

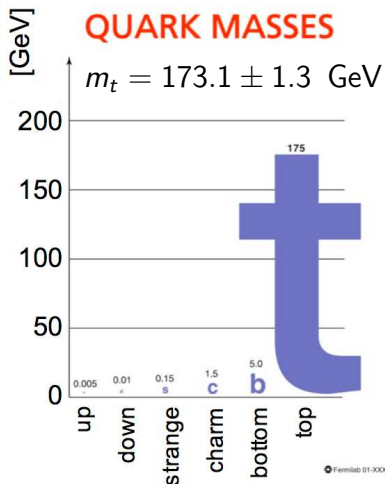
# TOP-QUARK PRODUCTION AT THE LHC

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*Les Houches, February 17, 2011*

# THE TOP QUARK



A particle which tends to stick out...

- elementary particle according to SM, but almost as heavy as a gold atom
- because of its large mass, the top quark couples strongly to the electroweak breaking sector  $\Rightarrow$  important in many BSM scenarios
- $m_t$  an important input in electroweak fits
- decays before hadronizing, can be studied as a “bare” quark

# THE TEVATRON AND THE LHC

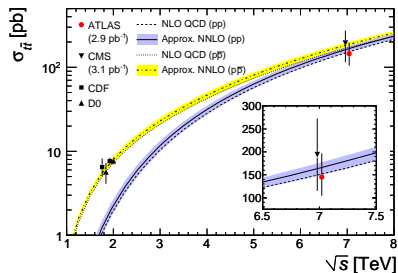
Top physics mature, thanks to Tevatron

- discovered in 1995, few thousand top-pairs analyzed ( $\sigma^{t\bar{t}} \sim 7\text{pb}$ )
- many measurements:  $m_t$ ,  $\sigma^{t\bar{t}}$ , differential distributions
- single top production observed in 2009
- experimental errors statistics limited

At the LHC millions of top quarks will be produced

- $\sigma(s = 7 \text{ TeV}) \sim 150 \text{ pb}$ ,  $\sigma(s = 14 \text{ TeV}) \sim 900 \text{ pb}$
- top sample at LHC will surpass Tevatron in 2011
- expect single top discovery in 2011
- in long run, top-quark properties will be precision physics

# FIRST LHC MEASUREMENTS NOW PUBLISHED



ATLAS: 37 top candidates in semi-leptonic/di-lepton channels

$$\sigma_{t\bar{t}} = 145 \pm 31^{+43}_{-27} \text{pb}$$

CMS: 11 top candidates in di-lepton channel

$$\sigma_{t\bar{t}} = 194 \pm 72 \pm 24 \pm 21 \text{pb}$$

Figure from ATLAS, arXiv:1012.1792v2

LHC goal:  $\delta\sigma/\sigma \sim 5\%$

## 1) Top-quark pair production

- status of QCD calculations
- some measurements and physics implications

## 2) Single top production

Almost immediately after production, decays as  $t \rightarrow bW^+$  (99% of time).

$$p\bar{p}, pp \rightarrow t\bar{t} X \rightarrow \begin{cases} \ell^+ + \ell'^- + j_b + j_{\bar{b}} + p_T^{miss} + n \geq 0 \text{ jets} \\ \ell^\pm + j_b + j_{\bar{b}} + p_T^{miss} + n \geq 2 \text{ jets} \\ j_b + j_{\bar{b}} + n \geq 4 \text{ jets} \end{cases}$$

- can factorize  $\sigma = \sigma_{\text{prod}}^{t\bar{t}X} \times \sigma_{\text{decay}}$ , corrections are order  $\Gamma_t/m_t \sim 0.01$

Will focus on production, but decay is important, and must include it to compare theory and experiment

Factorization for  $h_1 h_2 \rightarrow t\bar{t}X$ :

$$d\sigma_{h_1, h_2}^{t\bar{t}X} = \sum_{i, j=q, \bar{q}, g} \int dx_1 dx_2 f_i^{h_1}(x_1, \mu_F) f_j^{h_2}(x_2, \mu_F) d\hat{\sigma}_{ij}(s, m_t, \alpha_s(\mu_R), \mu_F, \mu_R)$$

