

# Global Fits of Dirac Dark Matter Effective Field Theories

**Ankit Beniwal**

(On behalf of the GAMBIT Collaboration)

P. Athron et al., *Thermal WIMPs and the Scale of New Physics: Global Fits of Dirac Dark Matter Effective Field Theories*, EPJC 81 (2021) 11, 992, [arXiv:[2106.02056](https://arxiv.org/abs/2106.02056)]



**14th International Conference on  
Identification of Dark Matter**

18-22 July 2022  
Vienna, Austria



- 1 Global fits and GAMBIT
- 2 Dirac fermion DM EFTs
- 3 Constraints and likelihoods
- 4 Results
- 5 Summary

Theories with *many* free parameters/constraints?

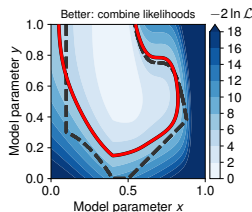
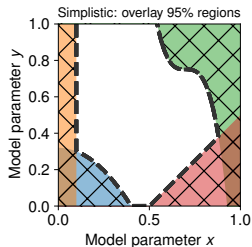
- 1 Construct a *composite likelihood* function:

$$\mathcal{L}_{\text{total}} = \mathcal{L}_{\text{DD}} \times \mathcal{L}_{\text{ID}} \times \mathcal{L}_{\text{Collider}} \times \dots$$

- 2 Traditional sampling methods (random, grid) are inefficient.
- 3 Explore parameter space using *advanced* sampling techniques (e.g., MCMC, nested sampling).
- 4 Interpret results in *frequentist* and/or *Bayesian* statistical frameworks.

→ GAMBIT

S. S. AbdusSalam et al., [arXiv:2012.09874]



## GAMBIT: The Global And Modular BSM Inference Tool

[gambit.hepforge.org](http://gambit.hepforge.org)

[github.com/GambitBSM](https://github.com/GambitBSM)

EPJC 77 (2017) 784

arXiv:1705.07908

- Extensive model database, beyond SUSY
- Fast definition of new datasets, theories
- Extensive observable/data libraries
- Plug&play scanning/physics/likelihood packages
- Various statistical options (frequentist /Bayesian)
- Fast LHC likelihood calculator
- Massively parallel
- Fully open-source



**Members of:** ATLAS, Belle-II, CLIC, CMS, CTA, Fermi-LAT, DARWIN, IceCube, LHCb, SHiP, XENON

**Authors of:** BubbleProfiler, Capt'n General, Contur, DarkAges, DarkSUSY, DDCalc, DirectDM, Diver, EasyScanHEP, ExoCLASS, FlexibleSUSY, gamLike, GM2Calc, HEPLike, IsaTools, MARTY, nuLike, PhaseTracer, PolyChord, Rivet, SOFTSUSY, SuperIso, SUSY-AI, xsec, Vevacious, WIMPSim

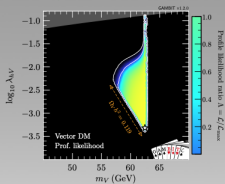
**Recent collaborators:** P Athron, C Balázs, A Beniwal, S Bloor, T Bringmann, A Buckley, J-E Camargo-Molina, C Chang, M Chrzaszcz, J Conrad, J Cornell, M Danninger, J Edsjö, T Emken, A Fowlie, T Gonzalo, W Handley, J Harz, S Hoof, F Kahlhoefer, A Kvellestad, P Jackson, D Jacob, C Lin, N Mahmoudi, G Martinez, MT Prim, A Raklev, C Rogan, R Ruiz, P Scott, N Serra, P Stöcker, W. Su, A Vincent, C Weniger, M White, Y Zhang, ++

70+ participants in many experiments and numerous major theory codes



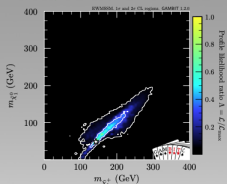
## Higgs-portal DM

[Eur.Phys.J.C 79 (2019) 1, 38]



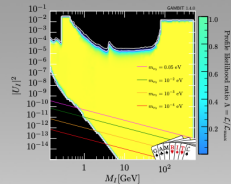
## MSSM-EW

[Eur.Phys.J.C 79 (2019) 5, 395]



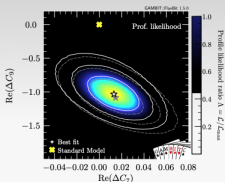
## Right-Handed Neutrinos

[Eur.Phys.J.C 80 (2020) 6, 569]



