

*The 17th Workshop of the LHC Higgs Working group*

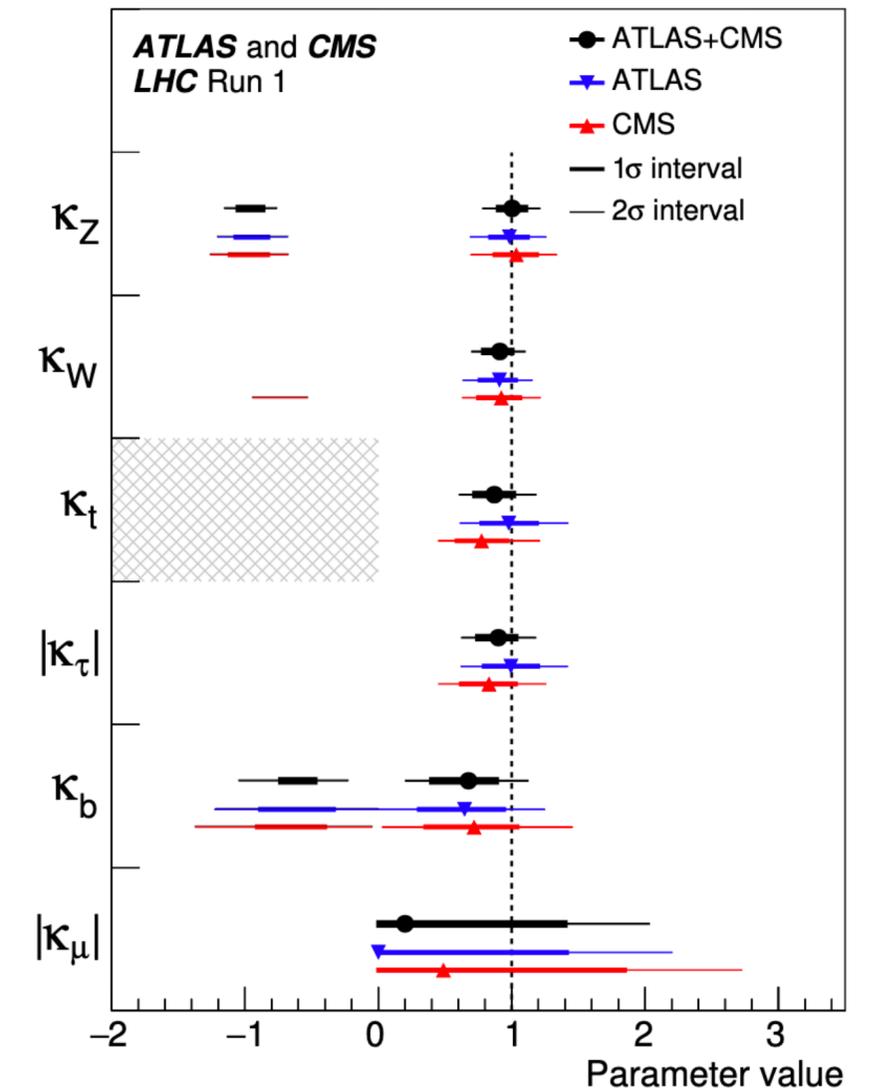
# STXS EFT interpretations

Ana Cueto (L.A.P.P.) on behalf  
of the ATLAS and CMS  
collaborations



# Introduction

- ❖ Extensive set of Higgs boson properties measurements from ATLAS and CMS
- ❖ Large Run 2 dataset has allowed to measure finer bins in Simplified Template Cross Section (STXS) framework separating different production modes kinematic regions
  - ▶ Unprecedented precision achieved
- ❖  $\kappa$ -framework served well for initial interpretations, but
  - ▶ Not a QFT, only possible at LO
  - ▶ Designed for rates and not sensitive to growth with energy in kinematic distributions



From [arXiv:1606.02266](https://arxiv.org/abs/1606.02266)

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# The Standard Model Effective Field Theory

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- ❖ SMEFT allows a systematic interpretation of large data sets in terms of new physics (NP)
- ❖ Extends the SM Lagrangian by adding new operators of  $d > 4$  suppressed by powers of the NP energy scale,  $1/\Lambda^{d-4}$ 
  - ▶ Valid for  $\Lambda \gg \text{vev}$ . Uses the same fields and keeps the same symmetries as the SM

$$\mathcal{L}_{SMEFT} = \mathcal{L}_{SM} + \sum_i \frac{c_i^{d=6}}{\Lambda^2} \mathcal{O}^{d=6} + \sum_i \frac{c_i^{d=8}}{\Lambda^4} \mathcal{O}^{d=8} + \dots$$

- ▶ Only  $c_i/\Lambda^{d-4}$  is measurable
  - ▶ Several operator bases can be worked out, different conventions in use
- ❖ Constrain EFT coefficients  $\rightarrow$  constrain large classes of UV theories

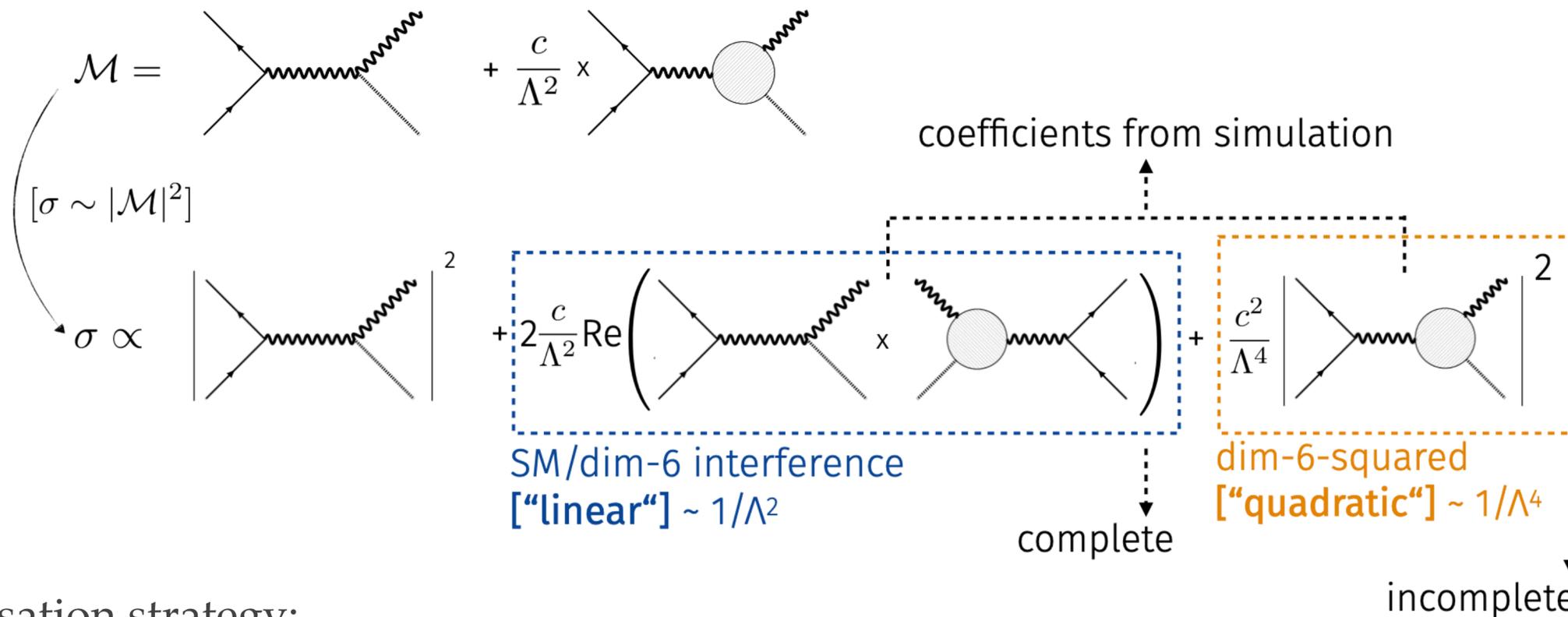
**In the analyses presented in this talk:**

**\* Focus on dimension 6 operators**

**\* Assuming  $U(3)^5$  flavour symmetry**

# From the SMEFT Lagrangian to STXS parametrisation

Brian Moser @ HIGGS2020



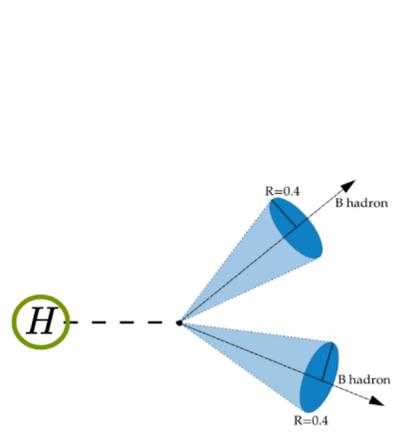
- ❖ Common parametrisation strategy:
  - ▶ Import the used SMEFT model in MadGraph and generate events for a given production mode switching on only the Wilson coefficients of interest (one-by-one or 2-by-2 for interference between 2 BSM amplitudes)
  - ▶ Analyse the generated events at particle level with a Rivet routine such as [this one](#)
  - ▶ Work out the parametrisation in each STXS bin by taking ratios to the SM predictions generated with the same setup and at the same calculation order
  - ▶ Assume same unfolding efficiencies as in the SM

# VH, H → bb (ATLAS)

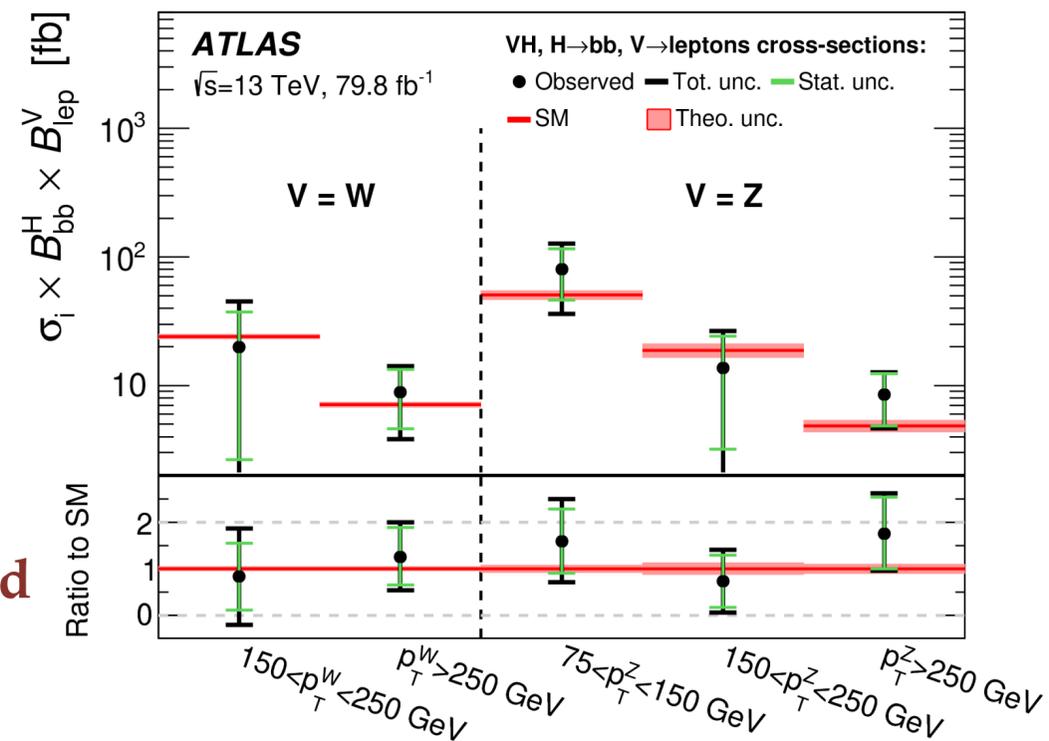
[arXiv:2007.02873](https://arxiv.org/abs/2007.02873)

[arXiv:2008.02508](https://arxiv.org/abs/2008.02508)

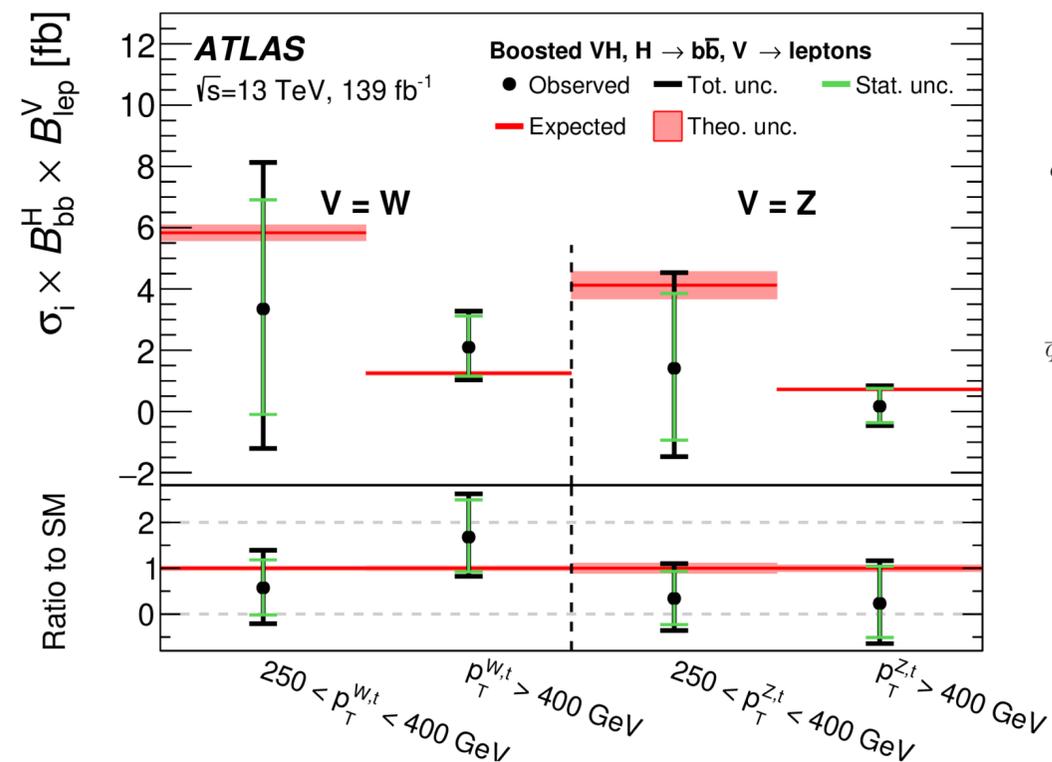
- Two analyses (resolved and boosted) using the same strategy for EFT interpretation
  - Warsaw basis as implemented in SMEFTsim in the Mw scheme.



