

Characterising DM substructures in strong lensing images with targeted simulation-based inference

Noemi Anau Montel

[Coogan et al. \(2020\)](#)

[Karchev et al. \(2021\)](#)

[NAM et al. \(2022\)](#)

and more very soon!



Adam Coogan



Camila Correa



Konstantin Karchev



Elias Dubbeldam

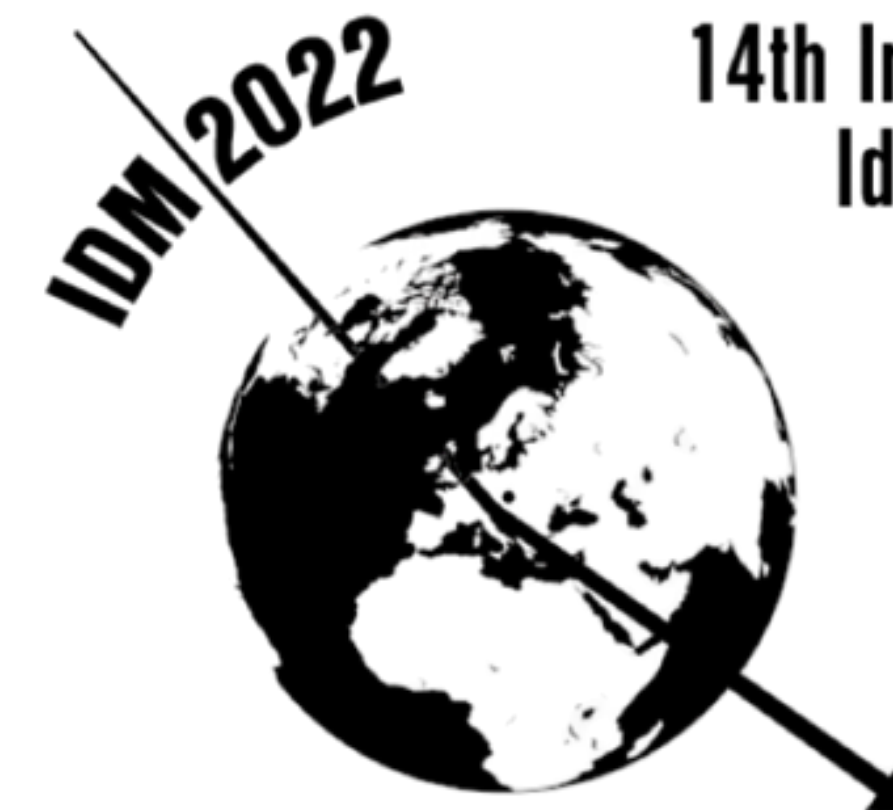


Christoph Weniger

with



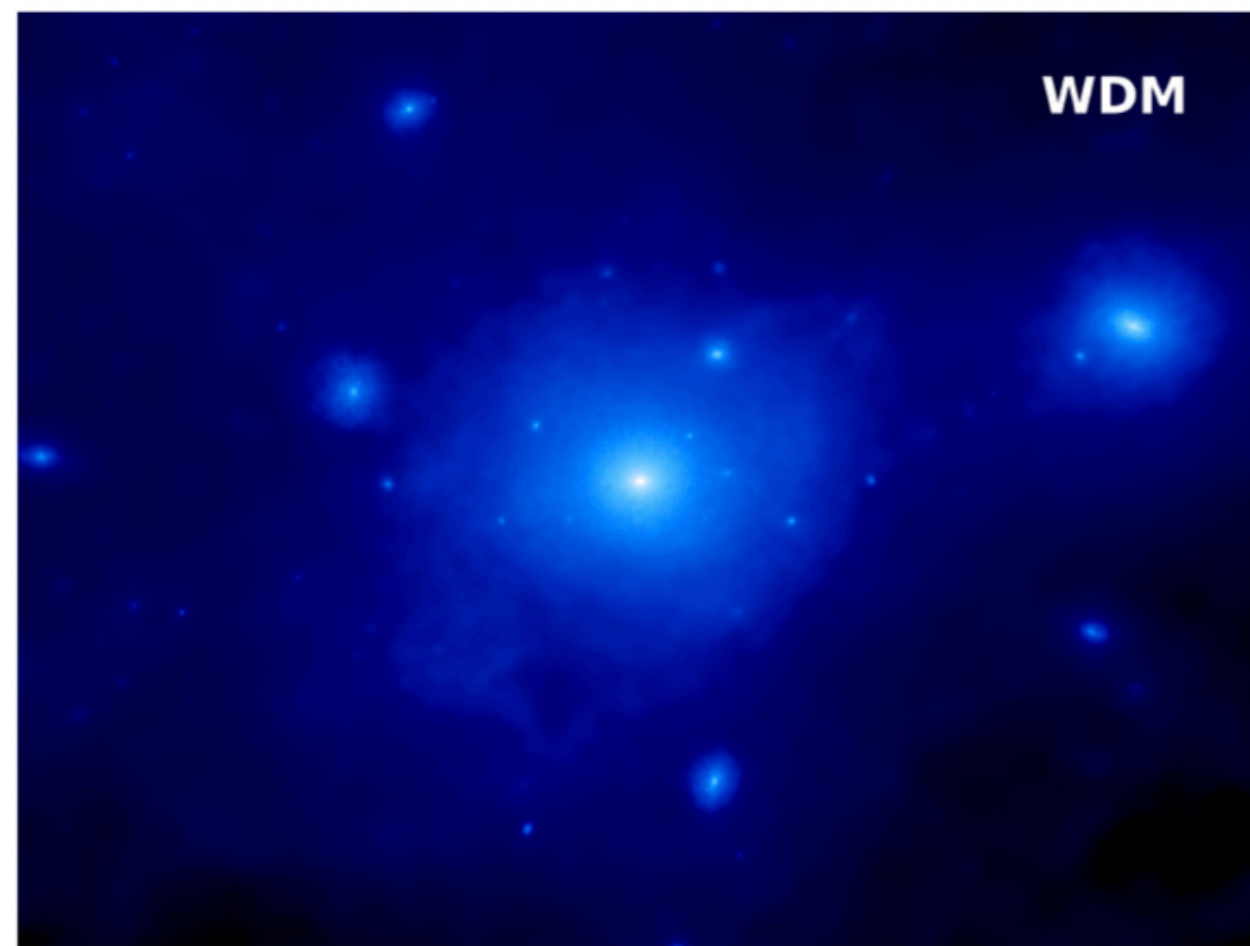
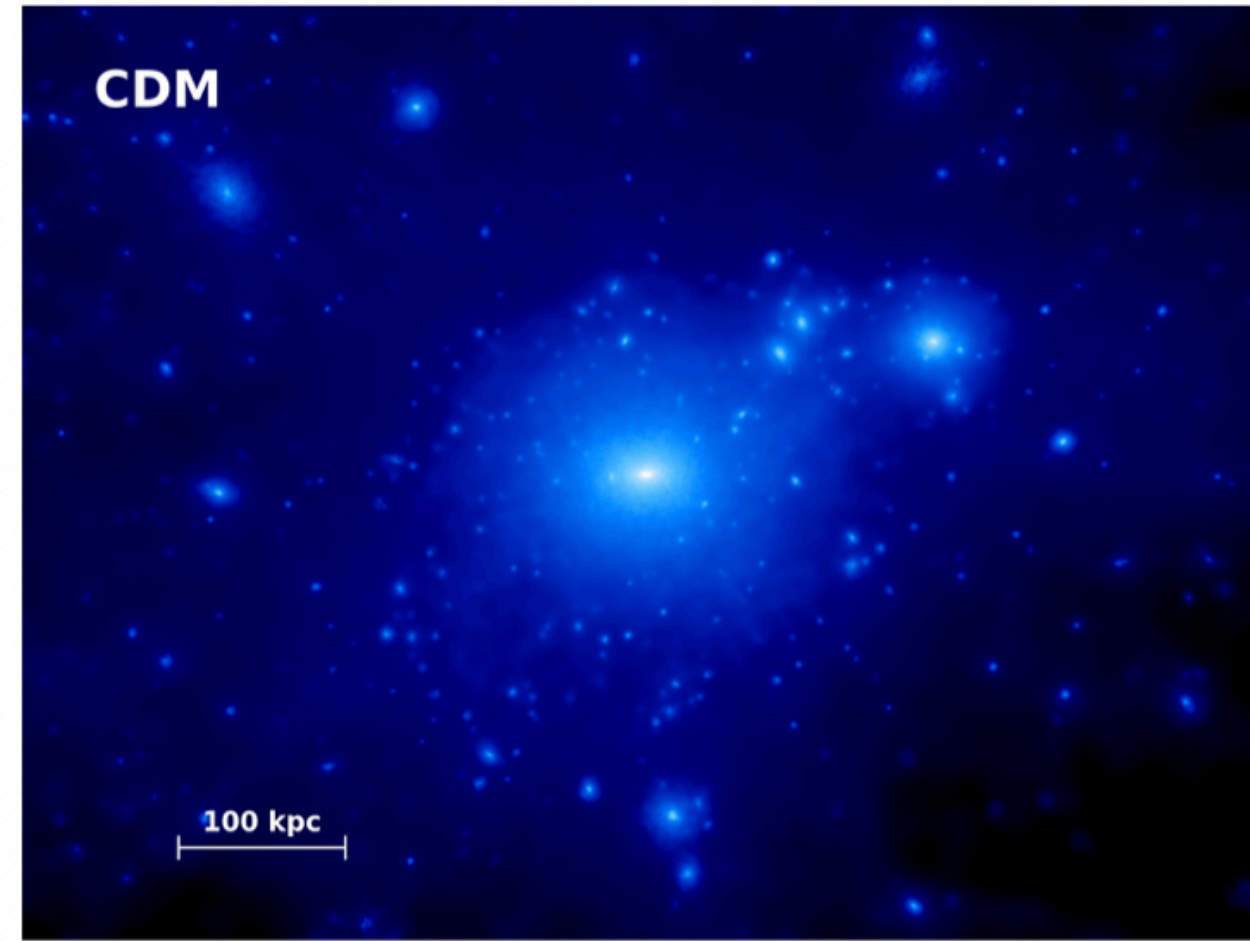
UNIVERSITY
OF AMSTERDAM



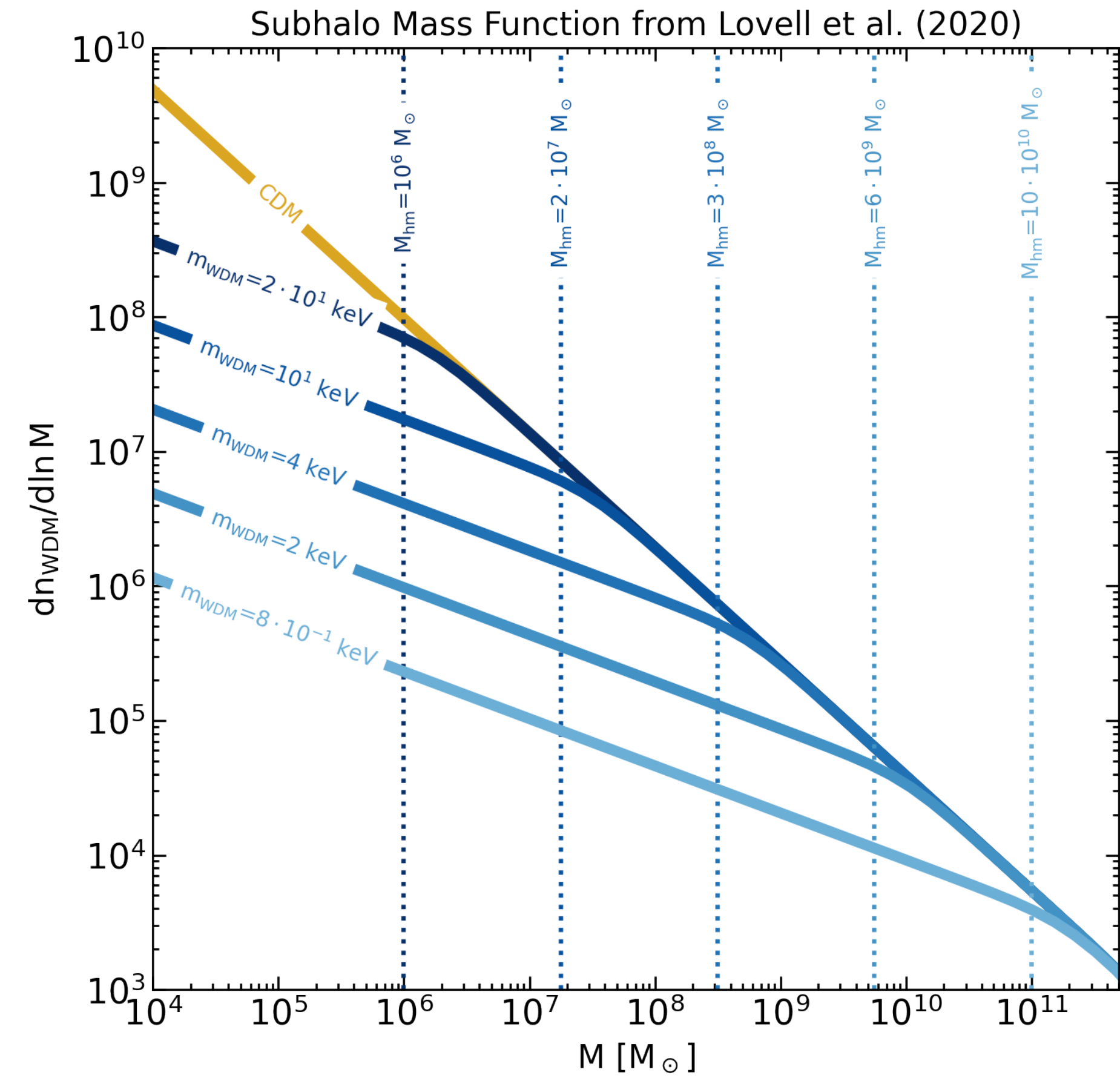
**14th International Conference on
Identification of Dark Matter**

