



# CMS results on diffraction *and low-x*



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on behalf of

**CMS Collaboration**

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MPI@LHC 2010:  
2nd International Workshop  
on Multiple Partonic Interactions at the LHC



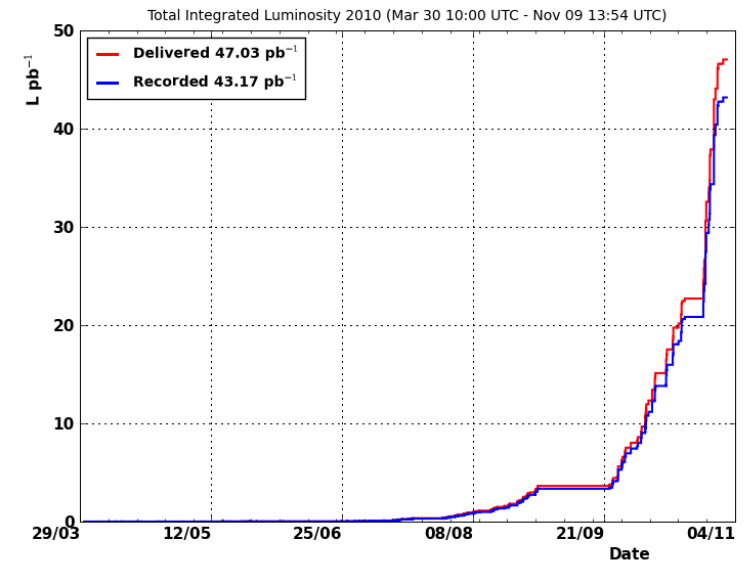
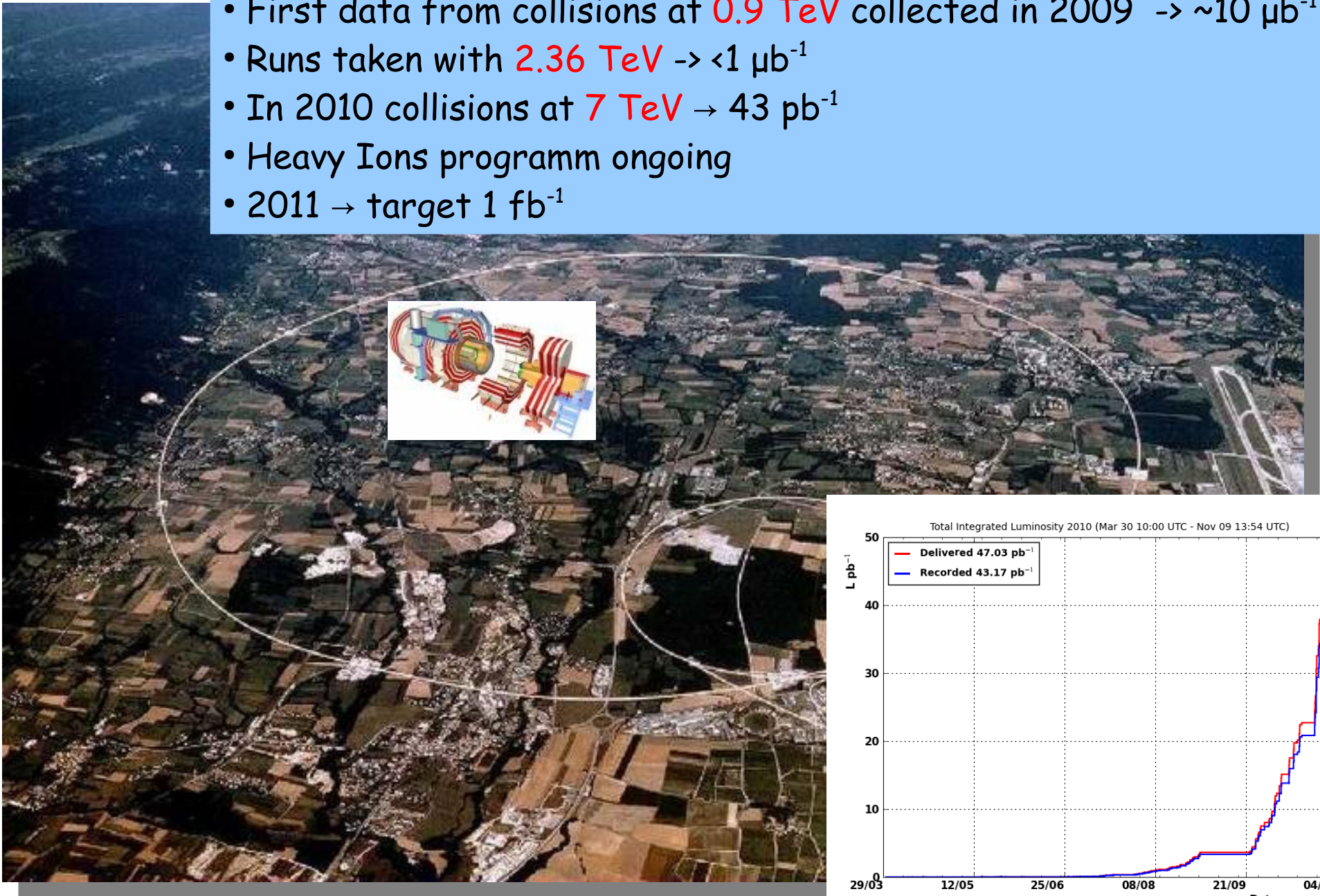
# The Outline

- **Apparatus**
- **Observation of inclusive diffraction**
- **Observation of hard diffraction**
- **Energy flow in the forward region**
- **Forward jets spectrum**
- **Outlook and Summary**

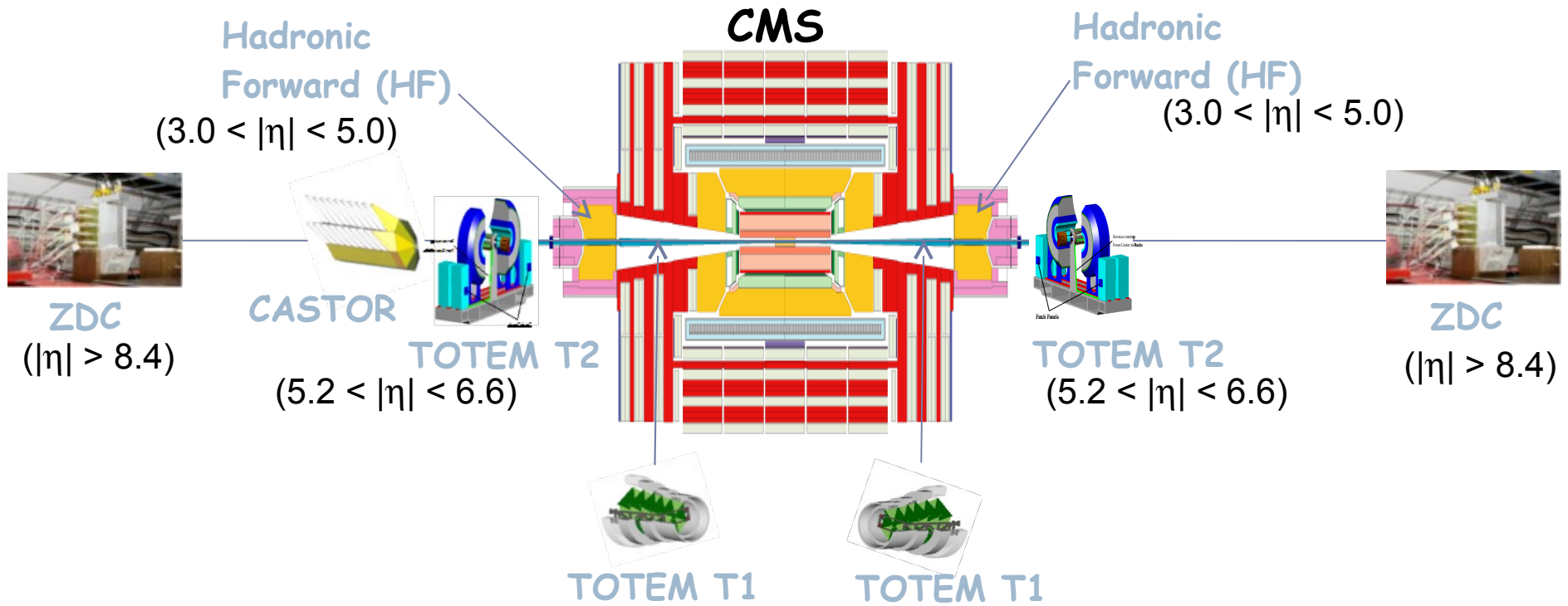


# CMS and LHC

- First data from collisions at **0.9 TeV** collected in 2009  $\rightarrow \sim 10 \mu\text{b}^{-1}$
- Runs taken with **2.36 TeV**  $\rightarrow < 1 \mu\text{b}^{-1}$
- In 2010 collisions at **7 TeV**  $\rightarrow 43 \text{pb}^{-1}$
- Heavy Ions programm ongoing
- 2011  $\rightarrow$  target  $1 \text{fb}^{-1}$



# The CMS detector

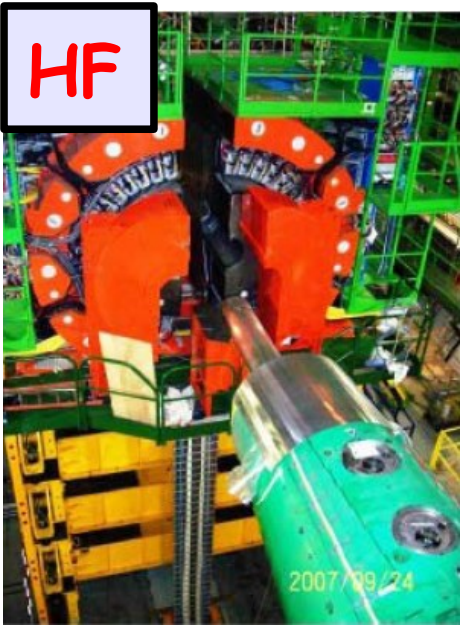


- **H**adronic **F**orward calorimeters (HF)
- **Z**ero **D**egree **C**alorimeter (ZDC)
- **C**entauro **A**nd **S**Trange **O**bjects **R**esearch (CASTOR) - calorimeter

- **TOTEM** - separate experiment:
  - T1 - in front of the HF, 7.5 m from IP
  - T2 - in front of CASTOR, 13.6 m from IP
  - RP - 147 & 149 and 216 & 220 m from IP



# The CMS forward detectors

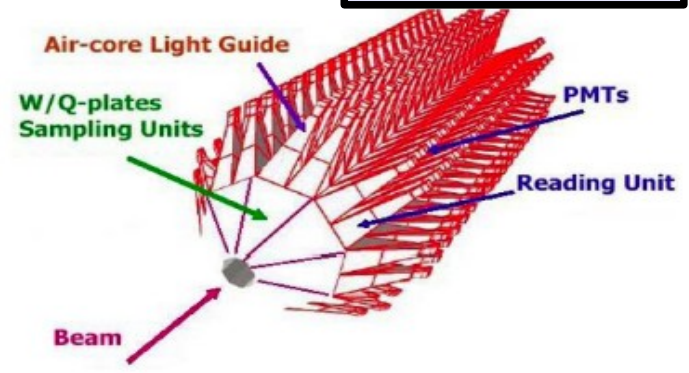


**HF**

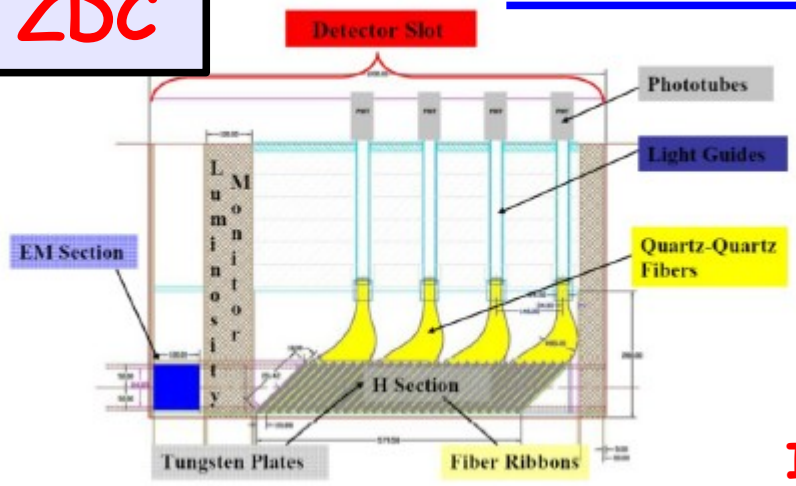
- Located at 11.2 m from IP
- Rapidity coverage:  $3 < |\eta| < 5$
- 0.175x0.175 segmentation in  $\eta$  and  $\phi$
- Steel absorbers and embedded radiation-hard quartz fibers for fast collection of Cherenkov light

- Located at 14.3 m from IP
- Rapidity coverage:  $-6.6 < \eta < -5.2$
- Segmentation in  $\phi$  (16 sectors)
- 14 modules (2EM+12HAD)
- Alternate tungsten absorbers and quartz plates

**CASTOR**



**ZDC**



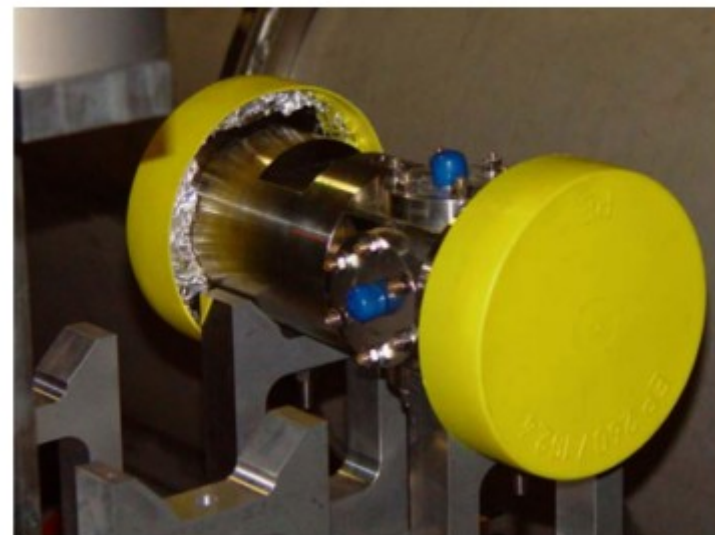
- Located at 140 m from IP
- Rapidity coverage:  $|\eta| > 8.1$
- Tungsten/quartz Cherenkov calorimeter with separated EM and HAD sections
- Detection of neutrals ( $\gamma$ ,  $\pi^0$ , n)

**In the presented analyses CASTOR and ZDC not used**

# Minimum Bias Triggers

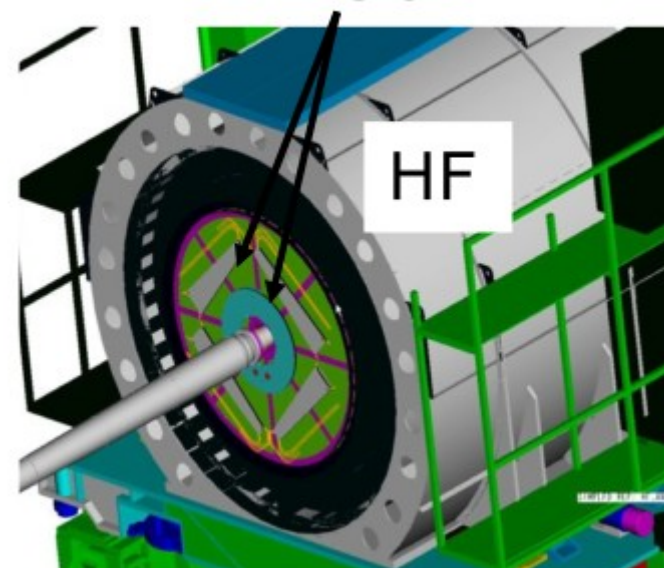
- Beam Pick-up Timing for eXperiments - BPTX
- 175 m from interaction point (both sides)
- Designed to provide precise info on the bunch structure and timing of the incoming beam
- Trigger formed if one (two bunches) present

BPTX



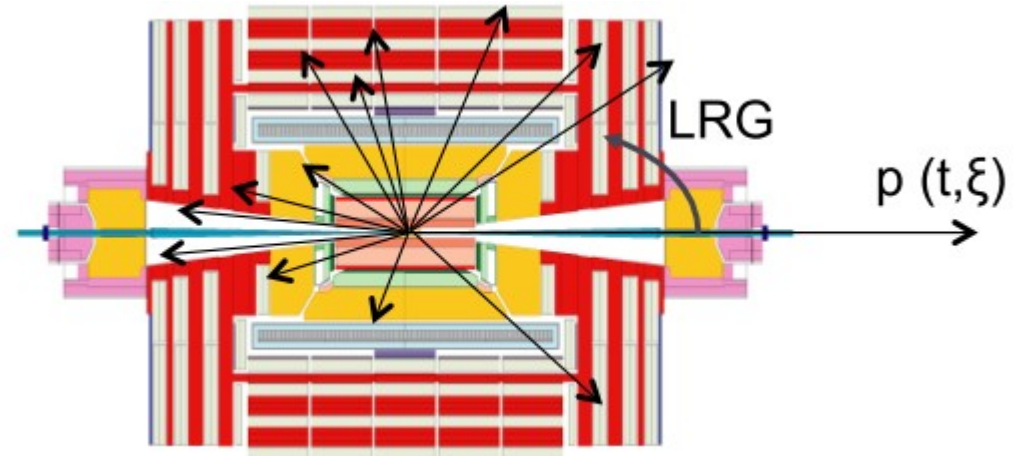
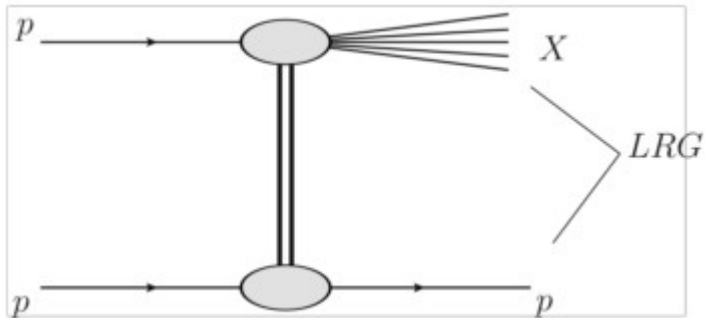
- Beam Scintillator Counters - BSC
- 10.86 m from interaction point (both sides)
- Each BSC is a set of 16 tiles
- Designed to provide hits and coincidence rates