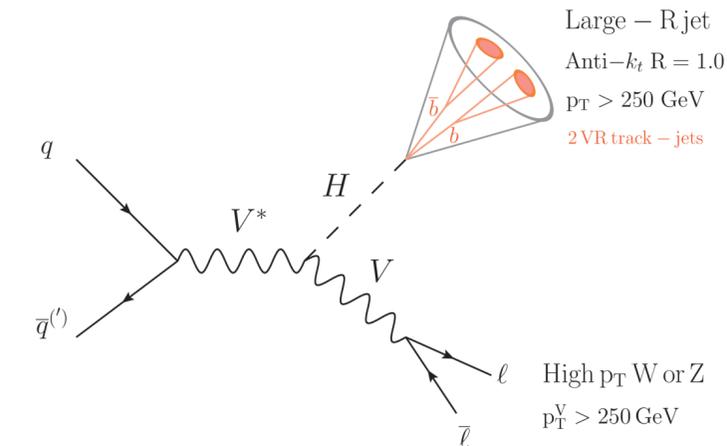
**Resolved**



Inclusive bin for  $p_T^V > 250$  GeV



Additional splitting at high  $p_T^V$



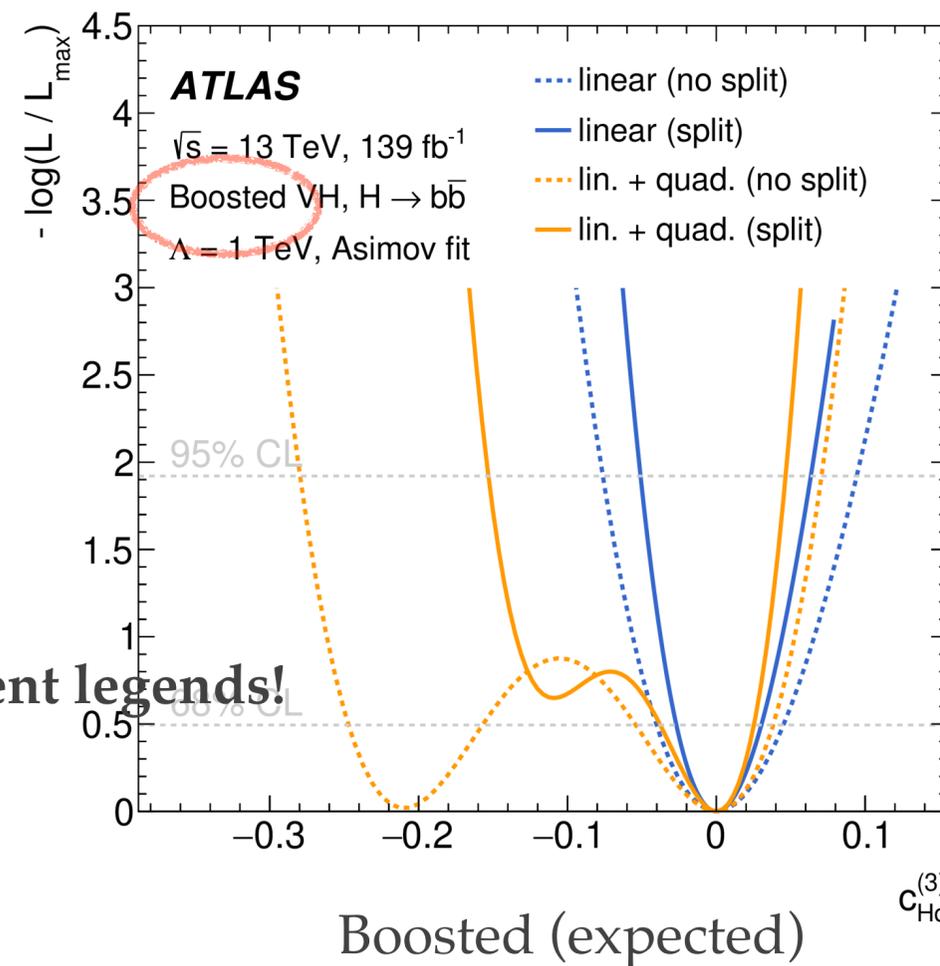
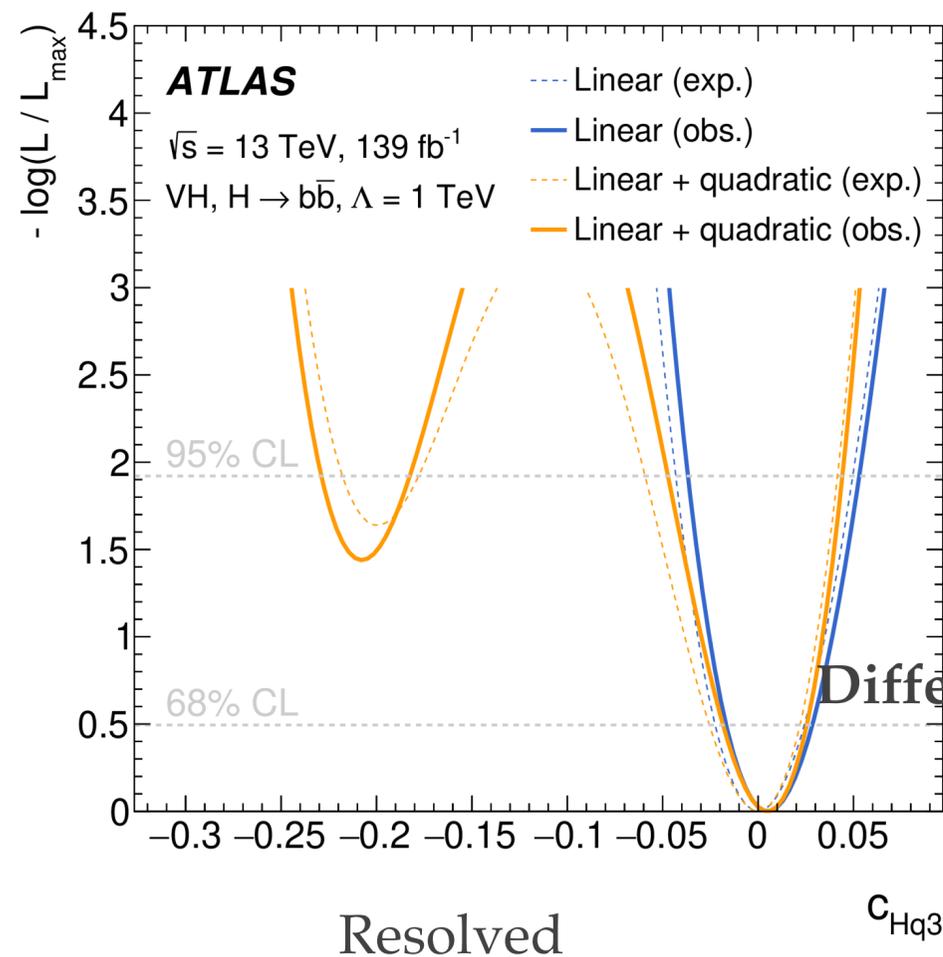
**Boosted**

# VH, H → bb (ATLAS)

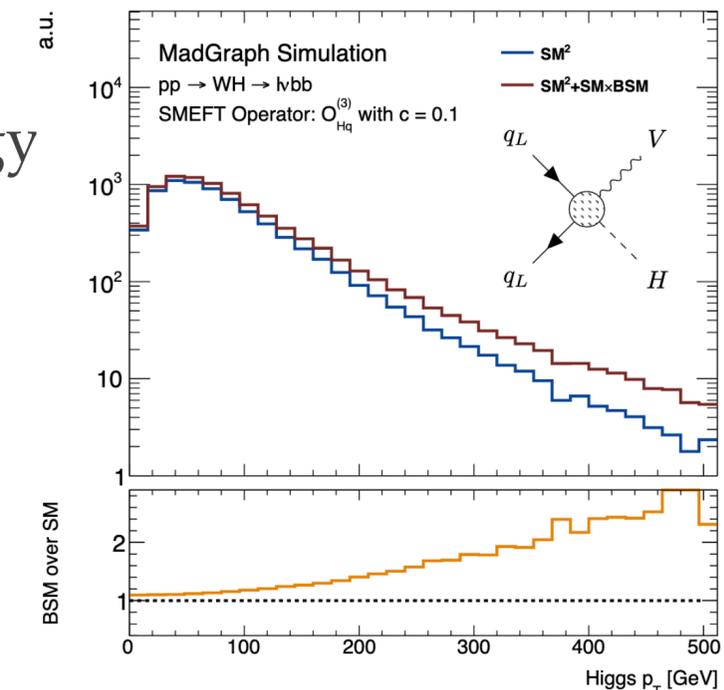
[arXiv:2007.02873](https://arxiv.org/abs/2007.02873)

[arXiv:2008.02508](https://arxiv.org/abs/2008.02508)

- How much improvement can be achieved with higher granularity at high  $p_T^V$ ?
  - 1-D likelihood scans (all other Wilson coefficients set to 0) to  $c_{Hq3}$  which shows an energy growth
  - Boosted analysis less precise but achieves competitive constraints thanks to higher reach in  $p_T^H$



Different legends!



Impact of  $c_{Hq3}$  in  $p_T^H$

$$p_T^V \sim p_T^H$$

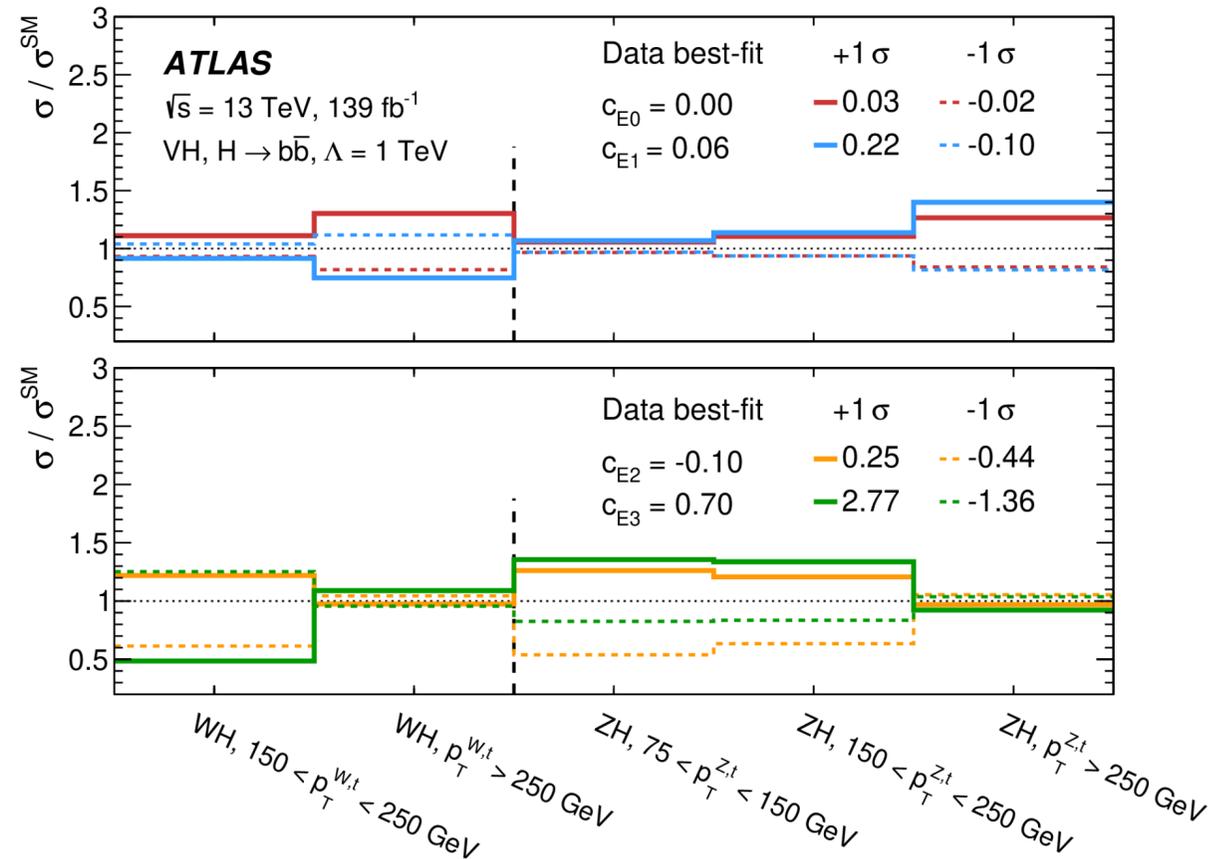
**Split at 400 GeV can improve limits by a factor of ~two**