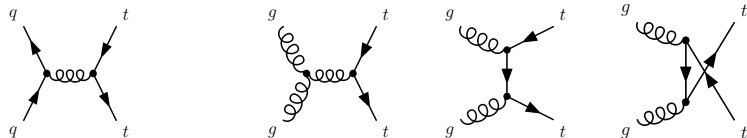
$$s_{\text{had}} = (p_{h_1} + p_{h_2})^2, \quad s = x_1 x_2 s_{\text{had}}$$

Strategy:

- take PDFs from data
- calculate partonic cross sections  $d\hat{\sigma}_{ij}$  in QCD

# Feynman Diagrams for $d\hat{\sigma}_{ij}$

Born level:



- $q\bar{q}$  dominant at Tevatron ( $\sim 90\%$  of cross section)
- $gg$  dominant at LHC ( $\sim 75\%$  of cross section at 7 TeV)

Higher-order corrections:

- virtual corrections and real emission
- $(qg, \bar{q}g) \rightarrow t\bar{t}X$  (numerically small)



NLO calculations of total and differential cross sections known for 20 years  
Nason, Dawson, Ellis ('88-'90); Beenakker, Kujif, van Neerven, Smith,  
Schuler ('89-'91); Mangano, Nason, Ridolfi ('92), Czakon and Mitov ('08)

- implemented in numerical parton MC programs; MCFM, MadGraph
- or including parton showers; MC@NLO, etc.

NLO calculations have roughly 15% factorization and renormalization scale uncertainties, to make full use of LHC data should go beyond them

# BEYOND NLO I: SOFT GLUON RESUMMATION

An “easy” way to improve on NLO is soft gluon resummation

Key quantity for NNLL resummation is 2-loop soft anomalous dimension matrix, obtained from UV poles in collinear and soft Wilson line operators in SCET (see e.g. [Ferrogli](#), [BP](#), [Neubert](#), [Yang](#) '09)

(Differential) cross sections known to  $\text{NLO} + \text{NNLL} \leftrightarrow \text{NNLO}_{\text{approx}}$  for three different soft limits:

- $d^2\sigma/dM_{t\bar{t}}d\cos\theta$ : ( $1 - M_{t\bar{t}}^2/\hat{s} \rightarrow 0$ )  
[Ahrens](#), [Ferrogli](#), [BP](#), [Neubert](#), [Yang](#) '10
- $d^2\sigma/dp_T dy$ : ( $s_4 = \hat{s} + \hat{t}_1 + \hat{u}_1 \rightarrow 0$ )  
[Kidonakis](#) '10
- $\sigma$ : ( $\beta = \sqrt{1 - 4m_t^2/\hat{s}} \rightarrow 0$ )  
[Langenfeld](#), [Moch](#), [Uwer](#) '08, '09; [Beneke et. al.](#) '09

These calculations favor upper range of NLO error band for  $\sigma$ , with reduced scale uncertainties

$$d\sigma_{t\bar{t}+X}^{\text{NNLO}} = d\sigma^{\text{VV}} + d\sigma^{\text{RV}} + d\sigma^{\text{RR}}$$

Many partial results in fixed order

- $d\sigma^{\text{VV}}$ : Czakon, Mitov, Moch; Bonciani, Ferroglia, Gehrmann; Neubert, BP, Yang; Kniehl, Korner, Merebashvili, Rogal ...
- $d\sigma^{\text{RV}}$  (1-loop  $t\bar{t} + j$ ): Dittmaier, Uwer, Weinzierl '07; Bevilacqua, Czakon, Papadopoloulos, Worek '10; Melnikov, Schulze '10
- $d\sigma^{\text{RR}}$ : Czakon '11

Need to combine the different pieces, now looks feasible!