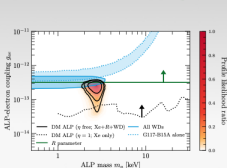
## Flavour EFT

[arXiv:2006.03489 hep-ph]



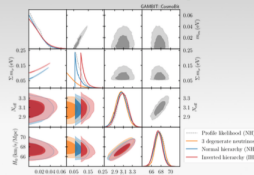
## DM ALPs

[arXiv:2007.05517 astro-ph.CO]



## Neutrino Masses

[arXiv:2009.03287 astro-ph.CO]



Slide from T. Gonzalo, Moriond 2021

- A Dirac fermion WIMP DM ( $\chi$ ) interacting with SM quarks or gluons via

$$\mathcal{L}_{\text{int}} = \sum_{a,d} \frac{C_a^{(d)}}{\Lambda^{d-4}} Q_a^{(d)}, \quad (1)$$

where  $C_a^{(d)}$  = dimensionless Wilson coefficients,  
 $\Lambda$  = scale of new physics,  $d \leq 7$  and  $Q_a^{(d)}$  =  
 DM-SM operators.

- Full Lagrangian is

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \mathcal{L}_{\text{int}} + \bar{\chi}(i\not{\partial} - m_\chi)\chi. \quad (2)$$

- Free model parameters:

$$6 \ (d = 6), \quad 16 \ (d = 6 \ \& \ 7).$$

$$\begin{aligned} Q_{1,q}^{(6)} &= (\bar{\chi}\gamma_\mu\chi)(\bar{q}\gamma^\mu q), \\ Q_{2,q}^{(6)} &= (\bar{\chi}\gamma_\mu\gamma_5\chi)(\bar{q}\gamma^\mu q), \\ Q_{3,q}^{(6)} &= (\bar{\chi}\gamma_\mu\chi)(\bar{q}\gamma^\mu\gamma_5 q), \\ Q_{4,q}^{(6)} &= (\bar{\chi}\gamma_\mu\gamma_5\chi)(\bar{q}\gamma^\mu\gamma_5 q). \end{aligned}$$

### Dimension-6 operators

$$\begin{aligned} Q_1^{(7)} &= \frac{\alpha_s}{12\pi} (\bar{\chi}\chi)G^{a\mu\nu}G_{\mu\nu}^a, \\ Q_2^{(7)} &= \frac{\alpha_s}{12\pi} (\bar{\chi}i\gamma_5\chi)G^{a\mu\nu}G_{\mu\nu}^a, \\ Q_3^{(7)} &= \frac{\alpha_s}{8\pi} (\bar{\chi}\chi)G^{a\mu\nu}\tilde{G}_{\mu\nu}^a, \\ Q_4^{(7)} &= \frac{\alpha_s}{8\pi} (\bar{\chi}i\gamma_5\chi)G^{a\mu\nu}\tilde{G}_{\mu\nu}^a, \\ Q_{5,q}^{(7)} &= m_q(\bar{\chi}\chi)(\bar{q}q), \\ Q_{6,q}^{(7)} &= m_q(\bar{\chi}i\gamma_5\chi)(\bar{q}q), \\ Q_{7,q}^{(7)} &= m_q(\bar{\chi}\chi)(\bar{q}i\gamma_5 q), \\ Q_{8,q}^{(7)} &= m_q(\bar{\chi}i\gamma_5\chi)(\bar{q}i\gamma_5 q), \\ Q_{9,q}^{(7)} &= m_q(\bar{\chi}\sigma^{\mu\nu}\chi)(\bar{q}\sigma_{\mu\nu} q), \\ Q_{10,q}^{(7)} &= m_q(\bar{\chi}i\sigma^{\mu\nu}\gamma_5\chi)(\bar{q}\sigma_{\mu\nu} q). \end{aligned}$$

### Dimension-7 operators



- **Mixing and threshold corrections:**

- For direct detection,  $C_a^{(d)}$ 's required at energy scale  $\mu = 2 \text{ GeV}$ ;
- Running/mixing of operators handled by DirectDM v2.2.0.

F. Bishara et al., [arXiv:1708.02678]; J. Brod et al., *JHEP*, [arXiv:1710.10218]

- Threshold corrections when  $\mu$  is below/above a quark mass, e.g.,  $m_t$ .

- **EFT validity:**

- ①  $\Lambda \gtrsim 2 \text{ GeV}$  (direct detection);
- ②  $\Lambda > 2m_\chi$  (relic density and indirect detection);
- ③  $E_T < \Lambda$  (collider searches). Modify  $E_T$  spectrum when  $E_T > \Lambda$ :

$$\frac{d\sigma}{dE_T} \rightarrow \begin{cases} 0, & \text{hard cut-off,} \\ \frac{d\sigma}{dE_T} \left(\frac{E_T}{\Lambda}\right)^{-a}, & \text{smooth cut-off.} \end{cases} \quad (3)$$

Here  $a \in [0, 4] =$  nuisance parameter.