# VH, H → bb (ATLAS)

[arXiv:2007.02873](https://arxiv.org/abs/2007.02873)

[arXiv:2008.02508](https://arxiv.org/abs/2008.02508)

- ❖ Several operators affecting VH, H → bb in the Warsaw basis
  - ▶ Not possible to to constrain all with 4/5 measured STXS bins
  - ▶ Do a principal component analysis (PCA). Methodology from [ATL-PHYS-PUB-2019-042](https://arxiv.org/abs/ATL-PHYS-PUB-2019-042)
  - ▶ Fit simultaneously the sensitive directions

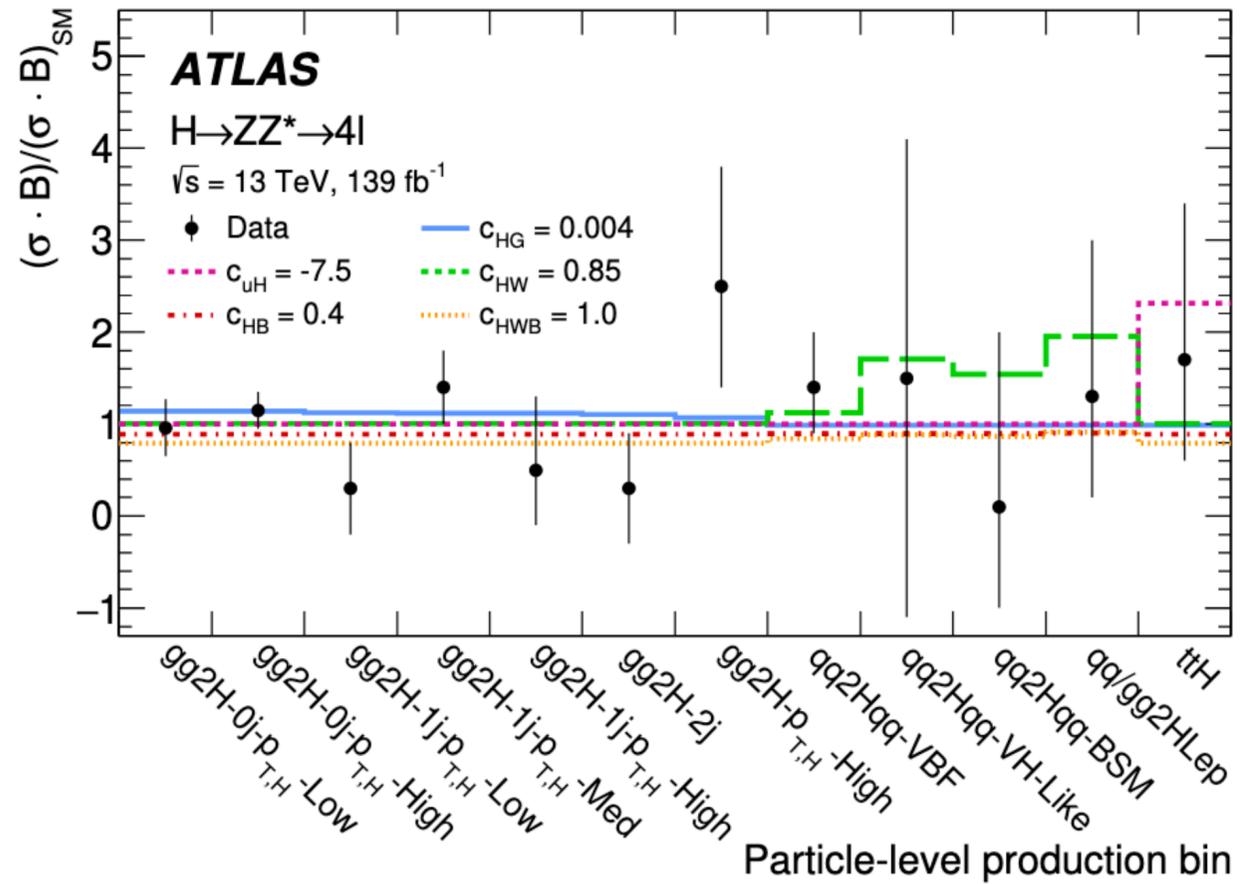


Wilson coefficient	Eigenvalue	Eigenvector
$c_{E0}$	2000	$0.98 \cdot c_{Hq3}$
$c_{E1}$	38	$0.85 \cdot c_{Hu} - 0.39 \cdot c_{Hq1} - 0.27 \cdot c_{Hd}$
$c_{E2}$	8.3	$0.70 \cdot \Delta\text{BR}/\text{BR}_{\text{SM}} + 0.62 \cdot c_{HW}$
$c_{E3}$	0.2	$0.74 \cdot c_{HWB} + 0.53 \cdot c_{Hq1} - 0.32 \cdot c_{HW}$
$c_{E4}$	$6.4 \cdot 10^{-3}$	$0.65 \cdot c_{HW} - 0.60 \cdot \Delta\text{BR}/\text{BR}_{\text{SM}} + 0.35 \cdot c_{Hq1}$

Only Wilson coefficients with an impact in an EV larger than 0.2 retained

# H → 4l (ATLAS)

arXiv:2004.03447



- ❖ Interpretation of STXS measurements in the Warsaw basis with Mw scheme
- ❖ Main operators affecting the measurement are selected
- ❖ Linear+quadratic terms included in the parametrisation as well as CP-even and CP-odd operators

CP-even			CP-odd			Impact on	
Operator	Structure	Coeff.	Operator	Structure	Coeff.	production	decay
$O_{uH}$	$HH^\dagger \bar{q}_p u_r \tilde{H}$	$c_{uH}$	$O_{\tilde{u}H}$	$HH^\dagger \bar{q}_p u_r \tilde{H}$	$c_{\tilde{u}H}$	$ttH$	-
$O_{HG}$	$HH^\dagger G_{\mu\nu}^A G^{\mu\nu A}$	$c_{HG}$	$O_{H\tilde{G}}$	$HH^\dagger \tilde{G}_{\mu\nu}^A G^{\mu\nu A}$	$c_{H\tilde{G}}$	ggF	Yes
$O_{HW}$	$HH^\dagger W_{\mu\nu}^l W^{\mu\nu l}$	$c_{HW}$	$O_{H\tilde{W}}$	$HH^\dagger \tilde{W}_{\mu\nu}^l W^{\mu\nu l}$	$c_{H\tilde{W}}$	VBF, VH	Yes
$O_{HB}$	$HH^\dagger B_{\mu\nu} B^{\mu\nu}$	$c_{HB}$	$O_{H\tilde{B}}$	$HH^\dagger \tilde{B}_{\mu\nu} B^{\mu\nu}$	$c_{H\tilde{B}}$	VBF, VH	Yes
$O_{HWB}$	$HH^\dagger \tau^l W_{\mu\nu}^l B^{\mu\nu}$	$c_{HWB}$	$O_{H\tilde{W}B}$	$HH^\dagger \tau^l \tilde{W}_{\mu\nu}^l B^{\mu\nu}$	$c_{H\tilde{W}B}$	VBF, VH	Yes

- ❖ CP-odd operators only appear in the quadratic terms
- ❖ For several operators, quadratic terms are relevant

# H → 4l (ATLAS)

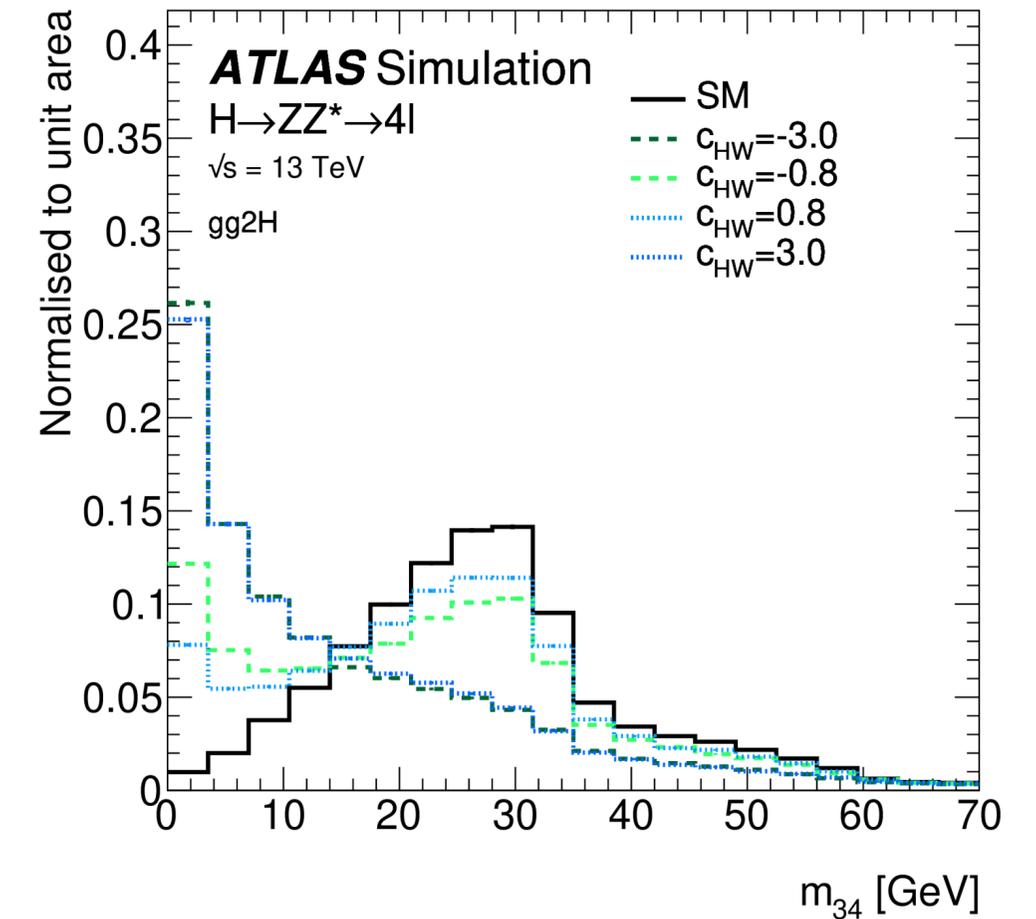
[arXiv:2004.03447](https://arxiv.org/abs/2004.03447)

- ❖ Reconstruction-level requirements on  $m_{12}$  and  $m_{34}$  to target  $H \rightarrow ZZ^*$
- ❖ EFT does not have the same acceptance as SM and needs to be corrected in the parametrization
- ❖ Other effects: differences in efficiencies or classification in reco bins used in the analysis found to be negligible

## Strategy:

- \* Mimic reco selection at particle level
- \* Fit a 3-D Lorentzian function for  $c_{HW}$ ,  $c_{HB}$ ,  $c_{HWB}$  for the acceptance correction relative to SM (or their CP-odd analogous assuming the CP-even ones vanish)

$$\frac{A(\vec{c})}{A_{SM}} = \alpha_0 + (\alpha_1)^2 \cdot \left[ \alpha_2 + \sum_i \delta_i \cdot (c_i + \beta_i)^2 + \sum_{\substack{ij \\ i \neq j}} \delta_{(i,j)} \cdot c_i c_j + \sum_{\substack{(i,j,k) \\ i \neq j \neq k}} \delta_{(i,j,k)} \cdot c_i c_j c_k \right]^{-1},$$