**18-22 July 2022
Vienna, Austria**

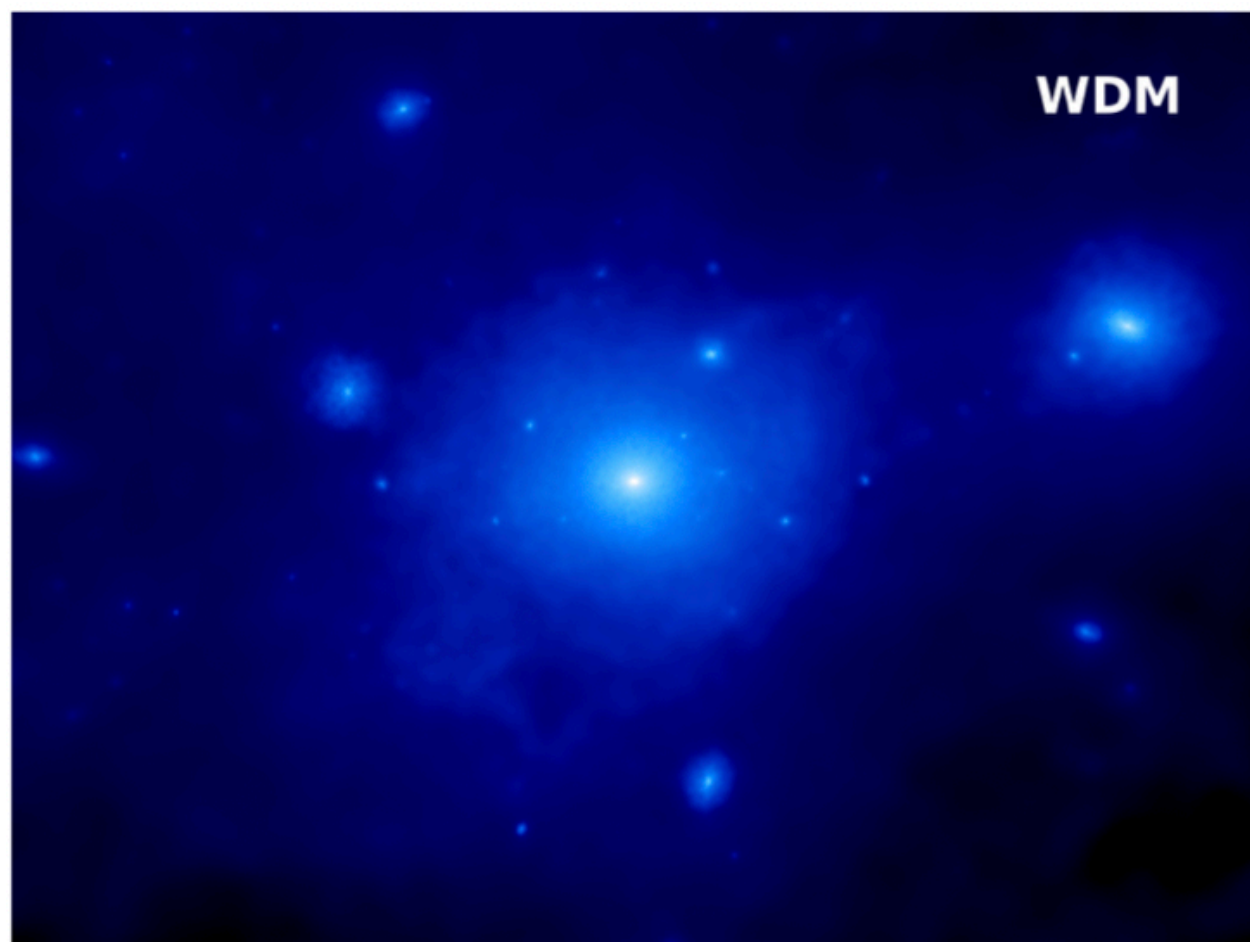
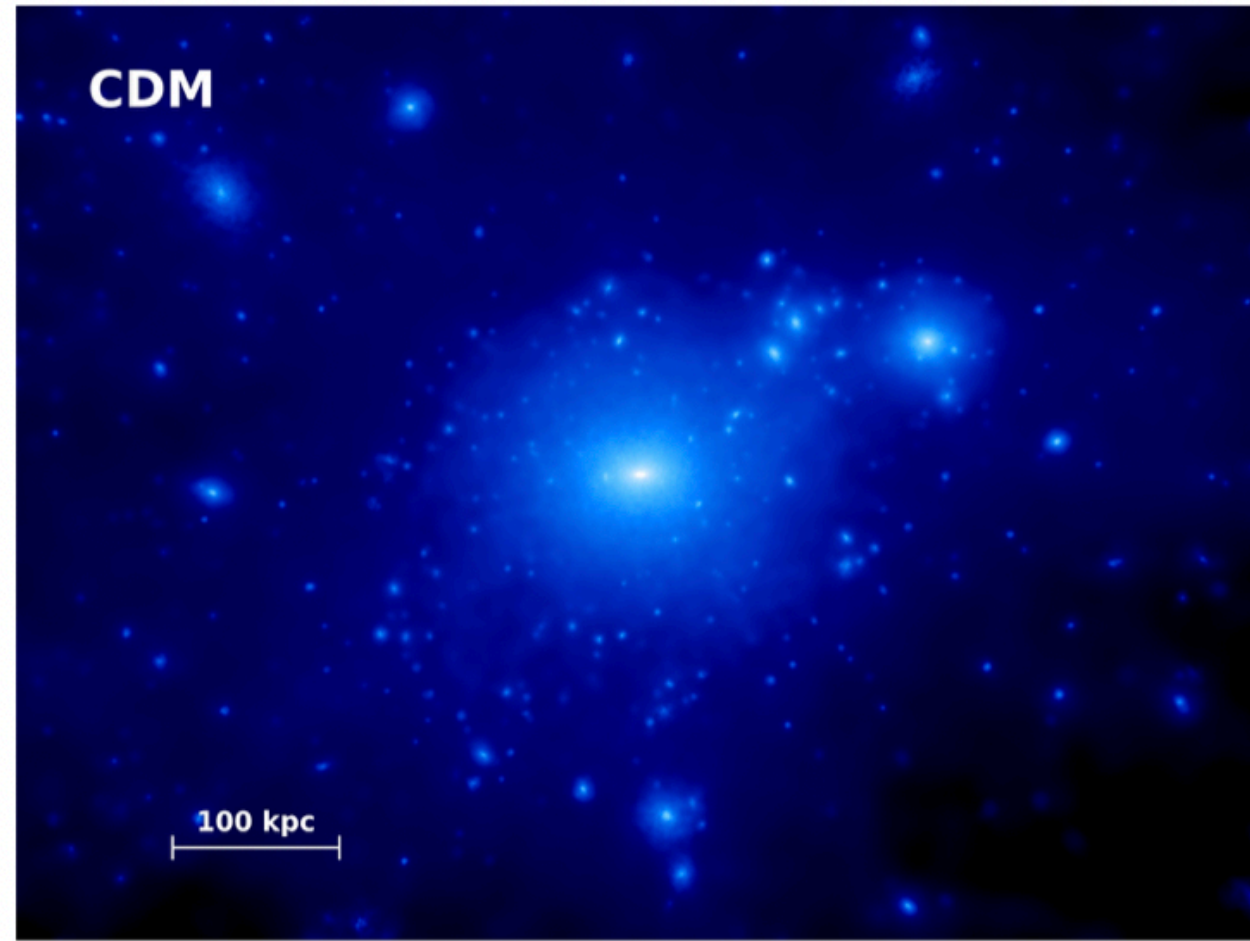
DM physics is encoded in the properties of DM halos



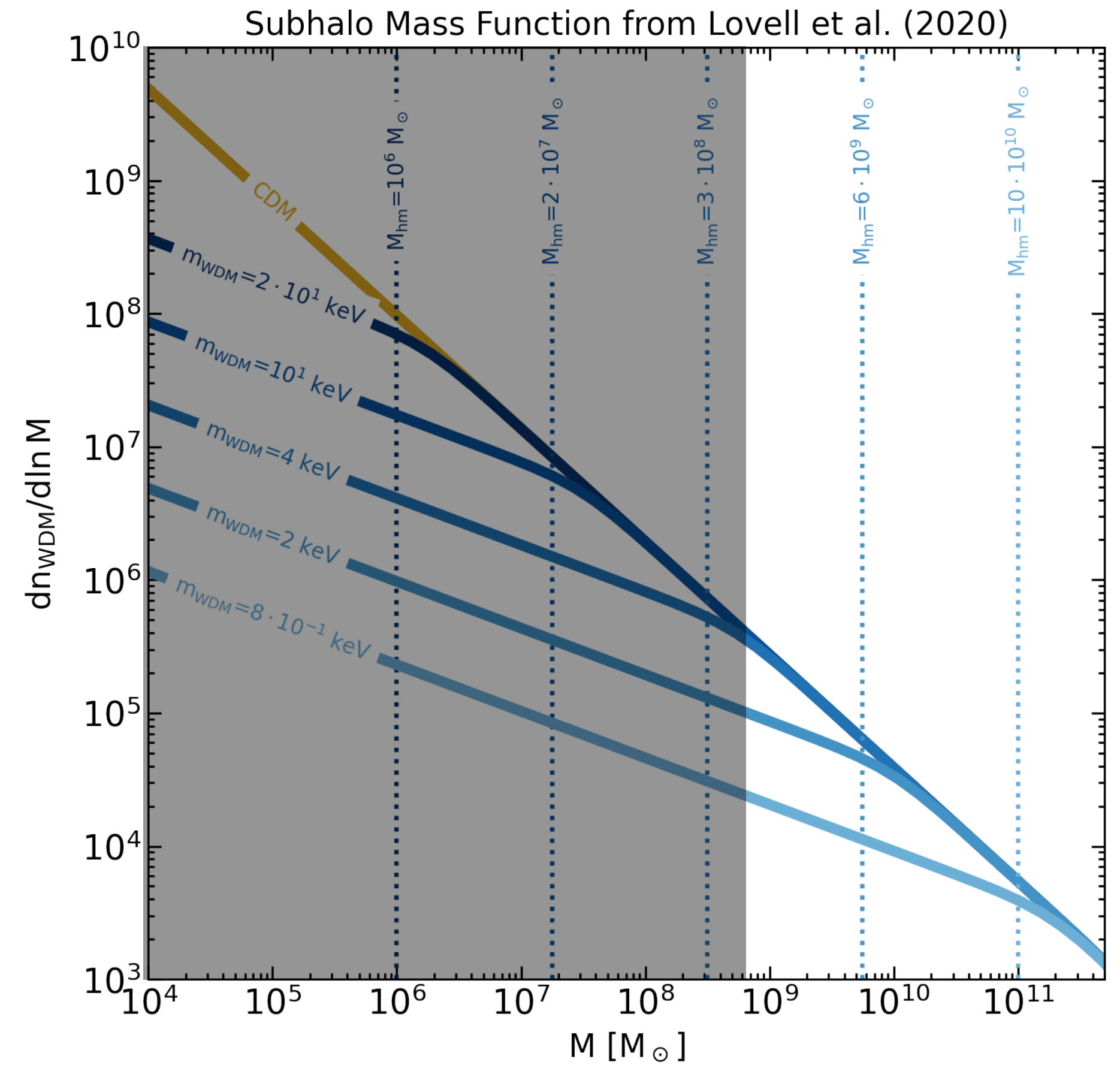
Boehm et al. (2014)



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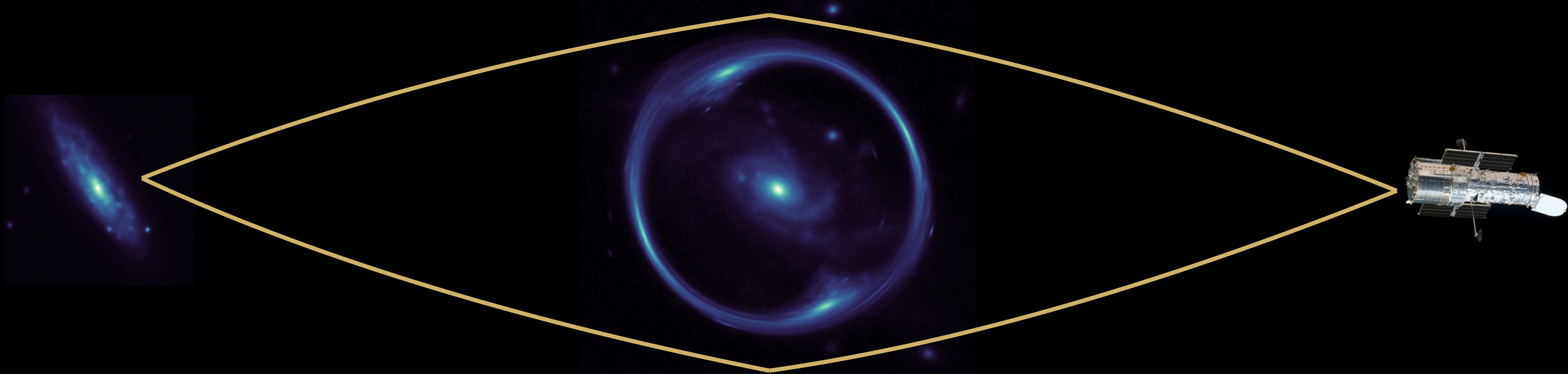
Boehm et al. (2014)