BSC

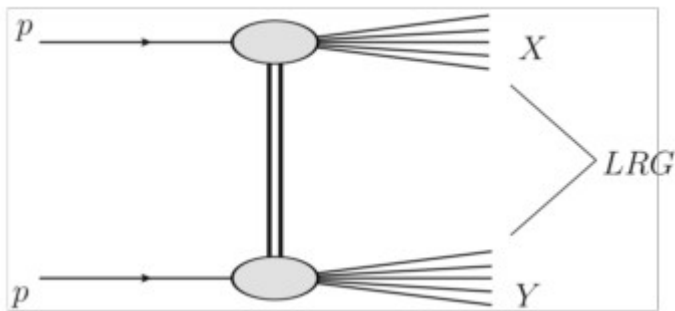


# Diffraction at CMS

## Single-diffractive dissociation SD

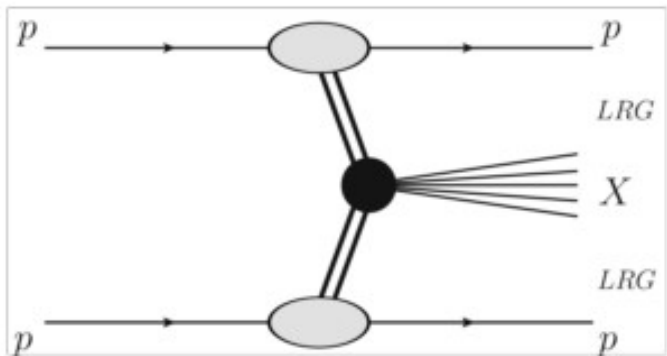


## Double-diffractive dissociation DD



- Diffractive events are an important fraction of MB events
- Without hard scale set - soft diffraction

## Central-diffractive dissociation CD



- Large differences between the models implemented in Monte Carlo generators
- Observation and measurement of soft diffraction characteristic an important ingredient of models testing and tuning

## Selection on trigger

- Coincidence of signals in BPTX (presence of two proton bunches)
- Activity at least in one BSC (at one side of CMS)

## General selection

- Vertex with at least 3 tracks and with  $|z| < 15$  cm
- Rejection of beam halo events
- Rejection of beam background events
- Rejection of events with large signals consistent with noise in HCAL

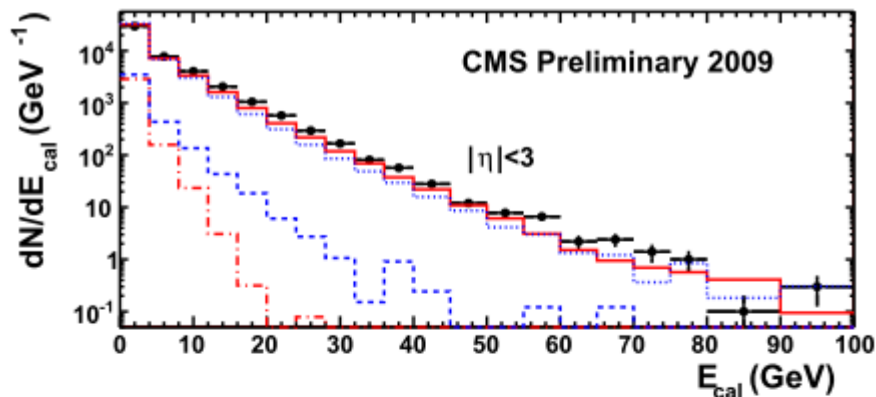
At 0.9 TeV : **207 000** events selected

At 2.36 TeV : **11 800** events selected

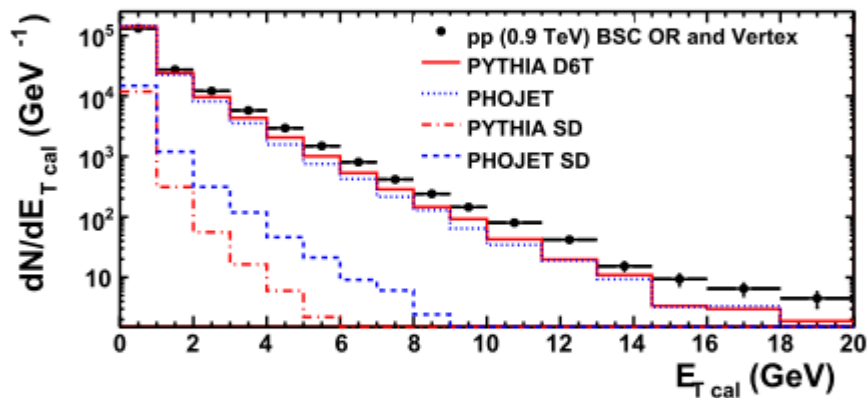
with residual contamination of beam-gas  $< 1\%$  (estimated from non-colliding bunches)



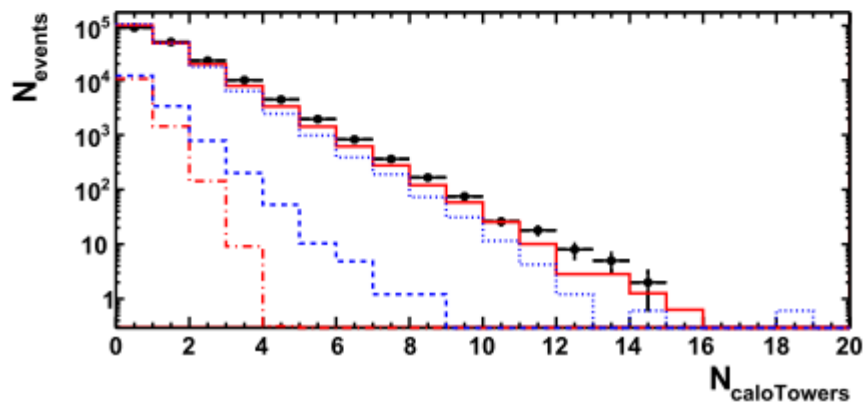
## 0.9 TeV



Energy distribution in calotowers in central CMS calorimeters (excl. HF)



Transverse energy distribution in calotowers in central CMS calorimeters (excl. HF)

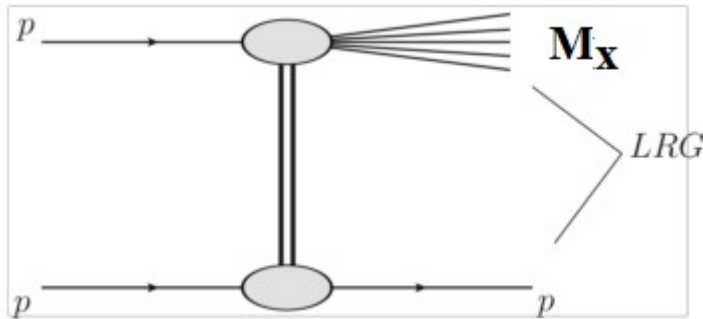


Multiplicity of calotowers in central CMS calorimeters (excl. HF), threshold of 3 GeV

All distributions - uncorrected  
 MC normalised to data

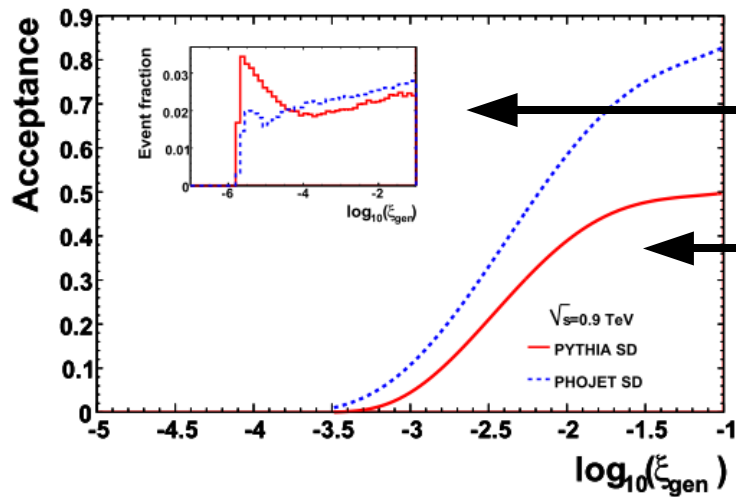
# Acceptance for SD

Acceptance as a function of  $\xi$  (fractional momentum loss of the scattered p):



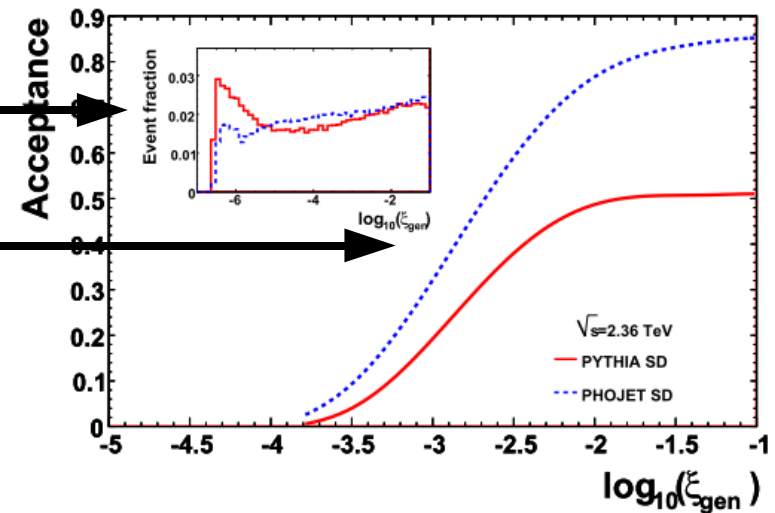
$$\xi = (M_x)^2 / S$$

PYTHIA and PHOJET different modeling of diffraction  
 → different selection efficiency



Generator level

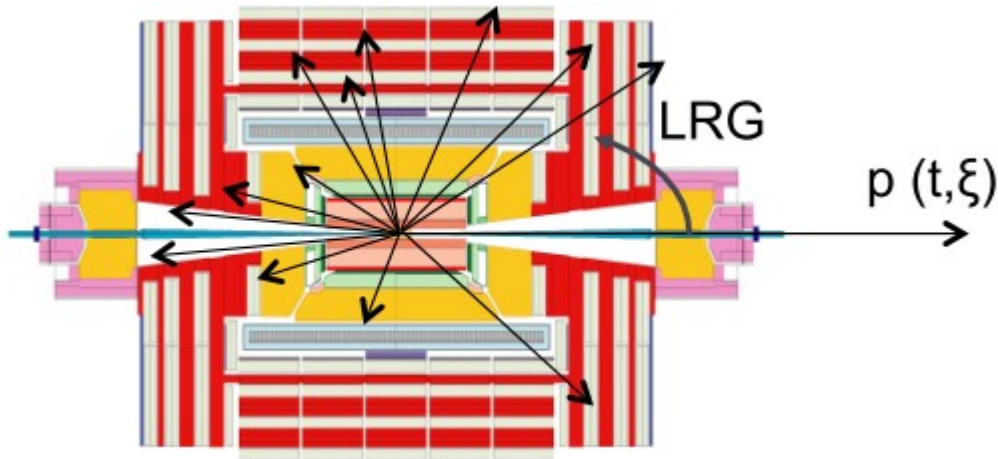
Detector level



Inefficiencies for: low  $\xi$  → escape undetected  
 low charge activity

SD efficiency: 0.9 TeV → 18% (PYTHIA), 32% (PHOJET)  
 2.36 TeV → 20% (PYTHIA), 37% (PHOJET)

# Observation of diffraction



Variables:

$$1) \sum (E_i \pm p_{z,i})$$

where sum runs over all calorimeters including HF,  $p_{z,i} = E_i \cos \theta_i$   
approx. twice the pomeron energy  
**for diffraction peaks at small values**

2)  $E_{HF}$  - total energy deposit in HF  
**diffractive events** with rapidity gap extending over HF appears in the **first bin** of this distribution

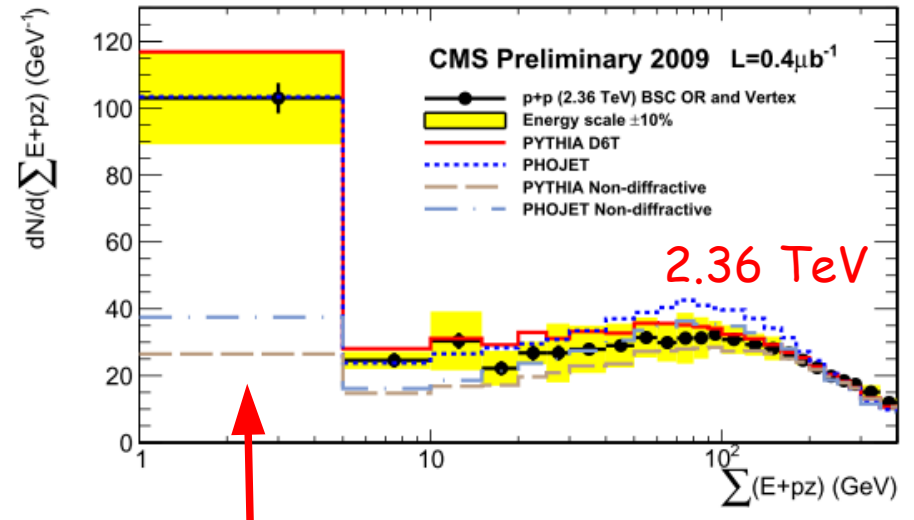
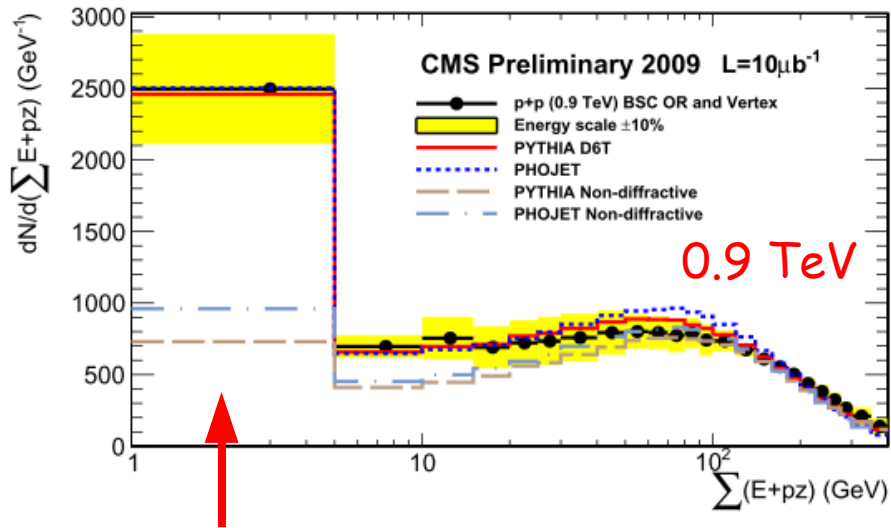
3)  $N_{HF}$  - multiplicity of the towers above threshold of 4 GeV  
**diffractive events cluster at zero multiplicities**

All variables are sensitive to the calorimeter energy scale uncertainty  $\rightarrow$  **10%**

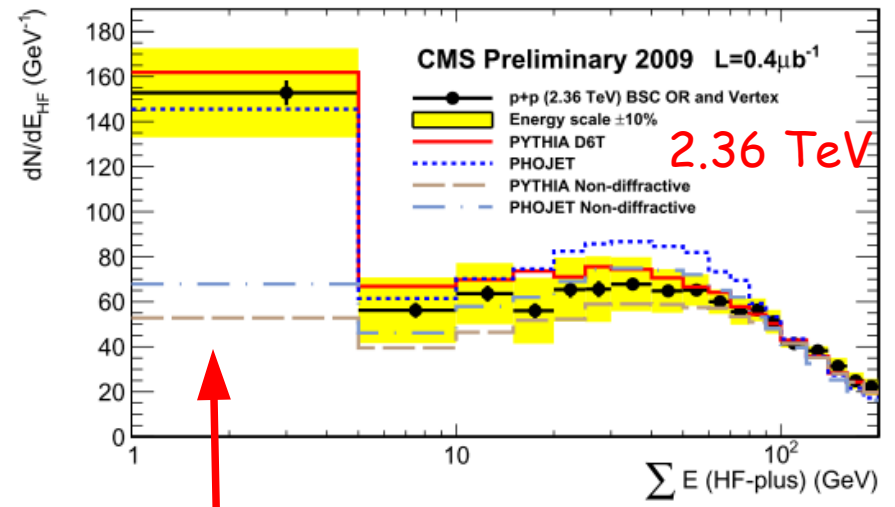
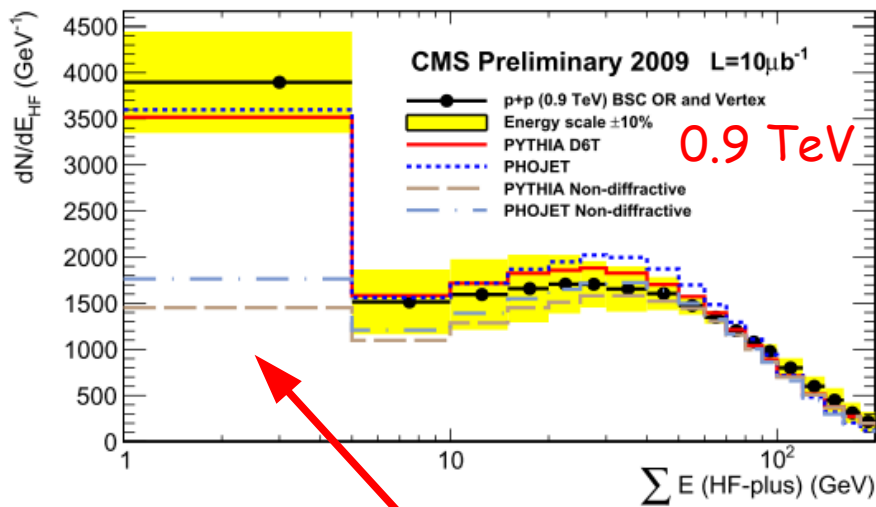


# Observation of diffraction

Comparison with PYTHIA-6 (D6T tune) and PHOJET

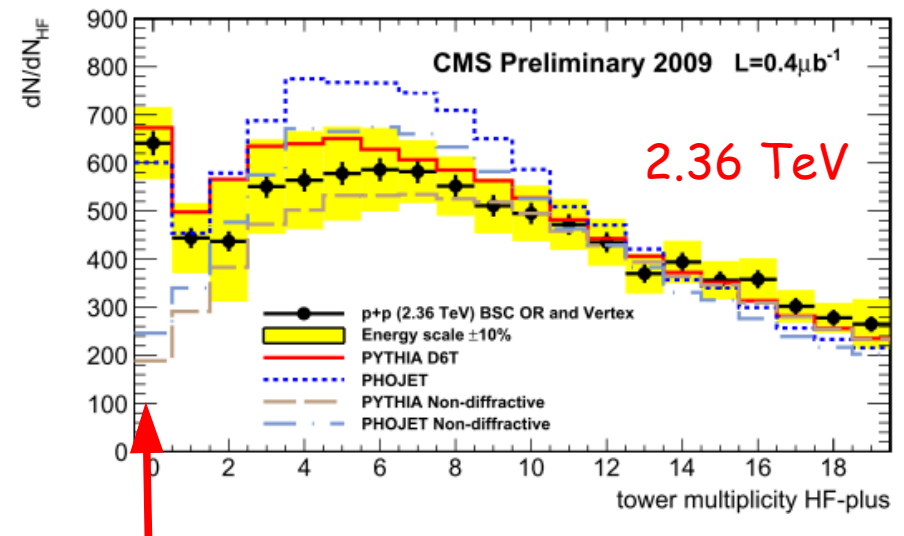
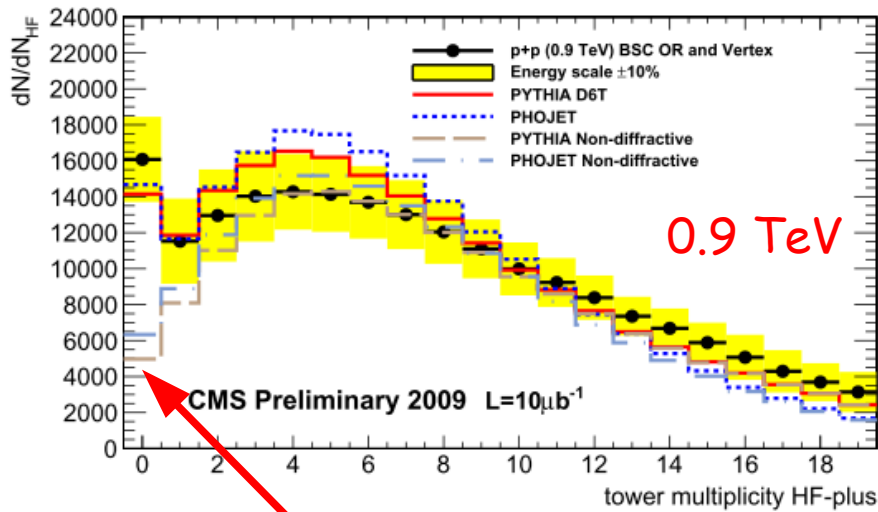


