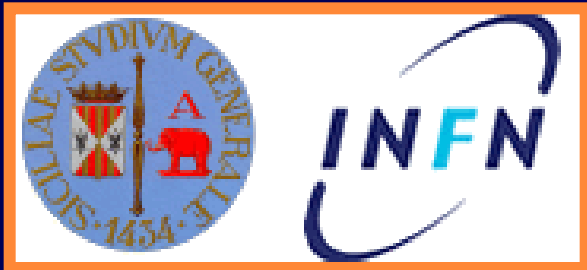


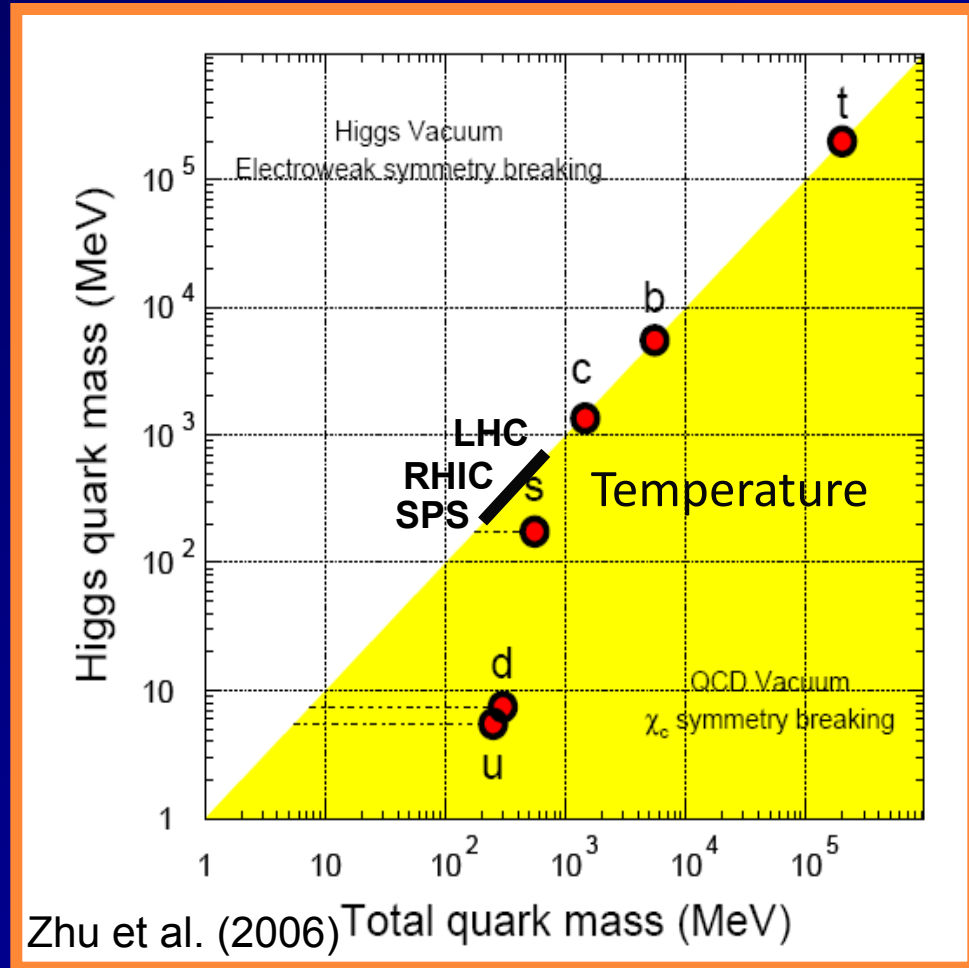
# Heavy Quark and Quarkonia dynamics in the QGP



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**UNIVERSITA DI CATANIA**

**INFN-LNS**



# Specific of Heavy Quarks

## Comparing $m_{HQ}$ to $\Lambda_{QCD}$ and $T$

- $m_{c,b} \gg \Lambda_{QCD}$  produced by pQCD processes (out of equil.)
- $\tau_0 \sim 1/m_{c,b} \ll \tau_{QGP}$  they go through all the QGP lifetime
- $m_{c,b} \gg T_0$  *no thermal production*
- $\tau_{eq} > \tau_{QGP} \gg \tau_{q,g}$  carry more information
- $m \gg T \rightarrow q^2 \ll m^2$  transport reduced to Brownian motion
- $q_0 \ll |\vec{q}|$  Concept of potential  $V(r) \leftrightarrow$  IQCD

# QGP structure in the Heavy Quark sector

---

## Open Heavy Flavor B and D

- ❖ Non perturbative HQ interaction:  $Q\bar{q}$  resonances
  - problematic  $R_{AA} - v_2$  relation for jet quenching (+ elastic)
  - Resonant D-like scattering at  $T > T_c$
- ❖ Relevance of Hadronization mechanism for HQ

## Quarkonia

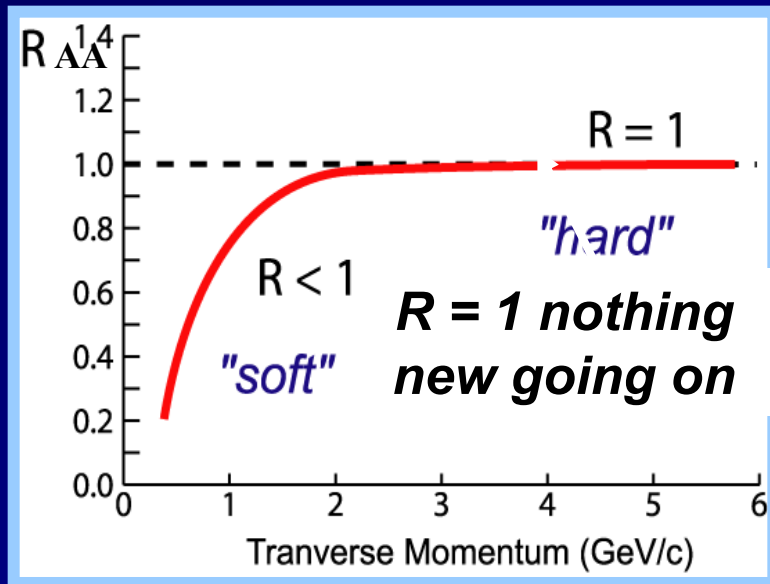
- ❖ Link  $J/\Psi \leftrightarrow D$  with a dominance of regeneration
  - one underlying  $c$  distribution

# Two Main Observables in HIC

## ❖ Nuclear Modification factor

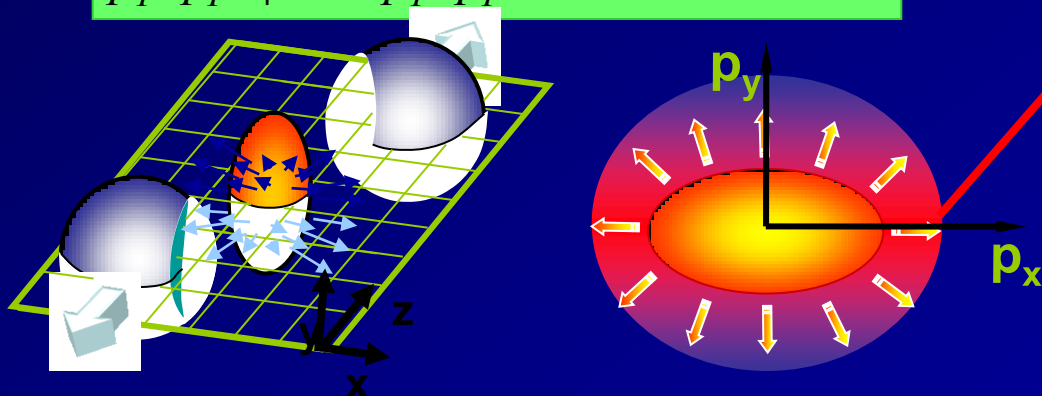
$$R_{AA}(p_T) = \frac{d^2 N^{AA} / dp_T d\eta}{N_{coll} d^2 N^{NN} / dp_T d\eta}$$

- Modification respect to pp
- Decrease with increasing partonic interaction

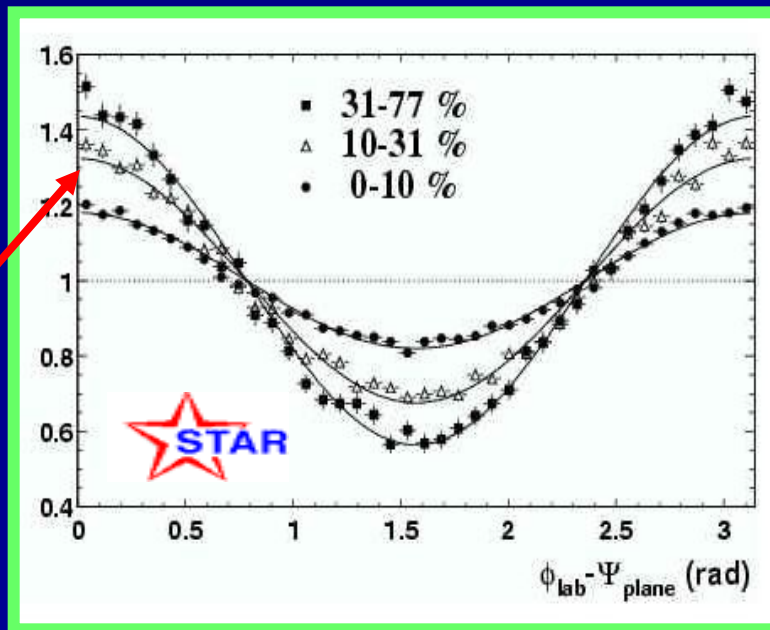


## ❖ Anisotropy p-space: Elliptic Flow $v_2$

$$\frac{dN}{p_T dp_T d\phi} = \frac{dN}{2\pi p_T dp_T} [1 + 2v_2 \cos(2\phi) + \dots]$$



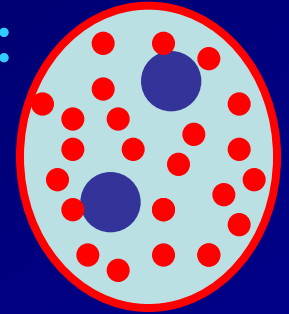
Increases with interaction!



# Ideas about Heavy Quarks before RHIC

1)  $m_Q \gg m_q$  HQ not dragged by the expanding medium:

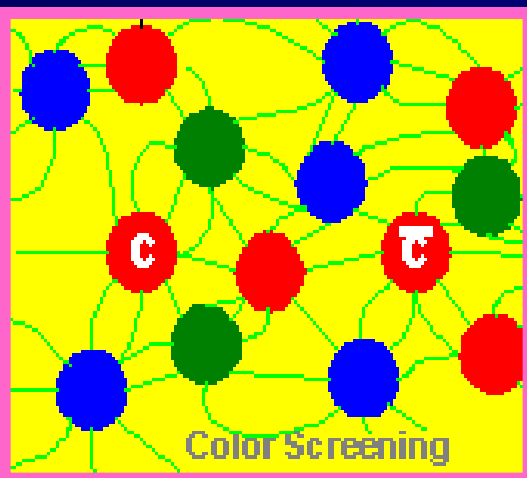
- spectra close to the pp one
- small elliptic flow  $v_2$



2)  $m_Q \gg \Lambda_{\text{QCD}}$  provide a better test of jet quenching:

- Color dependence:  $R_{AA}(D/h)$
- Mass dependence:  $R_{AA}(B/D/h)$

3)  $\bar{Q}Q$  Quarkonium dissolved by charge screening: Thermometer

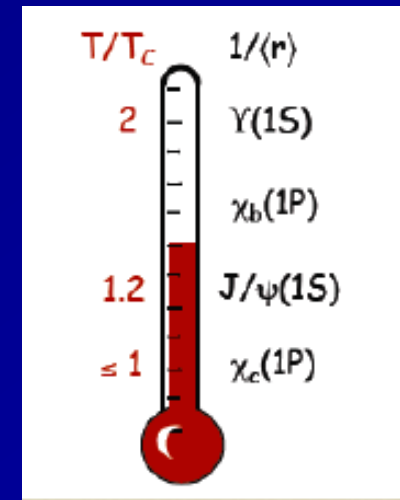


$$V \approx -\alpha_{\text{eff}} \frac{e^{-m_D r}}{r}$$

$$r_{Q\bar{Q}} \approx \frac{1}{m_D} \approx \frac{1}{gT}$$

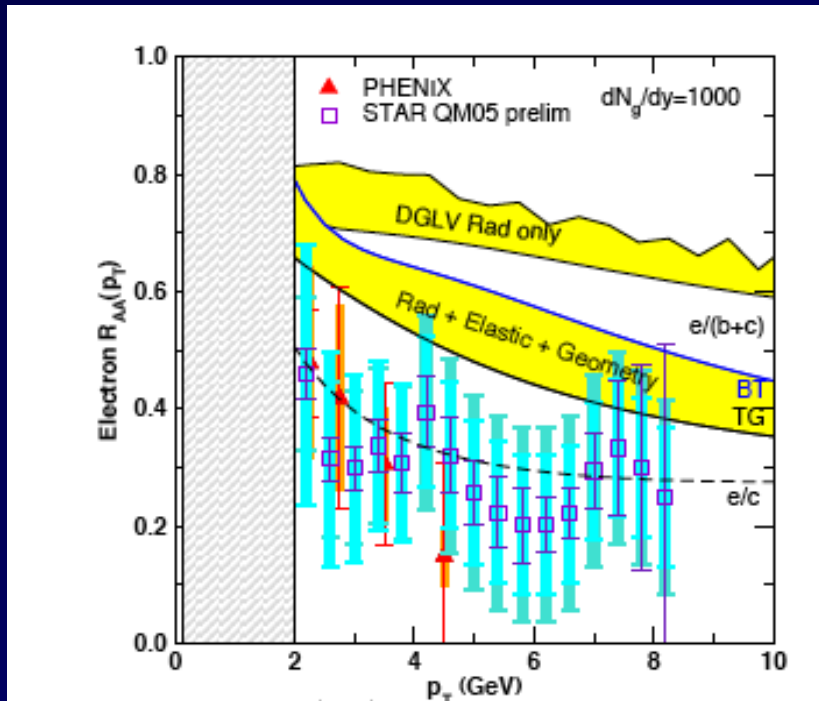
$\chi_c, J/\Psi, \chi_b, Y, \dots$

More binding smaller radius  
higher temperature



# Problems with ideas 1 & 2

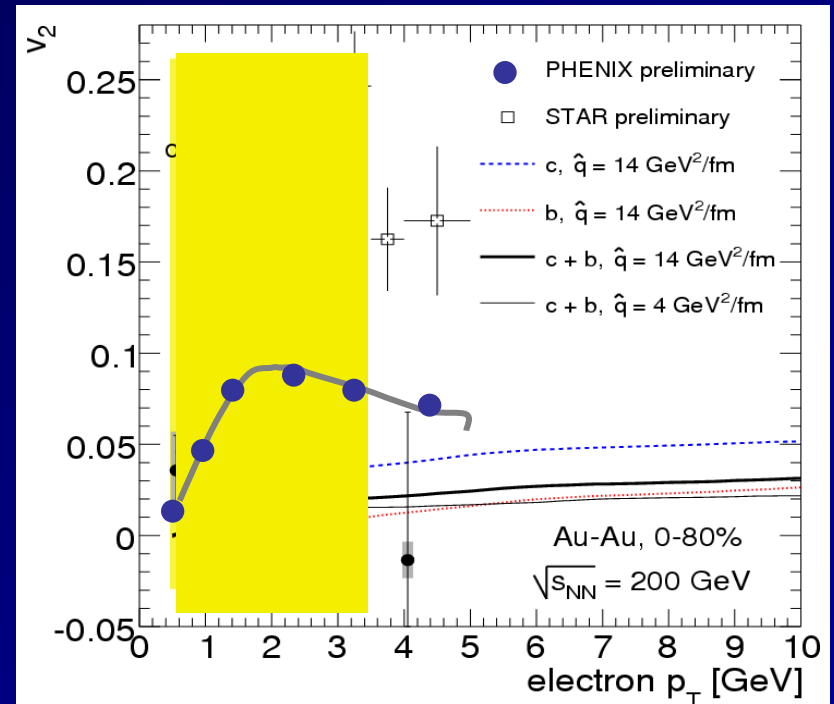
## Strong suppression



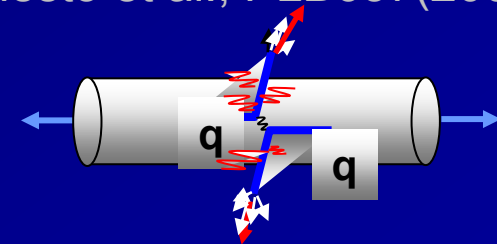
S. Wicks et al. (QM06)

- Radiative energy loss not sufficient
- Charm seems to flow like light quarks

## Large elliptic Flow



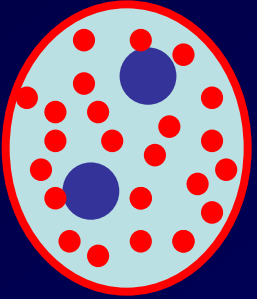
N. Armesto et al., PLB637(2006)362



Heavy Quark strongly dragged by interaction with light quarks

pQCD does not work may be the real cross section is a K factor larger

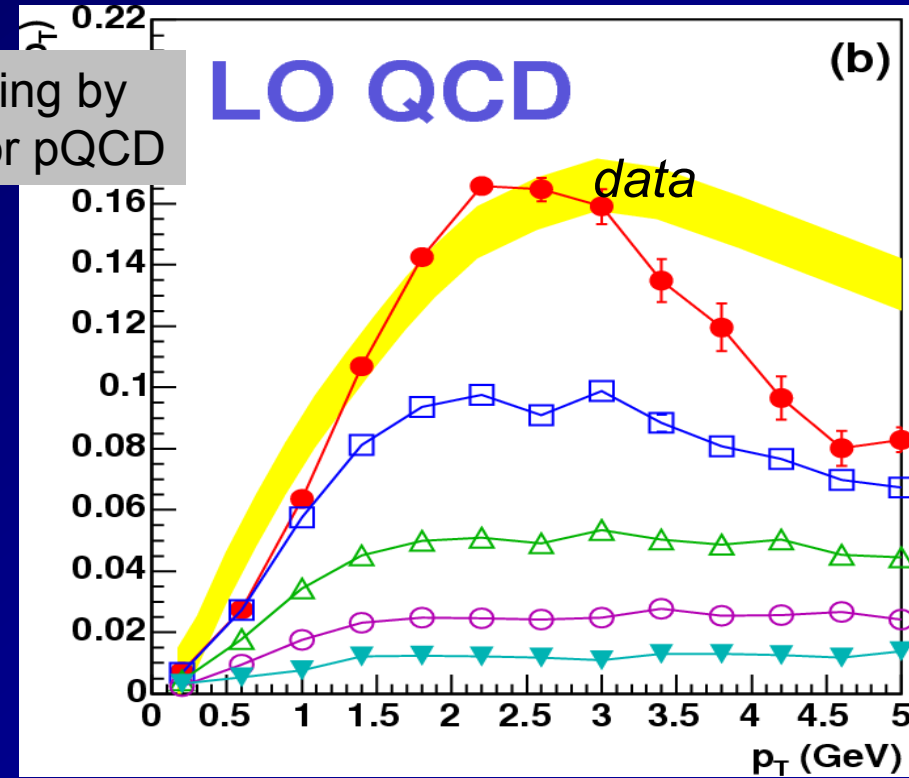
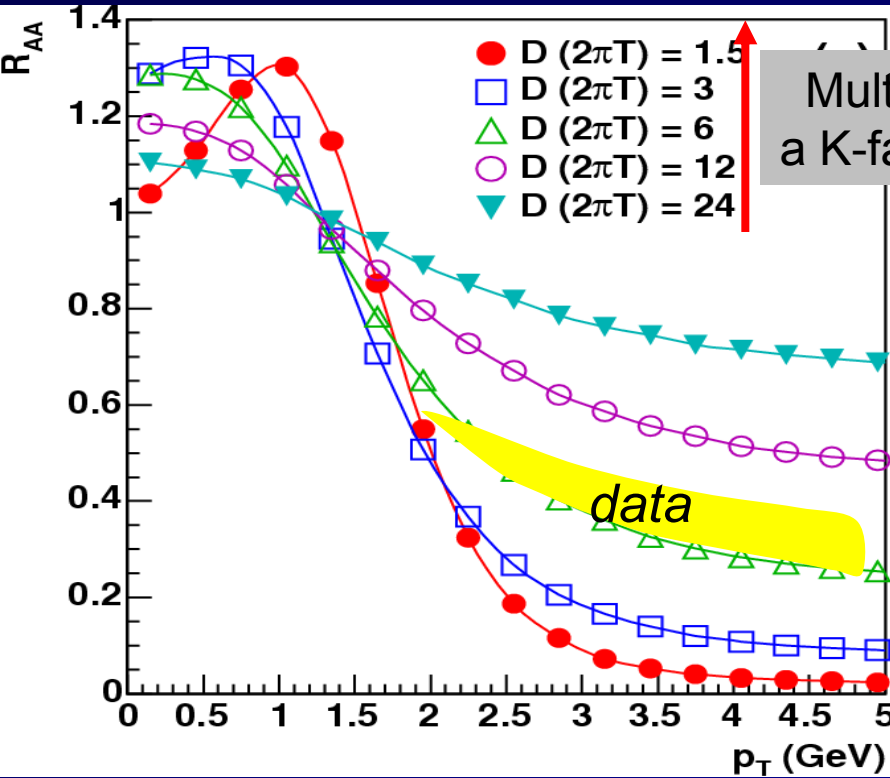
# Charm dynamics with upscaled pQCD cross section



Fokker-Plank for charm interaction in a hydro bulk

Diffusion coefficient

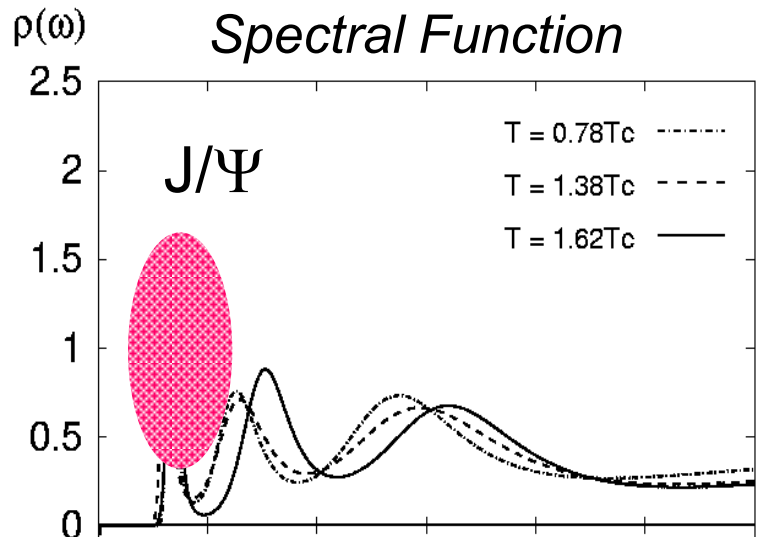
$$D \propto \int d^3k |M_{g(q)c}(k, p)|^2 k^2$$



Moore & Teaney, PRC71 (2005)

It's not just a matter of pumping up pQCD cross section:  
too low  $R_{AA}$  or too low  $v_2$

# Indications from IQCD



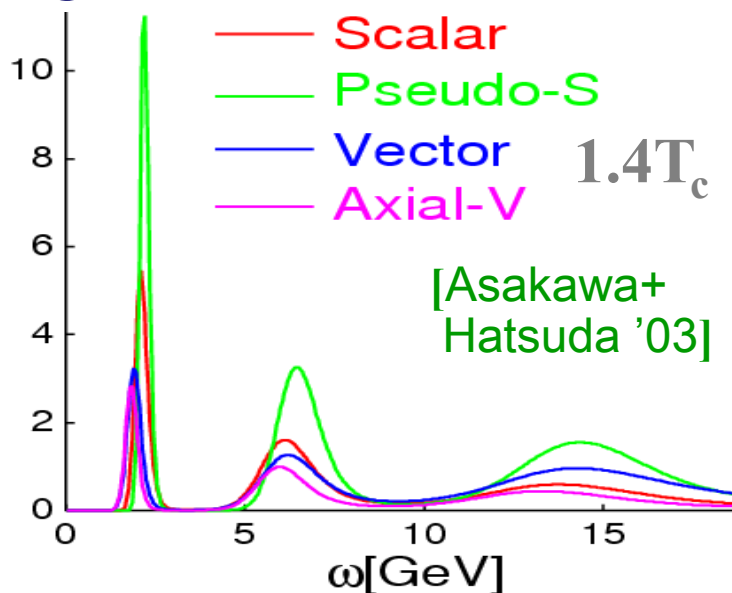
$J/\psi$  ( $\mathbf{p} = \mathbf{0}$ ) disappears around  $1.7 T_c$

We do not know what is behind  $\rho(\omega)$ :  
*bound states, resonances, ...*

$c\bar{q}, \bar{c}q$  does not undergo a free scattering, but there are remnants of confinement!?

Look at the scattering under a  $V(r)$  derived from IQCD

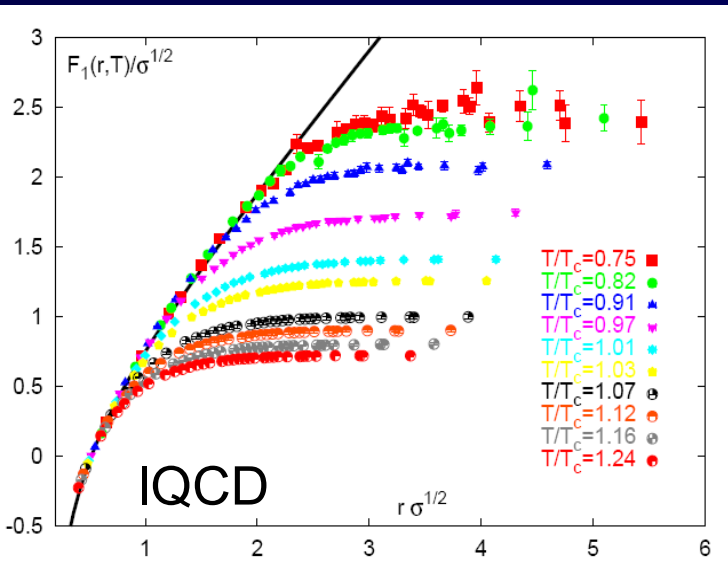
## “Light”-Quark Resonances



There can be  $Q\bar{q}$  (D-like) resonant scattering!?