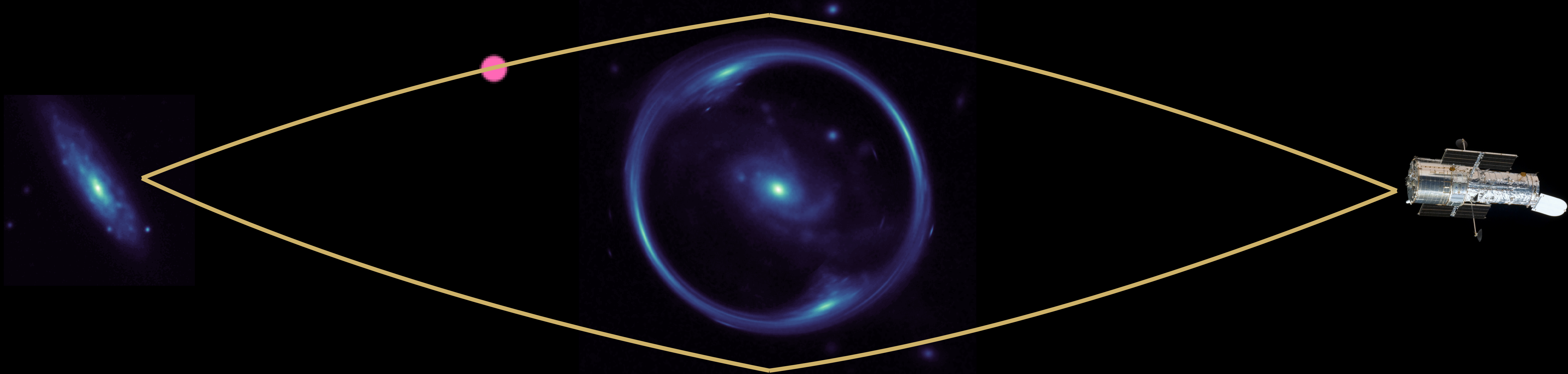
Dark region → use gravitational lensing

↓
As seen in Daniel Gilman's talk 

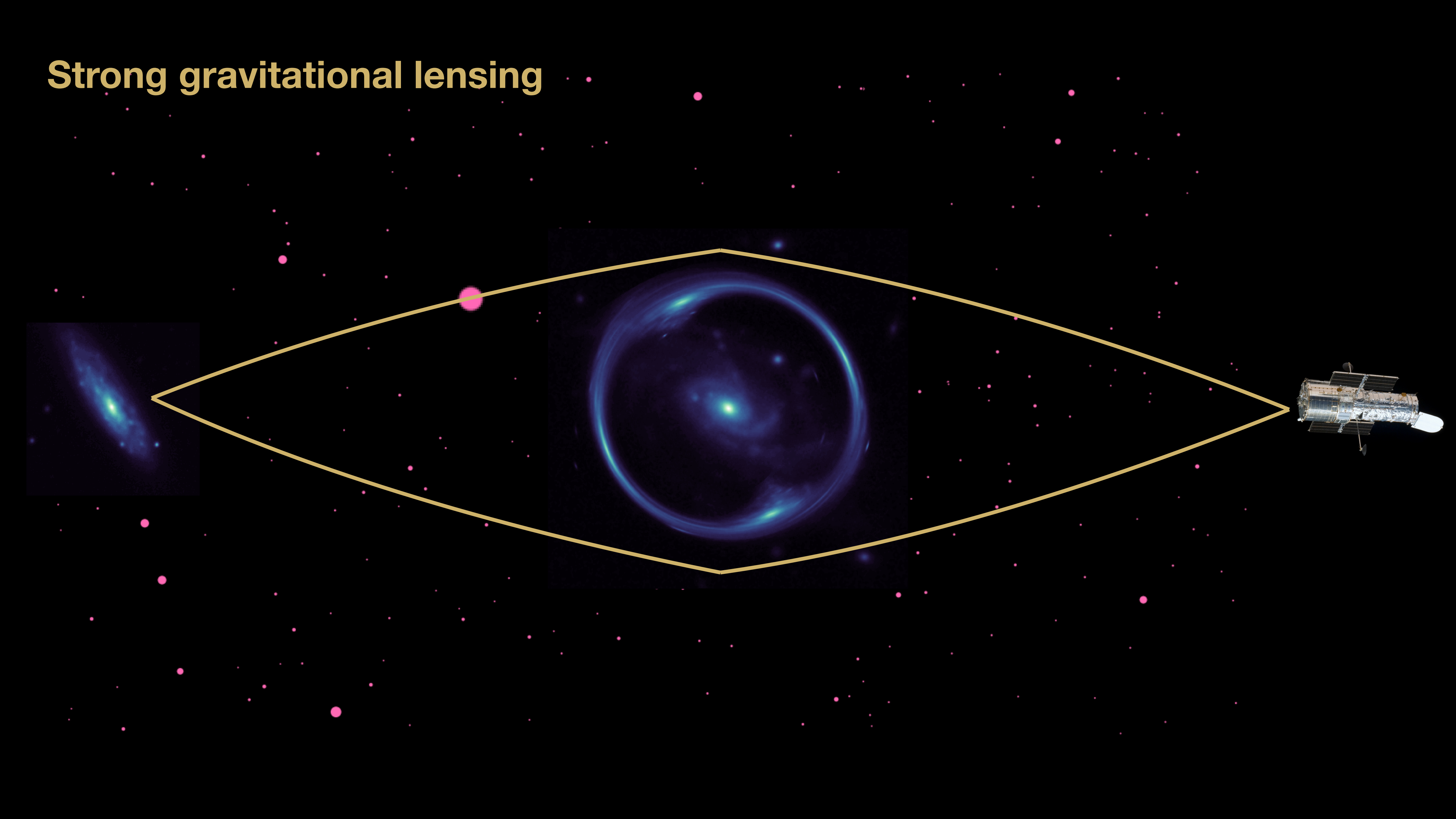
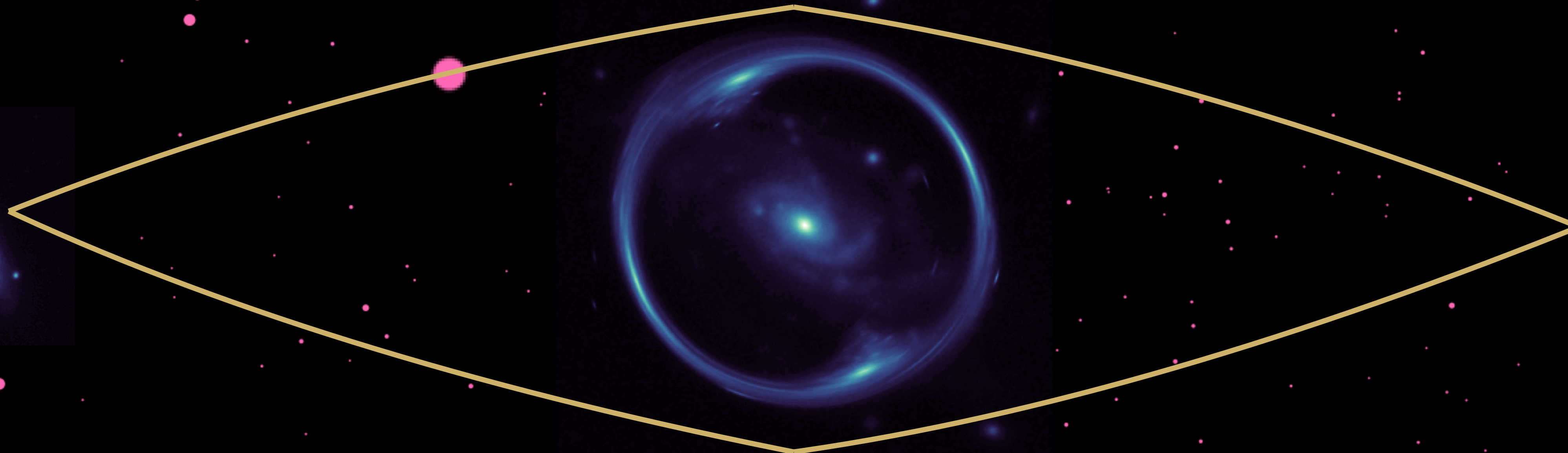
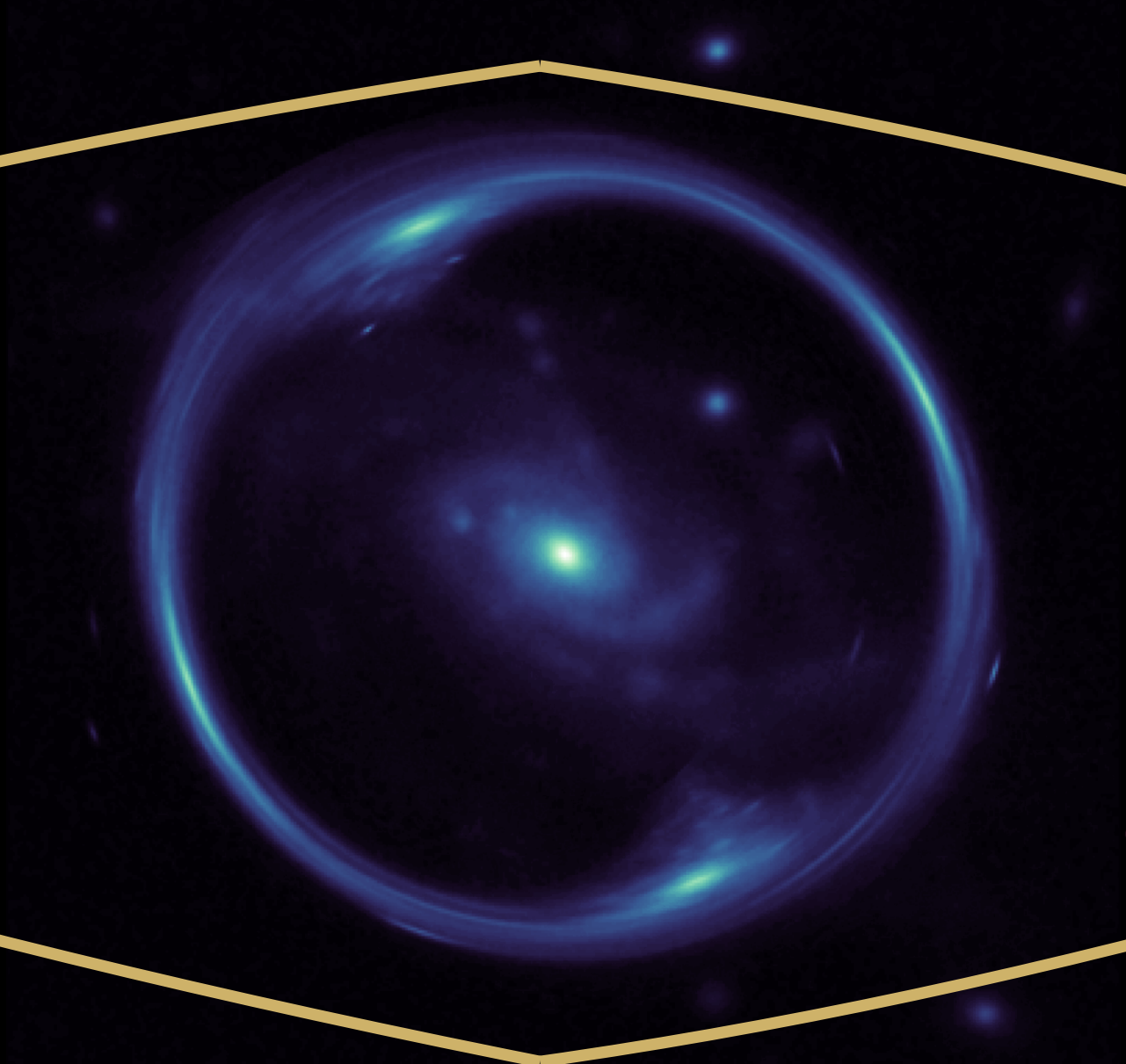
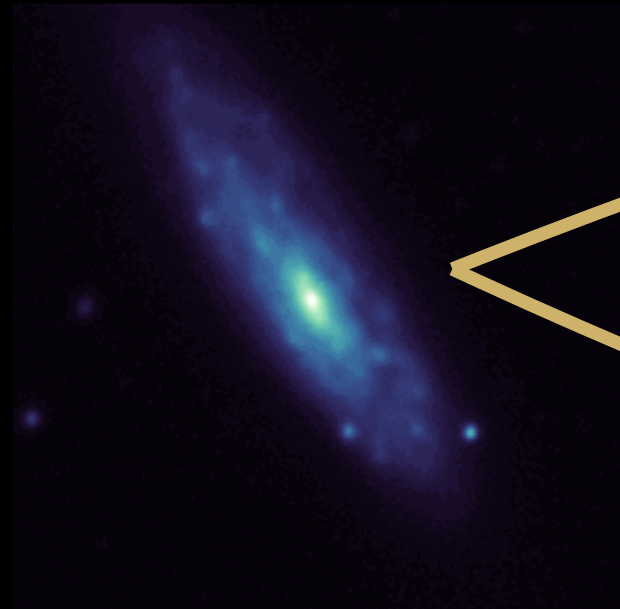
Strong gravitational lensing



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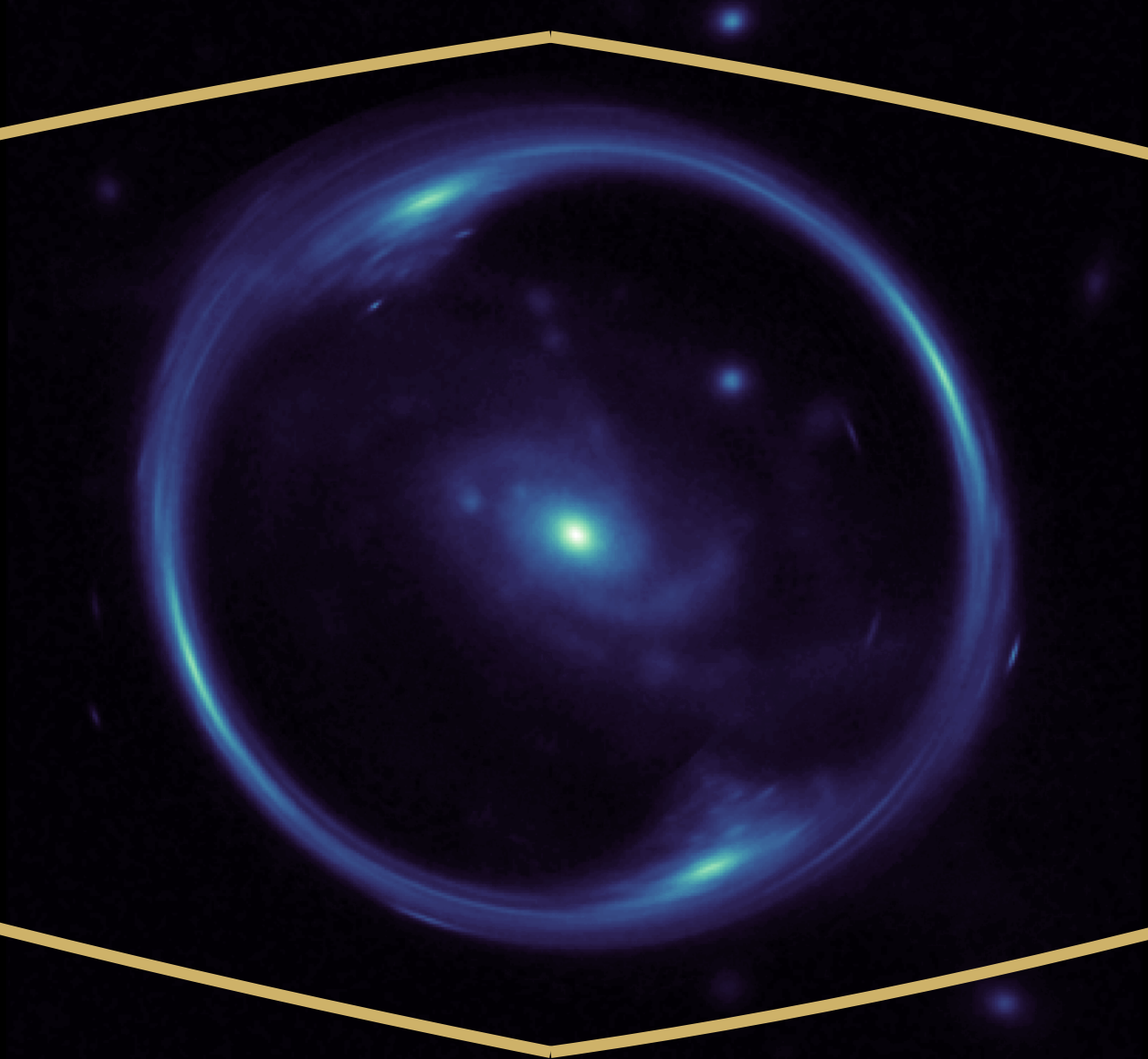
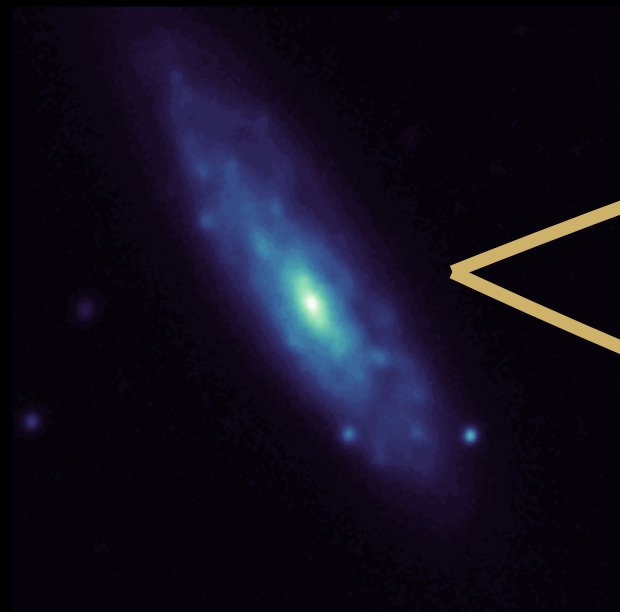
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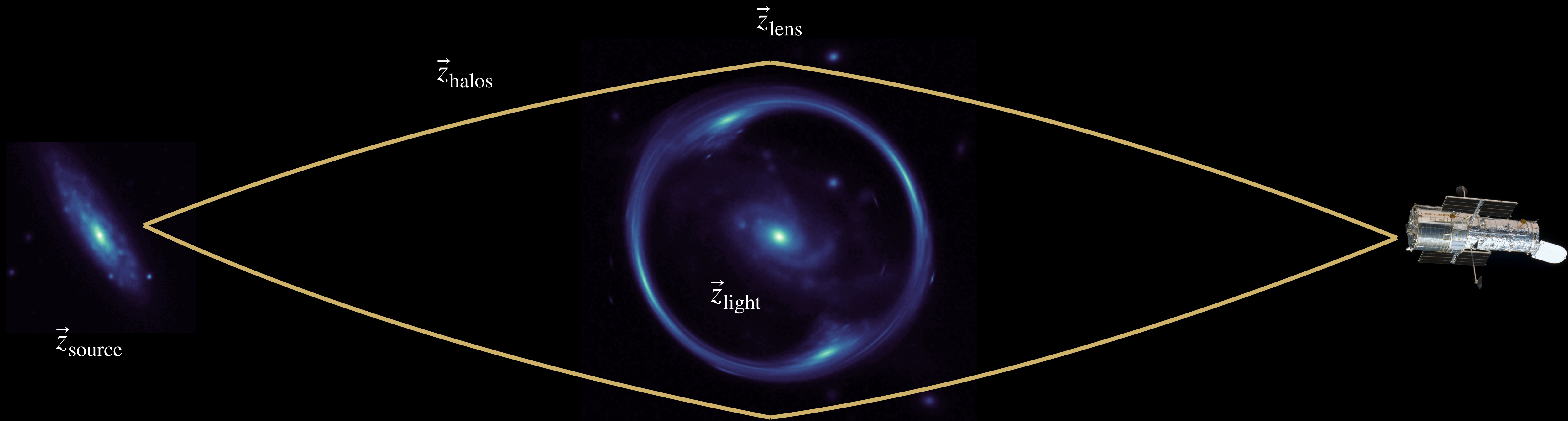
Inference challenge



Strong gravitational lensing



Inference challenge



$$p(\vartheta | \vec{x}) \propto \int \overbrace{d\vec{z}_{\text{light}} d\vec{z}_{\text{lens}} d\vec{z}_{\text{source}} d\vec{z}_{\text{halos}}}^{\text{Very hard!}} p(\vec{x} | \vec{z}_{\text{light}}, \vec{z}_{\text{lens}}, \vec{z}_{\text{source}}, \vec{z}_{\text{halos}}) p(\vec{z}_{\text{light}}) p(\vec{z}_{\text{lens}}) p(\vec{z}_{\text{source}}) p(\vec{z}_{\text{halos}} | \vartheta) p(\vartheta)$$

Signal of interest: e.g. single heavy small-scale halo position and mass, halo mass function parameters related to DM particle physics etc...

Traditional approaches

- **Likelihood-based approaches:**

- MCMC methods
- Nested sampling

→ compute the joint posterior and *then* marginalise, difficult to scale up for more complex models.

Subhalo detections: [Vegetti et al. \(2010, 2012\)](#), [Hezaveh et al. \(2016\)](#).

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- **Approximate Bayesian Computation (ABC):**

→ likelihood-free, but difficult to get a *good* diagnostic measure, a summary statistics.

