

Nuclear moments of excited states in neutron rich Sn isotopes studied by on-line PAC

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Nuclear moments – Why?

Magnetic dipole and electric quadrupole moments

- Sensitivity towards **single-particle** and **collective** properties of the nuclei

$$\vec{\mu} = \sum_{k=1}^A g_{\ell}^{(k)} \vec{\ell}^{(k)} + \sum_{k=1}^A g_s^{(k)} \vec{s}^{(k)}$$

$$2Q = e^{\pi} \sum_{p=1}^Z \overline{(3z^2 - r^2)} + e^{\nu} \sum_{n=1}^N \overline{(3z^2 - r^2)}$$

Free-nucleon vs. effective g factors

$g_s^{\pi} = 5.58$	$g_{\ell}^{\pi} = 1$	$g_s^{\pi} = 0.7 * g_s^{\pi}$	$g_{\ell}^{\pi} = 1 + \Delta g^{\pi}$
$g_s^{\nu} = -3.28$	$g_{\ell}^{\nu} = 0$	$g_s^{\nu} = 0.7 * g_s^{\nu}$	$g_{\ell}^{\nu} = \Delta g^{\nu}$

- ✓ valence particle configuration;
- ✓ core polarization (M1 excitations);
- ✓ purity of the wave function

additivity rule

$$g = \frac{g_1 + g_2}{2} + \frac{g_1 - g_2}{2} * \frac{I_1(I_1 + 1) - I_2(I_2 + 1)}{I(I + 1)}$$

Free-nucleon vs. effective charge

$e^{\pi} = 1e$	$e_{eff}^{\pi} = (1 + \Delta e^{\pi})e$
$e^{\nu} = 0$	$e_{eff}^{\nu} = \Delta e^{\nu} e$

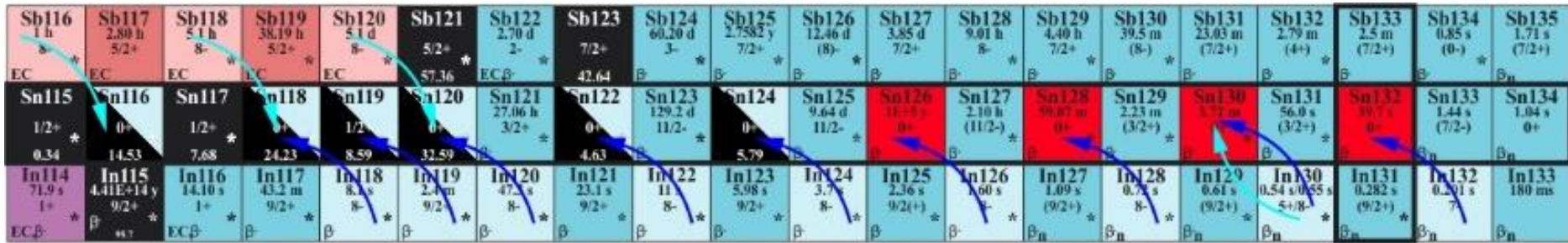
Single-particle case

$$Q_I = \frac{2j + 1 - 2n}{2j - 1} Q_j$$

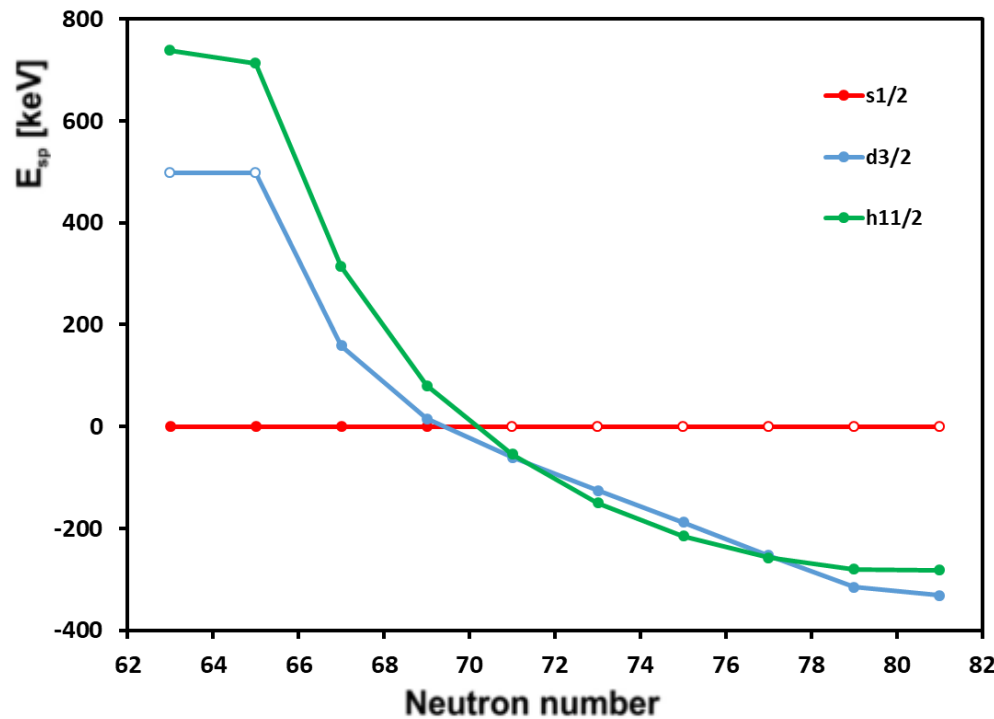
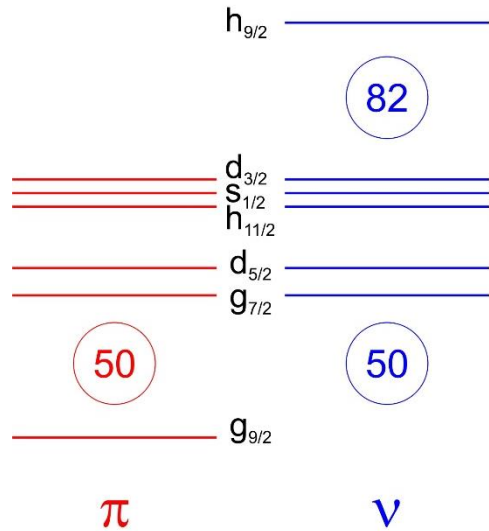
- ✓ valence orbital occupation n;
- ✓ collective properties;
- ✓ nuclear deformation

