



# Double electroweak scattering processes at the LHC

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with J. Gaunt, A. Kulesza, J. Stirling  
(arXiv:1003.3953 + work in progress)

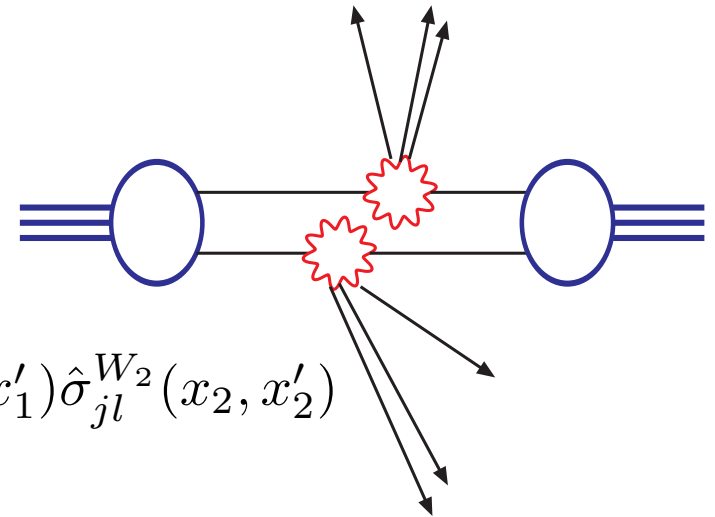
# Outline

- Quick recap of DPS basics
- Singal/background studies of
  - same sign  $W$  pairs
  - $Z(\gamma^*)$  pairs
- Summary

# Double parton scattering (DPS)

Two simultaneous hard interactions in one (p-p) collision.

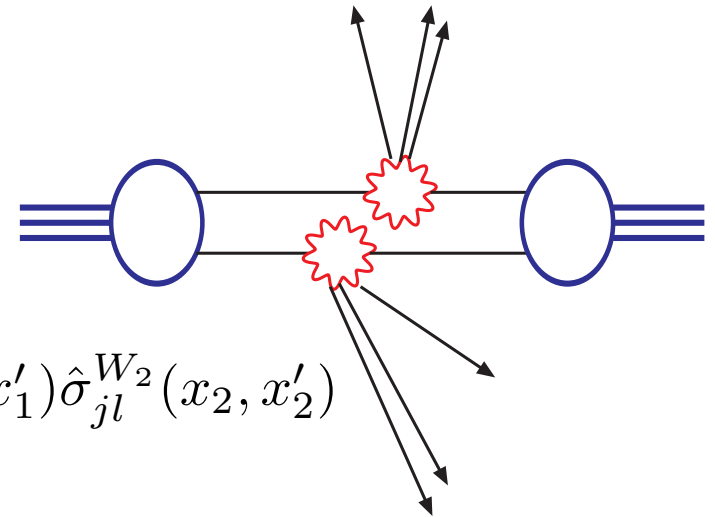
$$\sigma_{\text{DS}}^{(W_1, W_2)} = \frac{1}{2\sigma_{\text{eff}}} \int dx_1 dx_2 dx'_1 dx'_2 D^{ij}(x_1, x_2, t_1, t_2) D^{kl}(x'_1, x'_2, t_1, t_2) \hat{\sigma}_{ik}^{W_1}(x_1, x'_1) \hat{\sigma}_{jl}^{W_2}(x_2, x'_2)$$



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Usual assumptions:

- Uncorrelated longitudinal and transverse distributions ( $\sigma_{\text{eff}}$ )
- Same transverse distributions for different partons (universal  $\sigma_{\text{eff}}$ )
- Factorised double distributions ( $D^{ij}(x_1, x_2) = D^i(x_1)D^j(x_2)$ )

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- connections between sea and valence distributions ?

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**Need experimental handles from processes sensitive to different scales and initial state partons.**

# DPS phenomenology

- Experimental studies:  
AFS, (UA2,) & CDF on  $4j$ , CDF & D0 on  $\gamma + 3j$ , and RHIC  
also [Drees, Han 96](#)



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$b\bar{b}b\bar{b}$ ,  $b\bar{b}jj$ ,  $jjjj$  [Del Fabbro, Treleani 02](#), [Cattaruzza et. al. 05](#), [Berger et. al. 09](#), [Blok et. al. 10](#)

$W/Z + 4j$  [Maina 09](#)

Same sign W pairs (+  $nj$ ) [Kulesza, Stirling 99](#); [Maina 09](#)

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Same sign W pairs (+  $nj$ ) [Kulesza, Stirling 99](#); [Maina 09](#)
- Background:  
Associated W/Z+H production [Del Fabbro, Treleani 00](#), [Hussein 06](#)

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$Z(\gamma^*)Z(\gamma^*) \rightarrow 4l$  :

- characteristic DPS kinematics
- low scales compared to jet based observables possible

# Double electroweak processes 2

Aim:

$$W^\pm W^\pm \rightarrow l^\pm l^\pm + \cancel{E}_T :$$

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**Note:**

The rate for these processes are low (signal  $\sim$  bkgd  $\mathcal{O}(1)$  fb after BRs at 14TeV).

