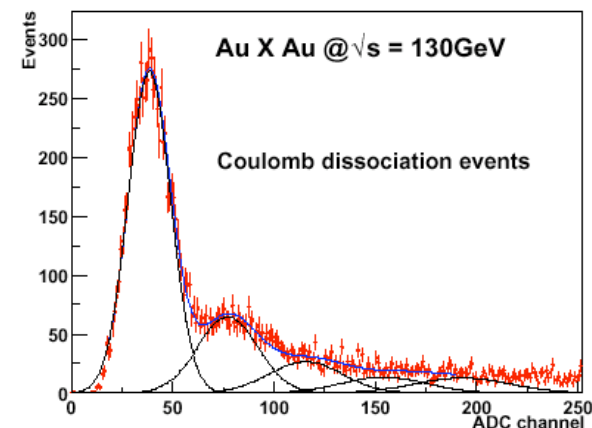


# Luminosity Measurement at pp&Heavy ion colliders



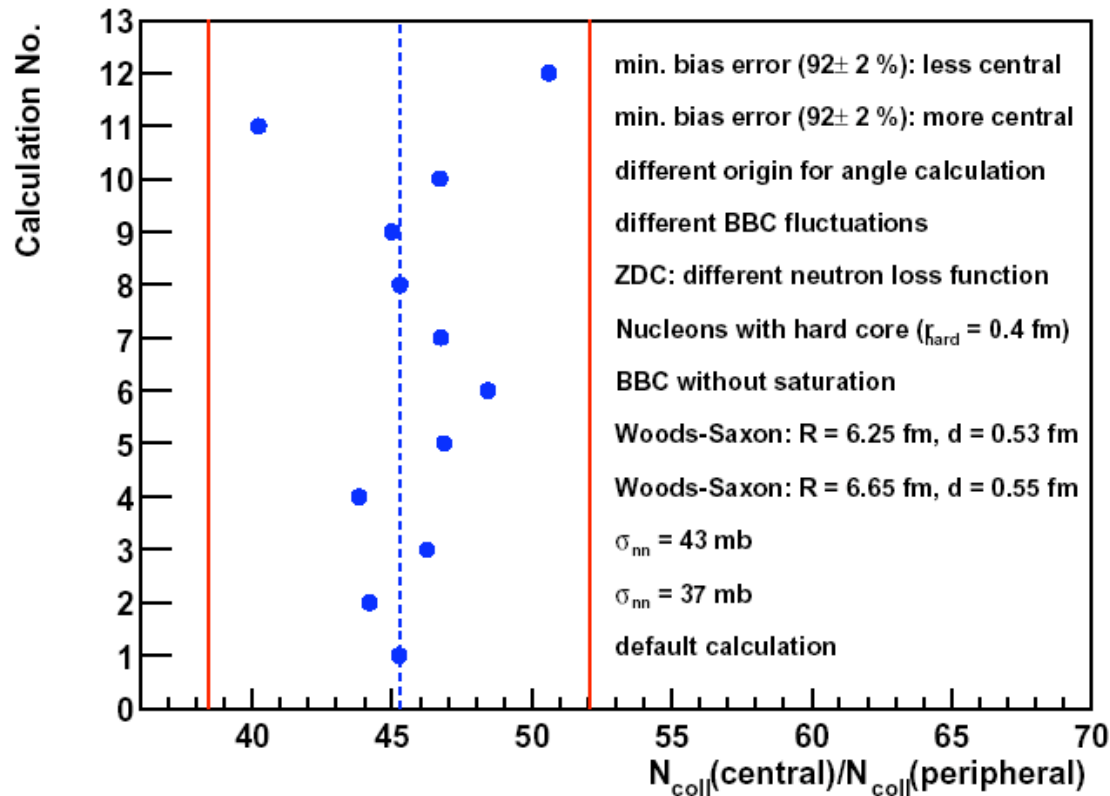
- I. Determination in pp using elastic scattering
- II. Determination for Heavy Ions
- III. The role of accelerator tools

# pp versus AA methodology

p-p(bar)	Heavy Ion
Elastic scattering Special optics/det	Minimum Bias (standard dets )
Available ~4-5 yrs after startup	Available ~day-1
$\square_L \sim 3\%$	$\square_L \sim 5\%$ 2% possible

## AA cross-normalization with pp

- 1) From pp comparison data
  - Error from AA & pp Luminosity uncertainties and  $n_{\text{collision}}$
- 2) From central/peripheral
  - Error from determination of centrality classes

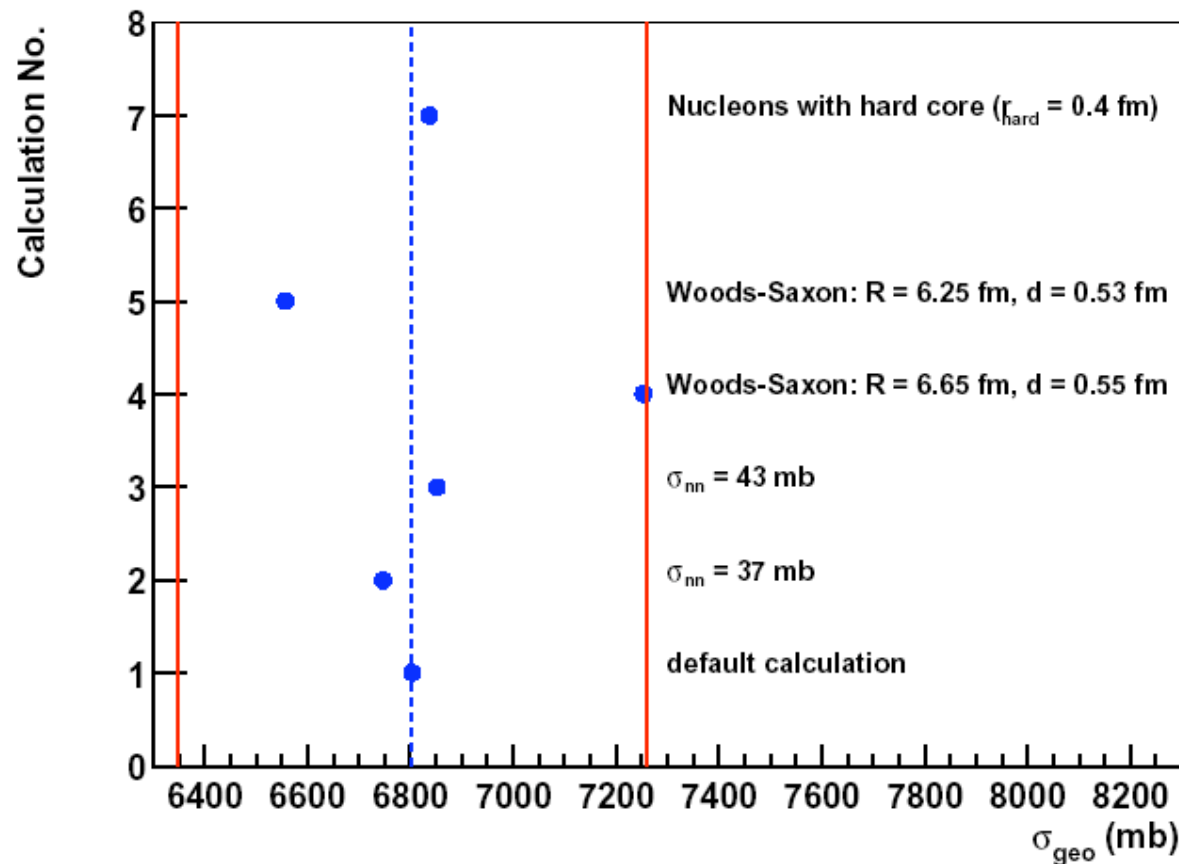


<- Klaus Reygers,  
*PHENIX internal note 7/01*

# Total Inelastic Cross sections

Ion Geometric cross sections decouple from  $\sigma_{nn}$

Au+Au geometrical cross section



<- ditto

## pp Methodology to calculate Luminosity

Since ISR, collider expts. have used:

1. Accelerator based calculation (more later)
  - uses  $I_{\text{beam}}$ ,  $\sigma$ ,  $\sigma^*$
1. “Dead reckoning” from published data
  - ie D0- uses E710&CDF average
2. “Luminosity independent method”
  - uses  $\sigma_{\text{tot}}$ ,  $\sigma_{\text{el}}$ ,  $\sigma$
3. “Pure Coulomb” region elastic scattering
  - uses  $\sigma_{\text{em}}$  and  $G(t)$

## *Luminosity at Hadron Colliders*

- In 70's, near end of ISR career, Cern-Roma and Pisa-SB joined forces and invented the “Luminosity independent method”. Subsequent studies of comparison w. van der Meer method and limits on precision( $\sim 1-2\%$ )
  - Van der Meer in machines with zero x-ing angle more complicated.
  - At SPPS, UA4 used “Lum Indep Method”, revised in UA4'
  - At TevI, 4 measurements disagree. Lum discrepancy not resolved.  
*In 1994 D0 increased it's “luminosity constant” by 12.4% to reflect world average and assigned an error of 12% to Luminosity*
  - RHIC Luminosity uncertainties in AuAu and pp data 5%, 30%
- QM 2002*

## pp Methodology for Luminosity

1. In “pure coulomb” region  $t \sim 10^{-4} (\text{GeV}/c)^2$  and scattering angle (ie  $\theta = 1\text{-}2$  mrad at LHC) is  $\sim \theta_{\text{beam}}$ 
  - a 2<sup>nd</sup> generation elastic scatt experiment
2. “Luminosity Independent Method” uses nuclear slope (ie  $t \sim 10^{-2} (\text{GeV}/c)^2$ ) and optical theorem:

$$(1 + \varrho^2) \cdot \sigma_{tot}^2 = \mathcal{L}^{-1} 16\pi (hc)^2 \frac{dR_{elast}}{dt} \Big|_{t=0}$$

From which:

$$(1 + \varrho^2) \cdot \sigma_{tot} = \frac{16\pi (hc)^2}{R_{elastic} + R_{inelastic}} \cdot \frac{dR_{elast}}{dt} \Big|_{t=0}$$

## pp Luminosity independent method

A large acceptance Luminosity monitor counter is embedded in the measurement which is calibrated in the process.

$$\sigma_{DA} = \frac{\sigma_{DA}}{\sigma_{tot}} \cdot \sigma_{tot} = \frac{R_{DA}}{(R_{elast} + R_{DA} + R_{SA} + R_{extrap})^2} \cdot \frac{16\pi(hc)^2}{(1 + \varrho^2)} \cdot \frac{dR_{el}}{dt} \Big|_{t=0}$$