Clear sign of diffraction at both energies, in agreement with PYTHIA and PHOJET



Rapidity gap extending over HF(plus)

# Observation of diffraction



Rapidity gap extending over HF(plus)

Both - PYTHIA and PHOJET describes well inclusive spectra

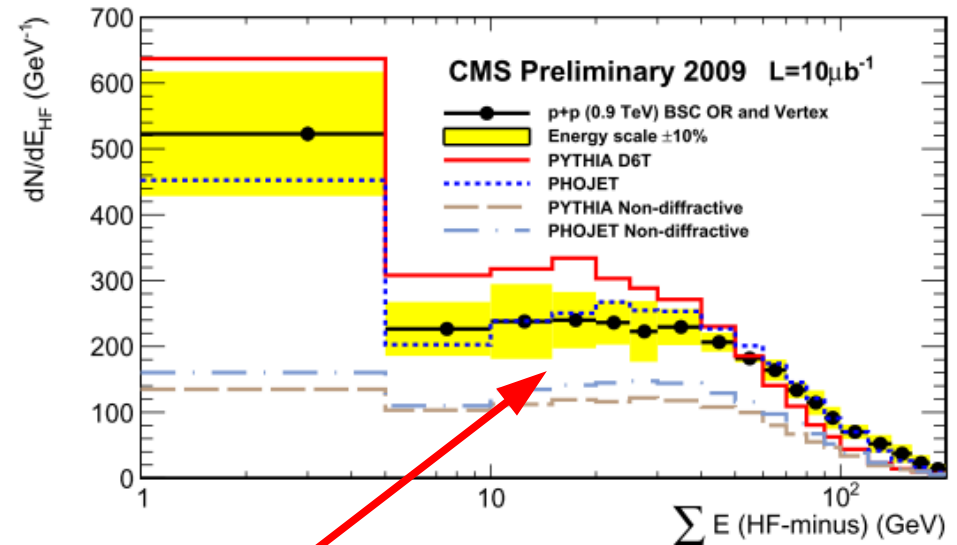
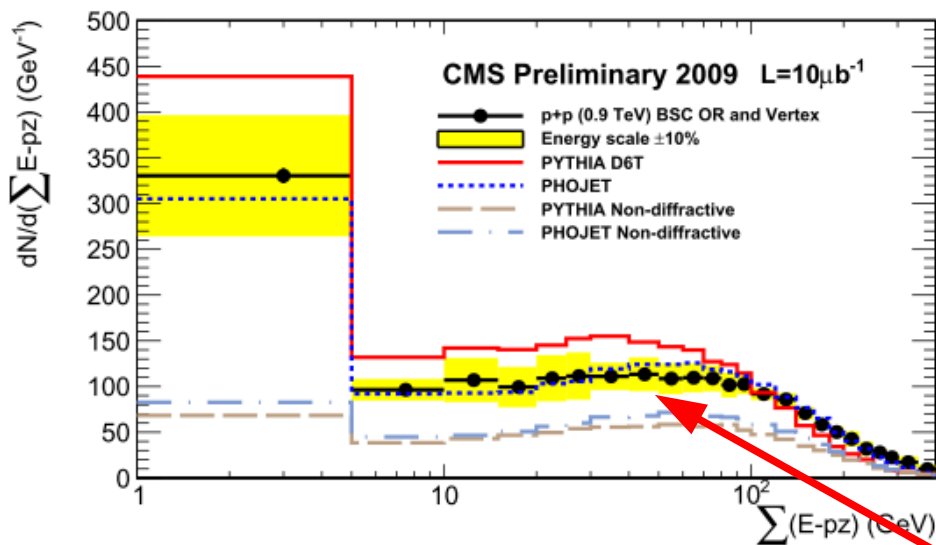
PYTHIA describes better higher-energy (non-diffractive) part of spectrum

# Enhancing diffractive component

Requirement: low activity at one side of HF calorimeter  
 → SD component is enhanced in the Minimum Bias data

Test the SD diffractive component in Monte Carlo

$$E_{\text{HF(plus)}} < 8 \text{ GeV}$$



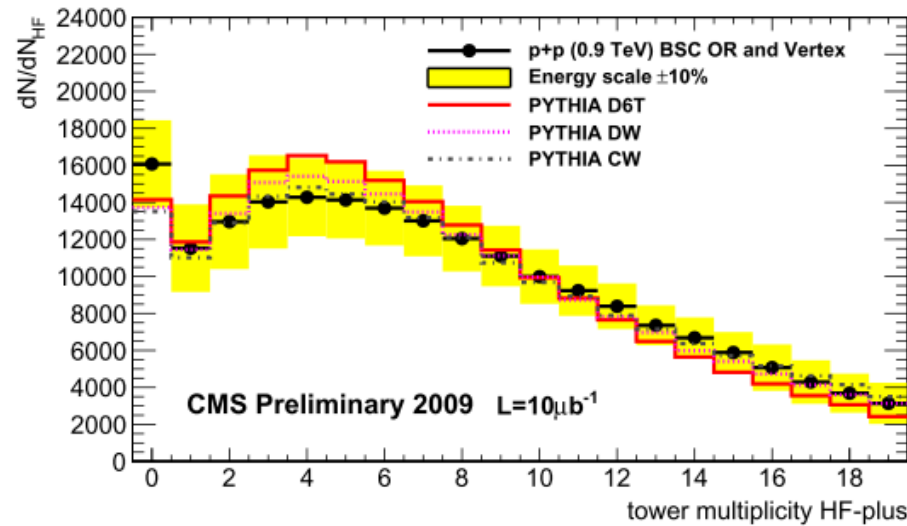
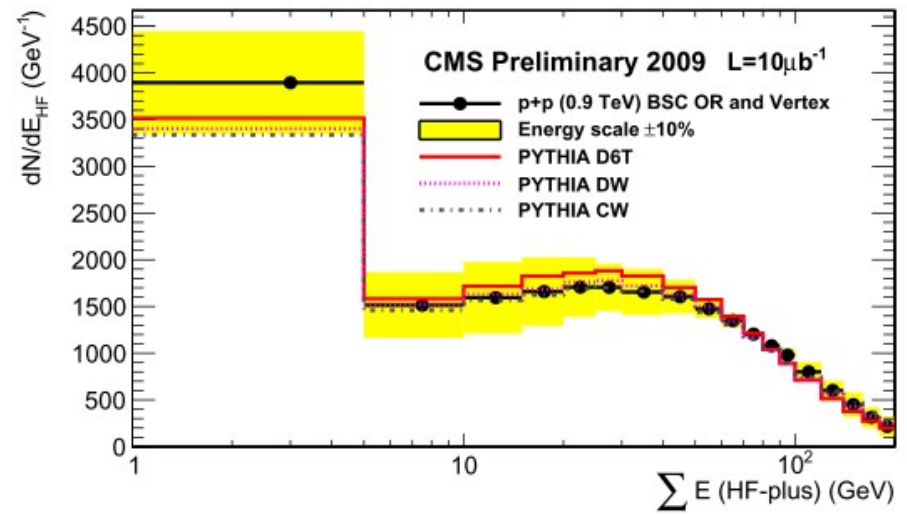
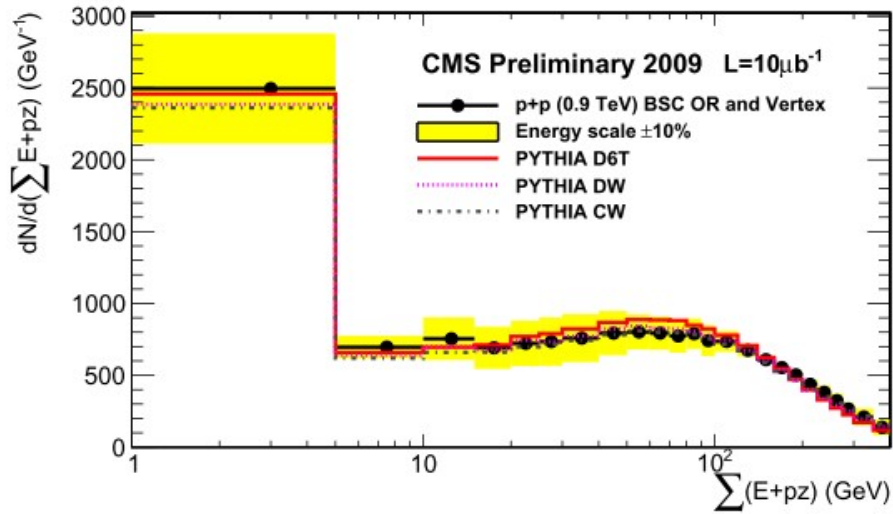
PHOJET agrees better with the data

- especially for a high mass diffractive system
- PYTHIA-6 shows a softer spectrum



# Different UE tunes

## Different PYTHIA tunes: DW and CW (comparison to D6T)

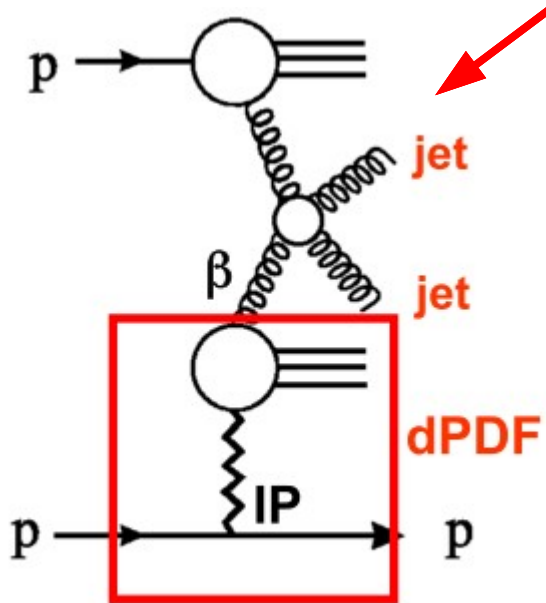


Given the **present** systematic uncertainties, the data **cannot** discriminate between tunes

# Hard diffraction

## Factorization:

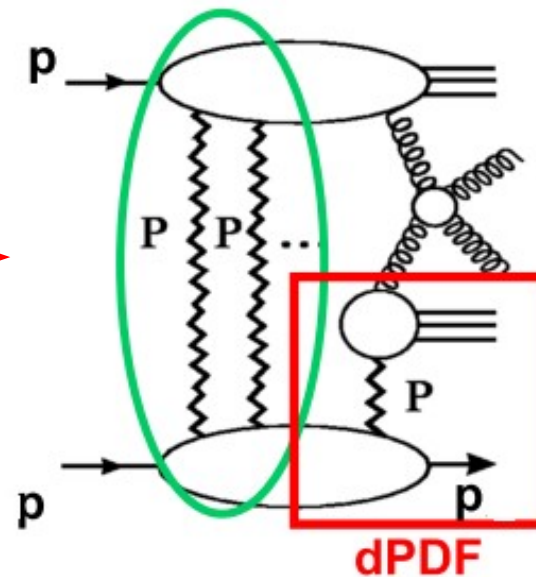
Hard scattering  
(hard scale eg. jets)



Diffractive PDFs

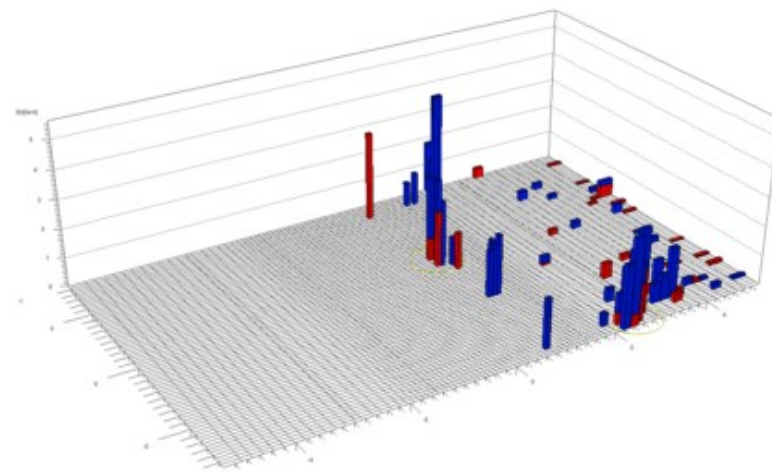
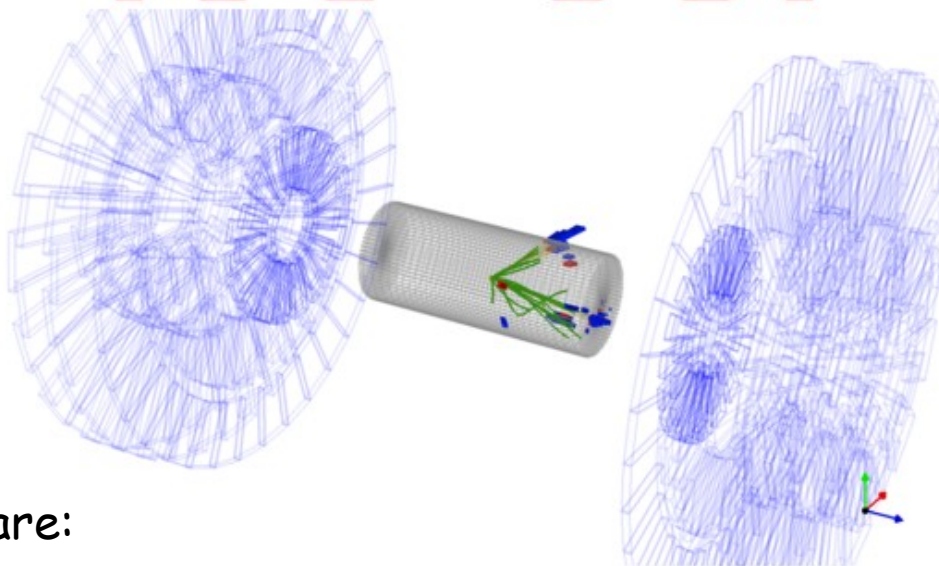
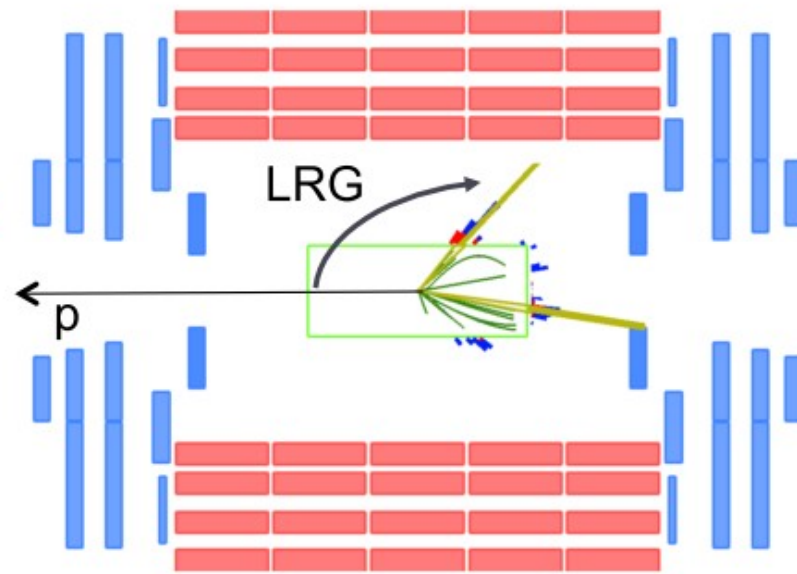
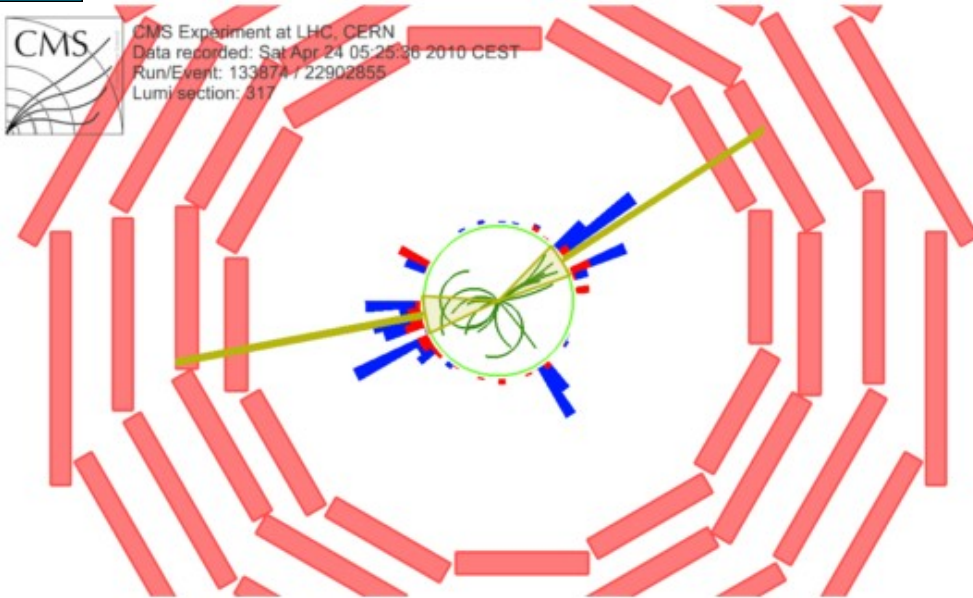
broken

Soft interactions/rescatterings among spectator partons  
 - fill the rapidity gap  
 - suppress visible x-section



- At Tevatron suppression of  $O(10\%)$  with respect to HERA
- At LHC predictions between vary by order of magnitude
- An important measurement at early LHC

