

***Jets at the LHC***  
***(both  $pp$  and  $PbPb$ )***

***aka Jets of a new generation***

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**In collaboration with Gavin Salam and Matteo Cacciari**

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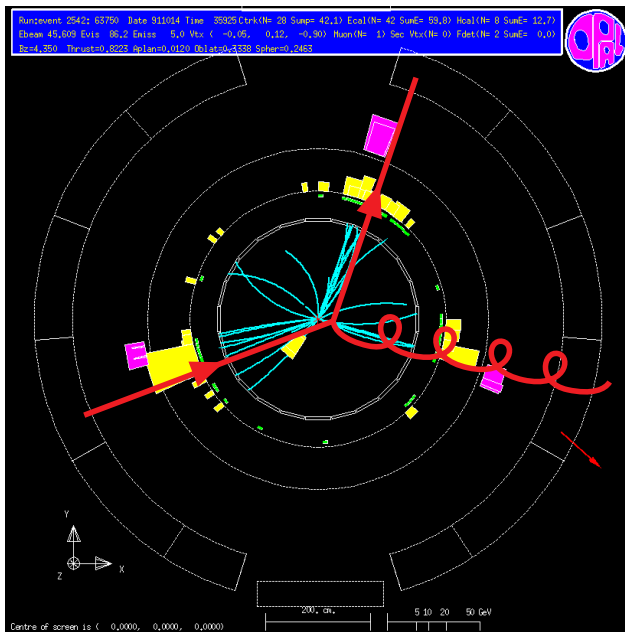
- Basic jet definitions
  - **Motivation**: the need for a jet definition
  - **Situation today**: meeting the 1990 requirements
- New directions (*selected topics*)
  - **Jet substructure**: filter UE, tag boosted objects
  - **Subtracting soft background using jet areas**
- New directions (*additional topics*)
  - **Optimisation**: kinematic dijet reconstruction
  - **Dijet asymmetries**: what room for quenching?
  - **Tools**: Towards FastJet 3.0

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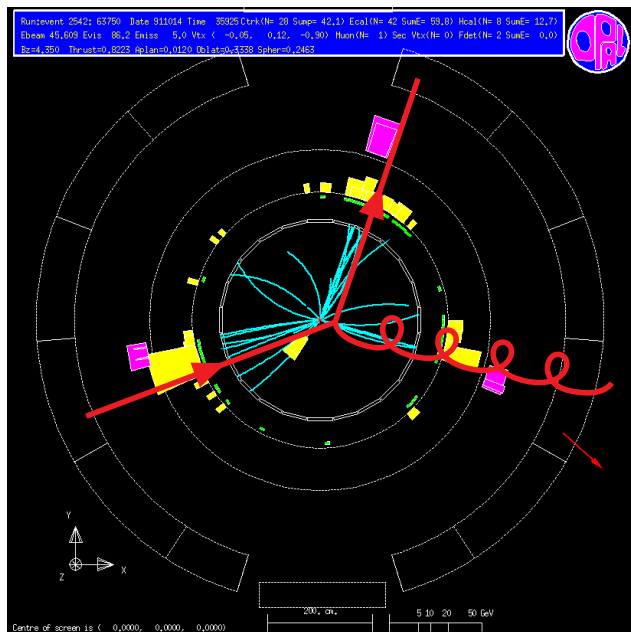
# Jet definitions

“Jets”  $\equiv$  bunch of collimated particles  $\cong$  hard partons



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In practice: use a jet definition

particles  $\{p_i\}$   $\xrightarrow[\text{definition}]{\text{jet}}$  jets  $\{j_k\}$

algorithm: the recipe (insufficient!)

definition: algorithm + params

“Jet=hadron” too simplistic: What opening for “collimated”? NLO?

# Jet algorithms: a big family

## Recombination:

- $k_t$  algorithm
- Cambridge/Aachen alg.
- anti- $k_t$  algorithm

## Cone:

- SISCone
- CDF JetClu
- CDF MidPoint
- D0 (run II) Cone
- PxCone
- ATLAS Cone
- CMS Iterative Cone
- PyCell/CellJet
- GetJet

# *Jet definitions: constraints*

## SNOWMASS accords (FermiLab, 1990)

Several important properties that should be met by a jet definition are [3]:

1. Simple to implement in an experimental analysis;
2. Simple to implement in the theoretical calculation;
3. Defined at any order of perturbation theory;
4. Yields finite cross section at any order of perturbation theory;
5. Yields a cross section that is relatively insensitive to hadronization.

20 years later, these are only recently satisfied!!!



# Jet algorithms: the situation now

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# Jet algorithms: the situation now

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Implementation:  
FastJet  
[www.fastjet.fr](http://www.fastjet.fr)

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# Inside jet definitions

- **Recombination**: successively recombine the closest pair

$$d_{ij} = \min(k_{t,i}^{2p}, k_{t,j}^{2p})(\Delta y_{ij}^2 + \Delta\phi_{ij}^2)$$

Stop at distance  $R$

- $p = 1$ :  $k_t$  algorithm (very close to QCD)

[Catani, Dokshitzer, Seymour, Webber, 93]

- $p = 0$ : **Cambridge/Aachen (C/A)** algorithm (substructure studies)

[Dokshitzer, Leder, Moretti, Webber, 93]

- $p = -1$ : **anti- $k_t$**  algorithm (circular/rigid jets)

[Cacciari, Salam, GS, 08]

- **Cone**:  $\approx$  flow of energy in a cone (of fixed  $R$ ) centred on the cone centre: **SISCone**

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Finite perturbative cross-section: only consider **infrared-and-collinear-safe** algorithms

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**the default at the LHC**

[Cacciari, Salam, GS, 08]

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# ***New generations***

# Challenges

Idea: set of solid algorithms: optimise their usage

- Handle pileup (in  $pp$ ) and large UE (in  $PbPb$ )
- Tag boosted objects/Study substructure
- filter out UE contamination to jets
- optimize reconstruction

# ***New generations***

## ***2. pileup subtraction using jet areas***

***[M.Cacciari,G.Salam, 07]***

***[M.Cacciari,G.Salam,GS, 08]***

***[M.Cacciari,J.Rojo,G.Salam,GS, 10]***

# Physics cases and scales

Typical applications: [GeV]

Case	$\rho = p_t/\text{unit area}$	$\sigma = \text{flucts}$	$\delta p_{t,\text{jet}}(R = 0.4)$
Pileup in $pp$	10-20	3-5	5-10
$AuAu$ (RHIC)	80-100	8-12	40-50
$PbPb$ (LHC)	150-250	15-25	75-125



## Central formula

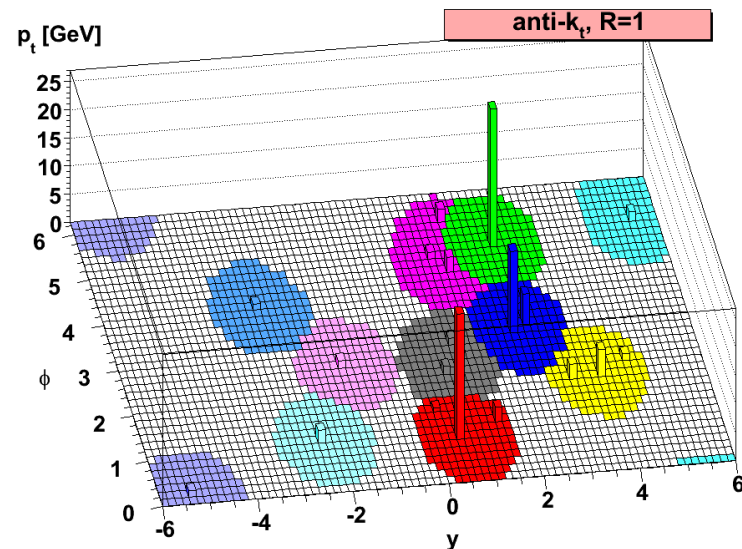
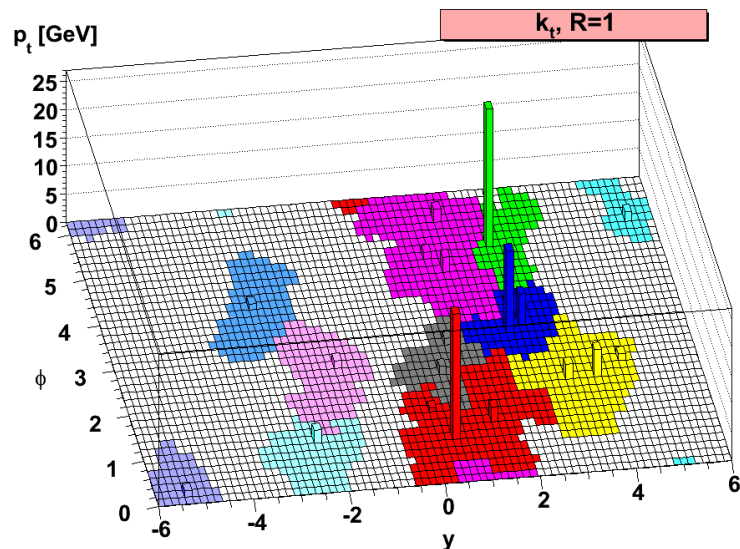
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## ● jet area:

- defined to mimic the reaction to the background
- implemented in FastJet
- analytic handle

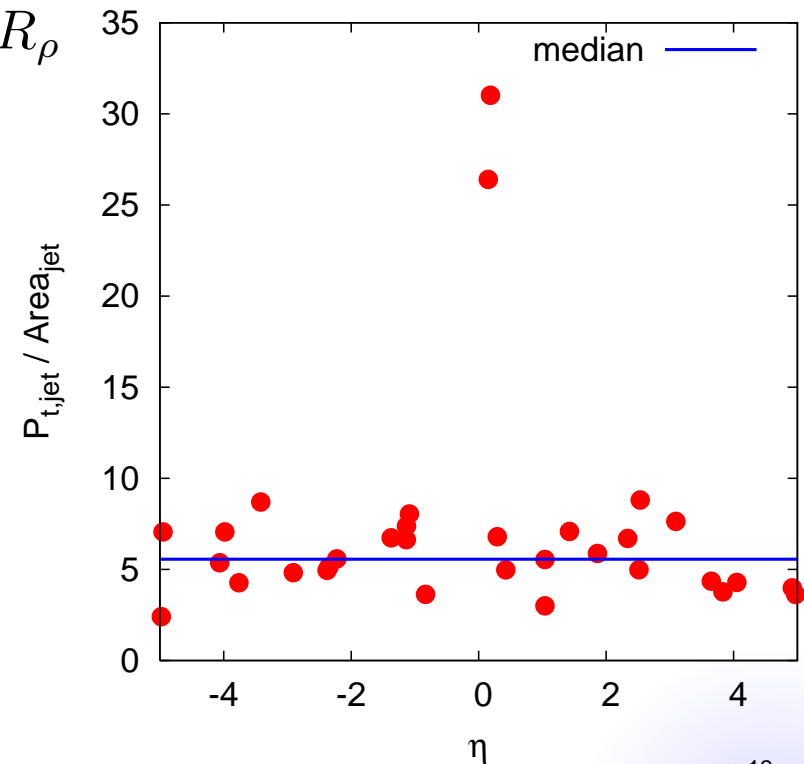


# Central formula

$$p_{t,\text{jet}}^{(\text{sub})} = p_{t,\text{jet}} - \rho_{\text{bkg}} A_{\text{jet}}$$

- jet area:
- $\rho_{\text{bkg}}$ , the background  $p_t$  density per unit area
  - Cluster with  $k_t$  of C/A with “radius”  $R_\rho$
  - Estimate  $\rho_{\text{bkg}}$  using

$$\rho_{\text{bkg}} = \text{median}_{j \in \text{jets}} \left\{ \frac{p_{t,j}}{A_j} \right\}$$



# Subtraction uncertainties

- 1 Background fluctuations: (inside an event!)

$$p_{t,\text{jet}} = p_{t,\text{jet}}^{\text{hard}} + \rho_{\text{bkg}} A_{\text{jet}} \pm \sigma_{\text{bkg}} \sqrt{A_{\text{jet}}}$$

Hint: reduce  $A_{\text{jet}}$  e.g. using filtering

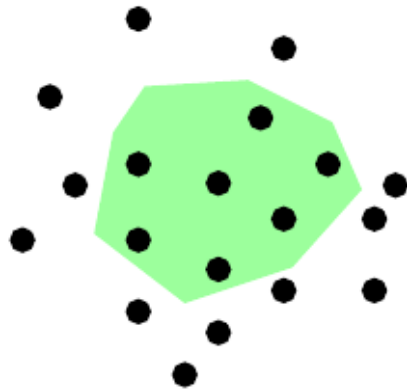
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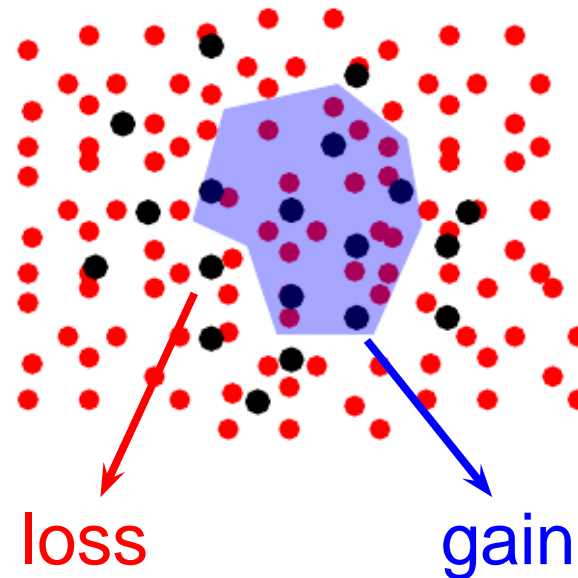
$$p_{t,\text{jet}} = p_{t,\text{jet}}^{\text{hard}} + \rho_{\text{bkg}} A_{\text{jet}} \pm \sigma_{\text{bkg}} \sqrt{A_{\text{jet}}}$$

## ② Back-reaction:

No background



With background



Hint: use anti- $k_t$  (rigidity!)

# Subtraction uncertainties

- 1 Background fluctuations: (inside an event!)

$$p_{t,\text{jet}} = p_{t,\text{jet}}^{\text{hard}} + \rho_{\text{bkg}} A_{\text{jet}} \pm \sigma_{\text{bkg}} \sqrt{A_{\text{jet}}}$$

- 2 Back-reaction:
- 3 Background non-uniform (e.g. rap dependence)

Use jets in a *local range* to estimate  $\rho_{\text{bkg}}$

$$\rho_{\text{bkg}} = \text{median}_{j \in \mathcal{R}} \left\{ \frac{p_{t,j}}{A_j} \right\}$$

The diagram illustrates two methods for estimating the background density  $\rho_{\text{bkg}}$ . The 'Global' method uses jets from the entire event, represented by a large blue rectangle from  $-y_{\text{max}}$  to  $y_{\text{max}}$  with a central 'jet' dot. The 'Strip( $\Delta$ )' method uses jets from a local range around the jet, represented by a vertical blue strip from  $y_{\text{jet}} - \Delta$  to  $y_{\text{jet}} + \Delta$  with a central 'jet' dot. The vertical axis for the strip ranges from 0 to  $2\pi$ .