# $V_{\text{IQCD}}$ gives resonance states!



Kaczmarek et al., PPS 129,560(2004)

$$U_1 = F_1 - T \frac{dF_1}{dT}$$

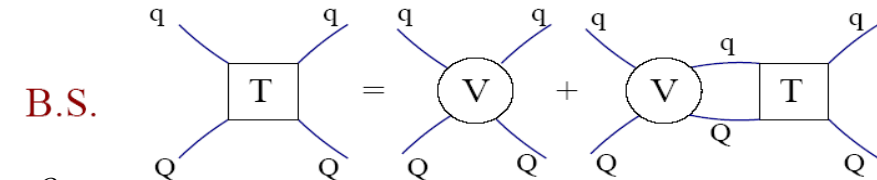
$$V_1(r, T) = U_1(r, T) - U_1(\infty, T)$$

Scattering states included:

Singlet + Octet -triplet -sextet

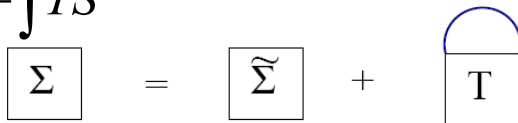
“Im T” dominated by meson and diquark channel

$$T = V + \int VGT$$



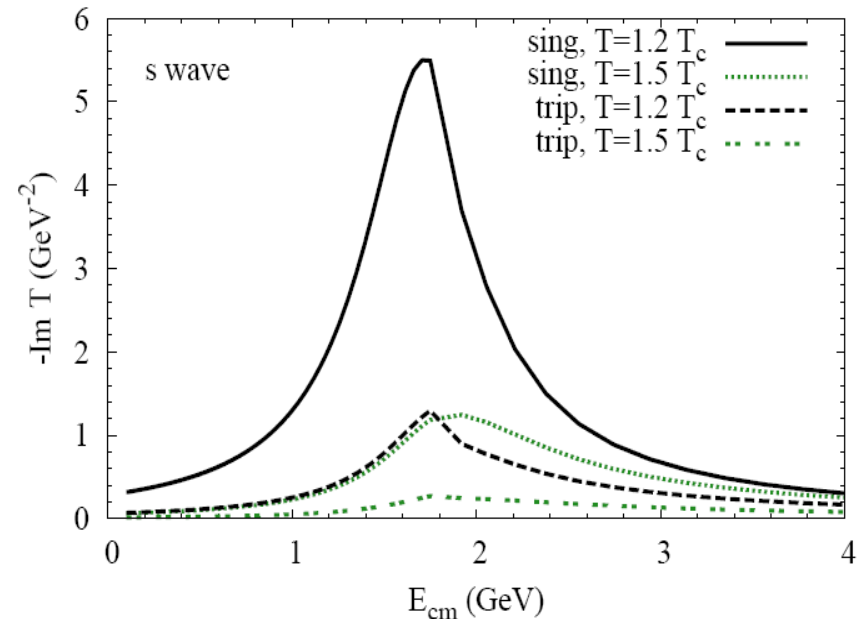
$$\Sigma^Q = \Sigma_g^Q + \int TS^Q$$

"Link"



$$S^Q = S_0^Q + S^Q \Sigma^Q S^Q$$

S.D.

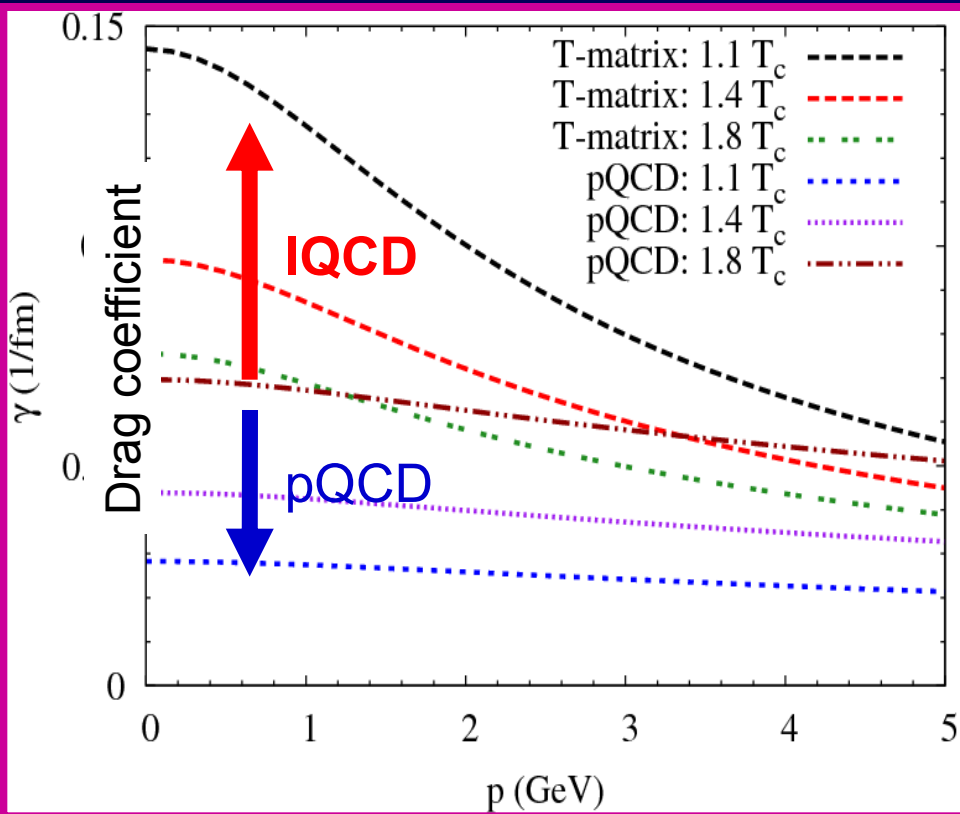


# Drag Coefficient from IQCD-V(r)

Opposite T-dependence of  $\gamma$   
not a K-factor difference

$$\gamma p = \int d^3k |M(k, p)|^2 p$$

Drag coefficient  
 $\gamma = D/mT$



With IQCD- V(r):

→ one can expect more  $V_2$  with the same  $R_{AA}$  because there is a strong interaction just when  $v_2$  is formed.

ImT increase with temperature  
compensates  
for decreasing scatterer density

Does it solve the problem of  
“too low  $R_{AA}$  or too low  $v_2$ ” ?

# The modeling

c,b quarks



## HQ scattering in QGP

$$\frac{\partial f_{c,b}}{\partial t} = \gamma \frac{\partial (p f_{c,b})}{\partial p} + D \frac{\partial^2 f_{c,b}}{\partial p^2}$$

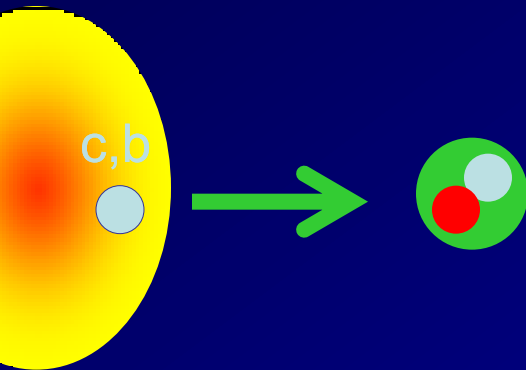
$T \ll m_Q$

From  
scattering  
matrix  $|M|^2$

$$\gamma p = \int d^3 k |M(k, p)|^2 p$$

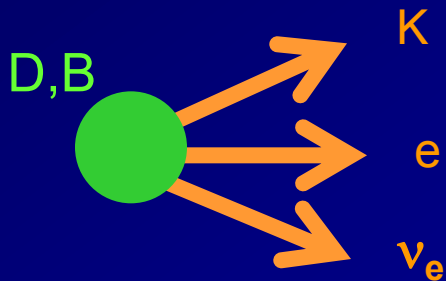
$$D = \frac{1}{2} \int d^3 k |M(k, p)|^2 p^2$$

- Elastic pQCD
- **T-matrix V(r)-IQCD**



## Hadronization

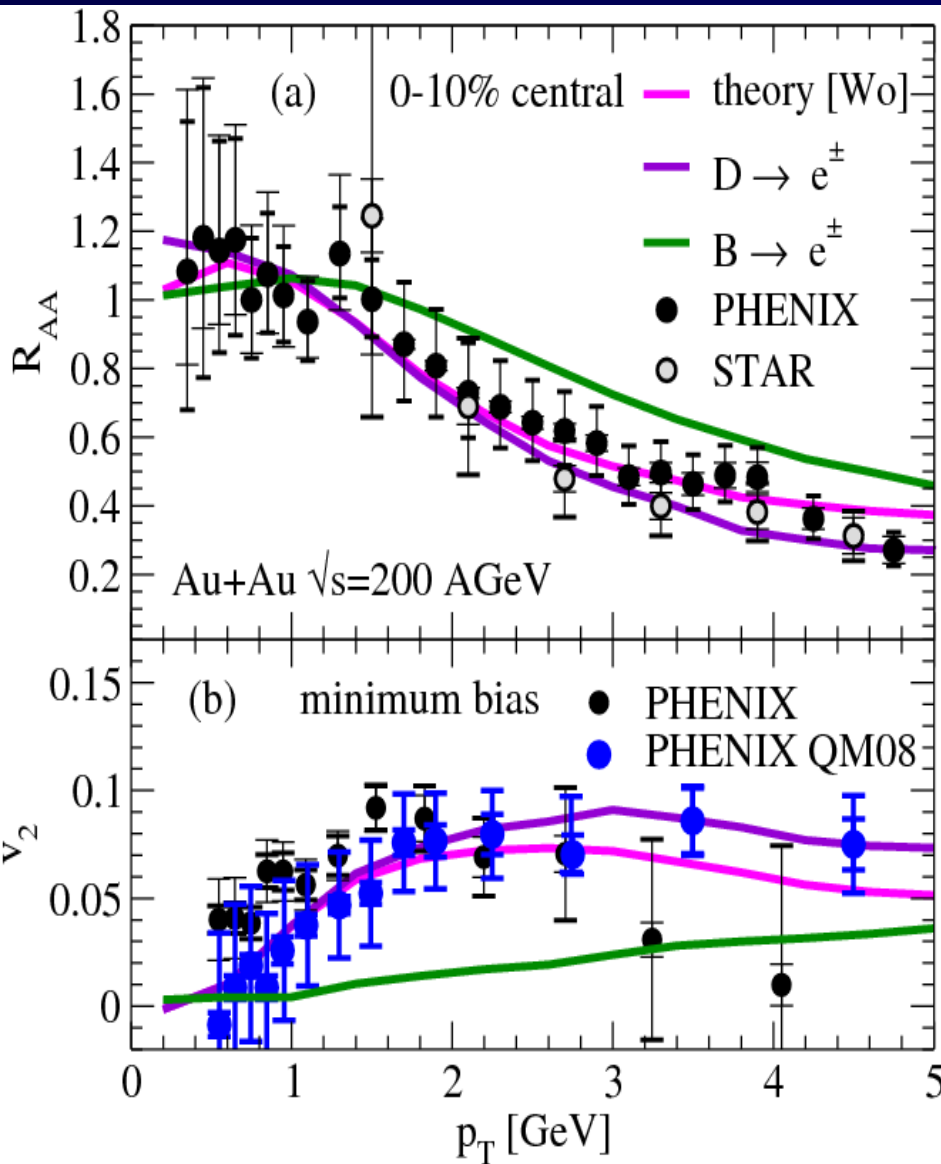
$$\frac{d^3 N_{D,B}}{d^3 P} = C_{D,B} \int_{\Sigma} f_{c,b} \otimes f_{\bar{q}} \otimes \Phi_M + \int_{\Sigma} f_{c,b} \otimes D_{c,b \rightarrow D,B}$$



## Semileptonic decay

$R_{AA}$  &  $v_2$  of “non-photonic” e  
(with B contamination ☹)

# T-matrix calculation vs PHENIX data



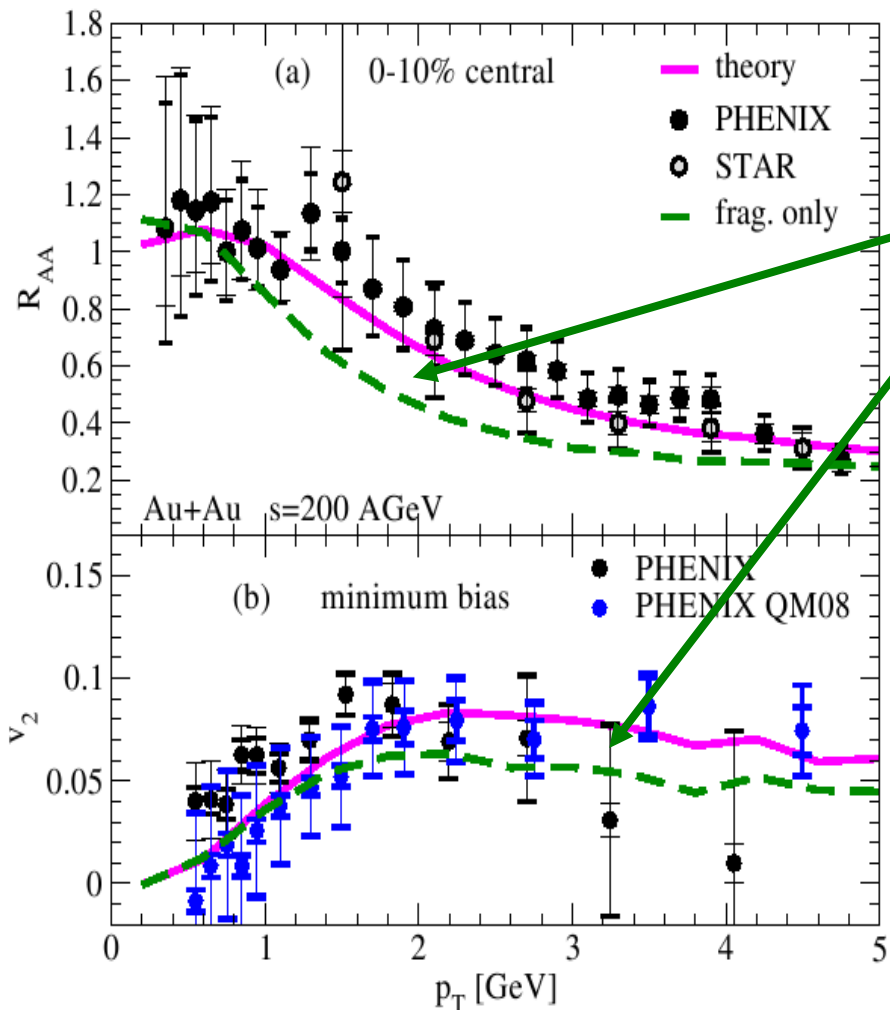
One can get both  $R_{AA}$  and  $v_2$  with no free tunable parameters:

Essential at LHC the possibility to disentangle B and D

Uncertainties:

- parametrization of  $V(r)$
- extraction of  $V(r)$  (U vs F)

# Impact of hadronization mechanism



Impact of hadronization

Coalescence increase

both  $R_{AA}$  and  $v_2$

toward agreement with data

• resonant states naturally merging into a coalescence mechanism

Hees-Mannarelli-Greco-Rapp, PRL100 (2008)

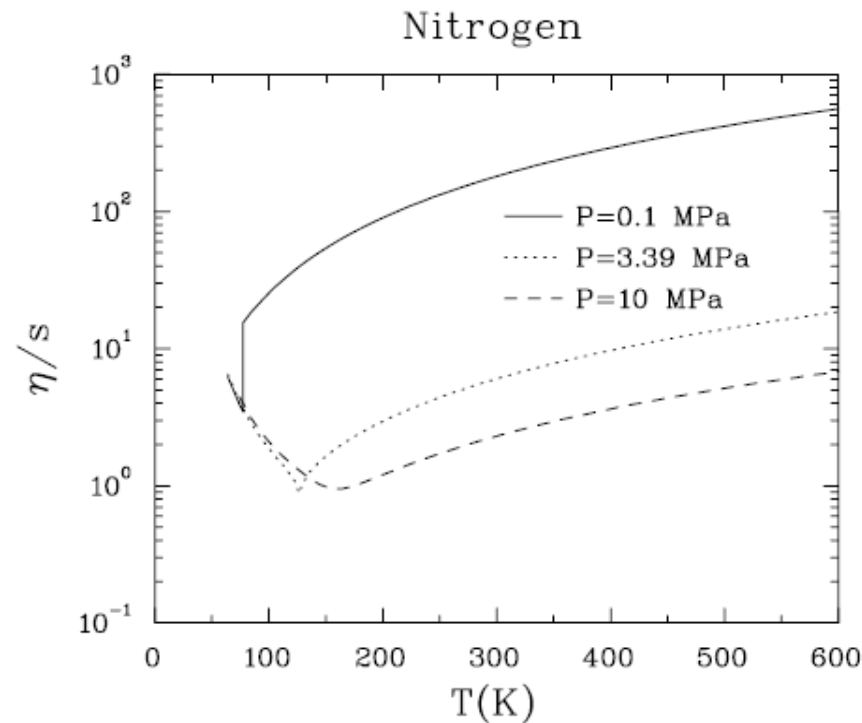
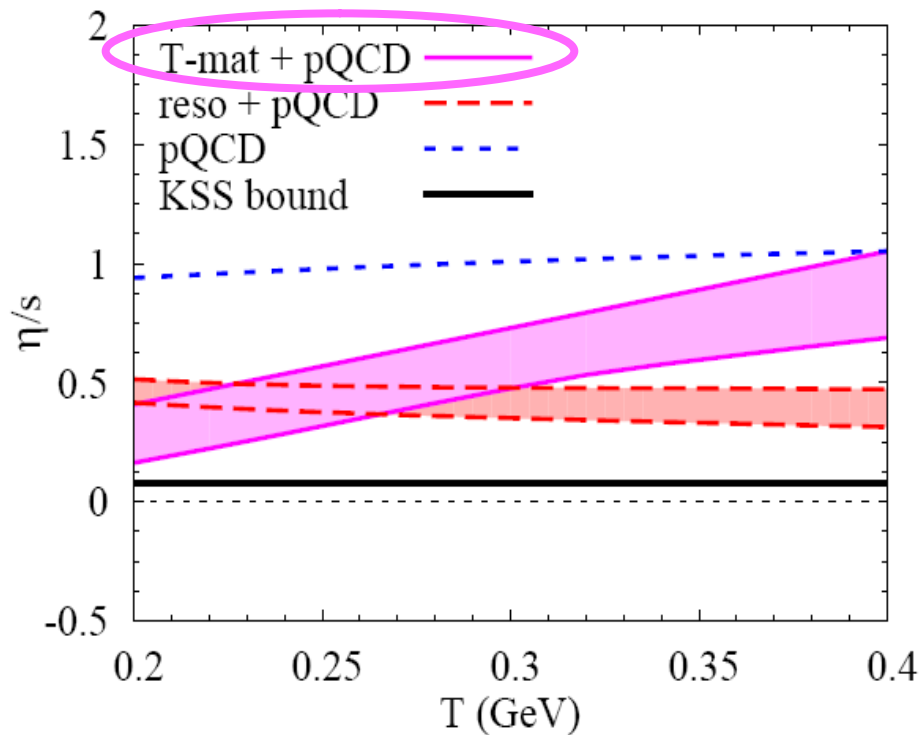
$$\frac{d^3 N_{D,B}}{d^3 P} = C_{D,B} \int_{\Sigma} f_{c,b} \otimes f_{\bar{q}} \otimes \Phi_M + \int_{\Sigma} f_{c,b} \otimes D_{c,b \rightarrow D,B}$$

add quark momenta

$f_q$  from  $\pi, K$   
Greco,Ko,Levai - PRL90



# From the point of view of the shear viscosity



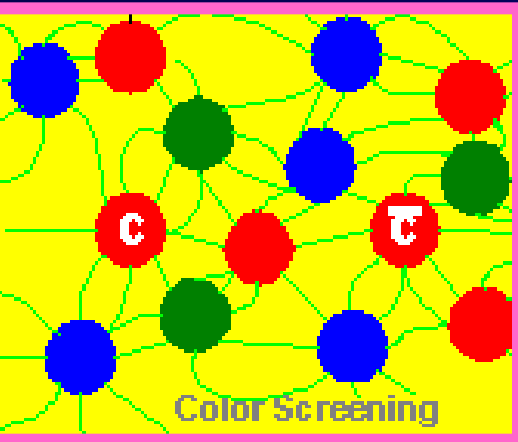
Csernai et al., PRL96(06)

HQ are more sensitive to the details of dynamics ( $t_{eq} \sim t_{QGP}$ )

It is necessary an interaction that increases as  $T \rightarrow T_c$ ,

i.e. when we approach the phase transition

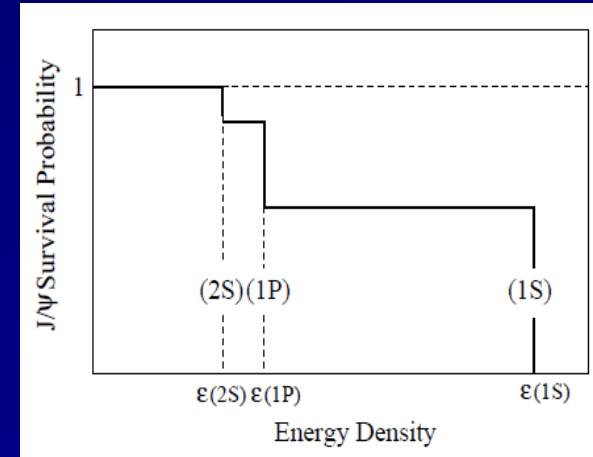
# The long standing issue of Quarkonia Suppression



$$r_{\Psi} \approx \frac{1}{m_D} \approx \frac{1}{gT}$$

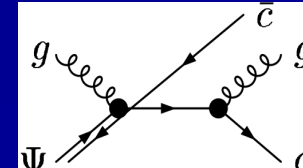
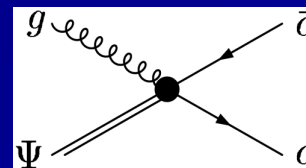
$$\Psi = \chi_c, J/\Psi, \chi_b, Y, \dots$$

More Quarkonia dissolved  
with increasing energy density!?



The Quarkonium Yield involves (problems with ideas 3):

- $T_{\text{diss}}(\Psi)$  destruction and absence of formation at  $T > T_{\text{diss}}$
- $\Gamma_{\text{inel}}(\Psi)$  formation and destruction ( $g\Psi \rightarrow c\bar{c}$ ,  $g\Psi \rightarrow c\bar{c}g$ )



# Dynamics of Quarkonia in the QGP

- Boltzmann-like transport or
- Include in-medium effects in  $\Gamma_\Psi$ ,  $\beta_\Psi$  which depend on  $\sigma^*$ ,  $\varepsilon_{\text{bind}}(T)$ ,  $m^*$

$$p^\mu \partial_\mu f_\Psi(\vec{r}, t; \vec{p}) = -\omega_p \Gamma_\Psi(\vec{r}, t; \vec{p}) f_\Psi(\vec{r}, t; \vec{p}) + \omega_p \beta_\Psi(\vec{r}, t; \vec{p})$$

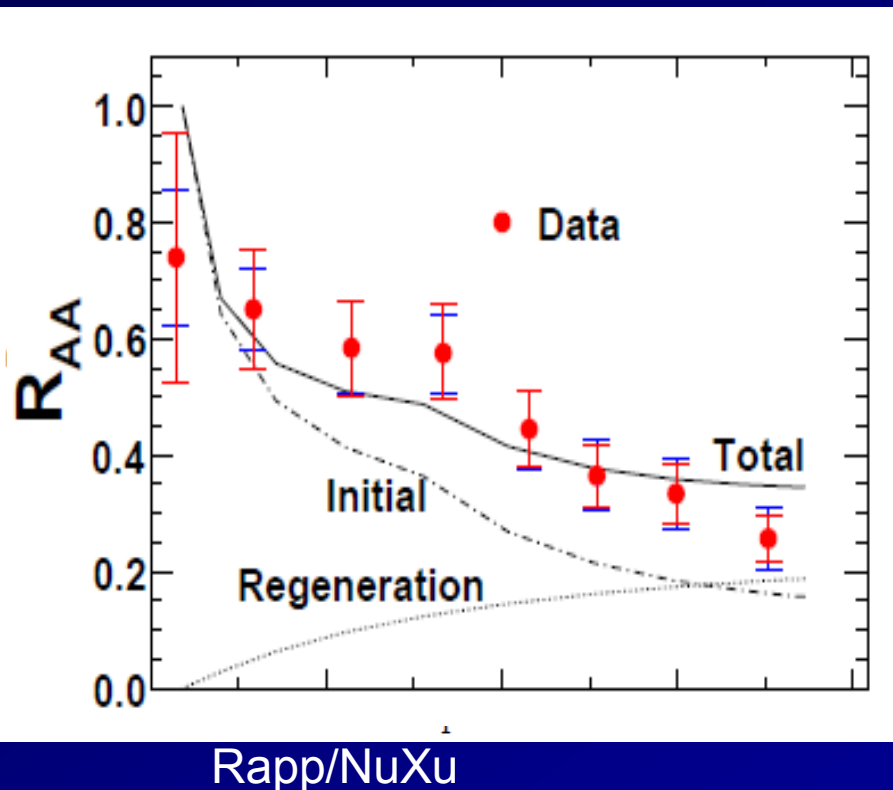
dissociation                      regeneration

Rate equations:

$$\frac{dN_\Psi}{d\tau} = -\Gamma_\Psi (N_\Psi - RN_\Psi^{\text{eq}})$$

Non-equilibrium effect

$$R = 1 - \exp\left(-\int d\tau / \tau_{eq}(T)\right)$$



At SPS the  $R_{AA}$  suppression is explained  
 No beauty regeneration  $\sim N_c^2$

$$dN_{c\bar{c}} / dy \approx 0.1 \quad (\text{SPS})$$

$$dN_{c\bar{c}} / dy \approx 2.5 \quad (\text{RHIC})$$

At RHIC models with no regeneration  
 predicted too much suppression...  
except the simple ones  
saying  $J/\Psi$  survives up  $T \sim 2T_c$



# Two opposite scenarios & all the intermediate ones

Trying to synthesize about 100 papers ... in 1 slide

## 1) STRONG BINDING:

$T_{\text{diss}} \sim 2T_c$  negligible suppression of  $J/\Psi$

*SPS & RHIC Similar because of the absence of  $\chi_c$ ,  $\Psi'$  feeddown*

## 2) WEAK BINDING:

$T_{\text{diss}} \sim T_c$  strong suppression increasing with energy

*SPS & RHIC similar because at RHIC*

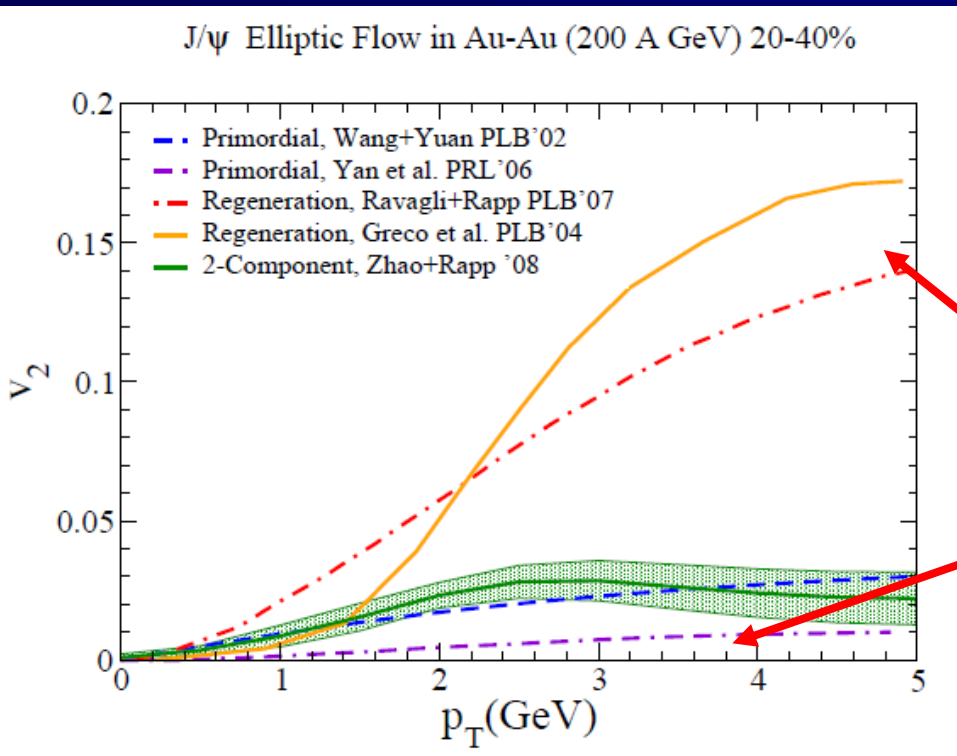
*the regeneration compensates (it was a prediction)*