# Hard diffraction



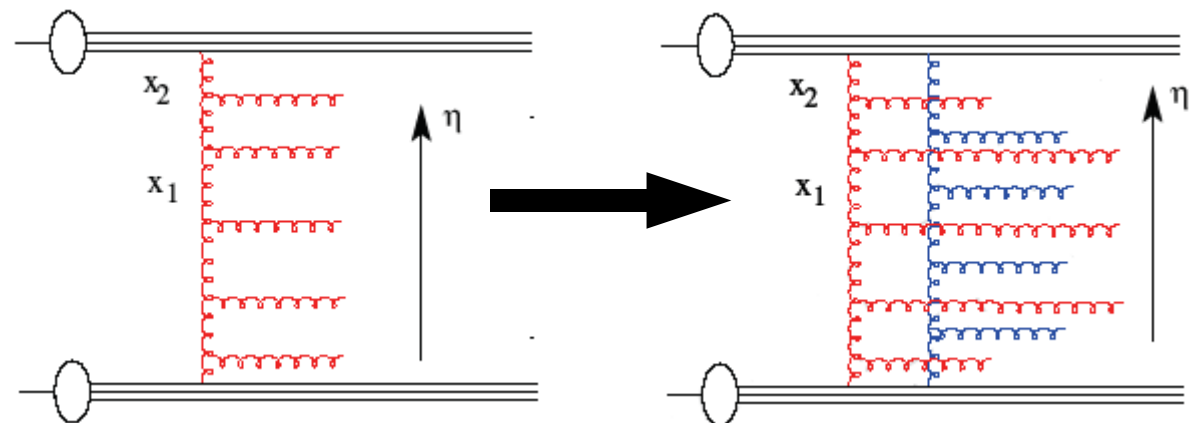
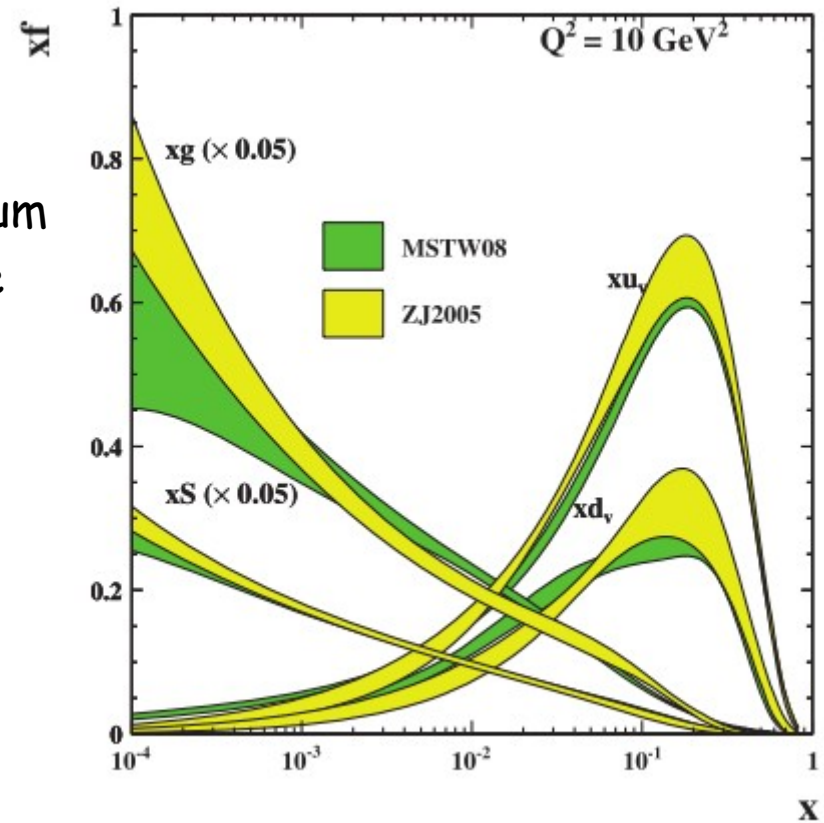
Visible are:

- calotowers with  $\eta < 3.0$  and  $E > 1.5 \text{ GeV}$
- $\eta > 3.0$  and  $E > 2.0 \text{ GeV}$
- tracks with  $p_T > 0.5 \text{ GeV}$

$p_T(\text{jet1}) = 43.5 \text{ GeV}$        $n(\text{jet1}) = 0.83$   
 $p_T(\text{jet2}) = 36.9 \text{ GeV}$        $n(\text{jet1}) = 2.55$



- A logical step before going to jets studies
  - but also a **meaningful, new** physics result
- At very large centre of mass energies, the momentum fraction of the proton carried by the partons in the hard scattering ( $x_1, x_2$ ) can become very small and the parton densities become very large.
- Probability for more than one partonic interaction per event increases.
- This approach is described in the **models** of **multiparton interactions**.
- Models implemented in Monte Carlo event generators need parameters to be adjusted to describe the measurement.
- Parameters tuned to data from Tevatron ( $|\eta| < 3$ ).



# Energy flow in the forward region

- Measurement done with Hadronic Forward calorimeter:  $3.152 < |\eta| < 4.903$
- Plans: extend it to CASTOR and to ZDC
- Three different cms energies included: 900 GeV, 2360 GeV, 7000 GeV
- The measurement done at the detector level - no factors correcting it to the hadron level applied
- A comparison with the Monte Carlo generators predictions at the detector level

- Distributions studied:

$$E_{FLOW}(dijet) = \frac{1}{N_{dijet}} \frac{\Delta E}{\Delta \eta}(dijet)$$

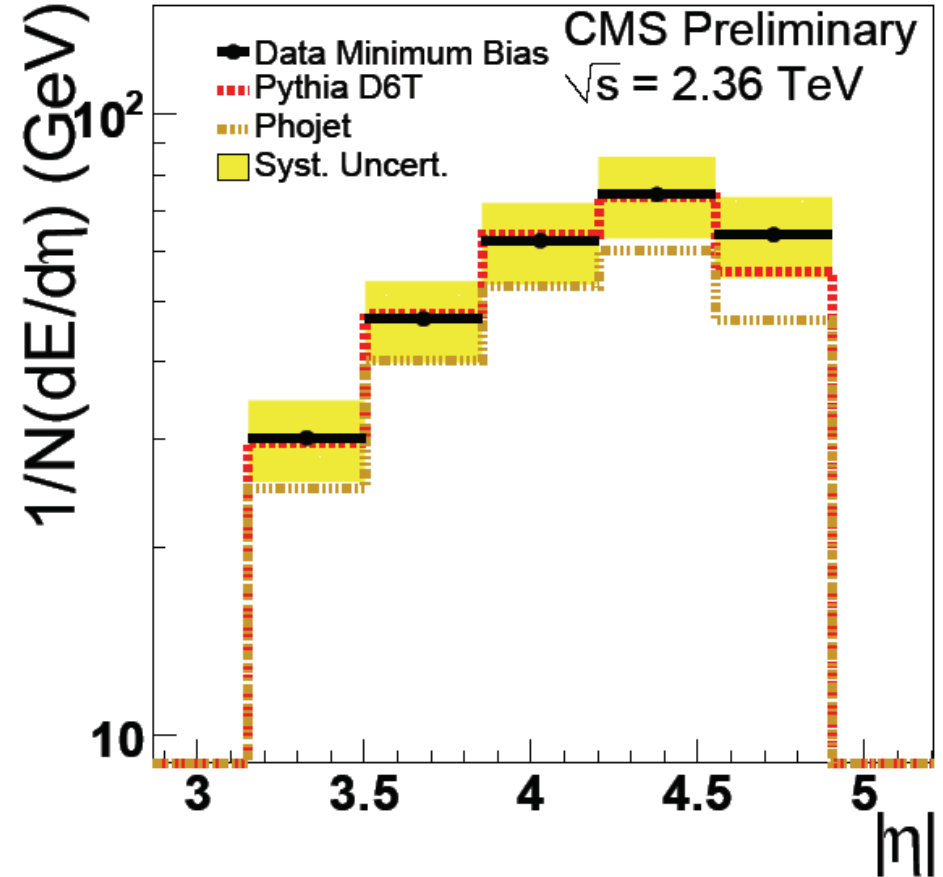
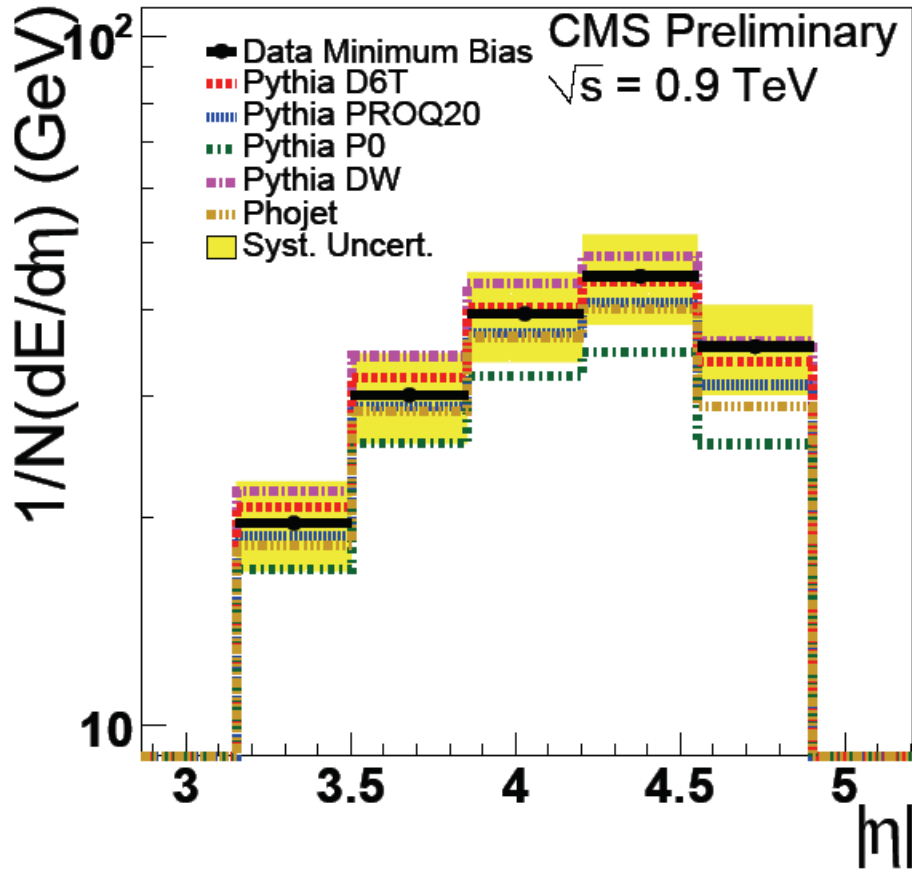
$$E_{FLOW}(minbias) = \frac{1}{N_{minbias}} \frac{\Delta E}{\Delta \eta}(minbias)$$

- Definition of Minimum Bias sample: all events trigger with MB trigger: activity at both sides of IP (coincidence between BSC) + vertex reconstructed
- Definition of Dijet sample: for 900/2360 GeV  $p_T > 8$  GeV, for 7000 GeV  $p_T > 20$  GeV,  $|\eta| < 2.5$

$\sqrt{s}$	900 GeV	2.36 TeV	7 TeV
MB sample	177475	10245	3713294
Dijet sample	433	86	4292

# Energy flow in the forward region

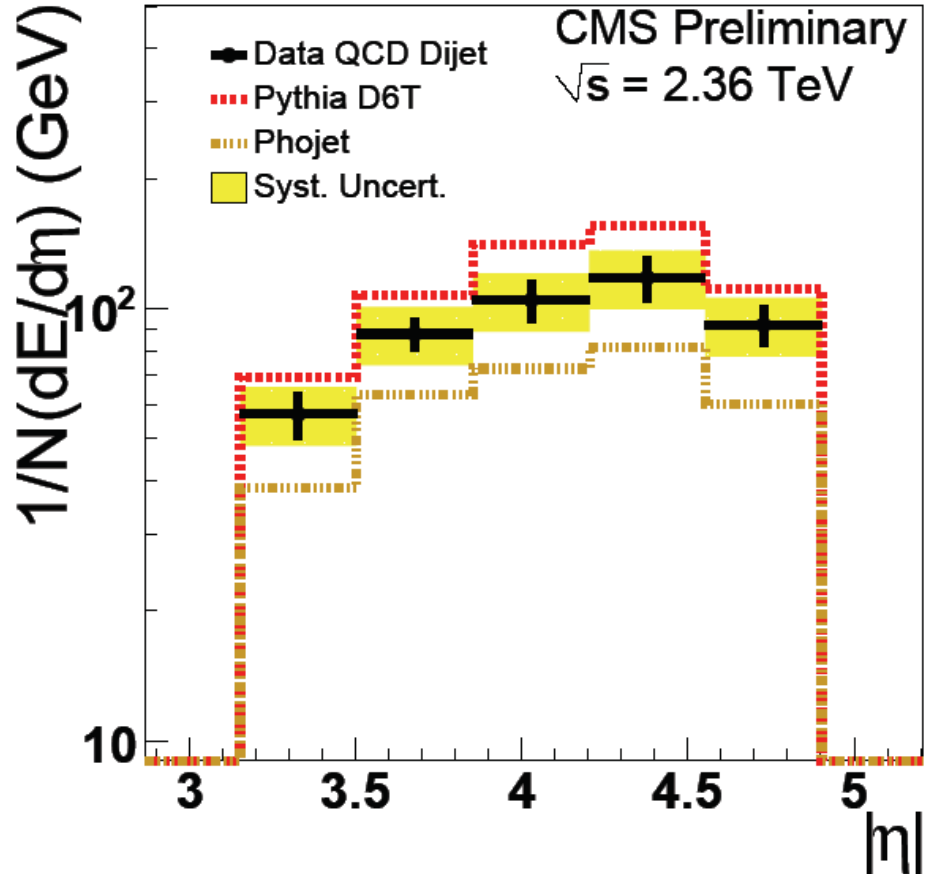
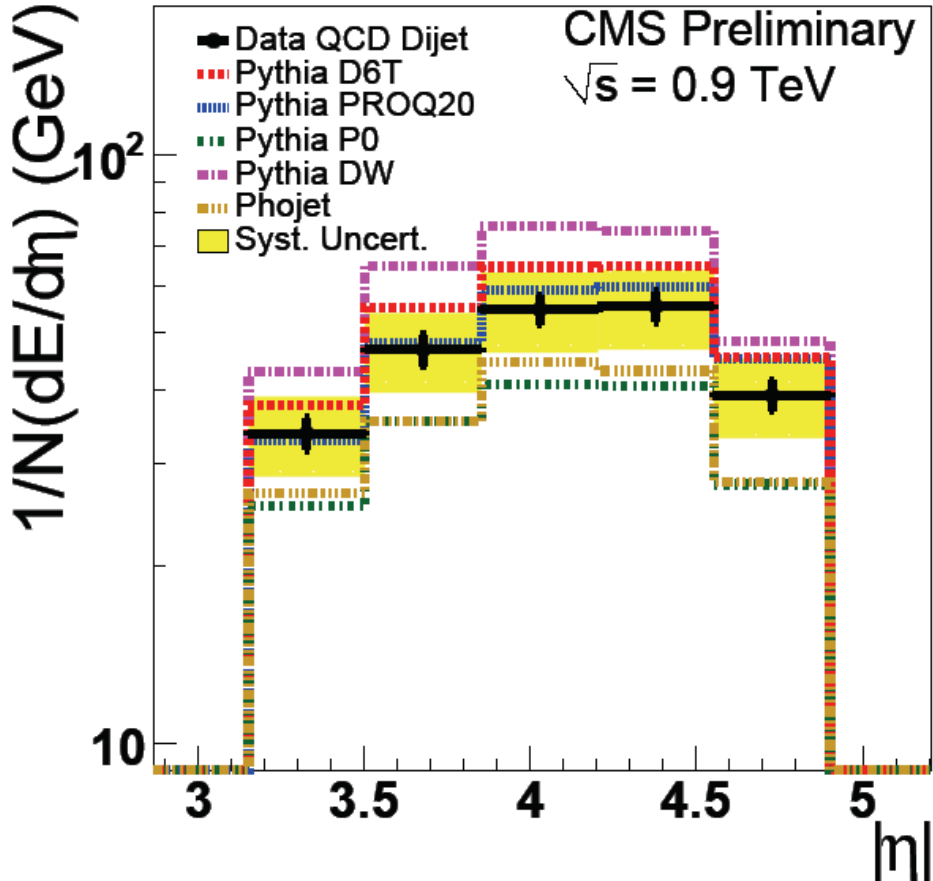
Energy flow in the Minimum Bias sample at 900/2360 GeV:



At 900 GeV the energy flow in minimum bias events is best described by the D6T tune, whereas the PROQ20, P0 tune and PHOJET is lower than the measurement.

# Energy flow in the forward region

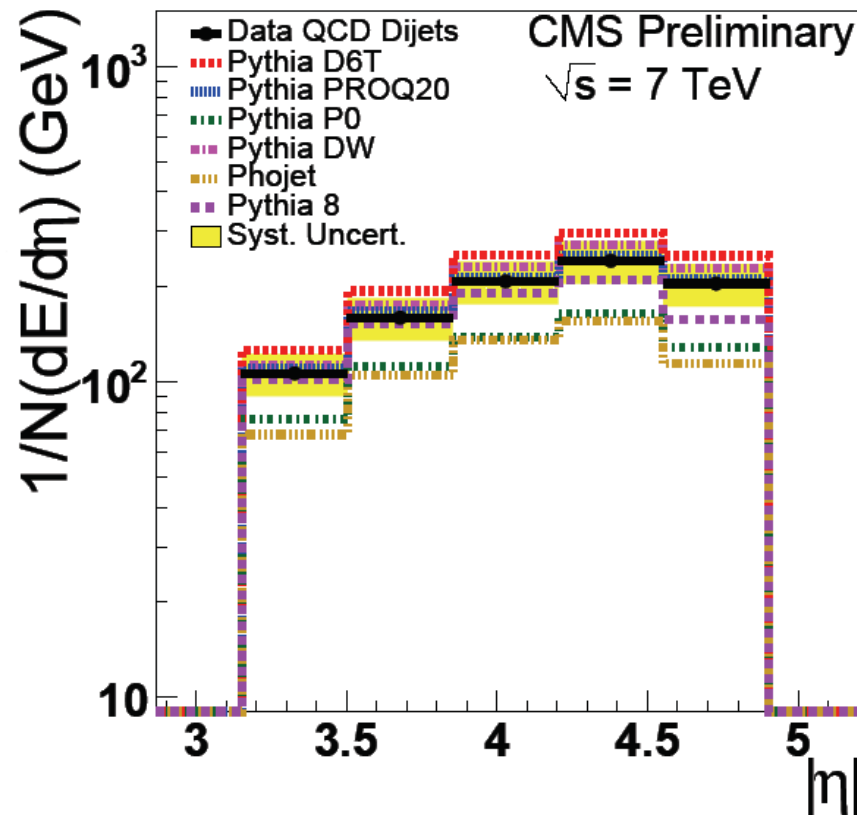
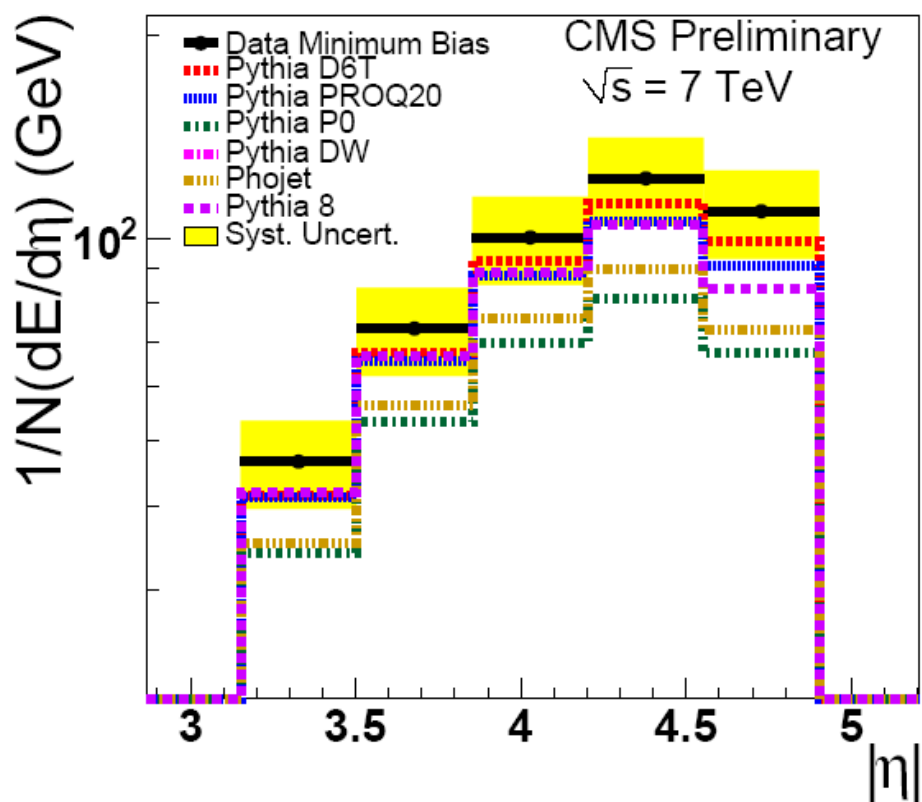
Energy flow in the Dijet sample at 900/2360 GeV:



In dijet events the increase of energy flow with increasing centre-of-mass energy is reproduced by the simulations. Here, the D6T tune predicts too high energy flow, whereas the PROQ20 tune is best and the P0 tune and PHOJET is too low.

