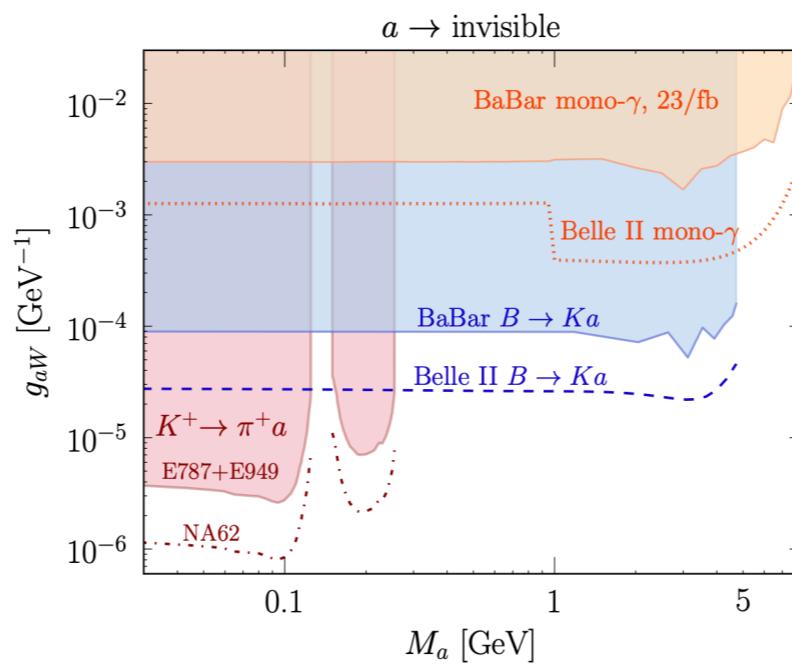
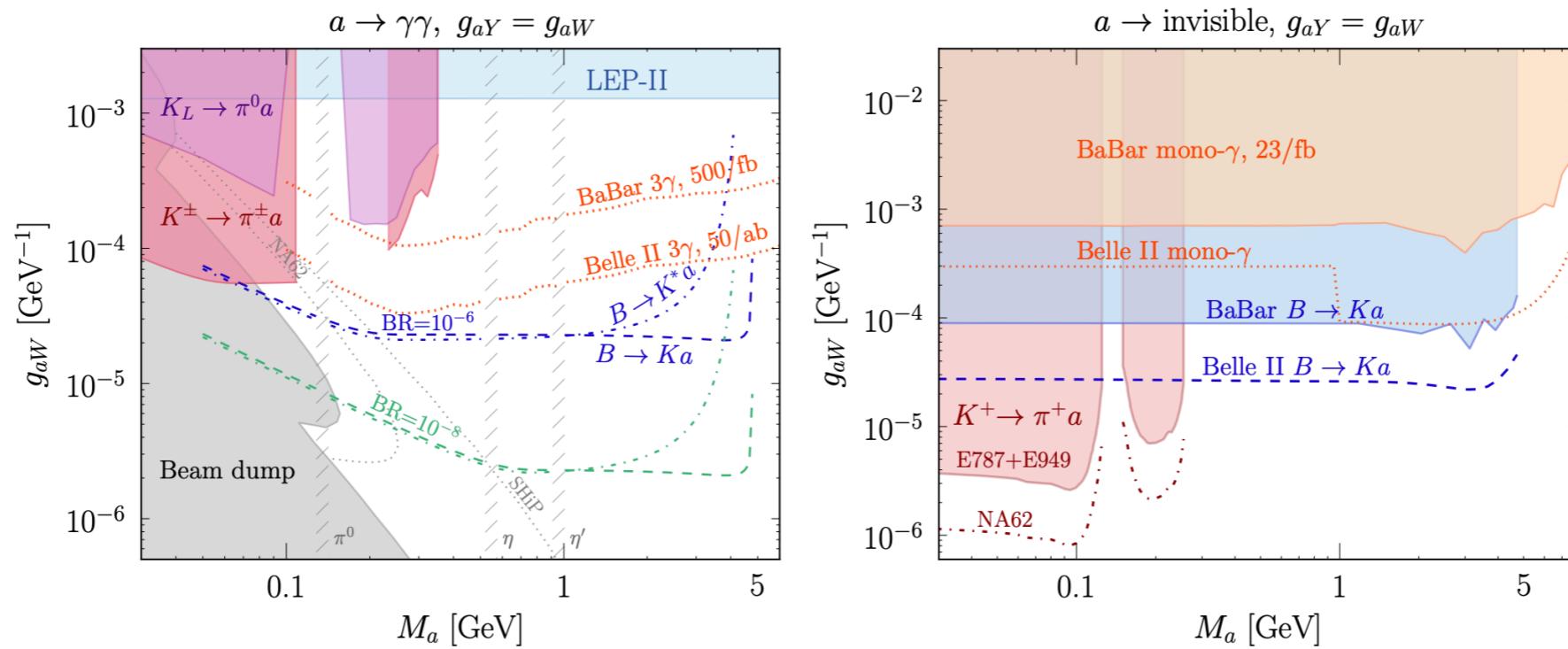
Backups