UA4:

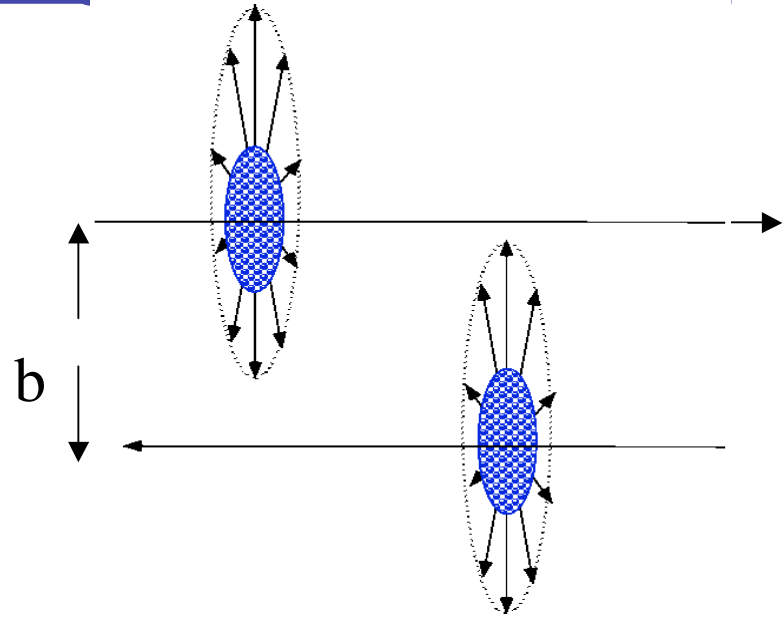
Trigger Contribution	$\eta$ -range	Fraction of $N_{inel}$ %
Double-arm(= $f_{DA}$ )	3.0 - 5.6	$82.7 \pm 0.8$
Single Arm	2.5 - 5.6	$16.3 \pm 0.6$
Central Detector	$\leq 1.7$	$0.08 \pm 0.04$
Small-angle extrapolation	$\geq 5.6$	$0.9 \pm 0.2$
Large angle correction	1.7 - 2.5	$0.04 \pm .02$



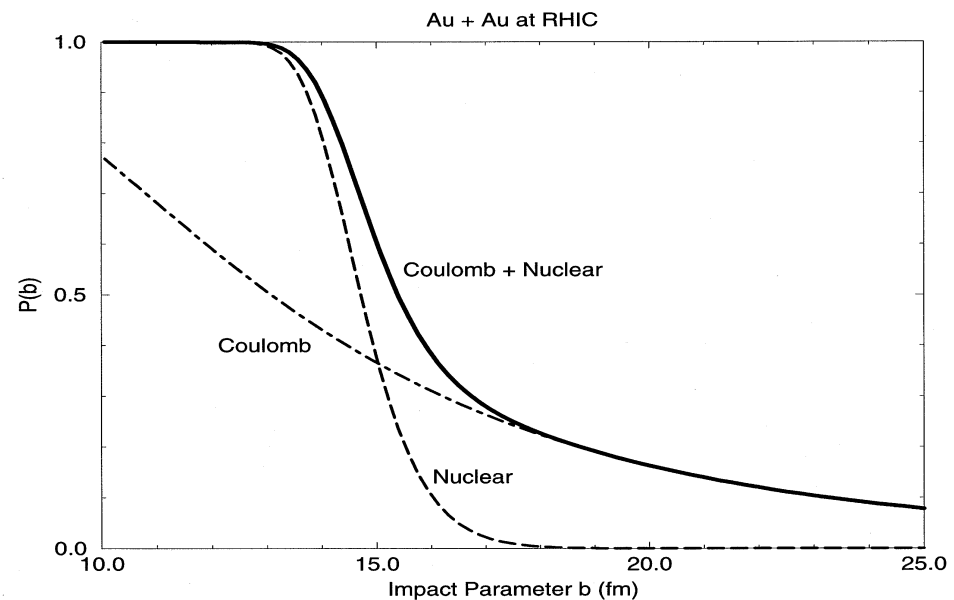
# Heavy Ion methodology for Luminosity

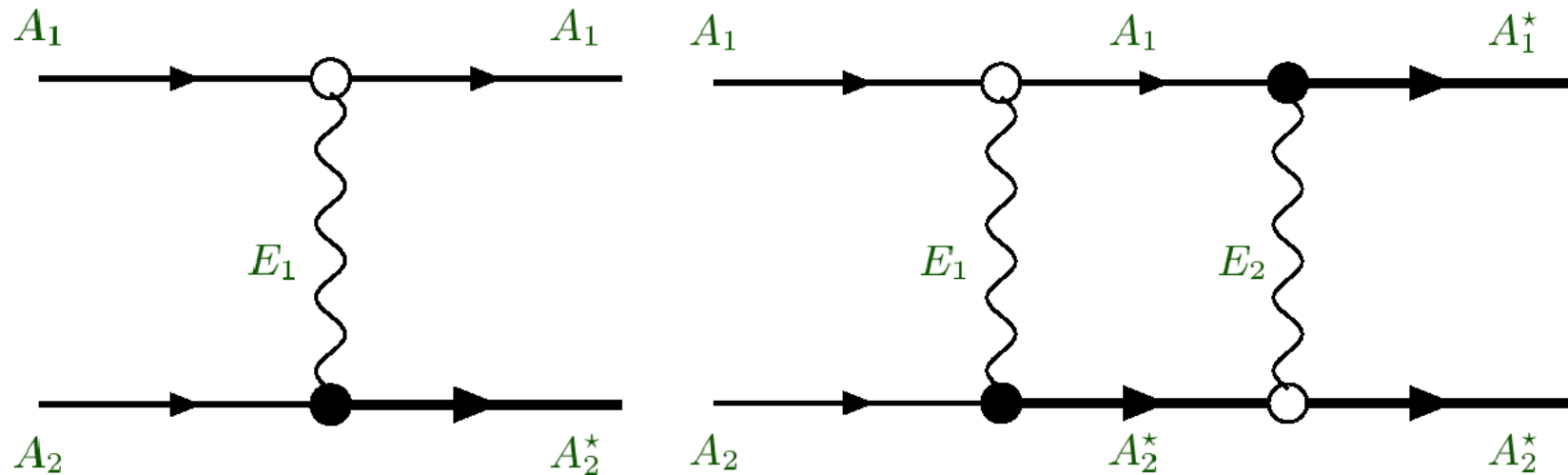
$\text{AuAu} \rightarrow \text{Au} + \text{Au}^*$  92 barns  
 $\quad \quad \quad \searrow$   
 $\quad \quad \quad \text{X} + \text{neutrons}$

$\text{AuAu} \rightarrow \text{Au}^* + \text{Au}^*$  3.6 barns  
 $\quad \quad \quad \searrow$   
 $\quad \quad \quad \text{X} + \text{neutrons}$   
 $\quad \quad \quad \swarrow$   
 $\quad \quad \quad \text{Y} + \text{neutrons}$