We are talking about longer term LHC possibilities here.

# $W^\pm W^\pm$ : DPS correlations

- dPDFs correlations break factorisations :

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For comparison we have MSTW<sub>n</sub> (n = 0, 1, 2) sets :

$$D_h^{ab}(x_1, x_2, t) = D_h^a(x_1, t) D_h^b(x_2, t) \theta(1 - x_1 - x_2) \times (1 - x_1 - x_2)^n$$

(pb)	$\sigma_{\text{GS09}}$	$\sigma_{\text{MSTW}_0}$	$\sigma_{\text{MSTW}_1}$	$\sigma_{\text{MSTW}_2}$
	$\sqrt{s} = 14 \text{ TeV}$			
$W^+W^-$	0.546	0.496	0.409	0.348
$W^+W^+$	0.321	0.338	0.269	0.223
$W^-W^-$	0.182	0.182	0.156	0.136
	$R$			
	0.784	1.00	1.00	1.00

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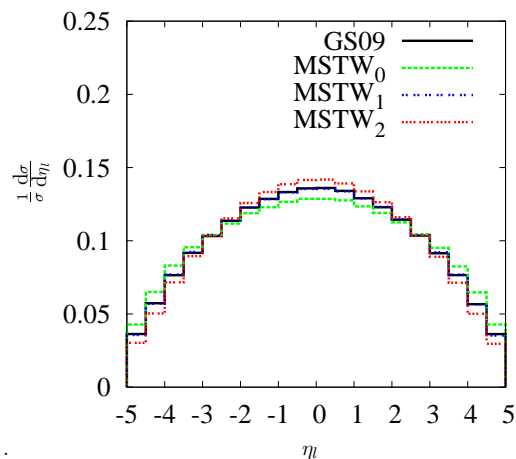
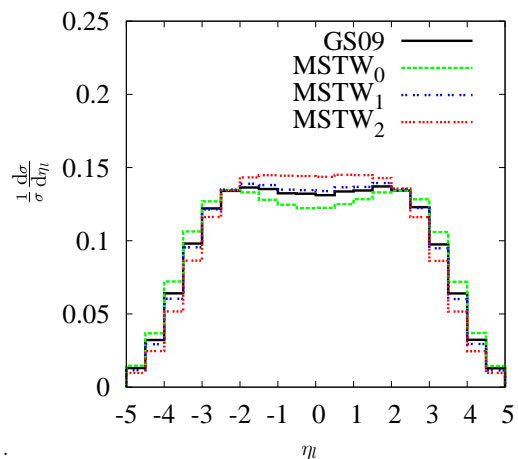
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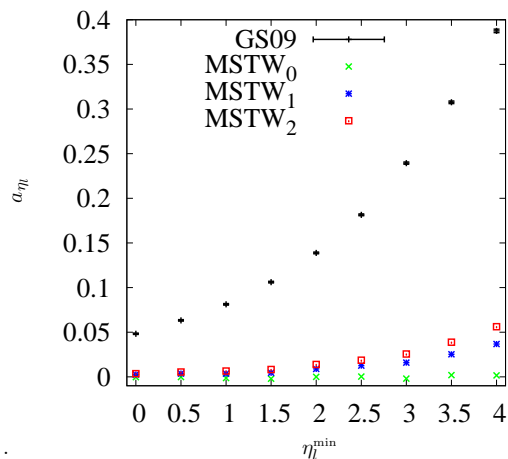
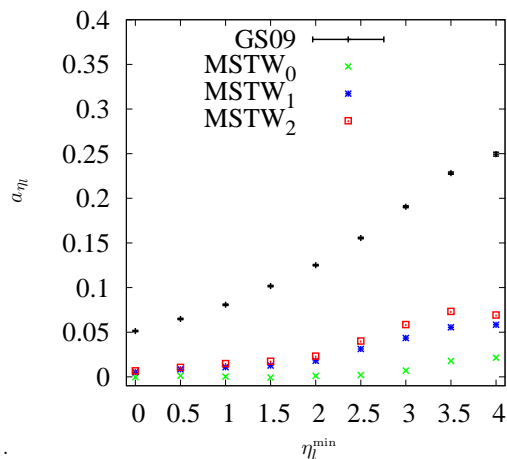
- Factorised approximation becomes better when  $\sqrt{s}$  increases.