ALP and LFV



Calibbi, Redigolo, Ziegler, Zupan - 2006.04795
and Cornella, Pradisi, Sumensari - 1911.06279





Sensitivity to ALPs

Sensitivity to ALPs

the number of signal photons

$$N_s = \frac{1}{2\omega_s} \int d^3x |E_a(x)|^2 = \frac{Q_s^2 V E_0^6}{2\omega_s} \frac{c_\gamma^4}{\Lambda^4} \left\{ \begin{array}{l} \frac{K_0^2}{\omega_s^4} \quad m_a \ll \omega_s \\ \frac{K_\infty^2}{m_a^4} \quad m_a \gg \omega_s \end{array} \right. \text{modes overlap}$$

quality factor

cavity volume

pump field strength

electric field of the induced ALP current

Sensitivity to ALPs

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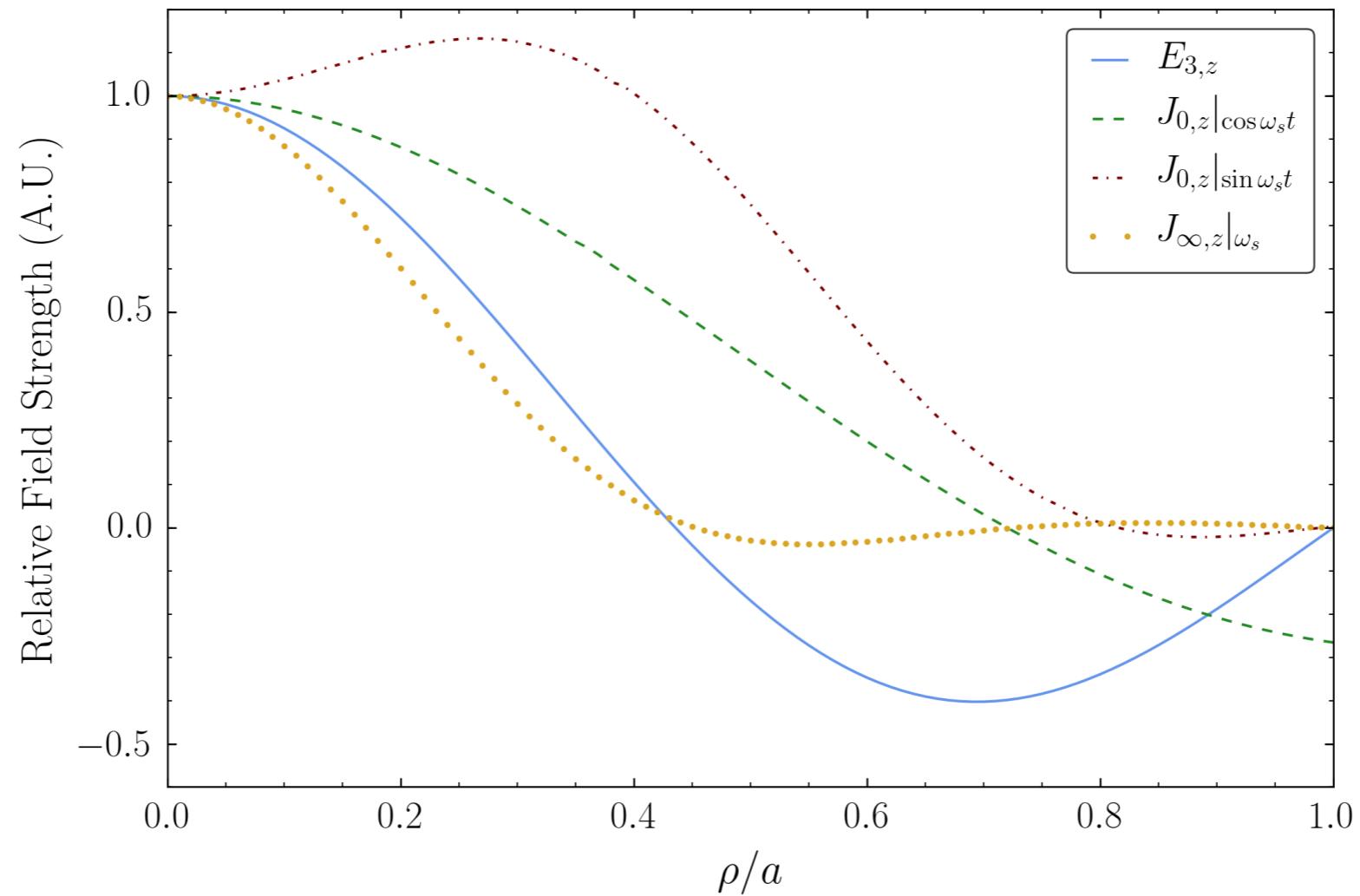
quality factor
cavity volume
pump field strength
electric field of the induced ALP current