additivity: $I_1 \times I_2$ coupling,
simple addition if stretched

The area of the present proposal – neutron-rich Sn



Single-particle (hole) states in odd Sn

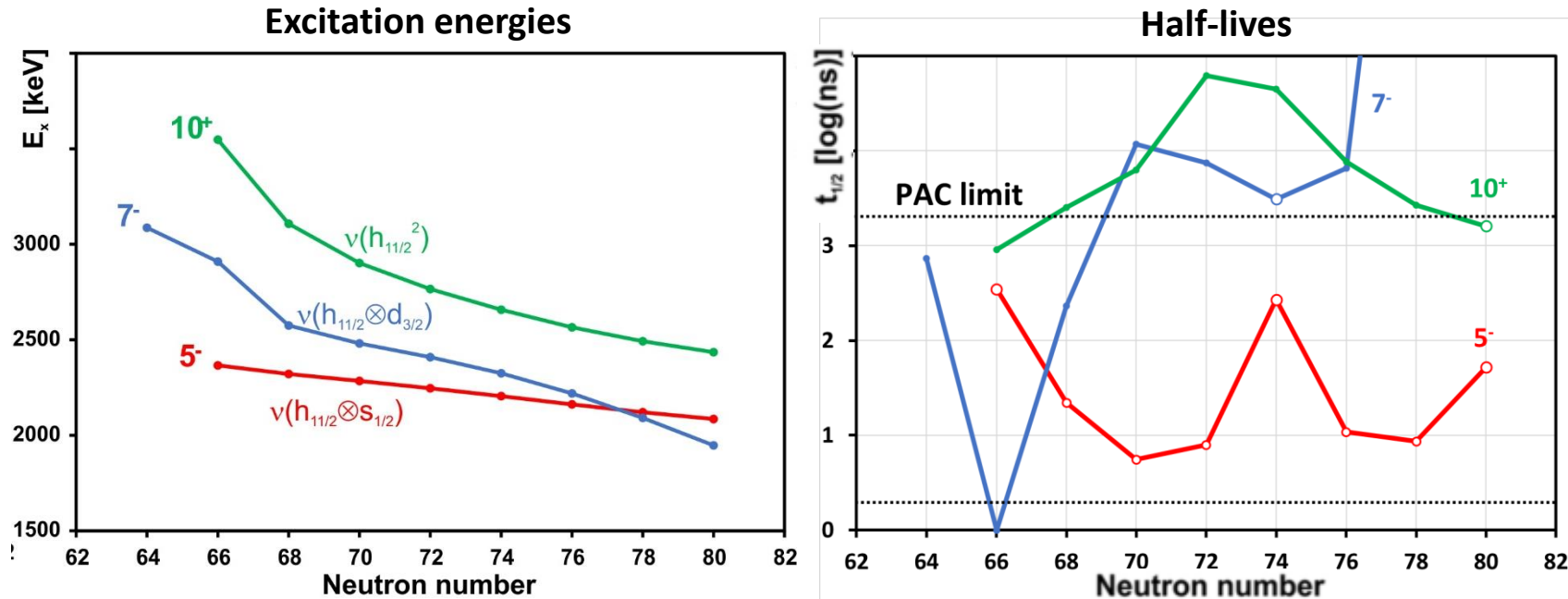


Most **nuclear moments of the single-particle states** have been determined, primarily by COLLAPS [D.T. Jordanov et al., Comm. Phys. 3, 107 (2020)]

μ for heavier $s_{1/2}$ not measurable!

Subject of the present proposal: two-quasi-particle states

Probing the interaction between the neutron $h_{11/2}$, $d_{3/2}$ and $s_{1/2}$ orbitals at $Z=50$



Our aim – test nuclear coupling concept (the additivity rule) for a chain of semi-magic (Sn) nuclei, a textbook case ?

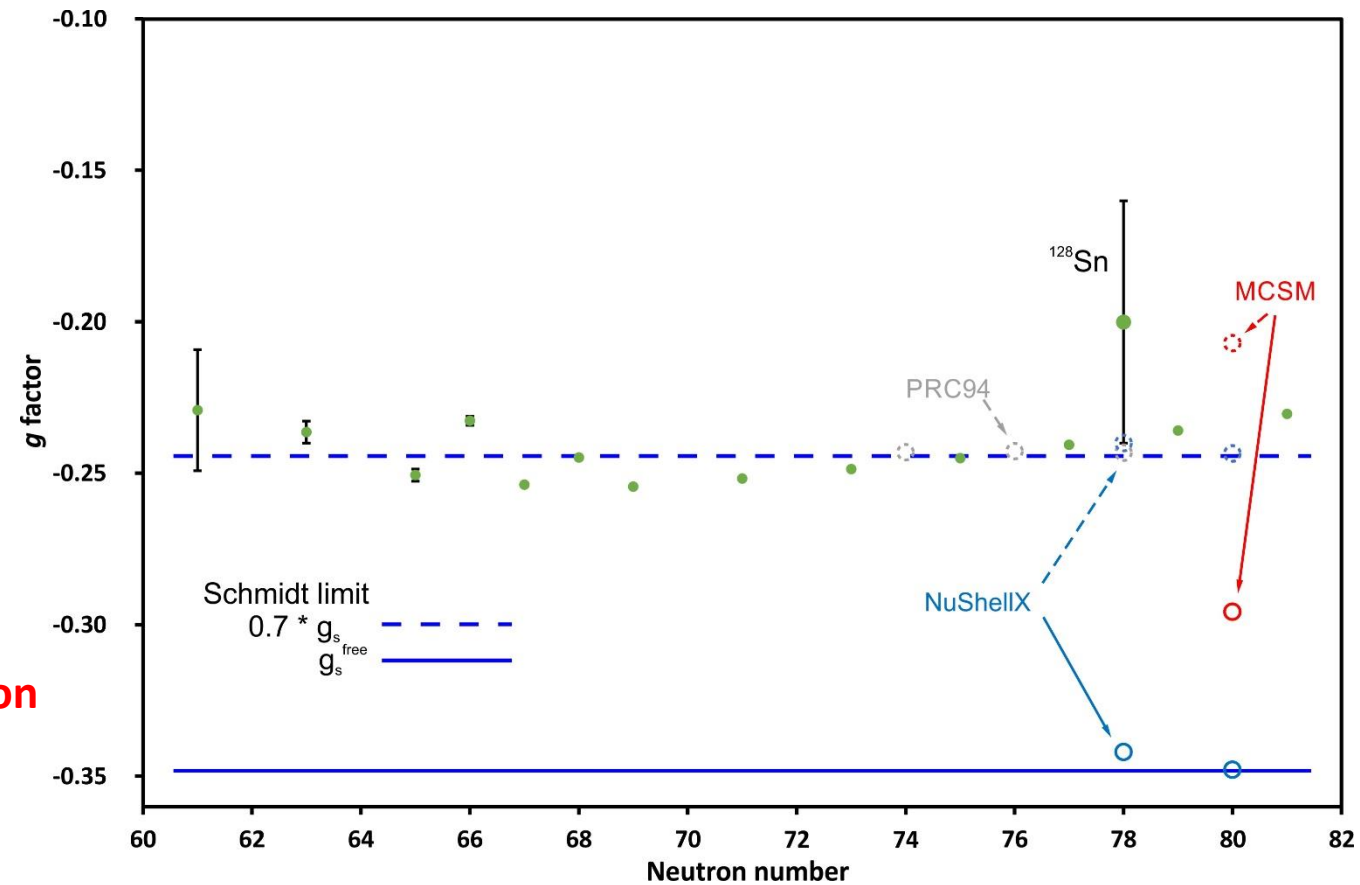
The magnetic dipole and electric quadrupole moments of the 5^- , 7^- and 10^+ states in a chain of Sn isotopes would provide a very stringent test of the nuclear models and demonstrate simple textbook concepts of nuclear physics