Correlated Forward-Backward Dissociation



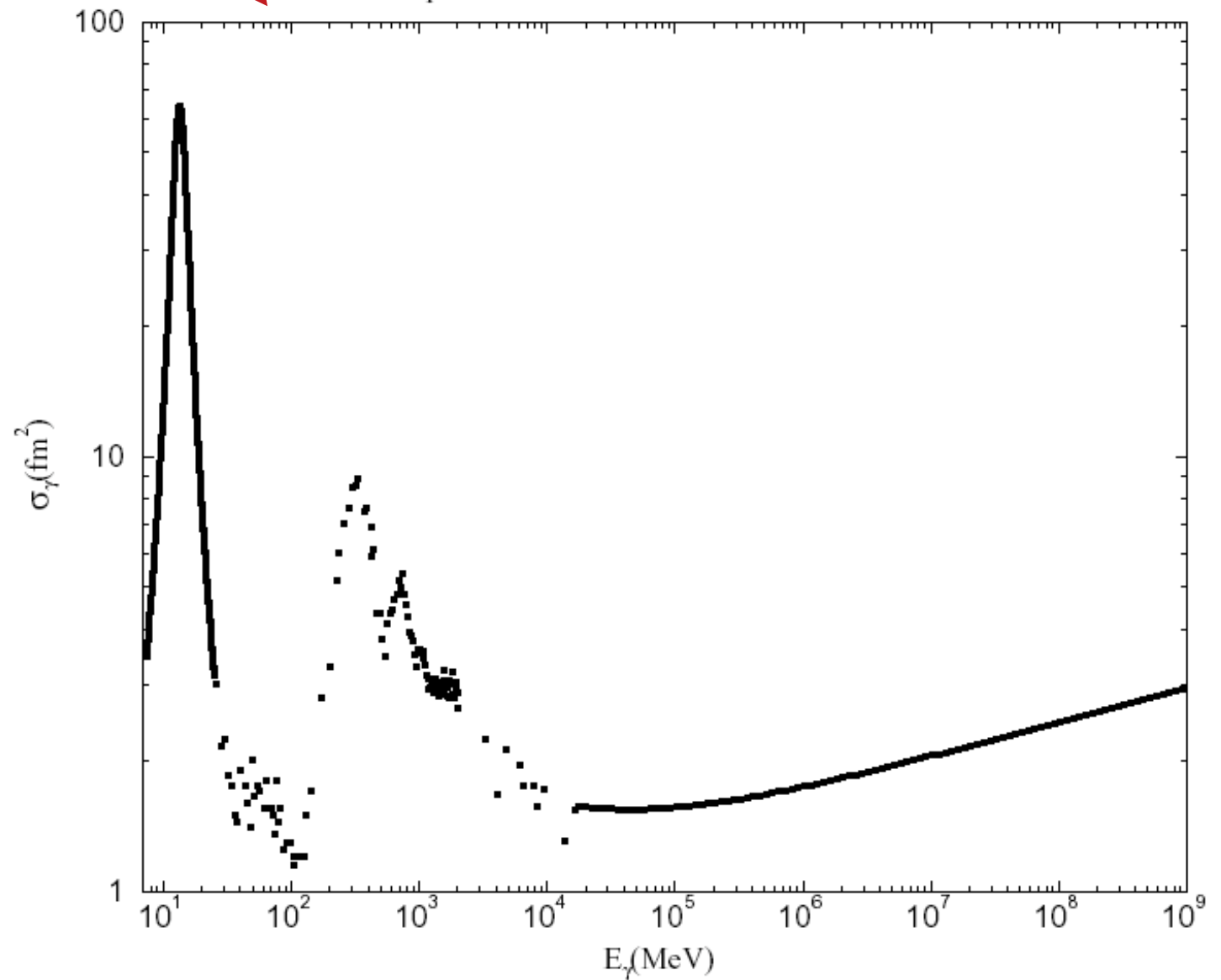


## Weizsäcker-Williams (WW) method

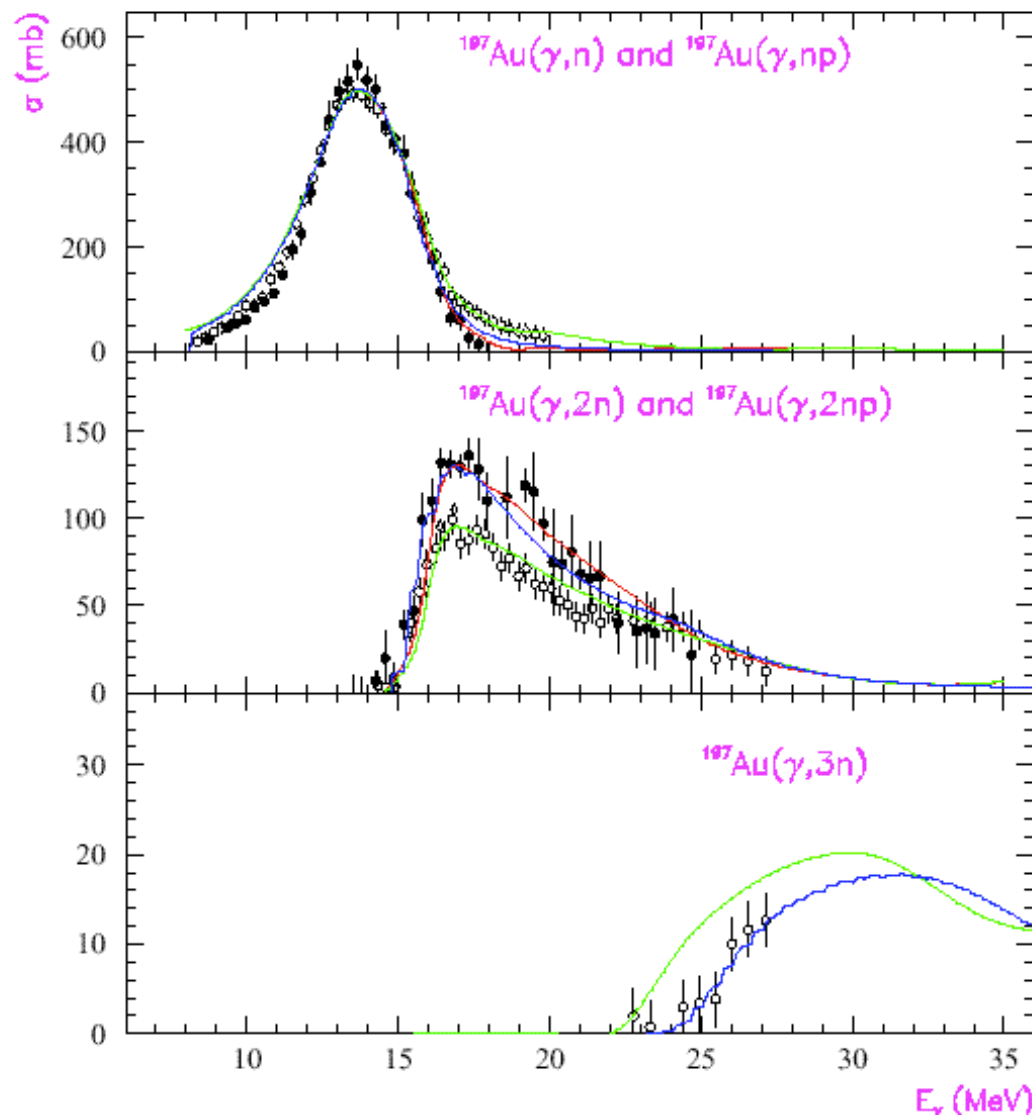
- [1] A.Baltz, M.J.Rhoades-Brown, J.Weneser, Phys. Rev. E 54 (1996) 4233.
- [2] A.J. Baltz, S.N.White, RHIC/DET Note 20, BNL-67127 (1996)
- [3] S.N.White, Nucl. Instrum. Meth. A409, 618 (1998).
- [4] A.J.Baltz, C.Chasman and S.N.White, Nucl. Instrum. Meth. A417, 1 (1998) nucl-ex/9801002.
- [5] I.A. Pshenichnov , J.P. Bondorf , I.N. Mishustin , A. Ventura , and S. Masetti, nucl-th/0101035

$$\sigma_{\text{MCD}} = \frac{2\pi^2 Z^4}{\pi^3 \pi^4} \int_{b_0} b db \left[ \int d\pi \pi_{ph}(\pi) K_1^2\left(\frac{b\pi}{\pi}\right) \right]^2$$

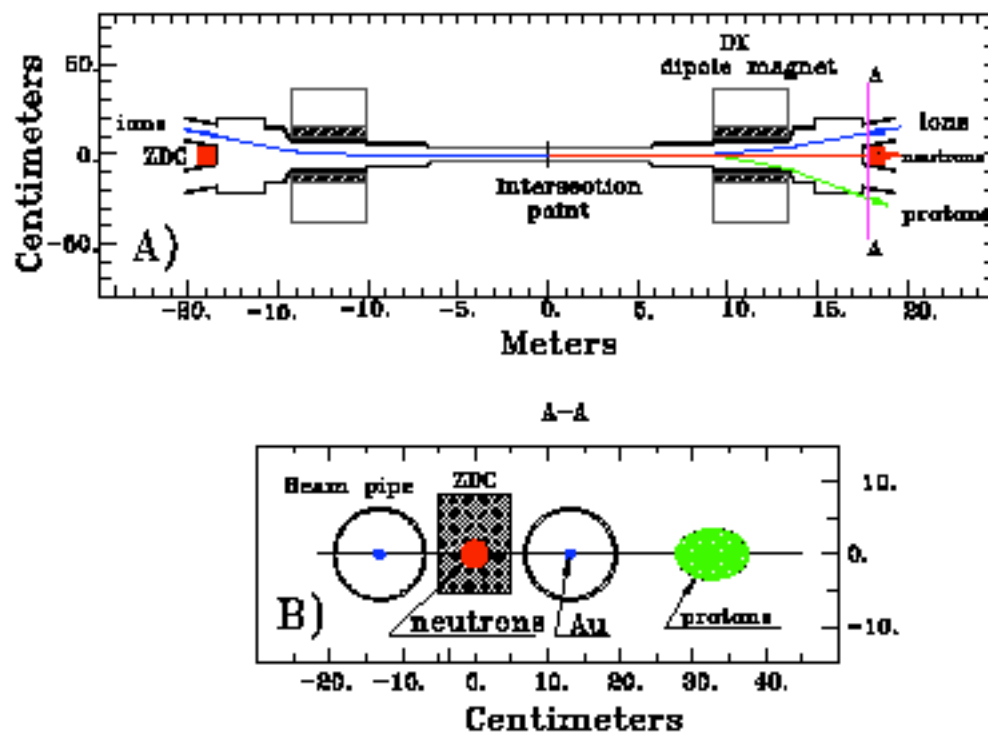
Input to Weizsacker-Williams Formula



Low Energy Photonuclear  
Cross sections and  
n-multiplicities, momenta  
(Saclay & Livermore data)