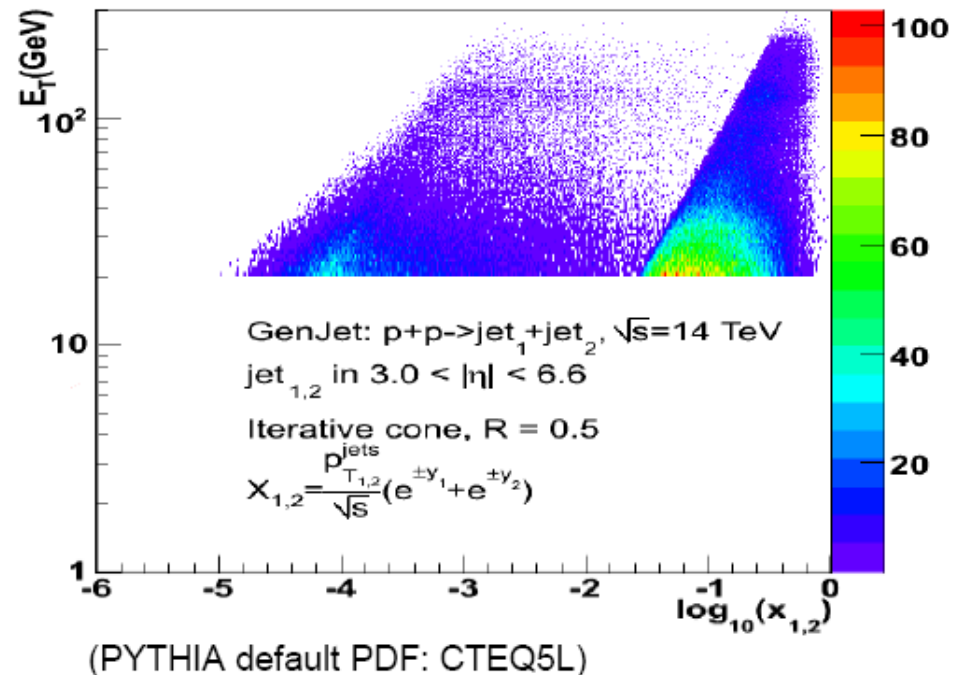


## Energy flow in the MB and Dijet samples at 7000 GeV:



- At 7000 GeV the predicted energy flow in minimum bias events is below the measurement for all tunes, the prediction of PYTHIA8 is similar to the tune PROQ20.
- For dijet sample D6T tune predicts too high energy flow, whereas the PROQ20 tune and PYTHIA8 are best and the P0 tune and PHOJET is too low.

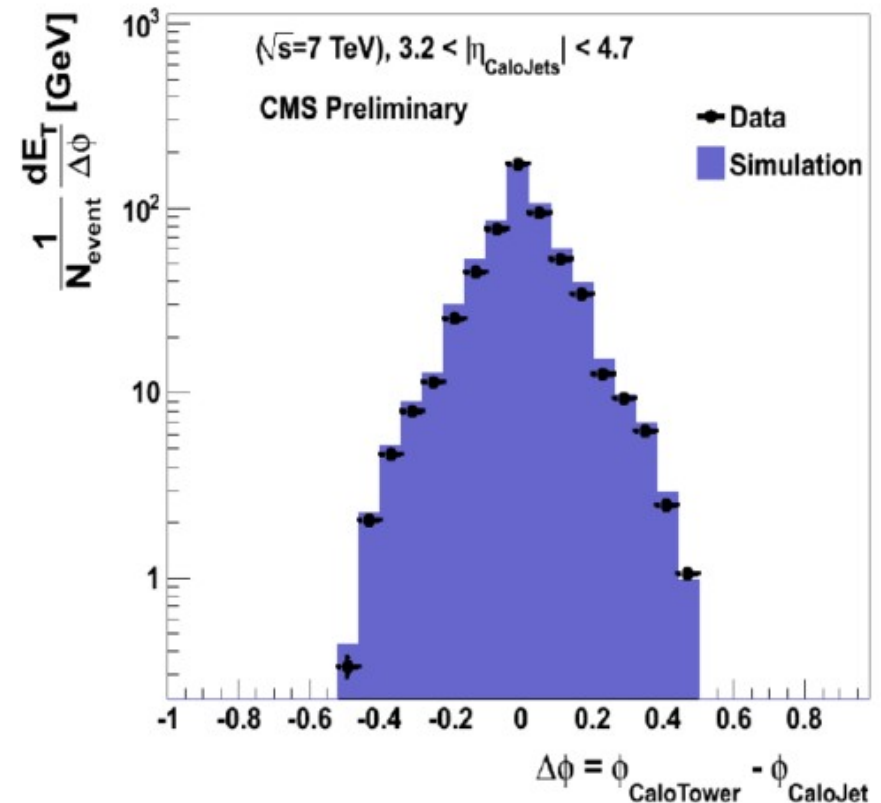
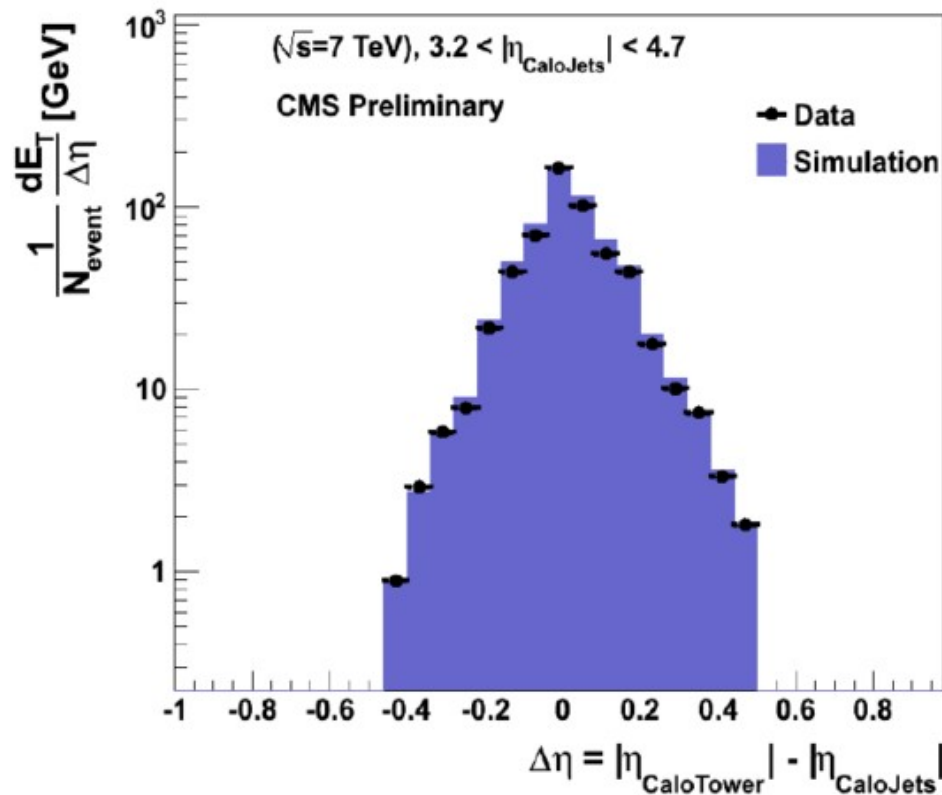
- Jets productions has never been investigated in such a forward region as the one covered by CMS HF calorimeter
- First measurement of forward jets in  $3.2 < |\eta| < 4.7$
- Forward jets probe low x region
- First step: **validate** the jets reconstruction in the forward region
- Trigger selection  $\rightarrow$  BSC coincidence
- Integrated luminosity  $10 \text{ nb}^{-1}$
- Jets reconstructed with anti-kT (R=0.5) algorithm
- $35 < E_T < 120 \text{ GeV}$  (energy corrected for detector effects)



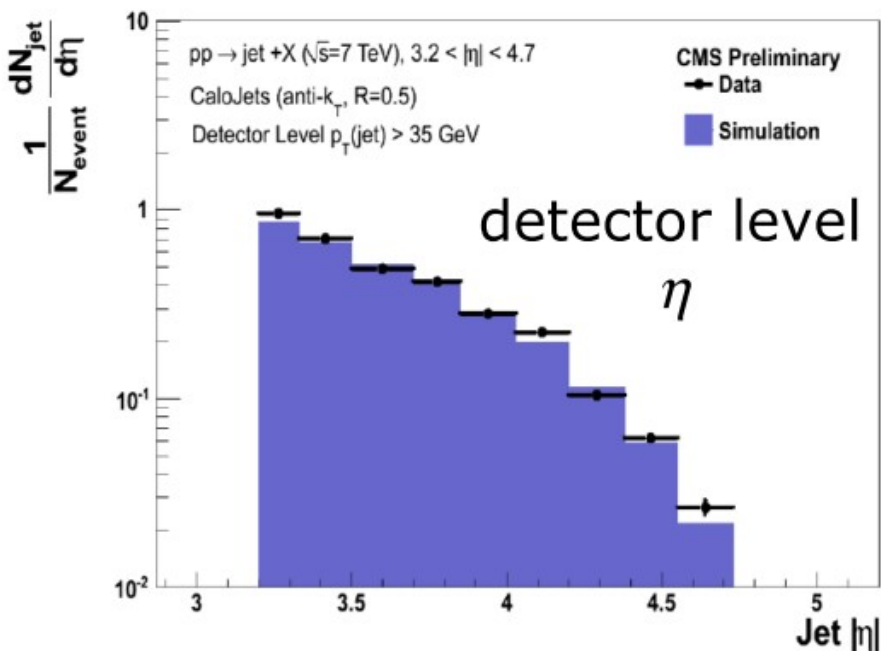
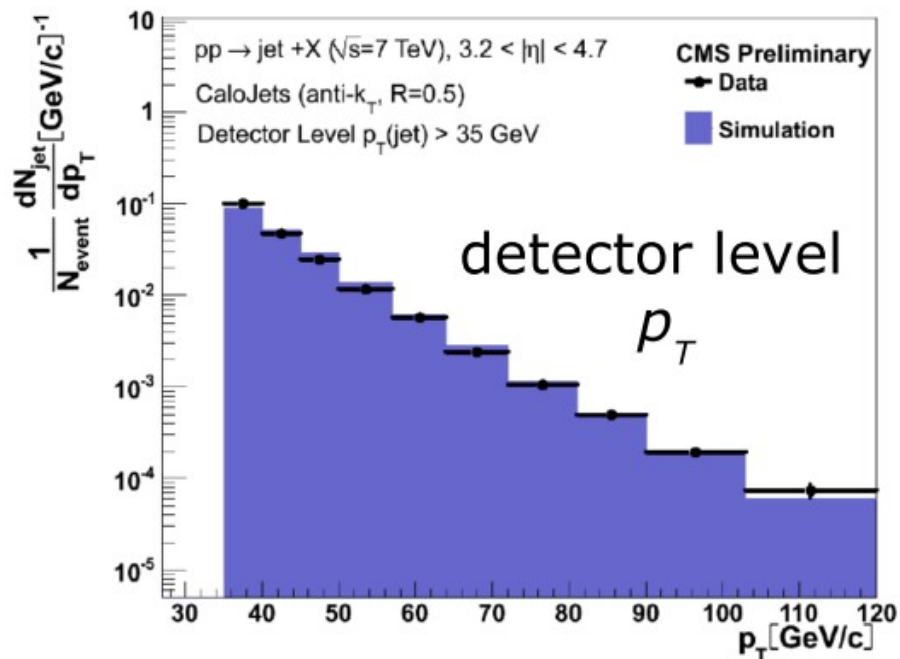
# Jets in forward region

- **Transverse energy  $E_T$  flow inside jet cone** - size and shape of calorimeter jets in the forward region
- Test of the description of data by MC - PYTHIA-6 D6T

→ transverse energy flow well described by MC



- $p_T$  and  $\eta$  distributions at the detector level
- No unfolding back to hadron level applied
- No systematic uncertainty taken into account
- Fair agreement between the the data and PYTHIA-6 D6T tune



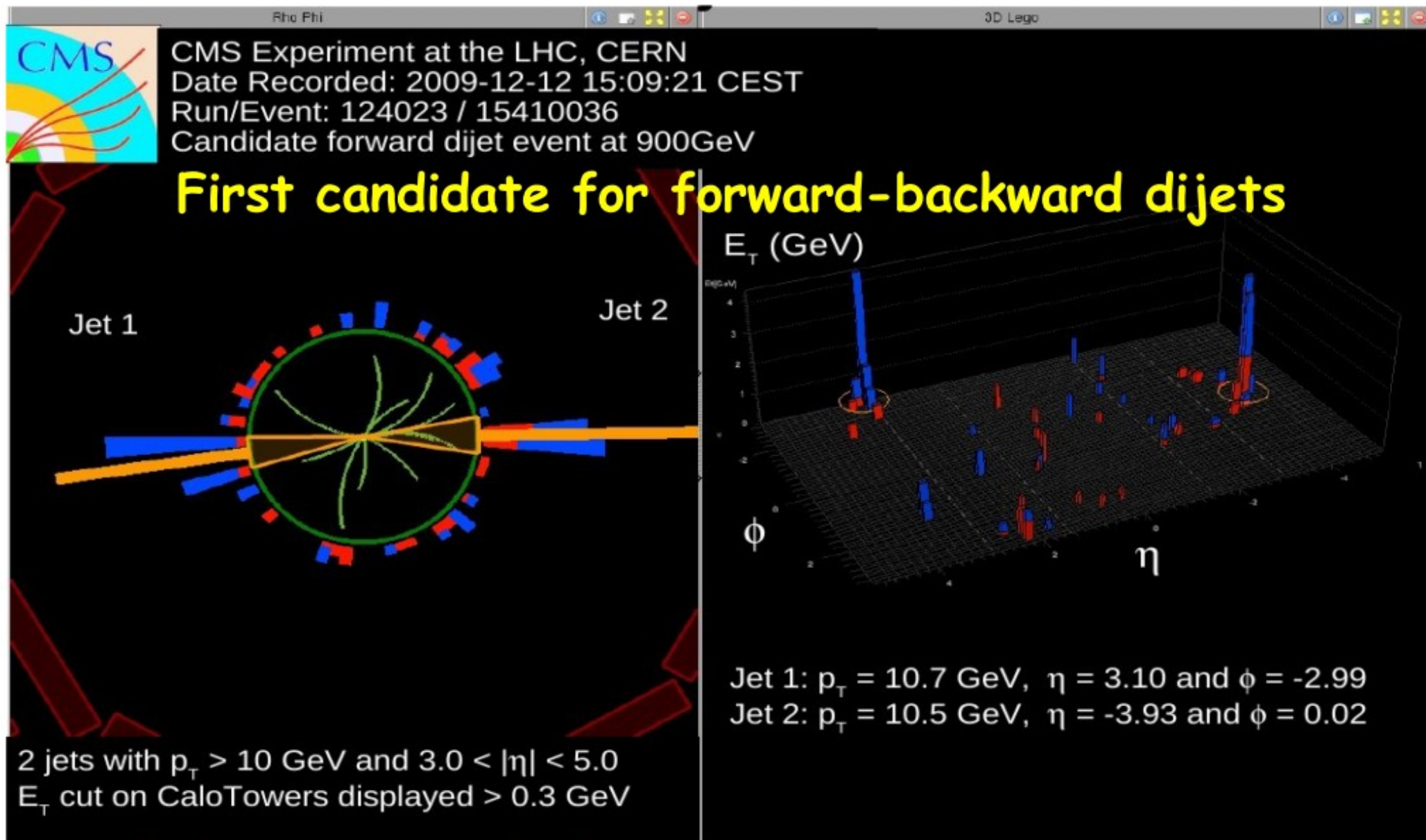
- Expected resolutions from MC:

- $\sigma(p_T)/p_T \sim 15\%$  at 20 GeV,  $\sim 12\%$  at 100 GeV
- $\sigma(\Delta\eta), \sigma(\Delta\phi) \sim 0.035$  at 20 GeV,  $\sim 0.025$  at 100 GeV



# Jets in forward region

First pairs of jets with large rapidity interval in-between observed (MN dijets)

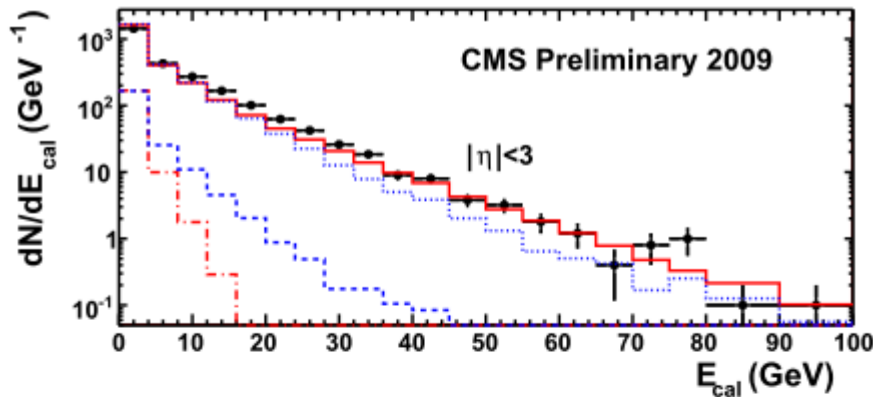


- **Rediscovery of diffraction** in the CMS minimum bias data: 0.9 and 2.36 TeV
- Fair agreement with the Monte Carlo models predictions
- **First observation of diffractive events with a hard scale** set by jets
- **First measurement of the energy flow in  $3.2 < |\eta| < 4.9$**  for Minimum Bias sample and for events with a hard scale set by central jets
- None of the MC can describe the energy flow in all aspects, at 7 TeV the energy flow is larger than in any MC predictions
- **First measurement of the jets in the  $3.2 < |\eta| < 4.7$**  range → validation of the forward jets reconstruction
- First measurement at 0.9, 2.36 and 7 TeV show very good performance of the CMS detector, especially its main forward calorimeter - HF