- **Perturbative couplings:**  $|C_a^{(d)}| < 4\pi$ .
- **Parameter ranges:**  $m_\chi \in [5, 500] \text{ GeV}$  and  $\Lambda \in [20, 2000] \text{ GeV}$ .

## 1 Direct detection (DirectDM v2.2.0 & DDCalc v2.2.0)

XENON1T; LUX (2016); PandaX (2016) and (2017); CDMSlite; CRESST-II and CRESST-III; PICO-60 (2017) and (2019); DarkSide-50

F. Bishara et al., [arXiv:1708.02678]; J. Brod et al., *JHEP*, [arXiv:1710.10218]; P. Athron et al., *EPJC*, [arXiv:1808.10465]

## 2 Relic density (CalcHEP v3.6.27, GUM & DarkSUSY v6.2.2)

A. Belyaev et al., *CPC*, [arXiv:1207.6082]; S. Bloor et al., [arXiv:2107.00030]; T. Bringmann et al., *JCAP*, [arXiv:1802.03399]

## 3 Fermi-LAT via gamma rays (gamLike v1.0.1)

T. Bringmann et al., *EPJC*, [arXiv:1705.07920]

## 4 Solar capture (Capt'n General) and CMB bounds (CosmoBit)

N. Avis Kozar et al., arXiv:2105.06810; J. J. Renk et al., *JCAP*, [arXiv:2009.03286]

## 5 ATLAS and CMS monojet searches (ColliderBit, FeynRules v2.0,

MadGraph\_aMC@NLO v2.6.6, Pythia v8.1 & Delphes v3.4.2)

G. Aad et al., [arXiv:2102.10874]; A. M. Sirunyan et al., *PRD*, [arXiv:1712.02345]

C. Balazs et al., *EPJC*, [arXiv:1705.07919]; A. Alloul et al., *CPC*, [arXiv:1310.1921]

J. Alwall et al., *JHEP*, [arXiv:1106.0522]; T. Sjostrand et al., *CPC*, [arXiv:0710.3820]

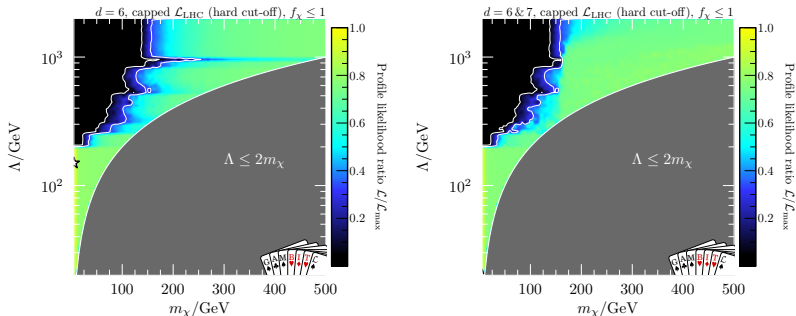
J. de Favereau et al., *JHEP*, [arXiv:1307.6346]

## + 8 nuisance parameters

Top-quark running mass, nuclear form factors, and astrophysical distribution of DM.



Capped  $\mathcal{L}_{\text{LHC}}$  likelihood (hard cut-off),  $f_\chi \equiv (\Omega_\chi + \Omega_{\bar{\chi}})/0.12 \leq 1$

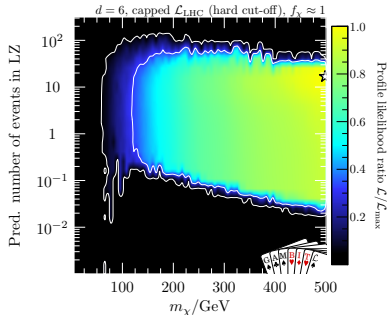
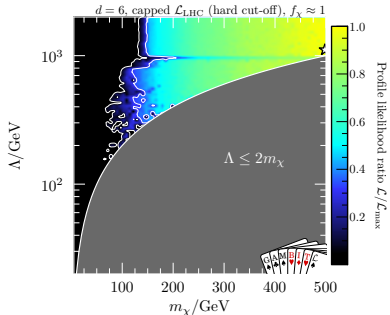


Left panel:  $d = 6$ ; Right panel:  $d = 6 \ \& \ 7$ ; White star = best-fit point.

