

“FLAVOURED LEPTOGENESIS AND TYPE-II SEESAW MECHANISM WITH TWO HIGGS TRIPLET SCALARS”

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Introduction

- Neutrino mass generation through type-II seesaw mechanism
- Baryon asymmetry estimation through flavoured triplet leptogenesis

Model description

- Two triplet Higgs scalars with hypercharge, $\mathcal{Y} = 2$

$$T_1 = \begin{pmatrix} \frac{\delta_1^+}{\sqrt{2}} & \delta_1^{++} \\ \delta_1^0 & -\frac{\delta_1^+}{\sqrt{2}} \end{pmatrix}, \quad T_2 = \begin{pmatrix} \frac{\delta_2^+}{\sqrt{2}} & \delta_2^{++} \\ \delta_2^0 & -\frac{\delta_2^+}{\sqrt{2}} \end{pmatrix}$$

- Triplet vacuum expectation values:

$$\langle \delta_1^0 \rangle = \omega_1 = |\omega_1| e^{i\alpha}, \quad \langle \delta_2^0 \rangle = \omega_2$$

- $\omega_1, \omega_2 \ll v$, $\omega_1 \sim [10^{-8} - 10^{-6}] \text{ GeV}$
- $M_{T_1} \gg M_{T_2}$, $M_{T_2} \sim 10^9 \text{ GeV}$

[Avinanda Chaudhuri, Biswarup Mukhopadhyaya (2016)]

Model description

- Extended Lagrangian

$$\mathcal{L} = \text{Tr}[(D_\mu T_k)^\dagger (D^\mu T_k)] - \frac{Y_{ij} L_i^T C_i \sigma T_k L_j}{\sqrt{2}},$$

- Lepton number breaking trilinear term $\mu_k \phi^\dagger T_k i \sigma_2 \phi^*$ in the potential $V(\phi, T_1, T_2)$, $\mu_1 = |\mu_1| e^{i\beta}$
- Neutrino mass generation

$$M_\nu = M_\nu^{(1)} + M_\nu^{(2)} = Y_1 \omega_1 \cos \alpha + Y_2 \omega_2$$

[Avinanda Chaudhuri, Biswarup Mukhopadhyaya (2016)]

Neutrino mass matrix

- Two-zero texture B_2 : [Madan Singh (2020)]

$$B_2 = \begin{pmatrix} \times & 0 & \times \\ 0 & \times & \times \\ \times & \times & 0 \end{pmatrix}$$

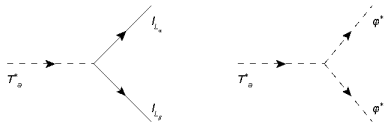
- The chosen neutrino mass matrix:

$$M_\nu = \begin{bmatrix} 0.04135 & 0 & 0.03411 \\ 0 & 0.05465 & 0.05085 \\ 0.03411 & 0.05085 & 0 \end{bmatrix}.$$

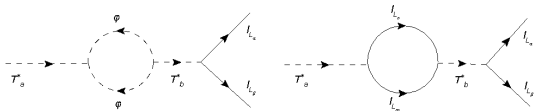
- $\Sigma = m_1 + m_2 + m_3 \approx 0.1459\text{eV} < 0.16\text{eV}$

Triplet decay modes

- Tree level decay diagram:



- One-loop decay diagram:



[R. Gonzalez Felipe, F.R. Joaquim, and H. Serodio (2013)]

Purely Flavoured Leptogenesis

- Fully flavoured CP asymmetry parameter: [Branco et al (2012)]

$$\epsilon^{\alpha\beta} = \frac{M_{T_2}(B_l B_\phi)^{\frac{1}{2}}}{4\pi v^2} \frac{\text{clm}[(M_\nu^{(2)})_{\alpha\beta}(M_\nu^{(1)*})_{\alpha\beta}]}{[\text{Tr}(M_\nu^{(2)\dagger} M_\nu^{(2)})]^{\frac{1}{2}}}$$

$$\sum_{\alpha,\beta} \epsilon_{\alpha\beta} = 0$$

- $B_l \gg B_\phi$

Fully flavoured Boltzmann equations

[R. Gonzalez Felipe, F.R. Joaquim, and H. Serodio (2013)]

