

EPS nPDFs & heavy boson production at the LHC

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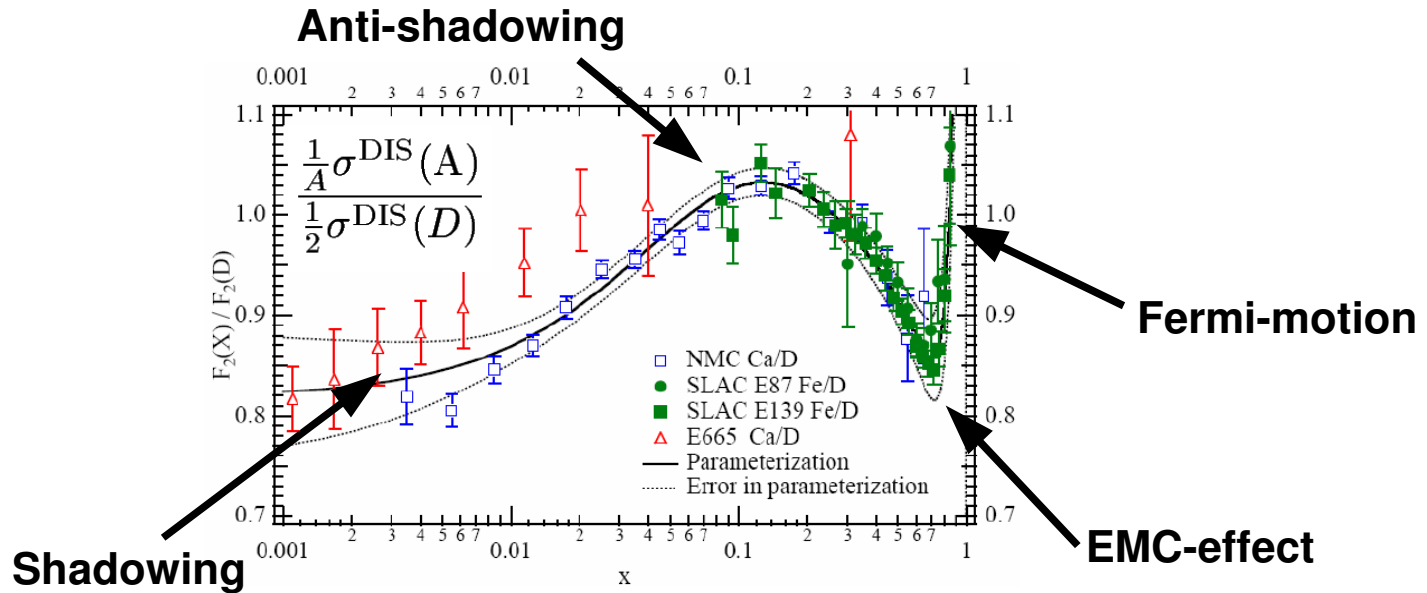
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nPDFs: Testing the factorization



- Nuclear modifications in experimental cross-sections:
 $\sigma_{\text{bound nucleon}} \neq \sigma_{\text{free nucleon}}$
- Various analyses indicate that such effects can be factorized to the universal nuclear PDFs: *EPS09, HKN07, nDS, nCTEQ...*

$$\sigma_{AB \rightarrow h+X} = \sum_{ij} \underbrace{f_i^A(x_1, Q^2) \otimes f_j^B(x_2, Q^2)}_{\text{Nuclear PDFs, obeying DGLAP equations}} \otimes \underbrace{\sigma^{i+j \rightarrow h+X}}_{\text{Standard pQCD cross-sections}}$$

12 years of EPS-studies

- **1998: EKS98** (Eskola, Kolhinen, Ruuskanen, Salgado) **LO**
The pioneering work – demonstrated that the factorization works for
$$e+A \rightarrow e + X \quad (DIS)$$
$$p+A \rightarrow \mu^+ + \mu^- + X \quad (Drell-Yan)$$
The “fit” was done by eye.
- **2007 : EKPS** (Eskola, Kolhinen, Paukkunen, Salgado) **LO**
Reanalysis of EKS98 – automated minimization (MINUIT) and a first try to estimate the uncertainties.
- **2008 : EPS08** (Eskola, Paukkunen, Salgado) **LO**
Motivated by small- p_T suppression of BRAHMS pion data, the purpose was to study how strong gluon suppression at small- x would be possible.
- **2009 : EPS09** (Eskola, Paukkunen, Salgado) **LO & NLO**
The analysis extended to NLO and an error analysis “a la CTEQ” was carried out.

Experimental constraints in EPS09

- Three types of data:

Deeply inelastic scattering: $e + A \rightarrow e + X$

Drell-Yan dilepton production: $p + A \rightarrow \mu^+ + \mu^- + X$

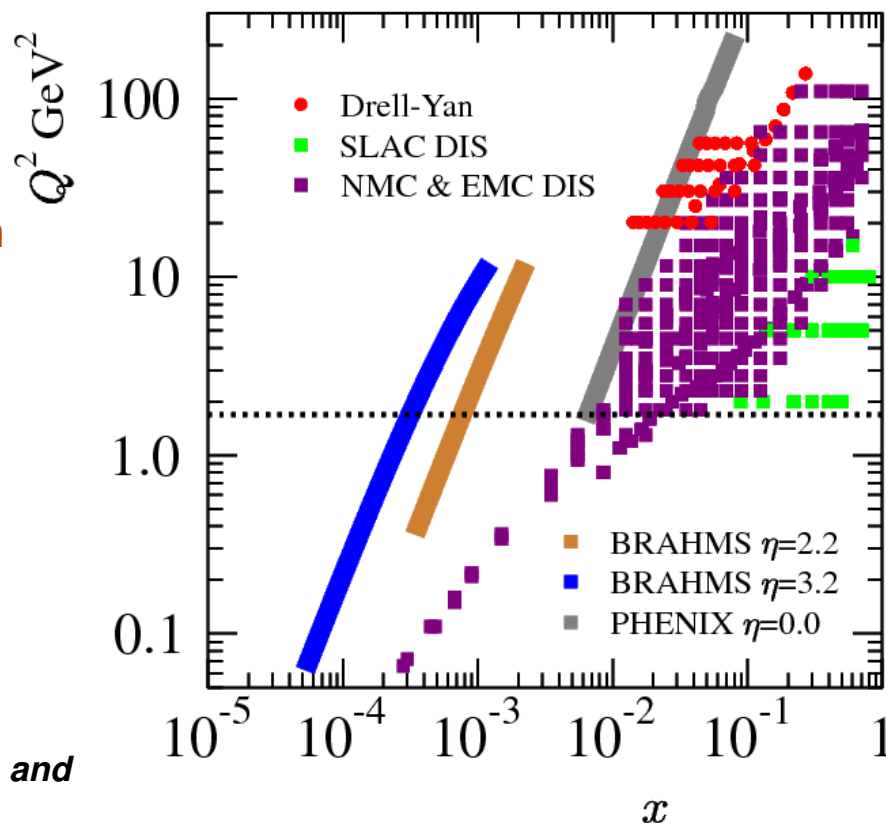
Inclusive pion production: $d + Au \rightarrow \pi + X$

- Mutual consistency between the data sets is necessary. For example:

- HERMES DIS data display a Q^2 -dependence not in agreement with other data. Not used.

- The forward rapidity pions from BRAHMS display tension with other data. Not used.

- Compatibility of the neutrino-nucleus DIS data with the rest is still under discussion. See e.g. *JHEP* 1007 (2010) 032, and *aXiv:1012.0286*.



The Framework of EPS09

- The bound proton PDFs $f_i(x, Q)$ in a nucleus A are defined as

$$f_i^A(x, Q^2) \equiv R_i^A(x, Q^2) f_i^{\text{CTEQ6.1M}}(x, Q^2)$$

- $\overline{\text{MS}}$, Zero-mass variable flavour number scheme

Our studies utilizing the SACOT-prescription (with e.g. CTEQ6.6) for the heavy quarks do not display large deviations from the zero-mass results in the regions constrained by the data.