+ exclude the (e.g.) 2 hardest jets

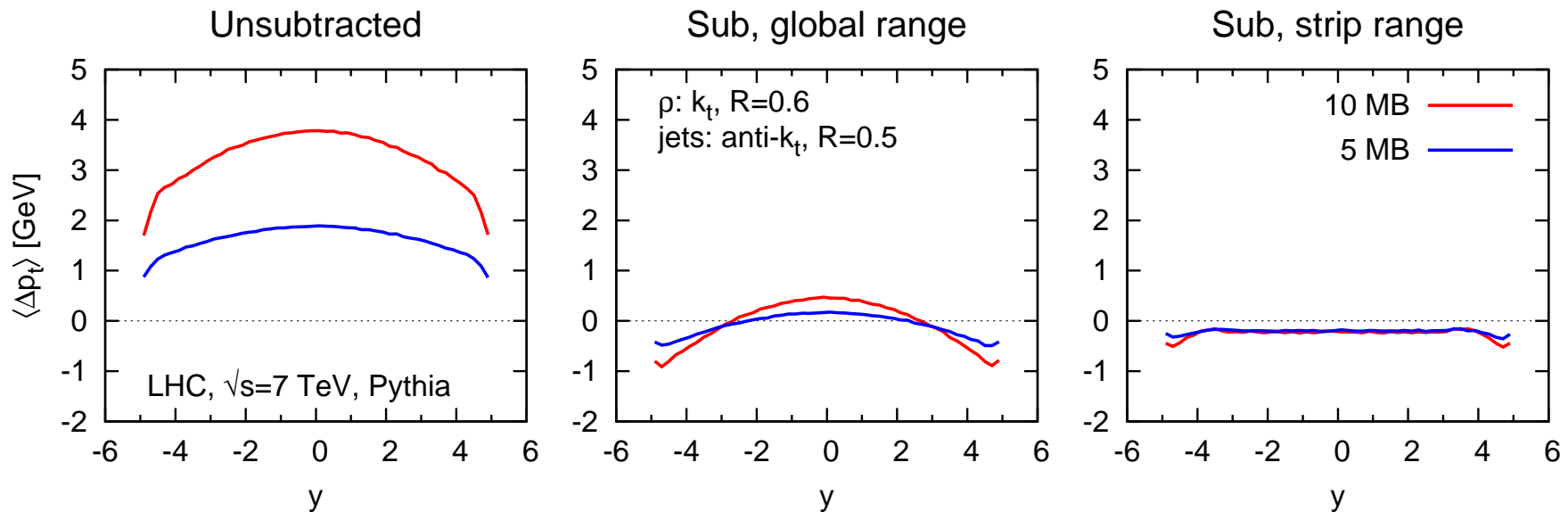
# Subtraction uncertainties

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- After subtraction:  $|\delta p_{t,\text{jet}}| \lesssim 1 \text{ GeV}$
- Left with fluctuations (and back-reaction)



# Physics cases and scales

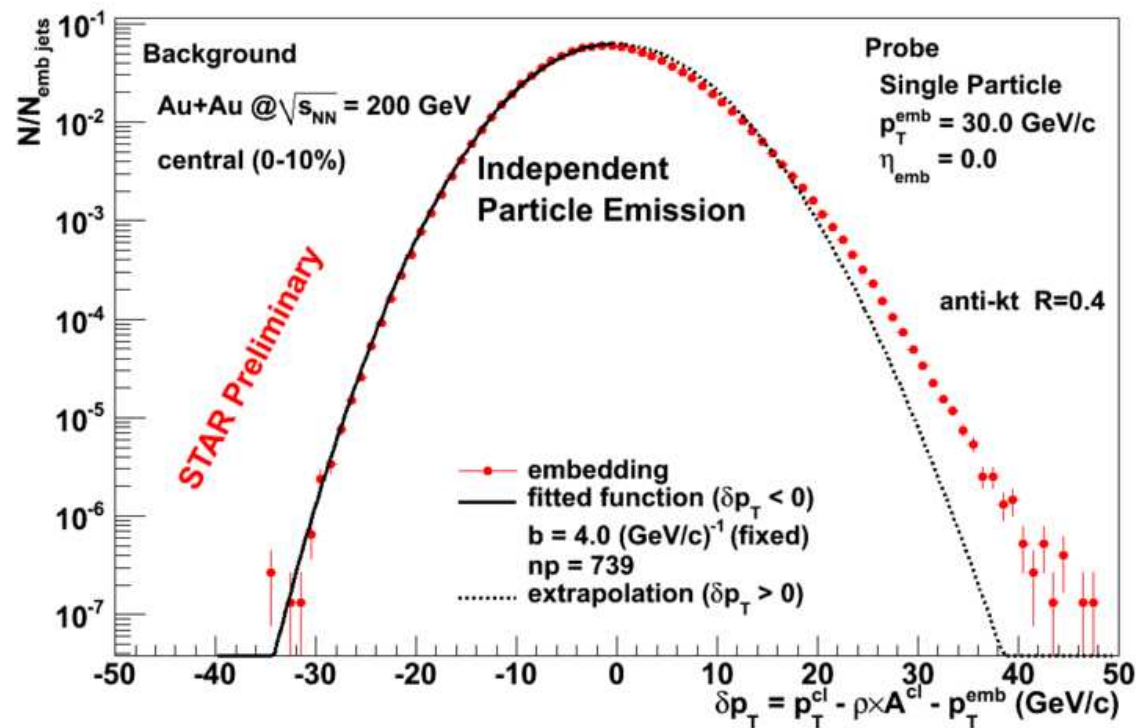
## Typical applications:

### Case

Pileup in  $pp$   
 $AuAu$  (RHIC)  
 $PbPb$  (LHC)

- After subtraction
- Left with flu

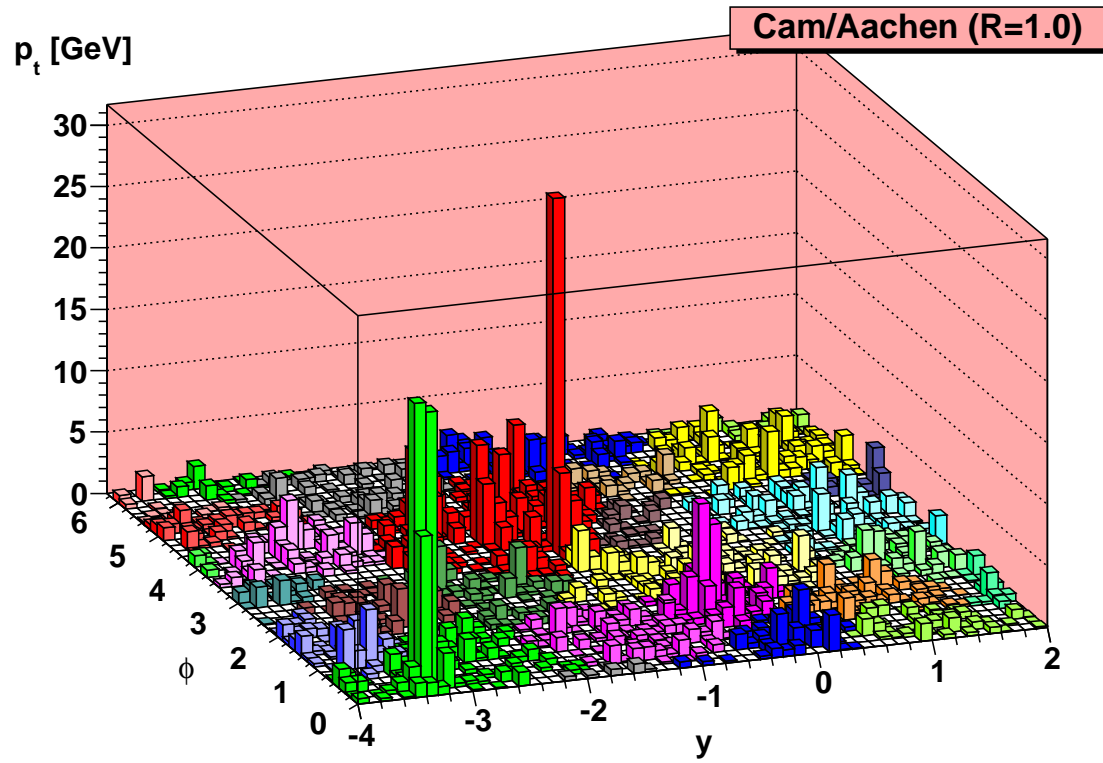
- Can be studied e.g. by embedding “known jets into background data” (→ unfolding)



0.4)

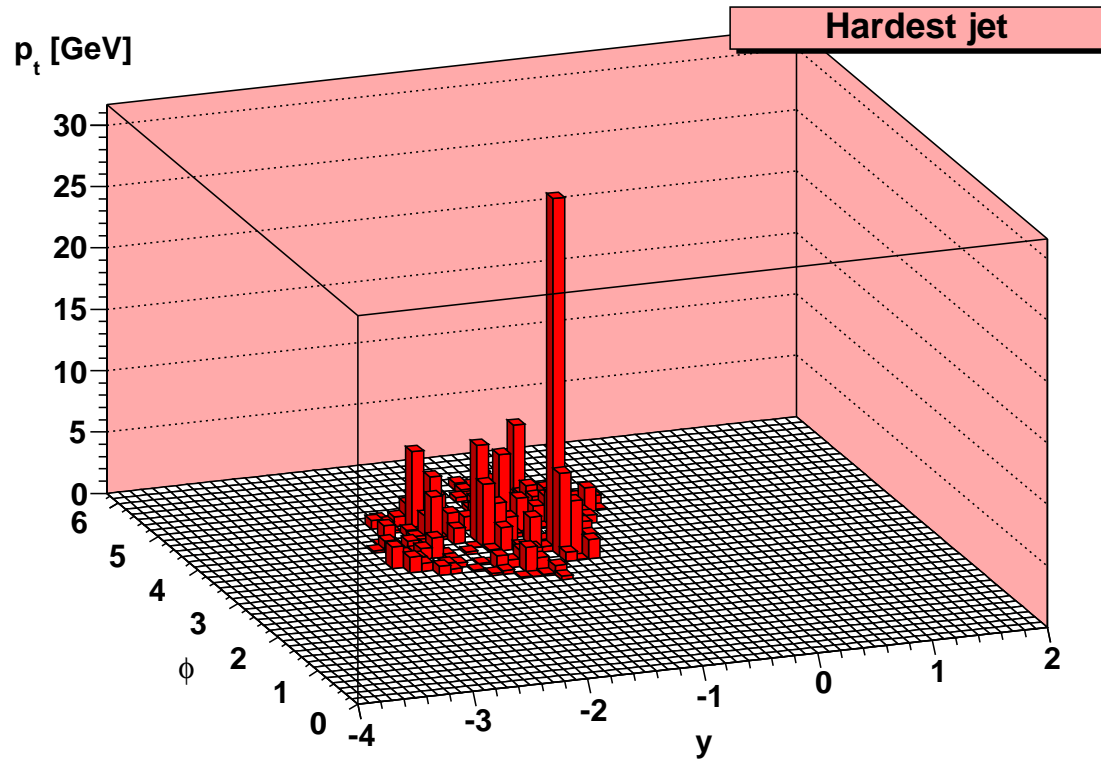
***New generations***  
***2. Jet substructure***

# Filtering



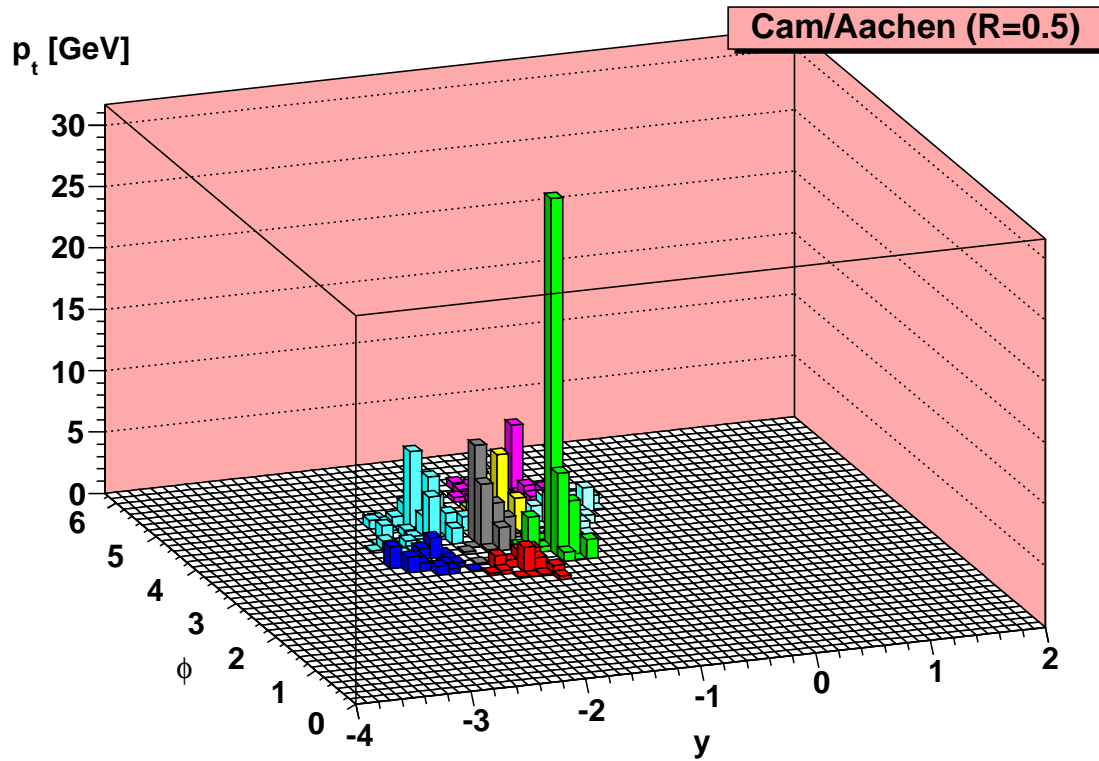
- cluster with Cambridge/Aachen(R)

# Filtering



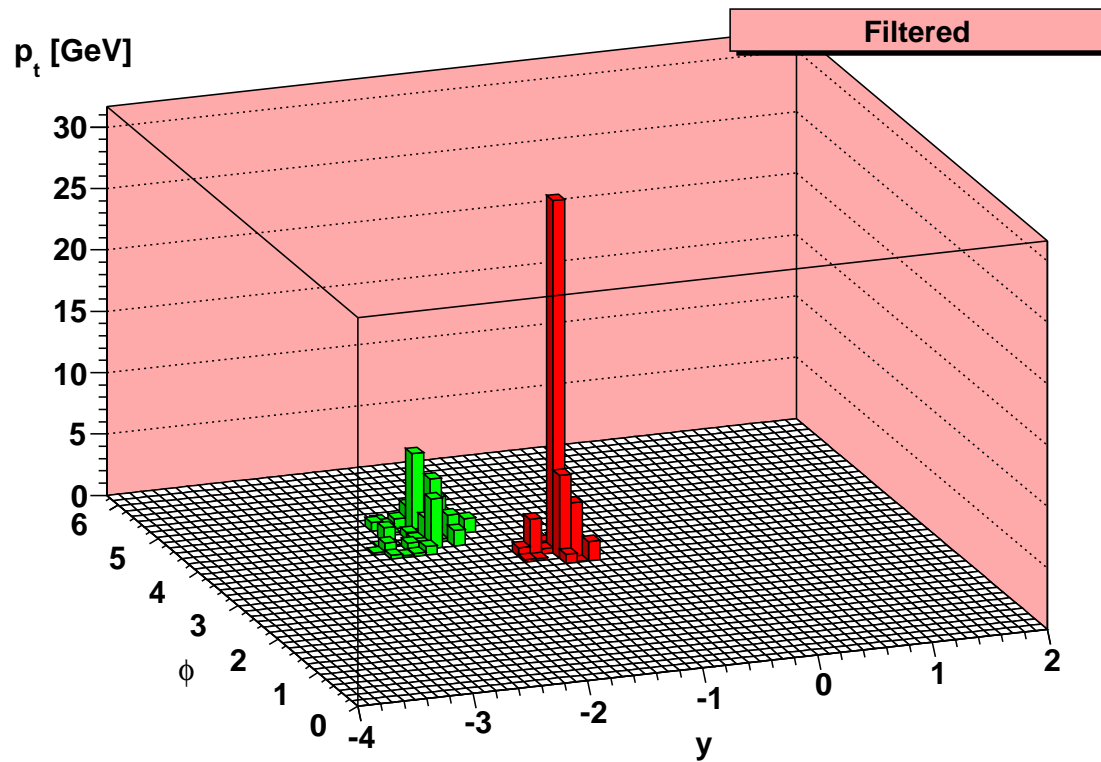
- cluster with Cambridge/Aachen(R)
- for each jet

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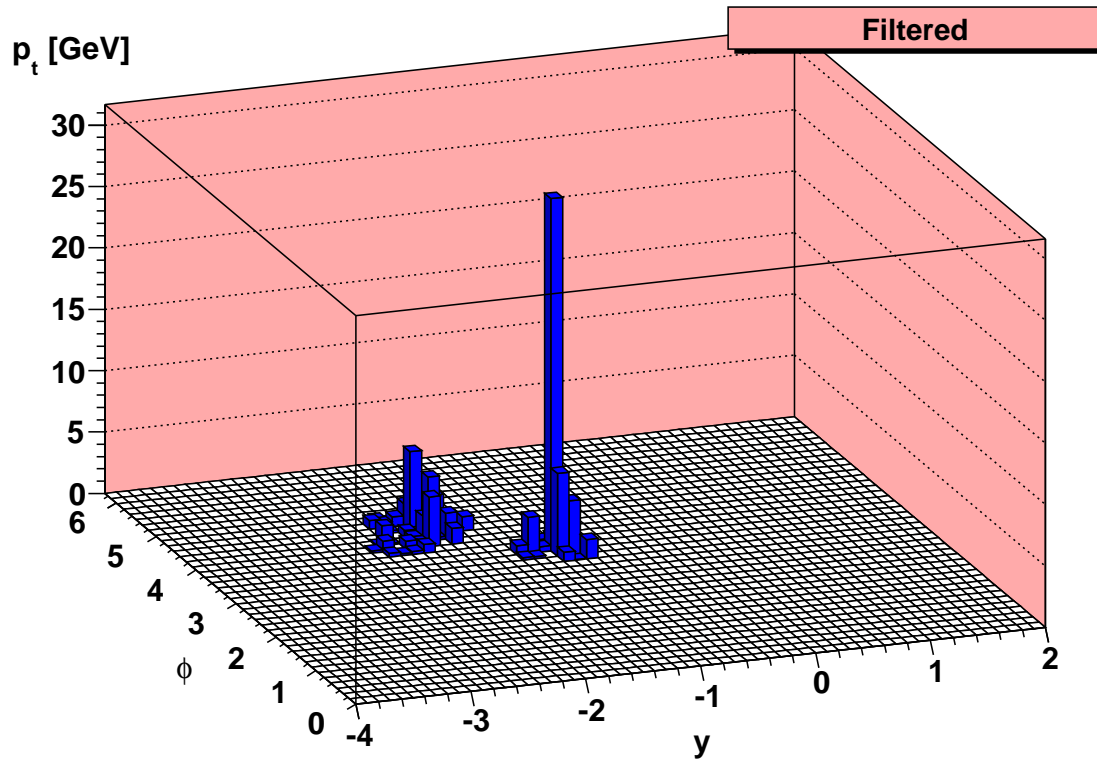
- cluster with Cambridge/Aachen( $R$ )
- for each jet
  - recluster with Cambridge/Aachen( $R/2$ )

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- cluster with Cambridge/Aachen(R)
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  - keep the 2 hardest subjets

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Idea:

- ✓ keep perturb. radiation
- ✓ remove UE

- Proven useful for boosted jet  $H \rightarrow b\bar{b}$  tagging

[J.Butterworth, A.Davison, M.Rubin, G.Salam, 08]

- Proven useful for kinematic reconstructions

[M.Cacciari, J.Rojo, G.Salam, GS, 08]

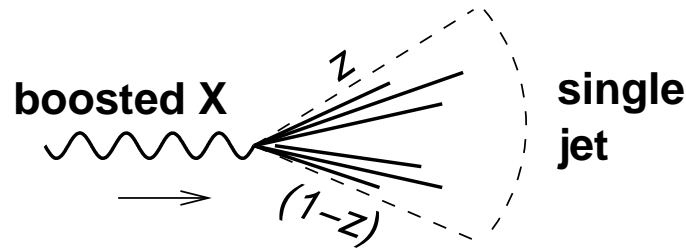
- Similar: trimming

[D.Krohn, J.Thaler, L-T.Wang, 10]

# Boosted object tagging

## Problem:

boosted heavy object  $\Rightarrow$  decays reconstructed in a **single jet**



$$R \gtrsim \frac{m}{p_t} \frac{1}{\sqrt{z(1-z)}}$$

How to disentangle that from a QCD jet?