# $W^\pm W^\pm$ : DPS correlations (2)



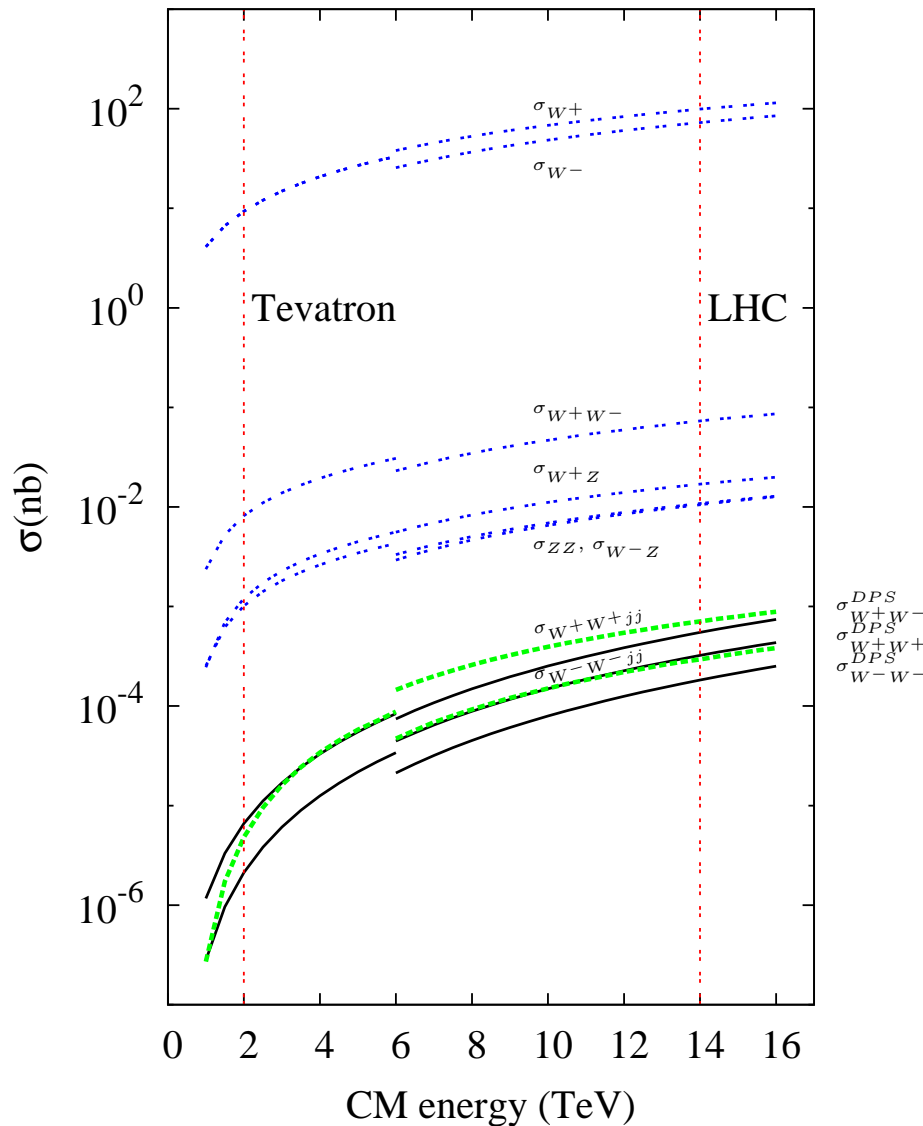
$\eta_l$  well modelled  
by MSTW<sub>1</sub>

$$a_{\eta_l} = \frac{\sigma(\eta_{l_1} \times \eta_{l_2} < 0) - \sigma(\eta_{l_1} \times \eta_{l_2} > 0)}{\sigma(\eta_{l_1} \times \eta_{l_2} < 0) + \sigma(\eta_{l_1} \times \eta_{l_2} > 0)}$$



Large  
 $\eta_l$  asymmetry

# $W^\pm W^\pm$ : signal vs (SPS) bkgd



Assume @ LHC

$$\sigma_{\text{eff}} = 14.5 \text{ mb}$$

$$\sigma_{\text{DS}}(2W^\pm) \sim \mathcal{O}(500) \text{ fb}$$

Bkgd considered:

1) single scattering

$$W^\pm W^\pm jj$$

2) diboson ( $W^\pm Z(\gamma^*)$ )