→ does the simple SM picture work or what could we learn?

→ indirect information on $s_{1/2}$ moments through 5^- states !

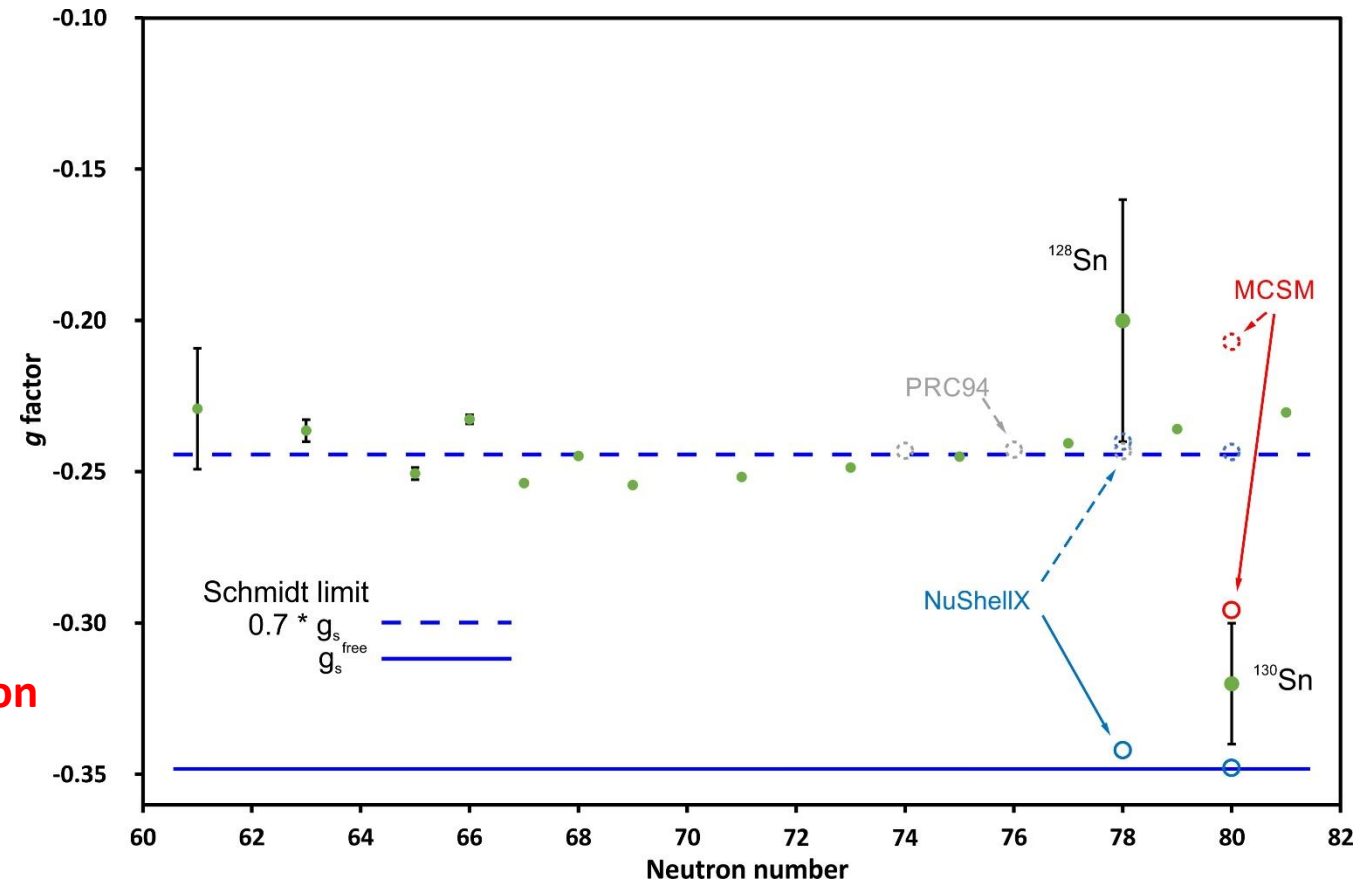
Unexpected results from RIKEN on $^{130}\text{Sn } 10^+$

- Gyromagnetic factors of the $11/2^-$ states (also including the 10^+ in ^{116}Sn) are quasi constant over the large range of neutron numbers. The only exception 10^+ in ^{128}Sn (reported with a large error-bar). They are all very close to the effective Schmidt line ($g_s = 0.7 * g_s^{\text{free}}$)
- Different theoretical calculations reproduce those, using effective g factors.
- **10^+ state in ^{130}Sn should have the most pure configuration** (high spin; no possible mixing below the shell closure)