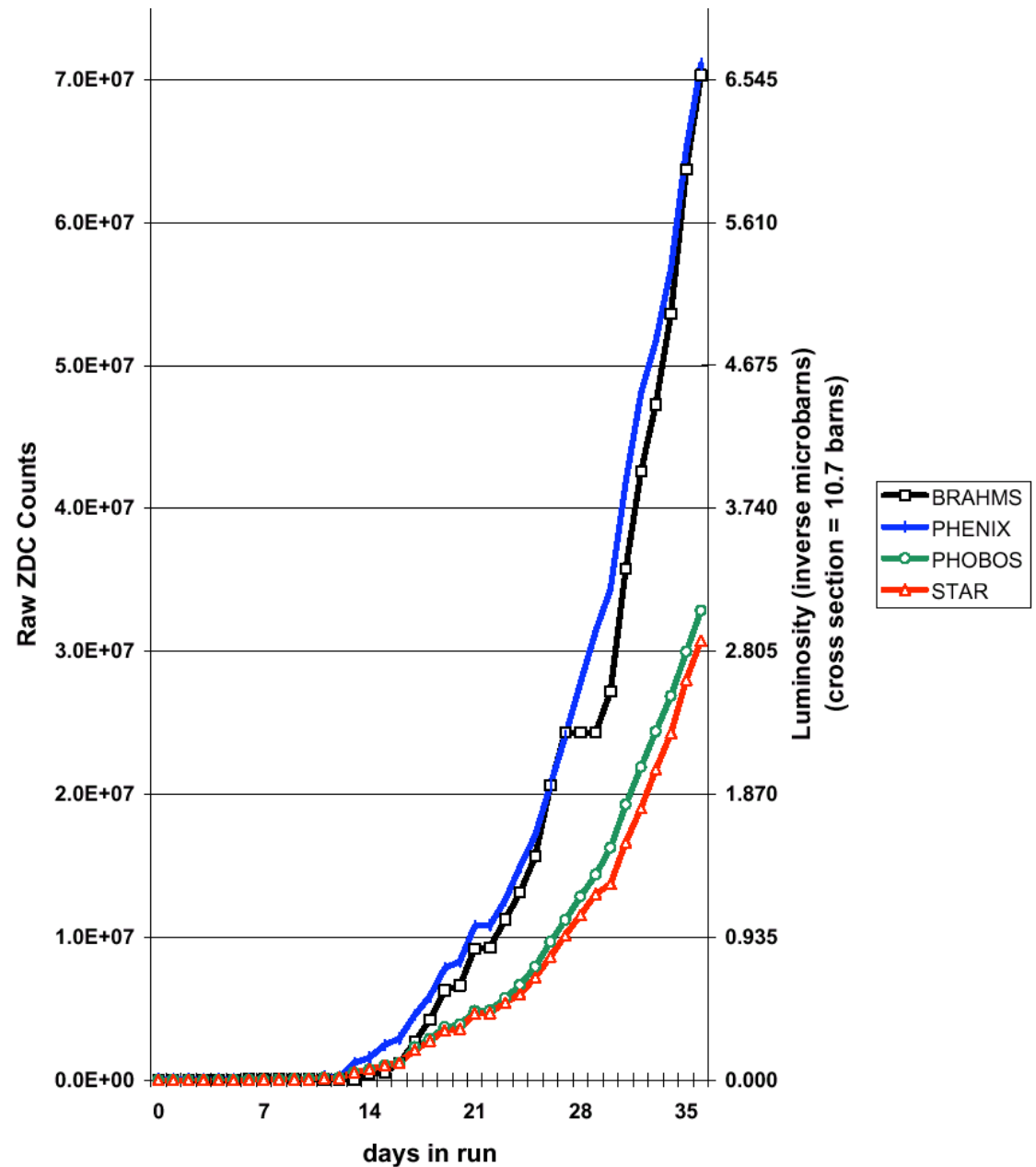


# Interaction Region Geometry



## Zero Degree Calorimeter Acceptance

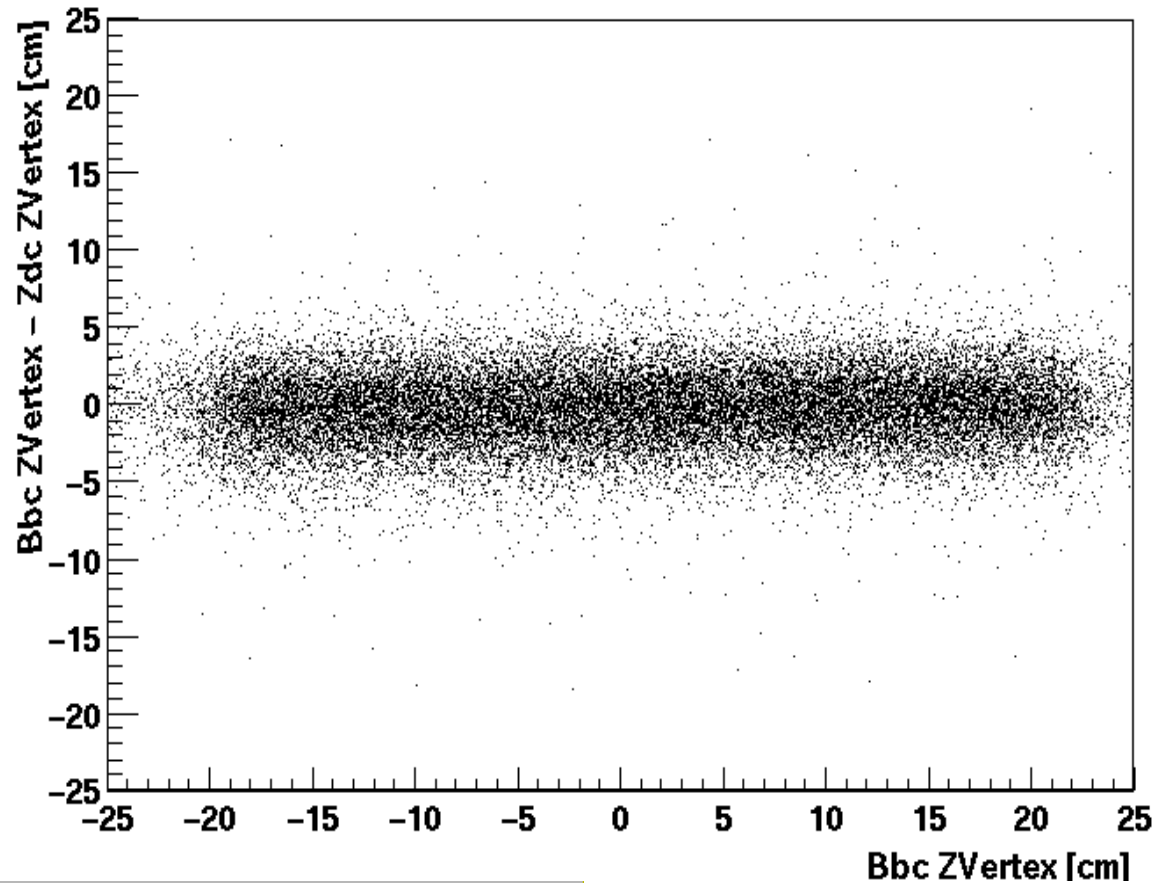
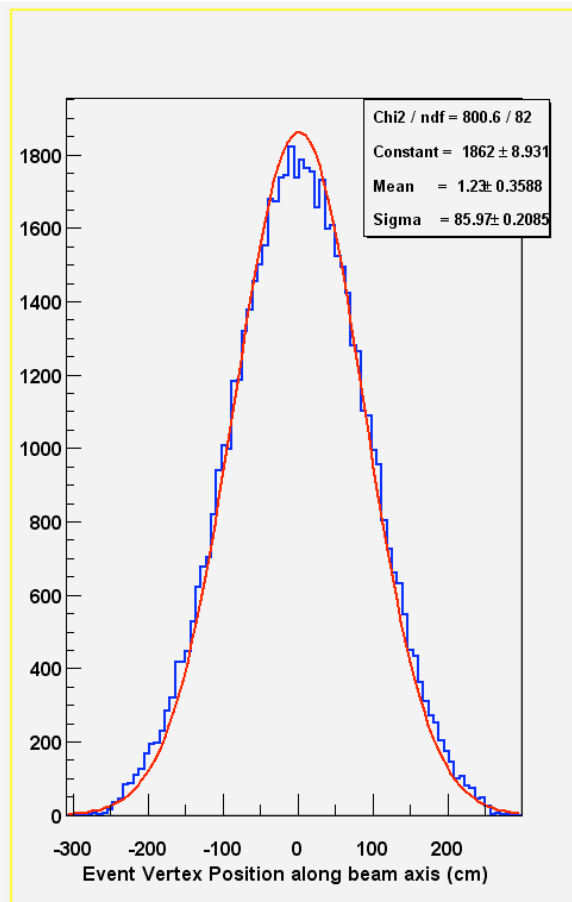
# Luminosity and Beam Quality



# ZDC measurement of Luminosity profile: $z_{\text{int}}$

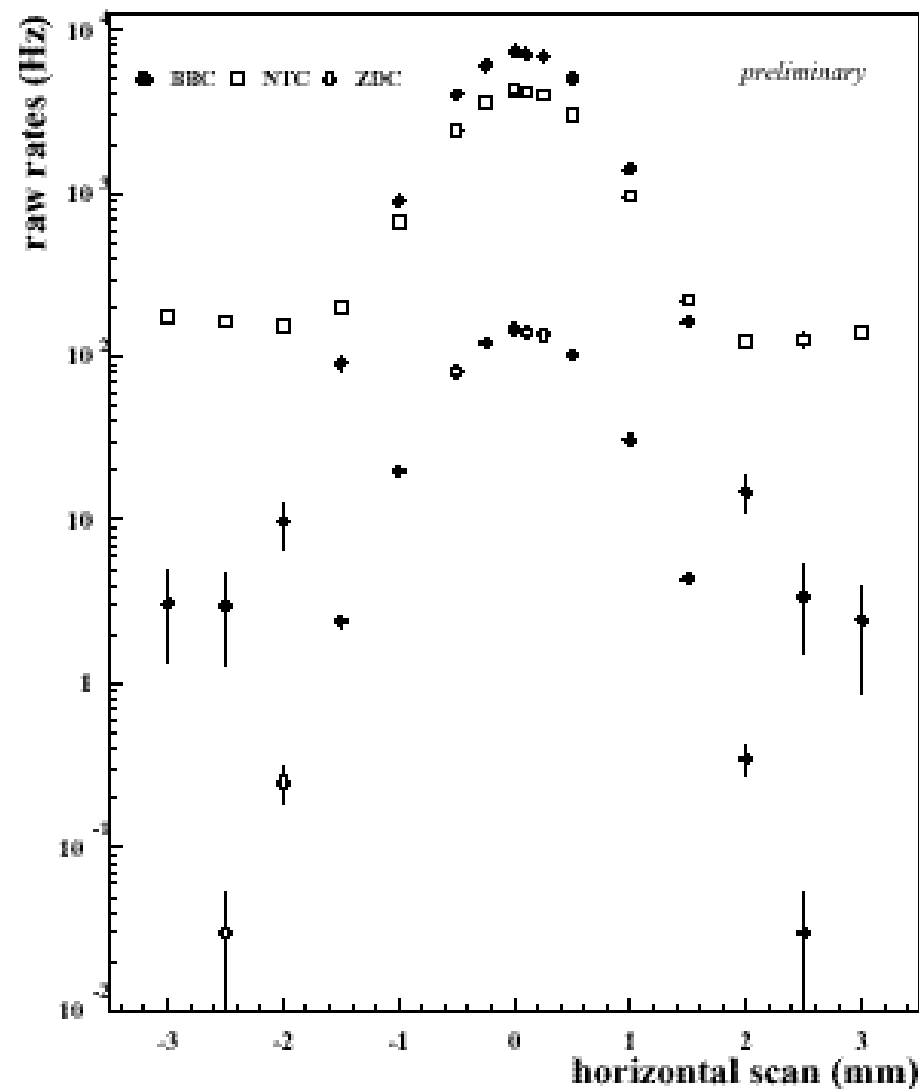
Interaction point(z)

ZDC resolution  $\sim 2$  cm ( $\Delta t \sim 120$  ps)



# Van der Meer scans

## Using different interaction triggers





# RHIC UPC Physics results from Run I.

published

VOLUME , NUMBER

PHYSICAL REVIEW LETTERS

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## Measurement of Mutual Coulomb Dissociation in $\sqrt{s_{NN}} = 130$ GeV Au + Au Collisions

Mickey Chiu,<sup>1</sup> Alexei Denisov,<sup>2</sup> Edmundo Garcia,<sup>3</sup> Judith Katzy,<sup>4</sup> Andrei Makeev,<sup>5</sup>  
Michael Murray,<sup>5</sup> and Sebastian White<sup>6</sup>

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<sup>2</sup>*IHEP, Protvino, Russia*