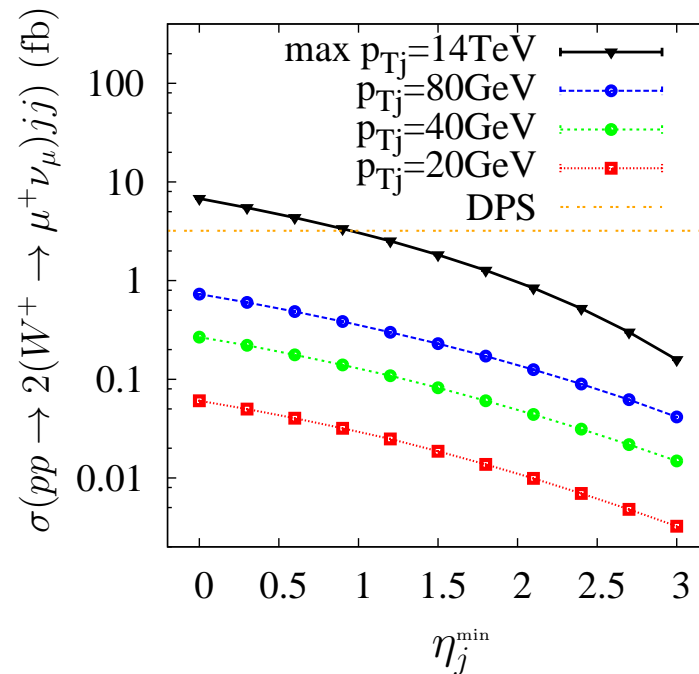
3) heavy flavours ( $Q\bar{Q}$ )

# $W^\pm W^\pm$ : SPS bkgd

- $W^\pm W^\pm jj$ : total cross section  $\sim \sigma_{\text{DS}}(W^\pm W^\pm)$

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- $W^\pm W^\pm jj$ : total cross section  $\sim \sigma_{\text{DS}}(W^\pm W^\pm)$
- Central jet veto ( $\eta_j^{\text{min}}, p_{\text{Tj}}^{\text{max}}$ ) effective:





# $W^\pm W^\pm$ : SPS bkgd (2)

- Diboson production, and when some leptons not identified :

$$q\bar{q}' \rightarrow W^\pm Z(\gamma^*) \rightarrow l^\pm \nu l^\pm (l^\mp)$$

$$q\bar{q} \rightarrow Z(\gamma^*)Z(\gamma^*) \rightarrow l^\pm (l^\mp) l^\pm (l^\mp)$$

- Z contributions  $\sim 2$  orders larger than  $\sigma_{\text{DS}}(W^\pm W^\pm)$
- $\gamma^*$  even larger (asymmetric decay into 1 hard + 1 soft  $l$ 's)
- cuts : central OSSF lepton veto, max lepton  $p_T$ ,  
isolated charged tracks [Chanowitz, Kilgore 95](#)

# $W^\pm W^\pm$ : SPS bkgd (3)

- Heavy flavour production:  $pp \rightarrow Q\bar{Q} + X$ ,  $Q = t, b$
- $t\bar{t}$  : e.g.  $t \rightarrow W^+ b \rightarrow l^+ \nu b$   
 $\bar{t} \rightarrow W^- \bar{b} \rightarrow q\bar{q}' l^+ \nu \bar{c}$ 
  - nominally final state is  $l^\pm l^\pm + \cancel{E}_T + 4j$
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- $b\bar{b}$  :  $gg \rightarrow b\bar{b} \rightarrow B\bar{B} + \dots$   
 $B \rightarrow l^+ \nu X$   
 $\bar{B}^0 \rightarrow B^0 \rightarrow l^+ \nu \tilde{X}$ 
  - huge cross section,  $b p_T$  falls steeply,  $\nu$  soft
  - cut: tight lepton isolation, min lepton  $p_T$  &  $\cancel{E}_T$

# $W^\pm W^\pm$ : simulation

- DS signal: MADGRAPH with GS09 and resummed  $W$   $p_T$  distribution.
- $b\bar{b}$ : HERWIG6 .510 with parton level cuts, forced semi-leptonic B decay and one  $B_d^0$ - $\bar{B}_d^0$  mixing.  $\sigma_{b\bar{b}}(p_T^b > 20\text{GeV}) \sim 5 \mu\text{b}$ .
- Diboson: MADGRAPH + VEGAS at LO.
- $W^\pm W^\pm jj$  &  $t\bar{t}$ : neglected as discussed before.
- Other backgrounds: multi-particle interactions estimated. Found negligible.
- Detector effects: not simulated.