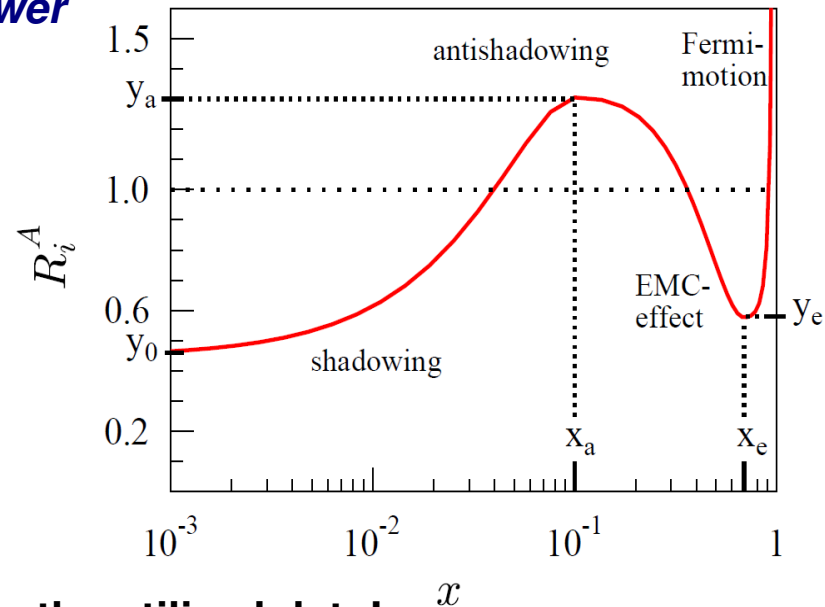
➔ *One may safely use EPS09 also with newer sets of CTEQ6.6, CT10, etc...*

- The nuclear modifications are parametrized at initial scale $Q_0=1.3 \text{ GeV}$

$R_V^A(x, Q_0^2)$ for all valence quarks

$R_S^A(x, Q_0^2)$ for all sea quarks

$R_G^A(x, Q_0^2)$ for gluons

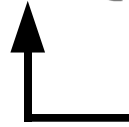


- The flavor-separation not well constrained by the utilized data!

The Framework of EPS09

- The optimal parameters are found by minimizing χ^2

$$\chi^2 \equiv \sum_N w_N \sum_{i \in N} \left(\frac{D_i - T_i}{\sigma_i} \right)^2$$



Some data sets are assigned an extra weight to improve the convergence of the fit. → Somewhat too optimistic nPDF errors?

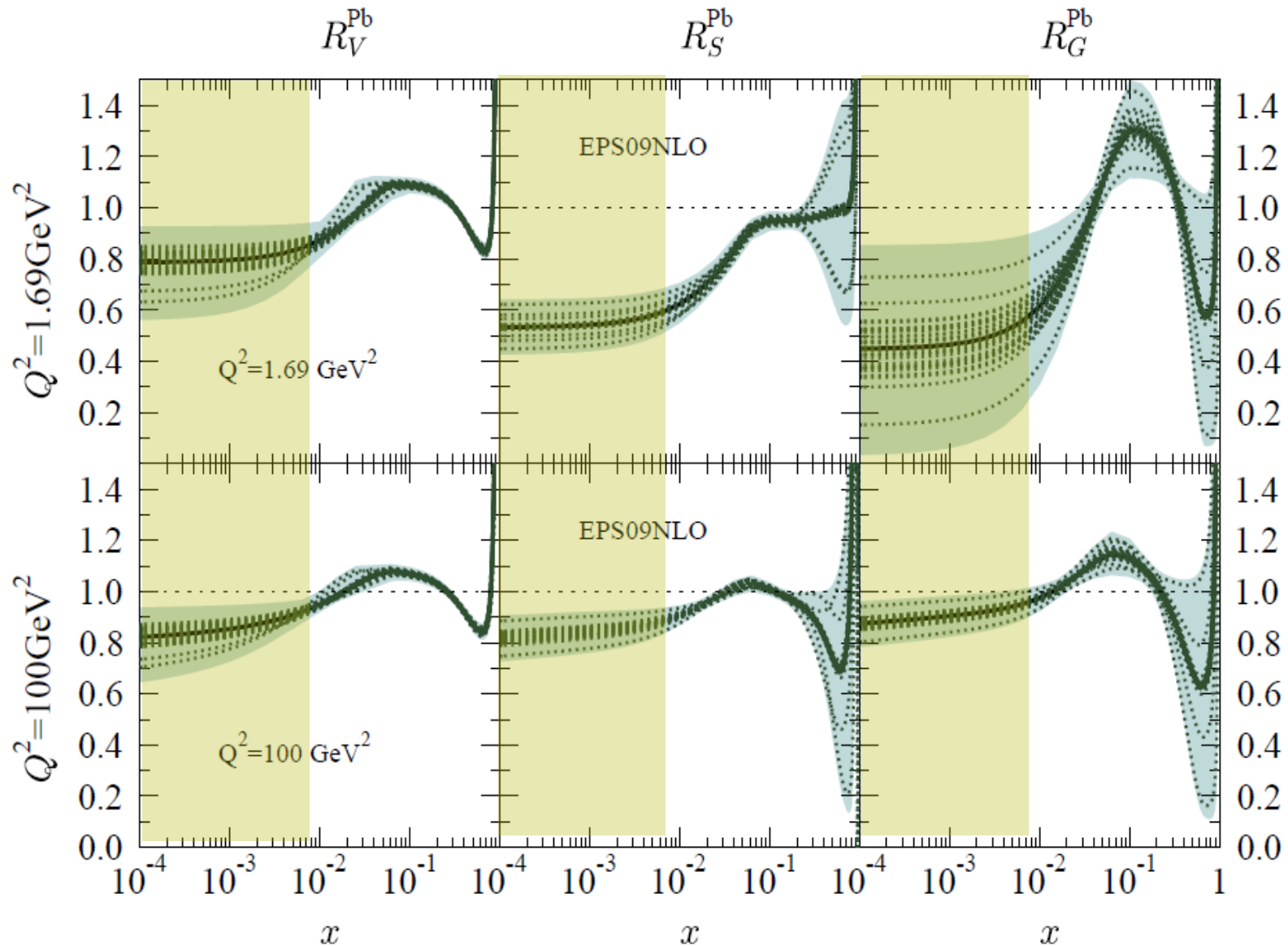
- We apply the Hessian error analysis approximating the χ^2 close to the minimum by

$$\chi^2(\{a_i\}) \approx \chi_0^2 + \sum_{ij} \delta a_i H_{ij} \delta a_j = \chi_0^2 + \sum_i z_i^2$$

- The uncertainty sets of nPDFs are constructed in z-space by requiring each data set to remain roughly within its "90% confidence limits".
- Uncertainty in any nPDF-dependent quantity X can be estimated by (S_0 is the central set and S_i^\pm the error sets)

$$\Delta X^{+\setminus-} = \sqrt{\sum_i \max \setminus \min [X(S_i^+) - X(S_0), X(S_i^-) - X(S_0), 0]^2}$$

EPS09NLO for Lead



■ = No data in these x regions

Application of EPS09 to the heavy boson production at the LHC.