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Our strategy



TMNRE = Truncated Marginal Neural Ratio Estimation

Implementation in [swyft](#)





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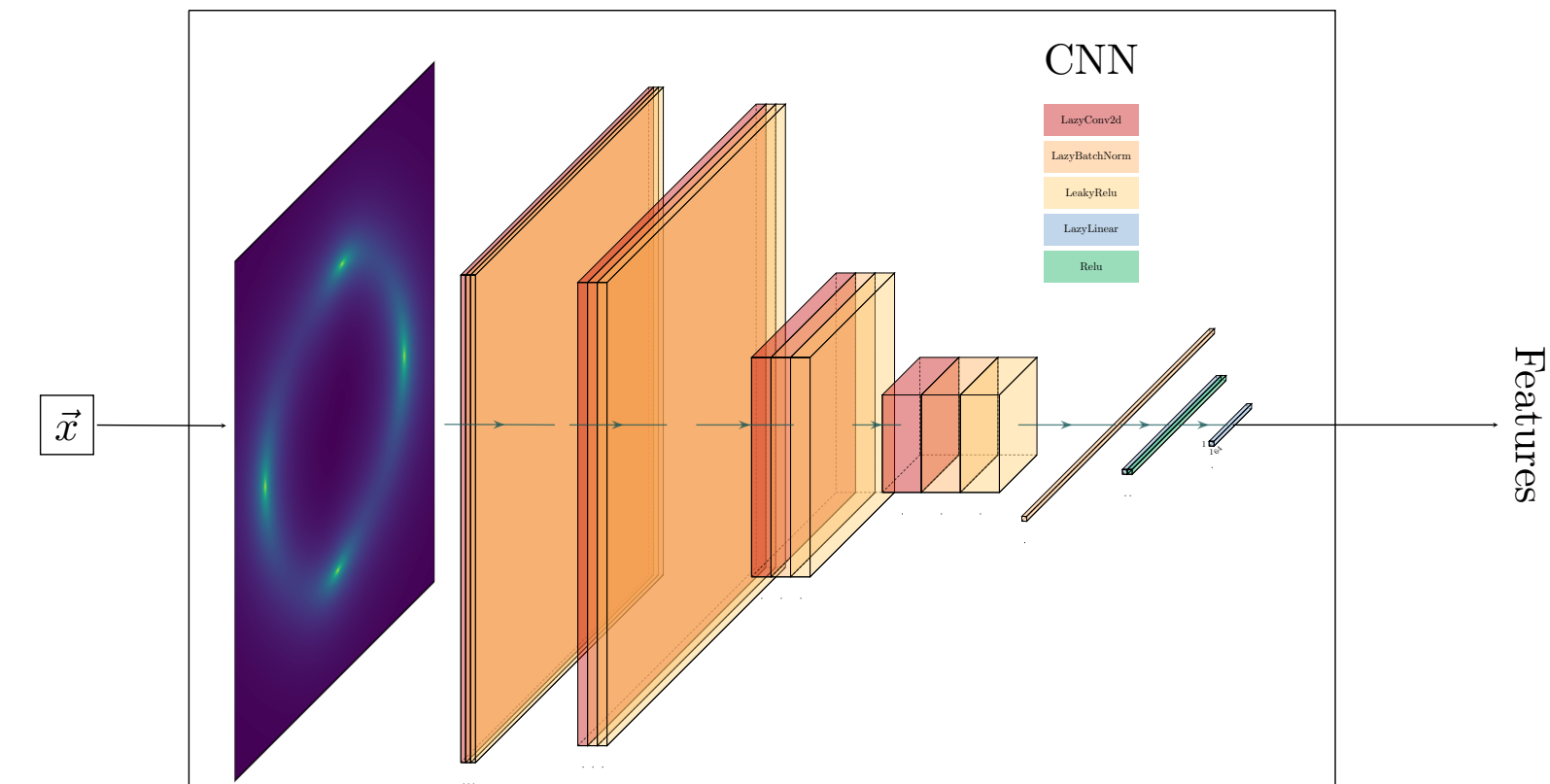
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TMNRE = *Truncated* Marginal Neural Ratio Estimation

Implementation in [swyft](#)

- Uses **NNs** to directly estimate the best summary statistic from the full input data





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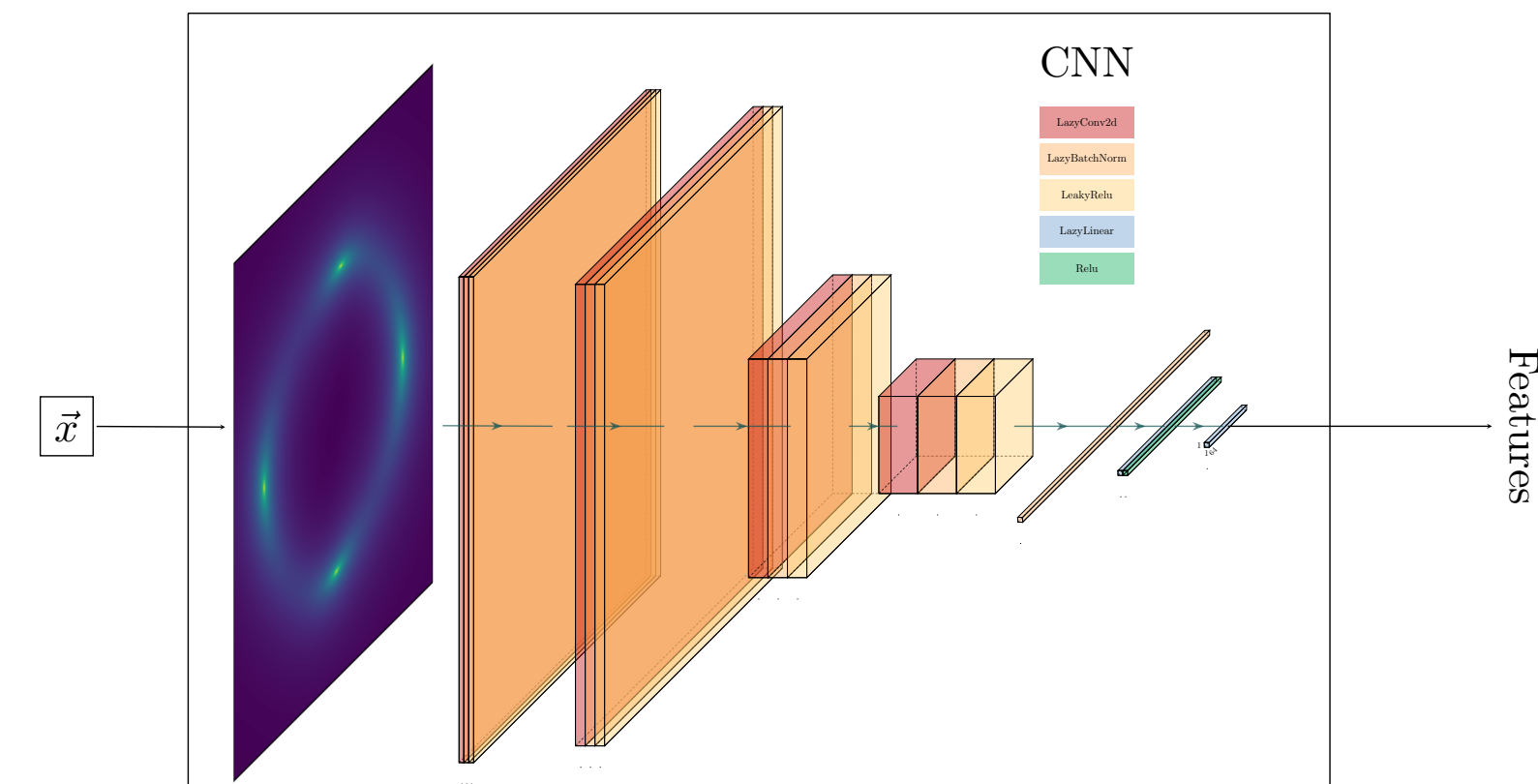
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TMNRE = *Truncated Marginal Neural Ratio Estimation*

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- Directly learns **marginals** posteriors for the signal of interest ϑ :

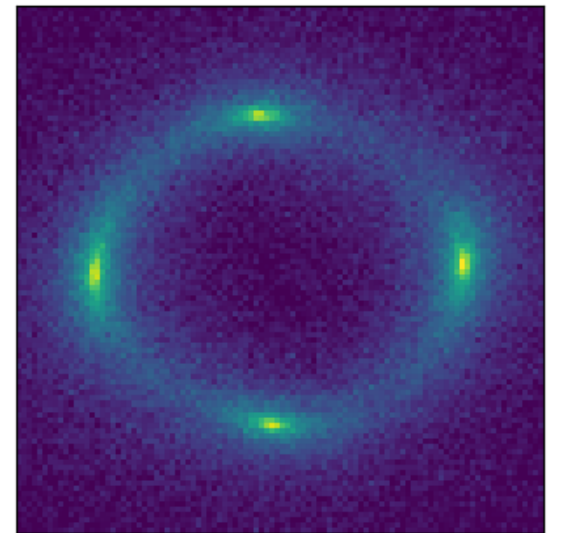
$$p(\vartheta | \vec{x}) = r(\vec{x}, \vartheta)p(\vartheta) = \frac{p(\vec{x} | \vartheta)}{p(\vec{x})} p(\vartheta)$$



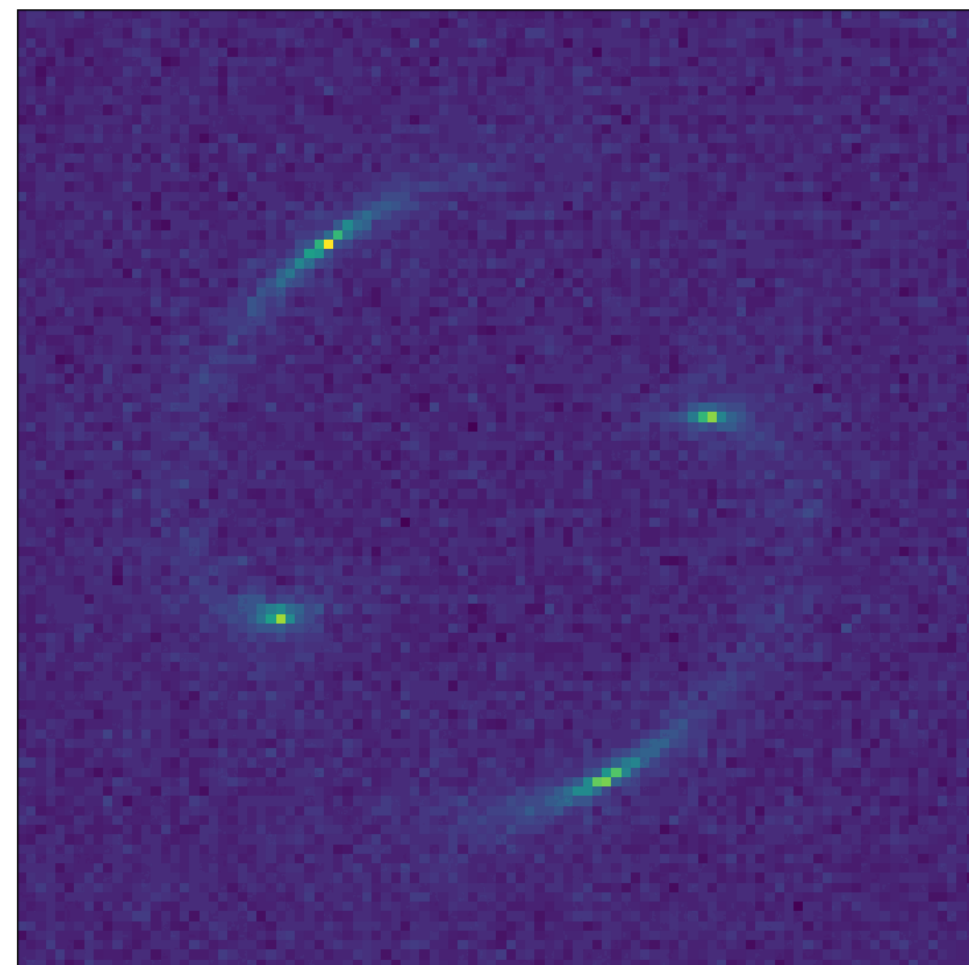
Constrain \vec{z}_{lens} and \vec{z}_{source} parameters with *truncation*

Truncation **focuses training data generation** in the regions of the parameter space most relevant for analysing a particular observation.

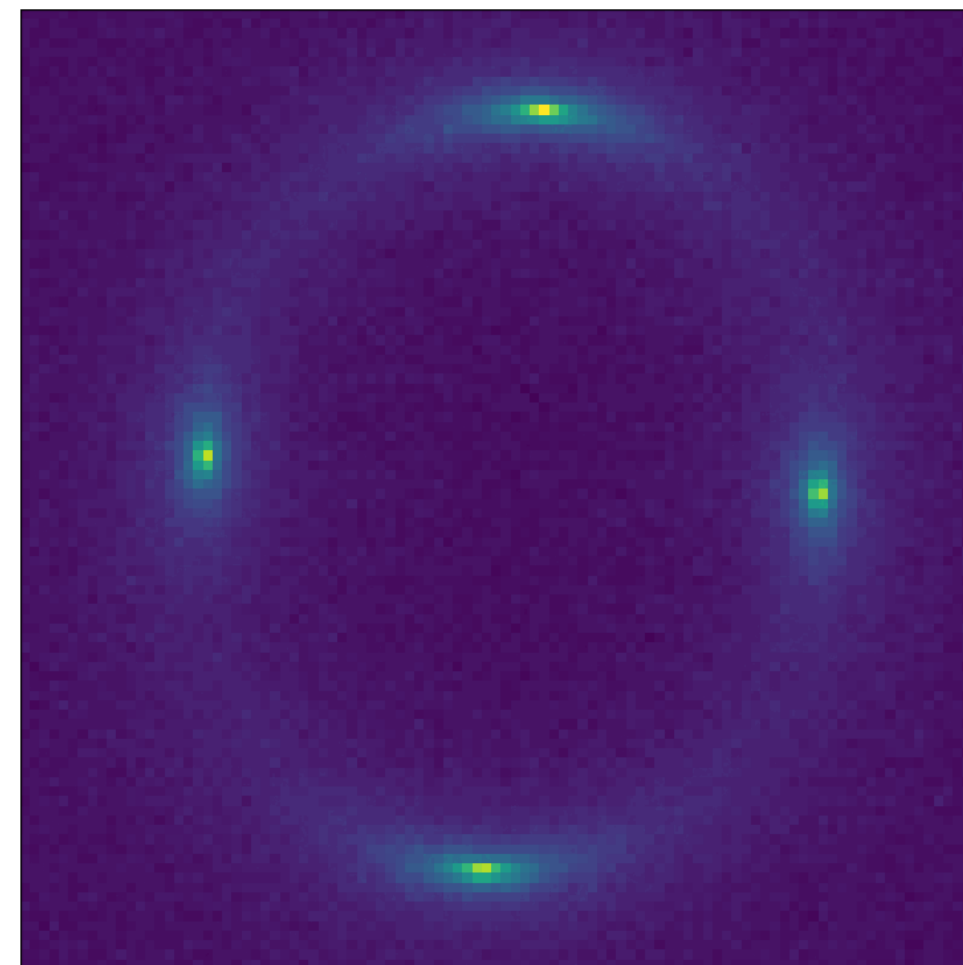
Target mock observation



Round 1

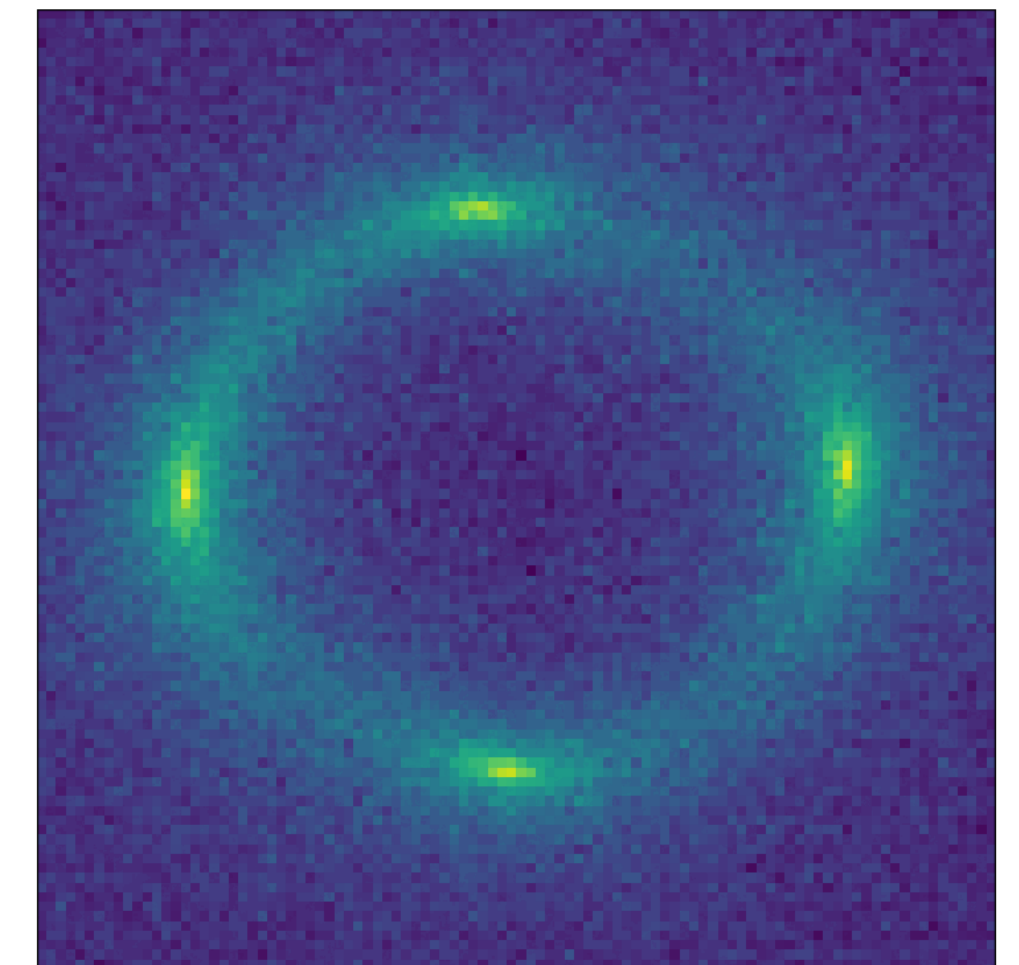


Round 2



...