**Idea:** **substructure** e.g. look inside the jet

Various methods: mass drop, pruning, use Jade distances, asymmetry cuts,...

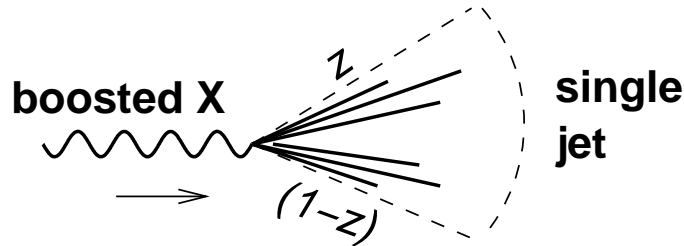
**Applications:** (examples)

- 2 decay products:  $W \rightarrow q\bar{q}$ ,  $H \rightarrow b\bar{b}$
- 3 decay products:  $t \rightarrow qq\bar{b}$ ,  $\tilde{\chi} \rightarrow qq\bar{q}$
- busier:  $t\bar{t}H$



# Example: boosted Higgs

[J.Butterworth, A.Davison, M.Rubin, G.Salam,08]



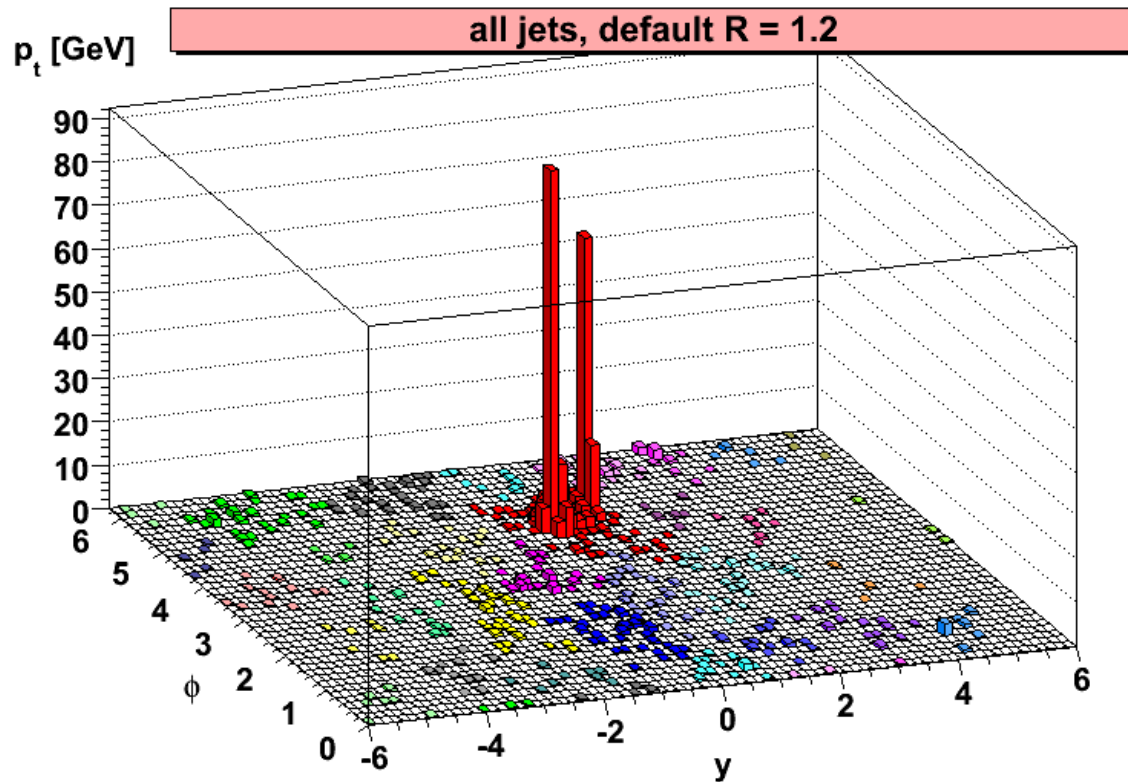
$$R \gtrsim \frac{m}{p_t} \frac{1}{\sqrt{z(1-z)}}$$

Method: start with a hard (C/A, radius R) jet  $j$

- 1 Undo the last clustering  $\rightarrow j_1, j_2$
- 2 If  $\max(m_1, m_2) < 0.67m$ , we have a mass drop, else back to 1  
idea: find the 2  $b$ -jets, dynamically find  $R_{bb}$
- 3 Require symmetric splitting  $y_{12} \approx \frac{\min(z_1, z_2)}{\max(z_1, z_2)} > 0.09$ , else go to 1  
idea: remove QCD asymmetric splittings
- 4 Require 2  $b$  taggings
- 5 Filter *i.e.* uncluster down to  $R_{\text{filt}}$ , keep the 3 hardest subjets  
idea: keep “hard” QCD radiations, reduce UE

# Boosted Higgs: one event, effects on $S/B$

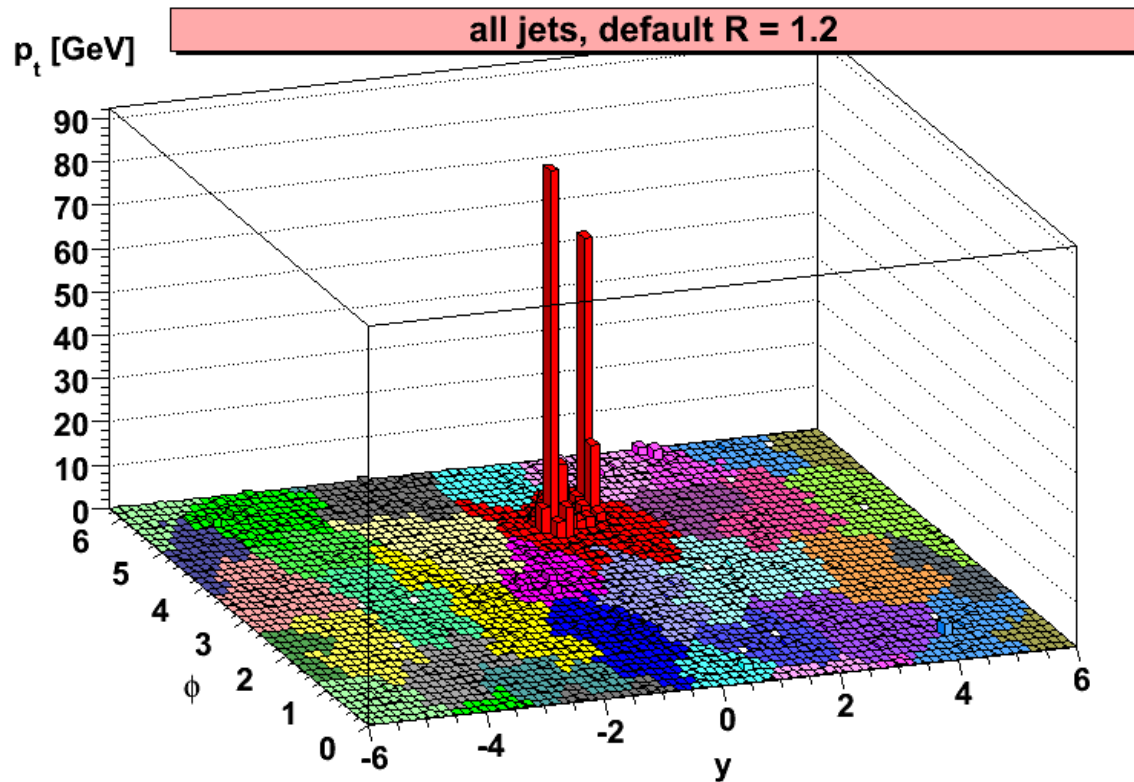
Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



Cluster C/A, R=1.2

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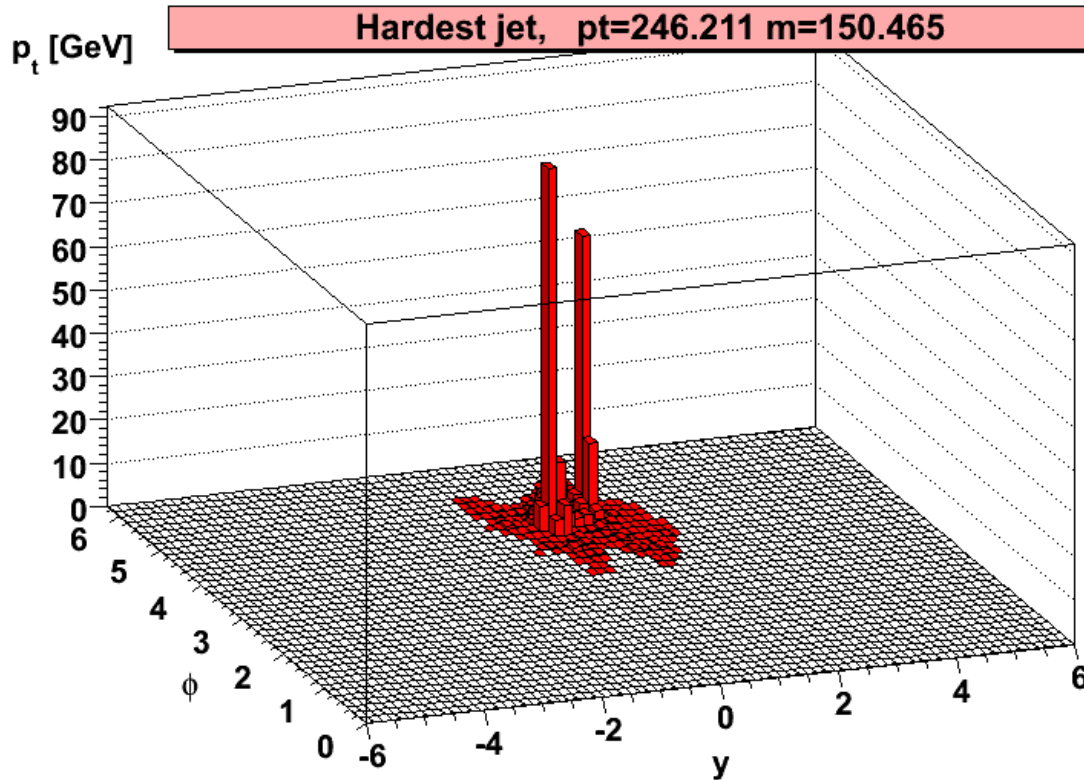
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Show jets more clearly

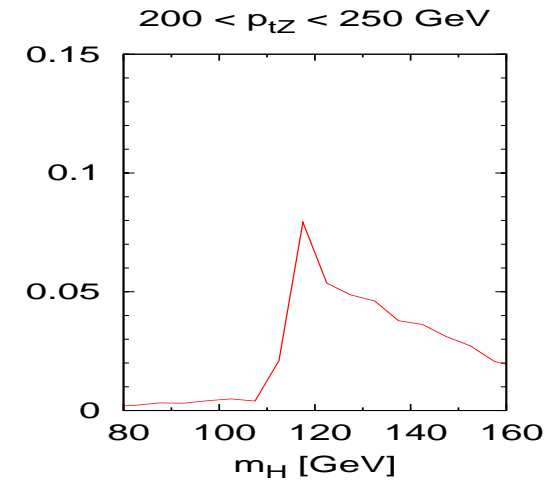
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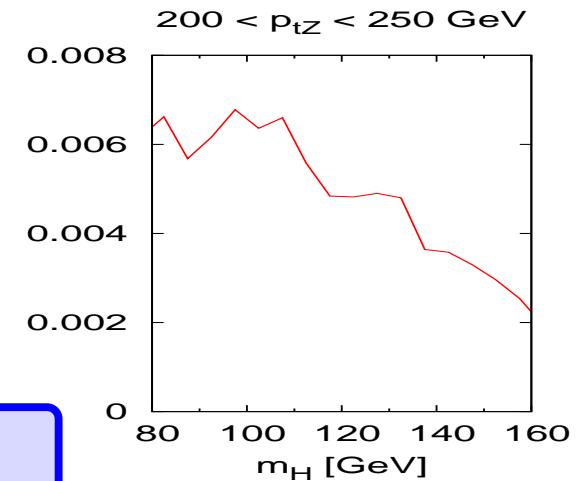


Hardest jet ( $m = 150$  GeV)