*arXiv:1010.5392 [hep-ph]
(submitted to JHEP)*

Framework: Z Production

- **We look at the leptonic channel:**
$$\frac{d^2\sigma(\sqrt{s}, H_1 + H_2 \rightarrow \ell^+ + \ell^- + X)}{dM^2 dy_R}$$

$y_R =$ rapidity of the lepton pair

$M = M_Z =$ invariant mass of the lepton pair

- **Experimentally well measurable – already seen in PbPb at the LHC!**
- **In the leading order the cross-section reads (we do of course NLO)**

$$\frac{d^2\sigma}{dM^2 dy_R} = \frac{4\pi\alpha_{\text{em}}^2}{9sM^2} \sum_q c_q^2 [q^{(1)}(x_1, Q_f^2)\bar{q}^{(2)}(x_2, Q_f^2) + \bar{q}^{(1)}(x_1, Q_f^2)q^{(2)}(x_2, Q_f^2)]$$

$$x_{1,2} \equiv (M/\sqrt{s})e^{y_R, -y_R}$$

Framework: Z Production

- We look at

$$y_R = \ln \frac{M^2}{M_0^2}$$

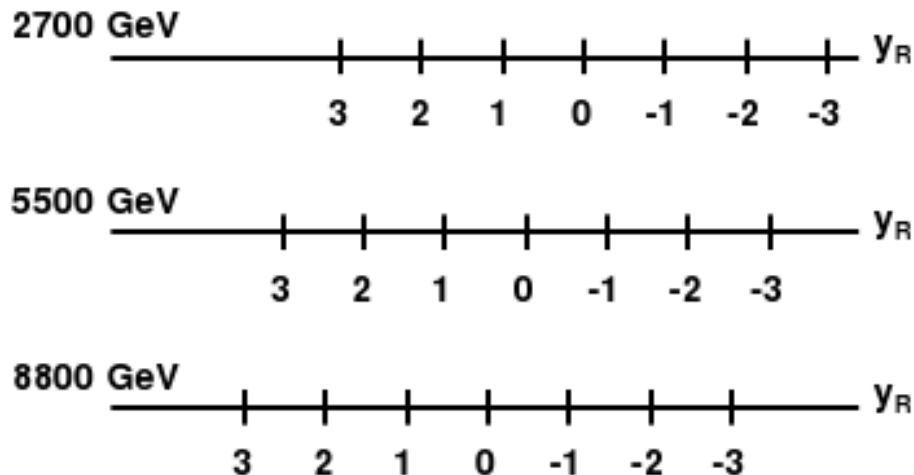
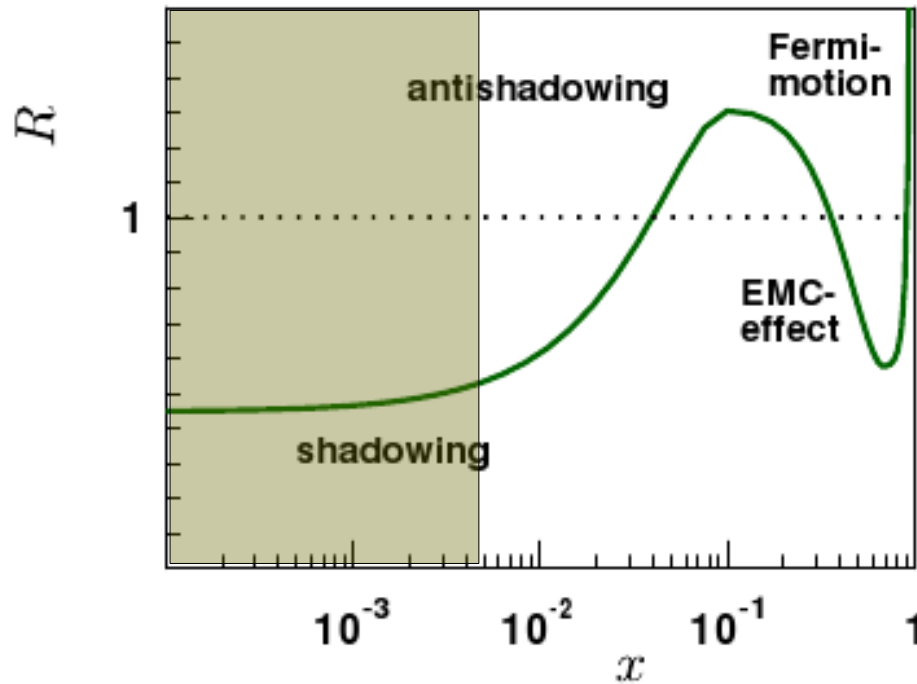
$$M = \sqrt{s} x$$

- Experiment

- In the lepton

$$\frac{d^2\sigma}{dM^2 dy_R} =$$

$$x_{1,2} \equiv$$



$$\frac{+ \ell^- + X)}{}$$

→ LHC!

→ NLO)

$$]q_f^{(2)}(x_2, Q_f^2)]$$

Framework: W Production

- **We look at the leptonic channel:**
$$\frac{d^2\sigma \left(\sqrt{s}, H_1 + H_2 \rightarrow \begin{cases} \ell^+ + \nu \\ \ell^- + \bar{\nu} \end{cases} + X \right)}{dM^2 dy_R}$$

$$\frac{d^2\sigma^{W^\pm}}{dM^2 dy_R} = \frac{\pi\alpha_{\text{em}}^2}{36sM^2 \sin^4 \theta_W} \frac{M^4}{(M^2 - M_W^2)^2 + M_W^2 \Gamma_W^2} \times \sum |V_{ij}|^2 \left[q_i^{(1)}(x_1, Q_f^2) \bar{q}_j^{(2)}(x_2, Q_f^2) + \bar{q}_j^{(1)}(x_1, Q_f^2) q_i^{(2)}(x_2, Q_f^2) \right]$$

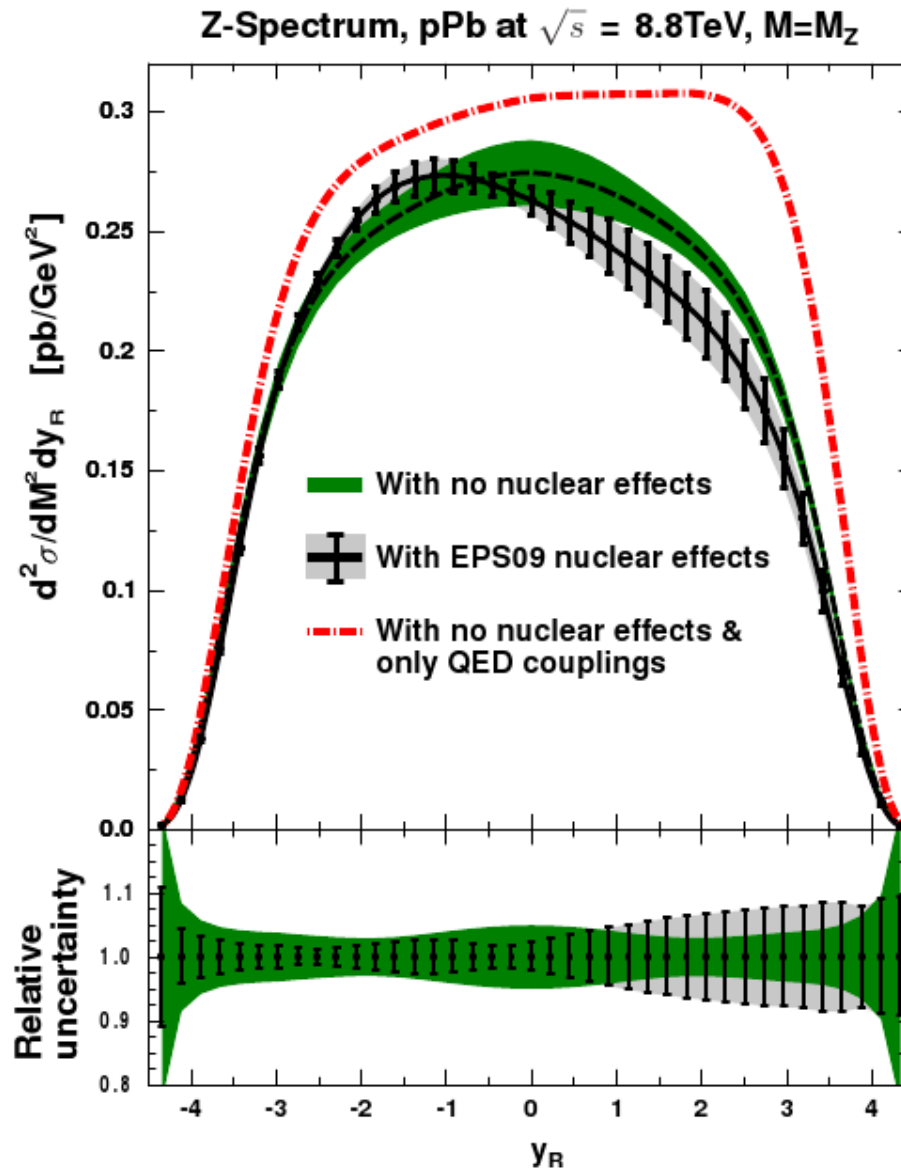
$$x_{1,2} \equiv (M/\sqrt{s}) e^{y_R, -y_R}$$