Round 6

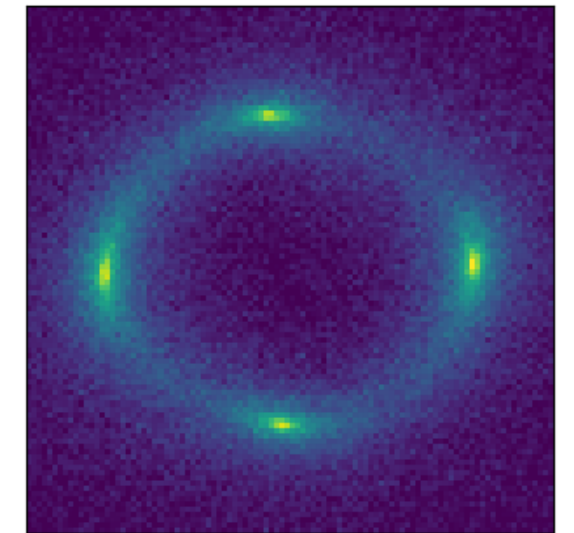


Training data

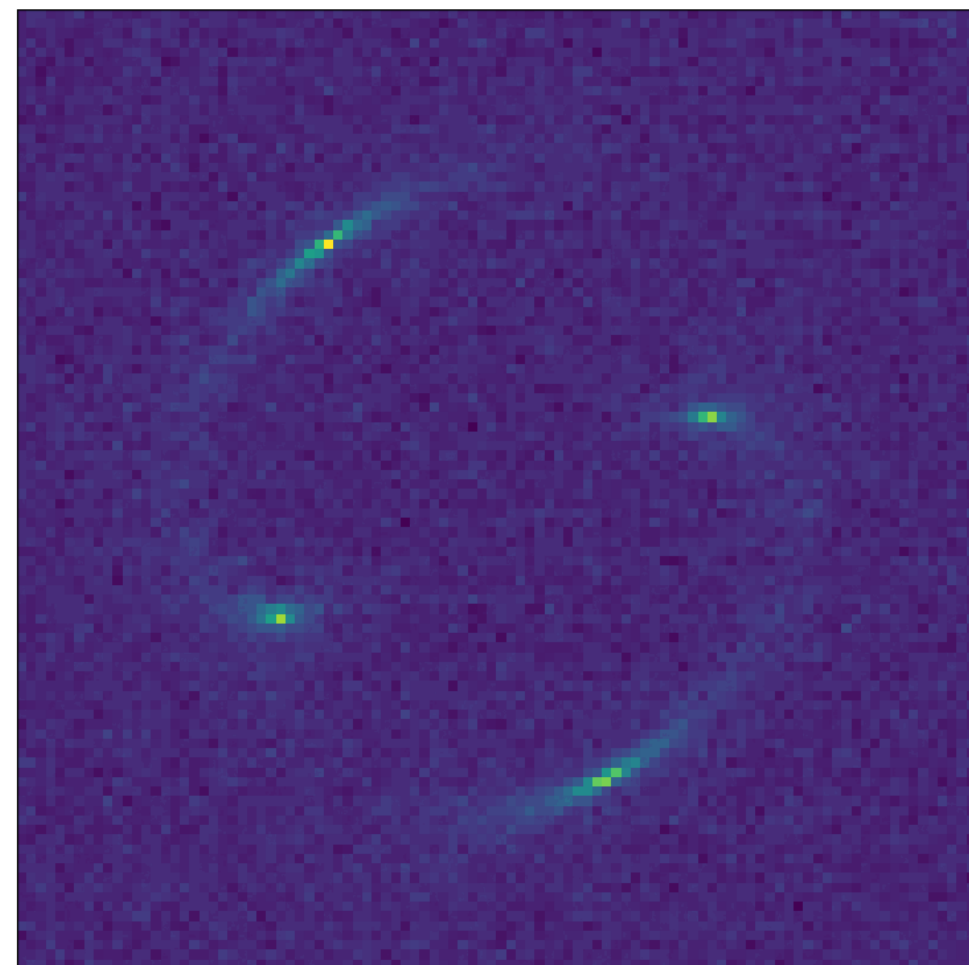
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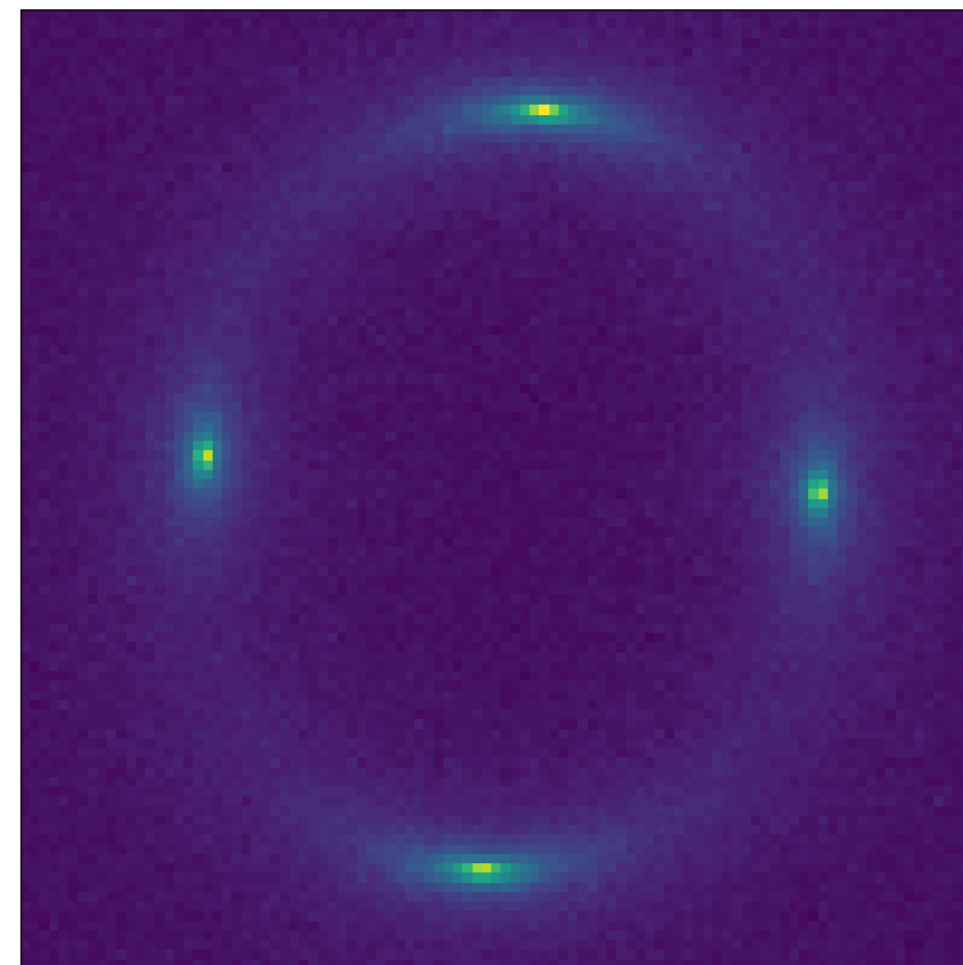
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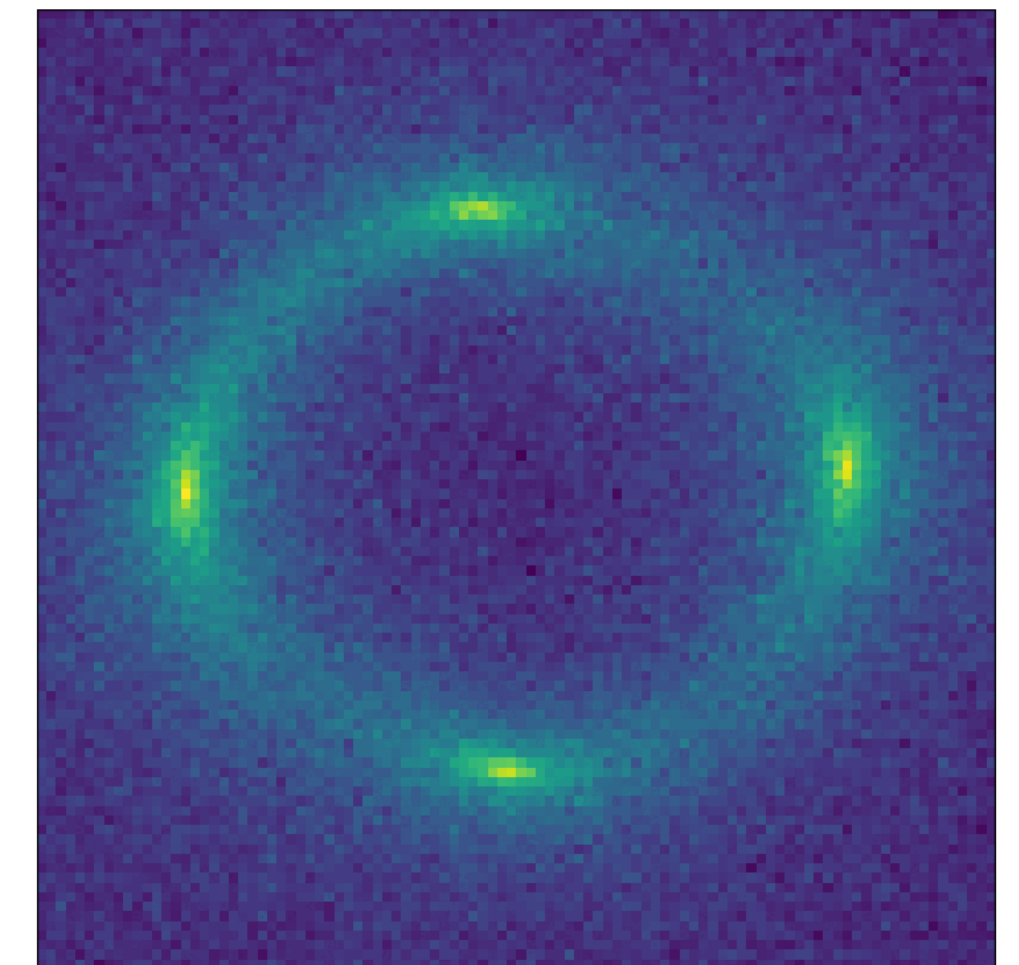


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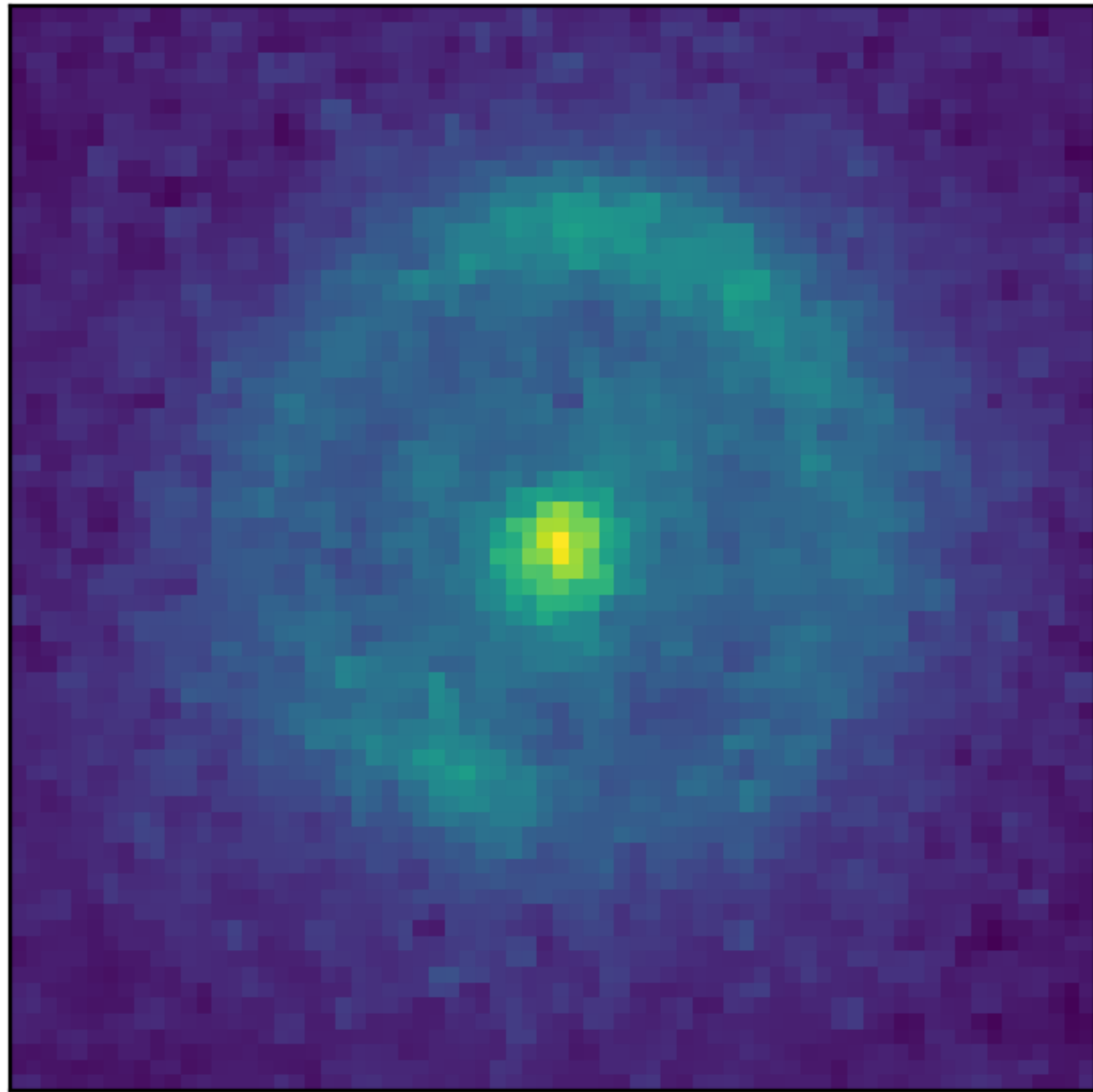