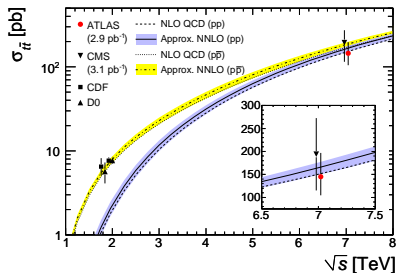
This talk

- total cross section
- $t\bar{t}$  invariant mass distribution
- charge asymmetry

Will skip many others

- $p_T$ , rapidity distributions, ...
- spin correlations

# THE TOTAL CROSS SECTION



ATLAS: 37 top candidates in semi-leptonic/di-lepton channels

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LHC goal:  $\delta\sigma/\sigma \sim 5\%$

How can this be used (other than subtracting  $t\bar{t}$  background)?

# THE TOTAL CROSS SECTION $\sigma^{t\bar{t}X}(s = 7 \text{ TeV})$ AND PDF UNCERTAINTIES

	$\sigma$ (pb)	$\delta\sigma$ (pb)	comment
ABKM09	139.55	7.96	combined PDF and $\alpha_s$
CTEQ6.6	156.2	8.06	combined PDF and $\alpha_s$ *
GJR08	169	6	PDF only
HERAPDF1.0	147.31	+5.18 -13.76	combined PDF and $\alpha_s$ **
MSTW08	168.1	+7.2-6.0	combined PDF and $\alpha_s$ ***
NNPDF2.0	169	7	combined PDF and $\alpha_s$ ****

$m_{\text{top}} = 171.3 \text{ GeV}$   
 zero width approximation,  
 no branching ratios  
 68% cl uncertainties  
 scales  $\mu_F = \mu_R = m_{\text{top}}$

\*  $\pm 6.63$  (PDF)  $\pm 4.59$  ( $\alpha_s$ )  
 \*\* expt.+model+param.+ $\alpha_s$ , see report for details  
 \*\*\* +4.7-5.6 (PDF) +3.8-4.6 ( $\alpha_s$ )  
 \*\*\*\*  $\pm 6$  (PDF)  $\pm 4$  ( $\alpha_s$ )

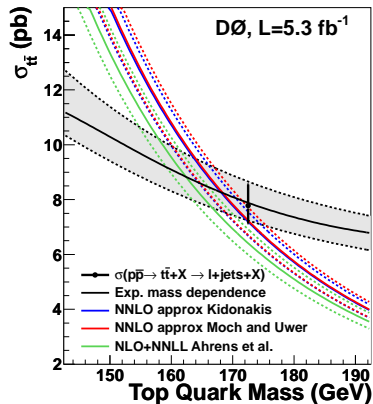
PDF4LHC Working Group Interim Report, arXiv:1101.0536 (January 2011)

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## Stirling, Heavy Particles at LHC, Zurich '11

- predictions range between 131-175pb at 68% CL (difference due mainly to gluon distribution at  $x \sim 2m_t/\sqrt{s}$ )
- measurement of  $\sigma^{t\bar{t}X}(s = 7 \text{ TeV})$  important for discriminating PDF sets

# THE TOTAL CROSS SECTION AND $m_t$



Can extract pole mass through cross section, but ...

- NNLO would be very useful
- better to use a short-distance mass such as  $\overline{MS}$  (improved convergence of perturbative series, no renormalon ambiguity)

Langenfeld, Moch, Uwer '09

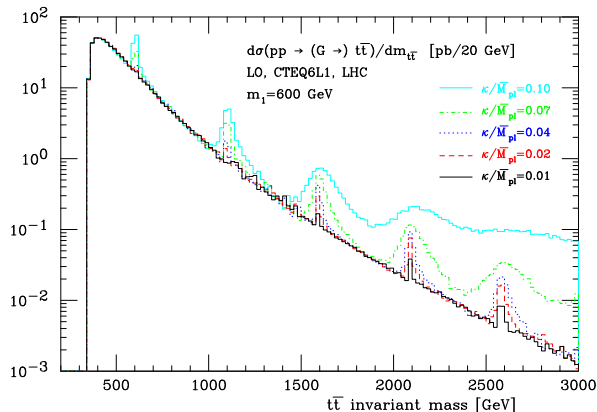
Figure from D0 in lepton+jets,  
arXiv:1101.0124

- total cross section
- $t\bar{t}$  invariant mass distribution
- charge asymmetry