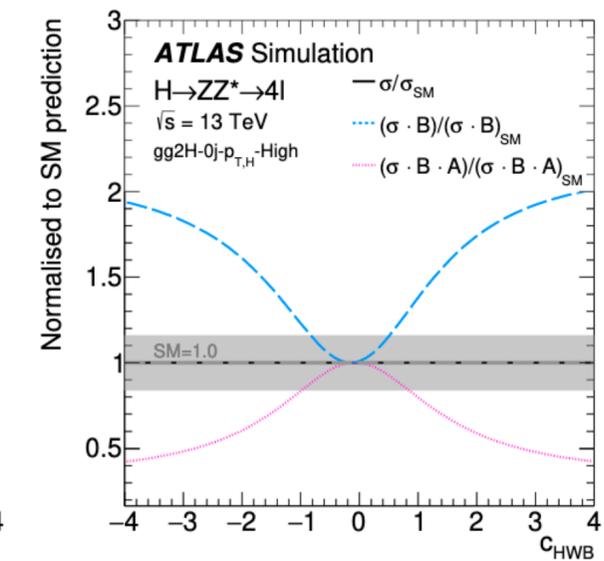
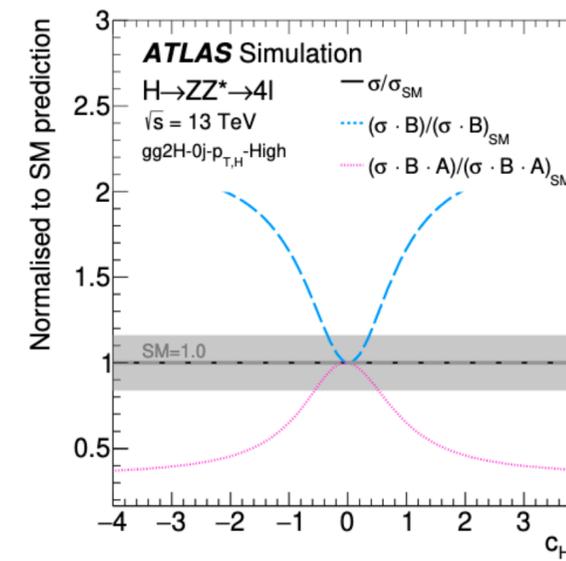
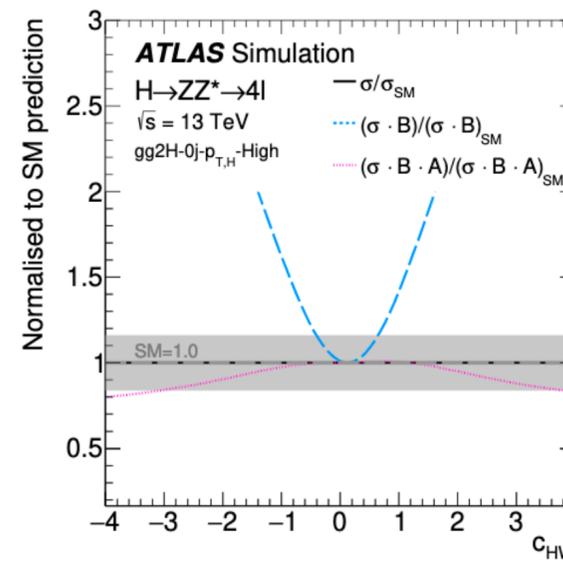
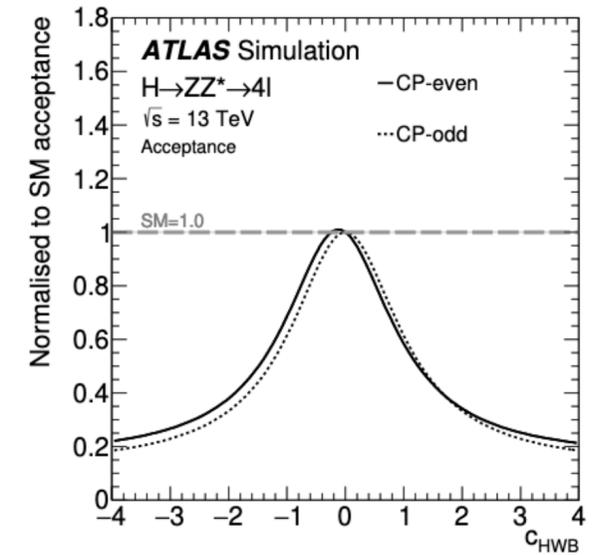
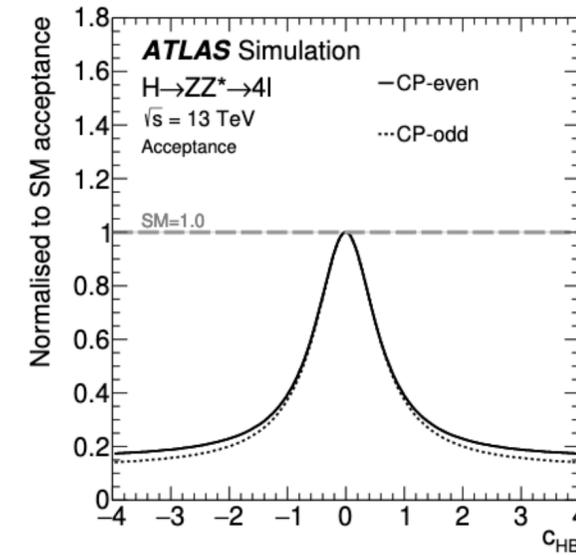
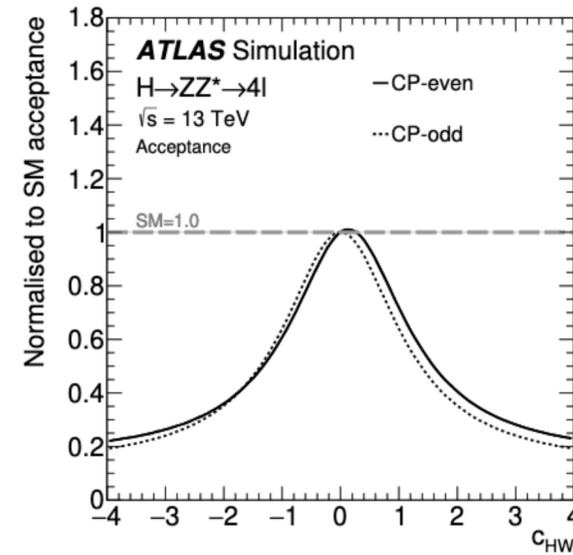
$i, j, k$  run over  $c_{HW}$ ,  $c_{HB}$ ,  $c_{HWB}$

$\alpha$ ,  $\beta$  and  $\delta$  parameters are free in the fit

# H → 4l (ATLAS)

arXiv:2004.03447

- ❖ Acceptance ratios varying one parameter at each time.
- ❖ Similar for CP-even and CP-odd operators (mostly from quadratic terms)
- ❖ Common acceptance parametrisation for all prod. modes
- ❖ Effects on the expected yields normalised to SM
- ❖ Non-linear dependence: effect of the BSM terms



Blue line: w.o. acceptance  
 Pink line: with acceptance

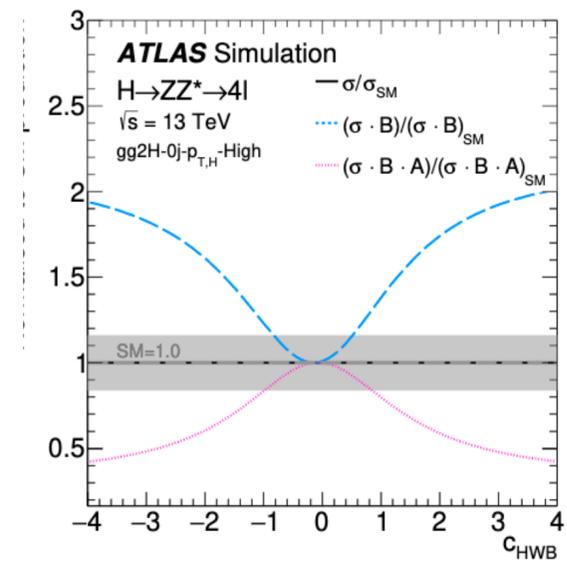
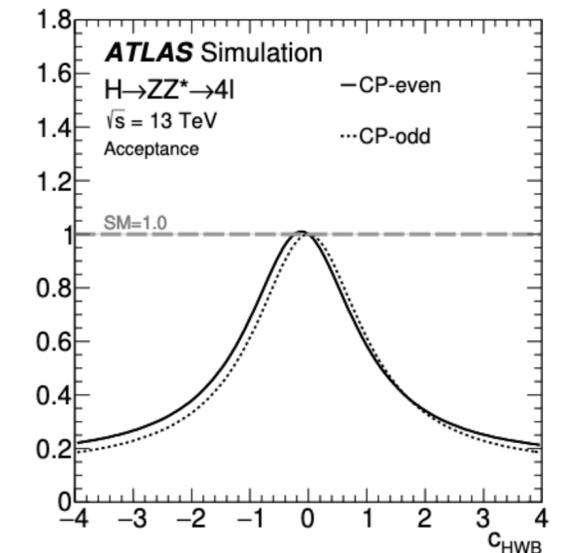
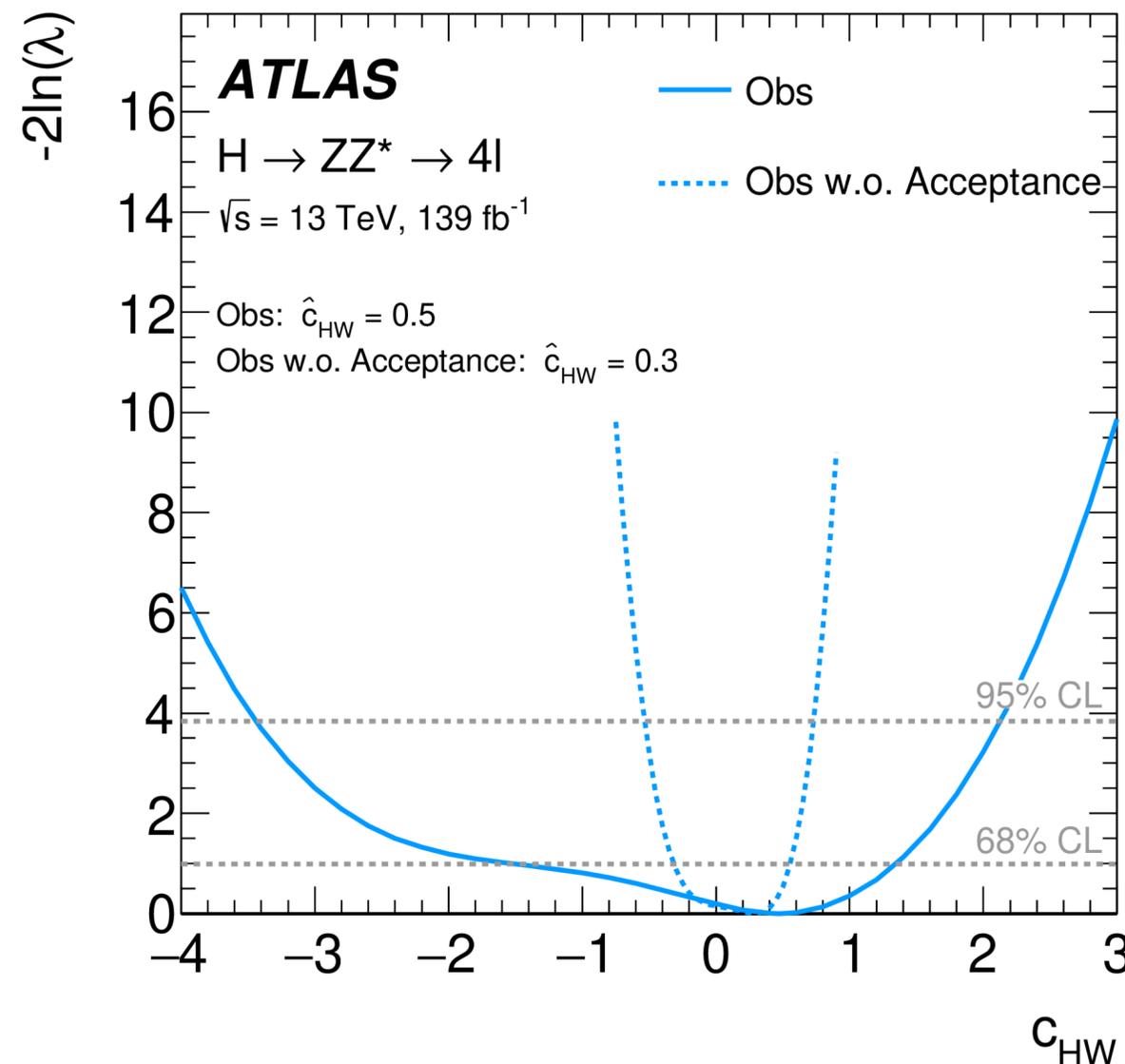
# H → 4l (ATLAS)

arXiv:2004.03447

Impact on 1-D scans:

**Acceptance correction is essential!**

- ❖ Acceptance ratios parameter at each
- ❖ Similar for CP-even operators (mostly terms)
- ❖ Common acceptance for all prod. modes
- ❖ Effects on the ex normalised to SM
- ❖ Non-linear dependence on the BSM terms