Partially possible also due to the uncertainty in the charm yield

**The way out is to look at Open Heavy Flavor  
to see Hidden Heavy Flavor**

# Quarkonium $\leftrightarrow$ Heavy-Quark

- ❖ We can go beyond the  $J/\Psi$  yield and thanks to the strong charm collective dynamics distinguish primordial from  $\bar{c}c$  coalescence:
  - softer  $p_T$  spectra of  $J/\Psi \leftrightarrow dN/dp_T$  of D
  - Large elliptic flow  $v_2(\Psi) \leftrightarrow v_2(D)$



**$v_{2\Psi}$  ALLOWS TO ESTIMATE**

$$\frac{N_{\text{COAL}}}{N_{\text{PRIM}}}$$

**FROM THE KNOWLEDGE OF  $v_{2D}$**

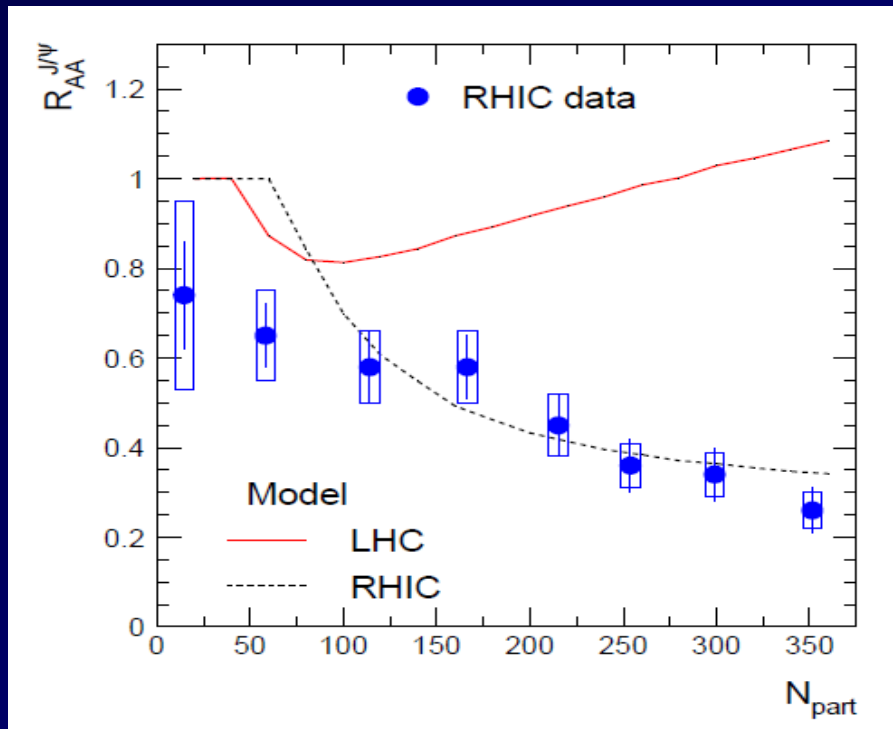
100% regeneration through  $v_{2c}(p_T)$   
inferred from D spectrum

100% primordial J/ $\Psi$

At LHC the regeneration component  
should dominate

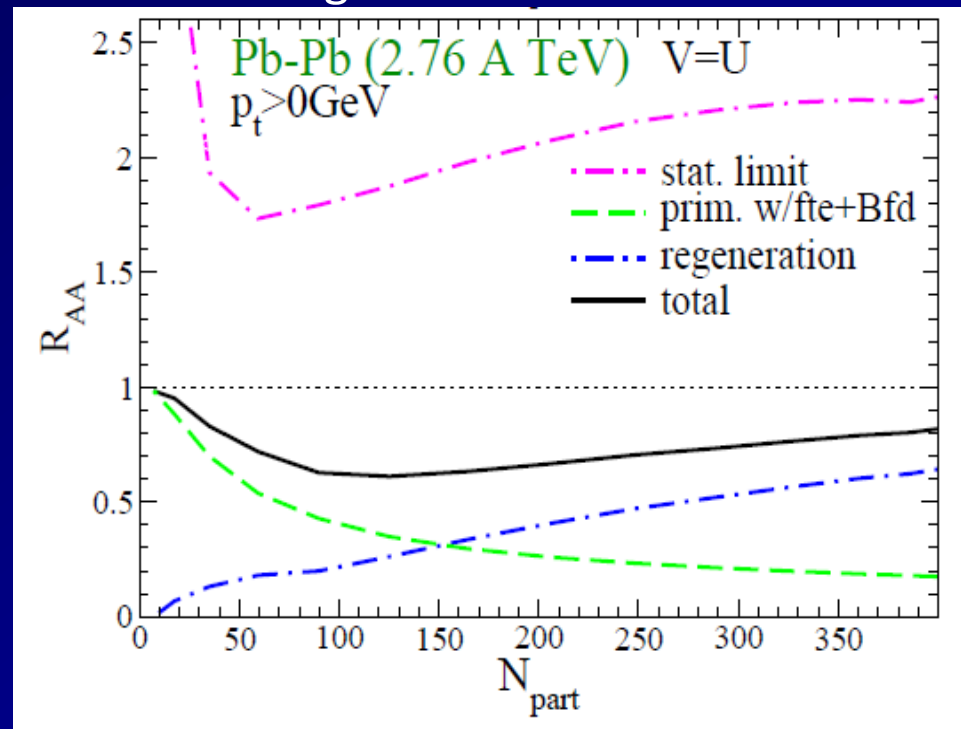
# Enhancement of $J/\Psi$ at LHC!?

Pure statistical model at  $T_c$   
+ corona effect



A. Andronic, P. B-M., et al., NPA 789 (2007)

Including both suppression and regeneration  
during all the evolution



Rapp R., X. Zhao, arXiv:1102.2194[hep-ph]

$$dN_{c\bar{c}} / dy \approx 0.1 \quad (SPS)$$

$$dN_{c\bar{c}} / dy \approx 2.5 \quad (RHIC)$$

$$dN_{c\bar{c}} / dy \approx 15-20 \quad (LHC)$$

$$N_{J/\psi} \propto N_{c\bar{c}}^2$$

# Summary

Open Flavor

- ❖ Heavy quarks entails npQCD dynamics:
  - meson-like and diquark resonant scattering in QGP
  - solves the problematic  $R_{AA} - v_2$  correlation
  - associated to a  $\eta/s(T)$  typical of phase transitions
  - need to disentangle B and D

$$dN_c / dp_T$$

$$v_{2c}(p_T)$$

- ❖ Relevance of hadronization via coalescence
  - resonant scattering is a precursor

- ❖ A new era for the understanding of c quarkonia
  - $dN/dp_T$  &  $v_2(p_T)$  for both *open* and *hidden* HF can be linked to one underlying c distribution

Hidden



# Signatures of a coalescence component!?

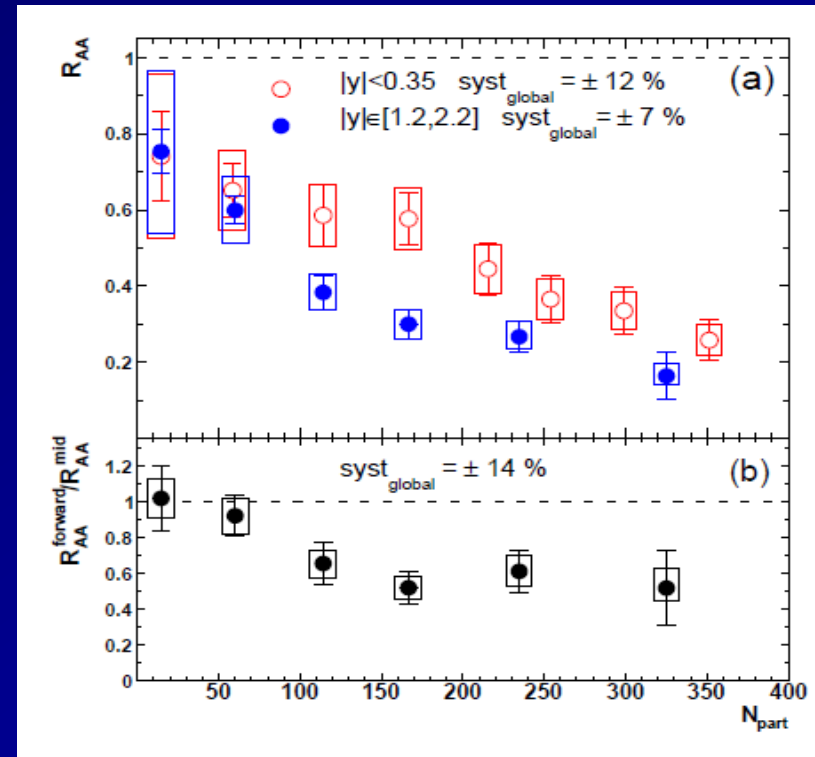
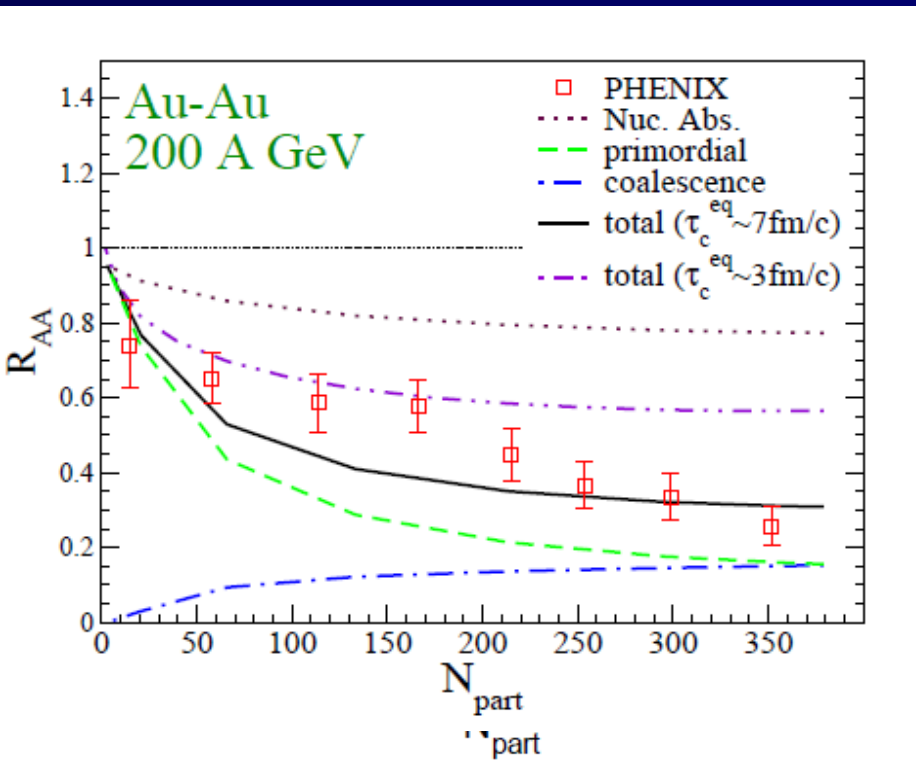
At SPS observed a suppression of about a factor 2