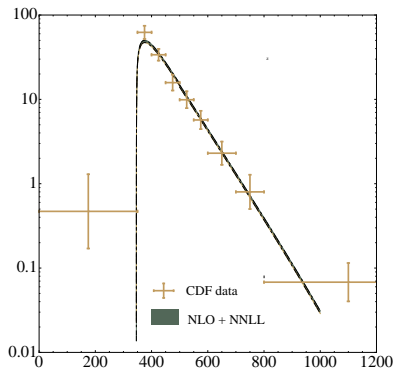
# INVARIANT MASS DISTRIBUTION

The distribution in the invariant mass  $M_{t\bar{t}}^2 = (p_t + p_{\bar{t}})^2$  can be used to search for  $s$ -channel heavy resonances



Frederix and Maltoni ('07)

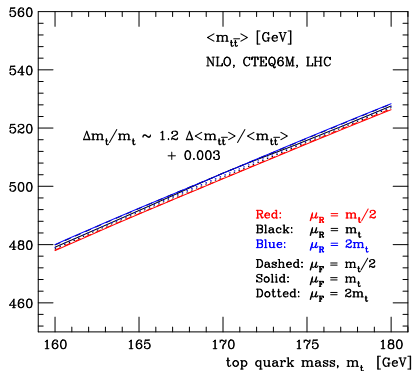
# INVARIANT MASS DISTRIBUTION AT TEVATRON



- good agreement with between theory and data at Tevatron

- Tevatron result: no  $t\bar{t}$  resonances to 900 GeV
- LHC will extend reach to higher energies

# INVARIANT MASS DISTRIBUTION AND $m_t$



Frederix and Maltoni ('07)

- theory errors can be reduced compared to total cross section
- example: 1% measurement of  $\langle M_{t\bar{t}} \rangle \Rightarrow \delta m_t/m_t \sim 1.3\%$

Mean invariant mass

$$\langle M_{t\bar{t}} \rangle = \int^{M_{\text{cutoff}}} dM_{t\bar{t}} M_{t\bar{t}} \frac{d\sigma}{dM_{t\bar{t}}} \Big|_{\text{norm.}}$$

- total cross section
- $t\bar{t}$  invariant mass distribution
- charge asymmetry

# CHARGE ASYMMETRY IN $pp(\bar{p}) \rightarrow t\bar{t}X$

Charge asymmetry:

$$A^c = \frac{N_t(y > 0) - N_{\bar{t}}(y > 0)}{N_t(y > 0) + N_{\bar{t}}(y > 0)}$$

- Tevatron:  $N_{\bar{t}}(y) = N_t(-y)$ , so is a forward-backward symmetry
- asymmetry depends on the frame

QCD predictions:

- Tevatron:  $A^c \sim 5\%$  is NLO ( $\alpha_s^3$ ) effect from  $q\bar{q}$  channel
- LHC:  $A^c = 0$ , since initial  $pp$  state is symmetric

# INCLUSIVE CHARGE ASYMMETRY AT THE TEVATRON

DO, 4.3fb<sup>-1</sup>

$$A_c(t\bar{t}) = 0.08 \pm 0.08 \text{ stat} \pm 0.01 \text{ syst}$$

CDF, 5.3fb<sup>-1</sup>

$$A_c(t\bar{t}) = 0.158 \pm 0.072 \text{ stat} \pm 0.017 \text{ syst}$$

$$A_c(\text{lab}) = 0.150 \pm 0.050 \text{ stat} \pm 0.024 \text{ syst}$$

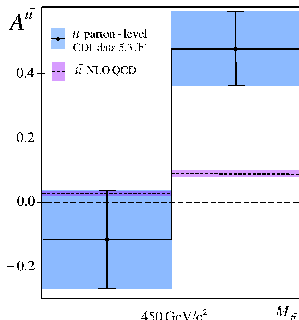
Theory

$$A_c(\text{lab}) = 0.051 \pm 0.006 \text{ (NLO+EW, Kuhn, Rodrigo '98)}$$

$$A_c(t\bar{t}) = 0.078 + 0.011 - 0.007 \text{ (NLO+NNLL, Ahrens et. al. '10)}$$

Theory and experiment agree at about  $2\sigma$

# INVARIANT MASS DEPENDENT ASYMMETRY AT TEVATRON (CDF ARXIV:1101:0034)



- $M_{t\bar{t}} < 450 \text{ GeV}$ : compatible with NLO within  $1\sigma$
- $M_{t\bar{t}} > 450 \text{ GeV}$ : disagrees with NLO at  $3.4\sigma$