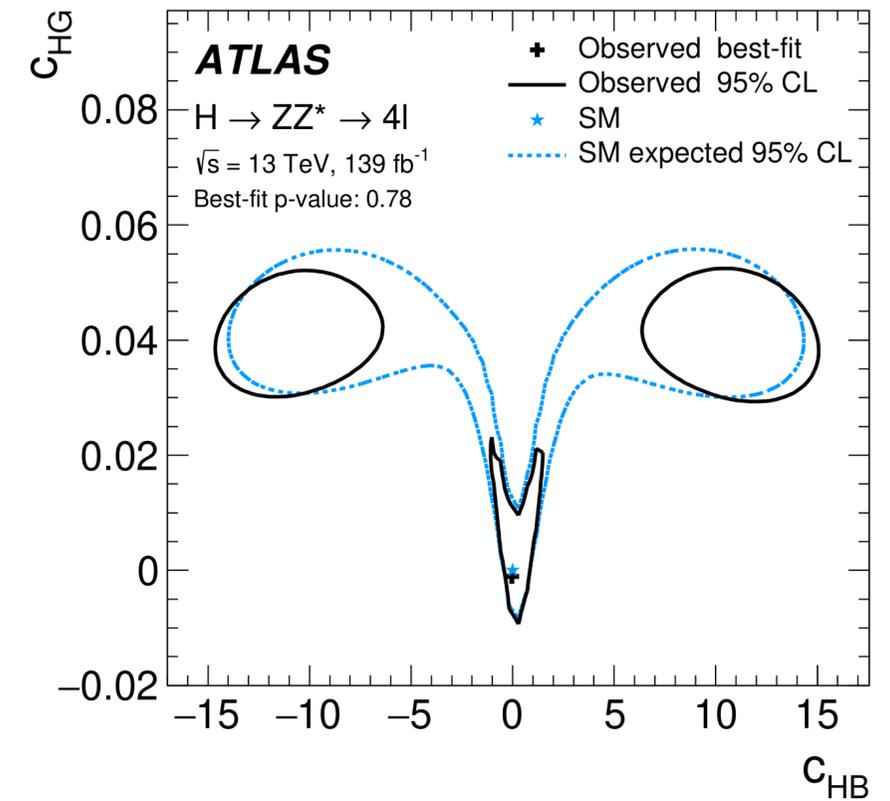
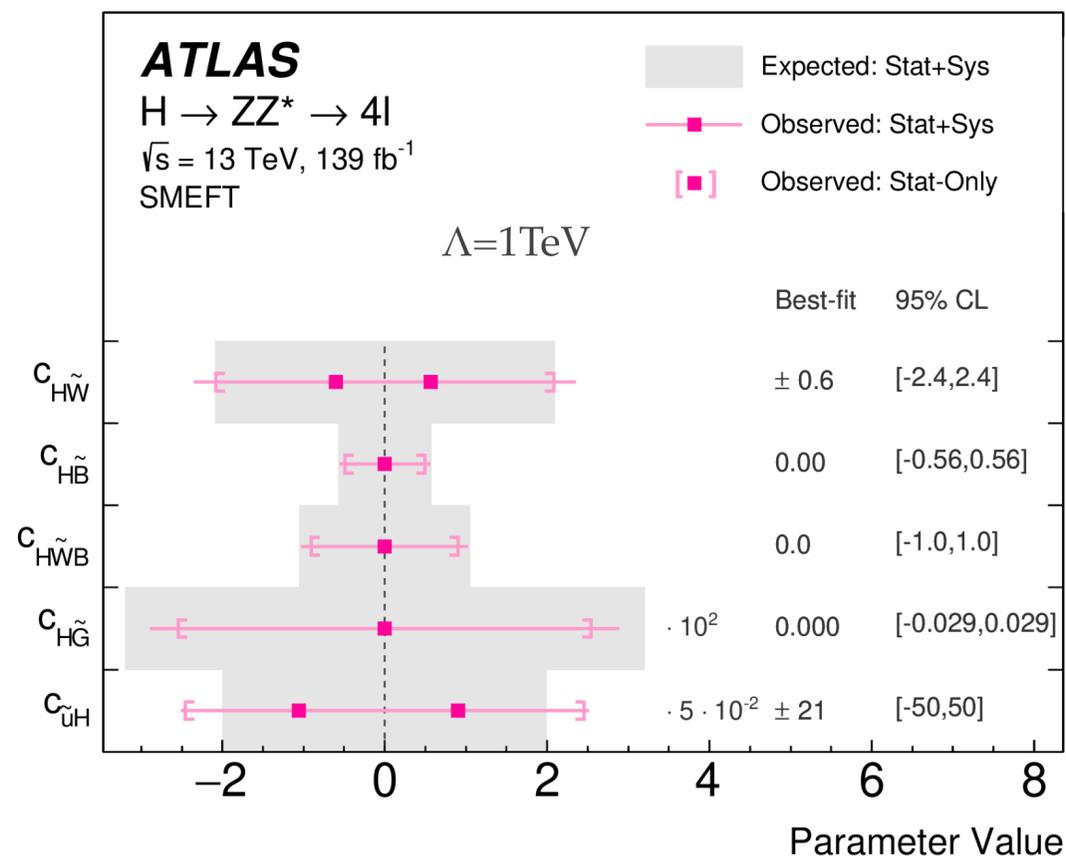
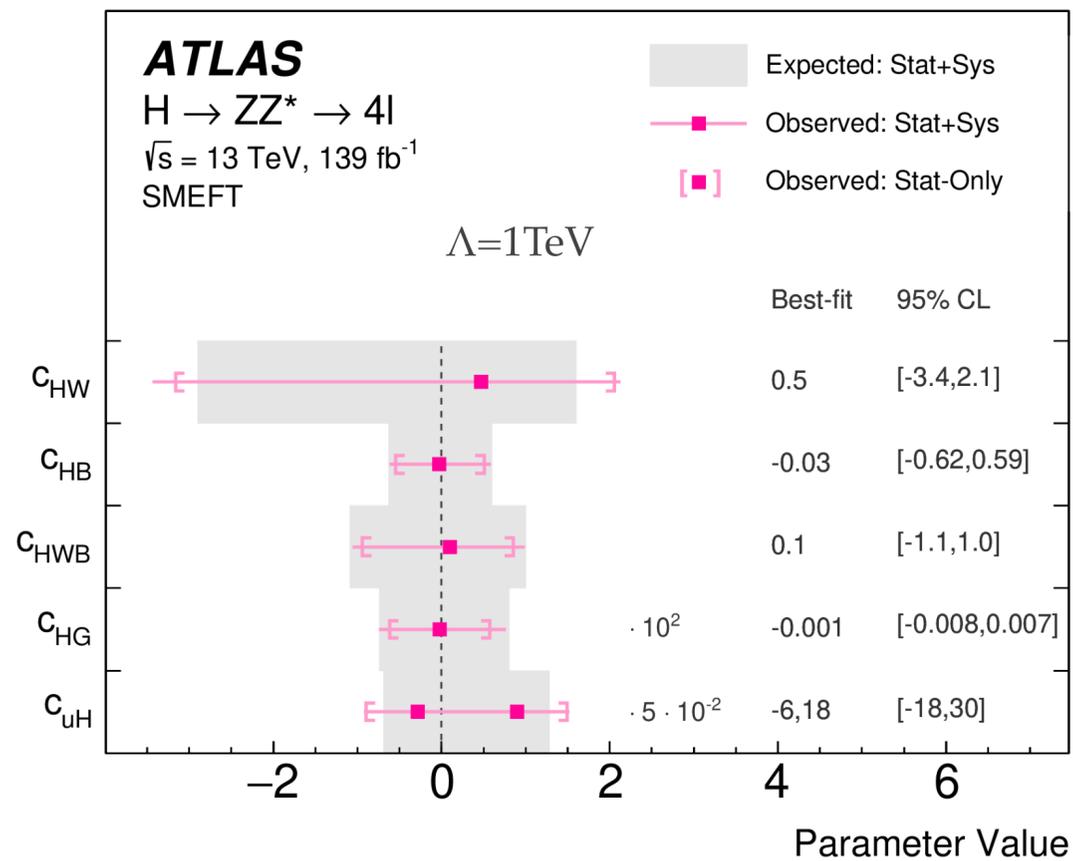
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link line: with acceptance

# H → 4l (ATLAS)

arXiv:2004.03447

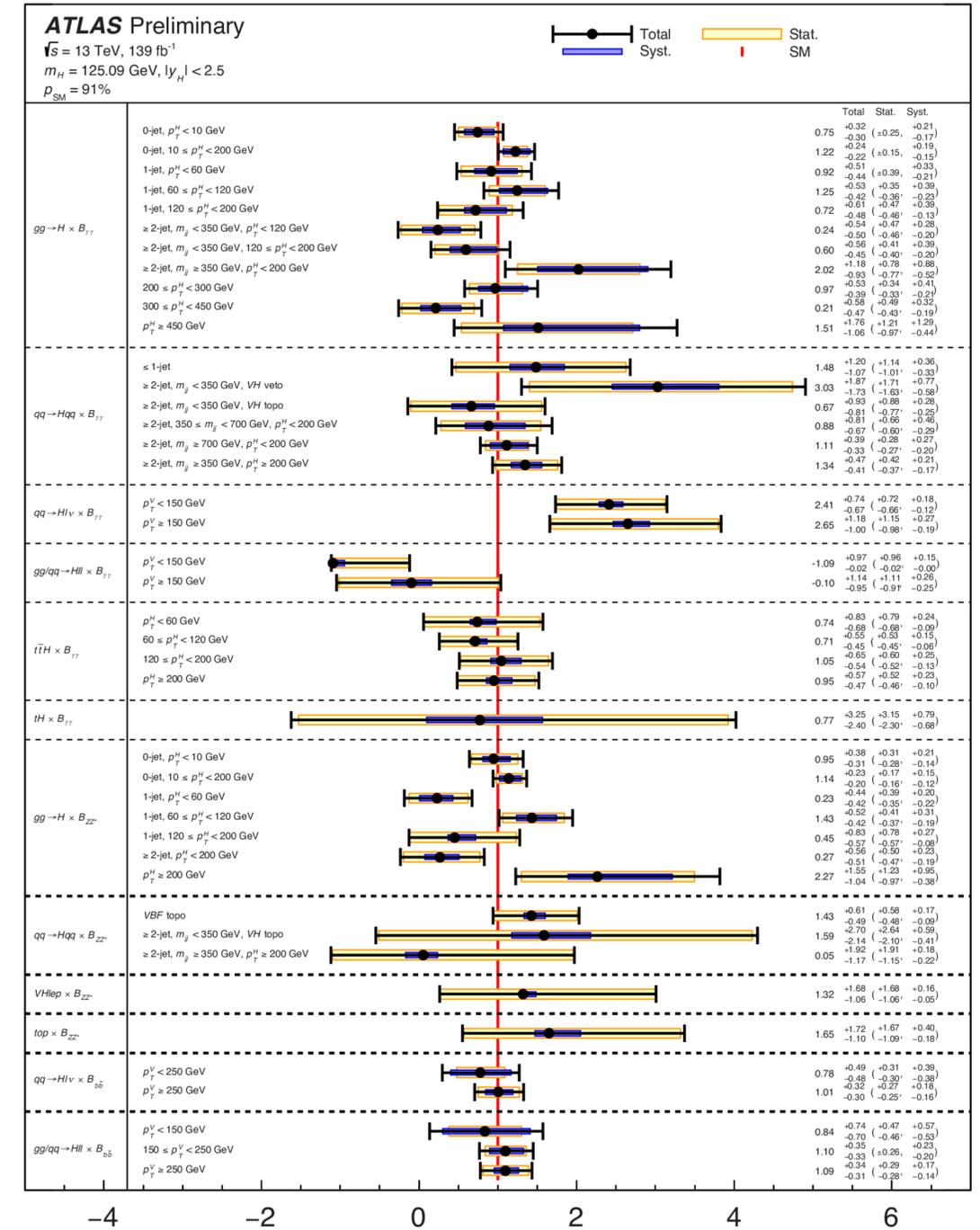
- ❖ Limits from 1-D fits (all others set to SM), correlations studied through 2D scans
  - ▶ Not trivial correlations between most of the parameter pairs



# Higgs combination (ATLAS)

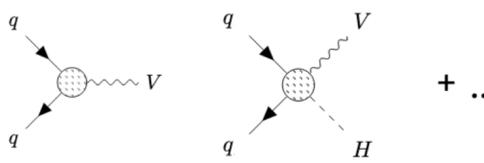
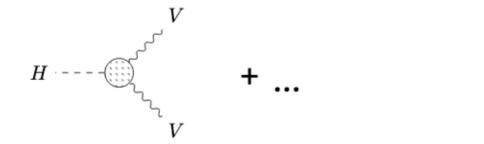
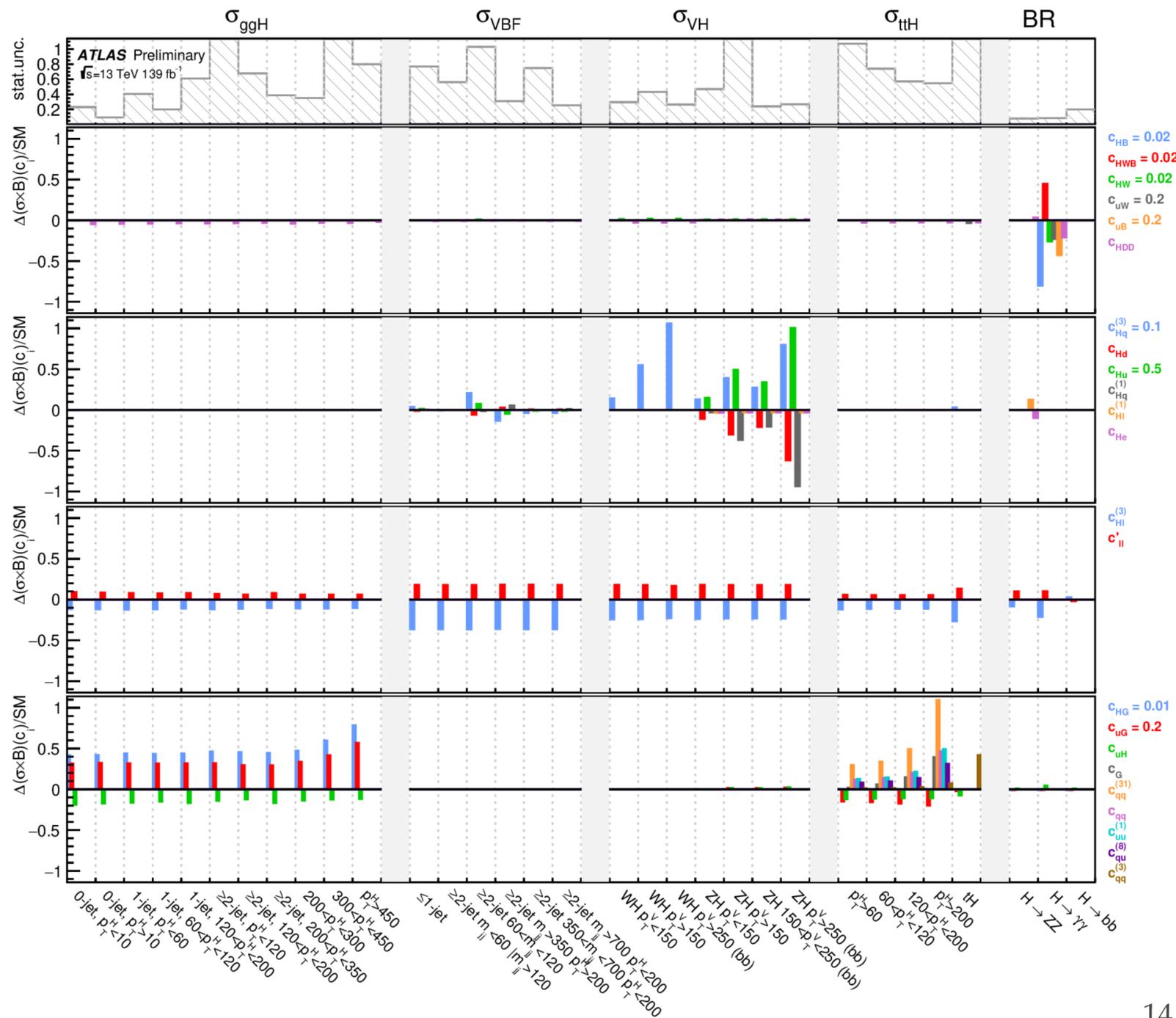
ATLAS-CONF-2020-053