$$N_{c\bar{c}} \approx 0.17 \quad (\text{SPS})$$

$$N_{c\bar{c}} \approx 10-20 \quad (\text{RHIC})$$

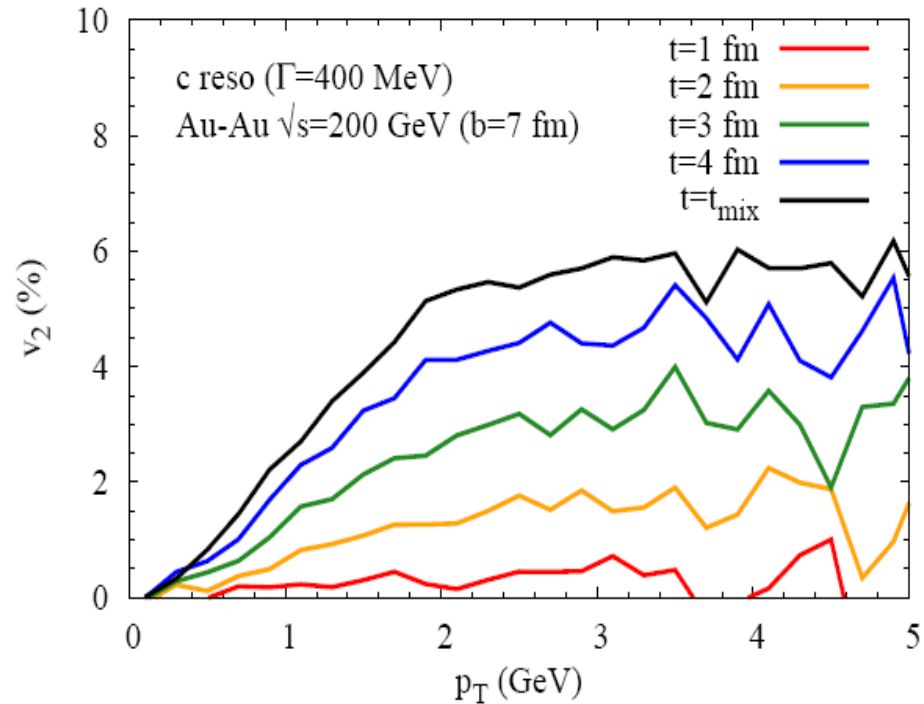
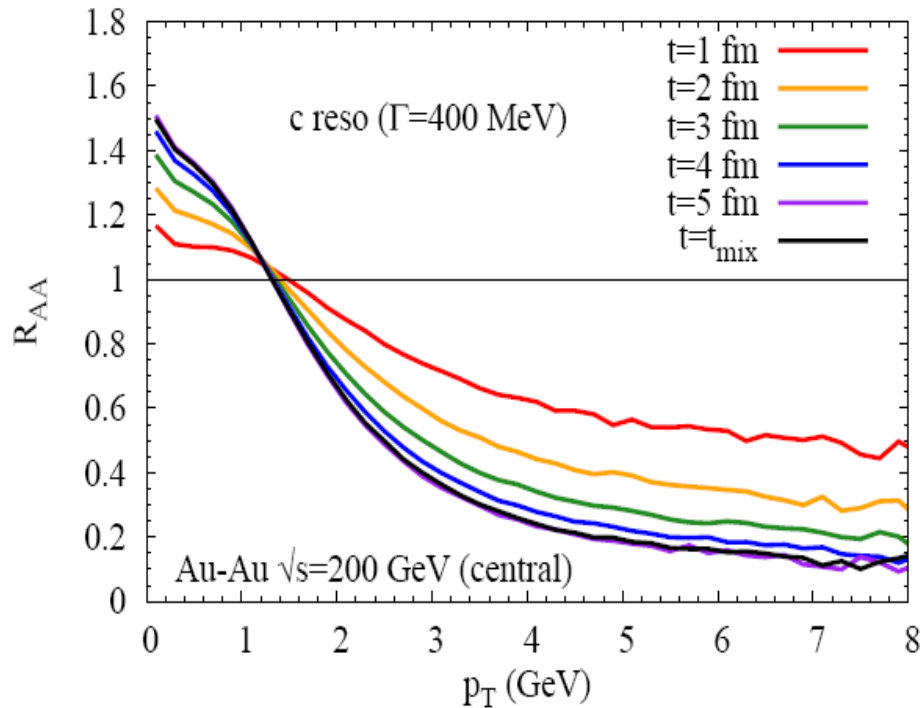
$$N_{c\bar{c}} \approx \quad (\text{LHC})$$

$J/\psi$  can come not from the initially produced  
Not suppressed but from the abundant charm  
can recombine



Less suppression at midrapidity!  
Because of more regeneration

# $R_{AA}$ and $v_2$ generation with time



RAA generated earlier than  $v_2$   
 $v_2$  grows almost linearly

# From RHIC to LHC?

For min. bias.

Hydro bulk  $dN/dy=1100$  ( $dN/dy=2200$  for central)

$T_{\text{init}} = 3 T_c$

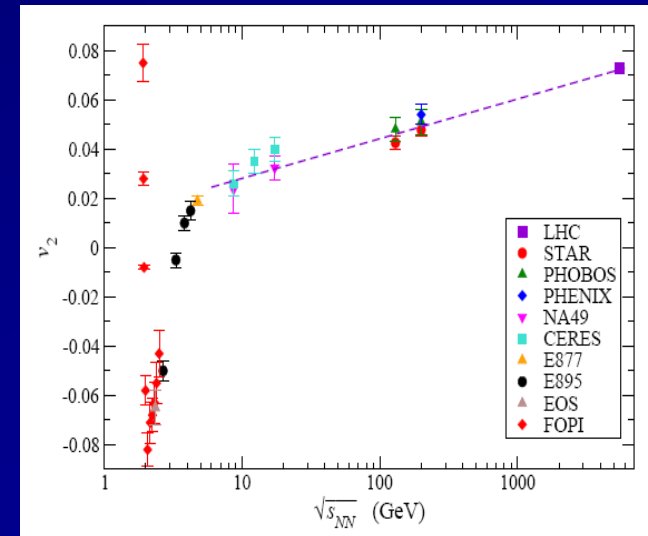
Radial flow  $\beta_{\text{max}}=0.68$

$v_{2q}$  light quark = 7.5 % (hydro or numerology)

$v_{2q}(p_T)$  from a cascade [ Ferini, Colonna, Di Toro, VG]

$dN/d^2p_T$  of b,c from PYTHIA (ALICE PPR-JPG32)

Resonances off  $T > 2T_c$



Borghini-Wiedemann, JPG3508)

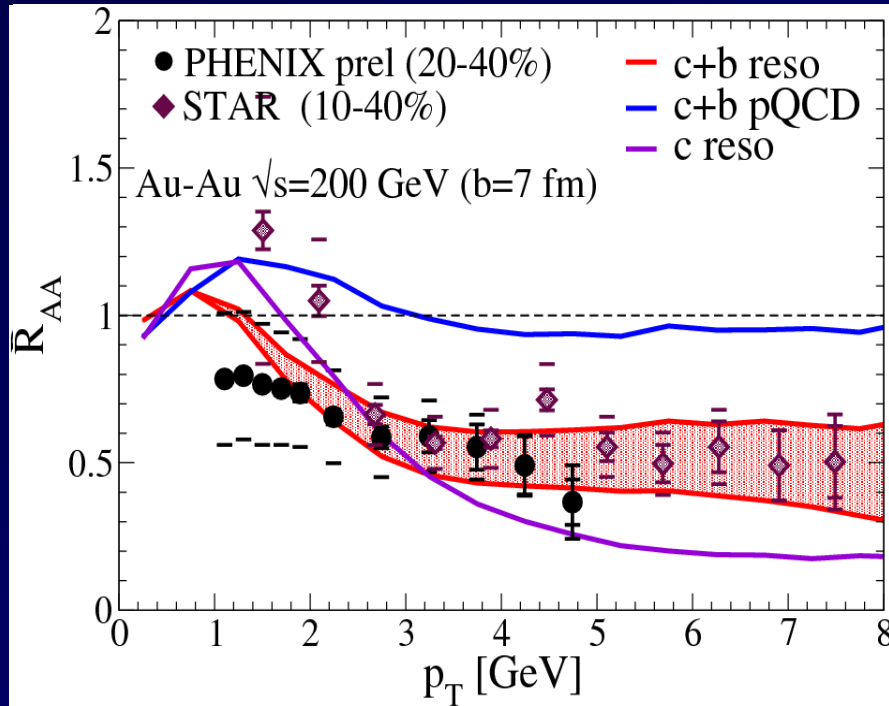
Calculation not done with IQCD, but

$$\mathcal{L}_{Dc\bar{q}} = G_D \bar{q} \frac{(1+\psi)}{2} \Gamma \phi_D c + \text{h.c.}$$

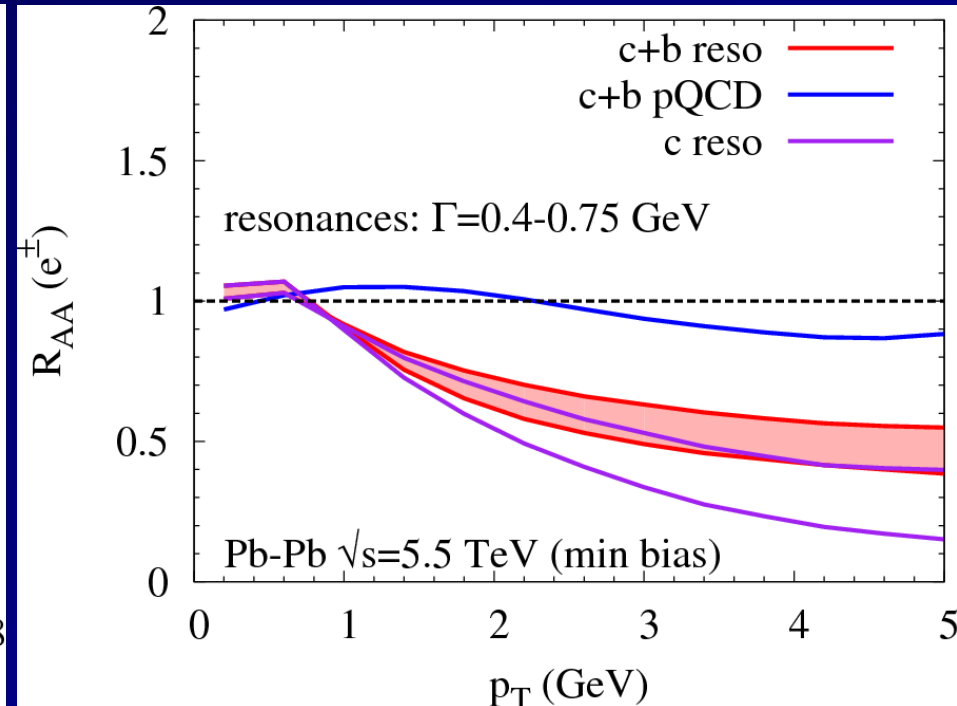


# From RHIC to LHC - $R_{AA}$

RHIC



LHC



❖ **Suppression:  $R_{AA}$  similar at RHIC and LHC!**

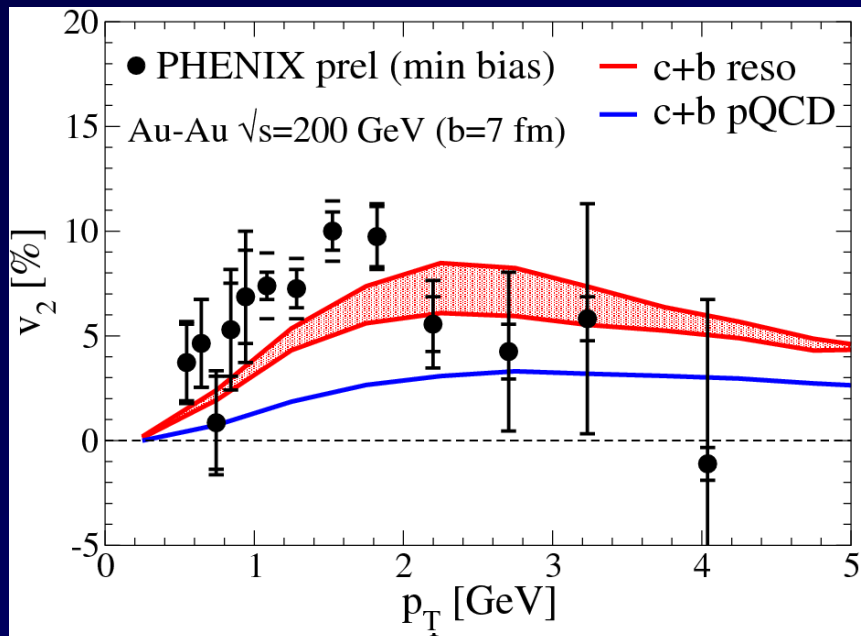
➤ Harder initial spectra at LHC

➤ Resonance ineffective ("melted"  $T > 2T_c$ ) at early stage!

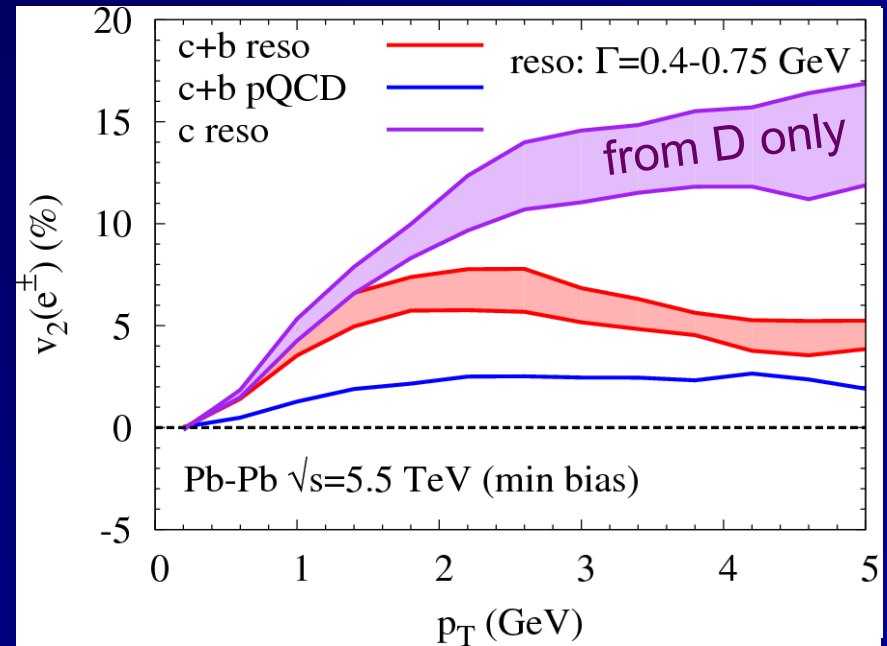
❖ **For 3-body scattering opposite behavior !**

# From RHIC to LHC – $v_2$ electrons

## RHIC



## LHC



❖  $v_2$  similar at RHIC and LHC!

- Resonance effective when anisotropy is reduced
- Strong drag with the bulk flow at later stage!
- $v_2$  slightly higher at low  $p_t$

❖ For 3-body scattering opposite behavior !