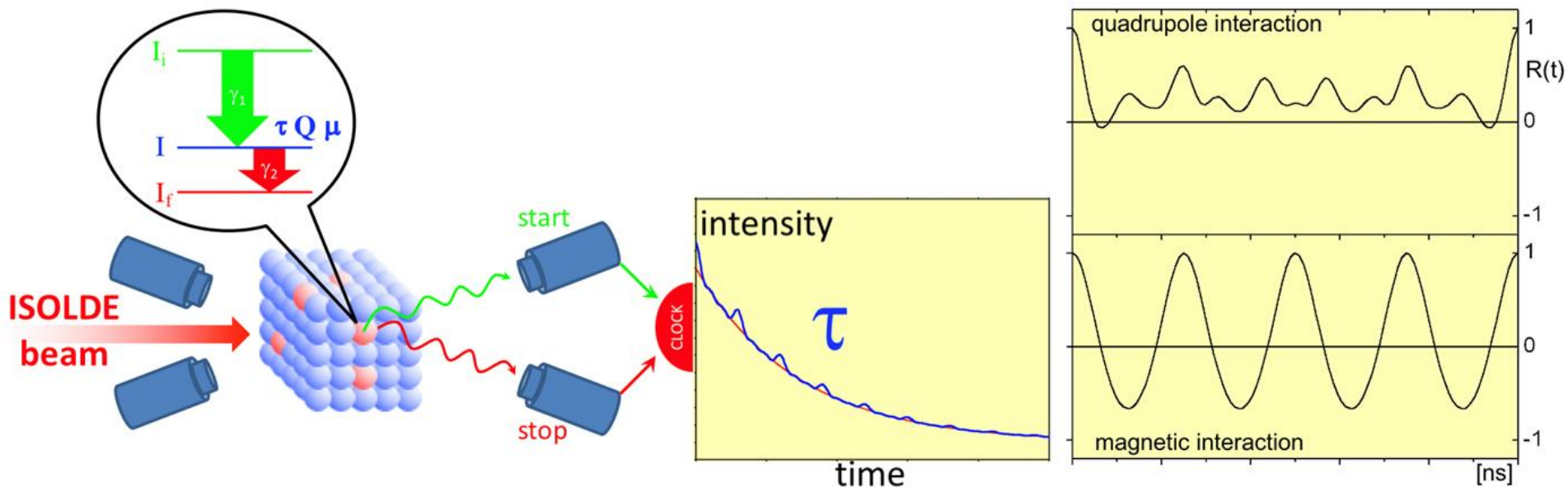
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- A recent study at RIBF, RIKEN of the 10^+ isomer in ^{130}Sn indicates a g factor very close to the **free Schmidt value**. **Is this another example that the “effective values” are due to shortcomings in theory rather than having any robust physical meaning?** (see e.g. P. Gysbers et al., *Nature Physics* 15, 428 (2019))
- **The unexpected RIKEN result (done with very poor statistics) needs reconfirmation beyond any doubts!**

The on-line PAC technique



From the experimental perturbation pattern one extracts

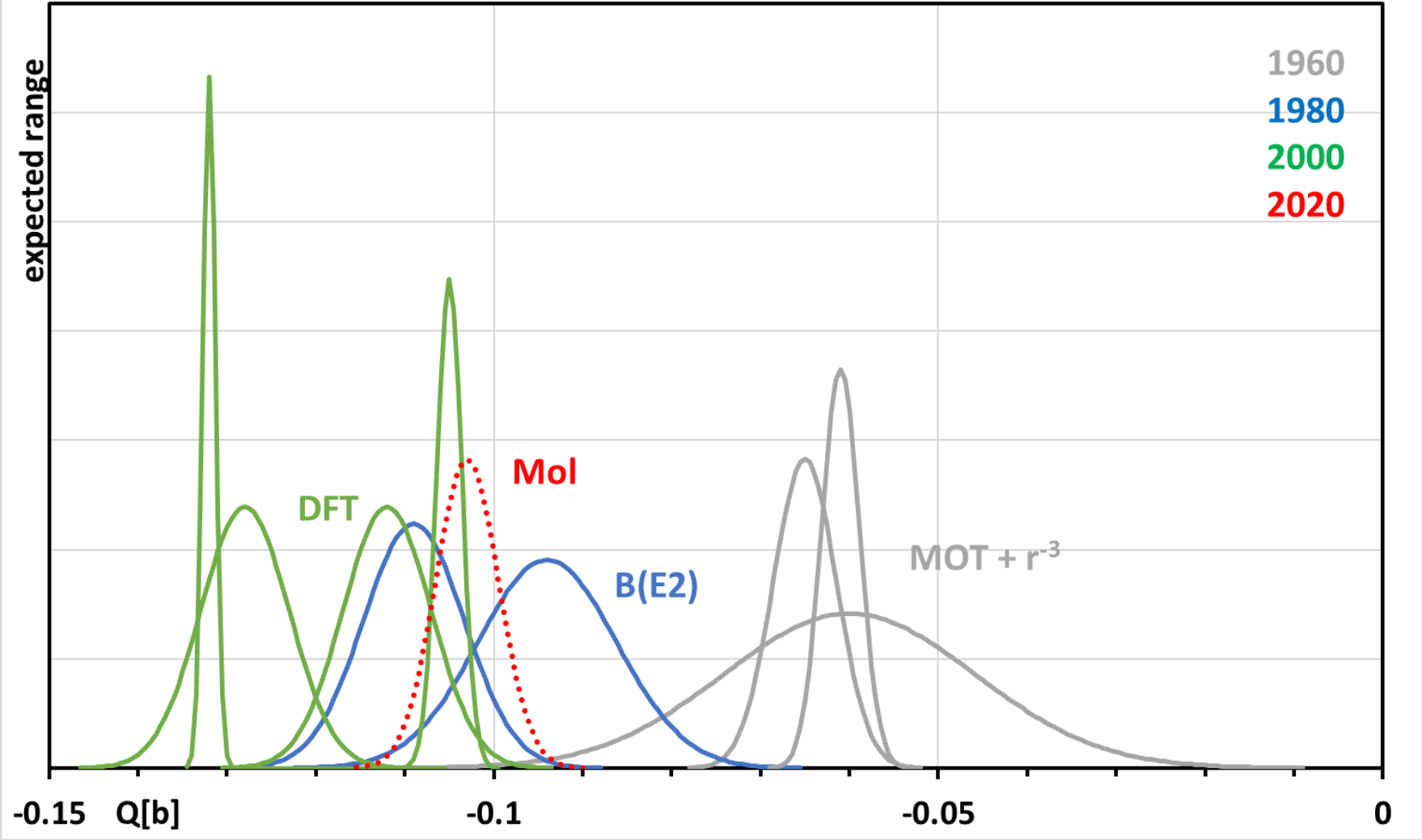
$$\nu_L = \mu / I * B / h$$

Magnetic field B from external magnet or ferromagnetic solid

$$\nu_Q = e Q * V_{zz} / h$$

Electric field gradient V_{zz} in non-cubic solid (from theory!) or reference isotope