- ❖ Stage 1.2 STXS combination of  $H \rightarrow \gamma\gamma$ ,  $VH(H \rightarrow bb)$  and  $H \rightarrow ZZ^* \rightarrow 4l$  for full Run 2
- ❖ Based on  $\sigma_{\text{STXS}i} \times \text{BR}_{H \rightarrow X}$  signal strength measurement
  - ▶ Warsaw basis in  $M_W$  scheme
  - ▶ Lowest order of each production mode or decay channel: NLO QCD for  $ggH$  and  $ggZH$  from SMEFT@NLO, NLO EW for  $H \rightarrow \gamma\gamma$ , LO for the rest from SMEFTsim
  - ▶ Only CP-even operators (no linear contribution from CP-odd ones and not available in SMEFT@NLO)
  - ▶ Include the acceptance effects in  $H \rightarrow ZZ^* \rightarrow 4l$  for cHW, cHB and cHWB

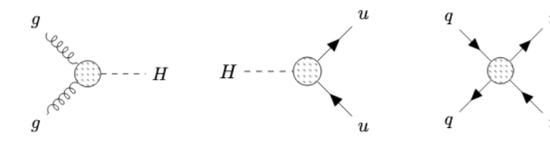


# Higgs combination (ATLAS)

ATLAS-CONF-2020-053



Shifts to  $G_f$



- ❖ Retain all operators that modify the production modes or BRs
- ❖ They can modify the couplings, introduce new diagrams, enter through field redefinitions or shifts to input quantities
- ❖ Simultaneous fit to all relevant single coefficients not possible due to degeneracies

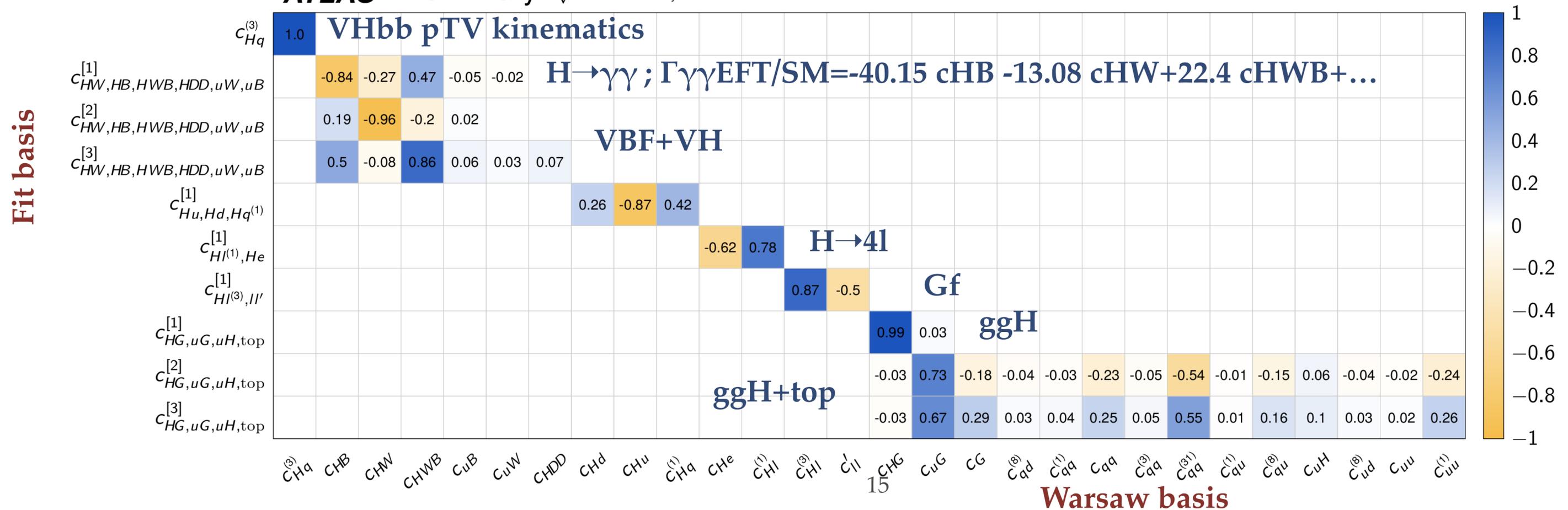
# Higgs combination (ATLAS)

ATLAS-CONF-2020-053

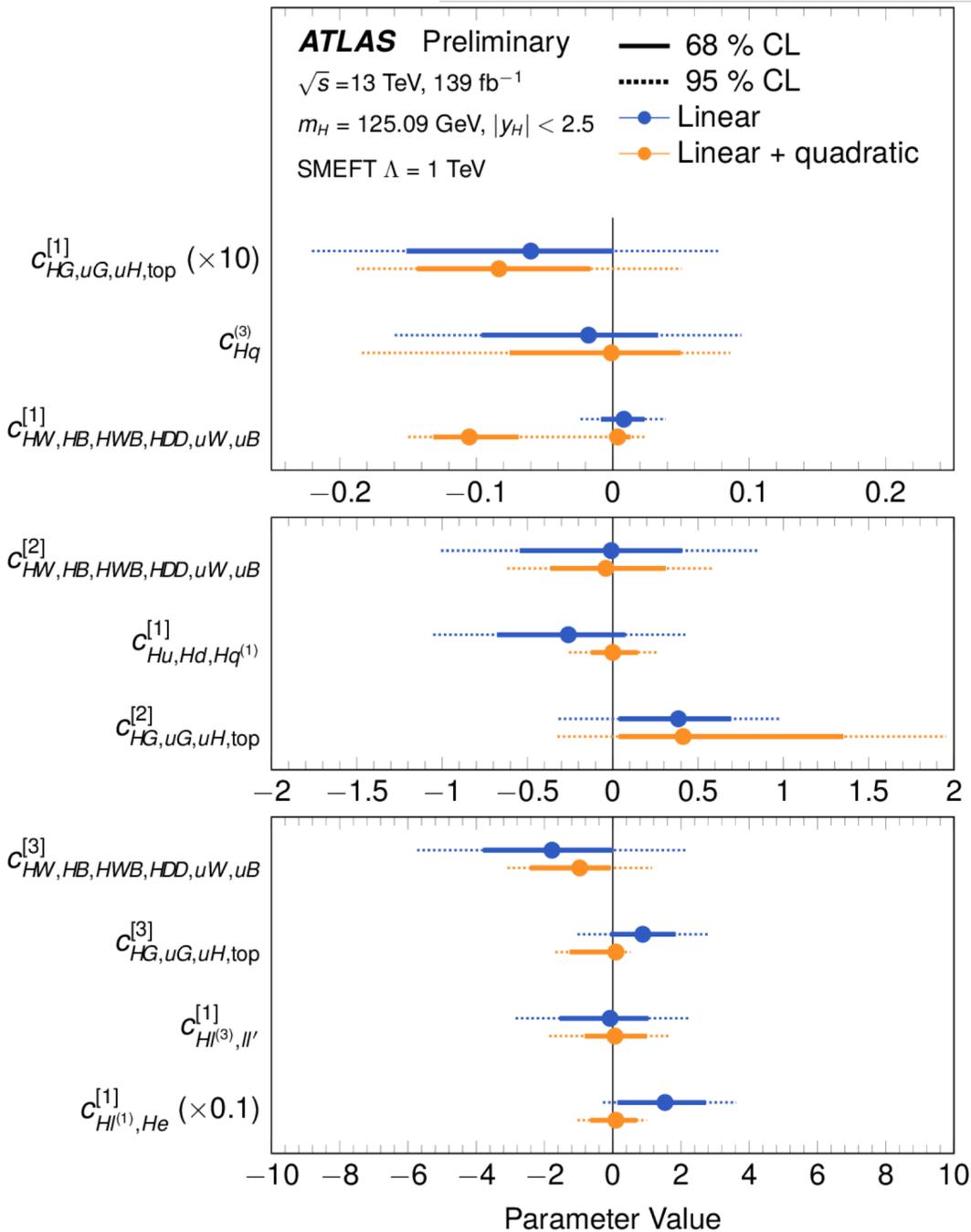
- To reduce the dimensionality of the fit a PCA is performed using the covariance matrix of the STXS measurement and propagating the EFT parametrisation
- Second PCA on sub-covariance matrices grouping operators affecting the same prod. mode or decay rates. Identify sensitive directions and neglect blind directions

$$\{c_i\} = \{c_{Hq}^{(3)}\} \times \{c_{HG}, c_{uG}, c_{uH}, c_{qq}^{(1)}, c_{qq}^{(3)}, c_{qq}^{(31)}, c_{uu}, c_{uu}^{(1)}, c_{ud}^{(8)}, c_{qu}^{(1)}, c_{qu}^{(8)}, c_{qd}^{(8)}, c_G\} \times \{c_{HW}, c_{HB}, c_{HWB}, c_{HDD}, c_{uW}, c_{uB}\} \times \{c_{HI}^{(1)}, c_{He}\} \times \{c_{HI}^{(3)}, c'_{II}\} \times \{c_{Hu}, c_{Hd}, c_{Hq}^{(1)}\}$$

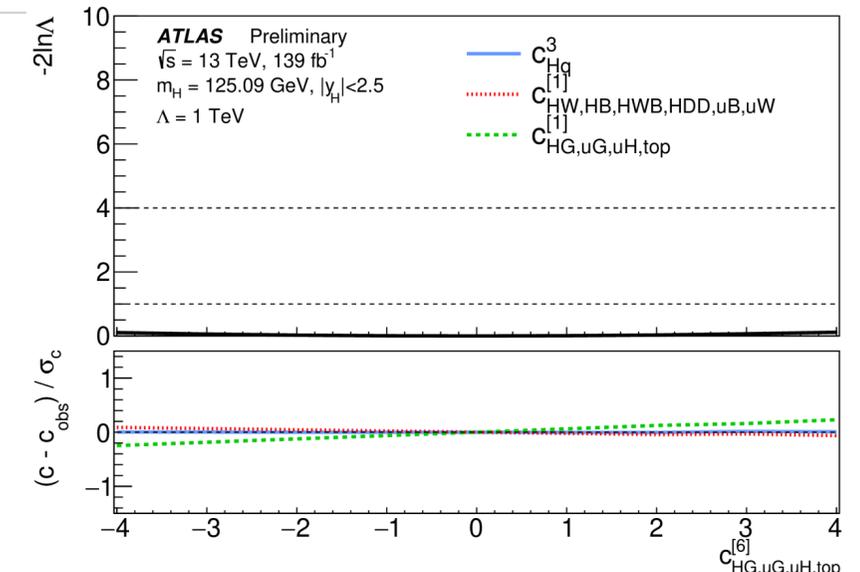
ATLAS Preliminary  $\sqrt{s} = 13 \text{ TeV}, 139 \text{ fb}^{-1}$