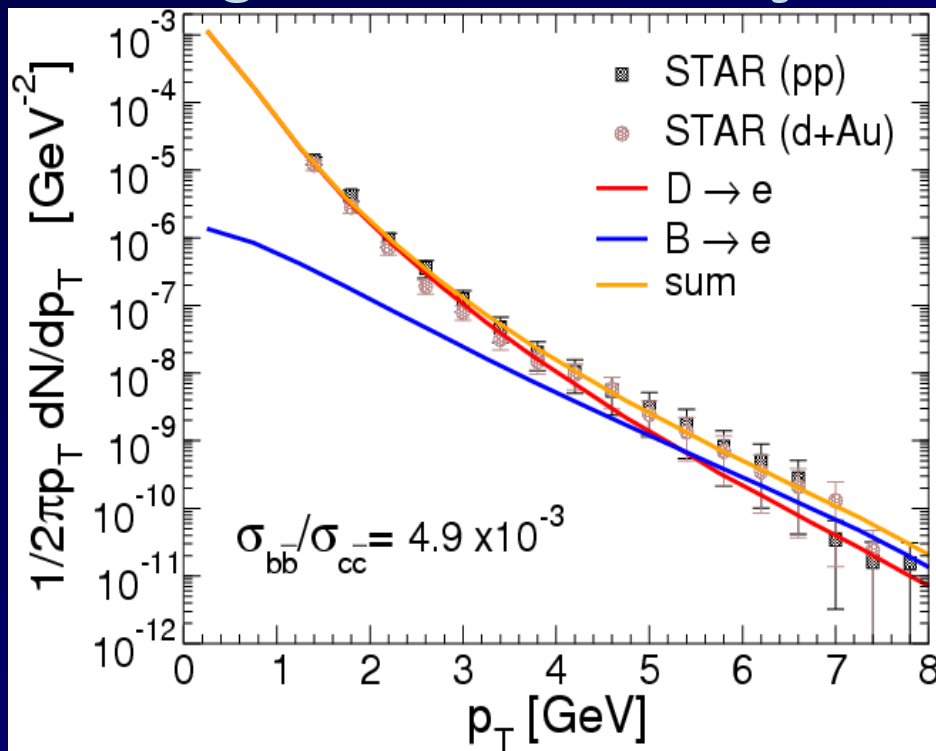
# What is measured till now is the single e

$$D \rightarrow Kl\nu_l$$

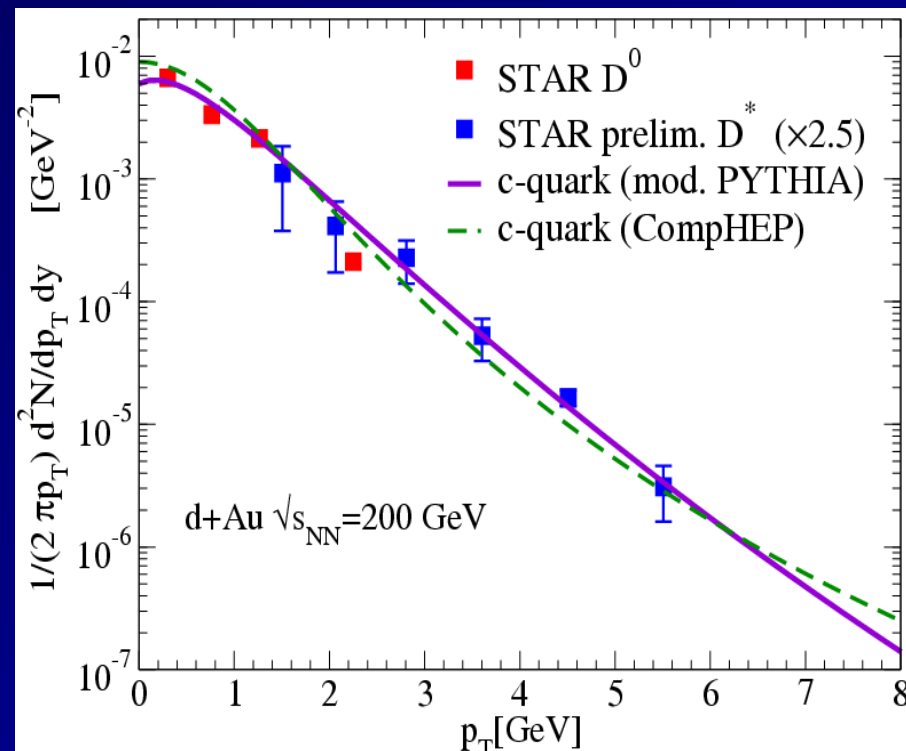
$$B \rightarrow Dl\nu_l$$

the lepton can be reconstructed

## Single-Electron Decays



## D-Mesons



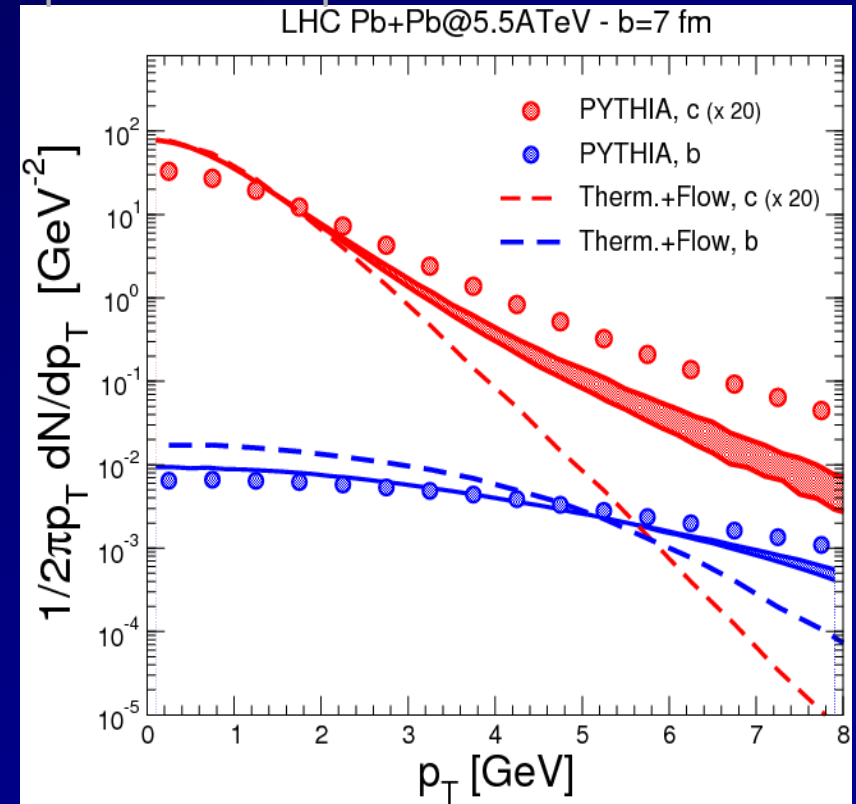
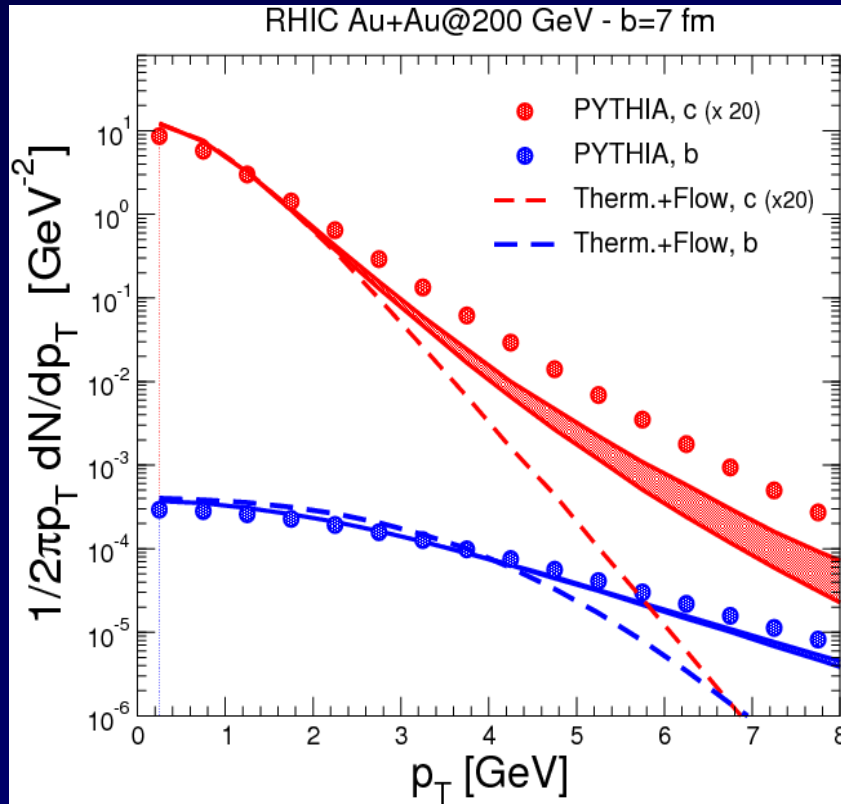
- bottom crossing at 5GeV !?
- strategy: fix charm with D-mesons, adjust bottom in  $e^\pm$ -spectra

b/c similar to pQCD Cacciari, Nason, Vogt, PRL95(2005)

# Charm Thermalization

Shadowing not included yet!

Spectra same parameter of PPR-ALICE



❖ LHC spectra considerably harder !

➤ At  $T_c$  charm nearly thermalized

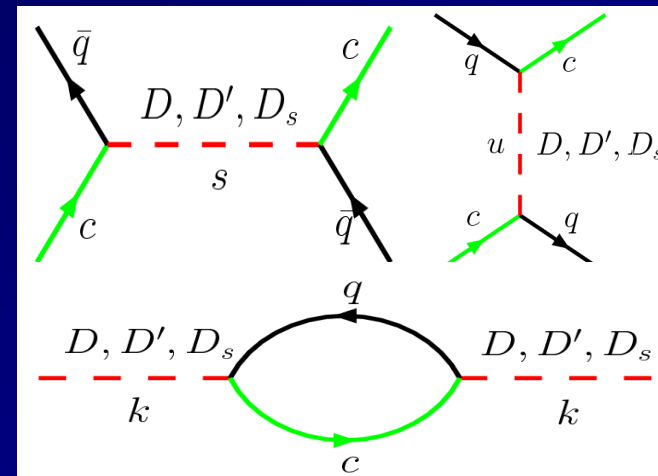
➤ Resonances switched-off at  $2 T_c$

# Open-Charm Resonances in QGP

As first test we used an effective model:

$$\mathcal{L}_{Dcq} = G_D \bar{q} \frac{(1 + \gamma_5)}{2} \Gamma \phi_D c + \text{h.c.}$$

$$\Gamma = 1, \gamma_5, \gamma_\mu, \gamma_5 \gamma_\mu \quad \text{2 parameters: } G_D, m_D$$