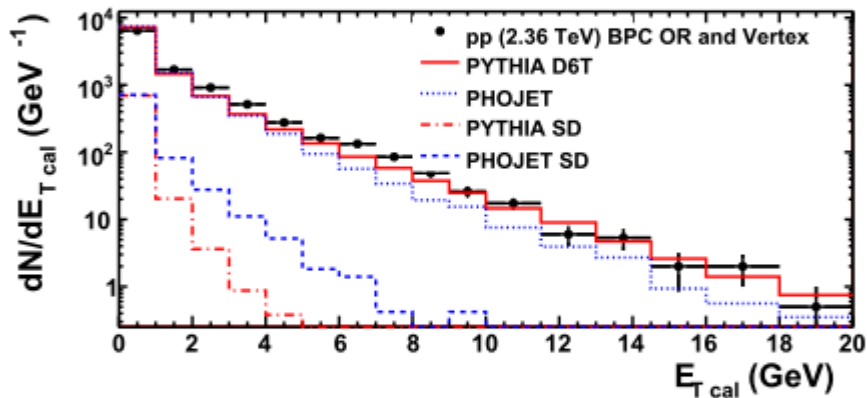
Spares

# Control plots

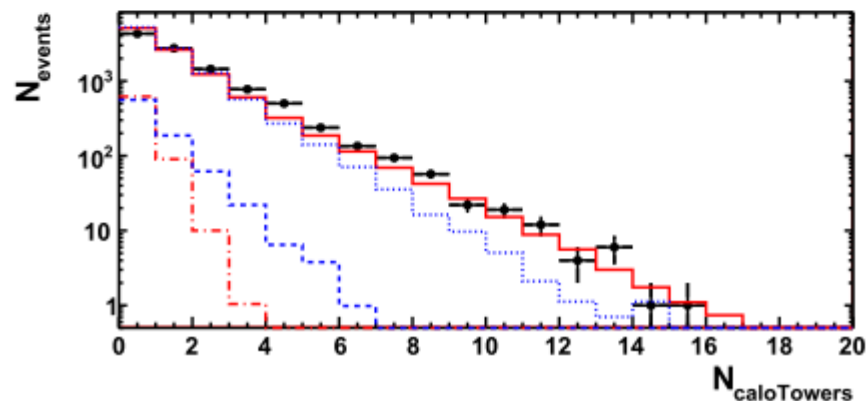
2.36 TeV



Energy distribution in calotowers in central CMS calorimeters (excl. HF)



Transverse energy distribution in calotowers in central CMS calorimeters (excl. HF)

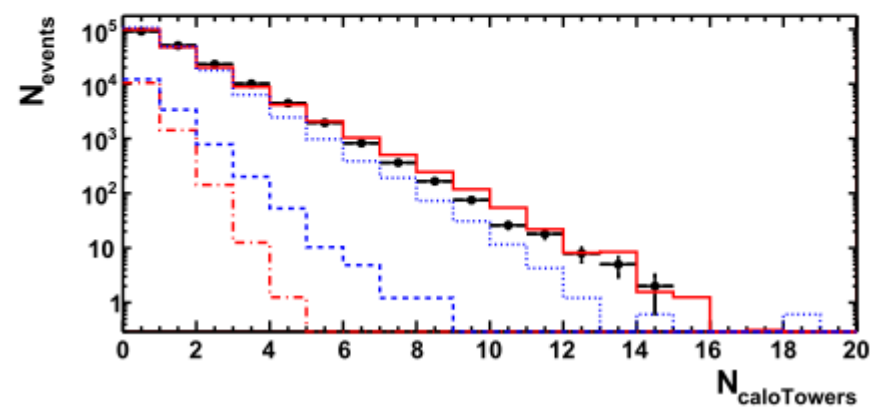
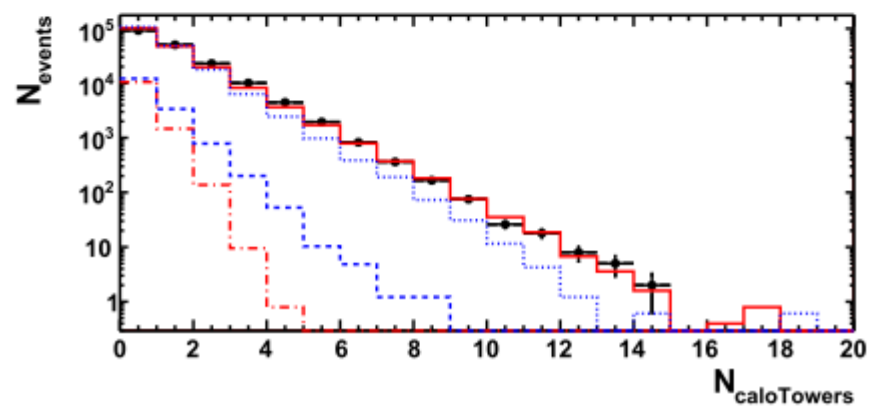
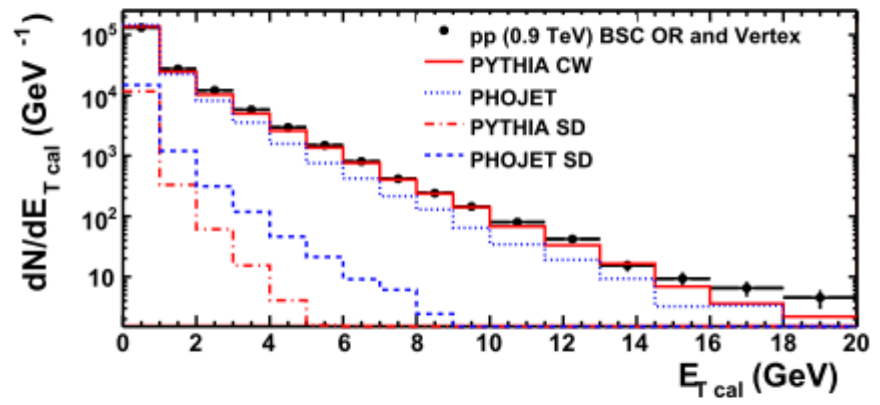
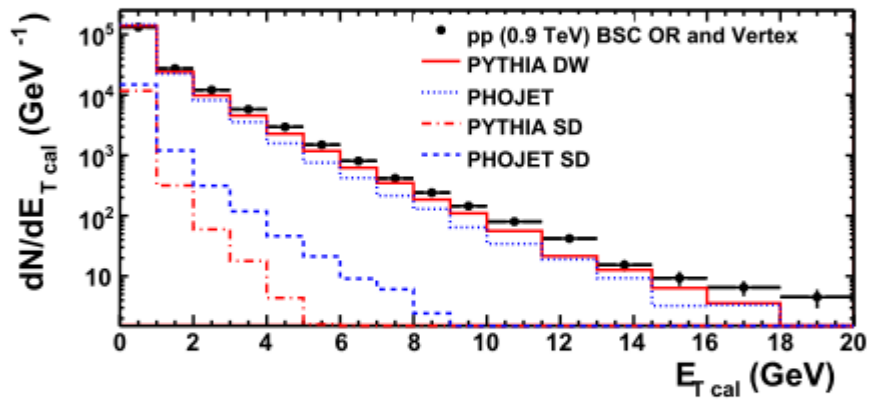
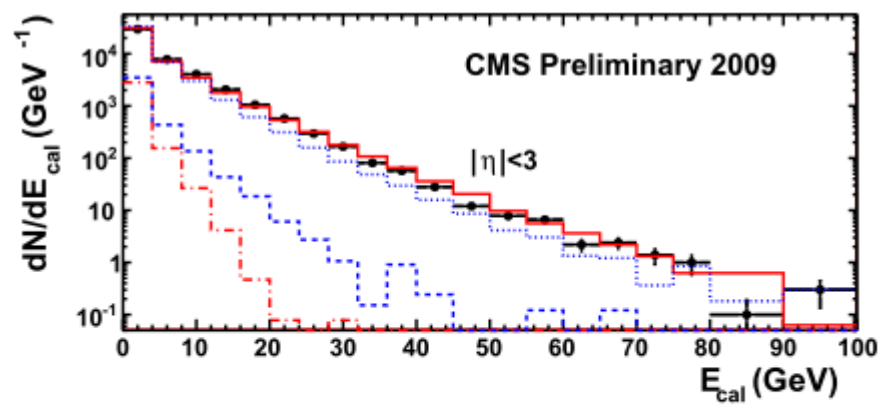
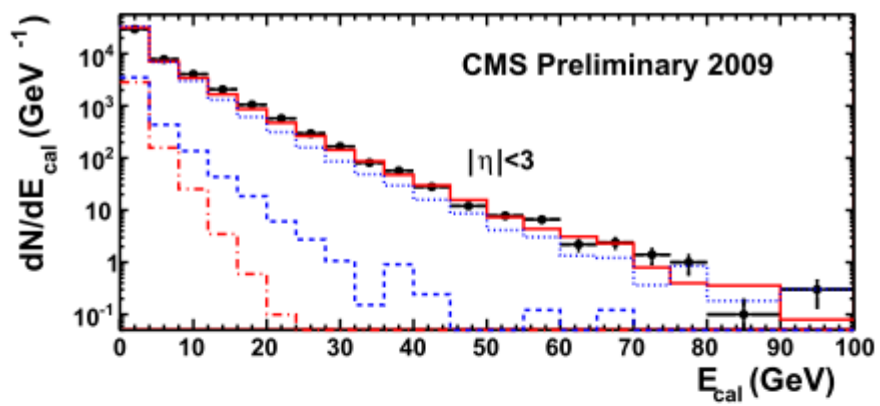


Multiplicity of calotowers in central CMS calorimeters (excl. HF), threshold of 3 GeV

All distributions - uncorrected  
 MC normalised to data



# Control plots (tunes)



# Tunes

- MPI model included in PYTHIA. The parameters of the model can be tuned - different sets of parameter values define different tunes.
- Avoid differences in hard scattering and MPI:  $\frac{1}{p_T^4} \rightarrow \frac{1}{(p_T^2 + p_{T0}^2)^2}$
- Where  $p_{T0}$  is parametrized:  $p_{T0}(\sqrt{s}) = p_{T0}(\sqrt{s_0}) \left( \frac{\sqrt{s}}{\sqrt{s_0}} \right)^\epsilon$
- Different pdfs, cuts for ISR and FSR, fragmentation model

		D6T (108)	DW (103)	Pro-Q20 (129)	P0 (320)
pdfs		CTEQ6L	CTEQ5L	CTEQ5L	CTEQ5L
$p_{T0}$	PARP(82)	1.84 GeV	1.9 GeV	1.9 GeV	2.0 GeV
$E_0$	PARP(89)	1.96 TeV	1.8 TeV	1.8 TeV	1.8 TeV
$\epsilon$	PARP(90)	0.16	0.25	0.22	0.26
fragmentation	standard	standard	standard	professor LEP tune	professor LEP tune
$Q_{\max}^2$ factor (ISR)	PARP(67)	2.5	2.5	2.65	1.0
$Q_{\max}^2$ factor (FSR)	PARP(71)	4.0	4.0	4.0	2.0

# Tunes

- Tunes of the PYTHIA generator (version 6.420): **D6T**, **DW**, **Perugia-0 (P0)**, **CW**
- **Pythia 8** (different model! only one tune along the lines of **P0**): version 8.135

PYTHIA **regularization** of the formal divergence of the leading order partonic scattering amplitude as the final state parton transverse momentum  $p_T$  approaches 0:

$$\left\{ \begin{array}{l} 1/\hat{p}_T^4 \rightarrow 1/(\hat{p}_T^2 + \hat{p}_{T_0}^2)^2 \\ \hat{p}_T(\sqrt{s}) = \hat{p}_{T_0}(\sqrt{s_0}) \cdot (\sqrt{s}/\sqrt{s_0})^\epsilon \end{array} \right.$$

Regularization: can be interpreted as inverse of effective color screening length

energy dependence

Reference value: e.g. at CDF  $\sqrt{s_0} = 1.8\text{TeV}$ ,  $\hat{p}_{T_0} = 2.0\text{GeV}/c$

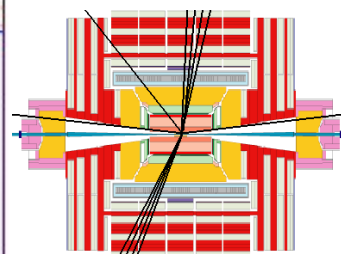
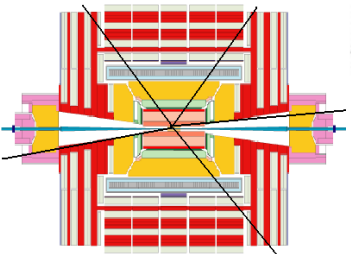
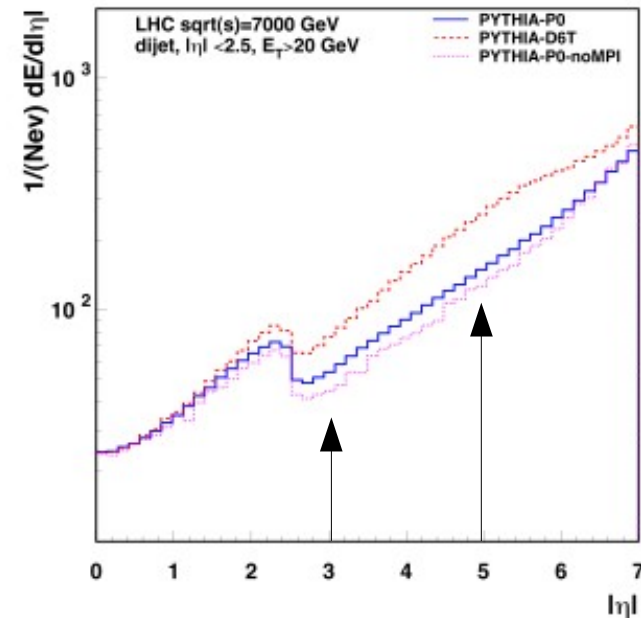
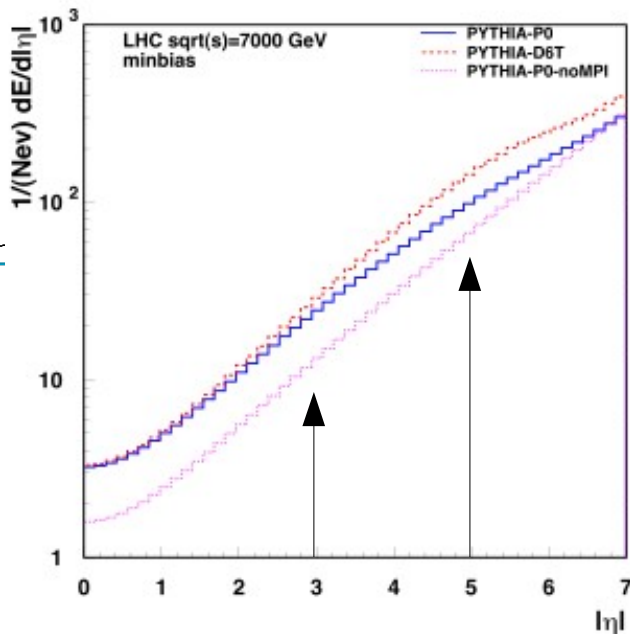
- Same parameter regularize **both MPI and hard scattering**: more MPI activity is predicted for smaller values of  $p_T^0$

Tune	$p_T^0(1.8\text{TeV})$	$\epsilon$	details
<b>D6T</b>	1.8 GeV/c	0.16	Consider ATLAS and LHCb studies on multiplicity at SPS; CTEQ6LL Parton distributions
<b>DW</b>	1.9 GeV/c	0.25	Consider 630GeV & 1.8TeV CDF results CTEQ5L parton distributions
<b>P0</b>	2 GeV/c	0.26	As above + New PYTHIA MPI model; PT ordered showers;
<b>CW</b>	1.8 GeV/c	0.3	Ad hoc for 900GeV CMS data, maximizing MPI but still compatible with Tevatron; default PYTHIA color reconnection; Parton distributions CTEQ5L

# Energy flow in the forward region

- The extrapolation of models to larger  $|\eta|$  is very uncertain, differences up to factors 5.
- The extrapolation of models to larger energies is also uncertain.
- Provide input to the determination of the parameters for the multiparton interaction models.