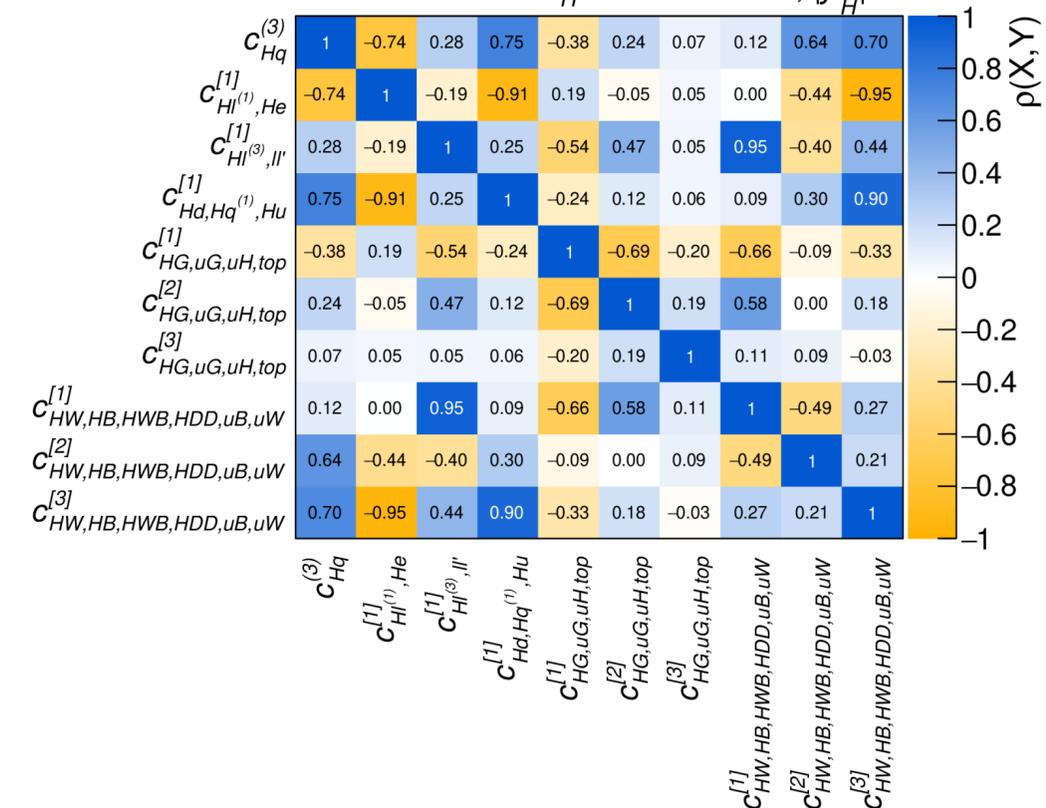
# Higgs combination (ATLAS)



- ❖ Very good sensitivity to the 10 fitted POI
- ❖ Quadratic terms relevant when constrained from low stat bins.
- ❖ Insensitivity to neglected direction and negligible impact on fitted POIs checked
- ❖ No reduction of “experimental” correlations (exact EVs not fitted) but checked to be linear



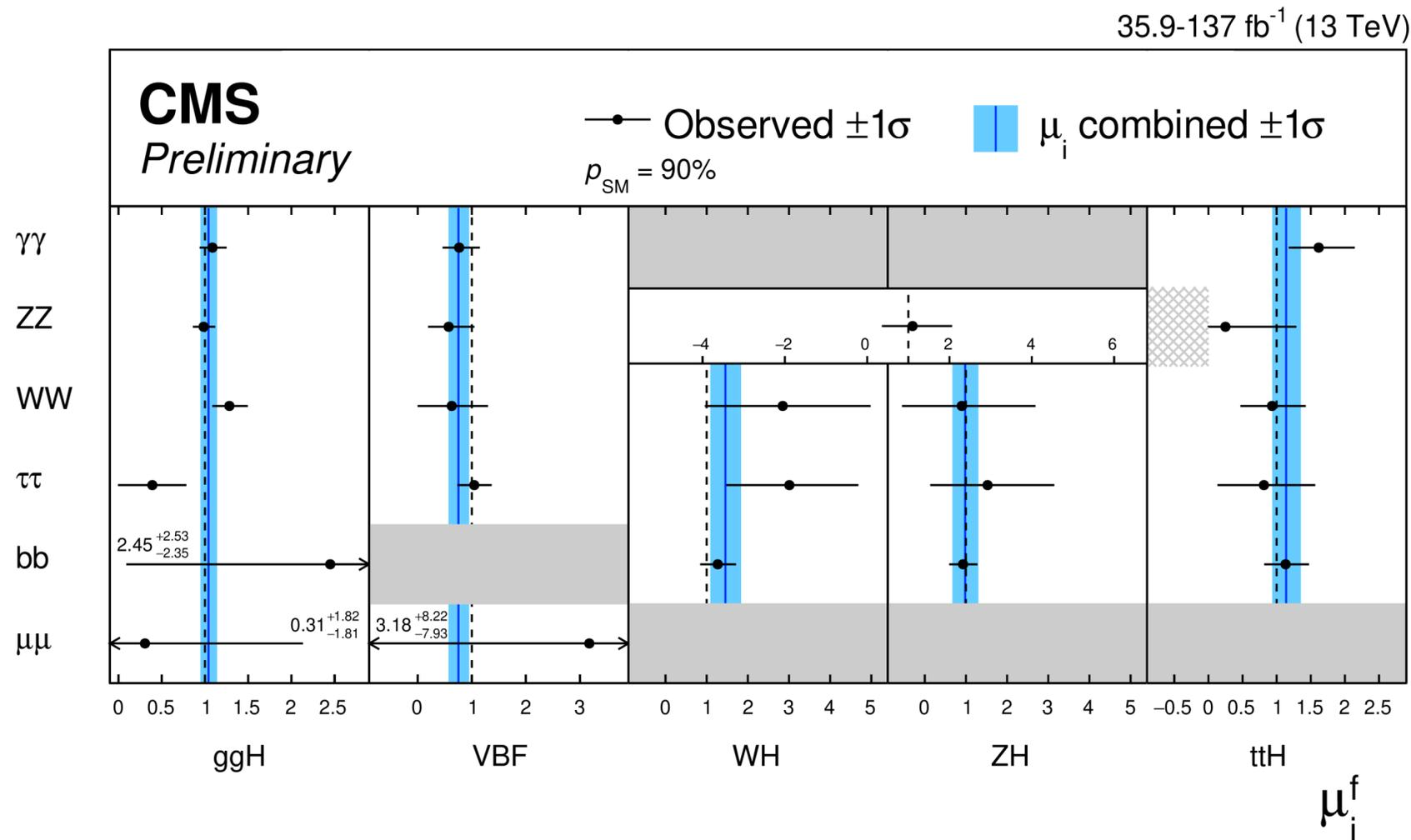
**ATLAS Preliminary**  $\sqrt{s} = 13 \text{ TeV}, 139 \text{ fb}^{-1}$   
 $m_H = 125.09 \text{ GeV}, |y_H| < 2.5$



# Higgs combination (CMS)

CMS-PAS-HIG-19-005

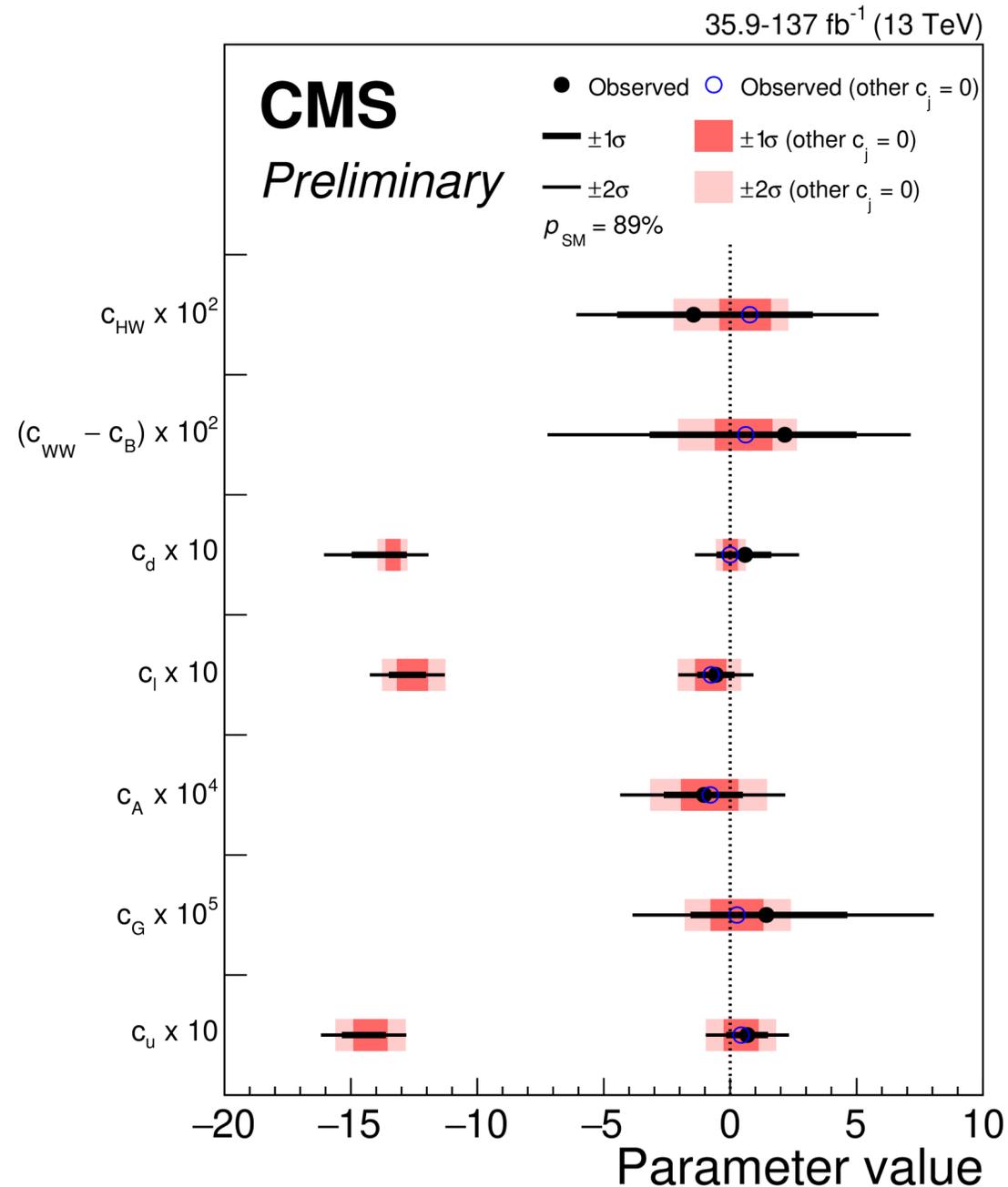
- ❖ Combined measurements of the production and decay rates of the Higgs boson and its couplings to vector bosons and fermions:  $H \rightarrow \gamma\gamma$ ,  $H \rightarrow bb$ ,  $H \rightarrow ZZ^* \rightarrow 4l$ ,  $H \rightarrow \tau\tau$ ,  $H \rightarrow WW^* \rightarrow l\nu l\nu$ ,  $ttH$ -multilepton (up to  $137 \text{ fb}^{-1}$ )



- ❖ Interpretation in the HEL Lagrangian
  - At LO. Using stage 0, 1.0 or 1.1 depending on the input channel
- ❖ Signal strength values reparametrized in terms of EFT coefficients.
- ❖  $ggZH$ ,  $bbH$  and  $tH$  fixed to SM
- ❖ Only CP-even terms not tightly constrained by other data considered
- ❖ Acceptance effects not taken into account

