

EPFL

Uniting low-scale leptogeneses

Juraj Klarić based on 2008.13771 in collaboration with M.E. Shaposhnikov and I. Timiryasov

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Some puzzles for physics beyond the Standard Model

The Baryon Asymmetry of the Universe



Neutrino masses





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The ν mass matrix

$$\mathcal{L} \supset rac{1}{2} egin{pmatrix} \overline{
u_L} & \overline{
u_R^c} \end{pmatrix} egin{pmatrix} 0 & m_D \ m_D^T & 0? \end{pmatrix} egin{pmatrix}
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u_R \end{pmatrix}$$

 $\cdot \nu_R$ are SM gauge singlets

Active neutrino masses

$$m_{\nu} = m_D?$$

[Minkowski 1977...]

¹"Everything not forbidden is compulsory." - Murray Gell-Mann

The ν mass matrix

$$\mathcal{L} \supset \frac{1}{2} \begin{pmatrix} \overline{\nu_L} & \overline{\nu_R^c} \end{pmatrix} \begin{pmatrix} 0 & m_D \\ m_D^T & M_M \end{pmatrix} \begin{pmatrix} \nu_L^c \\ \nu_R \end{pmatrix}$$

- $\cdot \nu_R$ are SM gauge singlets
- $m_D = vF$ and M_M ¹are free parameters
- minimal scenario:
 2 right-handed neutrinos (RHN)

Active neutrino masses

$$m_{\nu} = -m_D M_M^{-1} m_D^T$$

[Minkowski 1977...]



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How can we search for heavy neutrinos?



Baryogenesis through leptogenesis

Sakharov conditions

- 1. Baryon number violation
 - realized in the SM through sphaleron processes for $T\gtrsim 130~{\rm GeV}$ [D'Onofrio/Rummukainen/Tranberg 1404.3565]
- 2. C and CP violation
- 3. Deviation from thermal equilibrium
 - RHN freeze-in and freeze-out



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Leptogenesis mechanisms



- several leptogenesis mechanisms exist for different masses
- for hierarchical RHN $(M_1 \ll M_2 \ll M_3)$ the Davidson-Ibarra bound applies with:

 $M_1 \gtrsim 10^9 GeV$

Loopholes:

- \cdot Resonant leptogenesis $M_M\gtrsim\,{
 m TeV}$
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Are these mechanisms connected?

Resonant leptogenesis

- the BAU is mainly produced in RHN decays
- The lepton asymmetries follow the equation

$$\frac{dY_{\ell_a}}{dz} = -\epsilon_a \frac{\Gamma_N}{Hz} (Y_N - Y_N^{\text{eq}}) - W_{ab} Y_{\ell_b}$$



The key quantity determining the BAU is the decay asymmetry

$$\epsilon_a \equiv \frac{\Gamma_{N \to l_a} - \Gamma_{N \to \bar{l}_a}}{\Gamma_{N \to l_a} + \Gamma_{N \to \bar{l}_a}} = \frac{1}{8\pi} \frac{\mathrm{Im}(F^{\dagger}F)_{12}^2}{(F^{\dagger}F)_{11}} \frac{M_1 M_2}{M_1^2 - M_2^2}$$

Becomes enhanced if $M_2
ightarrow M_1$ [Kuzmin 1970 (baryogenesis);(leptogenesis:)

Liu/Segrè/Flanz/Paschos/Sarkar/Weiss/Covi/Roulet/Vissani/Pilaftsis/Underwood/Buchmüller/Plumacher...]

This enhancement is known as resonant leptogenesis.

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This enhancement is known as resonant leptogenesis.

- divergent when $M_2 = M_1$?
- · divergence is unphysical it needs to be regulated!