## $HZ$ Signal

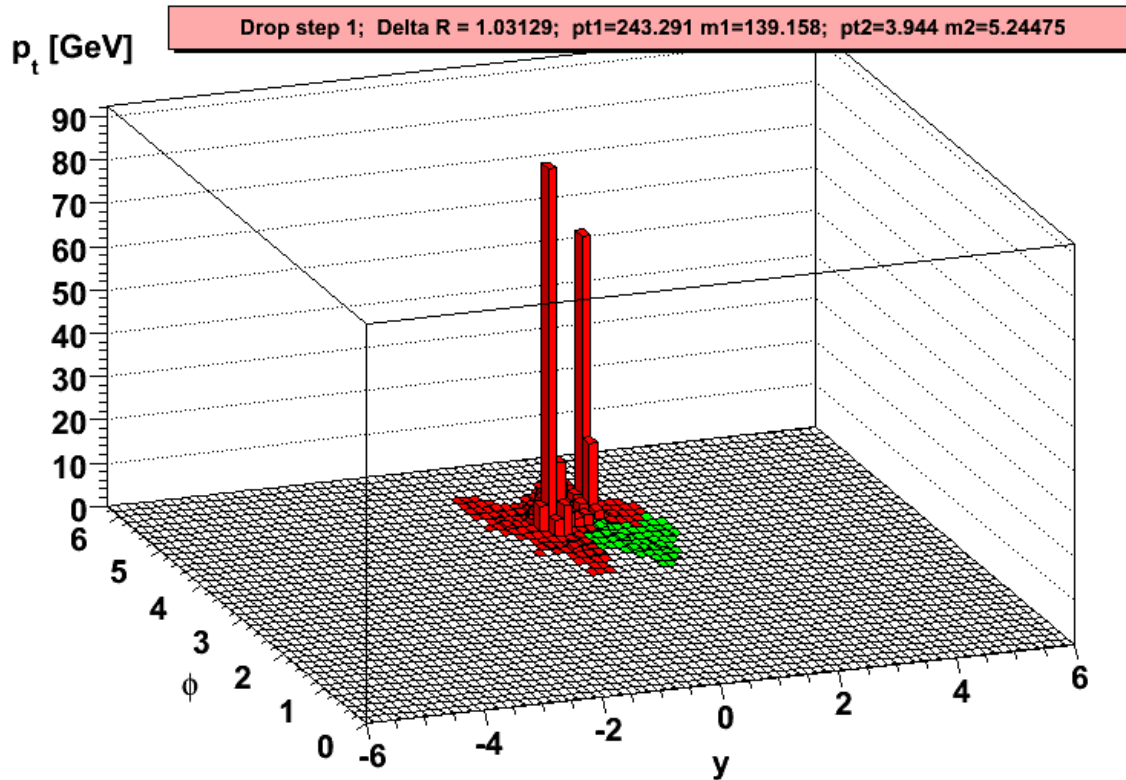


## $Zbb$ Background

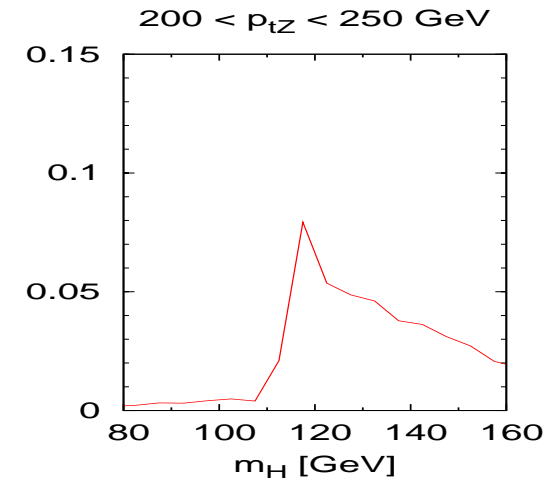


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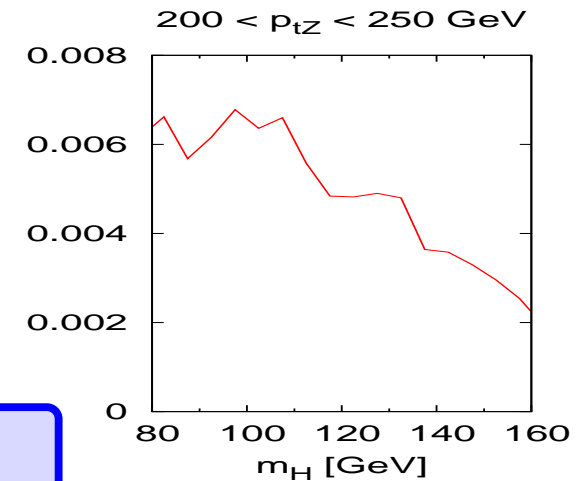
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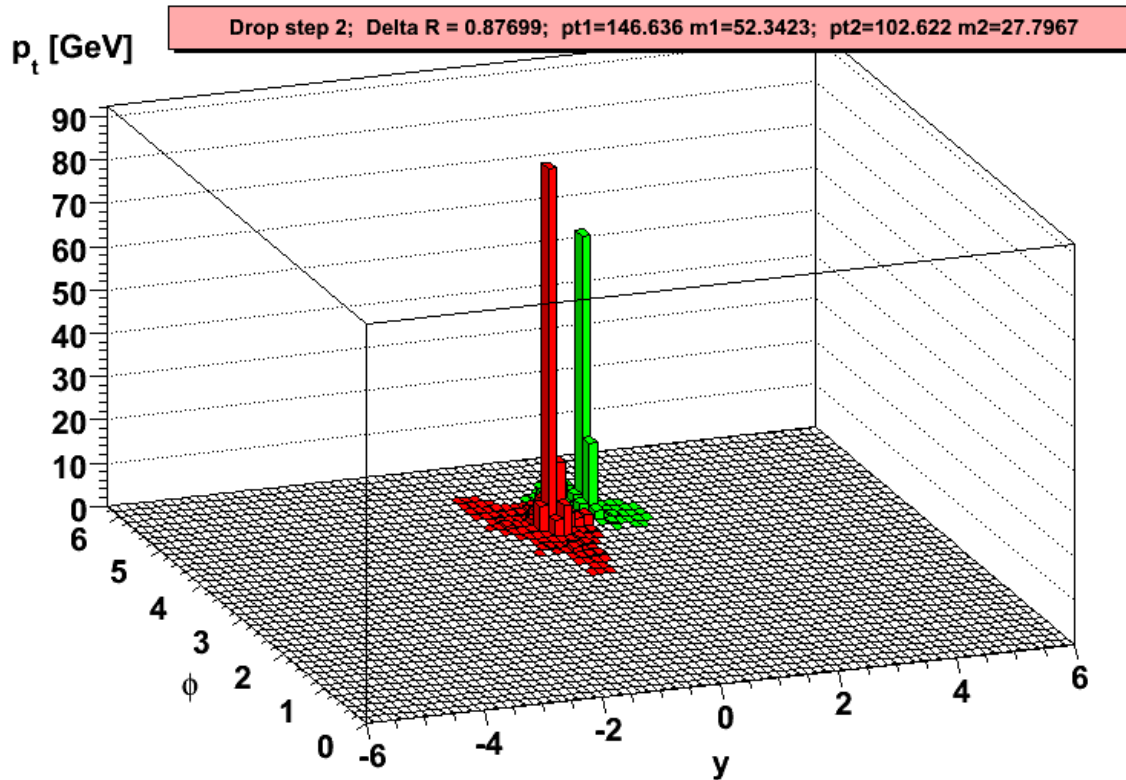
## $Zbb$ Background



Split:  $\frac{\max(m_1, m_2)}{m} = 0.92$ , repeat ( $m = 150$  GeV)

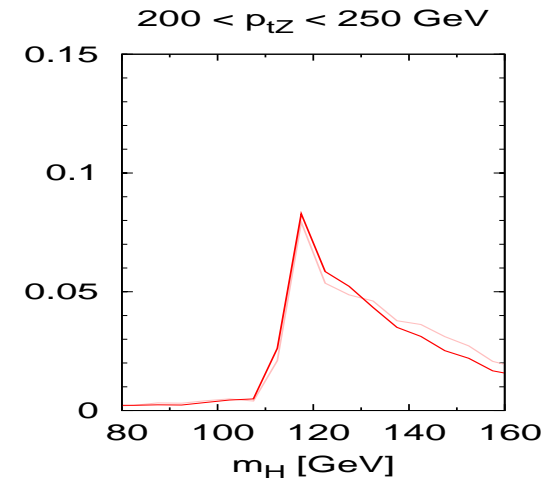
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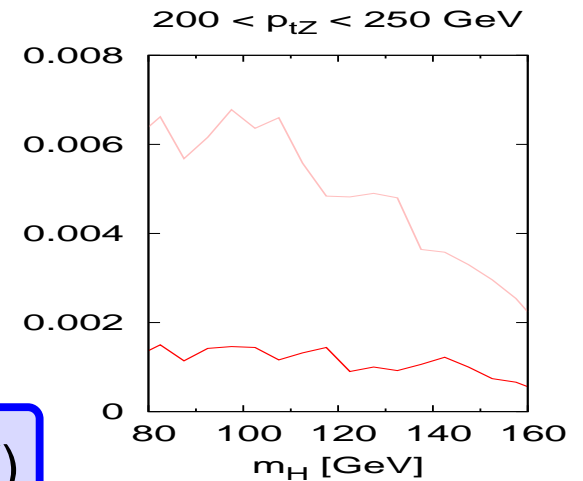


Split:  $\frac{\max(m_1, m_2)}{m} = 0.37$ , mass drop ( $m = 139$  GeV)

## $HZ$ Signal

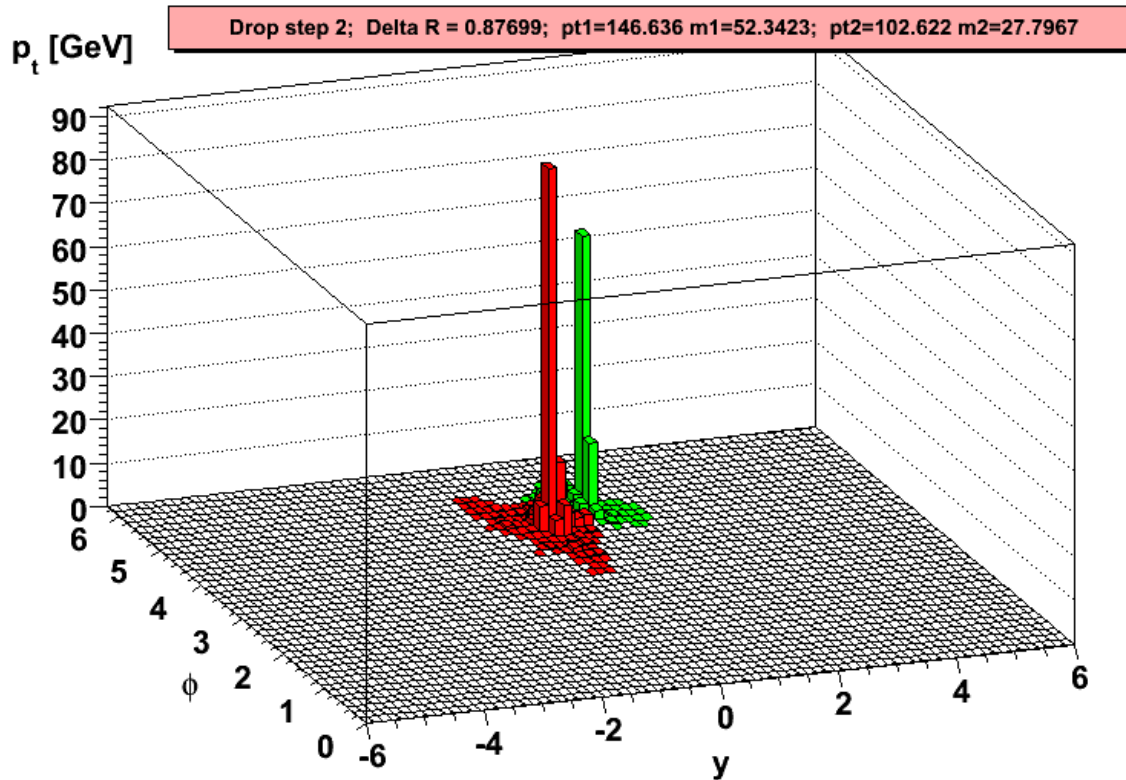


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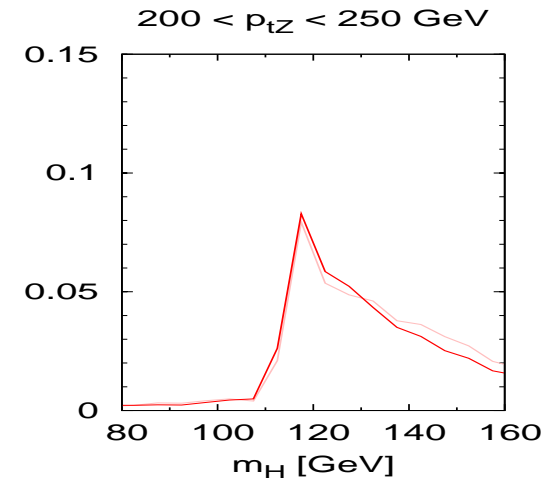
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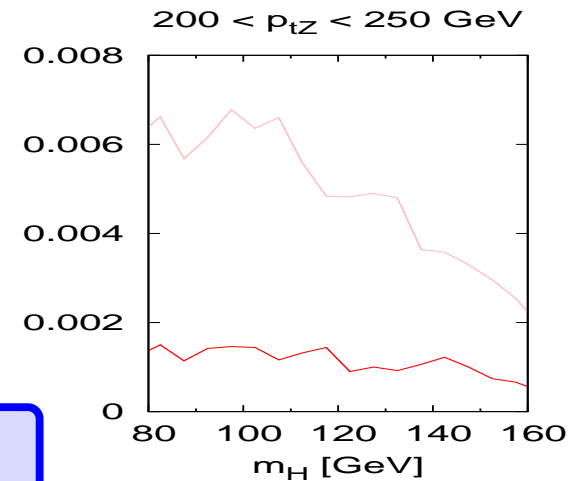


Split:  $y_{12} = 0.7$ , 2  $b$  tags  $\Rightarrow$  OK ( $m = 139$  GeV)

## $HZ$ Signal

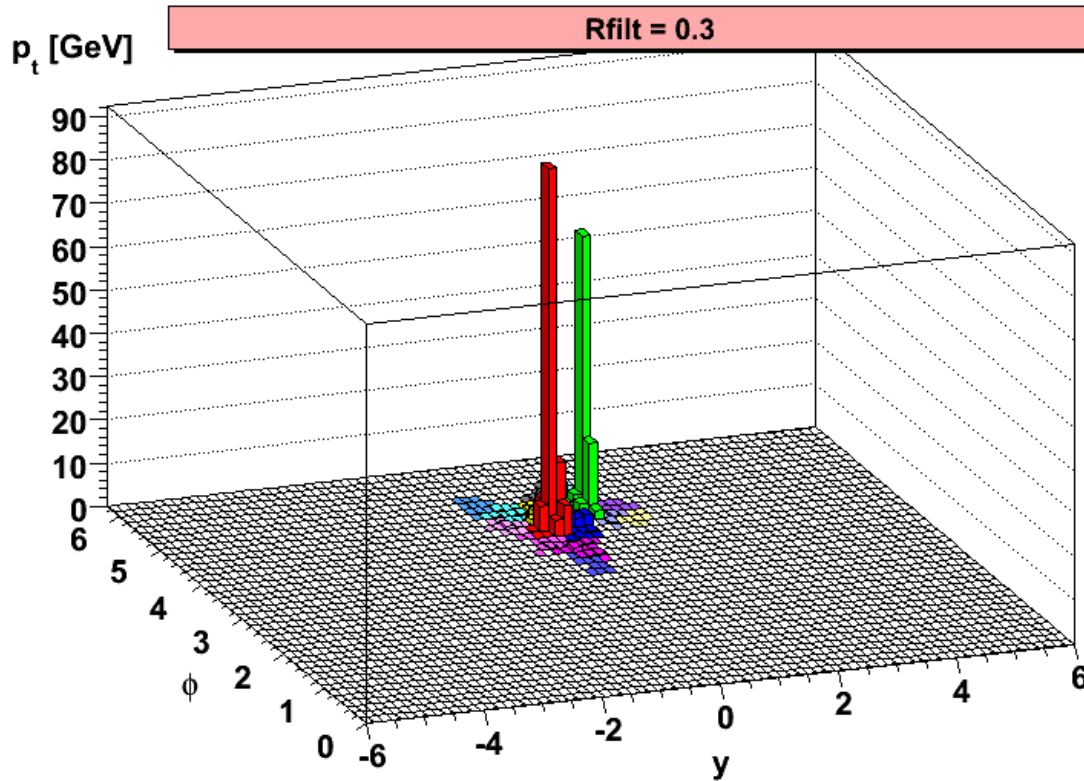


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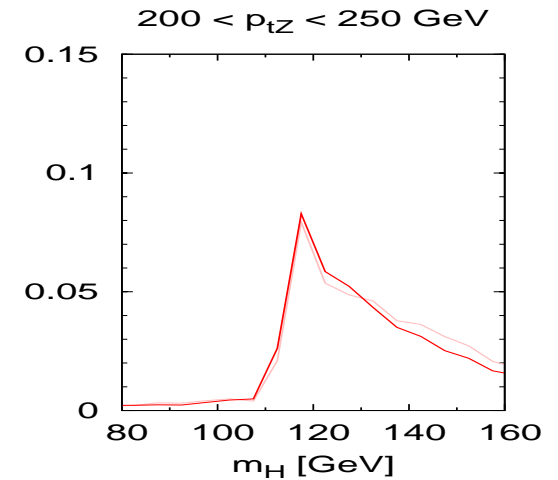
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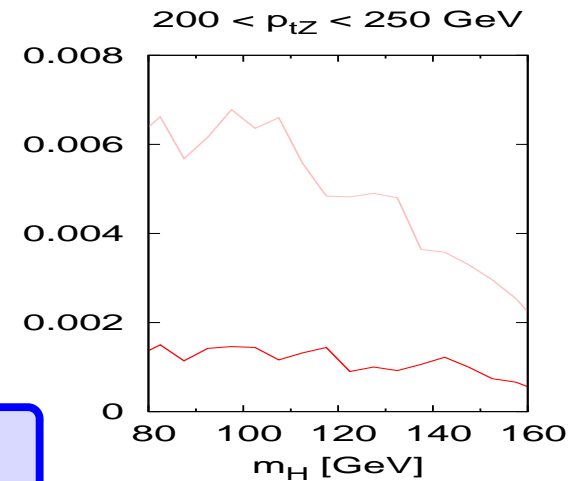