Predictions at **generator level** for two samples and for two Pythia6 tunes with MPI and no-MPI scenario





# Energy flow in the forward region

Systematic effects on the measurement:

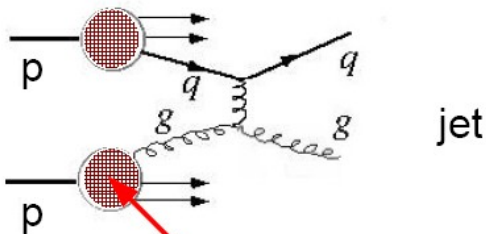
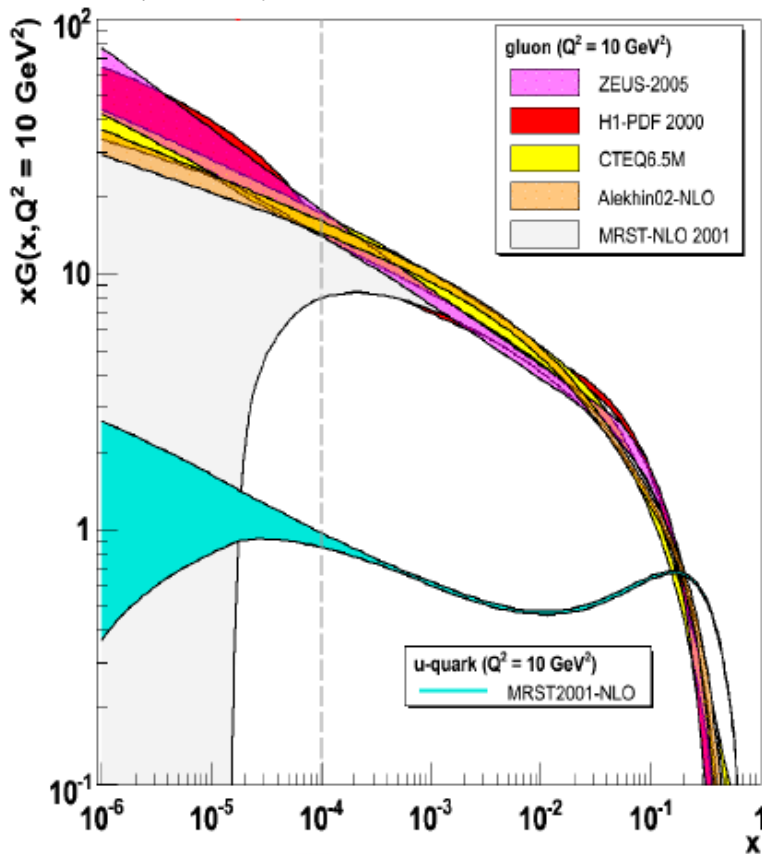
- Energy scale of HF (calibration → 15% - will improve in future)
- Position of interaction vertex
- Direct PMT hits → 3%
- Remaining noises in HF CaloTowers
- Random channel-by-channel miscalibration
- No beam-beam interactions

Negligible with comparison to HF energy scale

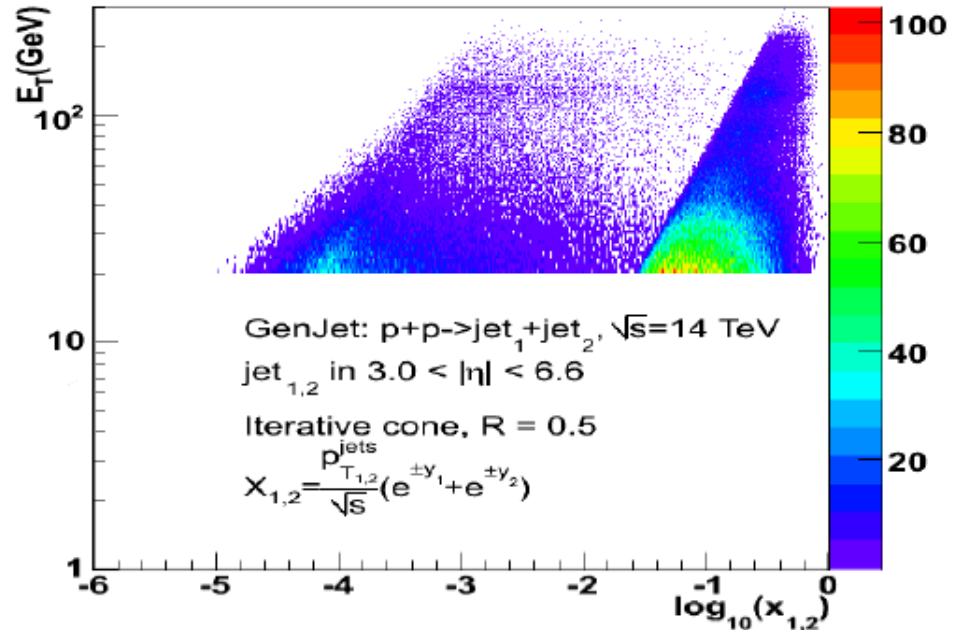
Effect	Minimum bias sample	Dijet sample
Energy scale	15%	15%
Primary vertex z position	1%	1%
Photomultiplier hits	3%	3%
Energy deposit cut in calorimeter towers	2%	2%
Channel-by-channel miscalibration	1%	1%
Total	15%	15%

# Forward Jets at CMS

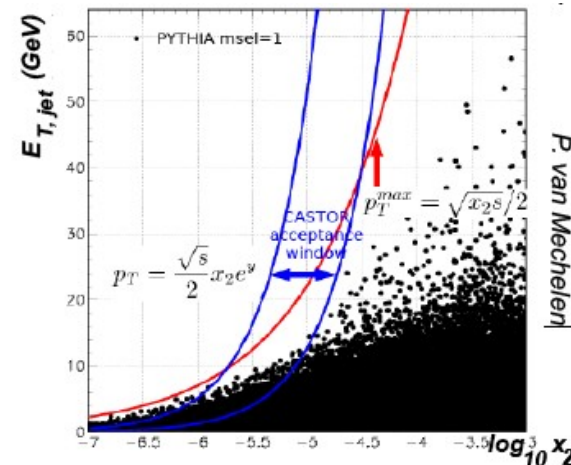
Small  $x$  gluon density  
poorly constrained:



$$d\sigma(pp \rightarrow \text{jet}) = \text{PDF}(x_1, Q^2) \otimes \text{PDF}(x_2, Q^2) \otimes d\sigma(qg \rightarrow \text{jet})$$



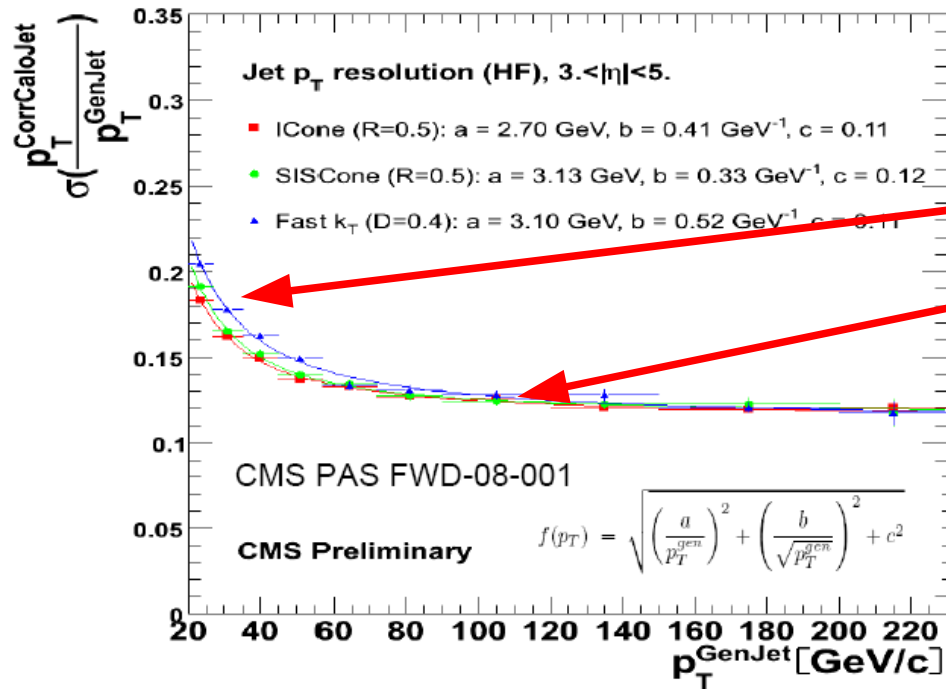
(PYTHIA default PDF: CTEQ5L)



Studies done with MC for 14 TeV

# Forward Jets at CMS

Studies done with MC for 14 TeV



$p_T$  resolution:

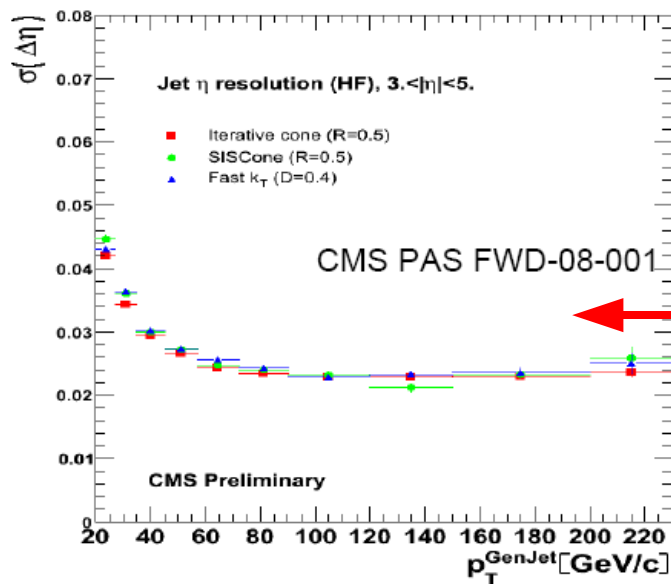
$\sim 20\%$  for  $p_T \sim 20 \text{ GeV}$

$\sim 12\%$  for  $p_T > 100 \text{ GeV}$

$\phi$  resolution:

$\sim 0.05$  for  $p_T \sim 20 \text{ GeV}$

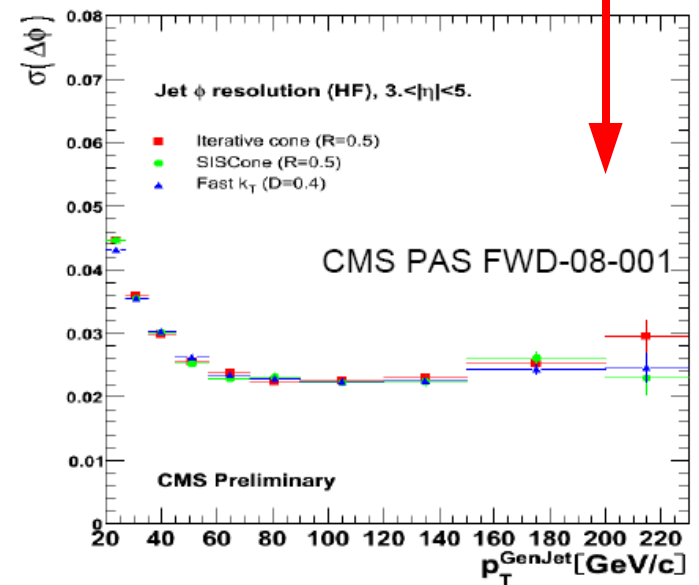
$\sim 0.02$  for  $p_T > 100 \text{ GeV}$



$\eta$  resolution:

$\sim 0.05$  for  $p_T \sim 20 \text{ GeV}$

$\sim 0.02$  for  $p_T > 100 \text{ GeV}$

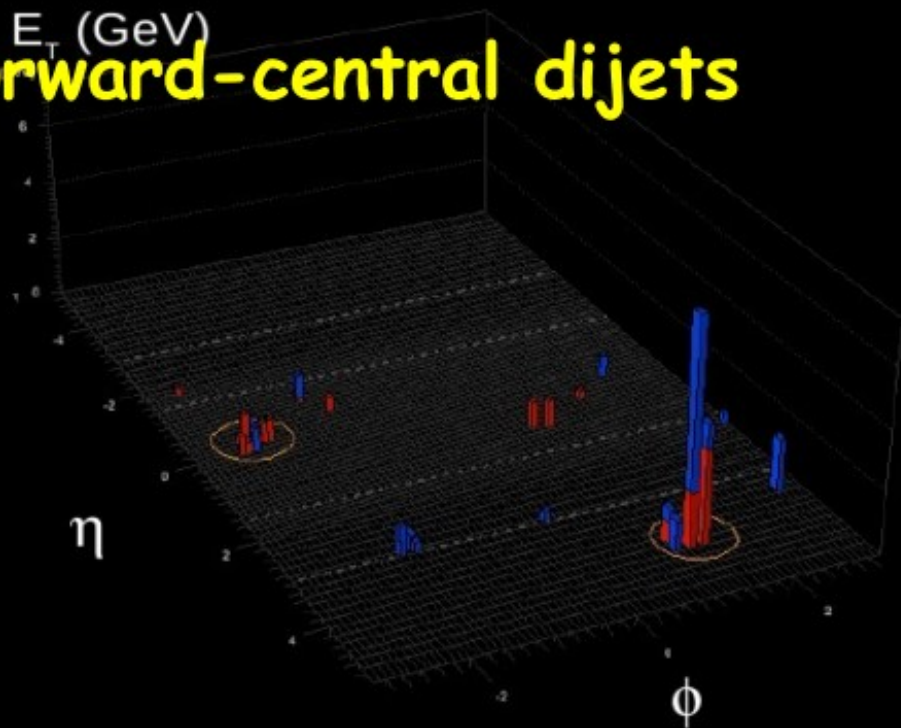
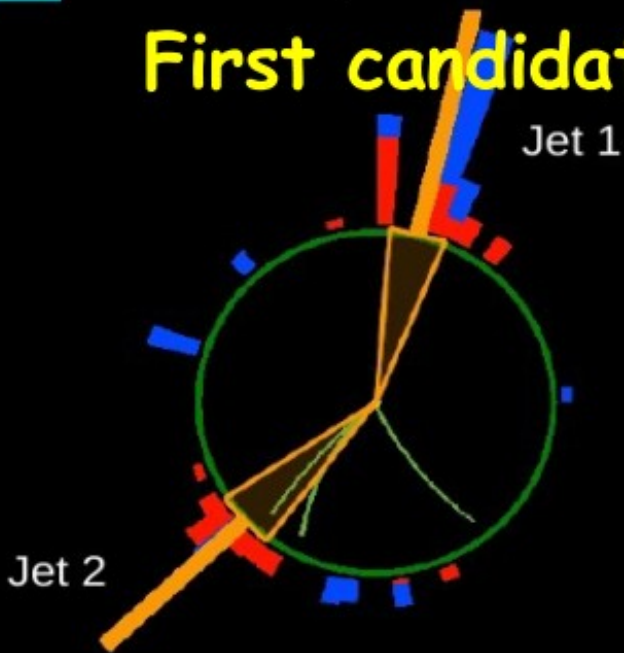




# First Forward Jets from CMS

CMS Experiment at the LHC, CERN  
Date Recorded: 2009-12-11 20:52:12 CEST  
Run/Event: 124009/18565450  
Candidate dijet event at 900GeV

## First candidate for forward-central dijets

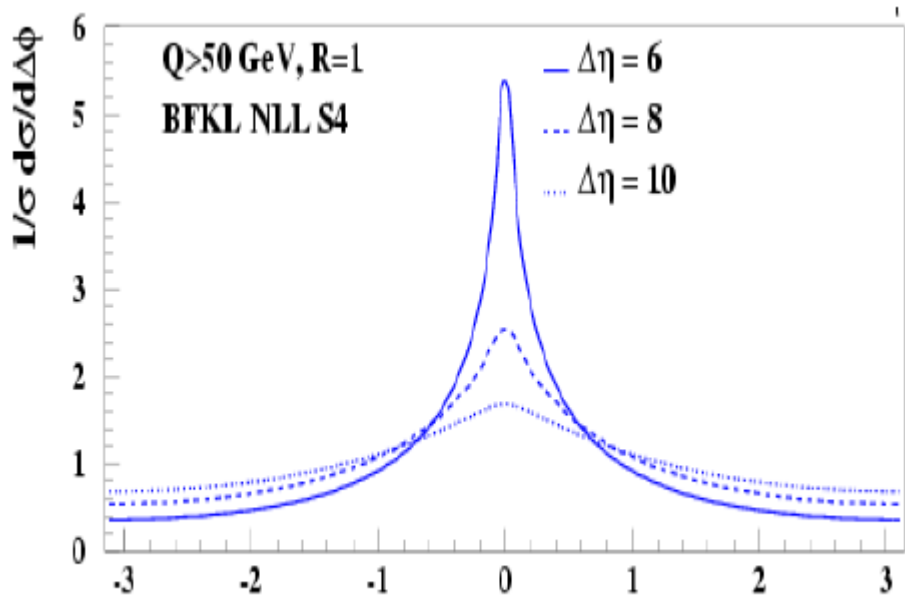
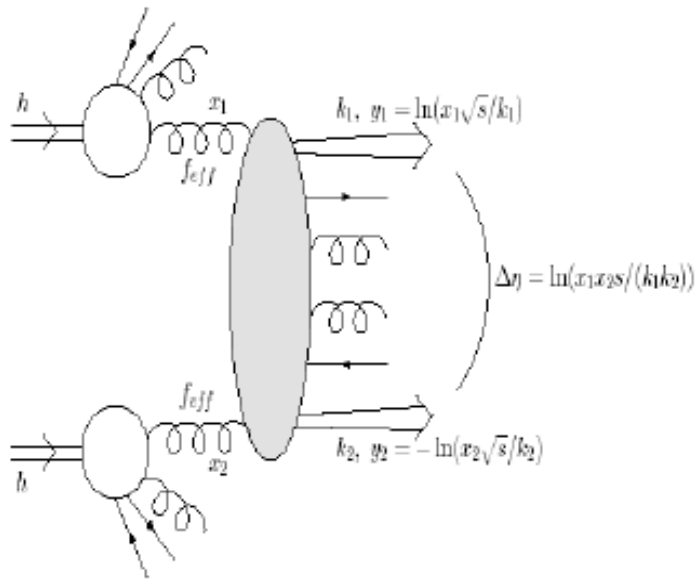


1 jet with  $p_T > 10$  GeV and  $3.0 < |\eta| < 5.0$   
 $E_T$  cut on CaloTowers displayed  $> 0.3$  GeV

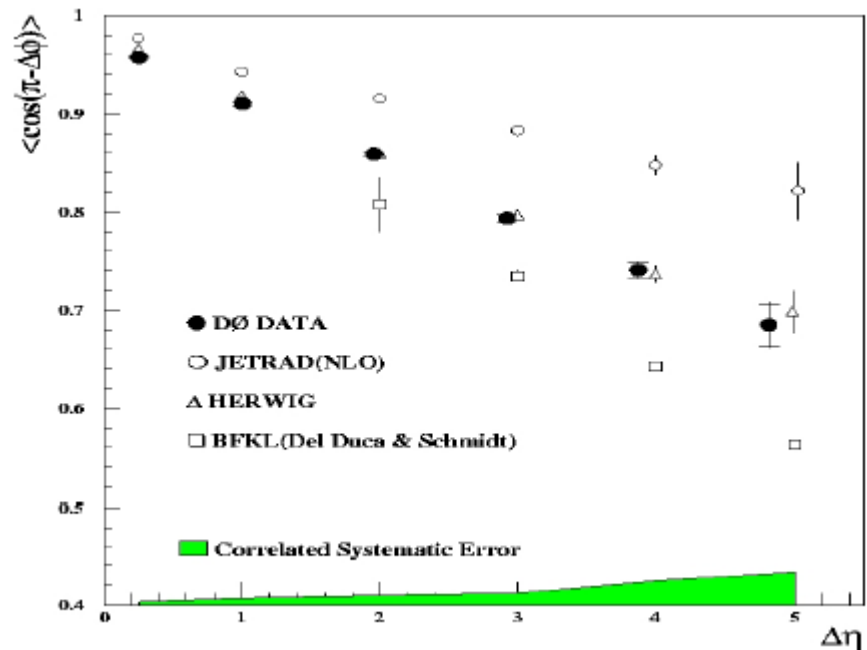
Jet 1:  $p_T = 13.4$  GeV,  $\eta = 4.10$  and  $\phi = 1.34$   
Jet 2:  $p_T = 13.8$  GeV,  $\eta = -0.15$  and  $\phi = -2.40$

# Jets correlations

- Mueller-Navelet dijets  $\rightarrow$  large  $\Delta\eta$  separation
- Testing BFKL evolution
- Extra radiation between two jets will smear back-to-back correlation
- 6-10 units in  $\Delta\eta$  for HF



[A.Sabio-Vera, F.Schwennsen]  
[C.Marquet, Royon]



S. Abachi et al. [D0 Collaboration]  
Phys. Rev. Lett. 77, 595 (1996).

A new CMS trigger will select dijet events with large  $\Delta\eta$



# Jets correlations

Other possible observables:

1. Dijet K-factor = inclusive dijet / "exclusive" dijet

Inclusive dijet V.Kim & G. Pivovarov (96-98)

Most forward/backward dijet A.Mueller & H.Navelet (87)

2.