Reference Q (¹¹⁹Sn 3/2⁺) history



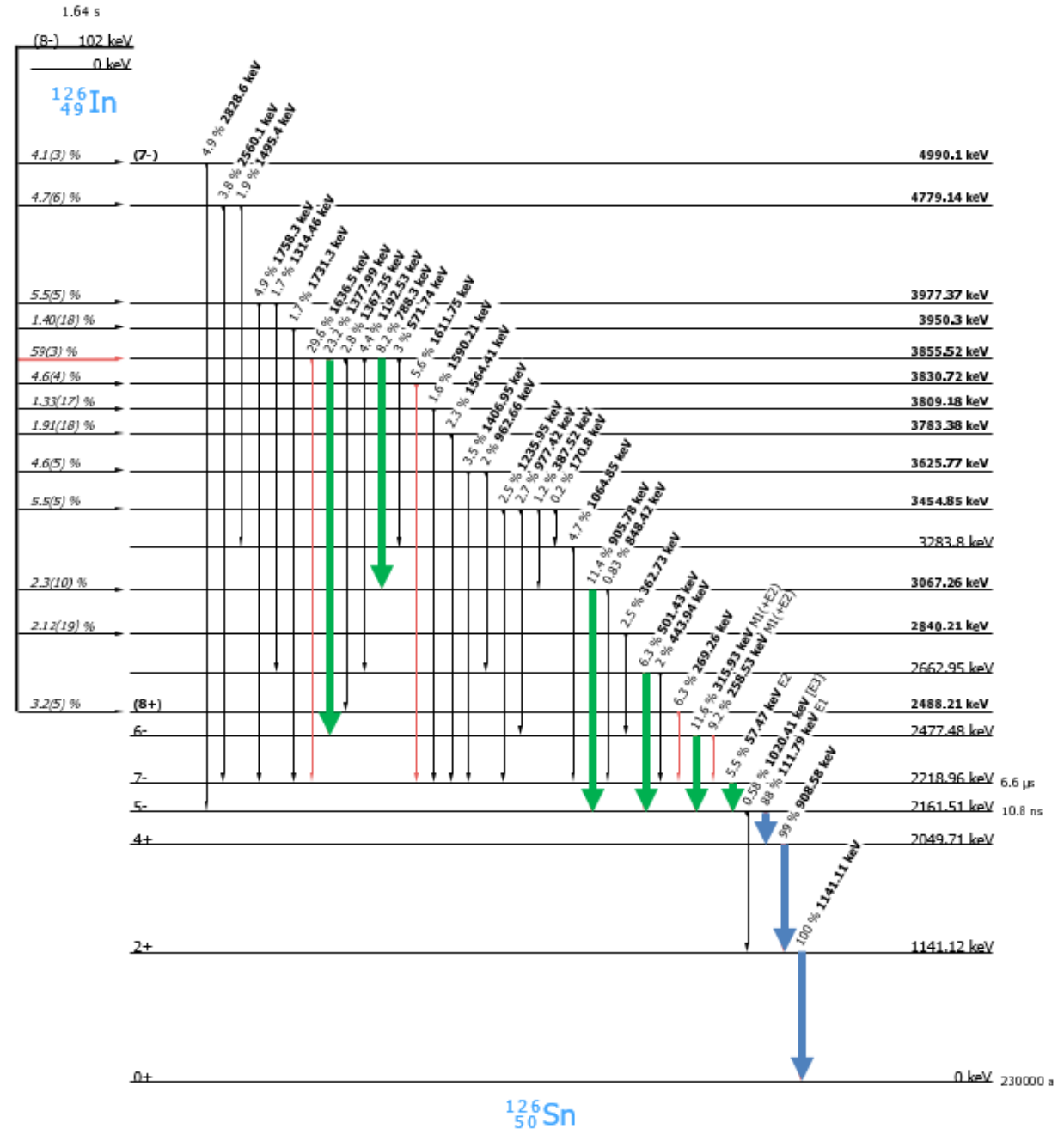
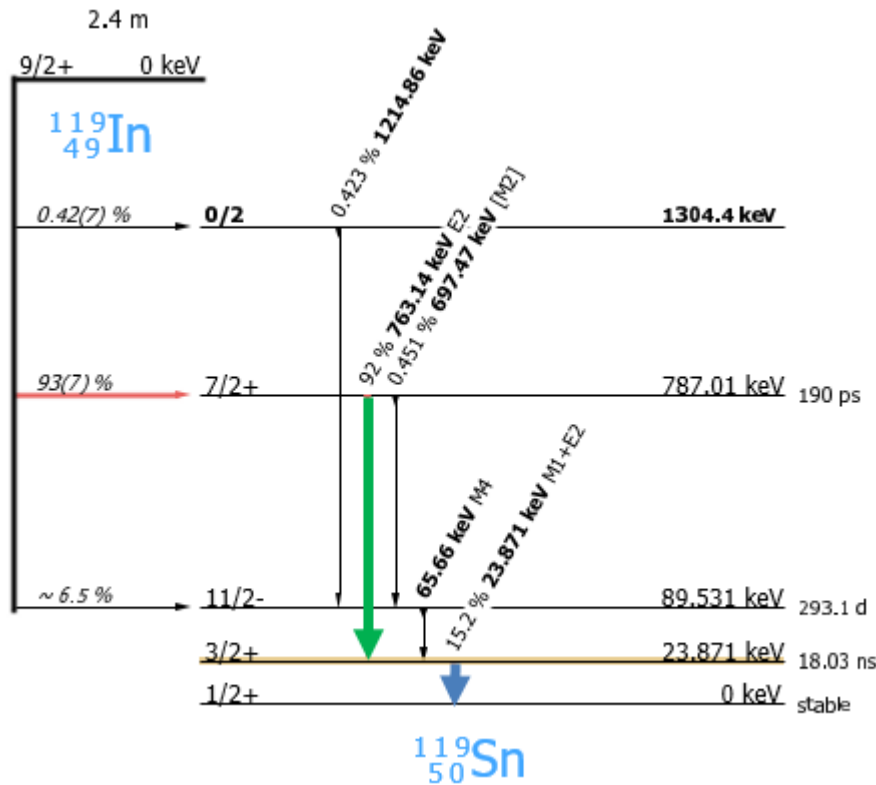
We shall clear up most of this mess !