Training data

JVAS B1938+666

Vegetti et al. (2012) - subhalo detection claim

Şengül et al. (2021) - detection reanalysed



JVAS B1938+666

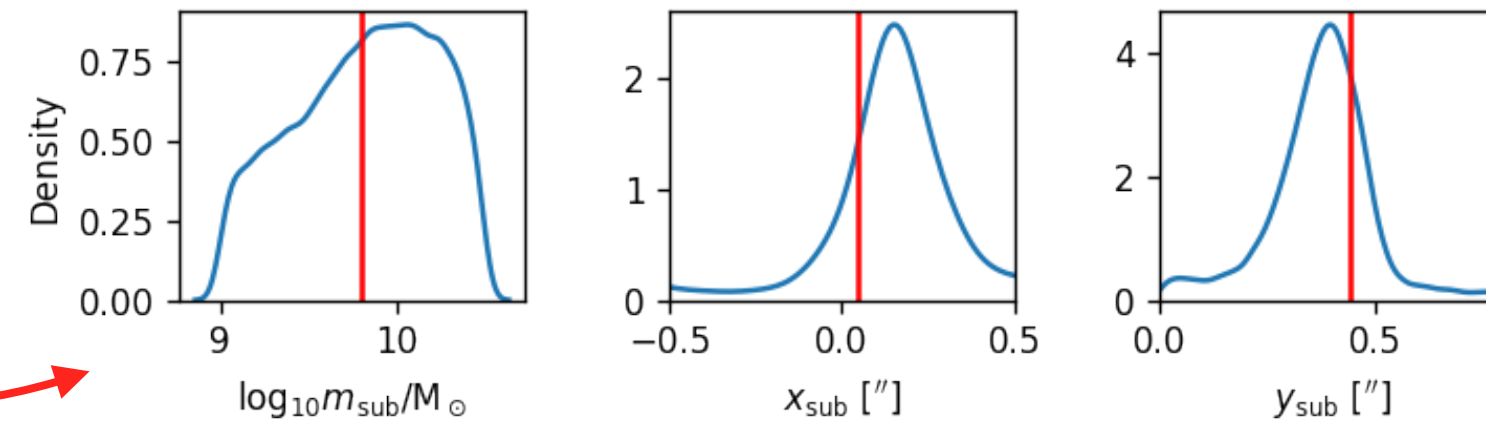
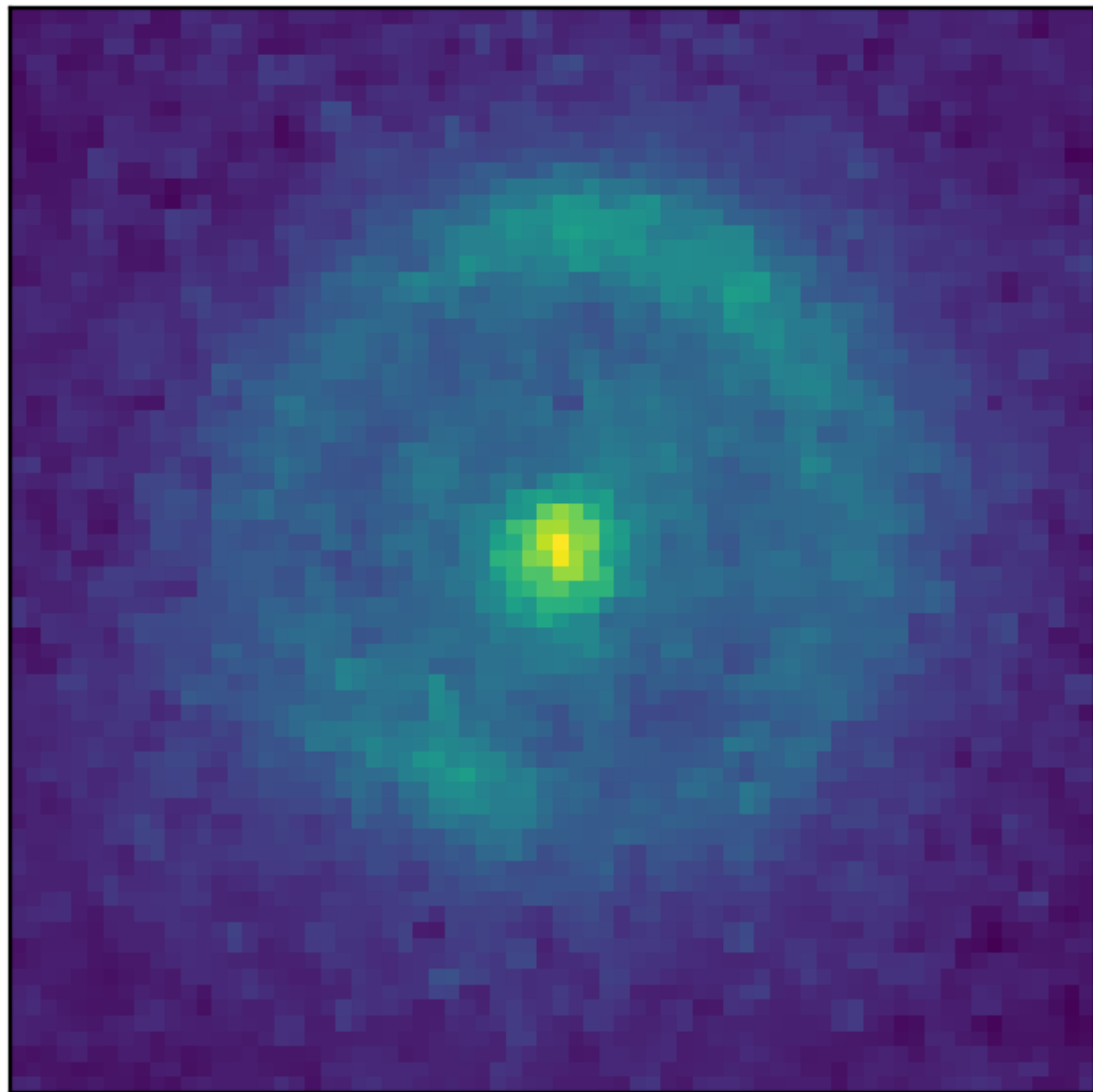
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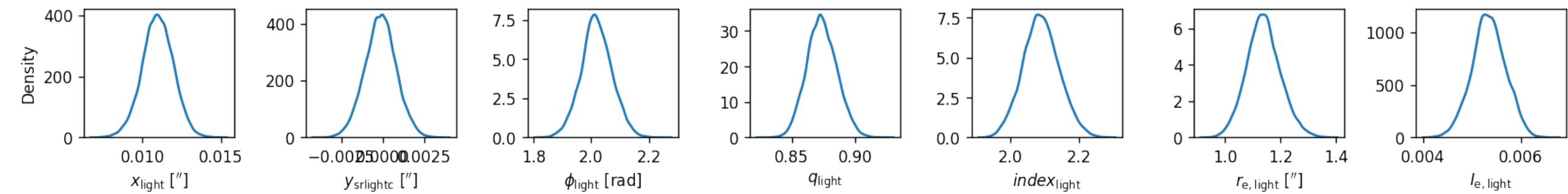
VERY PRELIMINARY

Small-scale halo mass and position

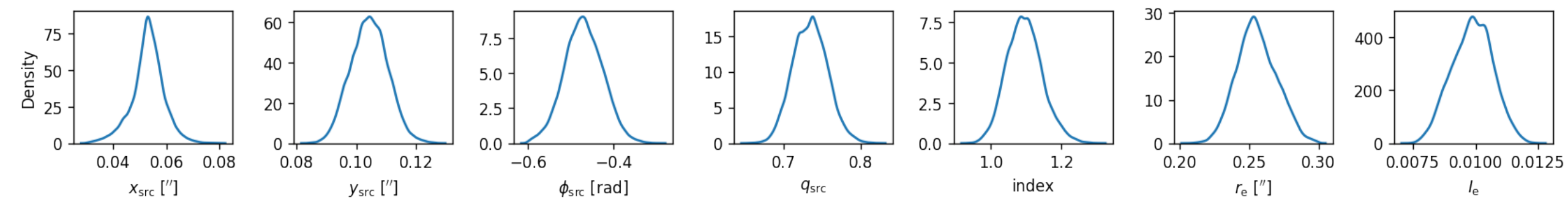
- First analysis to take into account lens light uncertainties!
- Next steps: more complex source model and including PSF and correlated pixel noise.



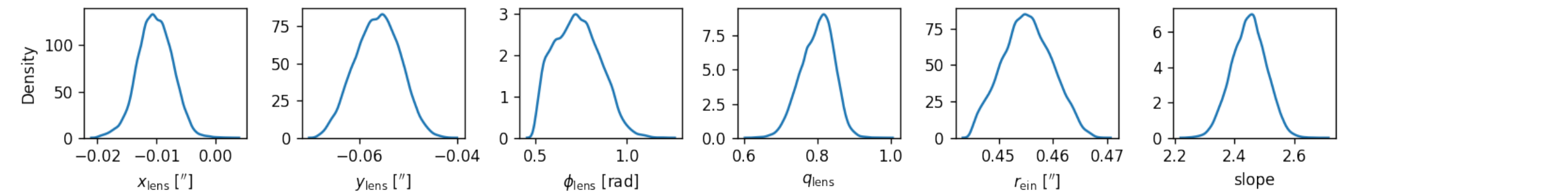
\vec{z}_{light}



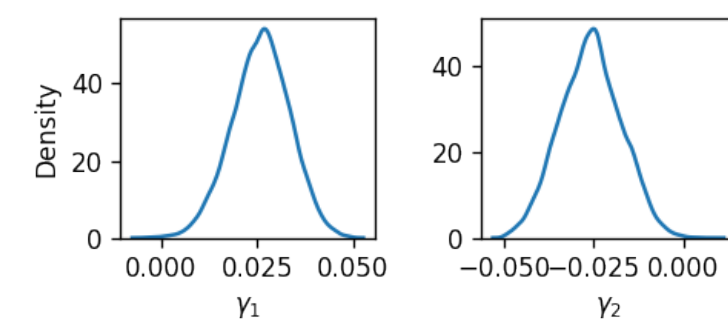
\vec{z}_{source}



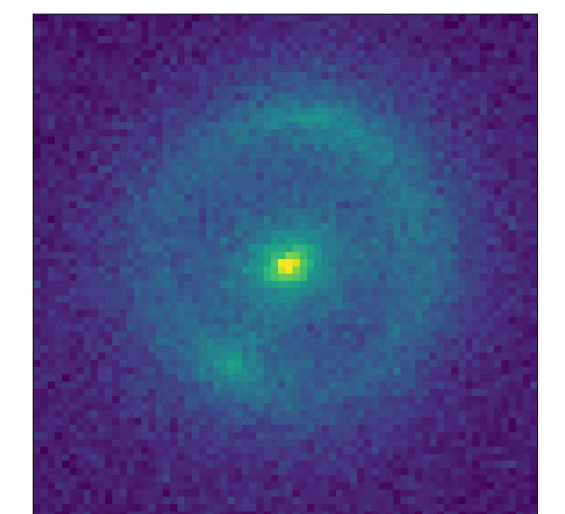
\vec{z}_{lens}



\vec{z}_{shear}



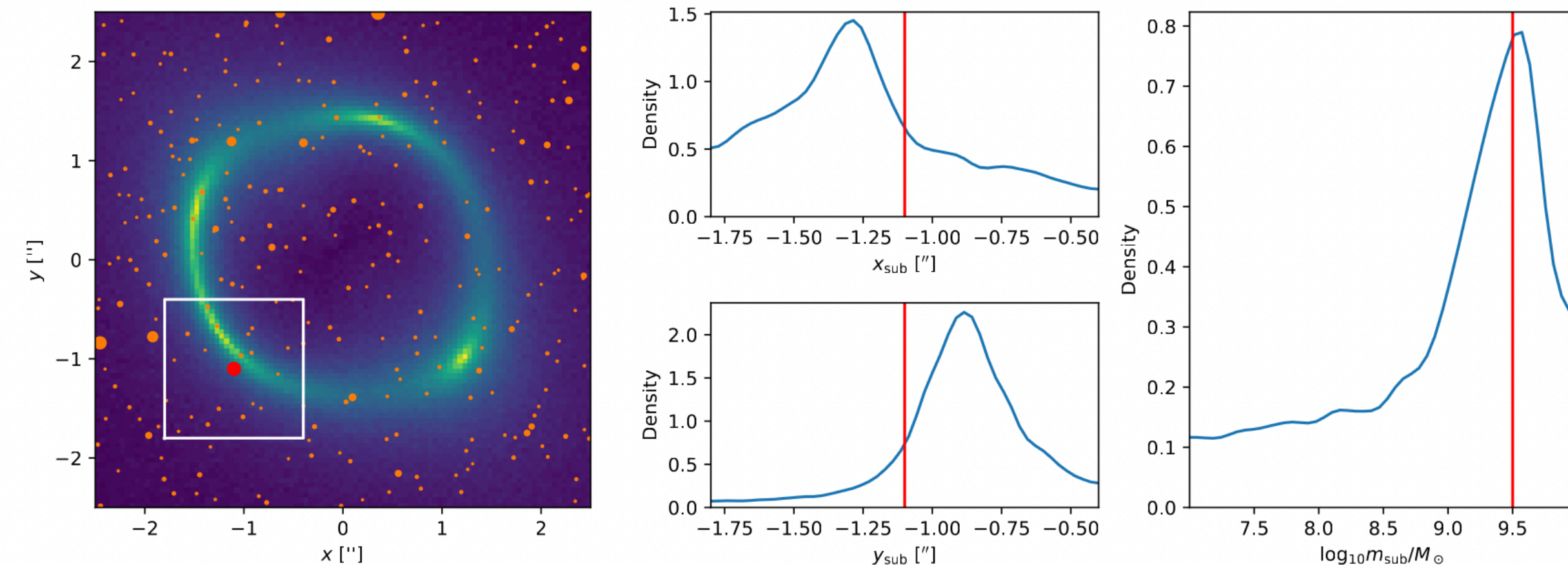
Training data:



Improving the realism of the model

Measuring a single subhalo position and mass marginalising over source and lens uncertainties and a population of other subhalos and line-of-sight halos.

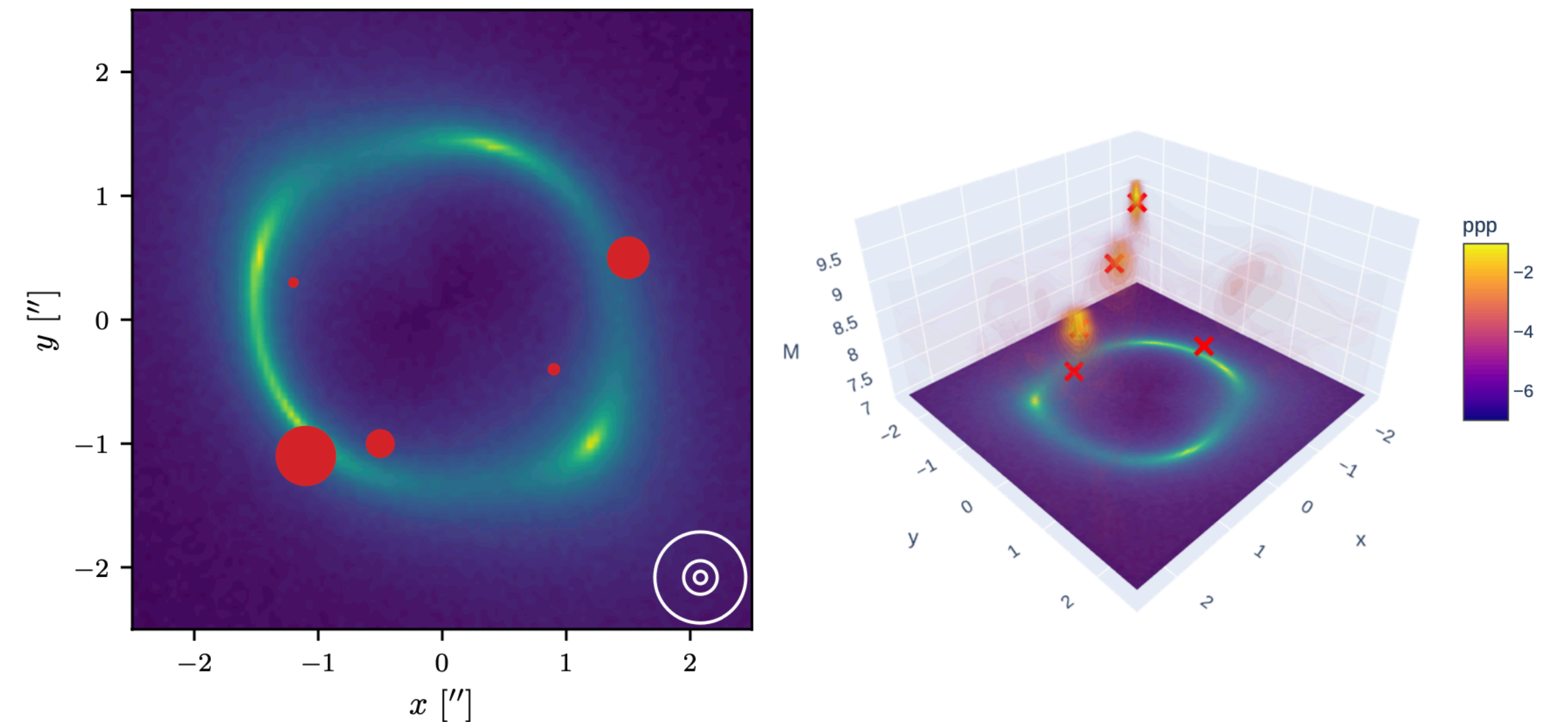
PRELIMINARY on mock images



[Coogan et al. \(in preparation\)](#)