$$szH(z) \frac{d\Sigma_T}{dz} = -\left(\frac{\Sigma_T}{\Sigma_T^{eq}} - 1\right)\gamma_D - 2\left(\frac{\Sigma_T^2}{\Sigma_T^{eq^2}} - 1\right)\gamma_A, \quad (1)$$

$$szH(z) \frac{d\Delta_T}{dz} = -\gamma_D \left(\frac{\Delta_T}{\Sigma_T^{eq}} + \sum_{\alpha,\beta} B_1^{\alpha\beta} \frac{\Delta_{L_\alpha}}{Y_L^{eq}} - B_1^\phi \frac{\Delta_\phi}{Y_\phi^{eq}}\right), \quad (2)$$

$$szH(z) \frac{d\Delta_\phi}{dz} = \sum_{\alpha,\beta} X_{\alpha\beta} - 2B_1^\phi \gamma_D \left(\frac{\Delta_\phi}{Y_\phi^{eq}} - \frac{\Delta_T}{Y_T^{eq}}\right), \quad (3)$$

$$szH(z) \frac{d\Delta_{L_\alpha}}{dz} = \sum_\alpha \left[X_{\alpha\beta} - 2B_1^{\alpha\beta} \gamma_D \left(\frac{\Delta_T}{Y_T^{eq}} + \frac{\Delta_{L_\alpha} + \Delta_{L_\beta}}{2Y_l^{eq}}\right)\right], \quad (4)$$

$$\left[z = \frac{M_T}{T}\right]$$

Lepton asymmetry plots: for different branching ratios

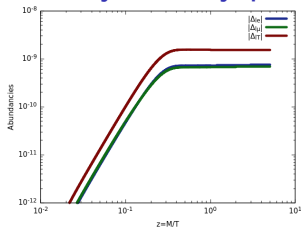


Figure: $B_l = 0.99999$

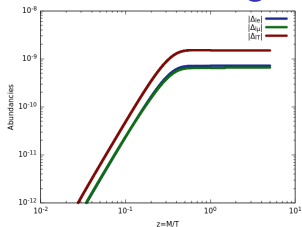


Figure: $B_l = 0.9999$

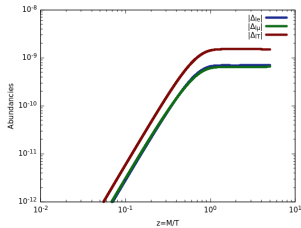


Figure: $B_l = 0.99$

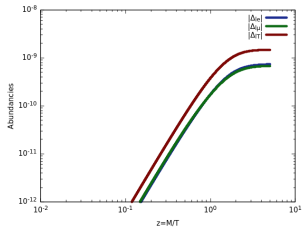


Figure: $B_l = 0.50$

Result

- Baryon asymmetry:

$$\eta_B = 3c_{sph} \sum_{\alpha,\beta} A_{\alpha\beta}^{-1} \Delta_{I\beta}$$

- Result table:

B_I	η_B
0.99999	-5.24×10^{-10}
0.9999	-5.30×10^{-10}
0.99	5.85×10^{-10}
0.50	5.34×10^{-10}

Conclusion

- Type-II seesaw mechanism and baryon asymmetry
- Future work

The background of the slide is a light yellow gradient. It is filled with a repeating pattern of faint, grey Feynman diagrams. These diagrams represent various particle interactions, including vertices, propagators, and loops, with arrows indicating the direction of particle flow. The diagrams are scattered across the entire page, creating a textured, scientific background.

The End

Back-up slides

Neutrino mass matrix with two zero texture- B_2

$$M_\nu = \begin{pmatrix} Ae^{i\phi_A} & 0 & Be^{i\phi_B} \\ 0 & Ce^{i\phi_C} & De^{i\phi_D} \\ Be^{i\phi_B} & De^{i\phi_D} & 0 \end{pmatrix}$$