- Small  $m_\chi$  and large  $\Lambda$ : strong constraints from LHC; impossible to satisfy relic density requirement. LHC constraints absent for  $\Lambda < 200$  GeV.
- Slight upward fluctuation in *Fermi*-LAT data fitted by (for  $d = 6$  case):

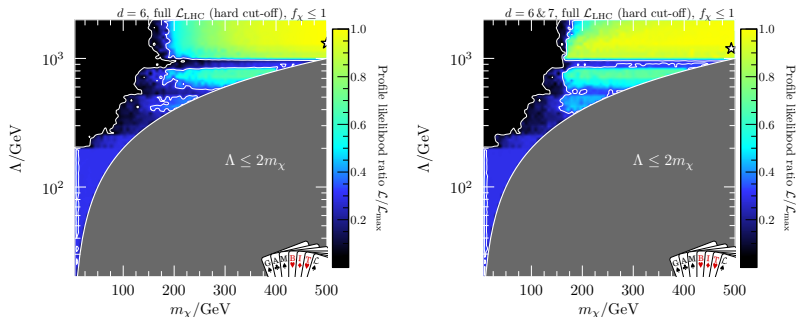
$$m_\chi = 5.0 \text{ GeV}, \quad f_\chi^2 \langle \sigma v \rangle_0 = 1.1 \times 10^{-27} \text{ cm}^3 \text{ s}^{-1}. \quad (4)$$

## Capped $\mathcal{L}_{\text{LHC}}$ likelihood (hard cut-off), $f_\chi \approx 1$



- Impossible to obtain  $\Omega_\chi h^2 = 0.12$  for  $m_\chi \lesssim 100 \text{ GeV}$ ; relic density requirement incompatible with *Fermi*-LAT and CMB bounds.
- Up to **10 events** predicted in LZ experiment  $\sim$  best-fit point  $\rightarrow$  require a non-zero  $Q_2^{(6)}$  (spin-independent, momentum-suppressed interaction).

## Full $\mathcal{L}_{\text{LHC}}$ likelihood (hard cut-off), $f_{\chi} \leq 1$

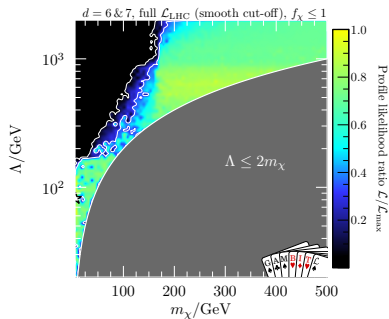
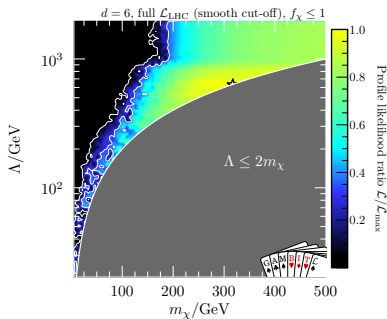


- For  $d = 6$ , excesses seen in few high- $\cancel{E}_T$  bins in the ATLAS & CMS monojet searches. Preferred values for  $\Lambda$  at  $1\sigma$  level:

$$\Lambda \approx 700 \text{ GeV (CMS)}, \quad \Lambda \gtrsim 1 \text{ TeV (ATLAS)}. \quad (5)$$

- Similar results for  $d = 6 \& 7$  (right panel).

## Full $\mathcal{L}_{\text{LHC}}$ likelihood (smooth cut-off), $f_\chi \leq 1$



- For  $d = 6$ , best-fit improves fit to both excesses (*Fermi*-LAT and LHC) simultaneously than in hard cut-off case (similar for  $d = 6 \& 7$ ).
- Requires  $\Lambda \sim 80$  GeV and soft cut-off  $a \approx 1.7$  in the  $\cancel{E}_T$  spectrum.