- **The missing neutrino momentum cannot be fully reconstructed, so this is not directly observable. However, one can show that in leading order**

$$E \frac{d^3\sigma^{h_1 h_2 \rightarrow \ell^\pm + X}}{d^3p} \Big|_{p_T = \frac{M_W}{2}} \propto \frac{d^2\sigma^{W^\pm}}{dM^2 dy_R} \Big|_{M = M_W}$$

 **The results I present roughly apply also to charged lepton production.**

Z Production in p+Pb Collisions

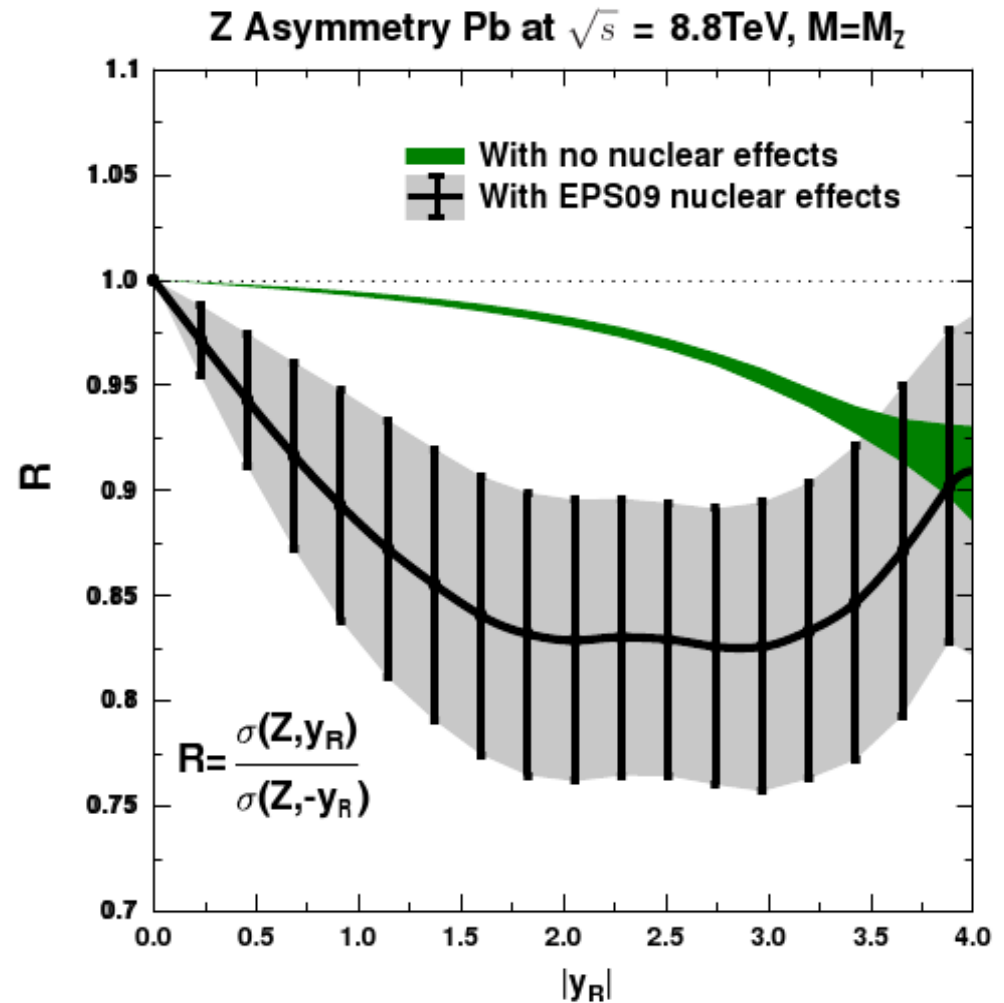


Z Production in p+Pb Collisions

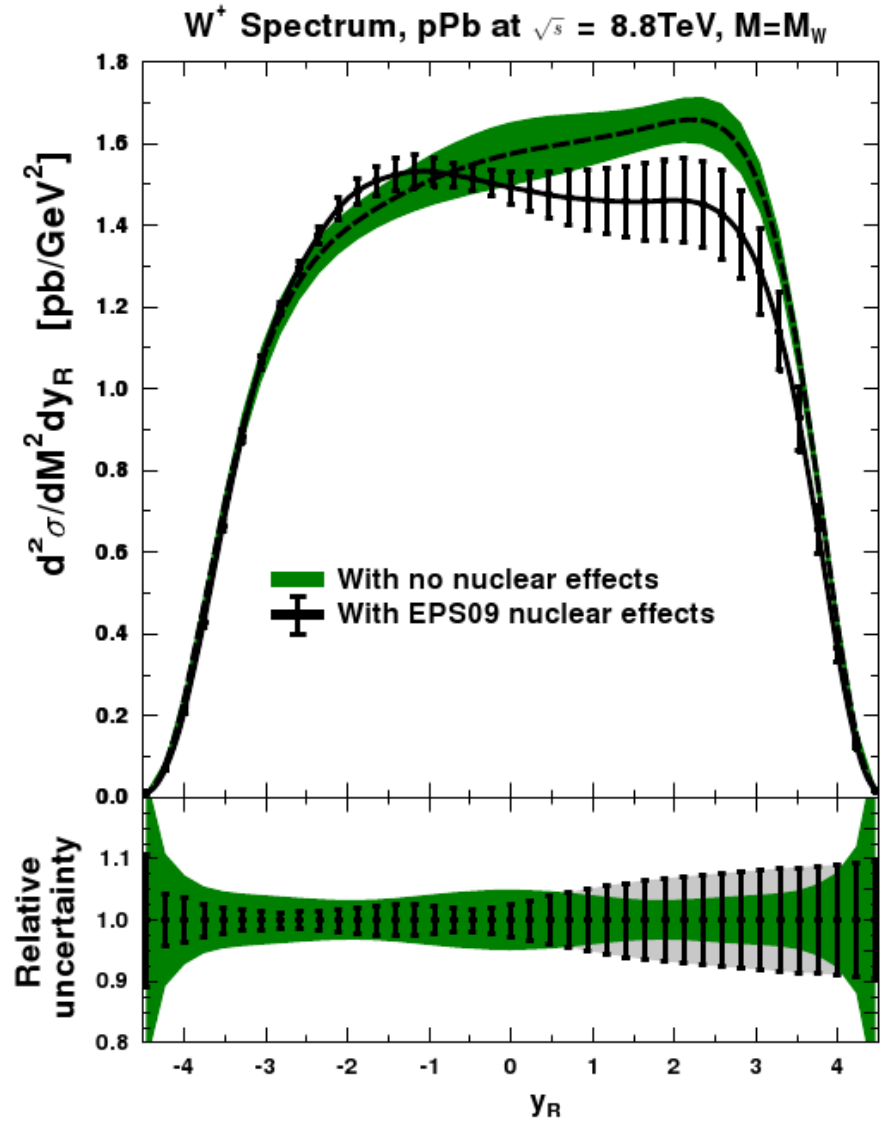
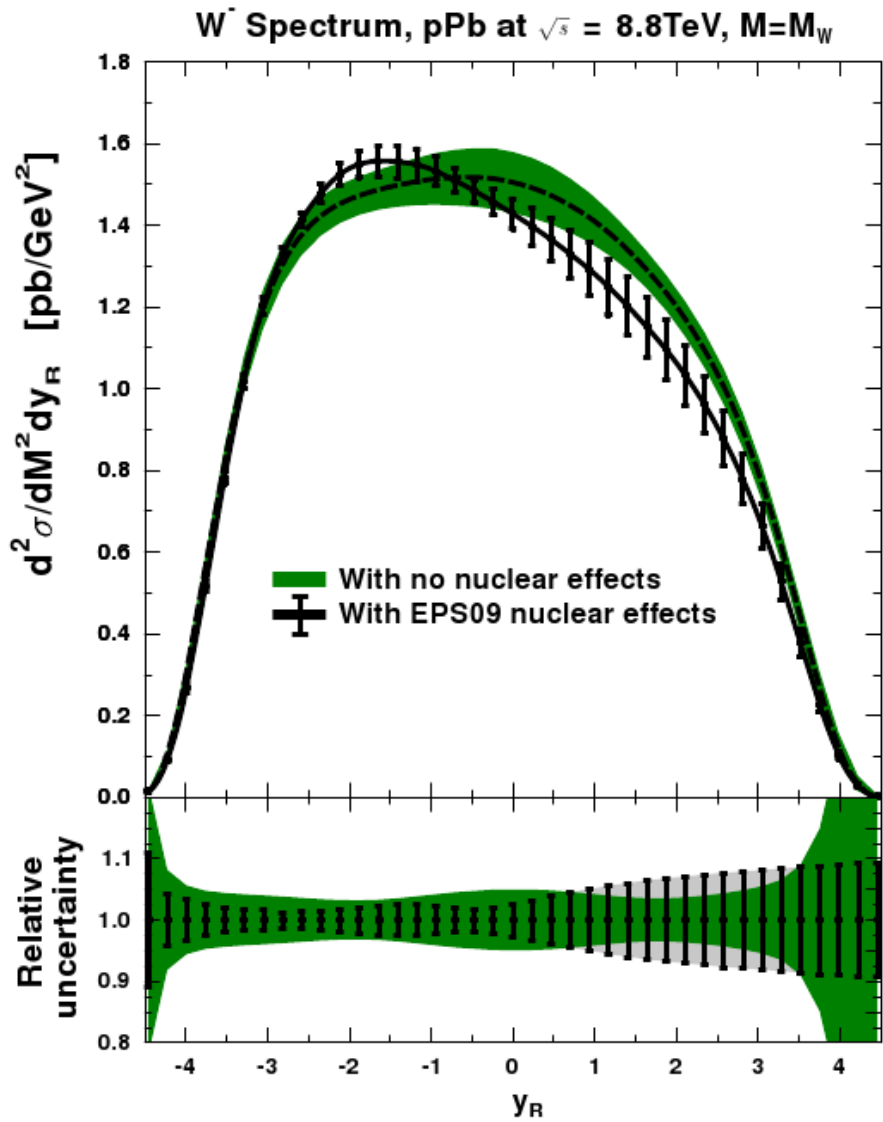
- Look at the ratio