Complex decay scheme

requires multi-dimensional on-line storage and off-line analysis

Simple decay scheme

for testing of target materials and effects of implantation damage



The test program using $^{119}\text{In} \rightarrow ^{119}\text{Sn } 3/2^+$

Experiment:

Test indium implantation into Zn single crystal, study damage effect as function of temperature

Measure precision value for QI at one optimal T

Test indium implantation into graphite or alternatives S, Se

Check effect of implantation damage in Fe at RT

Purpose:

Find optimal temperature for on-line experiments with 5^- states

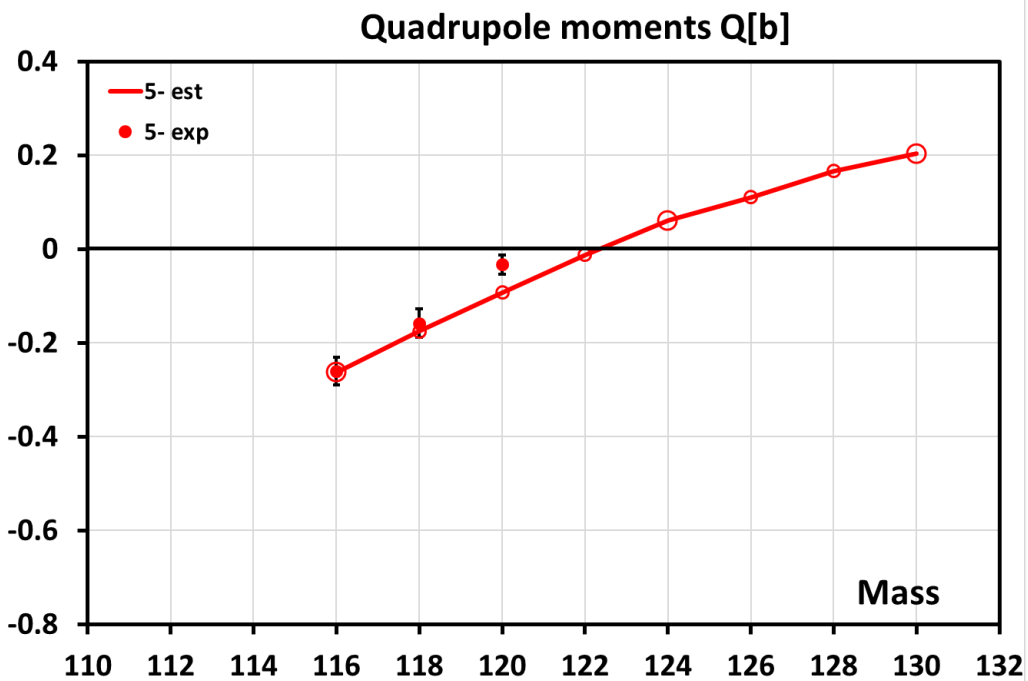