# Summary

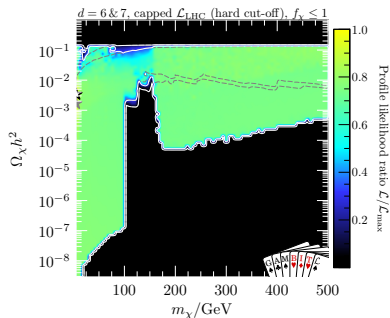
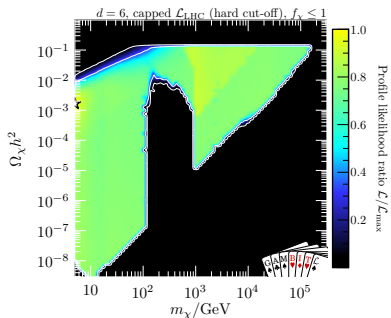
- First global analysis of full set of effective operators ( $d \leq 7$ ) for a Dirac fermion DM interaction with quarks/gluons.
- Novel approach addresses issue of EFT validity @ LHC via a cut-off parameter for  $E_T > \Lambda$ .
- Highly efficient likelihood calculations + sampling algorithms to sample 24 dimensions ( $m_\chi$ ,  $\Lambda$ ,  $14 \times C_a^{(d)} + 8$  nuisance parameters).
- Strong constraints on small  $m_\chi$  and large  $\Lambda \rightarrow$  slight preference for DM signal at relatively small  $\Lambda$ .
- Large hierarchy **not possible** between  $m_\chi$  and  $\Lambda$  without violating the relic density constraint.
- LHC constraints require  $\Lambda \lesssim 200$  GeV for  $m_\chi \lesssim 100$  GeV.
- Large viable regions of parameter space for  $f_\chi \lesssim 1$ .

All results, samples + input files publicly available via Zenodo:

<https://zenodo.org/record/4836397>

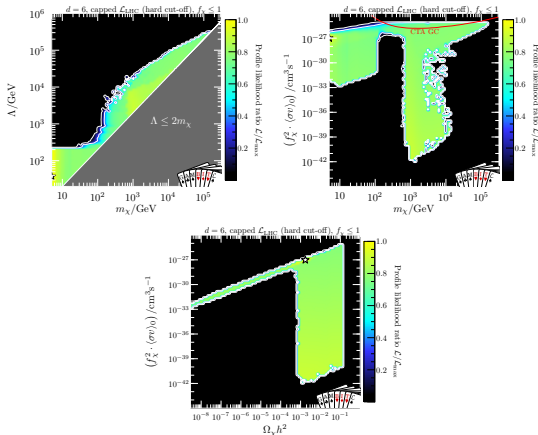
# Backup slides

## Capped $\mathcal{L}_{\text{LHC}}$ likelihood (hard cut-off), $f_\chi \leq 1$



- For  $d = 6$  and  $m_\chi \lesssim 100$  GeV, impossible to obtain  $\Omega_\chi h^2 = 0.12$  with combined indirect and direct detection constraints.
- In  $d = 6 \& 7$ , now possible to saturate relic density bound for small  $m_\chi$  (and small  $\Lambda$ ) thanks to suppressed signals from  $Q_{3,q}^{(7)}$  and  $Q_{7,q}^{(7)}$ .

## Capped $\mathcal{L}_{\text{LHC}}$ likelihood (hard cut-off), $f_\chi \leq 1$

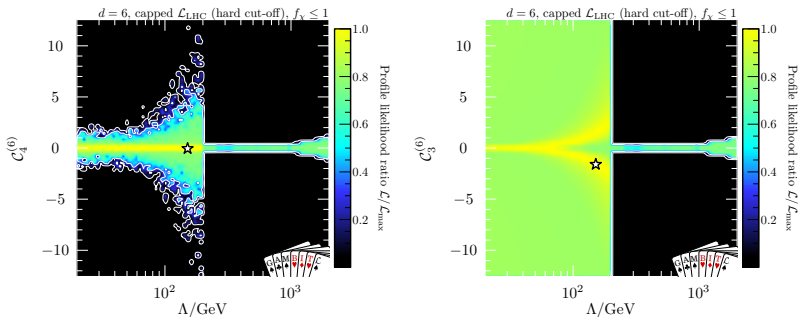


Left panel:  $(m_\chi, \Lambda)$  plane. Right panel:  $(m_\chi, f_\chi^2 \langle\sigma v\rangle_0)$  plane.

Bottom panel:  $(\Omega_\chi h^2, f_\chi^2 \langle\sigma v\rangle_0)$  plane.

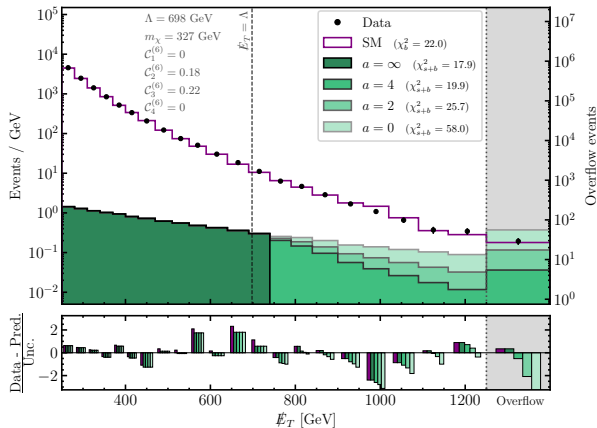


## Capped $\mathcal{L}_{\text{LHC}}$ likelihood (hard cut-off), $f_\chi \leq 1$



Left panel:  $(m_\chi, C_4^{(6)})$  plane. Right panel:  $(m_\chi, C_3^{(6)})$  plane.