Central jet

$$|y_j| < 2$$

$$p_{jt} > 20\text{GeV}$$

Forward jet

$$3 < y_j < 5$$

$$p_{jt} > 20\text{GeV}$$

Central jet

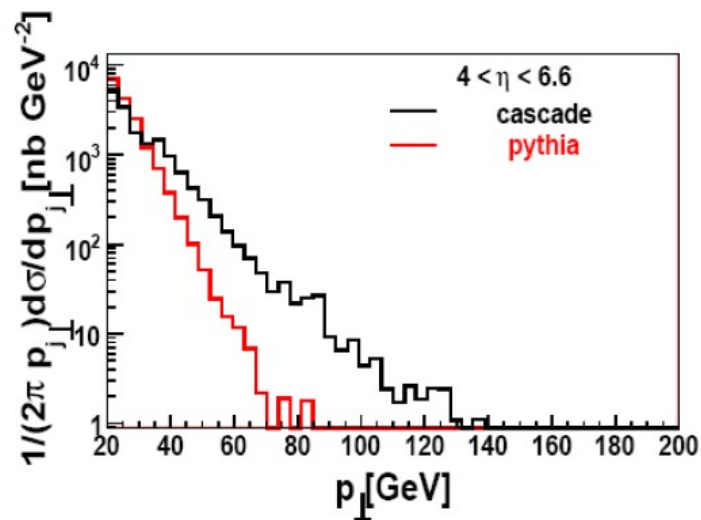
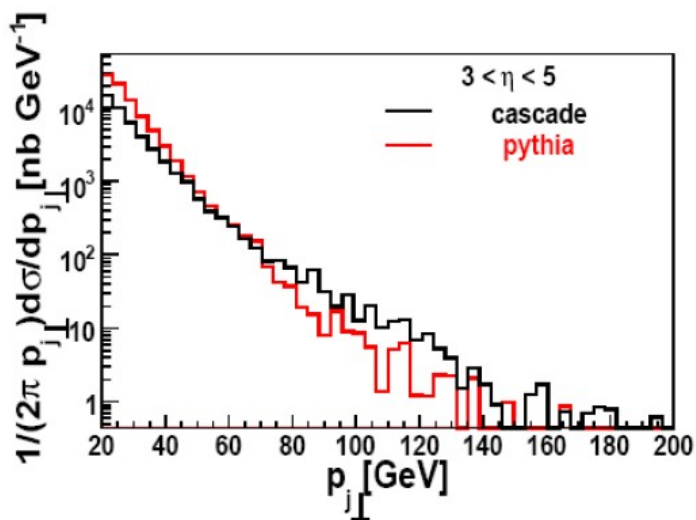
$$|y_j| < 2$$

$$p_{jt} > 20\text{GeV}$$

Forward jet

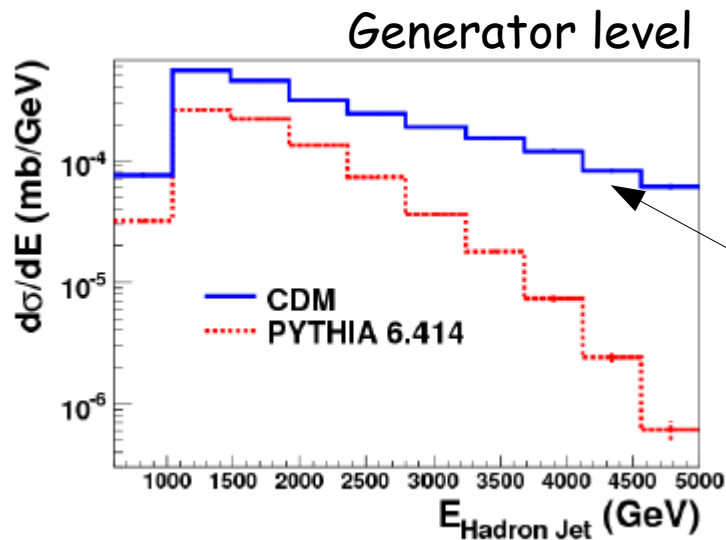
$$4 < y_j < 6.6$$

$$p_{jt} > 20\text{GeV}$$

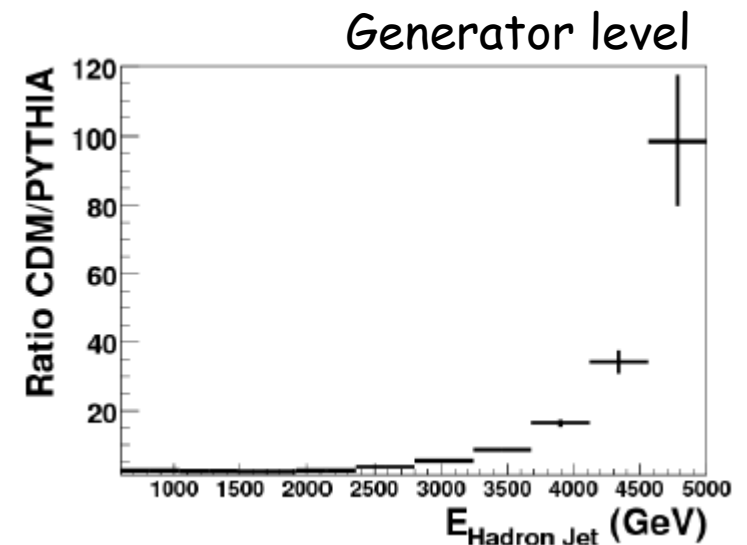


# Jets with CASTOR

Selection: 2 central jets,  $E_t > 50 \text{ GeV}$   
 1 jet in CASTOR region,  $E_t > 10 \text{ GeV}$



More hard jets predicted by Color Dipole Model

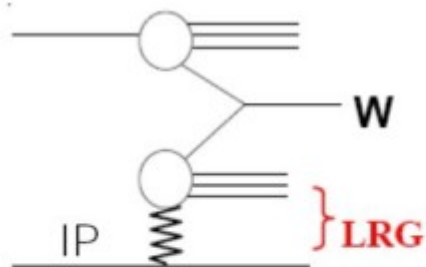


Both PYTHIA and ARIADNE are run together with Multiparton Interactions Tune A. (Tune A = to TEVATRON data.)

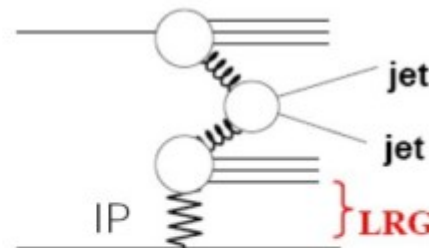
- A good tool to distinguish between DGLAP and non-DGLAP types of QCD evolution
- Also extend Mueller-Navelet studies into CASTOR acceptance

# SD production of W and dijets

- Both are hard diffractive processes characterized by the presence of a hard scale and a Large Rapidity Gap in the final state.
- Sensitive to the diffractive structure function of the proton



sensitive to the quark component of the proton



sensitive to the gluon component of the proton

- selection of diffractive candidates using the multiplicity distributions in the central tracker and HF/CASTOR: diffractive events on average have lower multiplicity in the central region and in the "gap side"

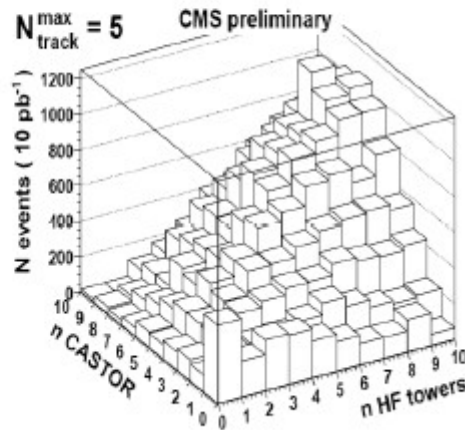
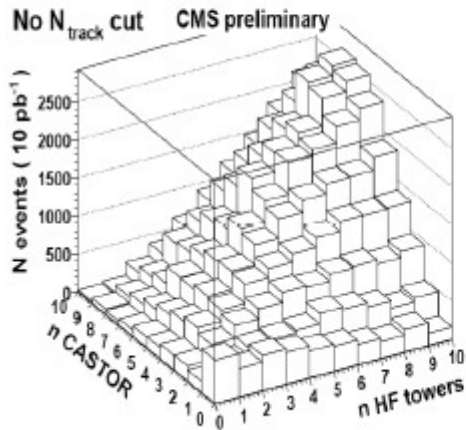
# SD production of W and dijets

- Dijets production:

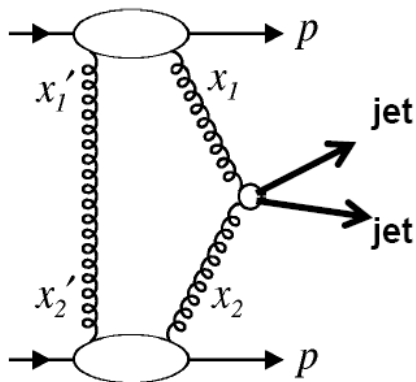
$O(300)$  evts/ $10 \text{ pb}^{-1}$  in  
 $[n(\text{Castor}), n(\text{HF})] = [0,0]$  bin

Next step: measurement of the ratio of SD to the total yields for W and dijet production giving an access to the estimation of:

- the rapidity gap survival probability
- the quark/gluon component in the diffractive PDFs of the proton

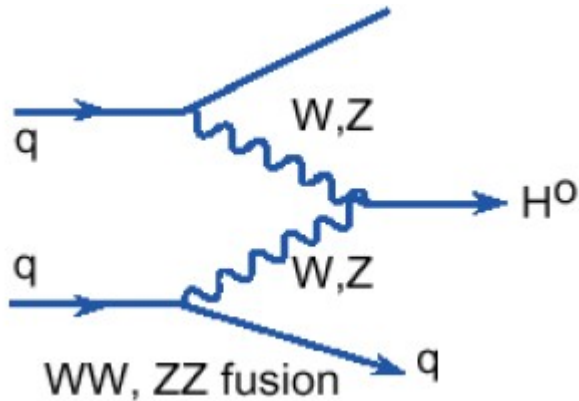


**Diffractive events peak at zero**



- Two jets produced exclusively
- $R_{jj} = M_{jj} / M_x$  variable (for CEP close to  $\sim 1$ )
- Observation at Tevatron (Phys. Rev. D77, 05, 2004)
- $\sigma \sim O(10)$  pb at LHC energies (large sample)
- Central two - three jets production can be used to constrain Sudakov factor

# Long term plans



Leptonic H decay:

$$qqH \rightarrow jj WW \rightarrow jj l\nu l\nu$$

Low activity in central region, forward jets

## Graviton production in trans-Planckian regime

*G. Giudice, R. Rattazzi & J. Wells (99,02)*

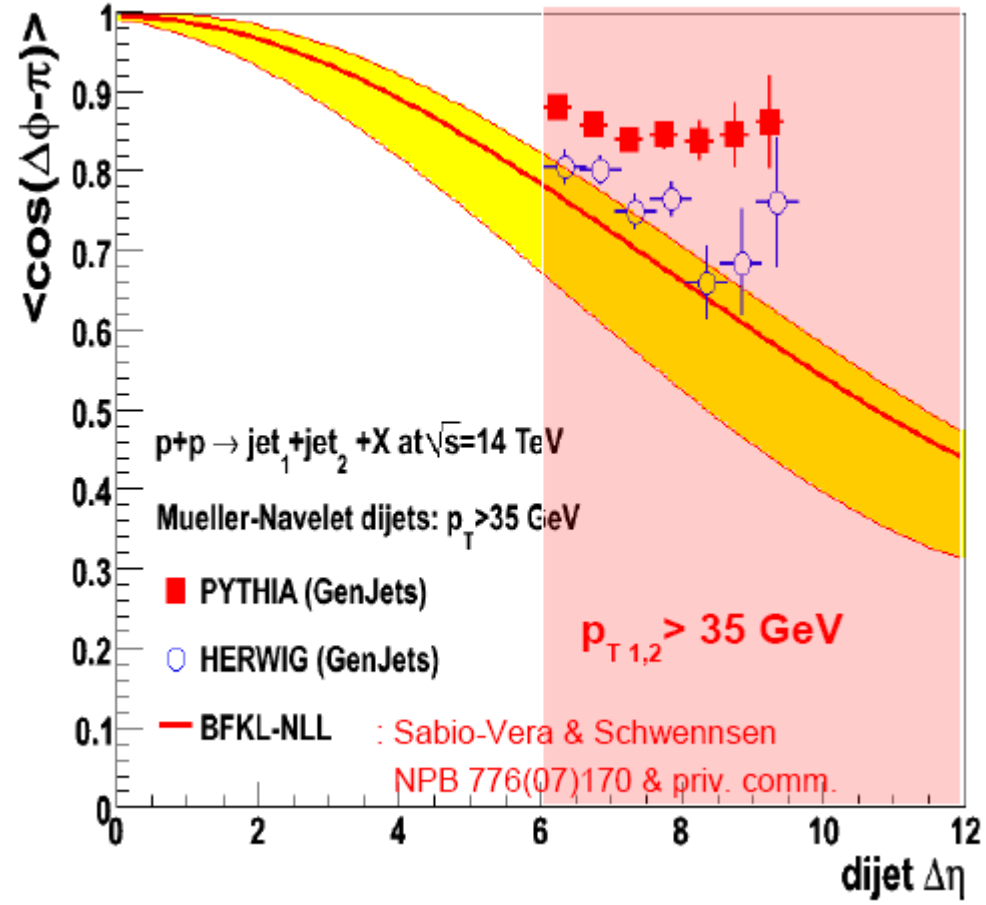
t-channel graviton contribution



large mass dijet with large rapidity interval  
few hundred pb<sup>-1</sup>



# Jets correlations



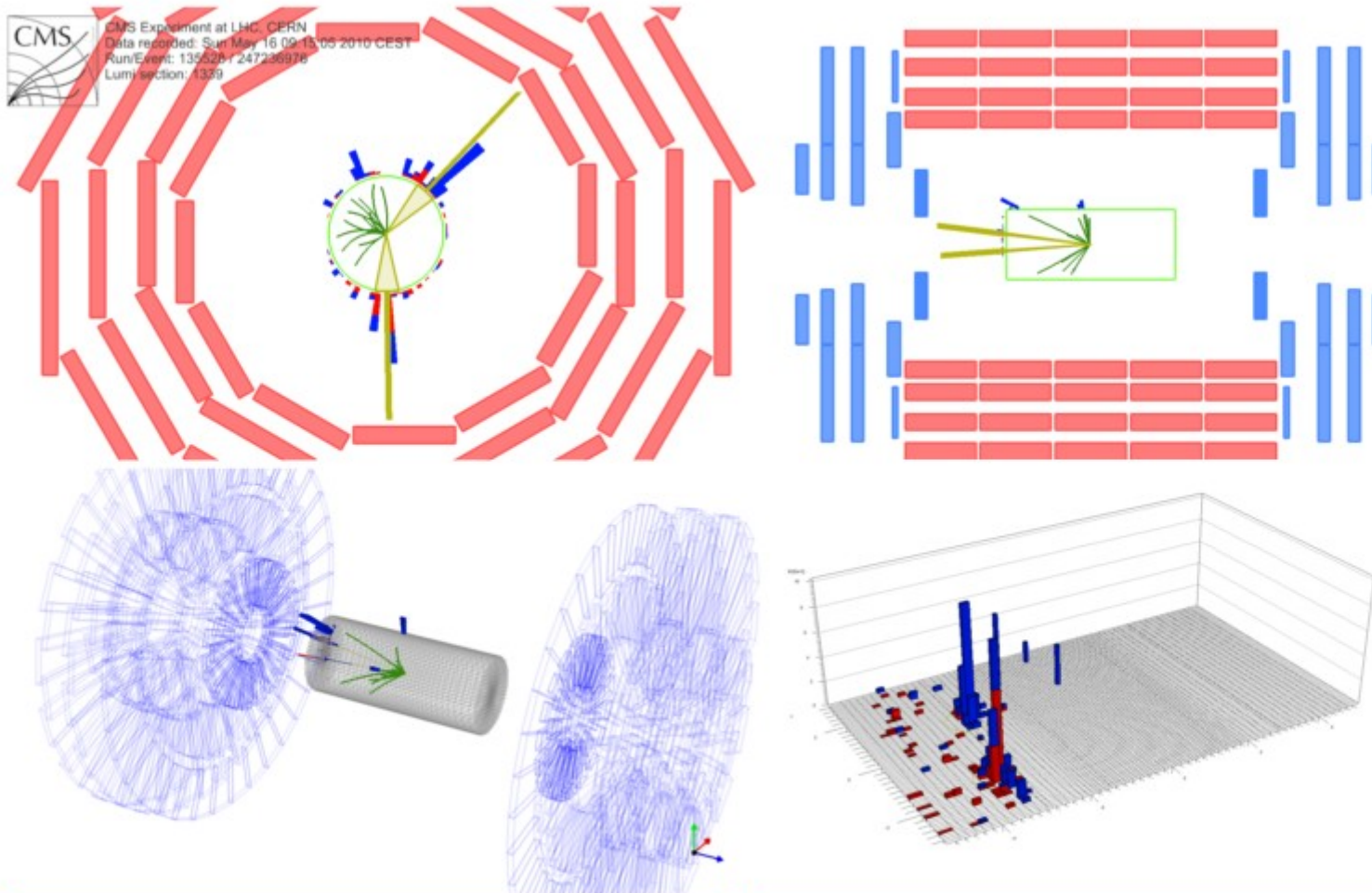
Average  $\cos(\Delta\phi - \pi)$  as a function of  $\Delta\eta$

HERWIG shows ~15% more decorrelation than PYTHIA and ~20% less than BFKL analytical estimates

Parton showering & hadronization has to be taken into account

# Yet another candidate...

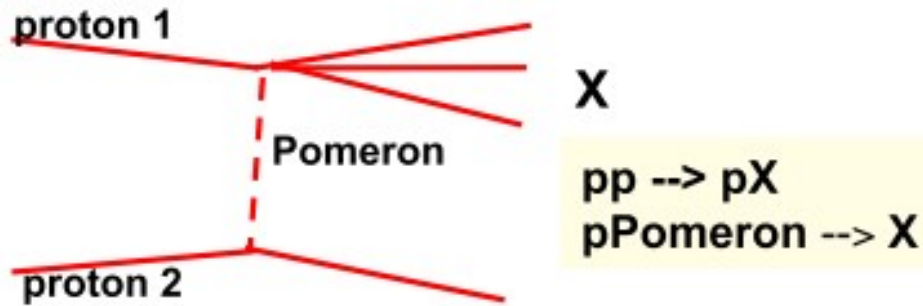
## Diffractive dijet candidate at 7 TeV



$E(\eta < 3.0) > 1.5 \text{ GeV}$      $p_T(\text{track}) > 0.5 \text{ GeV}$   
 $E(\eta \geq 3.0) > 2.0 \text{ GeV}$

$p_T(\text{jet1}) = 41.2 \text{ GeV}$ ,     $p_T(\text{jet2}) = 31.9 \text{ GeV}$   
 $\eta(\text{jet1}) = -2.8$ ,          $\eta(\text{jet2}) = -3.3$

# Variable $E+p_z$



- $\Sigma(E \pm p_z)$  runs over all calo towers
- Measure for the momentum of the Pomeron = momentum loss of the proton

Momentum and energy conservation:

$$E(\text{Pomeron}) + E(\text{proton 1}) = E(X)$$

$$p_z(\text{Pomeron}) + p_z(\text{proton 1}) = p_z(X)$$

Recall: in SD events proton loses almost none of its initial momentum.

If proton 1 moves in positive z direction:  $E(\text{proton 1}) - p_z(\text{proton 1}) \approx 0$  (and proton 2, and Pomeron, move in the negative z direction)

Hence:

$$E(\text{Pomeron}) - p_z(\text{Pomeron}) \approx 2E(\text{Pomeron}) \approx E(X) + p_z(X)$$

$$\text{i.e. } \xi = 2E(\text{Pomeron})/\sqrt{s} \approx (E(X) + p_z(X))/\sqrt{s}$$