# Higgs combination (CMS)

CMS-PAS-HIG-19-005



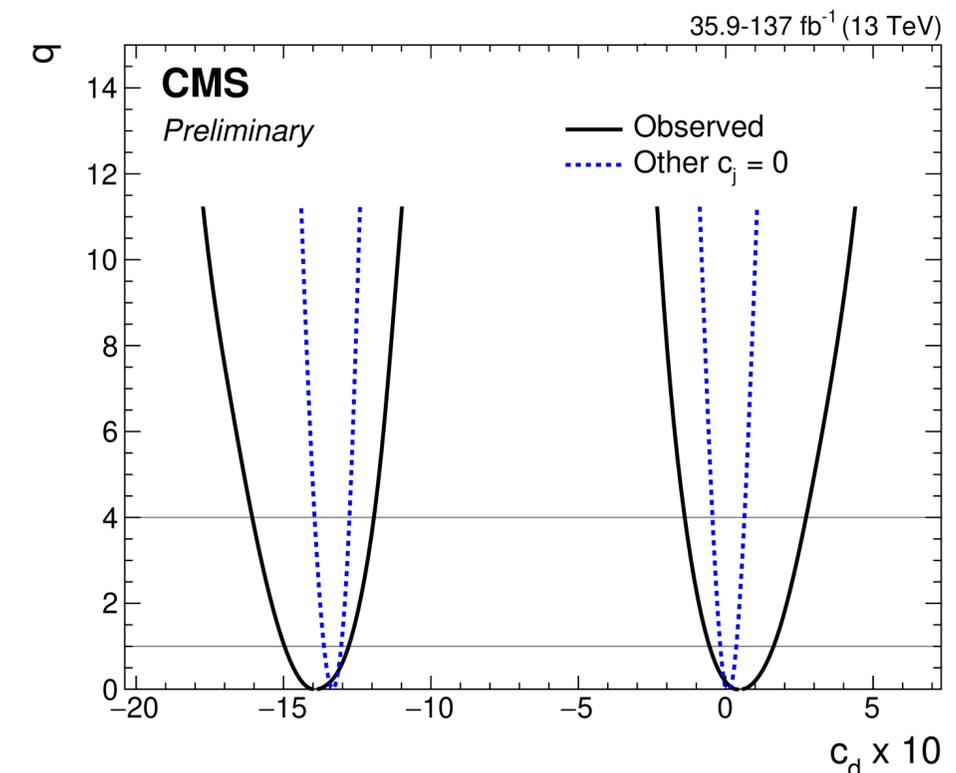
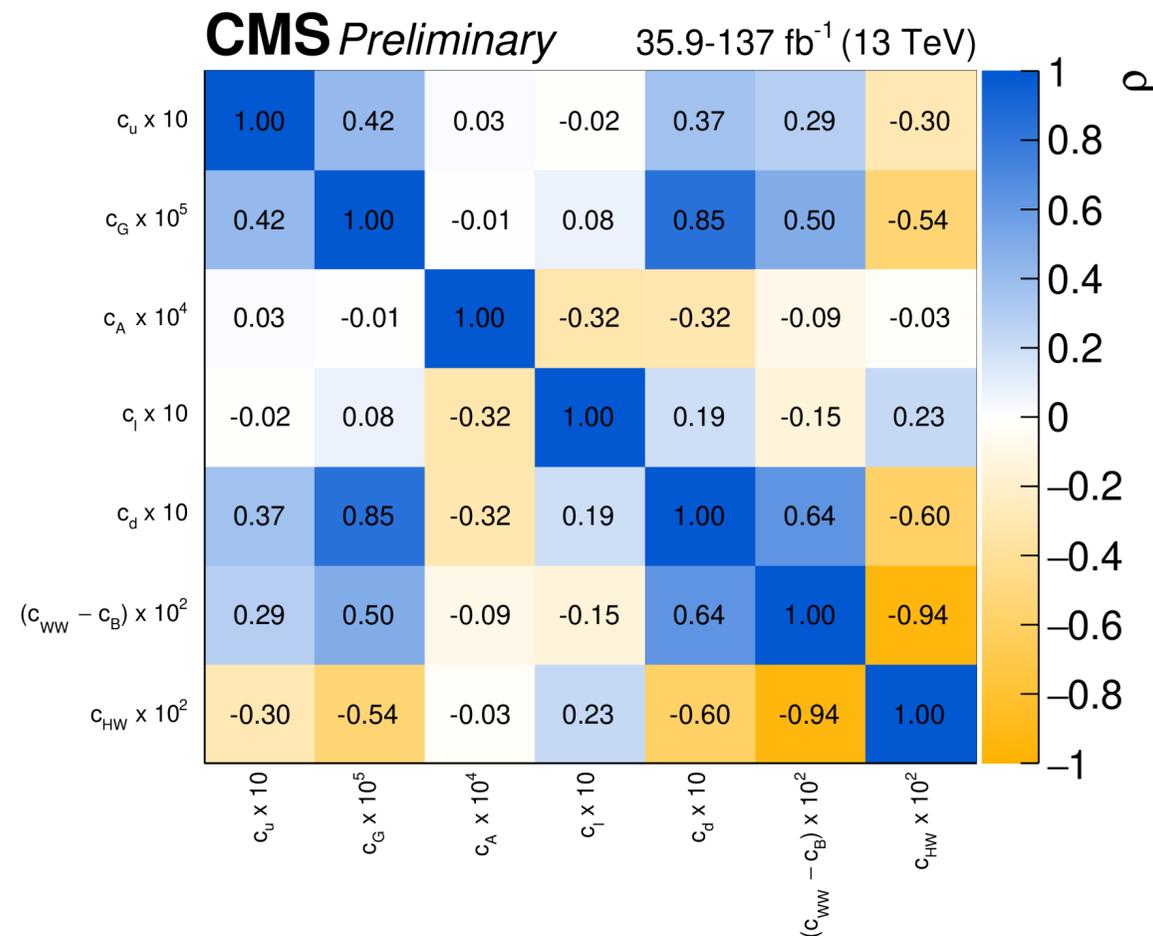
HEL Parameters	Definition	Others profiled	Fix others to SM
c <sub>A</sub> × 10 <sup>4</sup>	$c_A = \frac{m_W^2 f_A}{g'^2 \Lambda^2}$	-1.03 <sup>+1.53</sup> <sub>-1.59</sub> (+1.59) (-1.56)	-0.78 <sup>+1.11</sup> <sub>-1.16</sub> (+1.10) (-1.11)
c <sub>G</sub> × 10 <sup>5</sup>	$c_G = \frac{m_W^2 f_G}{g_s^2 \Lambda^2}$	1.43 <sup>+3.20</sup> <sub>-3.00</sub> (+3.13) (-2.74)	0.27 <sup>+1.05</sup> <sub>-1.05</sub> (+1.03) (-1.01)
c <sub>u</sub> × 10	$c_u = -v^2 \frac{f_u}{\Lambda^2}$	0.68 <sup>+0.82</sup> <sub>-0.83</sub> (+0.83) (-0.79)	0.43 <sup>+0.69</sup> <sub>-0.69</sub> (+0.68) (-0.67)
c <sub>d</sub> × 10	$c_d = -v^2 \frac{f_d}{\Lambda^2}$	0.59 <sup>+1.03</sup> <sub>-1.13</sub> (+1.08) (-1.05)	-0.01 <sup>+0.31</sup> <sub>-0.28</sub> (+0.30) (-0.28)
c <sub>l</sub> × 10	$c_l = -v^2 \frac{f_l}{\Lambda^2}$	-0.57 <sup>+0.74</sup> <sub>-0.73</sub> (+0.72) (-0.77)	-0.75 <sup>+0.60</sup> <sub>-0.64</sub> (+0.58) (-0.60)
c <sub>HW</sub> × 10 <sup>2</sup>	$c_{HW} = \frac{m_W^2 f_{HW}}{2g \Lambda^2}$	-1.45 <sup>+4.72</sup> <sub>-3.03</sub> (+3.93) (-3.27)	0.77 <sup>+0.84</sup> <sub>-1.20</sub> (+1.04) (-1.38)
(c <sub>WW</sub> - c <sub>B</sub> ) × 10 <sup>2</sup>	$c_{WW} = \frac{m_W^2 f_{WW}}{g \Lambda^2}, c_B = \frac{2m_W^2 f_B}{g' \Lambda^2}$	2.16 <sup>+2.84</sup> <sub>-5.35</sub> (+3.46) (-5.00)	0.62 <sup>+1.06</sup> <sub>-1.22</sub> (+1.09) (-1.23)

- ❖ Limits from simultaneous fit to HEL parameters
  - ▶ Very good sensitivity
  - ▶ Showed the relevance of simultaneous fits vs. 1-D fits setting other parameters to SM

# Higgs combination (CMS)

CMS-PAS-HIG-19-005

- ❖ Large correlations in operators affecting HV vertices and between cG and several operators
  - ▶ Limited information about the VH production in the input channels
  - ▶ ggH only affected by cG with small dependence on the STXS bin; overall increase in ggH difficult to disentangle from overall increase in the Higgs width
- ❖ Degeneracy on parameters constraint by decay rates (e.g cd in  $H \rightarrow bb$ ); could be solved adding bbH



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# Summary

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- ❖ SMEFT interpretations taking over kappa-framework interpretations of Higgs properties measurements as precision increase
  - ▶ No deviation from the SM observed
- ❖ Single analysis useful for specific studies
  - ▶ Differences in experimental acceptance in the EFT
  - ▶ Usefulness of further splittings at high transverse momentum of the Higgs.
- ❖ Analysis combination allow to constrain simultaneously several operators
- ❖ Methodologies not yet harmonised between experiments
- ❖ Ultimate goal: global EFT fits from the experimental community with Higgs, SM and top data

THANKS!

BACK UP

# Warsaw basis

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_\varphi$	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_W$	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

Table 2: Dimension-six operators other than the four-fermion ones.

# SILH basis

$$\Delta\mathcal{L}^{(6)} = \Delta\mathcal{L}_{\text{SILH}} + \Delta\mathcal{L}_{cc} + \Delta\mathcal{L}_{\text{dipole}} + \Delta\mathcal{L}_V + \Delta\mathcal{L}_{4\psi}$$

16 operators  
(12 CP even, 4 CP odd)

SILH operators

Giudice, Grojean, Pomarol, Rattazzi JHEP 0706 (2007) 045

$$\begin{aligned} \Delta\mathcal{L}_{\text{SILH}} = & \frac{\bar{c}_H}{2v^2} \partial^\mu (H^\dagger H) \partial_\mu (H^\dagger H) + \frac{\bar{c}_T}{2v^2} (H^\dagger \overleftrightarrow{D}^\mu H) (H^\dagger \overleftrightarrow{D}_\mu H) - \frac{\bar{c}_6 \lambda}{v^2} (H^\dagger H)^3 \\ & + \left( \frac{\bar{c}_u}{v^2} y_u H^\dagger H \bar{q}_L H^c u_R + \frac{\bar{c}_d}{v^2} y_d H^\dagger H \bar{q}_L H d_R + \frac{\bar{c}_l}{v^2} y_l H^\dagger H \bar{L}_L H l_R + h.c. \right) \\ & + \frac{i\bar{c}_W g}{2m_W^2} (H^\dagger \sigma^i \overleftrightarrow{D}^\mu H) (D^\nu W_{\mu\nu})^i + \frac{i\bar{c}_B g'}{2m_W^2} (H^\dagger \overleftrightarrow{D}^\mu H) (\partial^\nu B_{\mu\nu}) \\ & + \frac{i\bar{c}_{HW} g}{m_W^2} (D^\mu H)^\dagger \sigma^i (D^\nu H) W_{\mu\nu}^i + \frac{i\bar{c}_{HB} g'}{m_W^2} (D^\mu H)^\dagger (D^\nu H) B_{\mu\nu} \\ & + \frac{\bar{c}_\gamma g'^2}{m_W^2} H^\dagger H B_{\mu\nu} B^{\mu\nu} + \frac{\bar{c}_g g_S^2}{m_W^2} H^\dagger H G_{\mu\nu}^a G^{a\mu\nu} \\ & + \frac{i\bar{c}_{HW} g}{m_W^2} (D^\mu H)^\dagger \sigma^i (D^\nu H) \tilde{W}_{\mu\nu}^i + \frac{i\bar{c}_{HB} g'}{m_W^2} (D^\mu H)^\dagger (D^\nu H) \tilde{B}_{\mu\nu} \\ & + \frac{\bar{c}_\gamma g'^2}{m_W^2} H^\dagger H B_{\mu\nu} \tilde{B}^{\mu\nu} + \frac{\bar{c}_g g_S^2}{m_W^2} H^\dagger H G_{\mu\nu}^a \tilde{G}^{a\mu\nu} \end{aligned}$$

Bosonic CP-even		Bosonic CP-odd	
$O_H$	$\frac{1}{2v^2} [\partial_\mu (H^\dagger H)]^2$		
$O_T$	$\frac{1}{2v^2} (H^\dagger \overleftrightarrow{D}_\mu H)^2$		
$O_6$	$-\frac{\lambda}{v^2} (H^\dagger H)^3$		
$O_g$	$\frac{g_s^2}{m_W^2} H^\dagger H G_{\mu\nu}^a G_{\mu\nu}^a$	$\tilde{O}_g$	$\frac{g_s^2}{m_W^2} H^\dagger H \tilde{G}_{\mu\nu}^a G_{\mu\nu}^a$
$O_\gamma$	$\frac{g'^2}{m_W^2} H^\dagger H B_{\mu\nu} B_{\mu\nu}$	$\tilde{O}_\gamma$	$\frac{g'^2}{m_W^2} H^\dagger H \tilde{B}_{\mu\nu} B_{\mu\nu}$
$O_W$	$\frac{ig}{2m_W^2} (H^\dagger \sigma^i \overleftrightarrow{D}_\mu H) D_\nu W_{\mu\nu}^i$		
$O_B$	$\frac{ig'}{2m_W^2} (H^\dagger \overleftrightarrow{D}_\mu H) \partial_\nu B_{\mu\nu}$		
$O_{HW}$	$\frac{ig}{m_W^2} (D_\mu H^\dagger \sigma^i D_\nu H) W_{\mu\nu}^i$	$\tilde{O}_{HW}$	$\frac{ig}{m_W^2} (D_\mu H^\dagger \sigma^i D_\nu H) \tilde{W}_{\mu\nu}^i$
$O_{HB}$	$\frac{ig'}{m_W^2} (D_\mu H^\dagger D_\nu H) B_{\mu\nu}$	$\tilde{O}_{HB}$	$\frac{ig'}{m_W^2} (D_\mu H^\dagger D_\nu H) \tilde{B}_{\mu\nu}$
$O_{2W}$	$\frac{1}{m_W^2} D_\mu W_{\mu\nu}^i D_\rho W_{\rho\nu}^i$		
$O_{2B}$	$\frac{1}{m_W^2} \partial_\mu B_{\mu\nu} \partial_\rho B_{\rho\nu}$		
$O_{2G}$	$\frac{1}{m_W^2} D_\mu G_{\mu\nu}^a D_\rho G_{\rho\nu}^a$		
$O_{3W}$	$\frac{g^3}{m_W^2} \epsilon^{ijk} W_{\mu\nu}^i W_{\nu\rho}^j W_{\rho\mu}^k$	$\tilde{O}_{3W}$	$\frac{g^3}{m_W^2} \epsilon^{ijk} \tilde{W}_{\mu\nu}^i W_{\nu\rho}^j W_{\rho\mu}^k$
$O_{3G}$	$\frac{g_s^3}{m_W^2} f^{abc} G_{\mu\nu}^a G_{\nu\rho}^b G_{\rho\mu}^c$	$\tilde{O}_{3G}$	$\frac{g_s^3}{m_W^2} f^{abc} \tilde{G}_{\mu\nu}^a G_{\nu\rho}^b G_{\rho\mu}^c$

Table 1: Bosonic  $D=6$  operators in the SILH basis.