<sup>3</sup>*University of Maryland, College Park, Maryland 20742*

<sup>4</sup>*MIT, Cambridge, Massachusetts 02139*

<sup>5</sup>*Texas A&M University, College Station, Texas 77843-3366*

<sup>6</sup>*Brookhaven National Laboratory, Upton, New York 11973*

(Received 28 September 2001; revised manuscript received 19 November 2001; published )

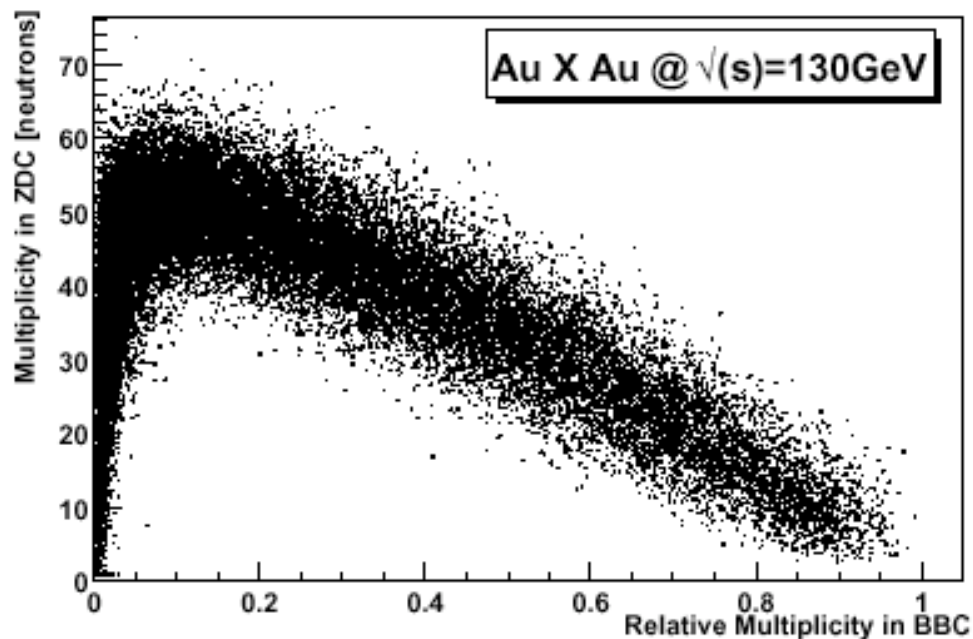
submitted

## Coherent $\rho^0$ Production in Ultra-Peripheral Heavy Ion Collisions

C. Adler<sup>11</sup>, Z. Ahammed<sup>23</sup>, C. Allgower<sup>12</sup>, J. Amonett<sup>14</sup>, B.D. Anderson<sup>14</sup>, M. Anderson<sup>5</sup>, G.S. Averichev<sup>9</sup>,  
J. Balewski<sup>12</sup>, O. Barannikova<sup>9,23</sup>, L.S. Barnby<sup>14</sup>, J. Baudot<sup>13</sup>, S. Bekele<sup>20</sup>, V.V. Belaga<sup>9</sup>, R. Bellwied<sup>31</sup>, J. Berger<sup>11</sup>,  
H. Bichsel<sup>30</sup>, L.C. Bland<sup>2</sup>, C.O. Blyth<sup>3</sup>, B.E. Bonner<sup>24</sup>, A. Boucham<sup>26</sup>, A. Brandin<sup>18</sup>, A. Bravar<sup>2</sup>, R.V. Cadman<sup>1</sup>,  
H. Caines<sup>20</sup>, M. Calderón de la Barca Sánchez<sup>2</sup>, A. Cardenas<sup>23</sup>, J. Carroll<sup>15</sup>, J. Castillo<sup>26</sup>, M. Castro<sup>31</sup>,  
D. Cebra<sup>5</sup>, P. Chaloupka<sup>20</sup>, S. Chattopadhyay<sup>31</sup>, Y. Chen<sup>6</sup>, S.P. Chernenko<sup>9</sup>, M. Cherney<sup>8</sup>, A. Chikanian<sup>33</sup>,  
B. Choi<sup>28</sup>, W. Christie<sup>2</sup>, J.P. Coffin<sup>13</sup>, T.M. Cormier<sup>31</sup>, J.G. Cramer<sup>30</sup>, H.J. Crawford<sup>4</sup>, W.S. Deng<sup>2</sup>,  
A.A. Derevschikov<sup>22</sup>, L. Didenko<sup>2</sup>, T. Dietel<sup>11</sup>, J.E. Draper<sup>5</sup>, V.B. Dunin<sup>9</sup>, J.C. Dunlop<sup>33</sup>, V. Eckardt<sup>16</sup>,

LEMIC Workshop on  
Luminosity 9/12/02

Sebastian White, BNL



### Efficiencies(hadronic):

$$\epsilon_{bbc} = (92 \pm 2)\% \text{ (HIJING)*}$$

$$\epsilon_{bbc} = (93 \pm 2)\% \text{ (JAM)}$$

$$\epsilon_{zdc} = (98 \pm 2)\% \text{ (conservative),}$$

$$\epsilon_{zdc} = (99.5 - 1.5)\% \text{ (realistic)}$$

\*(in PHENIX Multiplicity PRL)

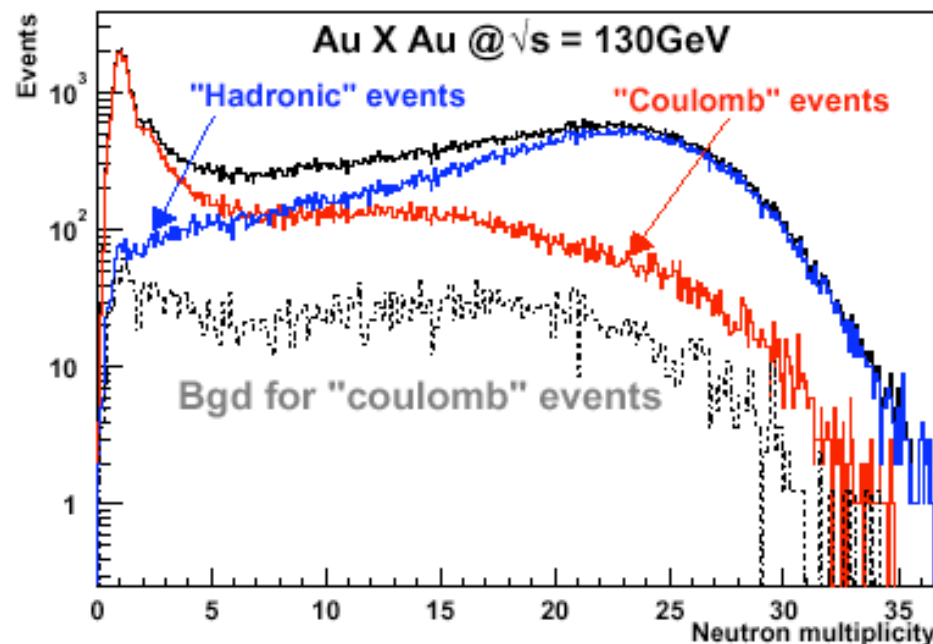
BBC ineff- $\rightarrow$  Coulomb bkg

### Other corrections

- Coulomb- $\rightarrow$  BBC hits
- Coulomb- $\rightarrow$  ZDC miss
- Diffraction Dissociation

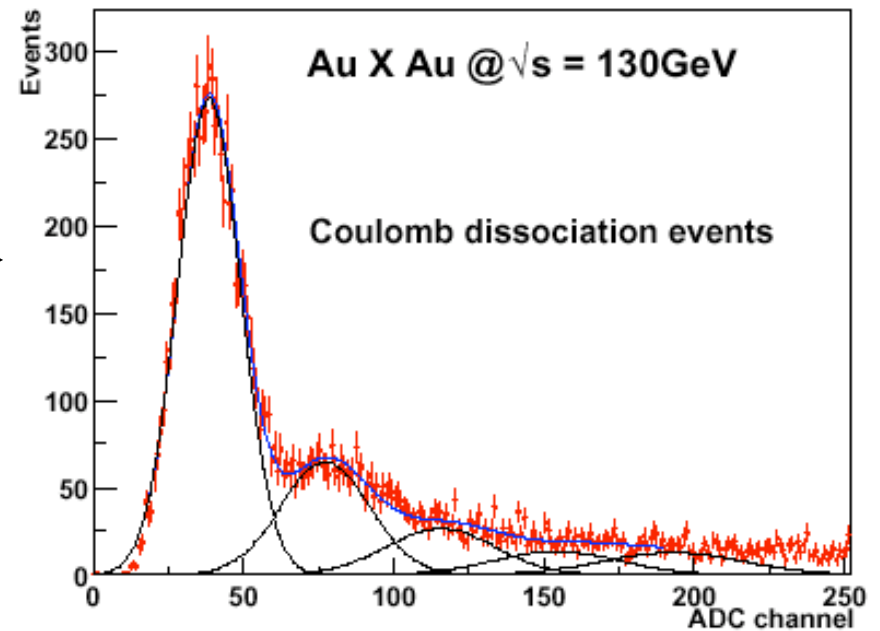
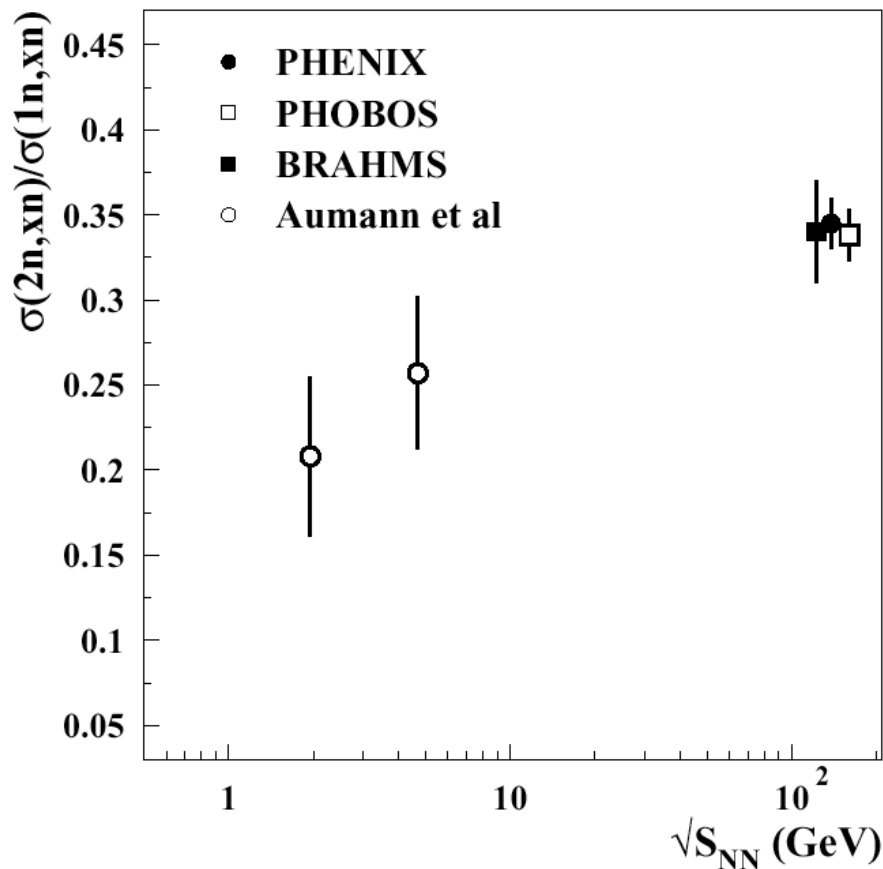
(all negligible)