Resonant leptogenesis and RHN oscillations

• in the degenerate limit perturbation theory breaks down

- to resolve this we need to go beyond the S-matrix formalism, RHN are unstable particles \rightarrow no asymptotic states!
- another way of describing the same process is to use density matrix equations (derived from the *Schwinger-Kelydish* formalism)

RHN density matrix $rac{\mathrm{d} ho}{\mathrm{d}z} = -i\left[H, ho ight] - rac{1}{2}\left\{\Gamma, ho-n^{\mathrm{eq}} ight\}$

Active lepton equations

$$\frac{\mathrm{d}Y_{\ell}}{\mathrm{d}z} = \mathrm{Tr}\left[\tilde{\Gamma}(\rho - \rho^*)\right] - WY_{\ell}$$

Resonant leptogenesis - summary

- \cdot resonant leptogenesis allows RHN below $10^9 \, {
 m GeV}$
- we run into conceptual problems for $M_2 \rightarrow M_1$
- these issues can be resolved with non-perturbative methods
 - resonant leptogenesis can be described through RHN oscillations

Issues:

- existing studies typically assume non-relativistic RHN and neglect relativistic effects
- non-thermal initial conditions still require solving the full density matrix equations
- + RHN decays require $M\gtrsim T \to {\rm not}$ clear what happens for $M\lesssim 130\,{\rm GeV}$

Leptogenesis via oscillations



Evolution Equations

System of kinetic equations

$$\begin{split} &i\frac{dn_{\Delta\alpha}}{dt} = -2i\frac{\mu\alpha}{T}\int\frac{d^3k}{(2\pi)^3}\operatorname{Tr}\left[\Gamma_{\alpha}\right]f_N\left(1-f_N\right) + i\int\frac{d^3k}{(2\pi)^3}\operatorname{Tr}\left[\tilde{\Gamma}_{\alpha}\left(\bar{\rho}_N-\rho_N\right)\right],\\ &i\frac{d\rho_N}{dt} = \left[H_N,\rho_N\right] - \frac{i}{2}\left\{\Gamma,\rho_N-\rho_N^{eq}\right\} - \frac{i}{2}\sum_{\alpha}\tilde{\Gamma}_{\alpha}\left[2\frac{\mu\alpha}{T}f_N\left(1-f_N\right)\right],\\ &i\frac{d\bar{\rho}_N}{dt} = -\left[H_N,\bar{\rho}_N\right] - \frac{i}{2}\left\{\Gamma,\bar{\rho}_N-\rho_N^{eq}\right\} + \frac{i}{2}\sum_{\alpha}\tilde{\Gamma}_{\alpha}\left[2\frac{\mu\alpha}{T}f_N\left(1-f_N\right)\right], \end{split}$$

- equations very similar to those used for resonant leptogenesis
- notably there are twice as many equations for the RHN \to helicity taken into account $(\rho_N\,,\rho_{\bar N})$
- temperature dependence of the equilibrium distributions often neglected

Compared to resonant leptogenesis, there exist a few important differences:

- initial conditions are crucial, all BAU is generated during RHN equilibration
- it is important to distinguish between the helicities of the RHN, as it carries an approximately conserved lepton number
- the decay of the RHN equilibrium distribution can typically be neglected $\dot{Y_N^{\rm eq}}\approx 0$

The parameter space of low-scale leptogenesis



Inverted Ordering

[Drewes/Garbrecht/Gueter/JK 1609.09069]

- several systematic studies over the past years
- leptogenesis is within reach of future experiments
- most studies stop around $\mathcal{O}(50) \, \mathrm{GeV}$
- why is this?

The parameter space of low-scale leptogenesis



[Eijima/Shaposhnikov/Timiryasov 1808.10833] [Boiarska

et. al. 1902.04535]

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What lies beyond $\mathcal{O}(50)$ GeV?