signal-to-noise ratio (SNR)
(Dicke radiometer equation)

$$\text{SNR} \approx \frac{N_s}{N_{\text{th}}} \frac{1}{2LQ_s} \sqrt{\frac{t}{B}}$$

time
signal bandwidth
cavity's length
thermal noise photons
Temperature/ ω_s

Overlap



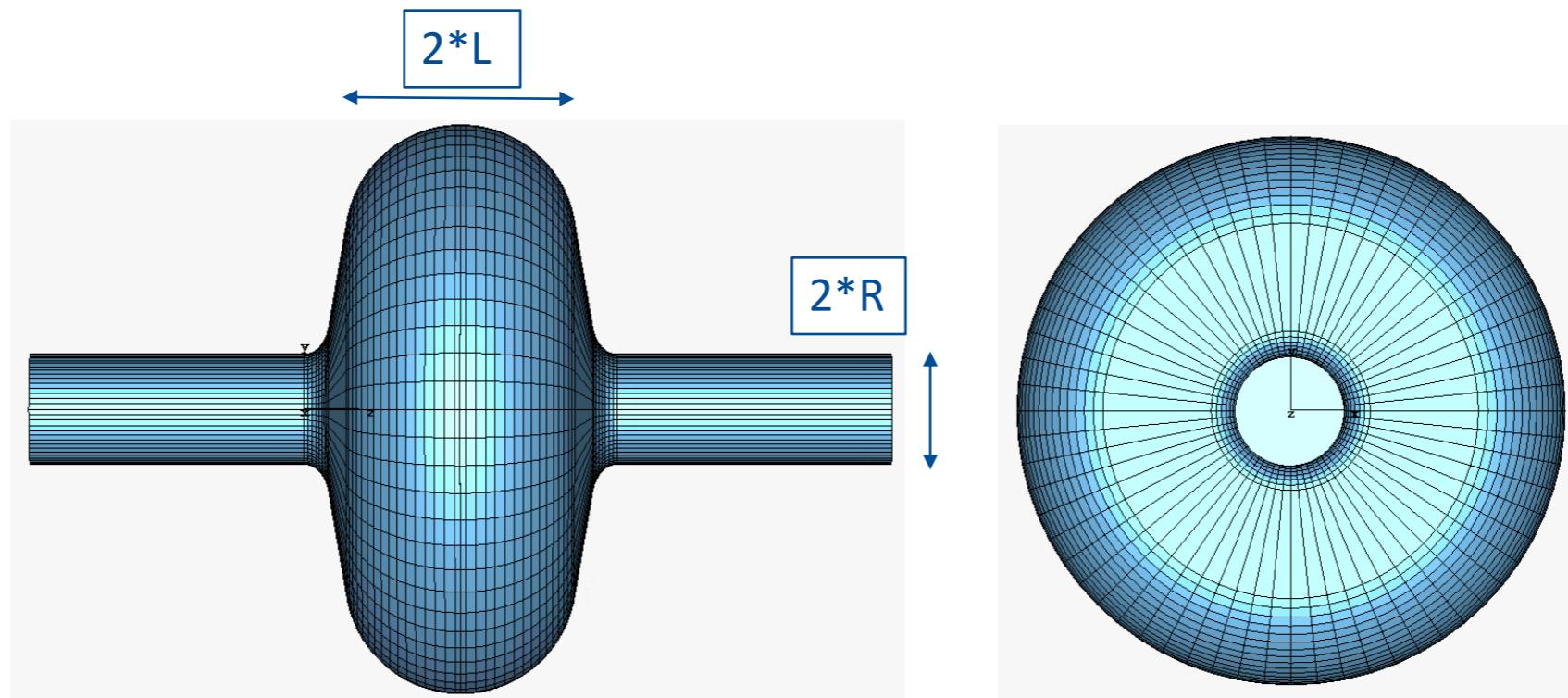
Cavity vs LSW

$$\left. \frac{N_s}{N_i} \right|_{\text{LSW}} \sim \left(\frac{c_\gamma}{\Lambda} \right)^4 B_{\text{prod.}}^2 B_{\text{det.}}^2 L^4$$