Re-cluster:  $R_{\text{filt}} = 0.3$

## $HZ$ Signal



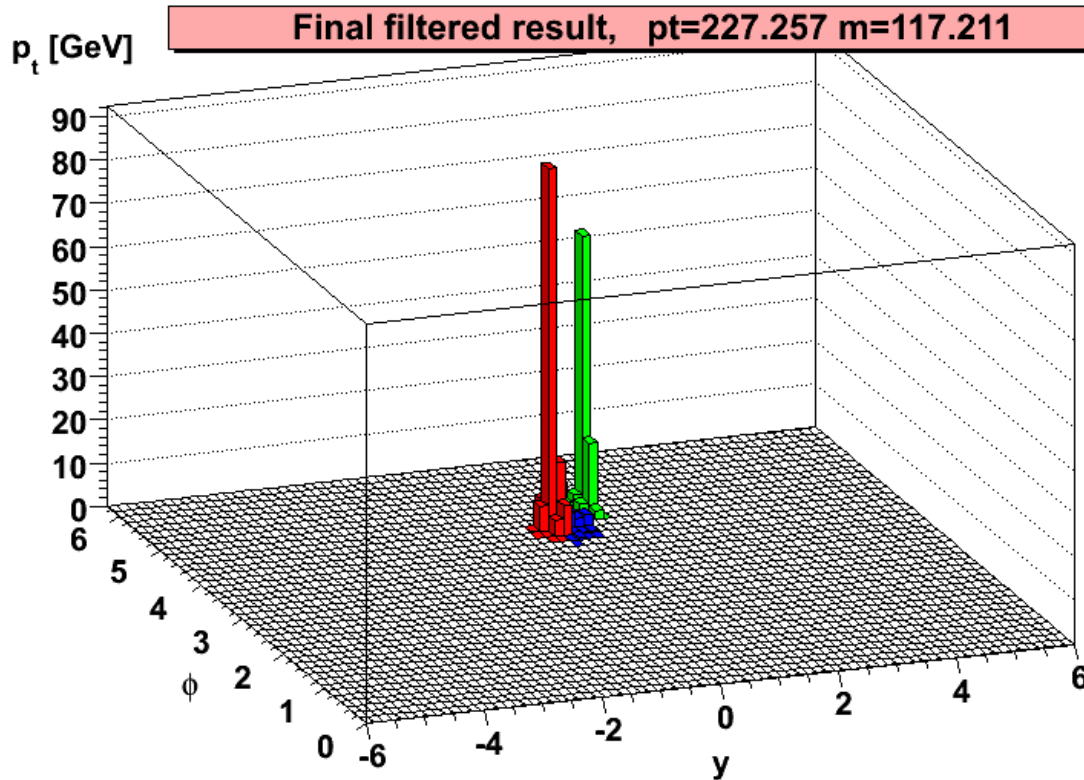
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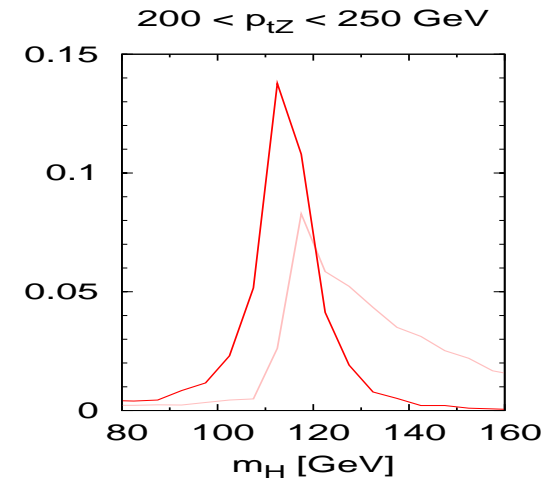
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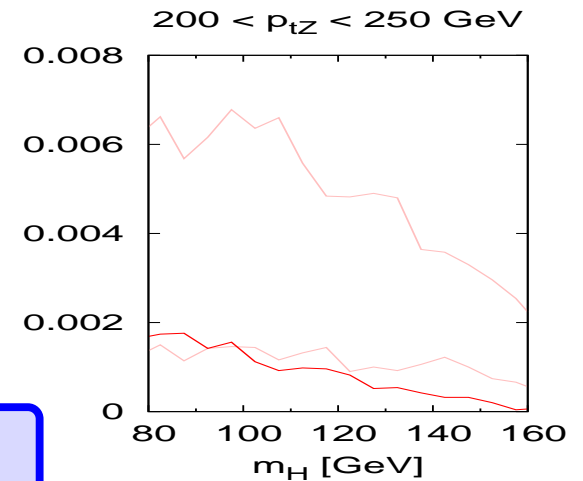


Filter: keep 3 hardets ( $m = 117$  GeV)

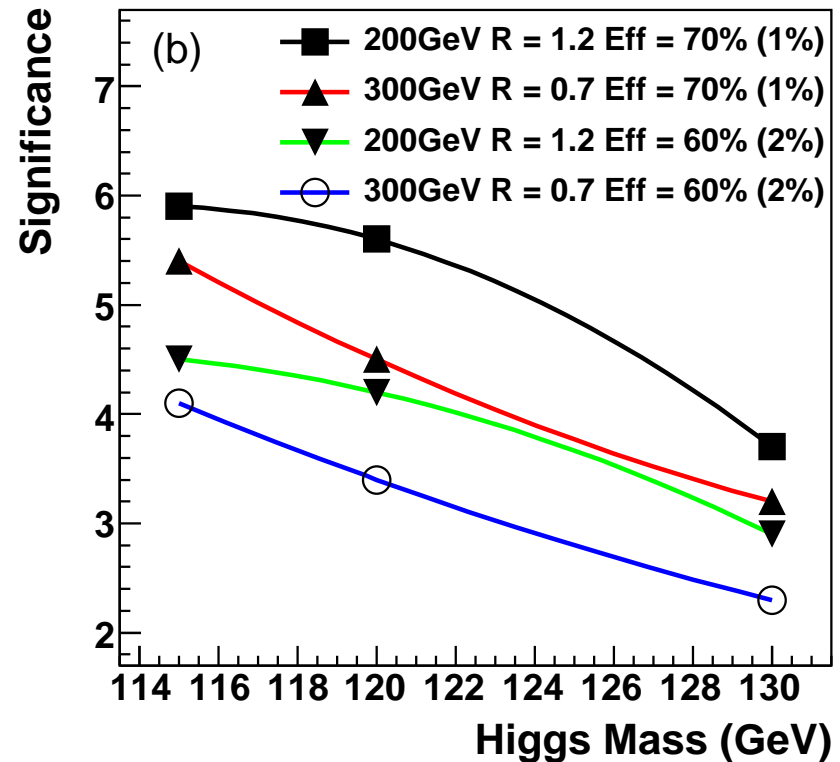
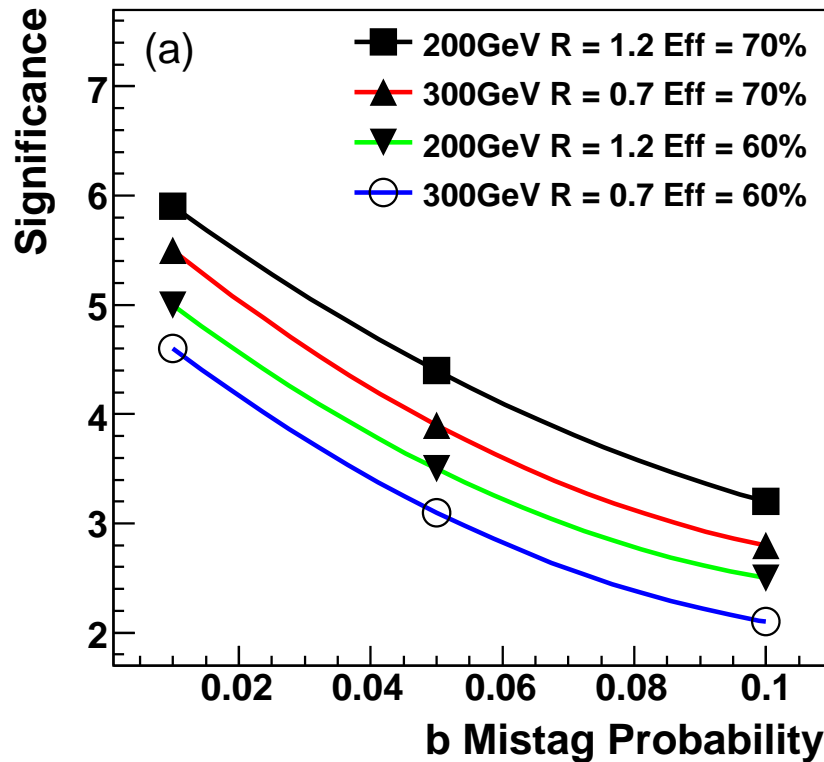
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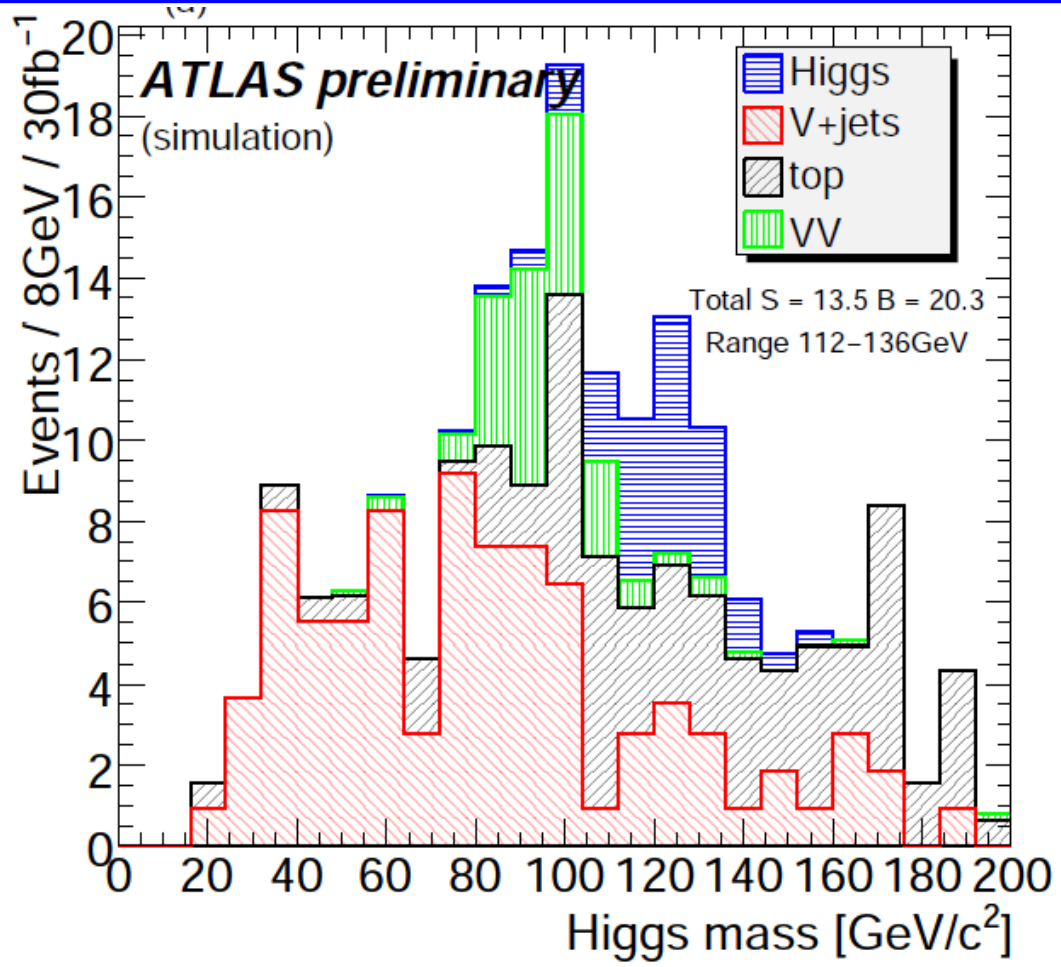
More than  $3\sigma$  for most scenarios ( $30 \text{ fb}^{-1}$ )

Filter: keep 5 hardest ( $m = 117 \text{ GeV}$ )

$m_H$  [GeV]

160

# Boosted Higgs: one event, effects on $S/B$



Under consideration in ATLAS (here  $WZ \rightarrow l\nu b\bar{b}$ , 30 fb<sup>-1</sup>)

Filter: keep 5 hardest ( $m = 117$  GeV)

# Conclusions

- Finally a set of **jet algs** meeting the fundamental requirements  
*i.e.* **Infrared-and-collinear-safe** and **fast**
- Allows **better/advanced usage of jets at the LHC**
  - **jet areas** for background subtraction
  - **jet substructure** for boosted-objects tagging
  - **UE-sensitivity** using filtering/trimming
- **Future**: improve in those directions
- *e.g.* towards **analytic understanding/optimisation**

## ***Additional topics:*** ***Optimisation***

***[M.Cacciari,J.Rojo,G.Salam,GS, 08]***

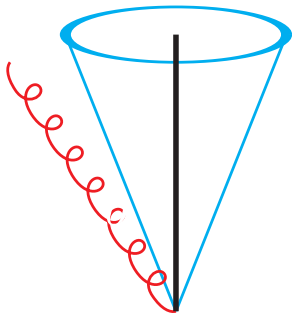
***[M.Dasgupta,L.Magnea,G.Salam, 08]***

***[GS, 10]***

# Optimisation: underlying idea

Competition between

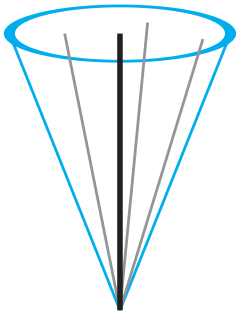
- catching perturbative radiation



Out-of-cone radiation:

$$\langle \delta p_t \rangle \propto - \int_R \frac{d\theta}{\theta} \sim -\log(1/R)$$

- not catching soft background radiation (underlying event)



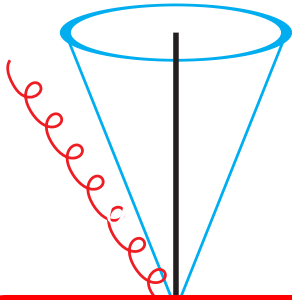
$$\langle \delta p_t \rangle \sim \text{Soft contents} \propto \text{jet area} \sim R^2$$

the coefficients depend on the algorithm

# Optimisation: underlying idea

Competition between

- catching perturbative radiation

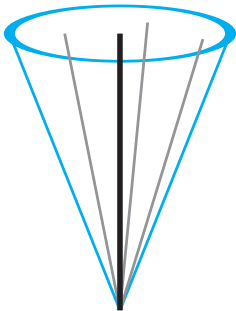


Out-of-cone radiation:

$$\langle \delta p_t \rangle \propto - \int_R \frac{d\theta}{\theta} \sim -\log(1/R)$$

What is the optimal jet definition (algo+ $R$ )?

- not



$$\langle \delta p_t \rangle \sim \text{Soft contents} \propto \text{jet area} \sim R^2$$

the coefficients depend on the algorithm

Example process to illustrate various effects:

$$Z' \rightarrow q\bar{q} \rightarrow 2 \text{ jets}$$

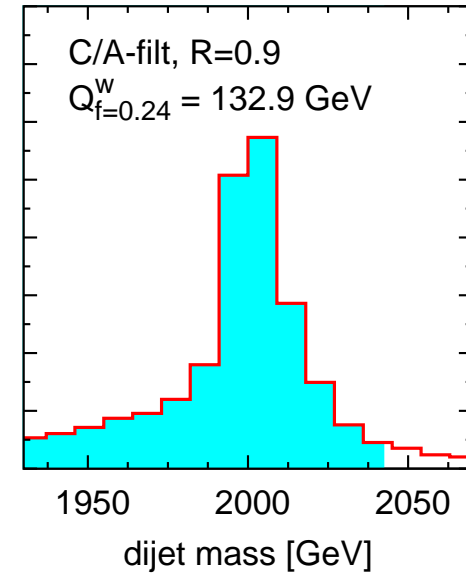
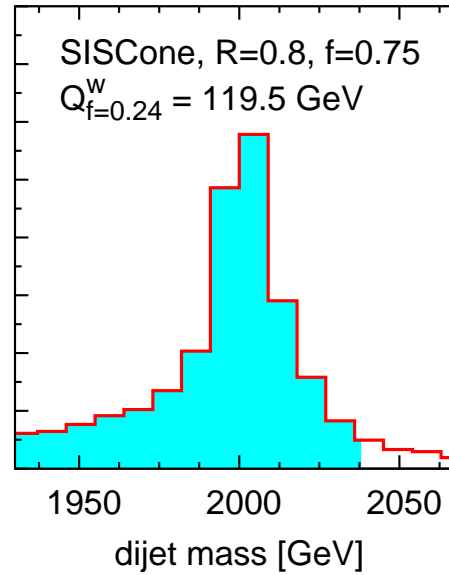
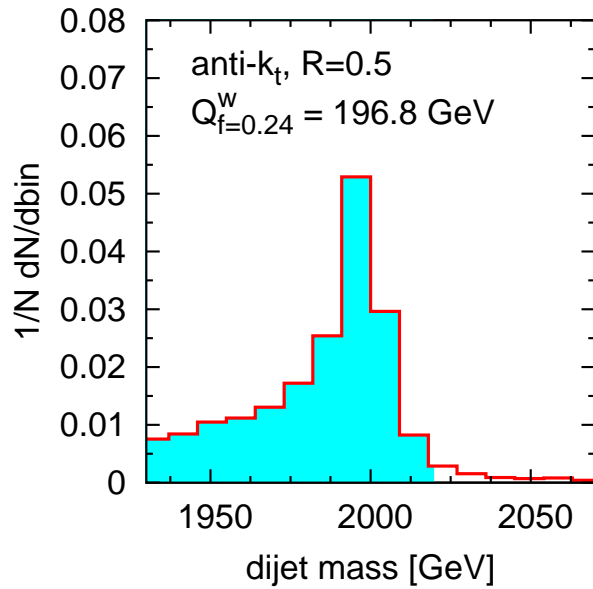
- $M_{Z'}$  can be varied (between 100 GeV and 4 TeV)
- Also valid for  $H \rightarrow gg$  to study gluon jets
- Reconstruction method:
  - get the 2 hardest jets:  $j_1$  and  $j_2$
  - reconstruct the  $Z'$ :  $m_{Z'} = (j_1 + j_2)^2$