$$\frac{d^2\sigma^{Z,y_R}}{dM^2 dy_R} / \frac{d^2\sigma^{Z,-y_R}}{dM^2 dy_R}$$

- Sizable effect from nuclear Modifications to the PDFs!
- The free proton uncertainties cancel to large extent!
- No normalization problems (e.g. luminosity)



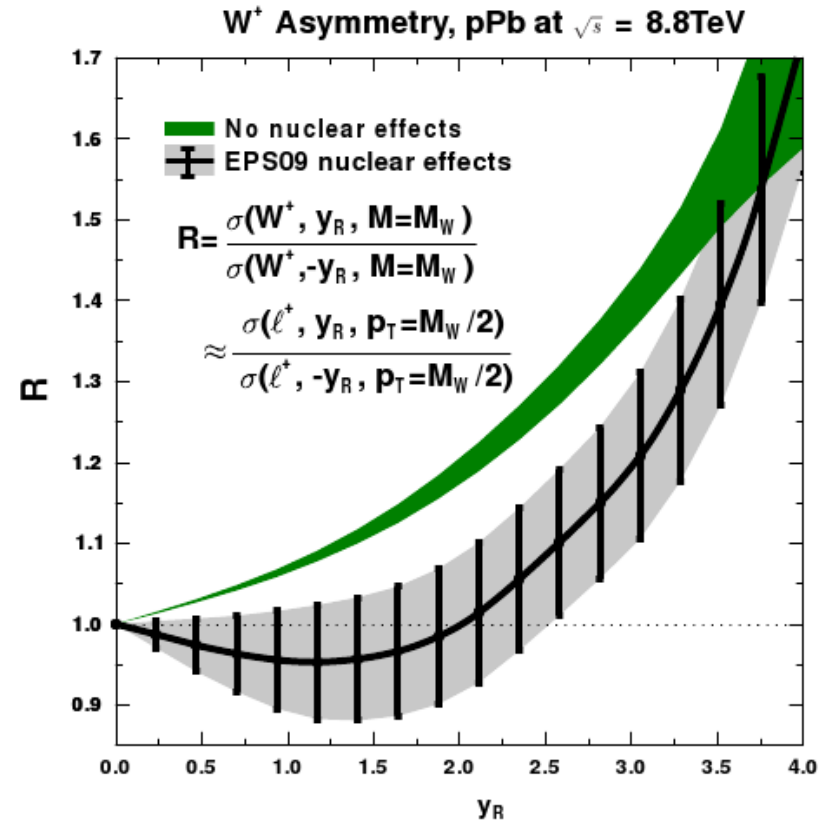
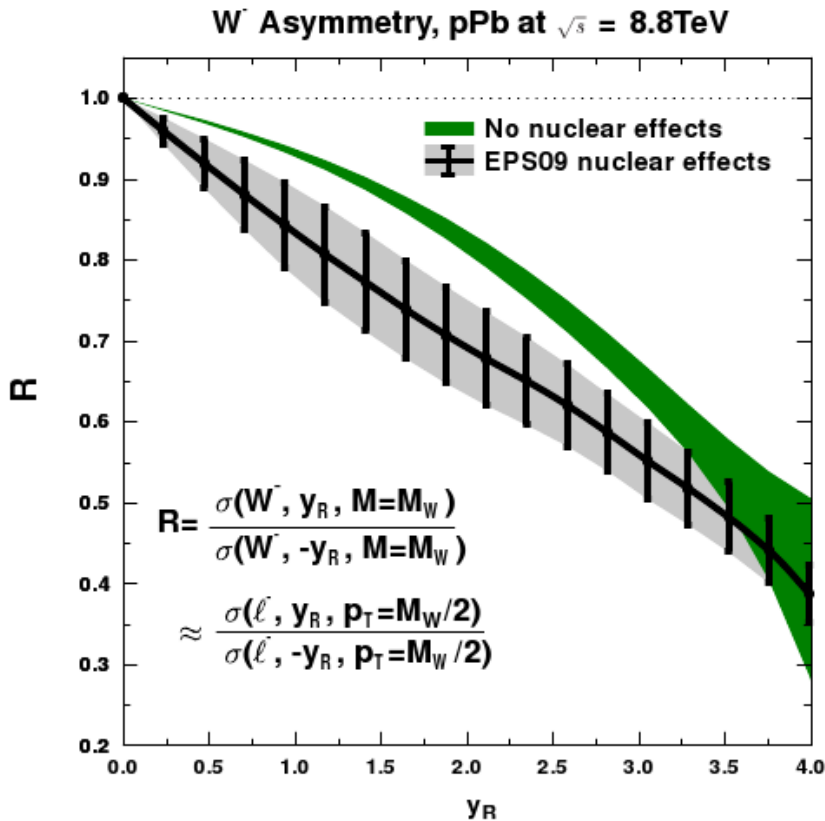
W Production in p+Pb Collisions



W Production in p+Pb Collisions

- The nuclear effect in rapidity asymmetry ratio is much smaller than in Z production.

$$\frac{d^2 \sigma^{W^\pm, y_R}}{dM^2 dy_R} / \frac{d^2 \sigma^{W^\pm, -y_R}}{dM^2 dy_R}$$