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Left ZDC neutron multiplicity  
cut on 1n in Right ZDC



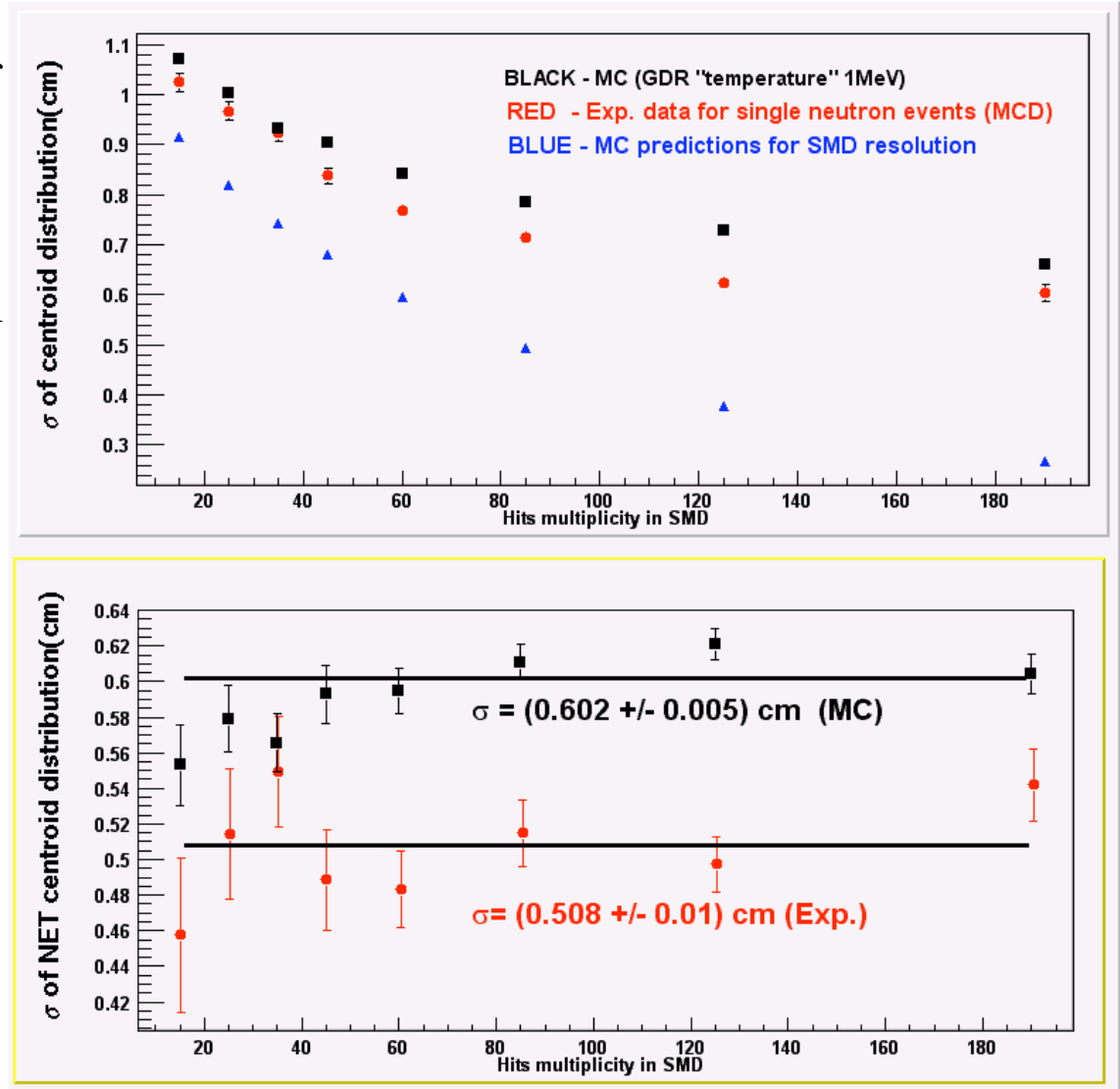
2n/1n cross sections, compared  
To low energy radiochemical data

## SMD centroid width for single neutron MCD at 100GeV

Top panel presents the dependence of shower centroid width (sigma of Gaussian fit) on light yield in the SMD for events with single neutron (MCD events, red points). Black points are ones for MC GDR events. Blue points are MC prediction for SMD resolution.

Bottom panel presents “net” widths for neutron x-distribution in MCD events after subtraction of SMD resolution.

The measured width of the centroid distribution is about 20% less than the one for MC events which have been generated for GDR with a decay temperature of 1.0 Mev.



PHENIX

“Private”

data

“Broad” part of  
the

distribution is due  
to spectator  
neutrons with a  
Fermi-motion  
spread.

this spread  
corresponds to

$\sigma = 2.21$  cm

## Centroid distribution for multineutron events

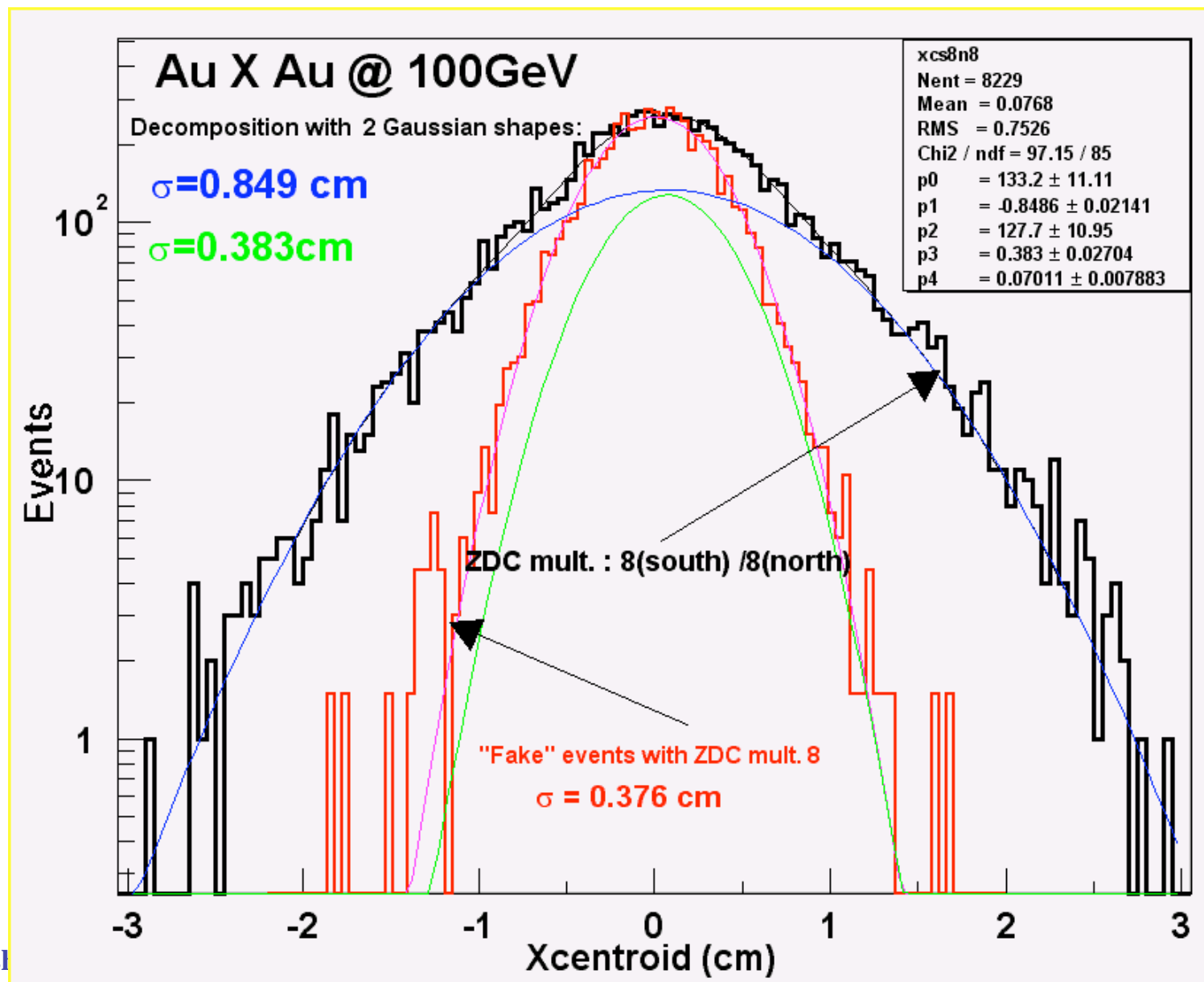


TABLE I. Cross sections calculated and derived from the data. The errors quoted on measurements include the uncertainty of the BBC cross section [8]

Cross Section	Calculated Value(1)	Calculated Value(2)	Measured
$\sigma_{tot}^*$	$10.83 \pm 0.5 \text{Barns}$	$11.19 \pm$	N.A.
$\sigma_{geom}$	$7.09 \pm xx$	$7.29 \pm xx$	N.A.
$\frac{\sigma_{geom}}{\sigma_{tot}}$	0.67	0.65	$0.661 \pm 0.014$
electromagnetic			
$\frac{\sigma(1n,Xn)}{\sigma_{tot}}$	0.125	xx	$0.117 \pm 0.003 \pm 0.002$
$\frac{\sigma(1n,1n)}{\sigma_{1n,Xn}}$	0.329	xx	$0.345 \pm 0.01 \pm 0.006$
$\frac{\sigma(2n,Xn)}{\sigma_{1n,Xn}}$	xx	0.327	$0.345 \pm 0.011 \pm 0.01$