Look how the mass peak is reconstructed

- Also  $t\bar{t}$  with full hadronic decay for multijet tests

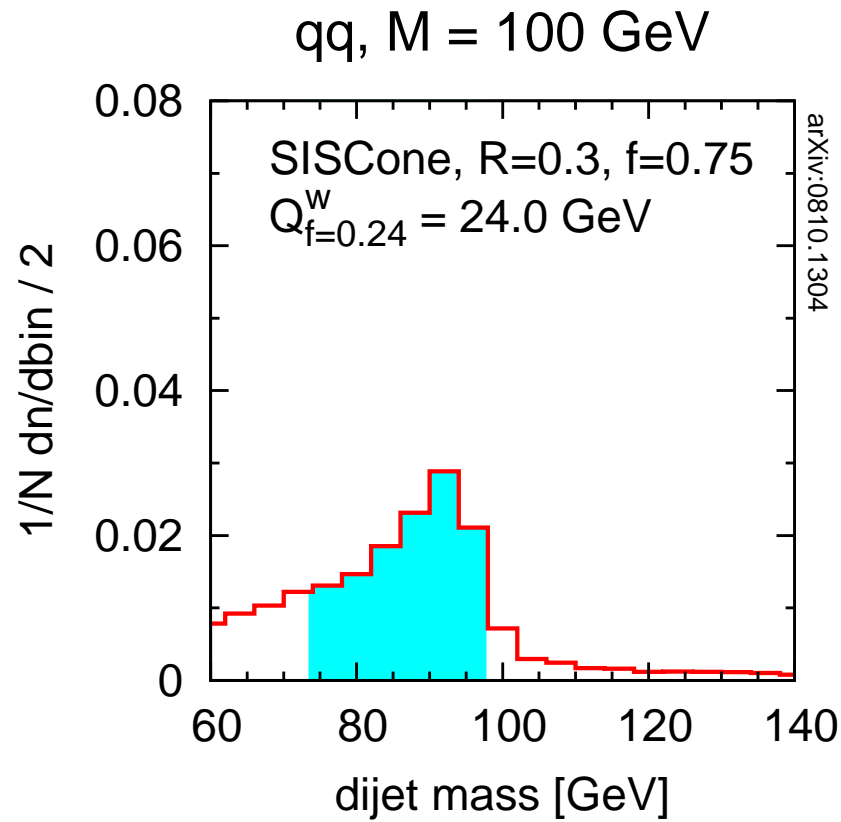


# Observations



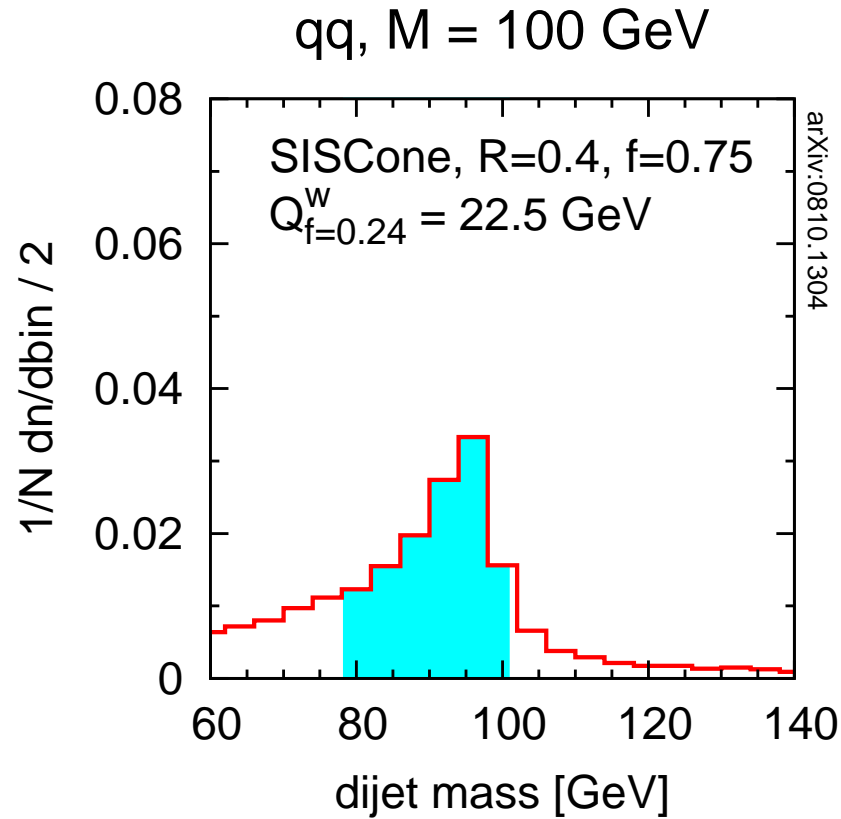
qq 2 TeV

# Observations



Histogram:  
fixed mass, algorithm

# Observations

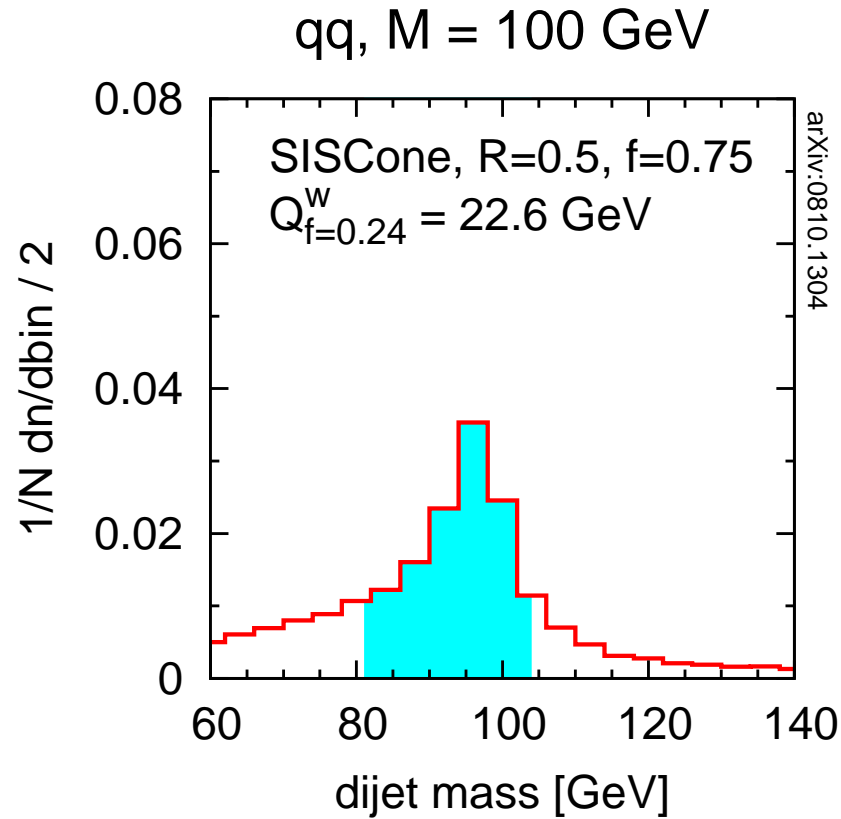


Histogram:

fixed mass, algorithm

vary  $R$

# Observations

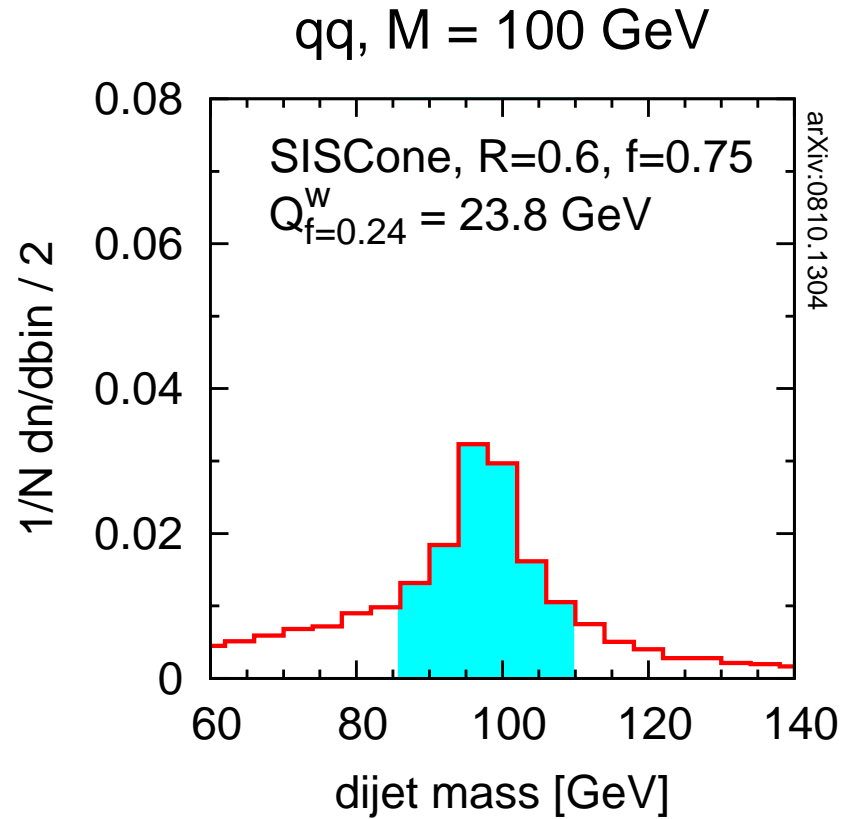


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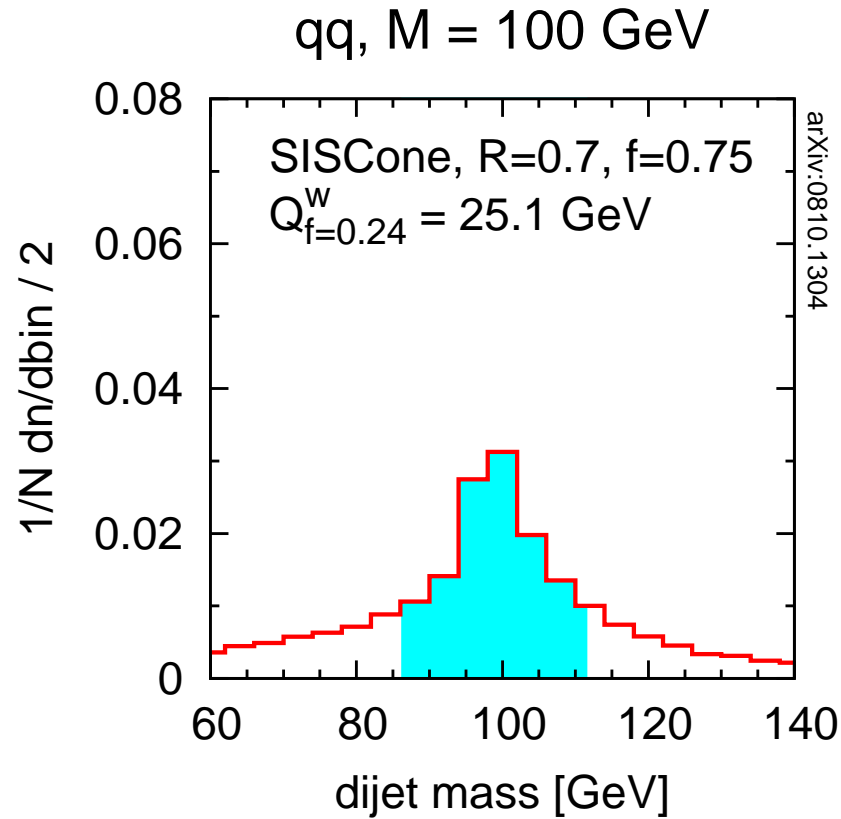


Histogram:

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vary  $R$

# Observations

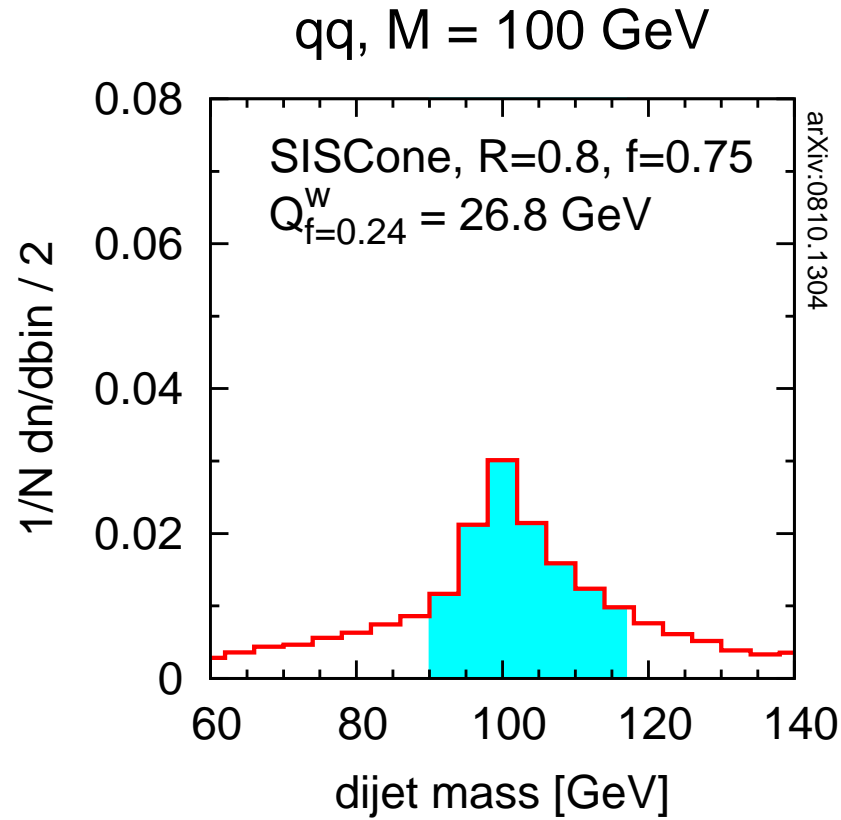


Histogram:

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vary  $R$

# Observations

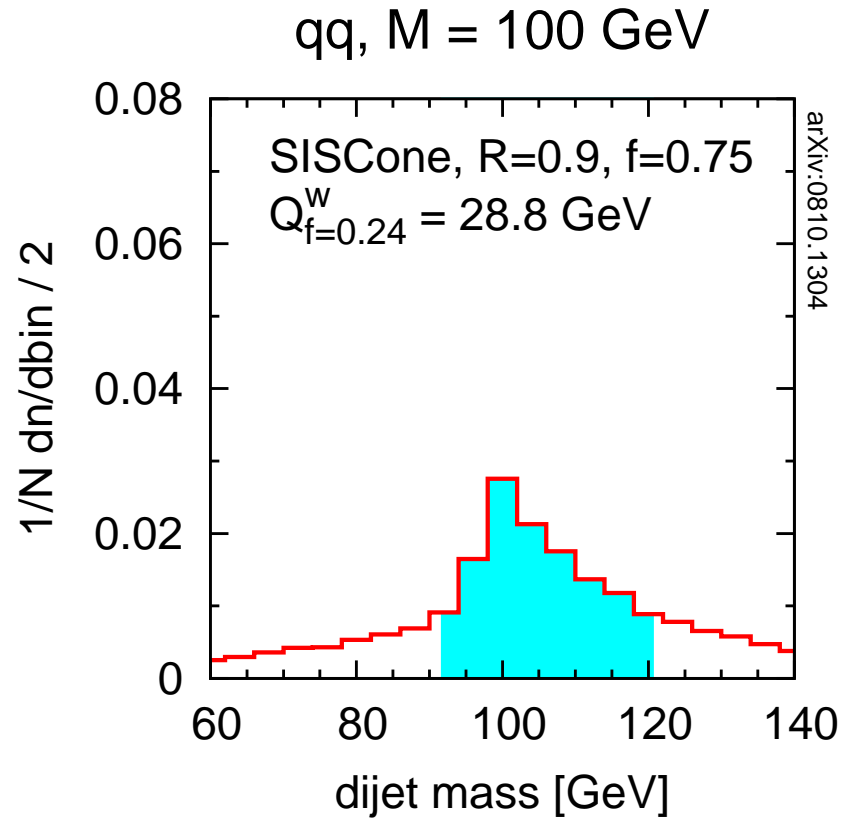


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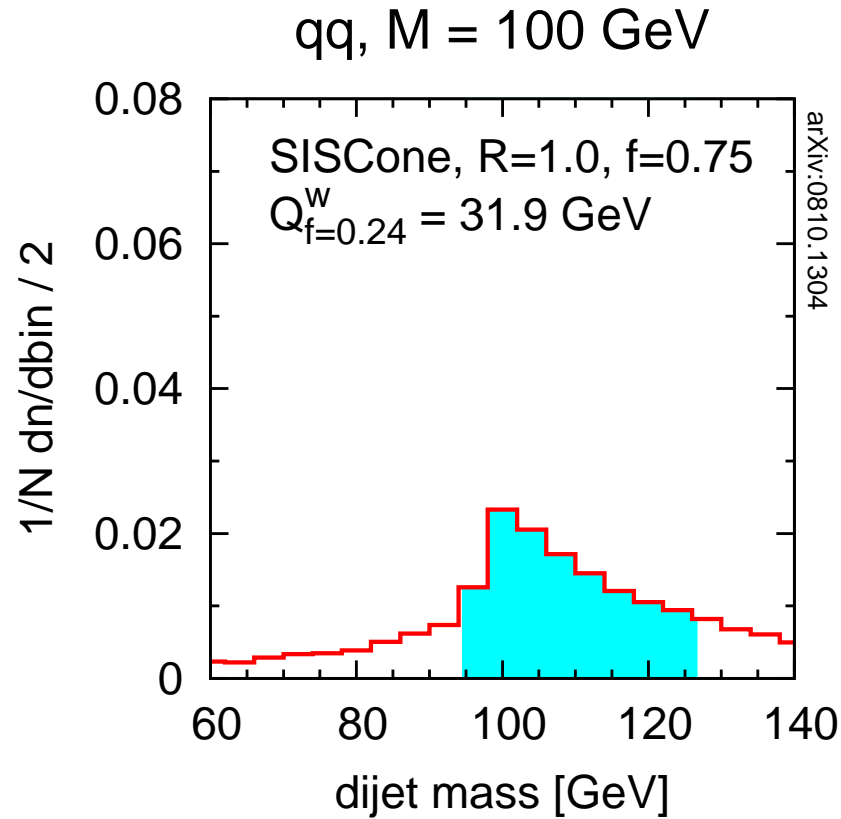