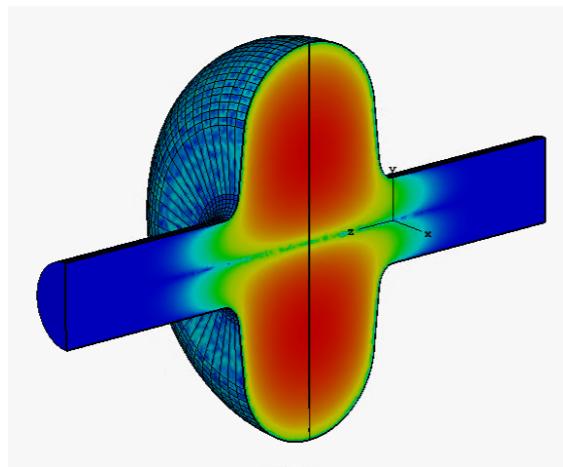
$$\left. \frac{N_s}{N_i} \right|_{\text{cavity}} \sim Q_s^2 \left(\frac{c_\gamma}{\Lambda} \right)^4 E_0^4 L^4$$

$$\text{SNR} = \frac{P_s}{T} \sqrt{\frac{t}{B}} \approx \frac{N_s}{N_{\text{th}}} \frac{1}{2LQ_s} \sqrt{\frac{t}{B}}$$

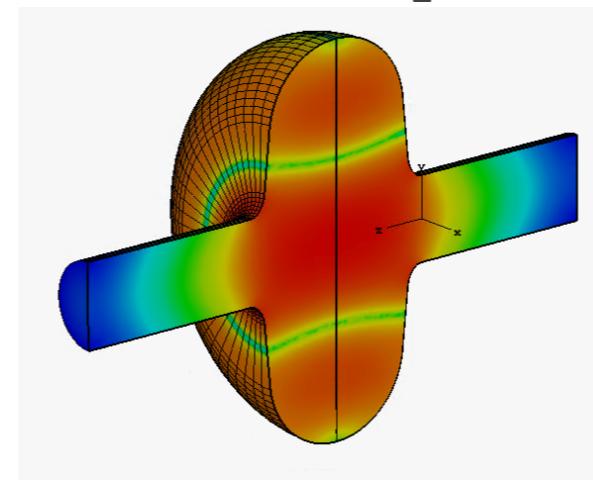
the cavity in practice at Fermilab



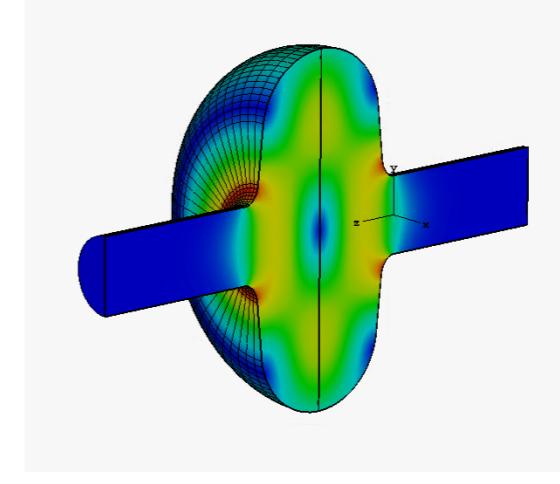
TE011 (ω_1)



TM021 (ω_2)



TM012 (ω_3)



Disentangling EH and ALPs

Proof of concept with rectangular cavity

$$E_p = r_1 E_1 + r_{1'} E_{1'} + r_2 E_2$$

pump 3 modes:

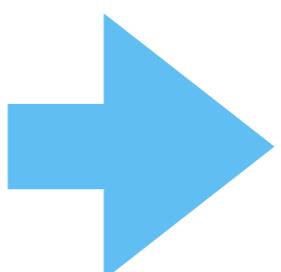
$$\text{TE}_{221}/\text{TM}_{221}/\text{TM}_{121}$$

signal mode:

$$\text{TM}_{163}$$

matching condition

$$\omega_s = 2\omega_1 - \omega_2$$



$$K_\infty = 0.047r_2(r_1^2 - 0.18r_{1'}^2)$$

$$K_{\text{EH}} = 0.059r_2(r_1^2 - 8.24r_{1'}^2)$$

ALP photons coupling

$$\mathcal{H}(m_N, m_a, s, t) \equiv 128\pi \frac{m_N^4}{m_a^3} \frac{m_a^2 t(m_N^2 + s) - m_a^4 m_N^2 - t((s - m_N^2)^2 + st)}{t^2(s - m_N^2)^2(t - 4m_N^2)^2}$$