- for $M_M > M_W$ new channels open up in low-scale leptogenesis
 - large equilibration rates for both FNV and FNC processes
 - generically we have $\Gamma_N/H \gtrsim 30$ for $T \sim 150$ GeV, $M \sim 80$ GeV
 - we should never underestimate large exponents $Y_L \sim e^{-t\Gamma_N/H} \times Y_L^{\text{init}}$
 - early estimate [Blondel/Graverini/Serra/Shaposhnikov 2014]



Baryogenesis window closes at $M_M \sim 80~{
m GeV}?$

- $\cdot\,$ there is no established lower bound from resonant leptogenesis
 - early estimates gave successful leptogenesis for $\mathcal{O}(200)\,{
 m GeV}$ [Pilaftsis/Underwood 2005]
 - updated study suggests $\mathcal{O}(2)~{\rm GeV}~_{[{\rm Hambye/Teresi~2016}]}$ however: not completely consistent with results of leptogenesis via RHN oscillations

Study of the parameter space

- \cdot we use a single set of equations for both leptogeneses
 - $\cdot \,$ for $M \gg T$ we recover resonant leptogenesis
 - $\cdot\,$ for $M\ll T$ we recover leptogenesis via oscillations
- we separate the freeze-in and freeze-out regimes
 - for thermal initial conditions freeze-out is the only source of BAU: "resonant" leptogenesis dominates
 - for vanishing initial conditions with $Y_N^{\dot{e}q} \to 0$ freeze-in is the only source of BAU: LG via oscillations dominates
- biggest challenge: rates!
 - + so far estimates of the rates only exist for $M \ll T$ and $M \gg T$
 - we combine the two by *extrapolating* the relativistic rate and adding it to the non-relativistic decays
- we perform a comprehensive numerical scan over the parameters between $0.1 \text{GeV} < M_M < 10 \text{ TeV}$



- the baryogenesis window remains open!
- there is significant overlap the two mechanisms

- they are described by the same equations
- in resonant leptogenesis decays, *i.e.* freeze-out dominates, we can start with thermal initial conditions $Y_N(0) = Y_N^{eq}$
- · leptogenesis via oscillations is freeze-in dominated, $Y_N(0) = 0$, we set the "source" term to $Y_N^{\rm leq} \to 0$ by hand



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Conclusions

- resonant leptogenesis and leptogenesis through neutrino oscillations are really two realizations of the same mechanism
- freeze-out leptogenesis is already possible for GeV-scale heavy neutrinos
- freeze-in leptogenesis remains important at the TeV-scale and beyond
- leptogenesis is a viable baryogenesis mechanism for all heavy neutrino masses above the $\mathcal{O}(100)$ MeV scale
- leptogenesis is testable at planned future experiments
 - there is synergy between high-energy and high-intensity experiments!
 - together they will cover a large portion of the low-scale leptogenesis parameter space

Thank you!

Rates for leptogenesis

- \cdot one of the major challenges is to estimate the coefficients H_N and Γ_N
- unlike resonant leptogenesis, where it is often assumed that the rates are dominated by RHN decays, the main contribution comes from thermal effects

$$\prec$$
 \prec \prec \prec \prec \succ \succ \succ

[Ghiglieri/Laine 2017]

Two main types of rates:

Fermion number conserving

 $\Gamma_+ \sim F^2 T \sim H$

Fermion number violating

$$\Gamma_{-} \sim F^2 \frac{M^2}{T} \ll H$$

[Ghiglieri/Laine 2017, Eijima/Shaposhnikov 2017]

Slices of the parameter space



- slices of the parameter space for fixed M, $\operatorname{Re}\omega$ and phases in the PMNS matrix
- both mechanisms contribute at all masses
- large ΔM region is highly sensitive to initial conditions
- \cdot freeze-out leptogenesis requires small mass splitting $\Delta M/M \lesssim 10^{-8}$

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RHN searches at the Intensity Frontier

Example of an IF experiment: SHiP



• RHN can be produced in D and B meson decays

[Gorbunov/Shaposhnikov 2007]

- GeV-scale RHN are very long lived—they decay into charged particles in the vacuum vessel
- SHiP can be very sensitive to HNLs [SHiP collaboration 2018]