## \*Definitions

$$\sigma_{tot} = \sigma_{\text{(Mutual Coulomb Dissociation)}} + \sigma_{\text{(geom)}} = \sigma_{\text{(hadronic)}}$$

## Calculated cross sections for PbPb@LHC

*A.J.Baltz, C.Chasman and SNW NIM A417(1998)p.1*

(errors can be inferred from above RHIC discussion)

$\sigma_{1n,1n}$	0.537 barns
$\sigma_{1n,xn}$	1.897
$\sigma_{xn,xn}$	14.75
$\sigma_{xn}$	227.3

# Accelerator Based Determination of Luminosity

To 1st order based on 3 accelerator measurements- ie.

$$\mathcal{L} = B \frac{N_p N_{\bar{p}}}{4\pi \sigma_x \sigma_y} f$$

$N_p$  = total current in a “bunch”

$\sigma_{x,y}$  = transverse dimensions of the bunches

**Above methodologies developed to check the instrumentation which measures these parameters.**

**This calibration is essentially independent of the beam species.**

**-ie calibrate at one energy-> all others (CDF example)**

**-@LHC calibrate with whatever species is more precise (pp or AA)**



## Accelerator based.. (to next order)

$$\mathcal{L}_{i,j} = N_p N_{\bar{p}} \int \frac{1}{\sqrt{2\pi}\sigma_z} \frac{e^{-\frac{z^2}{2\sigma_z^2}}}{4\pi\sigma_x(z)\sigma_y(z)} dz$$

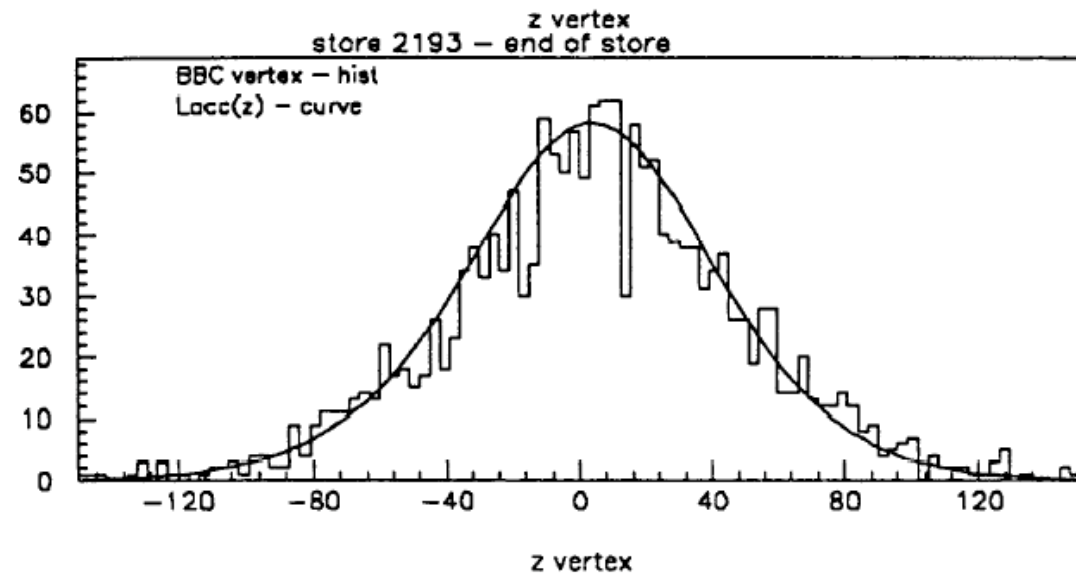
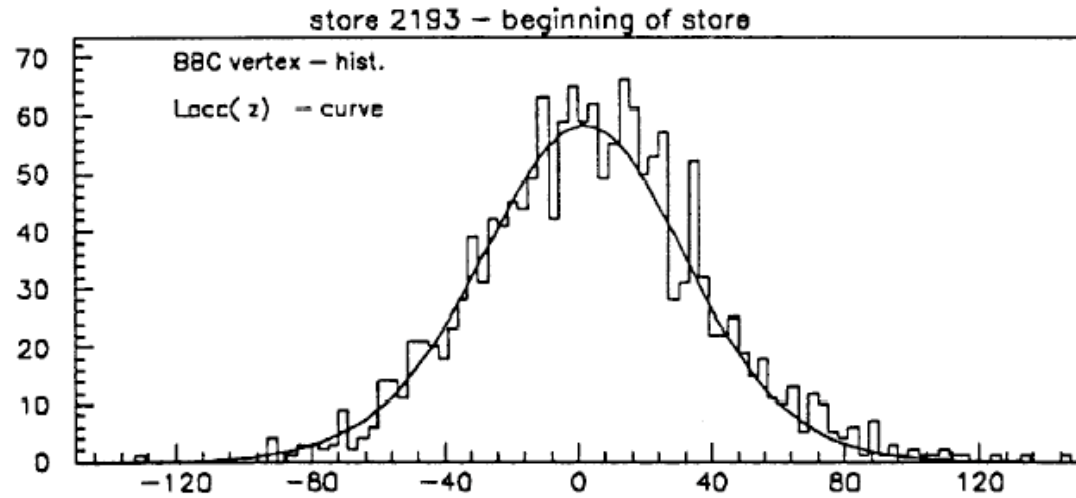
$$\sigma_x^2(z) = \frac{1}{6\pi\gamma} (\beta_x(z)\epsilon_x) + \left(\eta(z) \frac{dp}{p}\right)^2$$

$$\sigma_y^2(z) = \frac{1}{6\pi\gamma} \beta_y(z)\epsilon_y$$

ie things are more complicated if momentum dispersion.ne.0  
or  $\sigma^* \ll$  bunch length

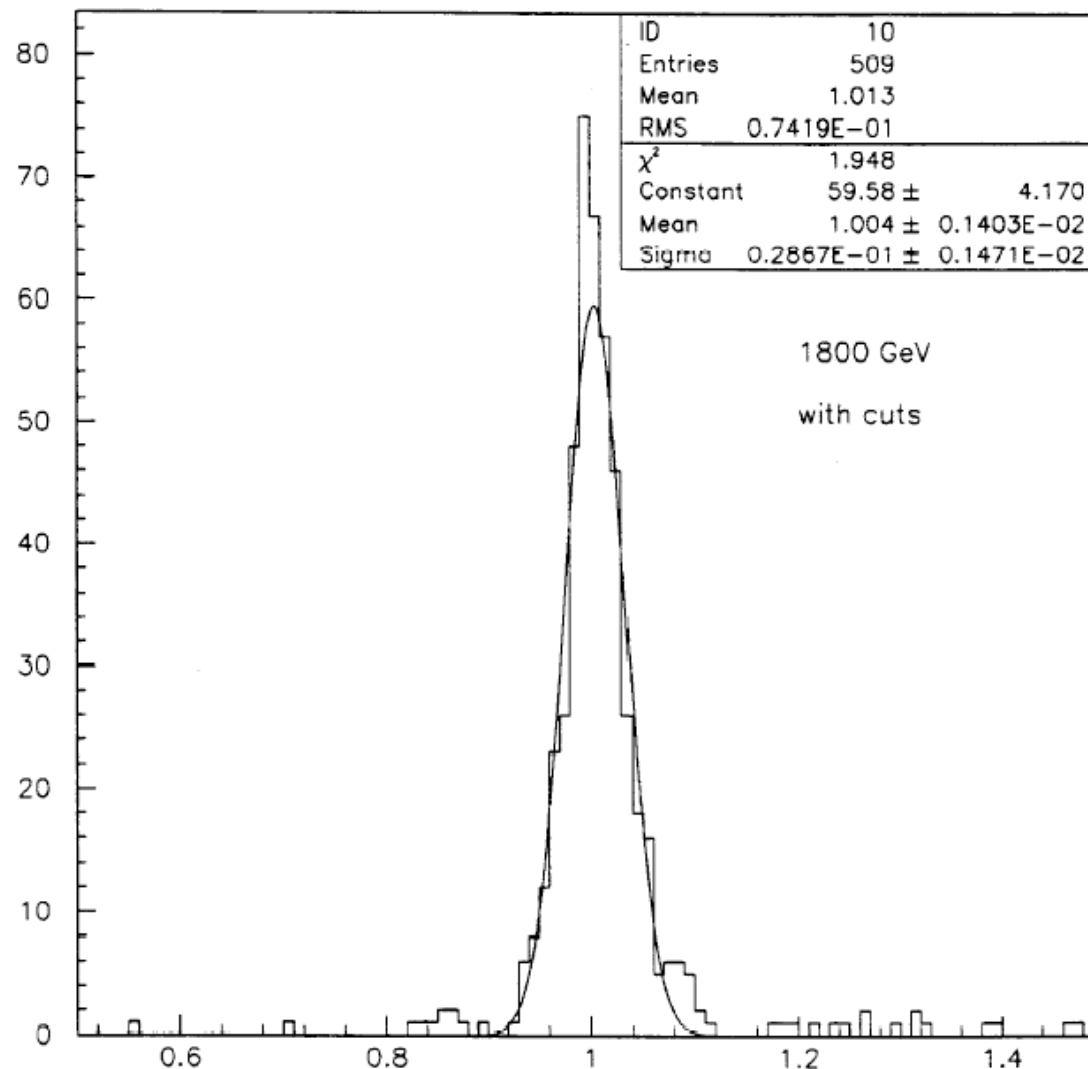
# CDF experience:

*C.Grosso-Pilcher and SNW ,FN-550(1990)*



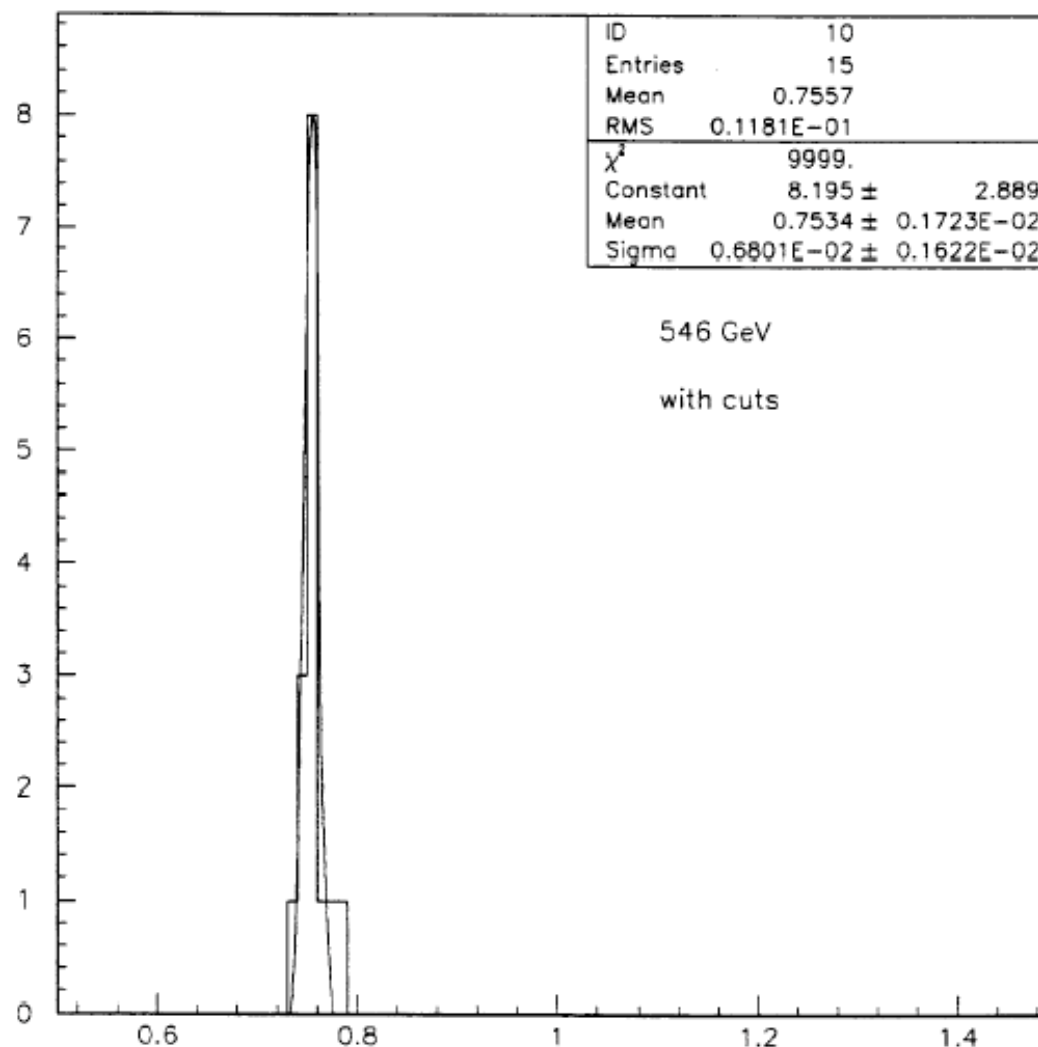
## CDF experience: (continued)

Ratio of monitor rate  
to accelerator calculated  
Luminosity  
(1 event=1 scan)  
1800 GeV data

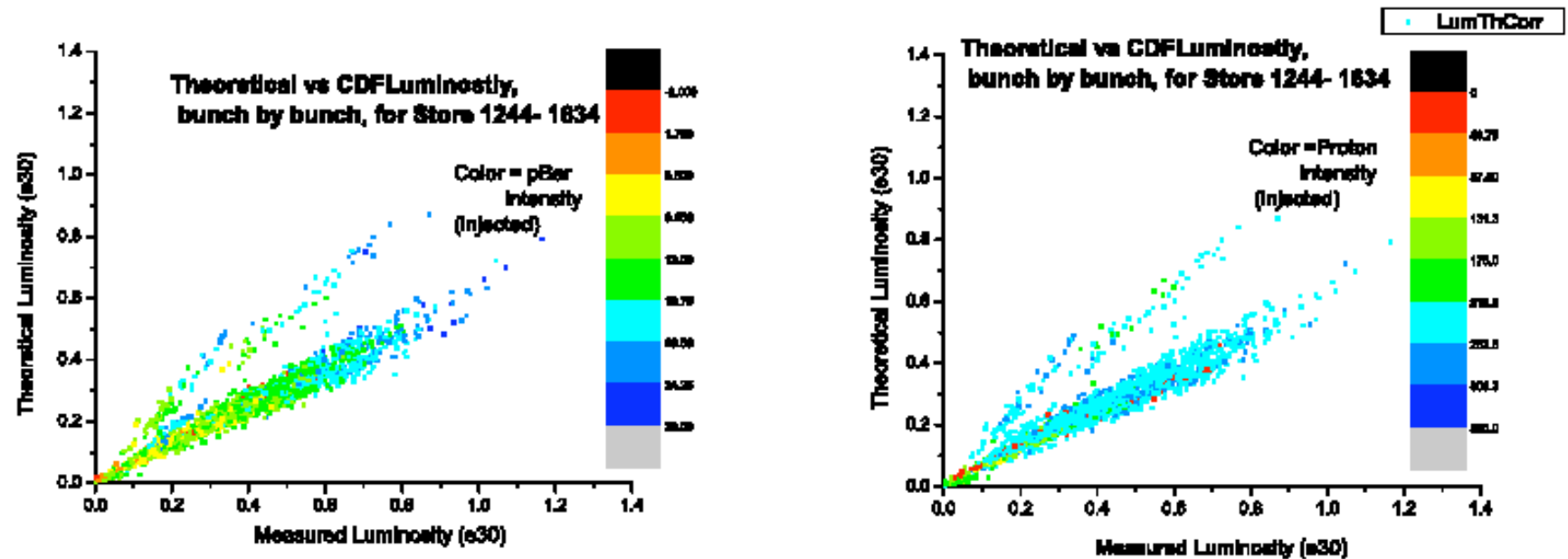


## CDF experience: (continued)

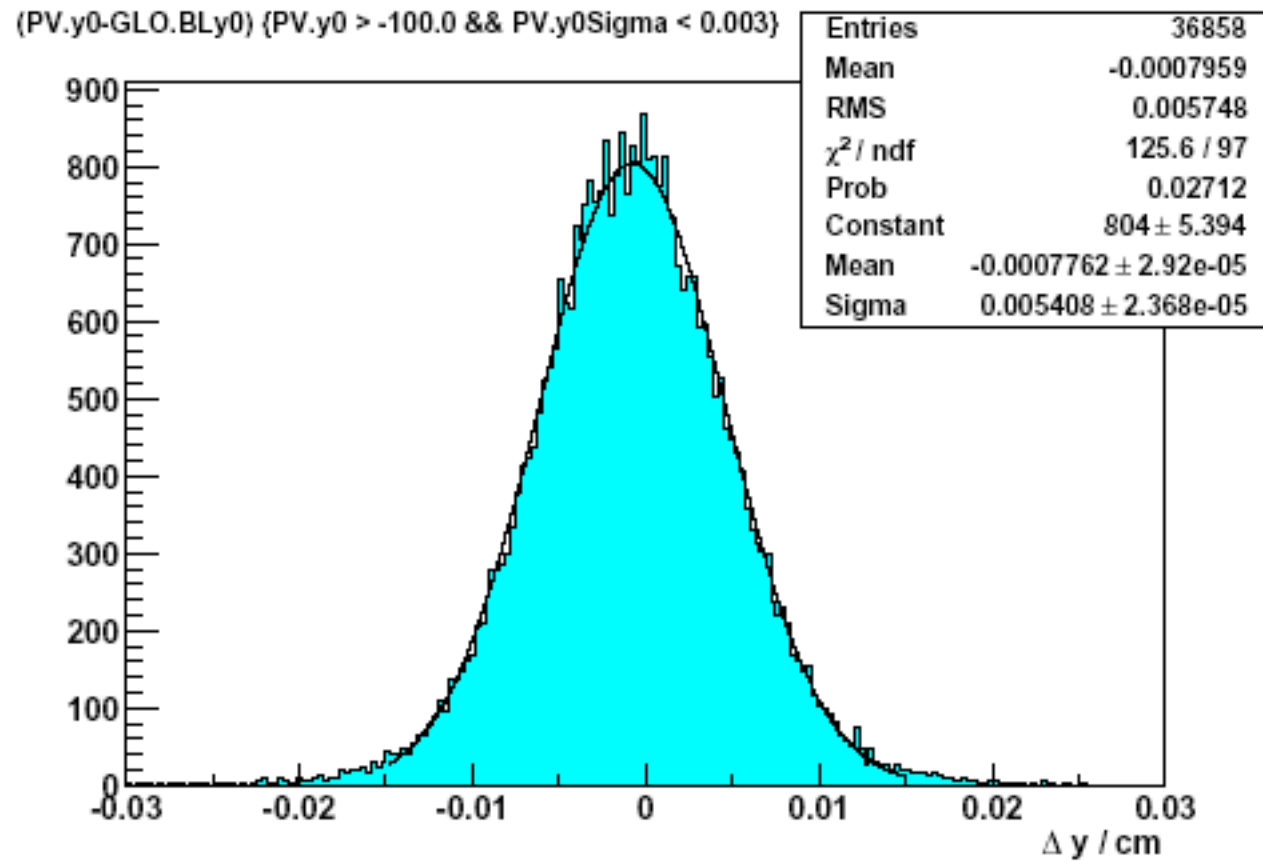
Ratio of monitor rate  
to accelerator calculated  
Luminosity  
(1 event=1 scan)  
546 GeV data



Similar studies in 2002 (courtesy P.Lebrun)



# CDF measurement of beam position and sigma (2002- SVX)



# Conclusions

1. 5% Luminosity measurement was achieved “at startup” in HI
2. This will be improved to  $\sim 2\%$  before LHC era
3. A coordinated luminosity measurement scheme was successfully implemented in 4 experiments (and used reliably also in RHIC acc. Control room)
4. It was very useful in pp running also.

# A Proposal

- A coordinated approach to LHC Heavy Ion luminosity measurements->performance criteria (LARP, DOE-NP, LHC Instrum)
- Actual detector technologies could differ(RHIC example)
- This has interesting implications for pp



MC simulation of the ZDC response to 2.7 TeV neutrons from GDR decay.  
ZDC module: 10mm Tungsten+0.5(dia) fibers @ 45Dgr, 13layers/module, (2λ)

Fiber's NA = 0.3.

Fit:  $\sim \exp(-(x-\mu)^2/(2\sigma^2))$

$\mu = p1, \sigma = p2 + p3*(x-\mu)/\mu$