# $W^\pm W^\pm$ : cuts

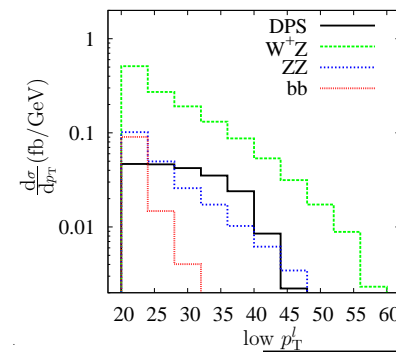
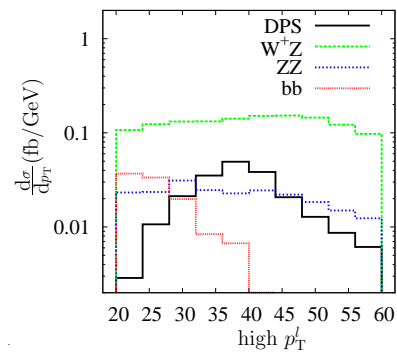
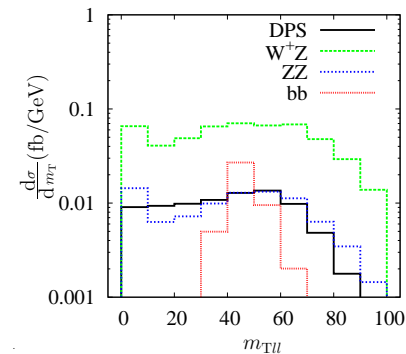
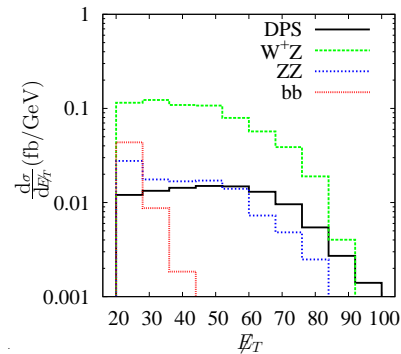
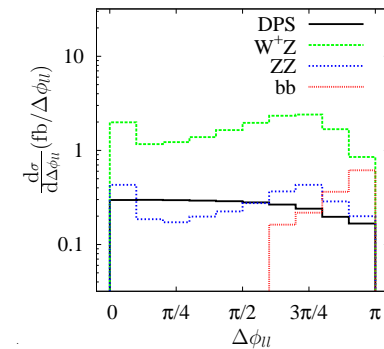
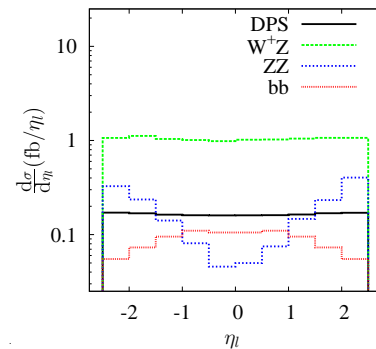
- Isolated SSL pair  $|\eta| < 2.5$ ,  $20 \leq p_T^l \leq 60$  GeV.
- OSSF lepton veto when a 3rd lepton is identified (100% eff. assumed when  $p_T^l \geq 10$  GeV and  $|\eta| < 2.5$ ).
- $\cancel{E}_T \geq 20$  GeV.
- Reject an event if a charged (lepton) track with  $p_T^{\text{id}} \geq p_T \geq 1$  GeV forms an invariant mass  $< 1$  GeV with one of the same-sign leptons.
- Jet veto to reject  $W^\pm W^\pm jj$ .

# $W^\pm W^\pm$ : results

$$\sqrt{s} = 14\text{TeV}$$

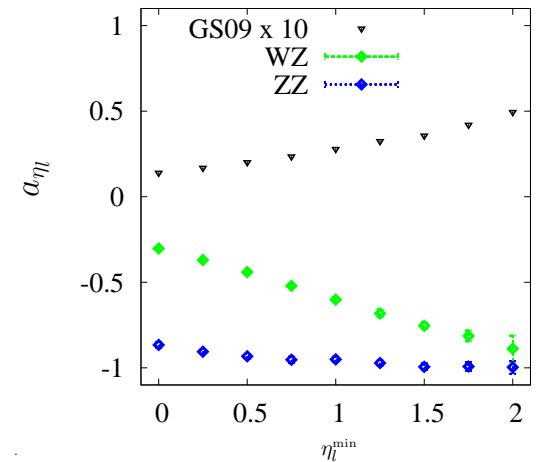
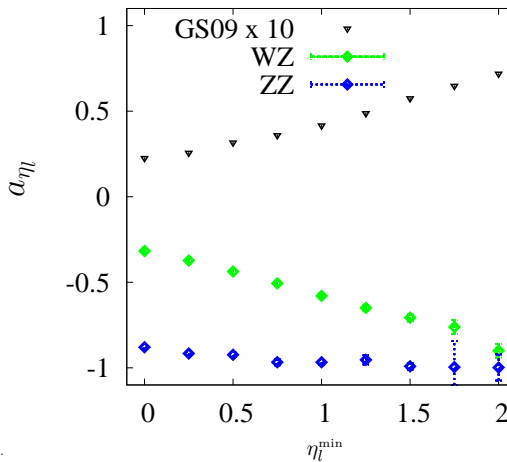
After cuts	$\sigma_{\mu^+\mu^+}$ (fb)	$\sigma_{\mu^-\mu^-}$ (fb)
$W^\pm W^\pm$ (DPS)	0.82	0.46
$W^\pm Z(\gamma^*)$	5.1	3.6
$Z(\gamma^*)Z(\gamma^*)$	0.84	0.67
$b\bar{b}$ ( $p_T^b \geq 20$ GeV)	0.43	0.43

Bkgd dominated by  $W^\pm Z(\gamma^*)$ , basic kinematic distributions similar to DPS signal.