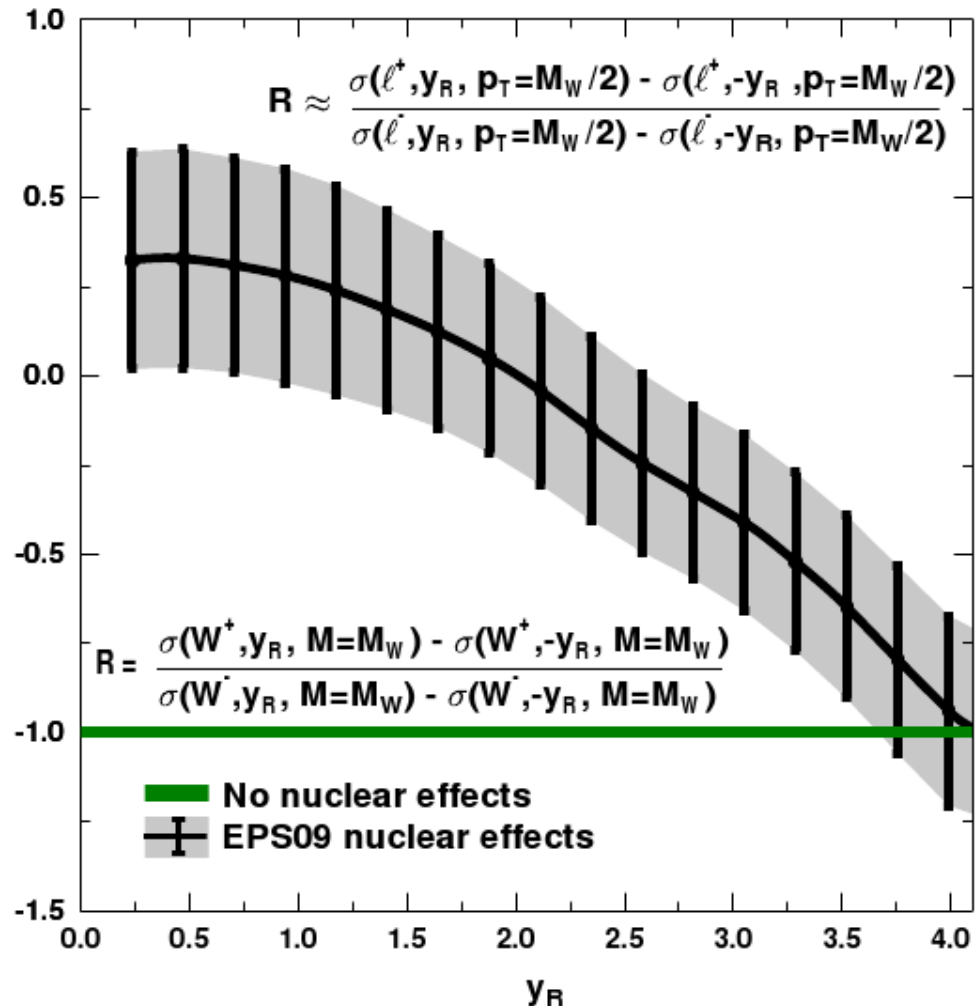


W Production in p+Pb Collisions

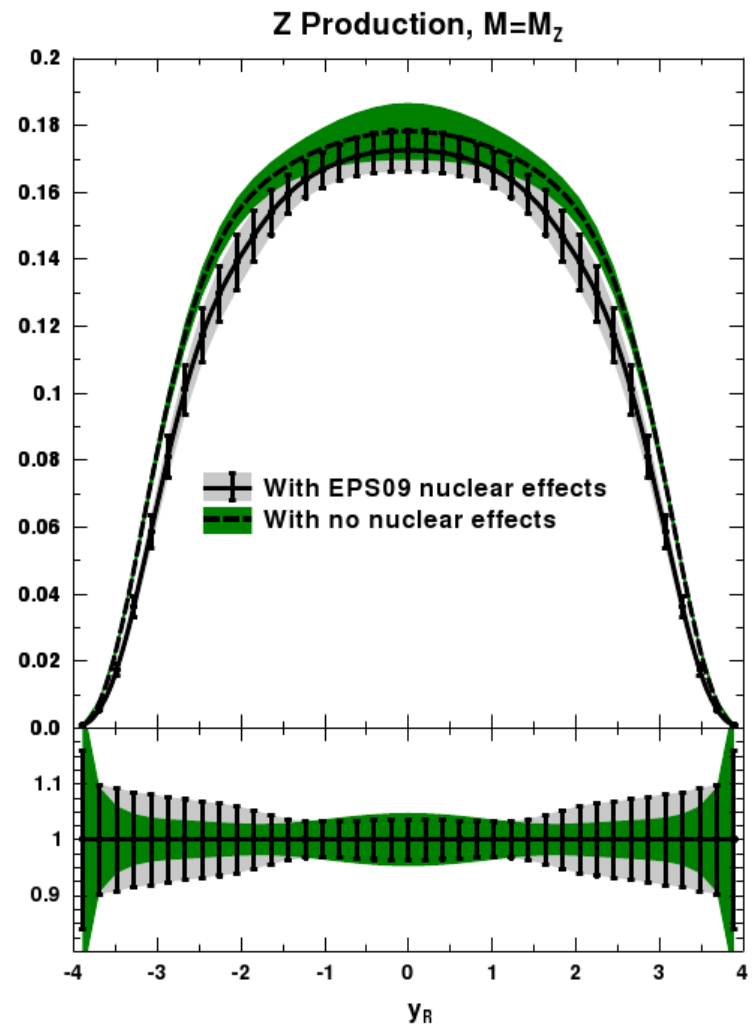
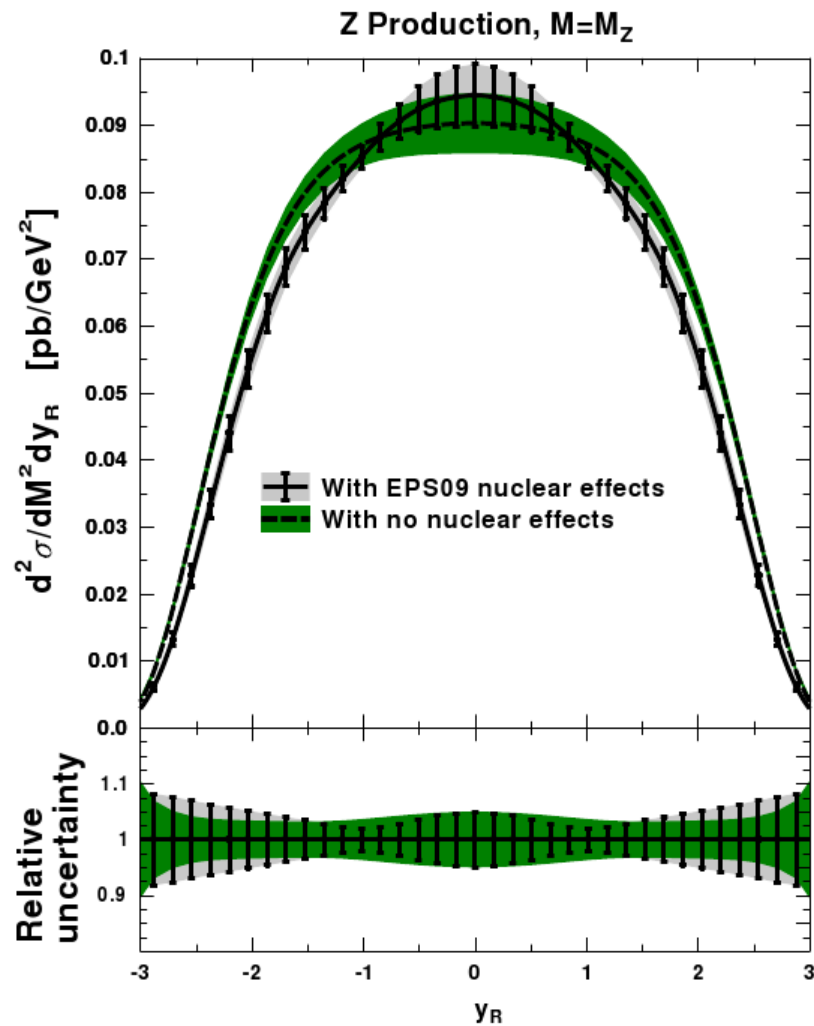
- Look at the combination $\left[\frac{d^2\sigma^{W^+,y_R}}{dM^2 dy_R} - \frac{d^2\sigma^{W^+,-y_R}}{dM^2 dy_R} \right] / \left[\frac{d^2\sigma^{W^-,y_R}}{dM^2 dy_R} - \frac{d^2\sigma^{W^-,-y_R}}{dM^2 dy_R} \right]$

Another Asymmetry, pPb at $\sqrt{s} = 8.8\text{TeV}$

- Large nuclear effect with a large uncertainty already at the midrapidity.
- Due to the “flavor-blind” parametrization of the nuclear modifications in EPS09, these uncertainties are, however, only lower limits.