Find Q ratio to $^{116}\text{Sn } 5^-$

Find optimal matrix for short-lived 5^- cases

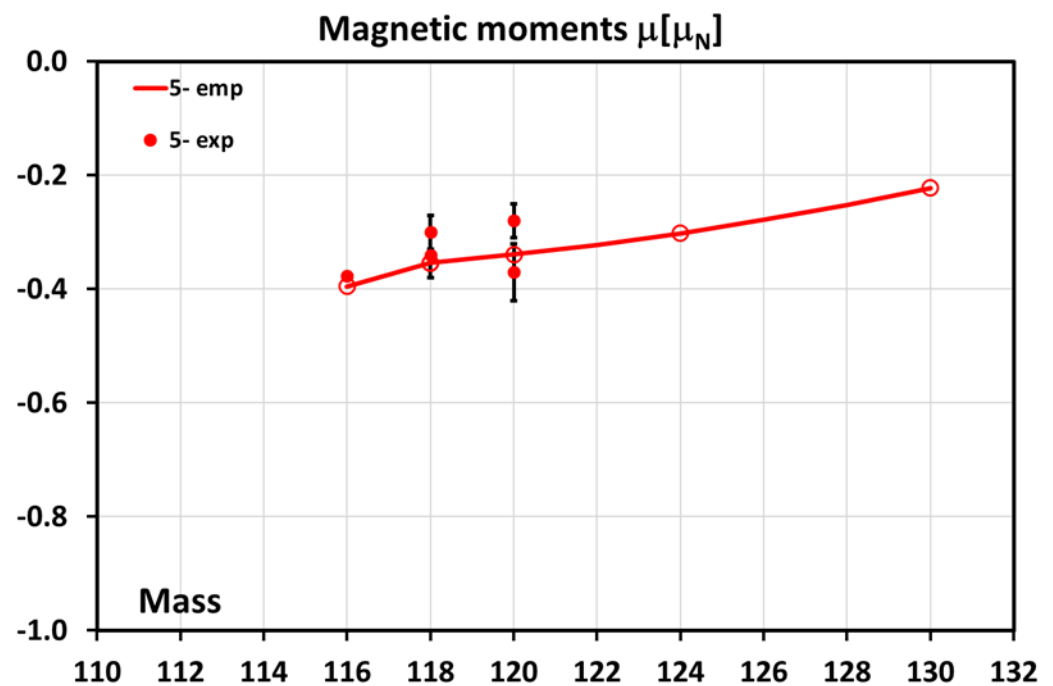
Understand origin of spectral damping

The 5⁻ states

Quadrupole moments expected identical to 11/2⁻ state in $A+1\text{Sn}$

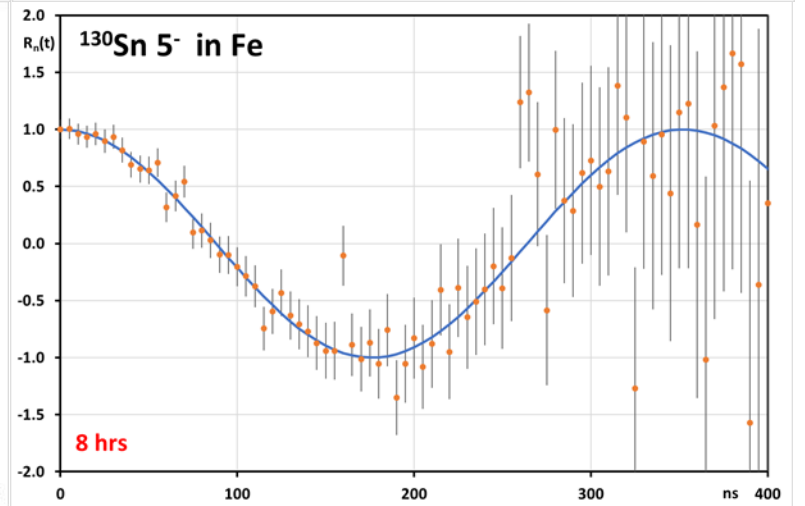
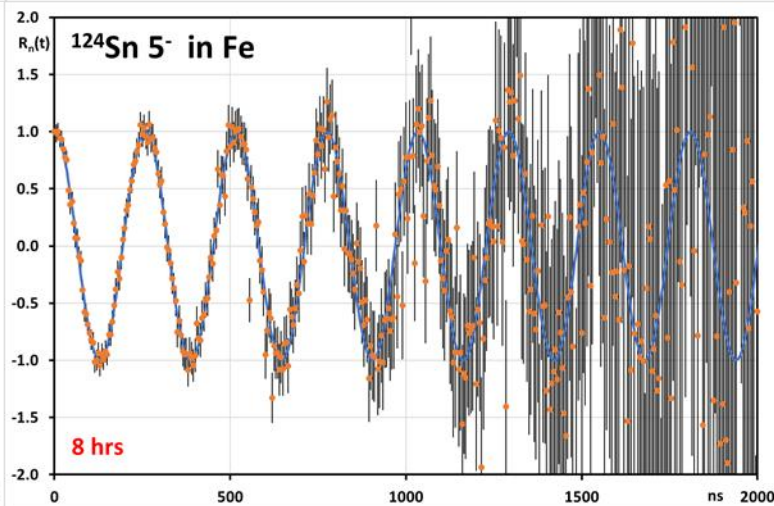
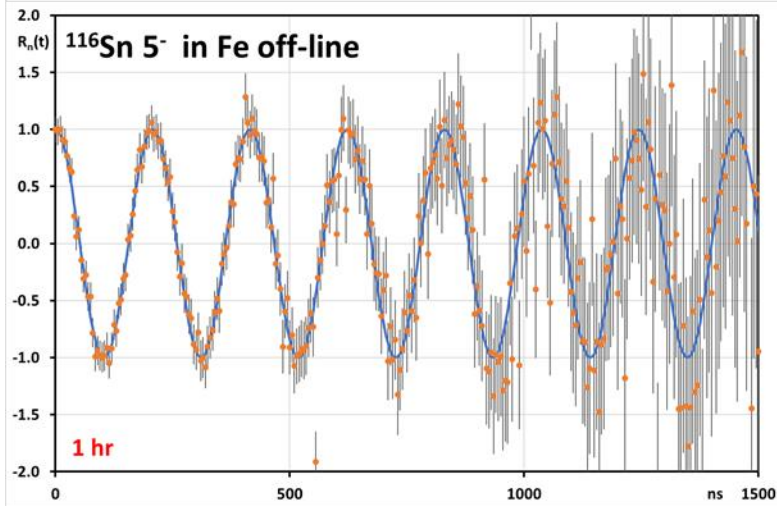
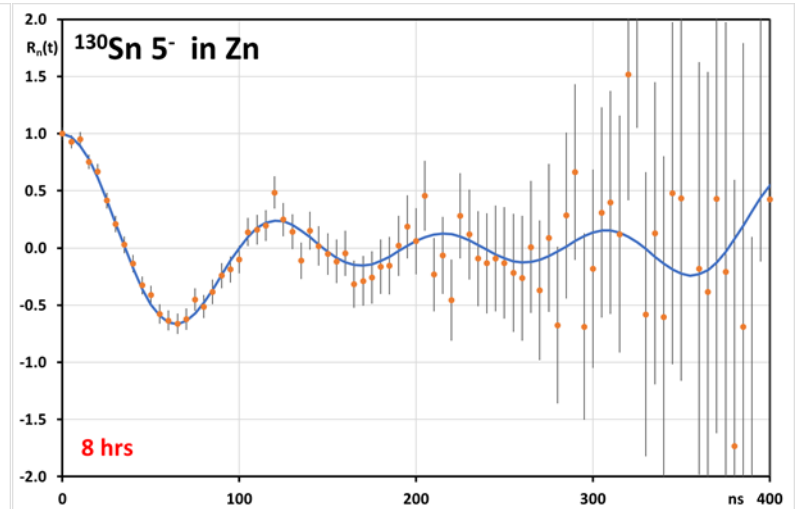
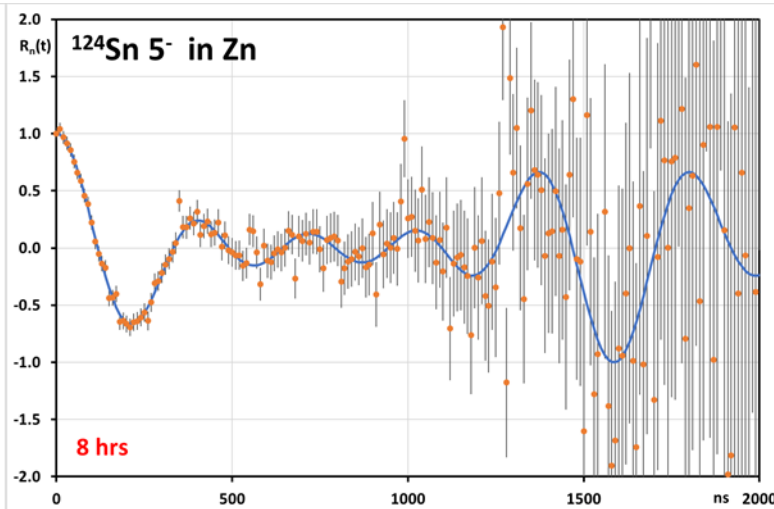
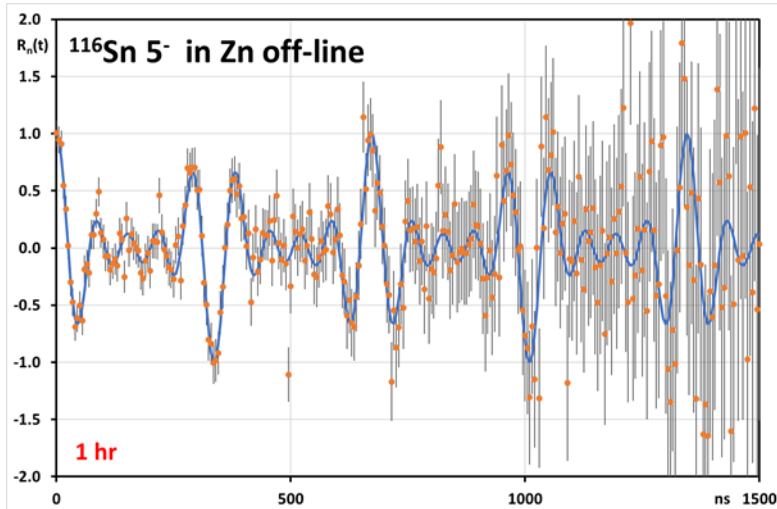


Magnetic moments as coupling of $\mu(11/2^-)$ and $\mu(1/2^+)$ in $A+1\text{Sn}$



Simulated spectra for long-lived 5⁻ states

note different running times!