Histogram:

fixed mass, algorithm  
vary  $R$



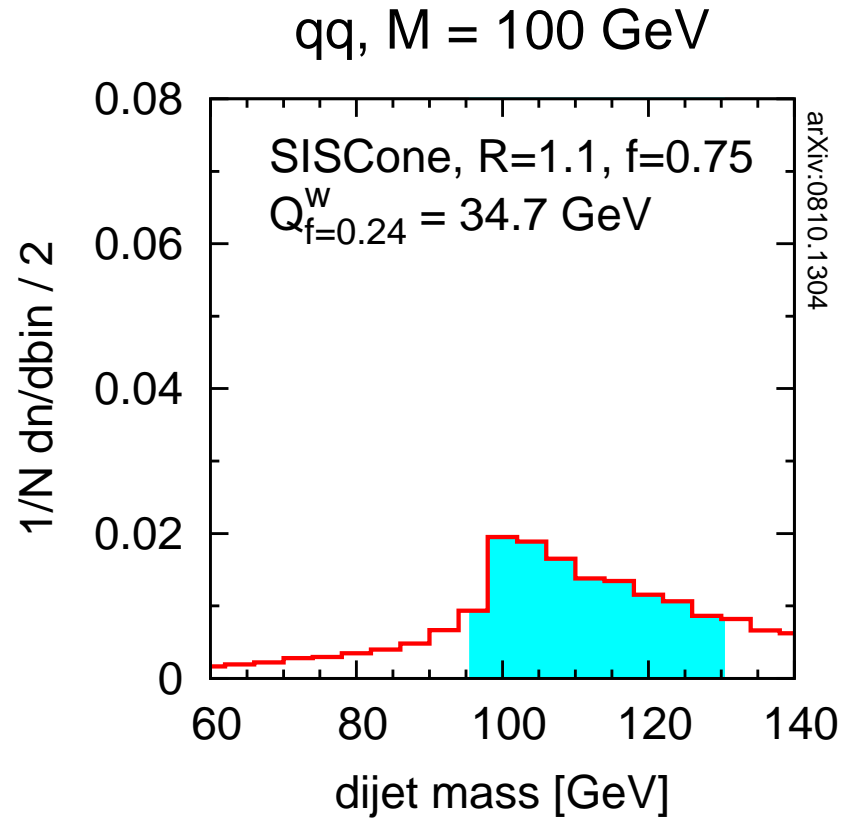
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Histogram:

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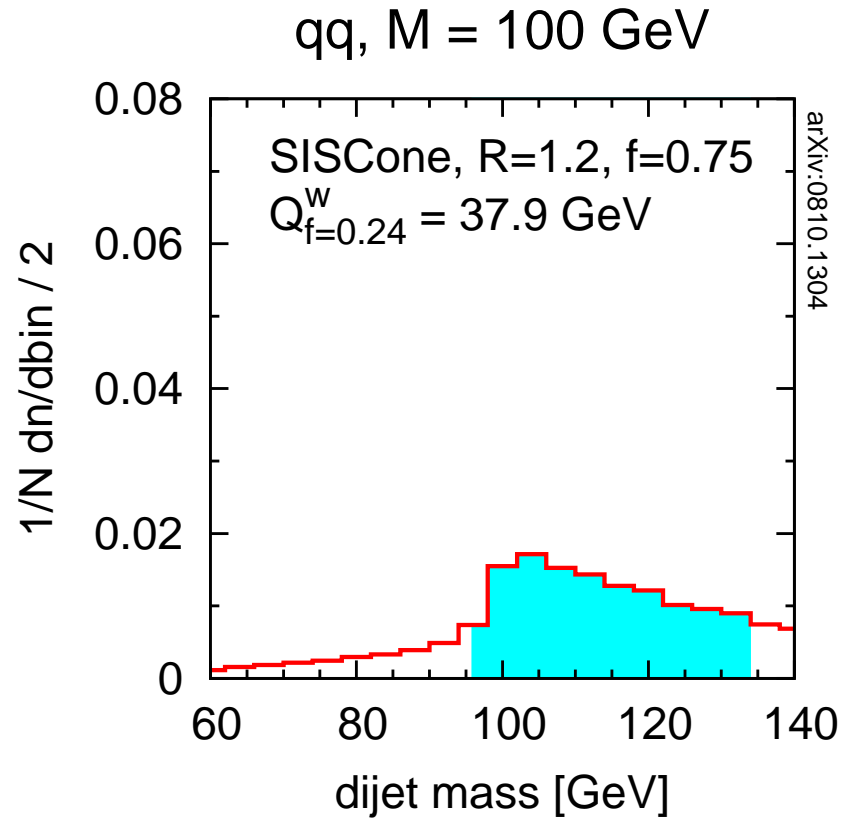
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Histogram:

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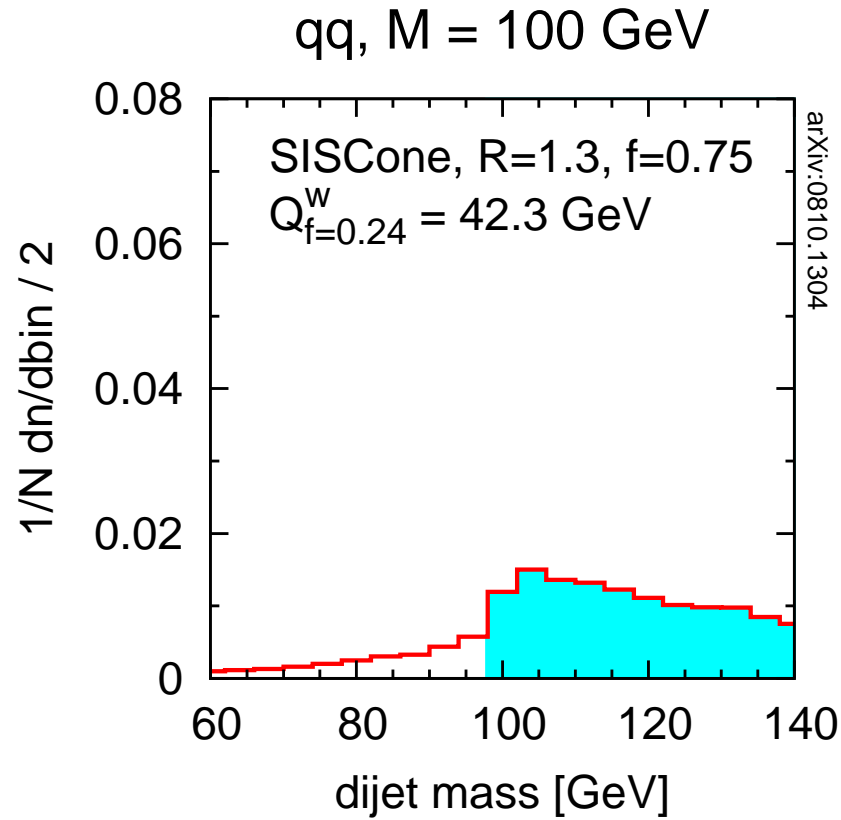
# Observations



Histogram:

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# Observations

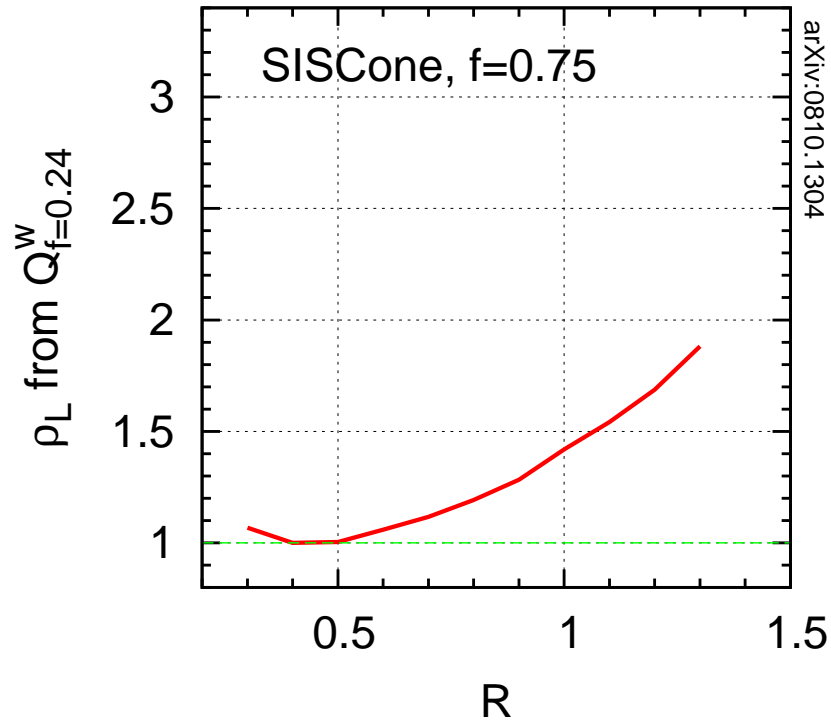


Histogram:

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# Observations

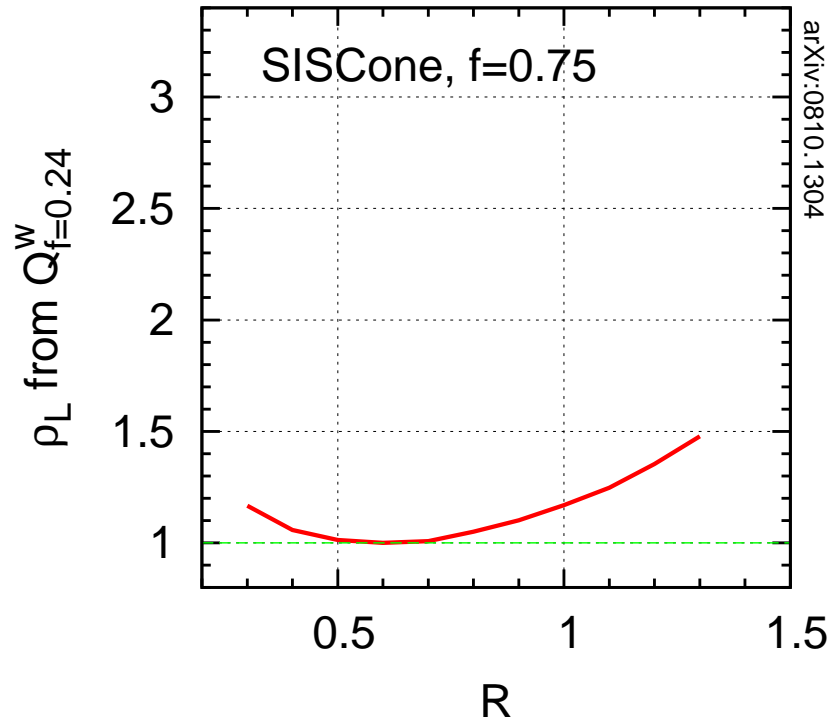
qq,  $M = 100$  GeV



Width vs.  $R$ :  
fixed algorithm

# Observations

qq,  $M = 200$  GeV



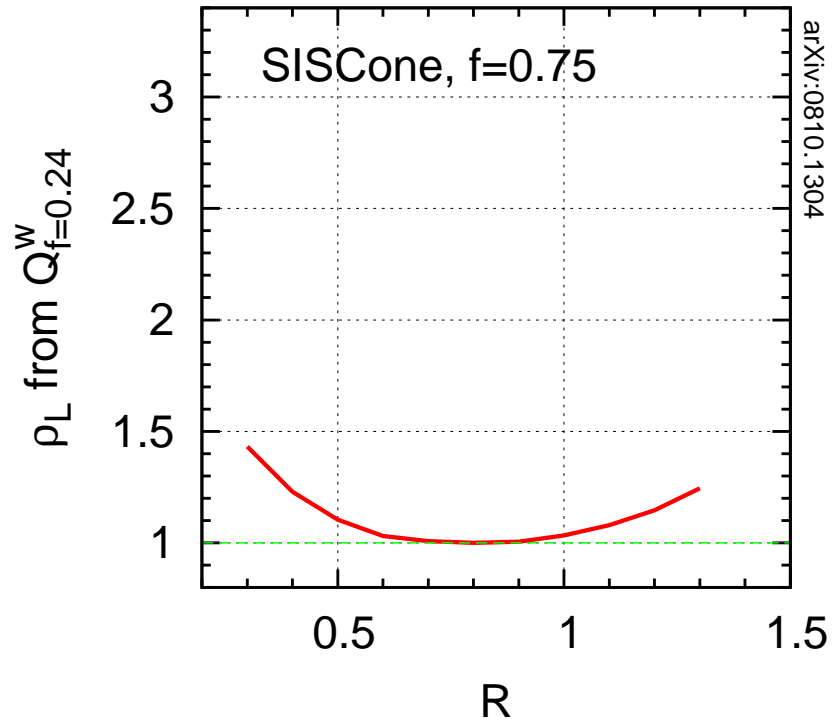
Width vs.  $R$ :

fixed algorithm

vary  $M$

# Observations

qq,  $M = 500$  GeV



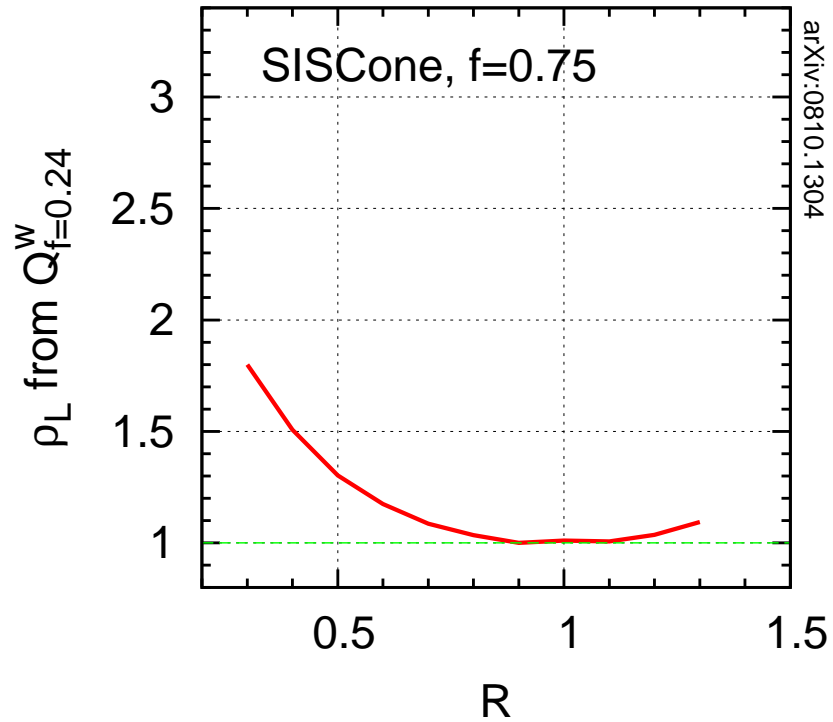
Width vs.  $R$ :

fixed algorithm

vary  $M$

# Observations

qq,  $M = 1000$  GeV



Width vs.  $R$ :