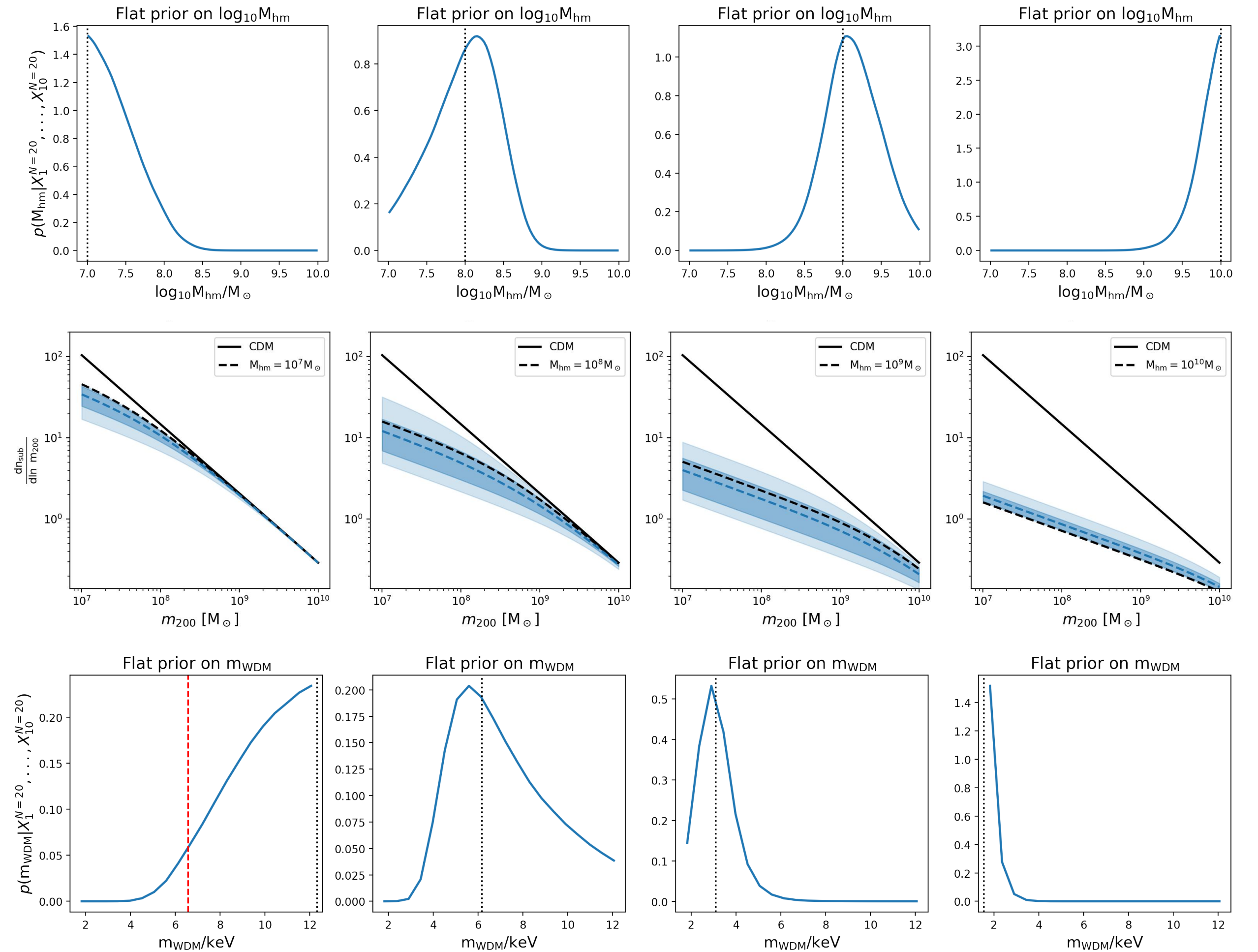
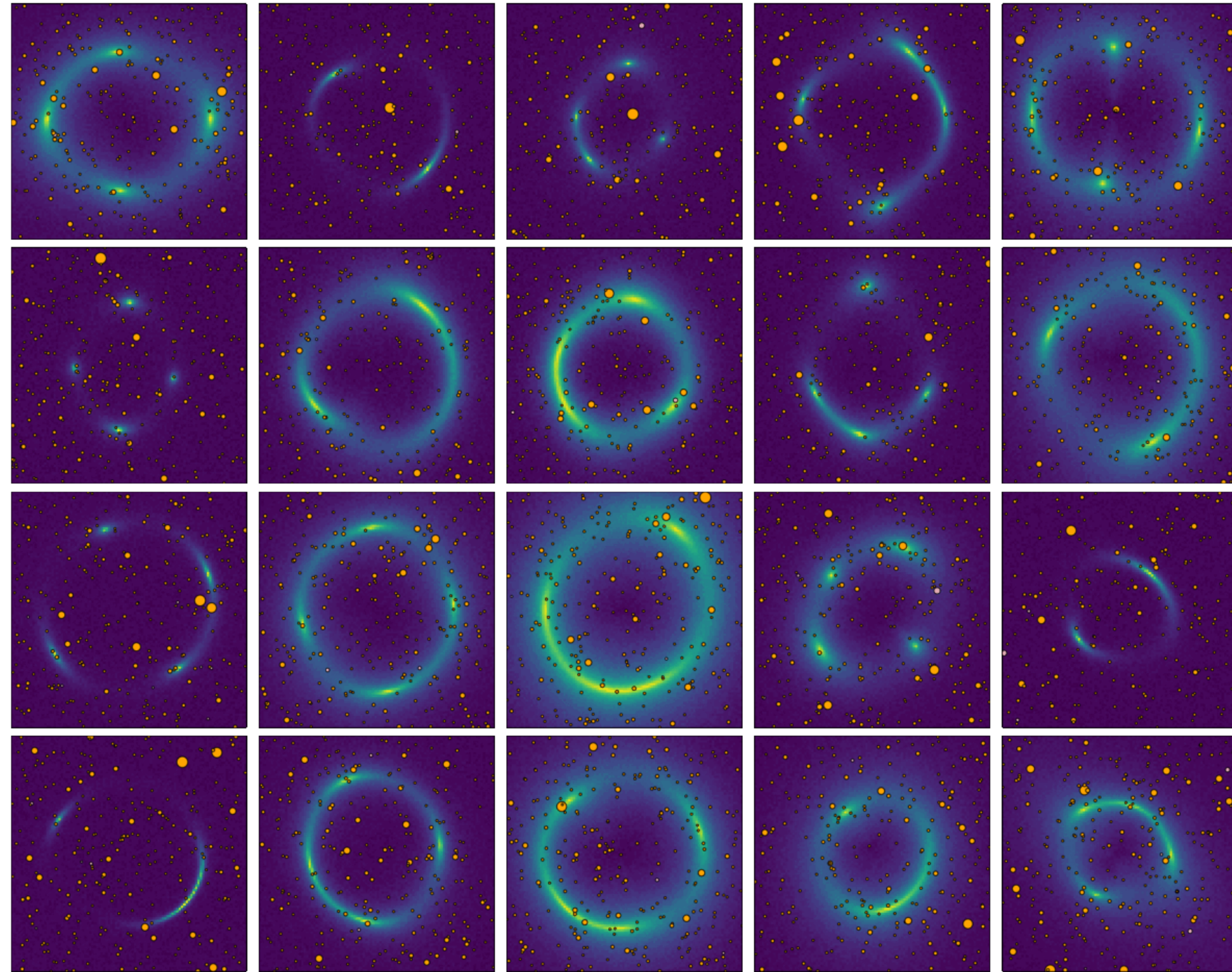
Probabilistic image segmentation to measure multiple subhalos.

PRELIMINARY on mock images

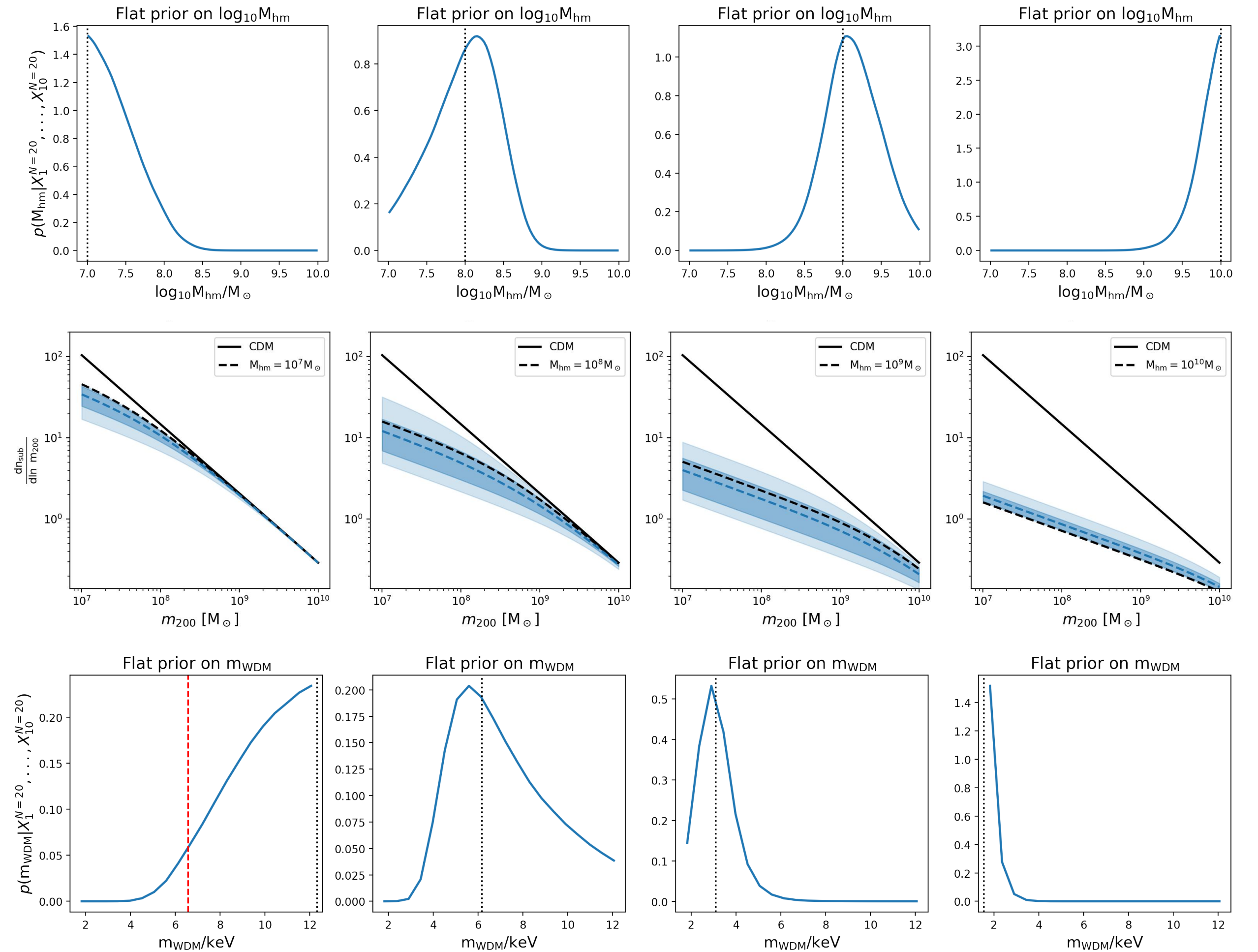
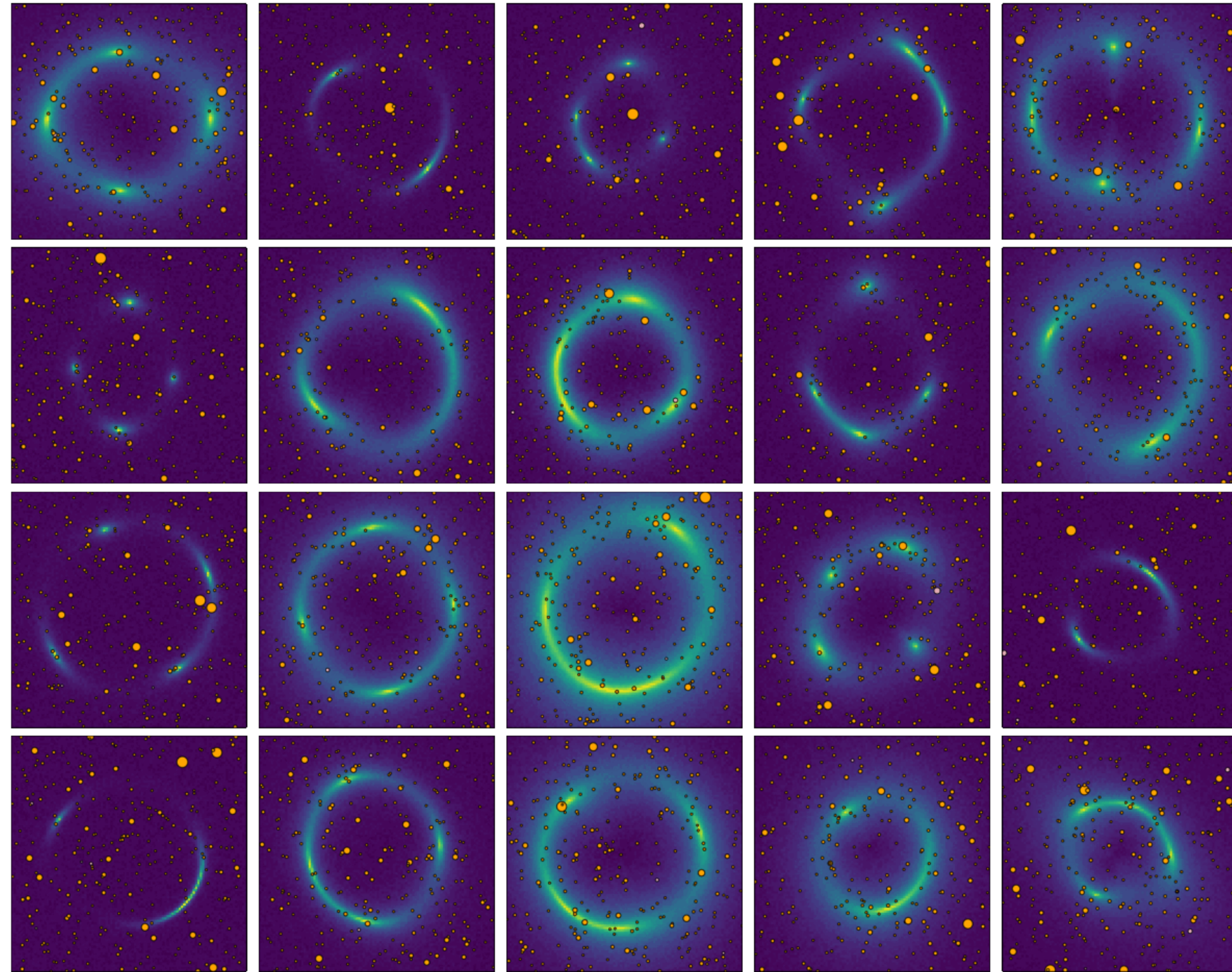


[credit: Elias Dubbeldam](#)