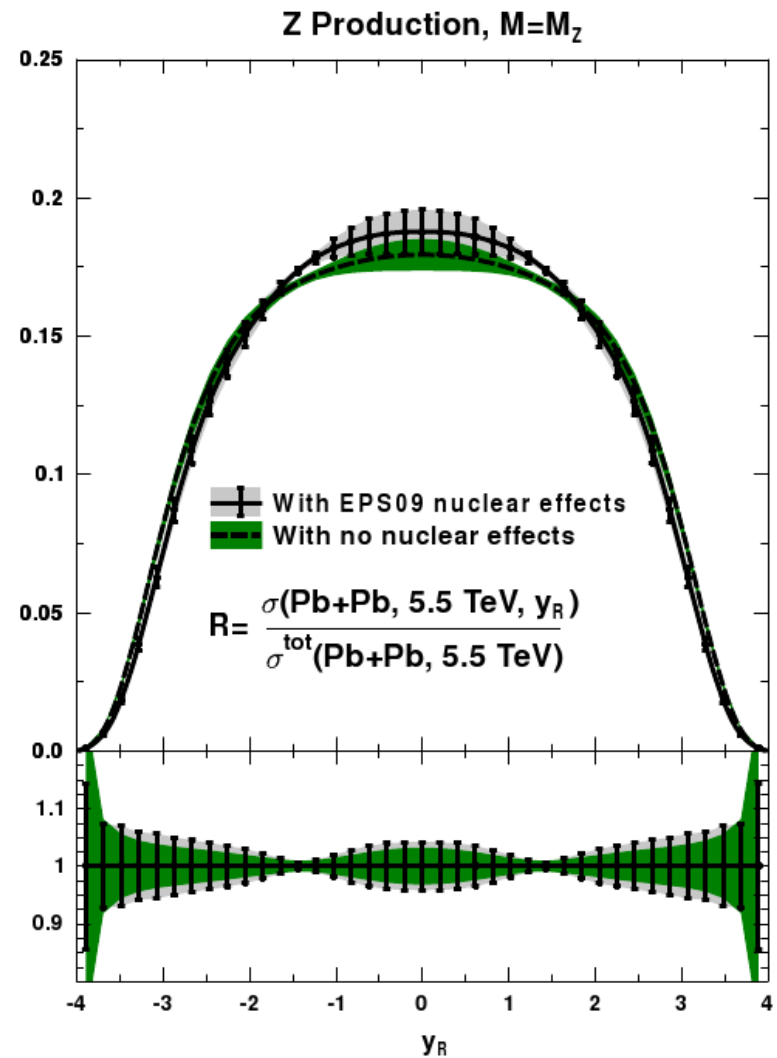
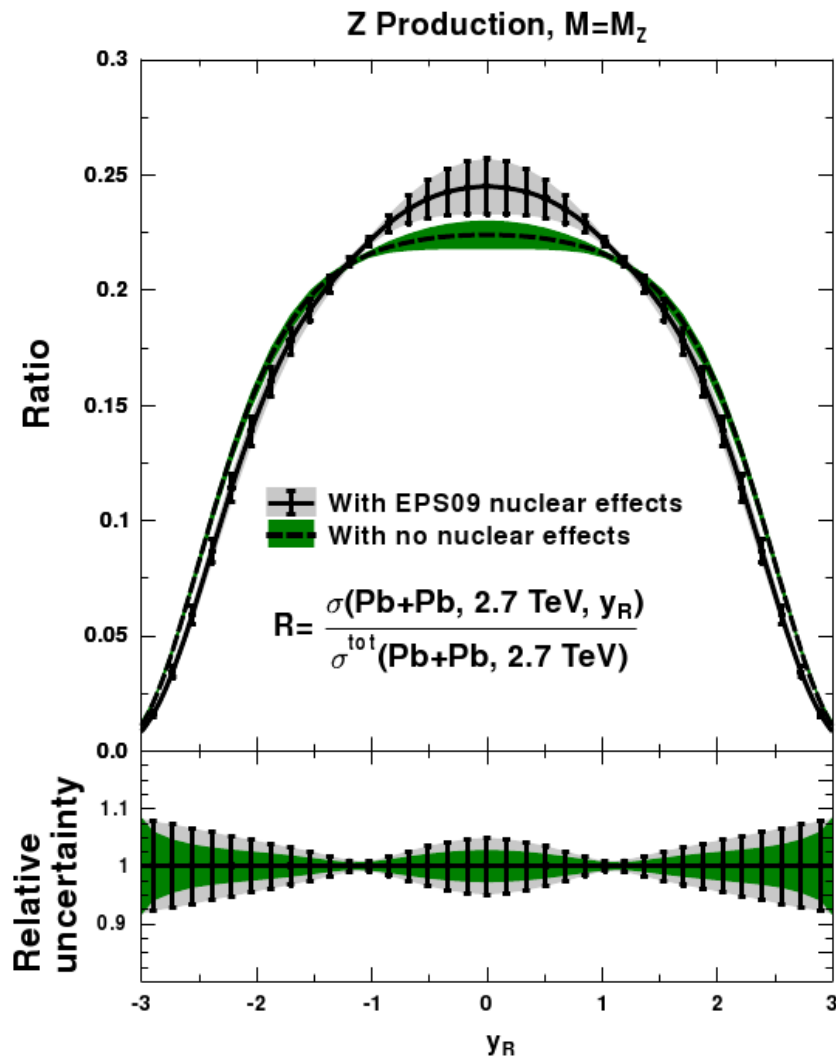


Z Production in Pb+Pb Collisions



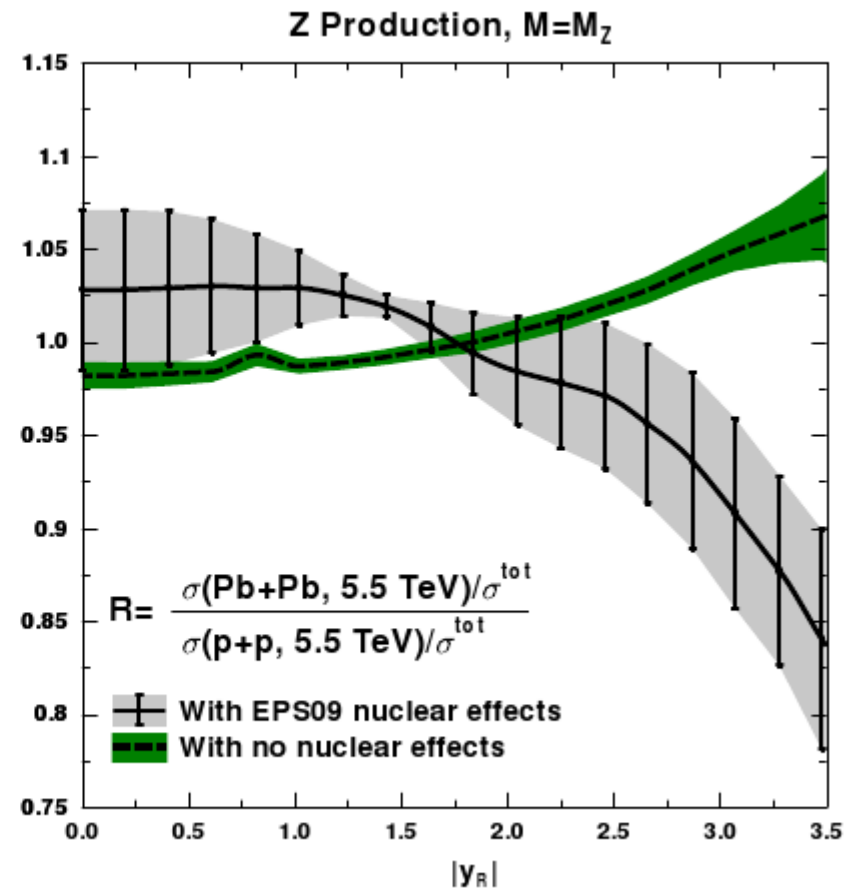
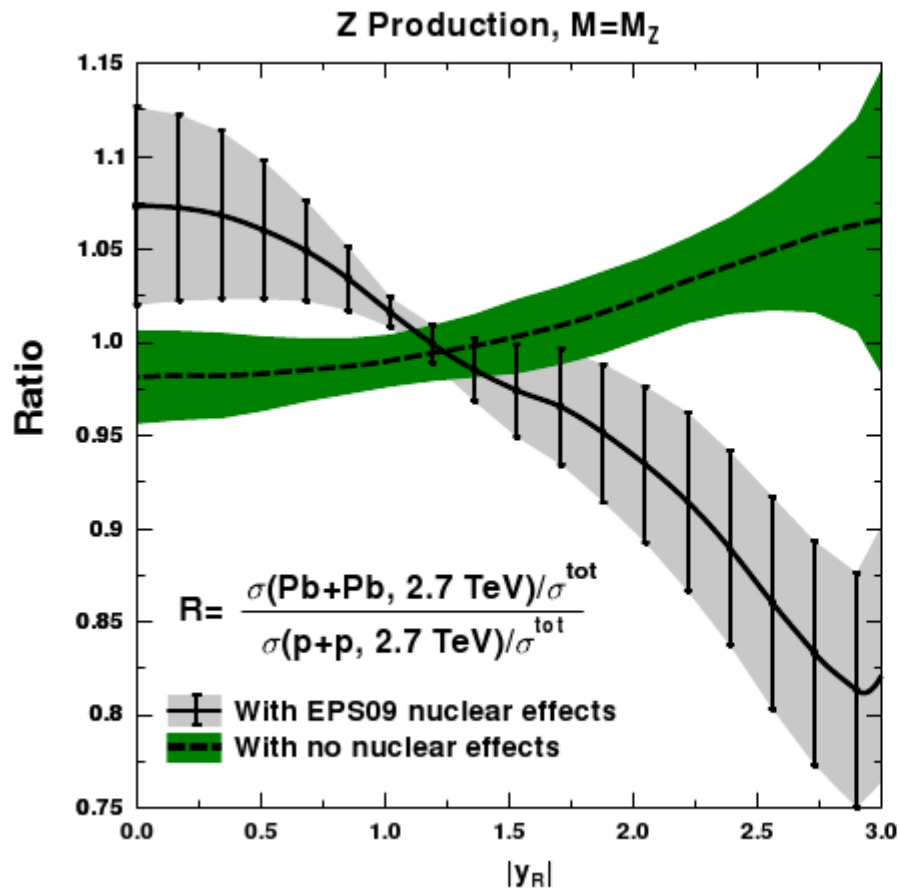
- Unlike in p+Pb, in Pb+Pb the spectra are symmetric in rapidity.