Fully flavoured CP asymmetry parameters

$$\epsilon^{ee} = \frac{M_{T_2}(B_l B_\phi)^{\frac{1}{2}} c_{ee} \omega_1 \cos\alpha \sin\theta_a}{4\pi v^2} \times \frac{A^2}{\sqrt{A^2 + 2(B^2 + D^2) + C^2}},$$

$$\epsilon^{e\tau} = \frac{M_{T_2}(B_l B_\phi)^{\frac{1}{2}} c_{e\tau} \omega_1 \cos\alpha \sin\theta_b}{4\pi v^2} \times \frac{B^2}{\sqrt{A^2 + 2(B^2 + D^2) + C^2}},$$

$$\epsilon^{\mu\mu} = \frac{M_{T_2}(B_l B_\phi)^{\frac{1}{2}} c_{\mu\mu} \omega_1 \cos\alpha \sin\theta_c}{4\pi v^2} \times \frac{C^2}{\sqrt{A^2 + 2(B^2 + D^2) + C^2}},$$

$$\epsilon^{\mu\tau} = \frac{M_{T_2}(B_l B_\phi)^{\frac{1}{2}} c_{\mu\tau} \omega_1 \cos\alpha \sin\theta_d}{4\pi v^2} \times \frac{D^2}{\sqrt{A^2 + 2(B^2 + D^2) + C^2}},$$

Boltzmann equations



$$X_{\alpha\beta} = \left(\frac{\Sigma_T}{\Sigma_T^{eq}} - 1 \right) \gamma_D \epsilon_1^{\alpha\beta} + 2\gamma_D (B_1^L \epsilon^{\alpha\beta} - B_1^{\alpha\beta} \epsilon_1) \\ - \left(2 \frac{\Delta_T}{Y_T^{eq}} + \frac{\Delta_{L_\alpha} + \Delta_{L_\beta}}{2Y_l^{eq}} \right) (2\gamma_{l_\alpha l_\beta}^{\overline{\phi\phi}} + \gamma_{l_\alpha \phi}^{\overline{l_\beta \phi}}),$$

- $z = \frac{M_T}{T}$,
- $H(z) = \frac{H_0(M_T)}{z^2}$, $H_0(T) = \sqrt{\frac{4\pi^3}{45} g_*} \frac{T^2}{m_P}$
- $m_P = 1.22 \times 10^{19} \text{ GeV}$, $s = \left(\frac{2\pi^2}{45} \right) g_* T^3$, $g_* = 106.75$
- $\Delta_x = \frac{n_x - n_{\overline{x}}}{s}$, $\Sigma_T = \frac{n_T + n_{\overline{T}}}{s}$, $Y = \frac{n_x}{s}$

Boltzmann equations

$$Y_T^{\text{eq}} = \frac{45g_T}{4\pi^4 g_*} z^2 K_2(z), \quad Y_l^{\text{eq}} = \frac{3}{4} \frac{45\zeta(3)}{2\pi^4 g_*} g_l, \quad Y_\phi^{\text{eq}} = \frac{45\zeta(3)}{2\pi^4 g_*} g_\phi,$$

- $g_T = 1$ for each triplet component, $g_l = 2$ and $g_\phi = 2$
- $\zeta(3) \simeq 1.202$, $K_i(z) =$ modified Bessel function.

$$\gamma_D = s\Gamma_T \Sigma_T^{\text{eq}} \frac{K_1(z)}{K_2(z)},$$

$$\gamma_A = \frac{M_T T^3 e^{-2\frac{M_T}{T}}}{64\pi^4} (9g^4 + 12g^2 g_Y^2 + 3g_Y^4) \left(1 + \frac{3T}{4M_T}\right).$$

$$B_l = \frac{M_T}{8\pi\Gamma_T} \text{Tr}(Y^{T\dagger} Y^T), \quad B_\phi = \frac{M_T}{8\pi\Gamma_T} |\lambda|^2, \quad B_l + B_\phi = 1,$$

Initial values taken for numerical analysis



$$\Sigma_T(z \ll 1) = \Sigma_T^{eq}(z \ll 1)$$



$$\Delta_T(z \ll 1) = 0, \quad \Delta_{I_\alpha}(z \ll 1) = 0, \quad \Delta_\phi(z \ll 1) = 0.$$

Baryon asymmetry calculation

$$c_{sph} = \frac{28}{79}, \quad A = \begin{pmatrix} -\frac{151}{25} & \frac{20}{179} & \frac{20}{14} \\ \frac{358}{25} & -\frac{537}{14} & \frac{537}{344} \\ \frac{358}{25} & \frac{14}{537} & -\frac{344}{537} \end{pmatrix}$$