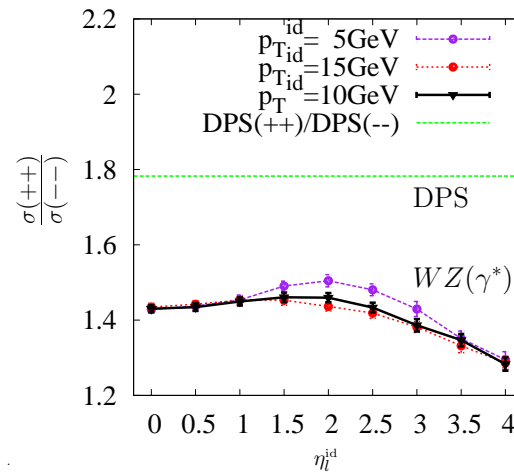
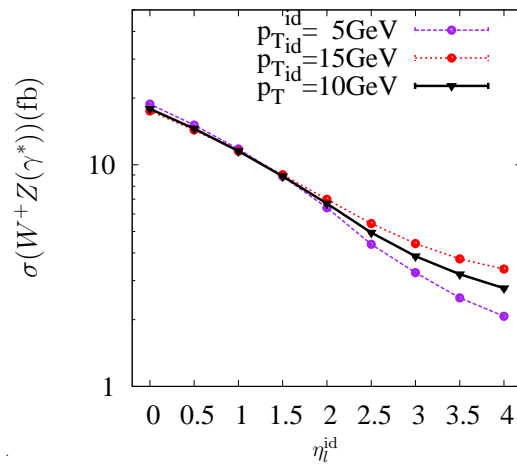
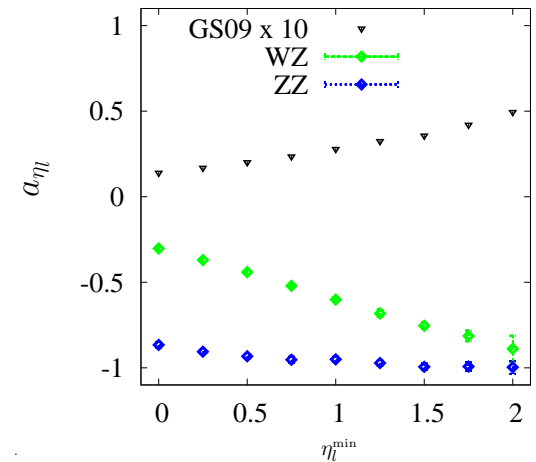
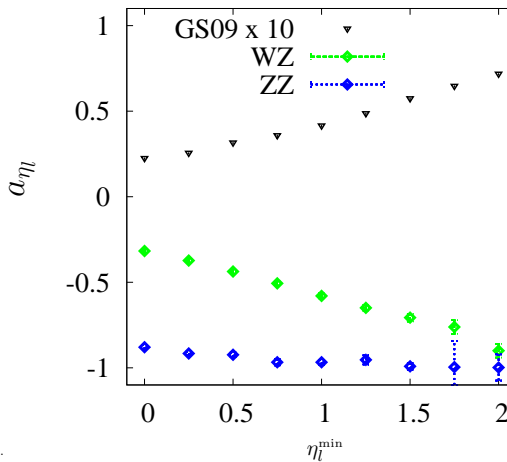
# $W^\pm W^\pm$ : further handles

$\eta$  asymmetry: SPS  
final states prefer  
small  $\Delta\eta$ , less so  
for signal :



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Charge asymmetry ratio  $\frac{\sigma(++)}{\sigma(--)}$  also different



# $Z(\gamma^*)Z(\gamma^*)$

Look for 4 muons,  $2\mu^+2\mu^-$

- 4 isolated leptons: very clean signal
- double  $Z \rightarrow l^+l^-$  rate low
- want to go to low scales, where DPS rate increases
- need to trigger on (low  $p_T$ ) leptons

LHCb might find easier in studying this process

Signal:  $(q\bar{q} \rightarrow Z(\gamma^*) \rightarrow \mu^+\mu^-)^2$

Bkgd:  $q\bar{q} \rightarrow Z(\gamma^*) \rightarrow 4\mu$ ,  $q\bar{q} \rightarrow 2(Z(\gamma^*) \rightarrow \mu^+\mu^-)$