# Supplementary results



**Top panel:** Examples of missing transverse energy ( $E_T$ ) spectrum for the CMS monojet search. **Bottom panel:** Pull ( $\equiv$  (data - predicted)/uncertainty) per bin.

- 1 **DarkBit** *EPJC*, [arXiv:1705.07920]  
Relic density, indirect and direct detection.
- 2 **SpecBit, DecayBit and PrecisionBit** *EPJC*, [arXiv:1705.07936]  
Spectrum calculation, decay widths and precision observables.
- 3 **FlavBit** *EPJC*, [arXiv:1705.07933]  
Flavour physics, observables and likelihoods.
- 4 **ColliderBit** *EPJC*, [arXiv:1705.07919]  
Collider observables and likelihoods.
- 5 **ScannerBit** *EPJC*, [arXiv:1705.07959]  
Module for scanners and printers
- 6 **NeutrinoBit** *EPJC*, [arXiv:1908.02302]  
Neutrino observables and likelihoods.
- 7 **CosmoBit** *JCAP*, [arXiv:2009.03286]  
Cosmological observables and likelihoods.

- Threshold corrections when energy scale  $\mu < m_q \rightarrow$  reduced degrees of freedom:

$$C_{i,q}^{(7)} = C_{i,q}^{(7)} - C_{i+4,q}^{(7)} \quad (i = 1, 2), \quad C_{j,q}^{(7)} = C_{j,q}^{(7)} + C_{j+4,q}^{(7)} \quad (j = 3, 4). \quad (6)$$

- Tensor operators  $Q_{9,q}^{(7)}$  and  $Q_{10,q}^{(7)}$  mix above EW scale  $\implies$  dim-5 dipole operators:

$$Q_1^{(5)} = \frac{e}{8\pi^2} (\bar{\chi} \sigma_{\mu\nu} \chi) F^{\mu\nu}, \quad Q_2^{(5)} = \frac{e}{8\pi^2} (\bar{\chi} i \sigma_{\mu\nu} \gamma_5 \chi) F^{\mu\nu}. \quad (7)$$

- For  $\Lambda > m_t$ ,  $Q_{9,10,t}^{(7)}$  gives a contribution to  $Q_{1,2}^{(5)}$  at one-loop level:

$$C_{1,2}^{(5)}(m_Z) = \frac{4m_t^2}{\Lambda^2} \log\left(\frac{m_Z^2}{\Lambda^2}\right) C_{9,10;t}^{(7)}(\Lambda). \quad (8)$$

- Axial-vector top-quark current  $Q_{3,t}^{(6)}$  mixes into operators  $Q_{1,q}^{(6)}$ :

$$C_{1,u/d}^{(6)}(m_Z) = C_{1,u/d}^{(6)}(\Lambda) + \frac{2s_w^2 \mp (3 - 6s_w^2)}{8\pi^2} \frac{m_t^2}{v^2} \log\left(\frac{m_Z^2}{\Lambda^2}\right) C_{3,t}^{(6)}(\Lambda).$$

- Collider process:  $pp \rightarrow \chi\chi j$  with missing transverse energy  $\cancel{E}_T$ .
- CMS and ATLAS monojet searches based on  $36 \text{ fb}^{-1}$  and  $139 \text{ fb}^{-1}$  of Run II data, respectively. G. Aad et al., [arXiv:2102.10874]; A. M. Sirunyan et al., PRD, [arXiv:1712.02345]
- Expected number of events in a given bin of  $\cancel{E}_T$  distribution:

$$N = L \times \sigma \times (\epsilon A). \quad (9)$$

- Produce separate interpolations of  $\sigma$  and  $(\epsilon A)$  based on output of MadGraph\_aMC@NLO, interfaced to Pythia.
- Matching between MadGraph and Pythia performed according to CKKW prescription, and detector response simulation using Delphes.
- Only  $\mathcal{C}_i^{(6)}$  and  $\mathcal{C}_{i=1,\dots,4}^{(7)}$  relevant for collider searches. Others suppressed by either PDFs (for heavy quarks) or mass term (for light quarks).
- Separate grids generated for operators that *do not* interfere. For  $d = 6$ , interference occurs between  $Q_{1,q}^{(6)}/Q_{4,q}^{(6)}$  and  $Q_{2,q}^{(6)}/Q_{3,q}^{(6)} \rightarrow$  parametrise tabulated grids by mixing angle  $\theta$  as  $\mathcal{C}_{1,2}^{(6)} = \sin \theta$  and  $\mathcal{C}_{3,4}^{(6)} = \cos \theta$ .