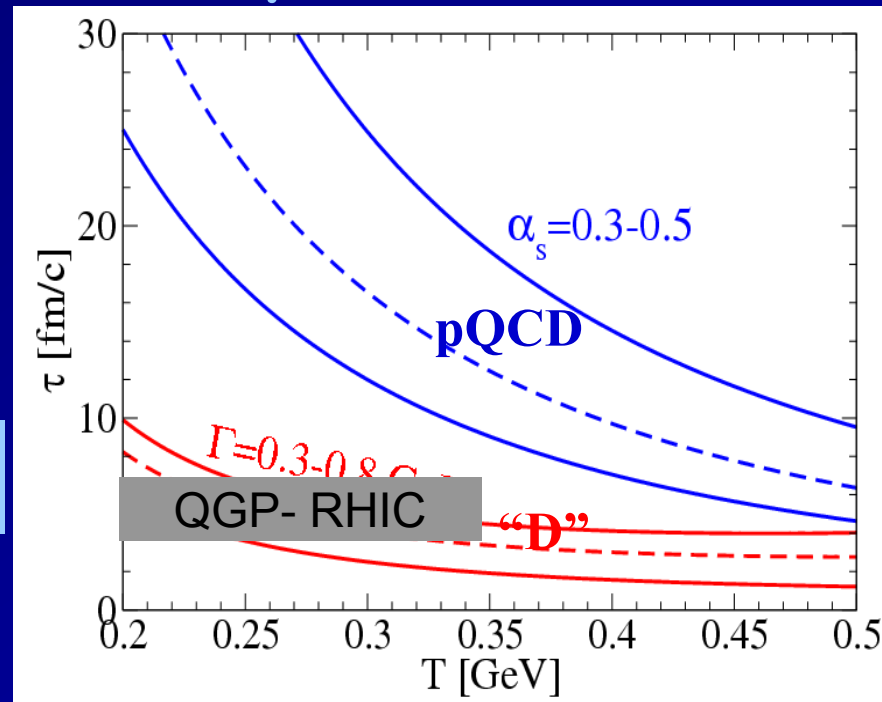


Equilibration time

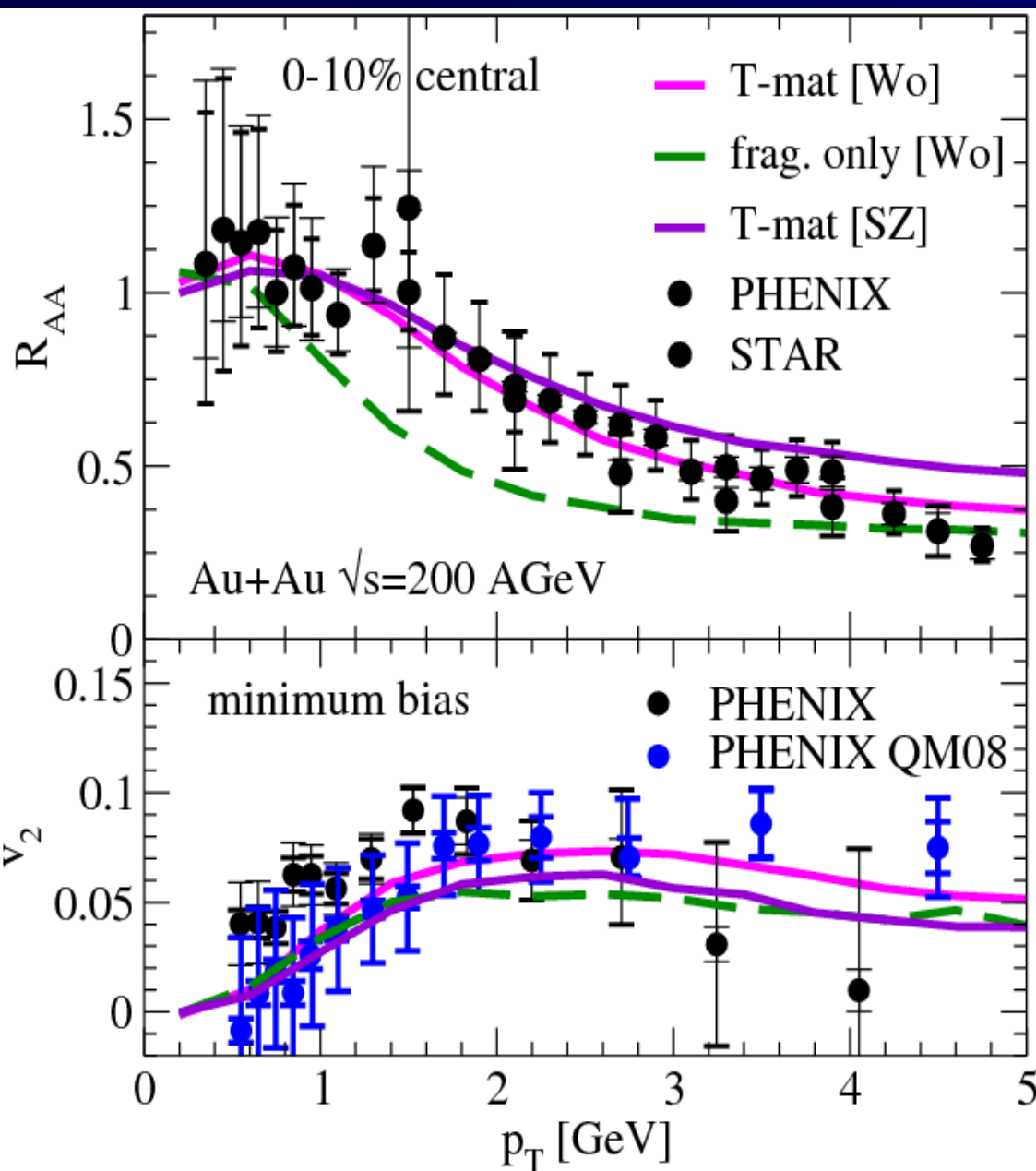
- Assuming  $\Phi$  field pseudo/scalar + axial/vector “D-like” mesons [chiral + HQ(spin) symmetry]
- cross section ISOTROPIC

❖  $t_{eq}$  down to 5 fm/c at RHIC !

Ok, but can it describe  $R_{AA}$  and  $v_2$ ?



# Uncertainty from potential parametrization



[Wo] quenched IQCD

Wong, PRC72(05)

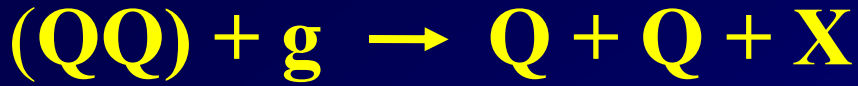
[SZ] unquenched IQCD

Shuryak-Zahed, PRD70

Moderate dependence  
on parametrization!

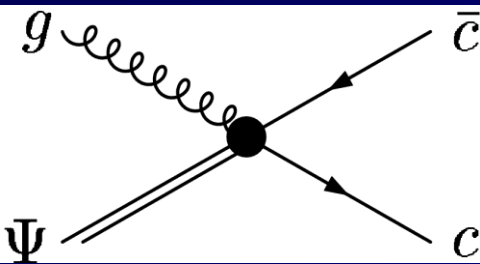
# In medium scattering

## Dynamical dissociation



$$(\tau_\Psi)^{-1} = \sum_{i=q,g} \int \frac{d^3k}{(2\pi)^3} f^i(k_0, T) \sigma_{\Psi}^{QG} v_{rel}$$

- ✓ Quarkonia dissociated also below  $T_{Diss}$
- ✓ Lifetime of the QGP is essential

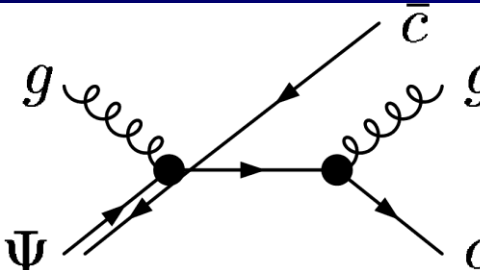


gluon-dissociation

inefficient for

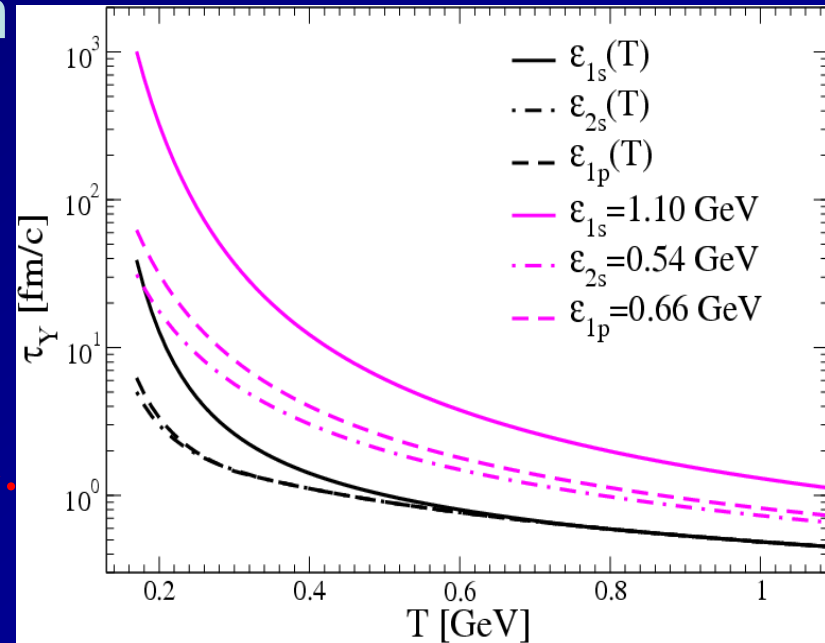
$$m_\Psi \approx 2 m_c^*$$

“new” mechanism



“quasifree” dissociation

[Grandchamp '01]

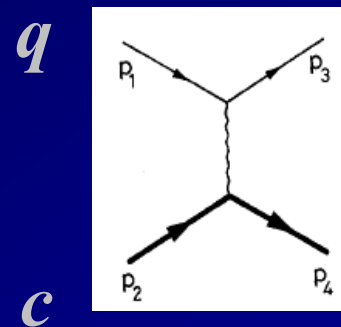
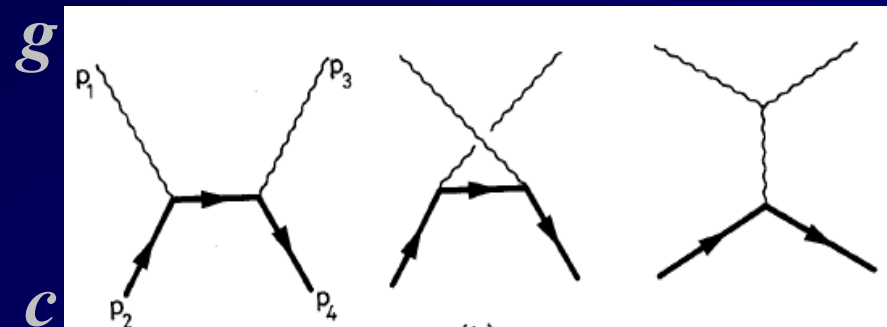


# Calculation of Collisional energy loss

Transport Equation in quasi-particle approx.

$$\left[ \frac{\partial}{\partial t} + \frac{\vec{p}}{E} \frac{\partial}{\partial \vec{x}} \right] f(x, p, t) = \int d^3k [w(p+k) f(p+k) - w(p,k) f(p)]$$

$w(p,k)$  directed linked to the cross section



[Svetitsky '88,  
Braaten '91,  
Mustafa etal '98,  
Molnar etal '04  
Zhang etal. '04,  
Teaney+Moore'04]

• dominated by *t*-channel gluon-ex in  $gc \rightarrow gc$ :

Expanding  $w(p,k)$  around  $p \sim k$  :  
dominated by soft scattering:  
(reasonable for heavy quarks)

$$\frac{\partial f}{\partial t} = \gamma \frac{\partial (pf)}{\partial p} + D \frac{\partial^2 f}{\partial p^2}$$

Fokker-Plank equation  
Background not affected  
by heavy quarks

$$\gamma p = \int d^3k w(k, p) k$$

scatt. rate

Drag & Diffusion  $p$ -independent

$$D = \frac{1}{2} \int d^3k w(k, p) k^2$$

diff. const.

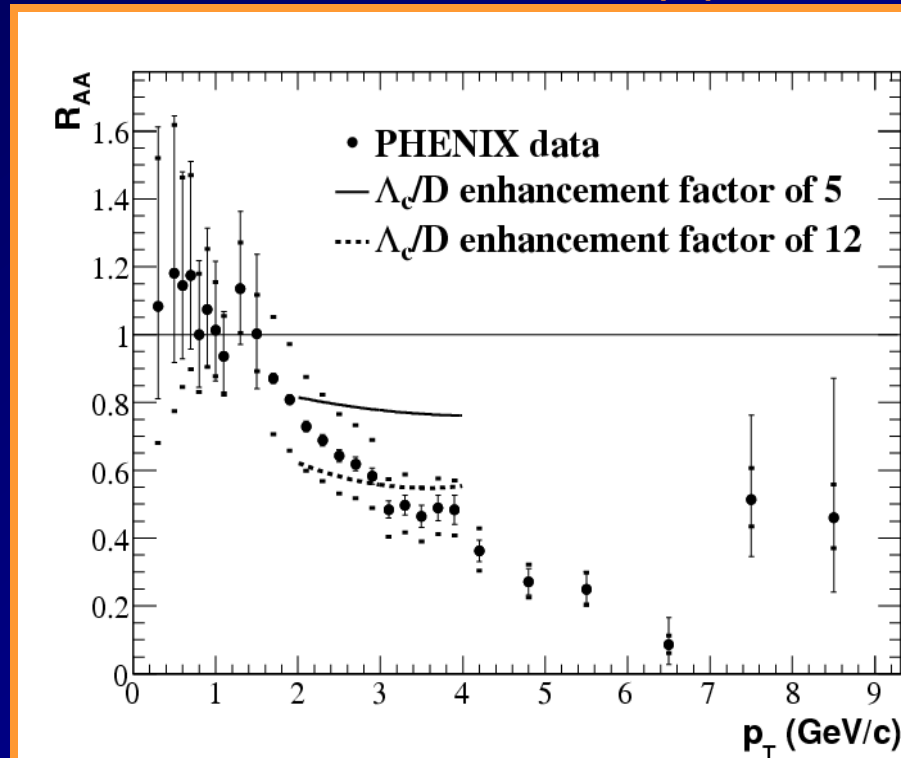
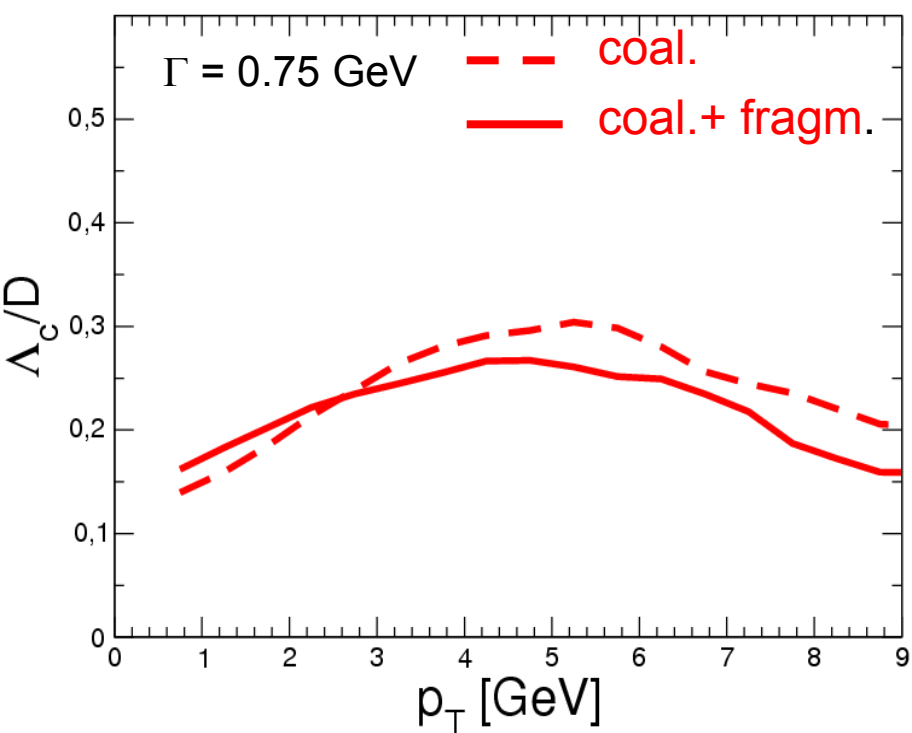
$$-\frac{dE}{dx} = \gamma p$$



# Baryon contamination due to coalescence ... !?

P. Soresen, nucl-ex/0701048

G. Martinez-Garcia et al., hep-ph/0702035



- Contamination of Lc in single e :  
enhance  $v_{2e}$ :  $v_{2\Lambda_c} > v_{2D}$
- enhancement modest + BRe 4.5%

Apparent reduction if  $\Lambda_c/D \sim 1$   
consistent with RHIC data  
( $p_T \sim 2-4 \text{ GeV}$ )

$$G_\alpha(\tau, p; T) = \int_0^\infty \frac{d\omega}{2\pi} \rho_\alpha(\omega, p; T) K(\omega, \tau; T)$$

with the finite- $T$  kernel

$$K(\omega, \tau; T) = \frac{\cosh[(\omega(\tau - 1/2T))]}{\sinh[\omega/2T]} .$$