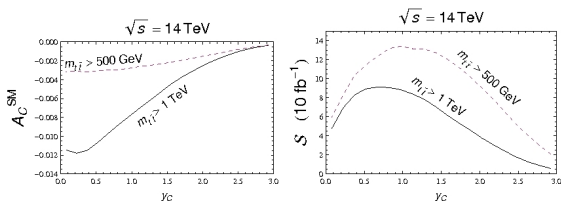
# CHARGE ASYMMETRY AT THE LHC

Integrated asymmetry vanishes.

Use cuts on  $y$

$$A_C(y_C) = \frac{N_t(|y| < y_C) - N_{\bar{t}}(|y| < y_C)}{N_t(|y| < y_C) + N_{\bar{t}}(|y| < y_C)}$$

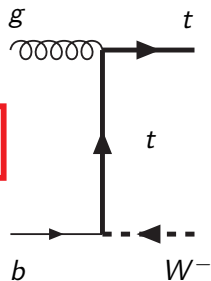
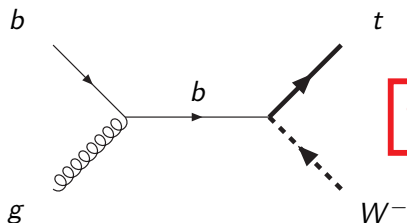
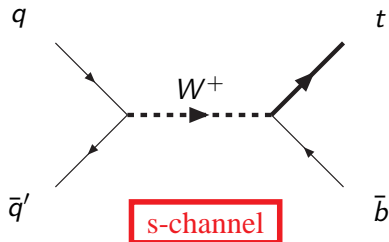
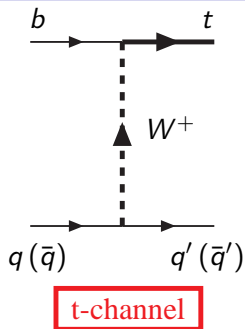
To reduce  $gg$  contribution to denominator (charge symmetric), also use cuts on  $M_{t\bar{t}}$



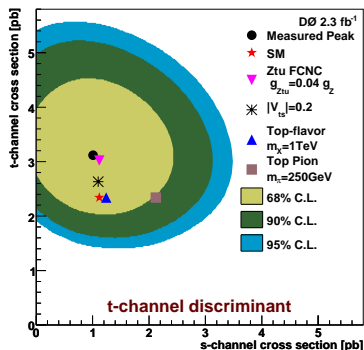
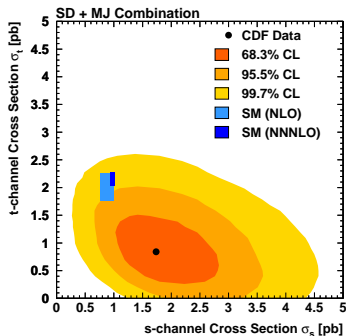
Ferrario and Rodrigo ('08)



# SINGLE TOP QUARK PRODUCTION



# SINGLE TOP PRODUCTION AT THE TEVATRON II: SEPARATE $s$ AND $t$ CHANNEL



- Good overall agreement with SM, although CDF has  $2\sigma$  discrepancy in  $t$  channel
- can extract  $|V_{tb}| = 0.88 \pm 0.07$  ( $|V_{tb}| = 0.999$  from unitarity of CKM matrix)

Top physics mature field due to Tevatron

- many measurements, many agreements with SM
- couple  $2 - 3\sigma$  deviations
  - FB asymmetry (especially with cut  $M_{t\bar{t}} > 450\text{GeV}$ )
  - $t$ -channel single top at CDF
- most measurements statistics limited

At LHC statistics will not be a factor, many interesting measurements to come ...