- 22 and 13 exclusive signal regions in CMS and ATLAS monojet analyses, respectively.
- For CMS analysis, combine all signals using publicly available information. For ATLAS, only a single signal region used at once  $\rightarrow$  maximise sensitivity by combining 3 highest  $\cancel{E}_T$  bins.
- For CMS analysis, we have

$$\mathcal{L}_{\text{CMS}}(\mathbf{s}, \boldsymbol{\gamma}) = \prod_{i=1}^{22} \left[ \frac{(s_i + b_i + \gamma_i)^{n_i} e^{-(s_i + b_i + \gamma_i)}}{n_i!} \right] \frac{1}{\sqrt{\det 2\pi \boldsymbol{\Sigma}}} e^{-\frac{1}{2} \boldsymbol{\gamma}^T \boldsymbol{\Sigma}^{-1} \boldsymbol{\gamma}}.$$

- Define profiled CMS likelihood ( $\mathcal{L}_{\text{CMS}}(\mathbf{s}) \equiv \mathcal{L}_{\text{CMS}}(\mathbf{s}, \hat{\boldsymbol{\gamma}})$ ) by profiling over 22 nuisance parameters in  $\boldsymbol{\gamma}$ .
- For ATLAS analysis,  $\mathcal{L}_{\text{ATLAS}}(s_i) \equiv \mathcal{L}_{\text{ATLAS}}(s_i, \hat{\boldsymbol{\gamma}}_i)$ , where  $i$  = signal region with best expected sensitivity (one with lowest likelihood when  $n_i = b_i$ ).
- Total LHC likelihood:  $\ln \mathcal{L}_{\text{LHC}} = \ln \mathcal{L}_{\text{CMS}} + \ln \mathcal{L}_{\text{ATLAS}}$ .

$$\Delta \ln \mathcal{L}_{\text{LHC}} = \ln \mathcal{L}_{\text{LHC}}(\mathbf{s}) - \ln \mathcal{L}_{\text{LHC}}(\mathbf{s} = \mathbf{0}), \quad (10)$$

$$\Delta \ln \mathcal{L}_{\text{LHC}}^{\text{cap}}(\mathbf{s}) = \min [\Delta \ln \mathcal{L}_{\text{LHC}}(\mathbf{s}), \Delta \ln \mathcal{L}_{\text{LHC}}(\mathbf{s} = \mathbf{0})]. \quad (11)$$

Nuisance parameter		Value ( $\pm 3\sigma$ range)
Local DM density	$\rho_0$	0.2–0.8 GeV cm <sup>-3</sup>
Most probable speed	$v_{\text{peak}}$	240 (24) km s <sup>-1</sup>
Galactic escape speed	$v_{\text{esc}}$	528 (75) km s <sup>-1</sup>
Running top mass ( $\overline{\text{MS}}$ scheme)	$m_t(m_t)$	162.9 (6.0) GeV
Pion-nucleon sigma term	$\sigma_{\pi N}$	50 (45) MeV
Strange quark contrib. to nucleon spin	$\Delta s$	-0.035 (0.027)
Strange quark nuclear tensor charge	$g_T^s$	-0.027 (0.048)
Strange quark charge radius of the proton	$r_s^2$	-0.115 (0.105) GeV <sup>-2</sup>