Again consider only physics bkgd

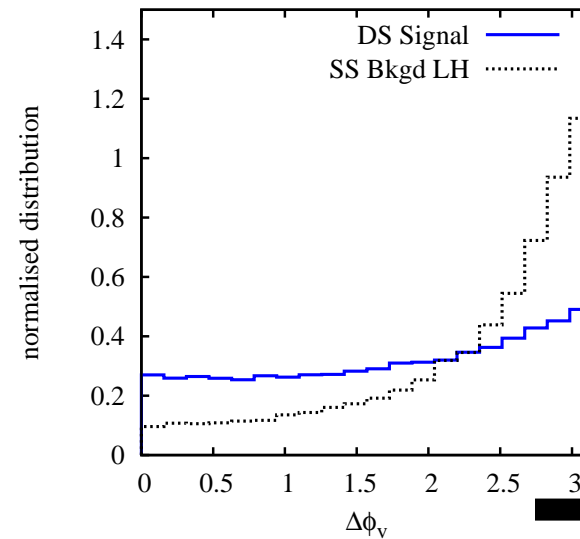
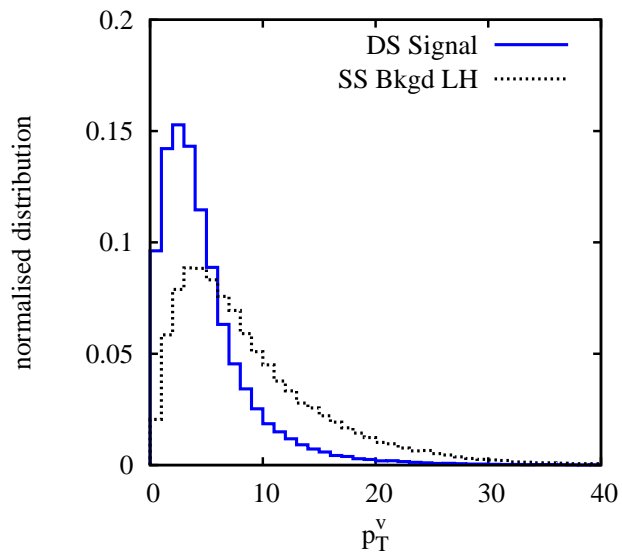
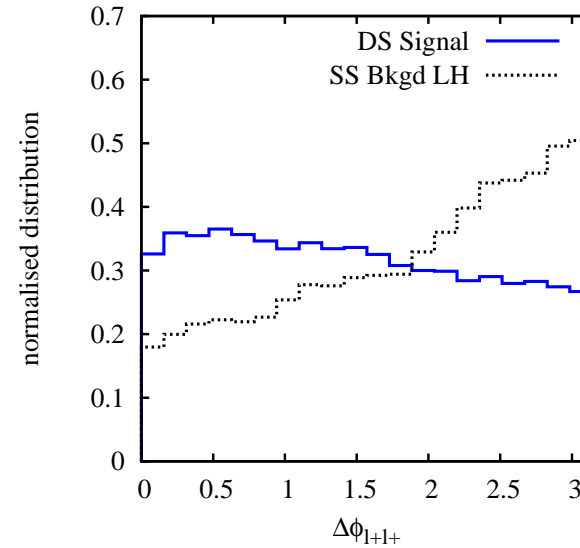
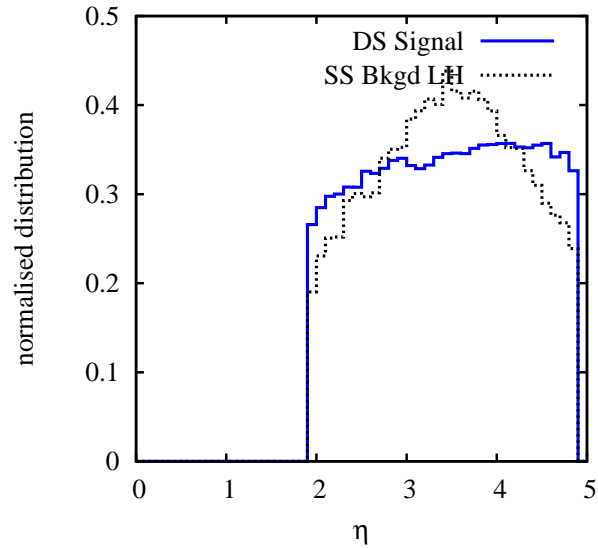
# $Z(\gamma^*)Z(\gamma^*)$ : simulation

- Signal: HERWIG++, assuming simple factorised model
- Bkgd: MADEVENT + HERWIG++

Cuts:

- $1.9 < \eta_l < 4.9$
- $1 < p_T^l < 50$  GeV
- $\Delta R_{\mu\mu} > 0.2$  for all muon ( $++$ ,  $--$ ,  $+-$ ) pairs
- $4 < m_{\mu^+\mu^-} < 50$  GeV for both  $\mu^+\mu^-$  pairs
- $m_{4l} < 50$  GeV (to suppress the Z single resonance bkgd)

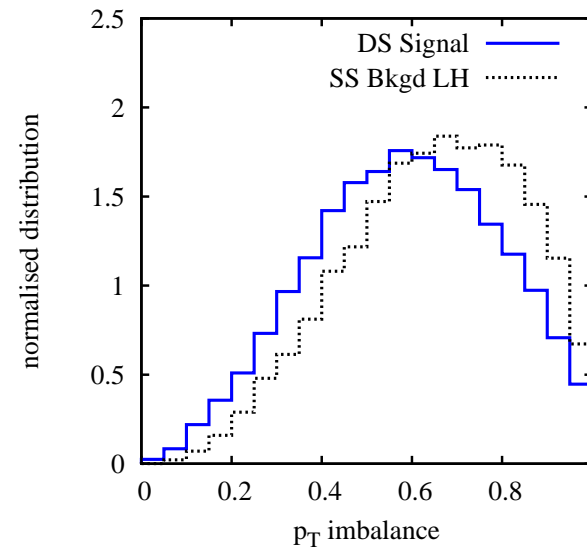
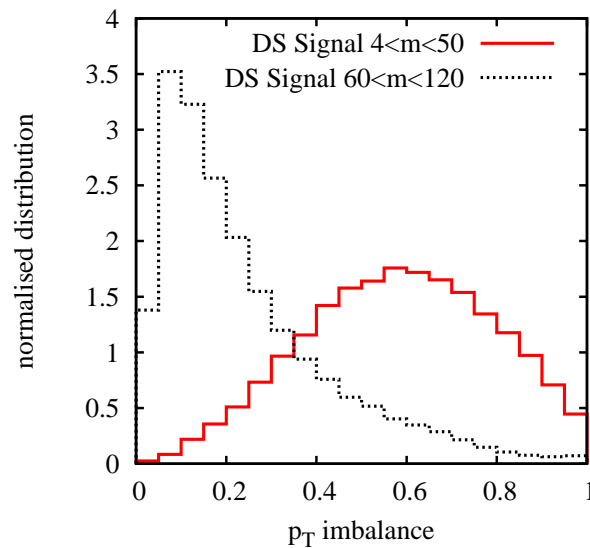
# $Z(\gamma^*)Z(\gamma^*)$ : preliminary results



# $Z(\gamma^*)Z(\gamma^*)$ : pair-wise balance

Define  $p_T$  imbalance  $S$  as

$$S = \frac{1}{2} \left( \frac{|p_T^{l_1} + p_T^{l_2}|}{p_T^{l_1} + p_T^{l_2}} + \frac{|p_T^{l_3} + p_T^{l_4}|}{p_T^{l_3} + p_T^{l_4}} \right)$$



- different from D0 variables. Comparisons needed.
- effectiveness depends on mass scales involved

# Summary and next steps

- dPDFs including correlation effects (GS09) leads to qualitative changes in signal properties (rapidity asymmetry, cross section ratios).
- DPS  $W^\pm W^\pm$  has many appealing properties, but background can be problematic. However strategies are available to help suppress bkgd beyond basic cuts.
- DPS  $Z(\gamma^*)Z(\gamma^*)$  very clean signal. Simple distributions different from bkgd, but can be hard to cut on.
- Looking at correlations between different dilepton/vector boson observables



# Backup slides

# Multiple particle interactions

- Given luminosity ( $L = 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ ), single scattering cross section ( $\sigma$ ), rate of bunch crossing ( $B = 4 \cdot 10^7 \text{ s}^{-1}$ ):  
Average number of events per bunch crossing,  $\langle n \rangle = \frac{L\sigma}{B}$

- Multiple particle interaction cross section,  $\sigma_N$ :

$$\sigma_N = e^{-\langle n \rangle} \frac{\langle n \rangle^N}{N!} \frac{B}{L} \simeq \frac{\sigma^N}{N!} \left( \frac{L}{B} \right)^{N-1}$$

$$= \frac{\sigma^N}{N! (\sigma_{N,\text{eff}})^{N-1}}$$

$$\sigma_{N,\text{eff}} \equiv \left( \frac{B}{L} \right) = 4 \text{ mb}$$

- RMS bunch length : 7.5 cm, z-resolution : 115  $\mu\text{m}$  (Pixel), 580  $\mu\text{m}$  (SCT) at ATLAS

the probability that 2 independent scatterings overlap  $\sim \mathcal{O}(0.1)\%$ .