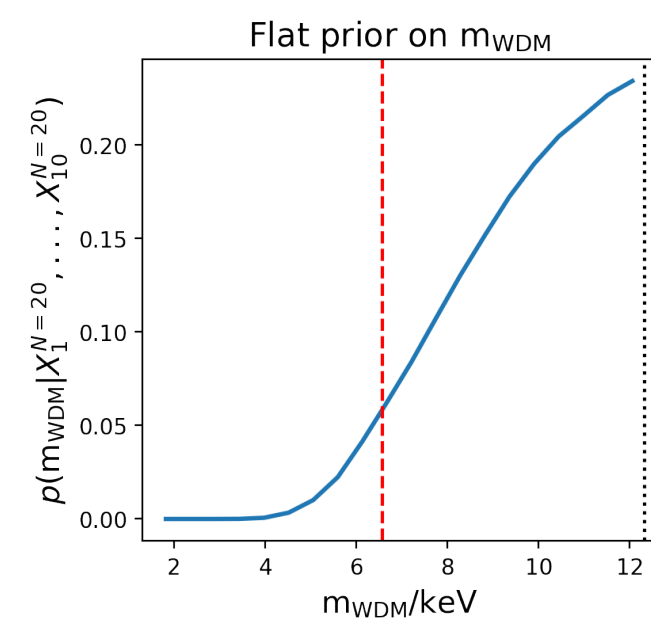
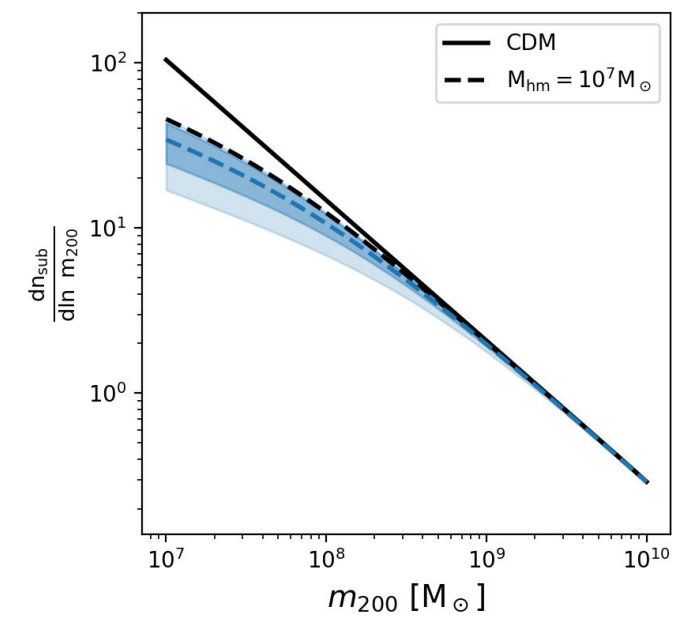
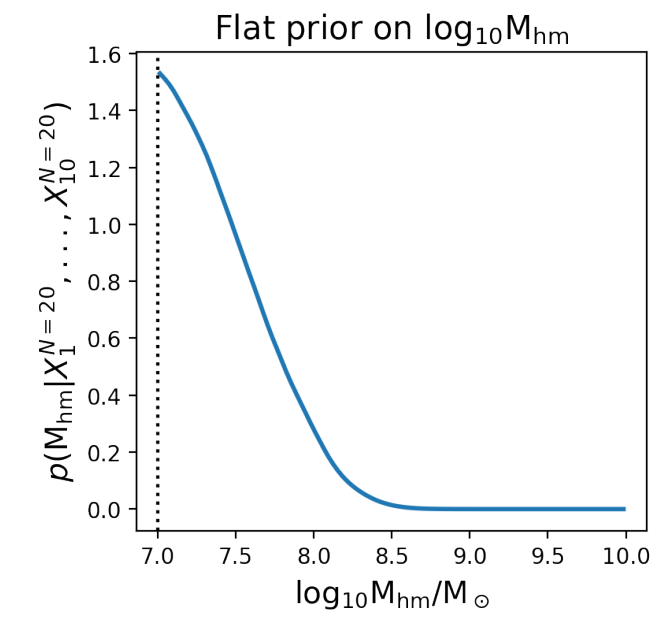
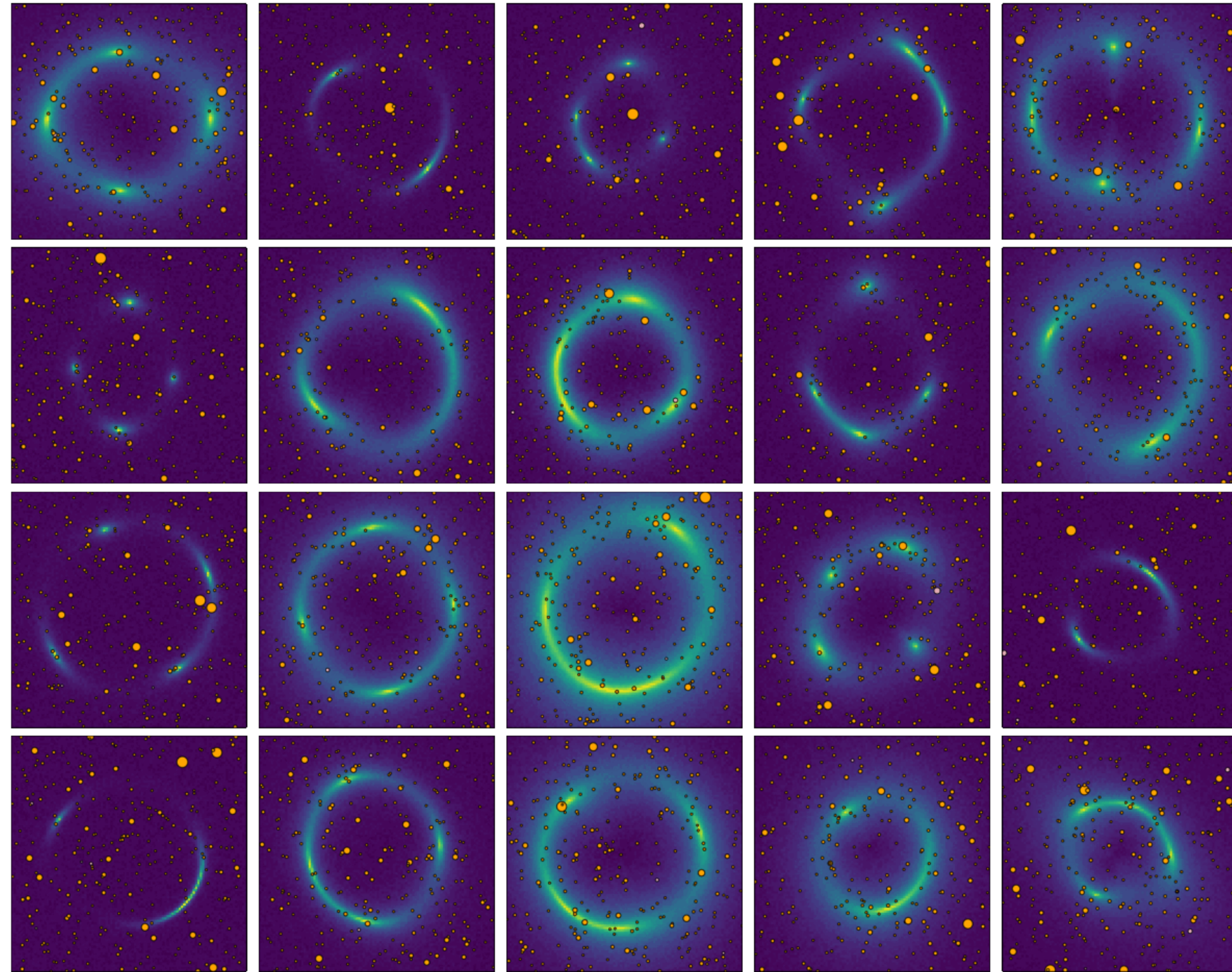
Inferring the SHMF cutoff scale from a population of subhalos and line-of-sight halos *combining different mock observations*



Inferring the SHMF cutoff scale from a population of subhalos and line-of-sight halos *combining different mock observations*



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In case of the scenario closest to CDM in our SHMF cutoff scale range ($M_{hm} = 10^7 M_{\odot}$), we obtain an expected 95% credible lower limit around 6.5 keV on DM mass.



Conclusions

- * Measuring **individual halos** and **halos collective properties** is an important component of dark matter lensing analyses.
- * **Truncated marginal neural ratio estimation** enables **full marginalisation** over light, lens, source and small-scale halos population.
- * **Next steps:** implement more complex source, light, lens, noise models.
- * These first results demonstrate that this method is **imminently applicable** to existing lensing data and to the large sample of lenses that will be delivered by near-future telescopes.

Soon $\sim \mathcal{O}(10^5)$ observations from JWST, Euclid, ELT Rubin (Collet 2015)

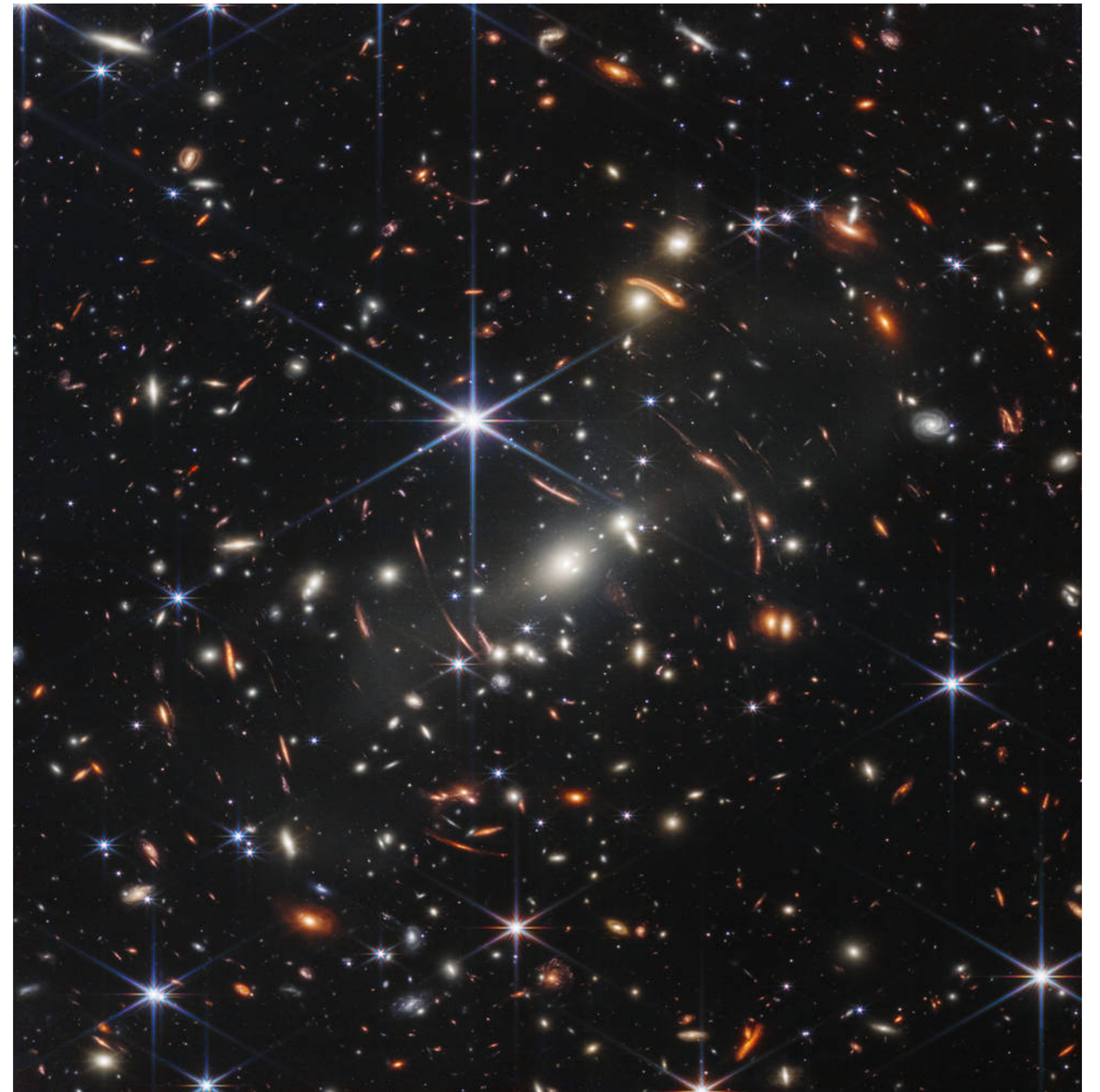
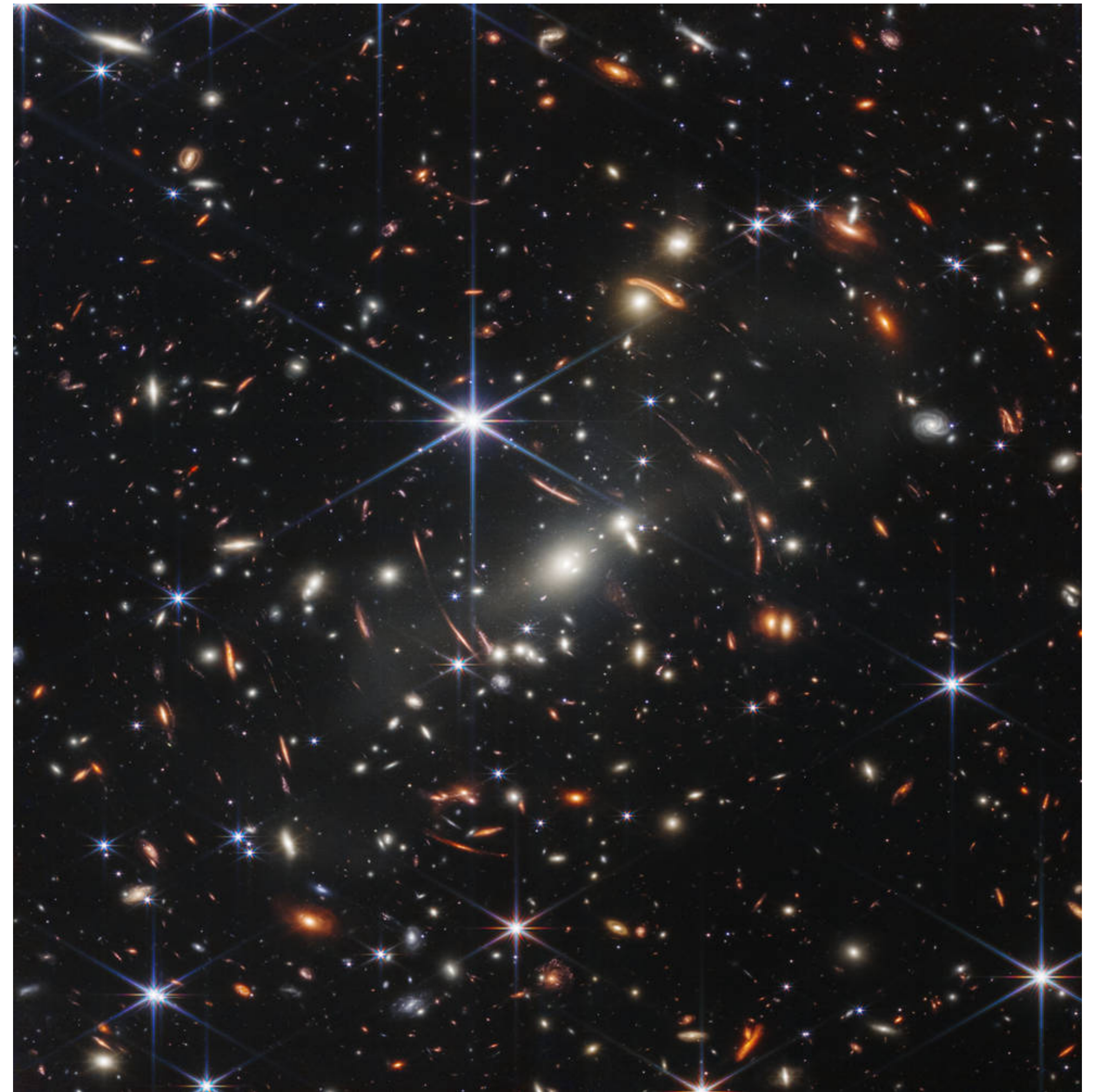


Image credit: NASA, ESA, CSA, and STScI

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THANK YOU!

Image credit: NASA, ESA, CSA, and STScI