**Table 1:** List of nuisance parameters that are varied simultaneously with the DM EFT model parameters.

# Type of interactions

	SI scattering	SD scattering	Annihilations
<b>Dimension-6 operators</b>			
$\mathcal{Q}_{1,q}^{(6)} = (\bar{\chi}\gamma_{\mu}\chi)(\bar{q}\gamma^{\mu}q)$	unsuppressed	—	s-wave
$\mathcal{Q}_{2,q}^{(6)} = (\bar{\chi}\gamma_{\mu}\gamma_5\chi)(\bar{q}\gamma^{\mu}q)$	suppressed	—	p-wave
$\mathcal{Q}_{3,q}^{(6)} = (\bar{\chi}\gamma_{\mu}\chi)(\bar{q}\gamma^{\mu}\gamma_5q)$	—	suppressed	s-wave
$\mathcal{Q}_{4,q}^{(6)} = (\bar{\chi}\gamma_{\mu}\gamma_5\chi)(\bar{q}\gamma^{\mu}\gamma_5q)$	—	unsuppressed	s-wave $\propto m_q^2/m_{\chi}^2$
<b>Dimension-7 operators</b>			
$\mathcal{Q}_1^{(7)} = \frac{\alpha_s}{12\pi}(\bar{\chi}\chi)G^{a\mu\nu}G_{\mu\nu}^a$	unsuppressed	—	p-wave
$\mathcal{Q}_2^{(7)} = \frac{\alpha_s}{12\pi}(\bar{\chi}i\gamma_5\chi)G^{a\mu\nu}G_{\mu\nu}^a$	suppressed	—	s-wave
$\mathcal{Q}_3^{(7)} = \frac{\alpha_s}{8\pi}(\bar{\chi}\chi)G^{a\mu\nu}\tilde{G}_{\mu\nu}^a$	—	suppressed	p-wave
$\mathcal{Q}_4^{(7)} = \frac{\alpha_s}{8\pi}(\bar{\chi}i\gamma_5\chi)G^{a\mu\nu}\tilde{G}_{\mu\nu}^a$	—	suppressed	s-wave
$\mathcal{Q}_{5,q}^{(7)} = m_q(\bar{\chi}\chi)(\bar{q}q)$	unsuppressed	—	p-wave $\propto m_q^2/m_{\chi}^2$
$\mathcal{Q}_{6,q}^{(7)} = m_q(\bar{\chi}i\gamma_5\chi)(\bar{q}q)$	suppressed	—	s-wave $\propto m_q^2/m_{\chi}^2$
$\mathcal{Q}_{7,q}^{(7)} = m_q(\bar{\chi}\chi)(\bar{q}i\gamma_5q)$	—	suppressed	p-wave $\propto m_q^2/m_{\chi}^2$
$\mathcal{Q}_{8,q}^{(7)} = m_q(\bar{\chi}i\gamma_5\chi)(\bar{q}i\gamma_5q)$	—	suppressed	s-wave $\propto m_q^2/m_{\chi}^2$
$\mathcal{Q}_{9,q}^{(7)} = m_q(\bar{\chi}\sigma^{\mu\nu}\chi)(\bar{q}\sigma_{\mu\nu}q)$	loop-induced	unsuppressed	s-wave $\propto m_q^2/m_{\chi}^2$
$\mathcal{Q}_{10,q}^{(7)} = m_q(\bar{\chi}i\sigma^{\mu\nu}\gamma_5\chi)(\bar{q}\sigma_{\mu\nu}q)$	loop-induced	suppressed	s-wave $\propto m_q^2/m_{\chi}^2$

**Table 2:** Full list of dimension-6 and 7 operators included in our study, and the types of interactions they induce. Here SI (SD) = spin-independent (spin-dependent) DM-nucleon interaction.



# Best-fit points

LHC likelihood	Relic density constraint	$2\Delta \ln \mathcal{L}$	Best-fit $m_\chi$ (GeV)	Best-fit $\Lambda$ (GeV)	Best-fit constrained coupling combination(s) ( $\text{TeV}^{-2}$ )
Capped	Upper bound	0.3	5.0	$< 200$	$ C_3^{(6)} /\Lambda^2 = 67$
Capped	Saturated	-0.5	500	$> 1000$	$ C_2^{(6)} /\Lambda^2 = 0.22$ $ C_3^{(6)} /\Lambda^2 = 0.041$
Full (hard cut-off)	Upper bound	2.2	500	$> 1250$	$ C_3^{(6)} /\Lambda^2 = 0.14$
Full (smooth cut-off)	Upper bound	2.6	320	640	$ C_3^{(6)} /\Lambda^2 = 0.18$
Full (hard cut-off)	Saturated	1.9	500	$> 1250$	$ C_3^{(6)} /\Lambda^2 = 0.047$ $\sqrt{(C_2^{(6)})^2 + (C_4^{(6)})^2}/\Lambda^2 = 0.15$
Full (smooth cut-off)	Saturated	2.0	420	840	$ C_3^{(6)} /\Lambda^2 = 0.052$ $\sqrt{(C_2^{(6)})^2 + (C_4^{(6)})^2}/\Lambda^2 = 0.23$

**Table 3:** Best-fit points from our various scans involving dimension-6 operators with restricted parameter ranges ( $5 \text{ GeV} \leq m_\chi \leq 500 \text{ GeV}$  and  $20 \text{ GeV} \leq \Lambda \leq 2 \text{ TeV}$ ). Here we only quote the combination that is well-constrained rather than each parameter individually.