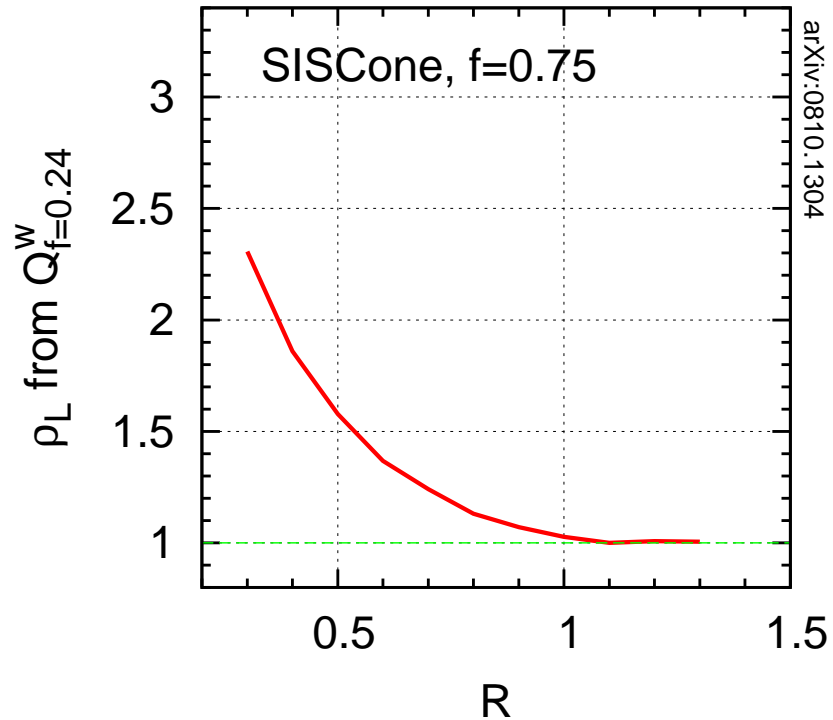
fixed algorithm

vary  $M$



# Observations

qq,  $M = 2000$  GeV



Width vs.  $R$ :

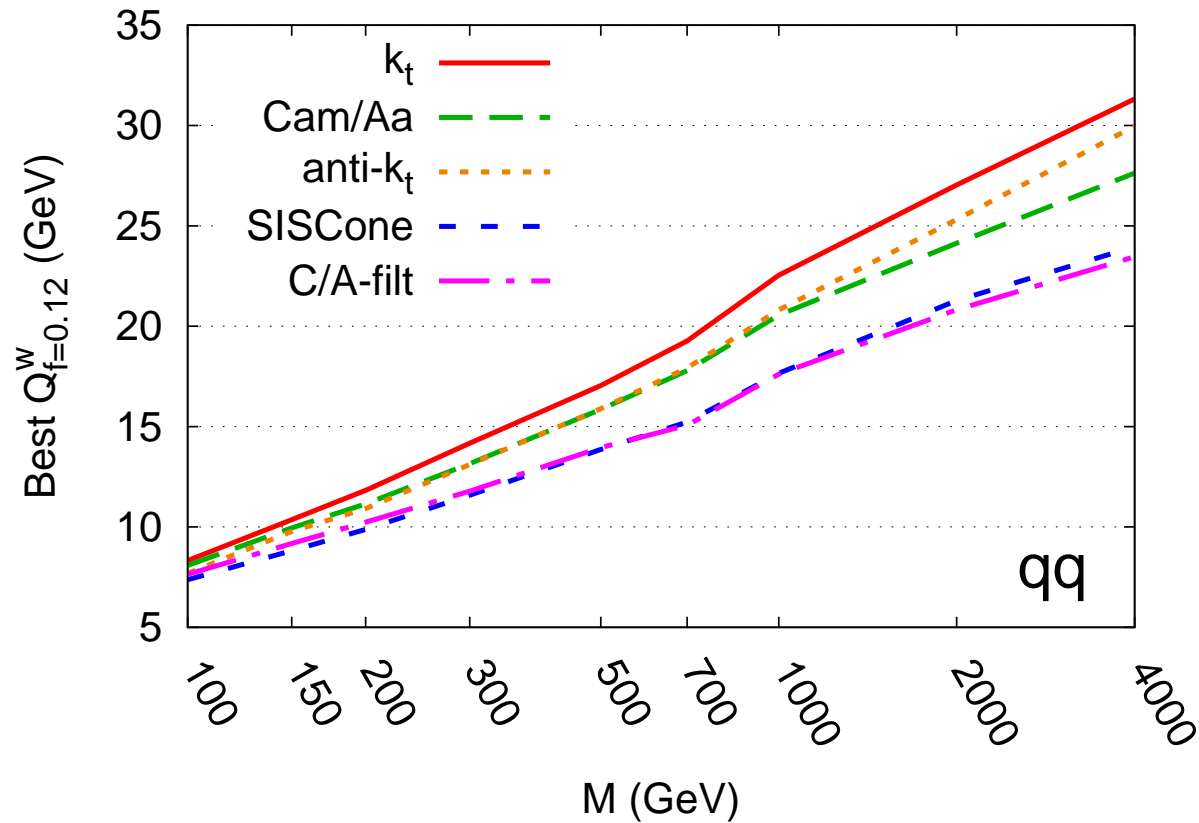
fixed algorithm

vary  $M$

In summary:

- width vs.  $R$ : **strong  $R$  dependence**

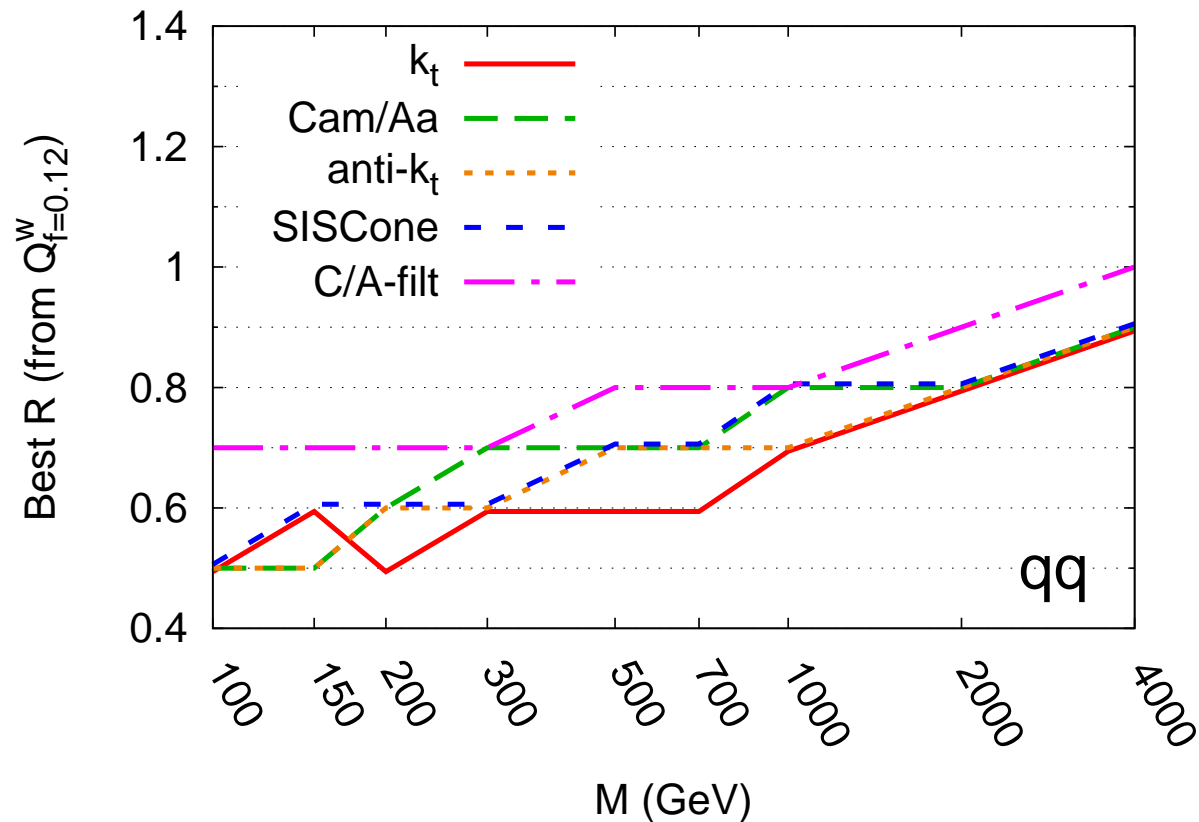
# Observations



In summary:

- width vs.  $R$ : **strong  $R$  dependence**
- optimal width vs.  $M$ : **SISCone, C/A(filt) preferred**

# Observations



In summary:

- width vs.  $R$ : **strong  $R$  dependence**
- optimal width vs.  $M$ : **SISCone, C/A(filt) preferred**
- optimal  $R$  vs.  $M$ :  **$R_{\text{best}}$  increases with  $M$**

# Towards analytics

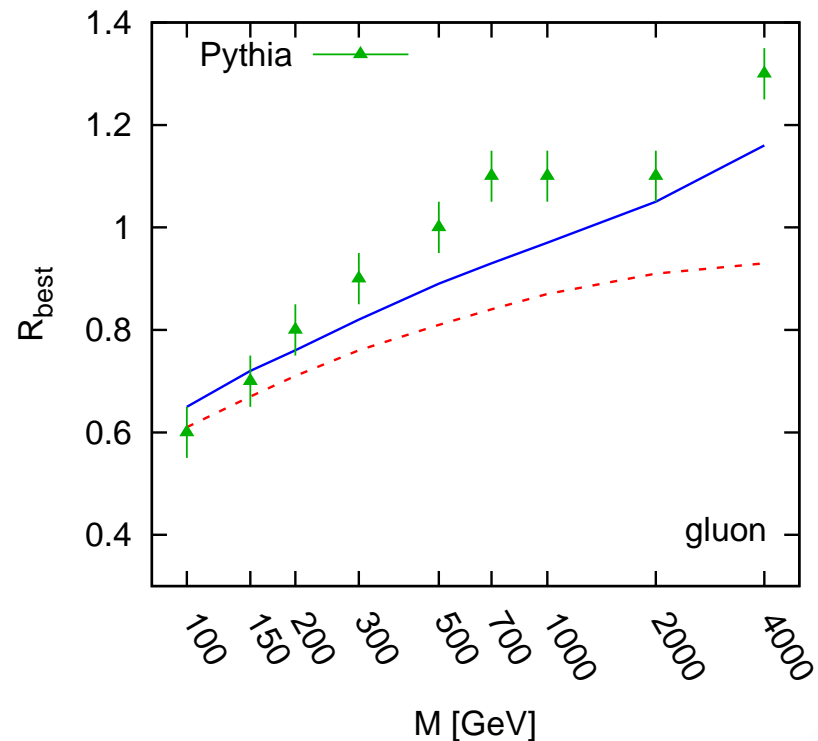
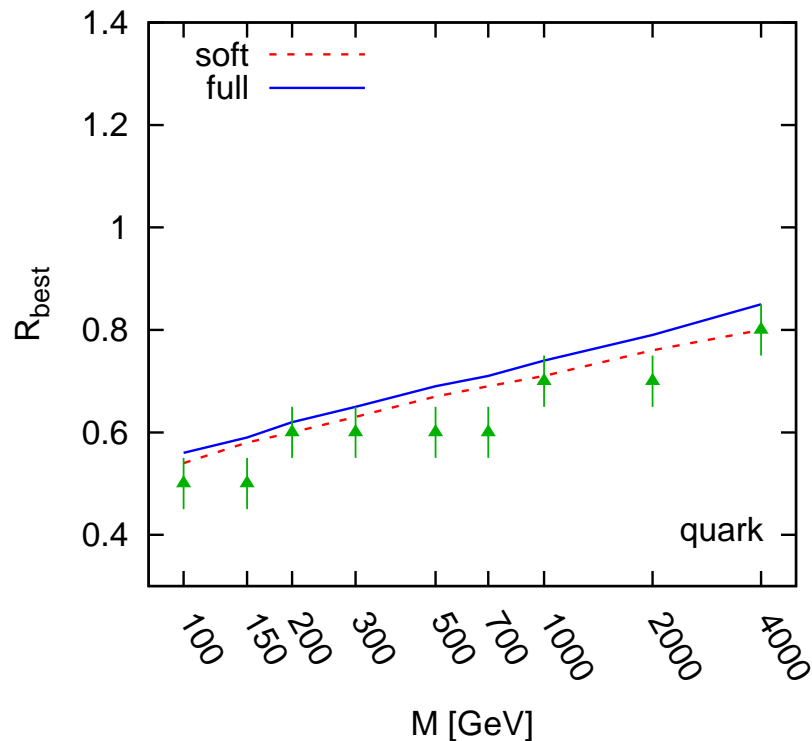
Analytic computation of the histogram including:

- **pert. final-state radiation: loss**  $\propto \alpha_s M \log(1/R)$
- **pert. initial-state radiation: gain**  $\propto \alpha_s M R^2$  (+PDFs)
- **UE contamination: gain**  $\propto \rho_{\text{UE}} R^2$

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***Additional topic:  
the FastJet interface***

# Future of FastJet

FastJet 3.0 on its way (3.0alpha1 on January the 26th):

- Interface: a jet knows about its clustering, *e.g.*

```
clust_seq.constituents(jet);  
→ jet.constituents();
```

- Generic additional info in PseudoJet: `jet.extra_info()`

- `Selector` for selecting objects in a list, *e.g.*

```
Selector jet_sel =  
    SelectorMaxAbsRap(2.5) && SelectorPtMin(20);  
jets = jet_sel(clust_seq.inclusive_jets());
```

- Improved bkgd subtraction: `BackgroundEstimator`

- FastJet tools *e.g.* `Filter`

***Additional topic:***  
***dijet asymmetries in  $PbPb$***

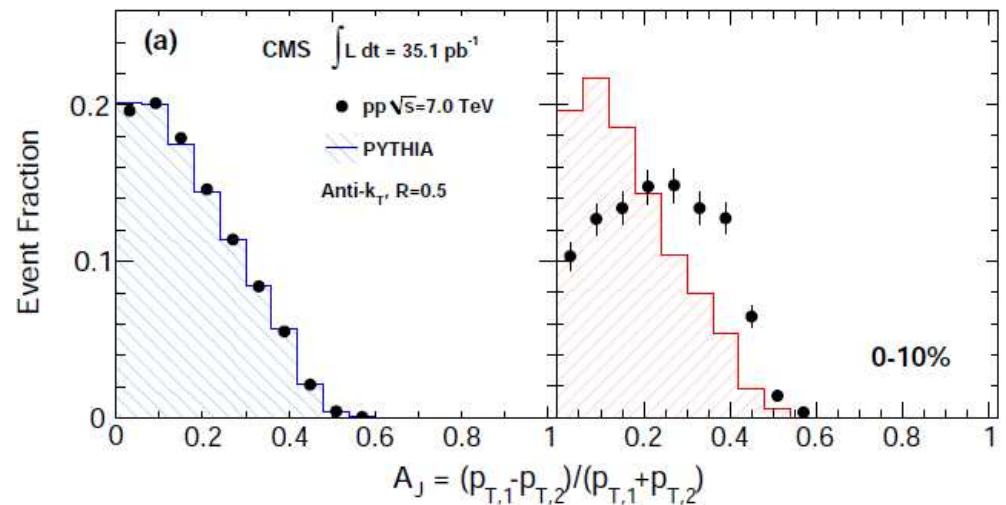
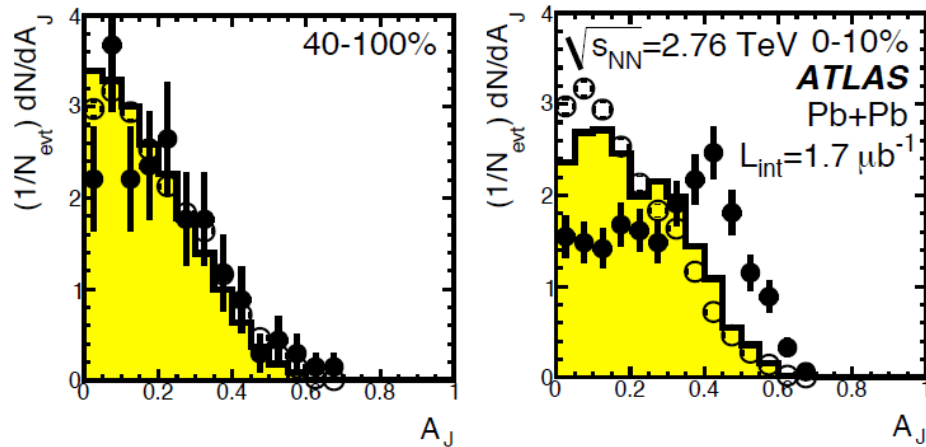


# Asymmetry measurement

Fully reconstructed (and subtracted) jets in  $PbPb$  coll.

$$A_J = \frac{p_{t,1} - p_{t,2}}{p_{t,1} + p_{t,2}}$$

Physics interpretation:  
more frequent large  $A_J$  due to jet quenching



# *Quantitative interpretation?*

## Warning:

background fluctuations go in the same direction  
might affect quantitative estimate of quenching effects!

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might affect quantitative estimate of quenching effects!

Ex.: Pythia+Gaussian smearing(width  $\sigma_{\text{jet}}$ )