Z Production in Pb+Pb Collisions



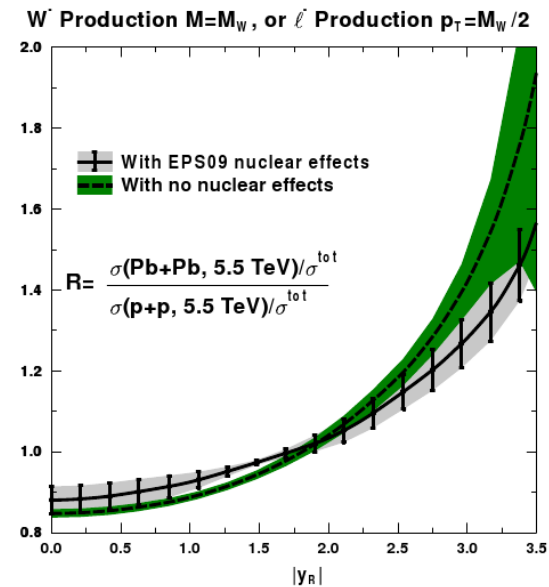
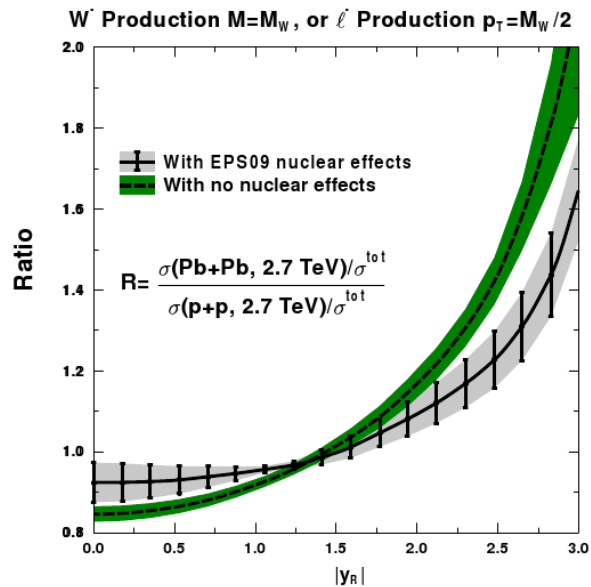
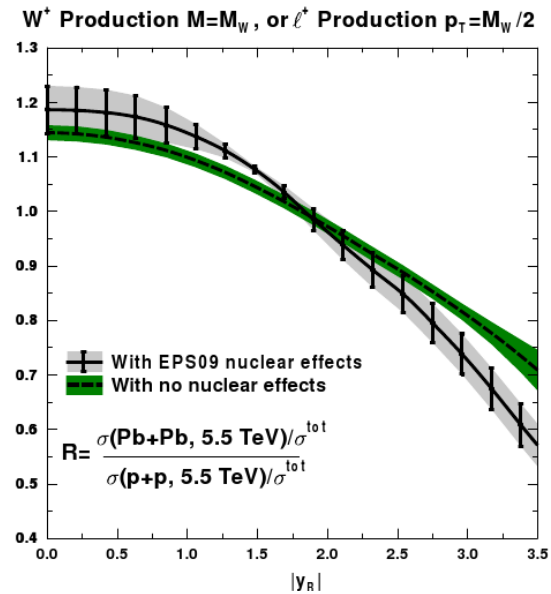
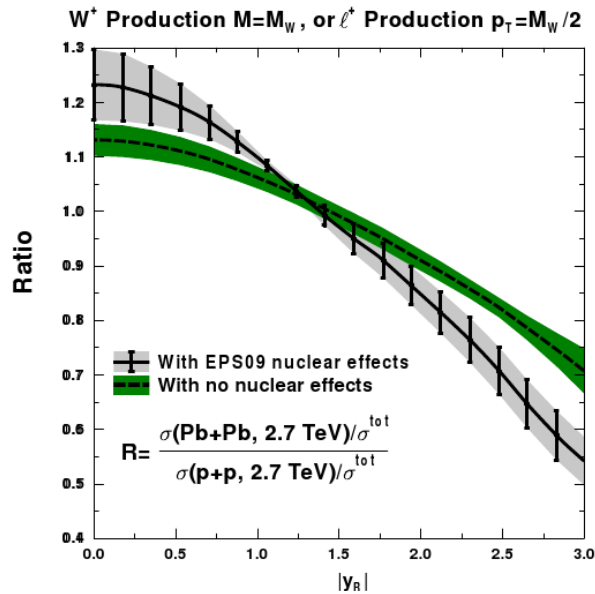
- Normalizing by the rapidity-integrated cross-section reduces especially the free proton uncertainties.

Z Production in Pb+Pb Collisions



Normalizing by a reference cross-section from p+p collisions brings up the nuclear effects. The free proton uncertainties estimated from a interpolation 7 TeV \rightarrow 2.7 & 5.5 TeV.

W Production in Pb+Pb Collisions



Conclusions

- The p+Pb collisions at the LHC would be extremely useful to study the nuclear effects in PDFs. Large effects expected in quantities:

$$\frac{d^2\sigma_{\text{pPb}}^{Z,y_R}}{dM^2 dy_R} / \frac{d^2\sigma_{\text{pPb}}^{Z,-y_R}}{dM^2 dy_R}$$
$$\left[\frac{d^2\sigma^{W^+,y_R}}{dM^2 dy_R} - \frac{d^2\sigma^{W^+,-y_R}}{dM^2 dy_R} \right] / \left[\frac{d^2\sigma^{W^-,y_R}}{dM^2 dy_R} - \frac{d^2\sigma^{W^-,-y_R}}{dM^2 dy_R} \right]$$

- Nuclear effects in Pb+Pb are more difficult to extract. A baseline from p+p collisions would be needed to better see the nuclear effects in PDFs. The Z production probably more useful than the W production.