The off-line program for 5^- states with Sb sources using 4-5 existing PAC spectrometers of solid-state collaboration

QI (temperature) for ^{116}Sn in Zn after annealing (at least 2 points)

QI for ^{116}Sn in In for precise V_{zz}

QI for ^{118}Sn in Zn for precise Q

Test implantation of ^{118}Sb into graphite

QI for ^{120}Sn in graphite to obtain Q

MI at RT for ^{116}Sn in Fe after annealing for precise B_{hf}

MI for ^{116}Sn in Ni at 200C

MI for ^{118}Sn in Fe for precise μ

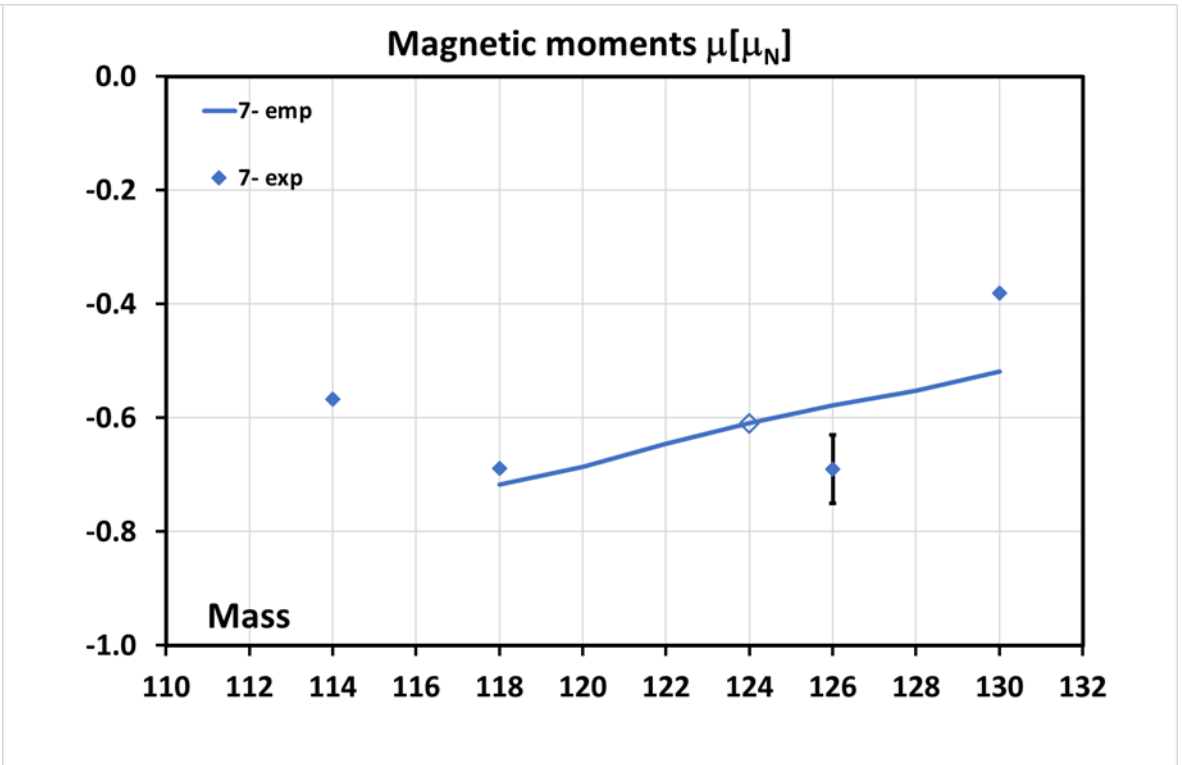
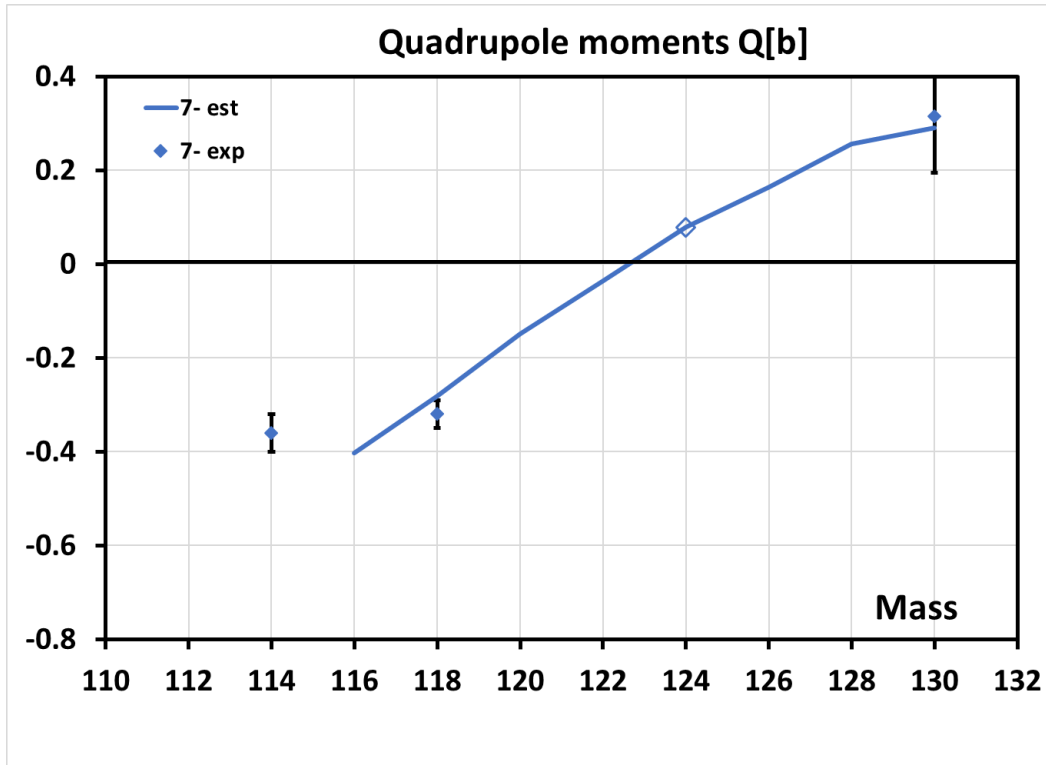
Test implantation of ^{118}Sb into Gd

MI for ^{120}Sn in Gd to obtain μ

The 7⁻ states

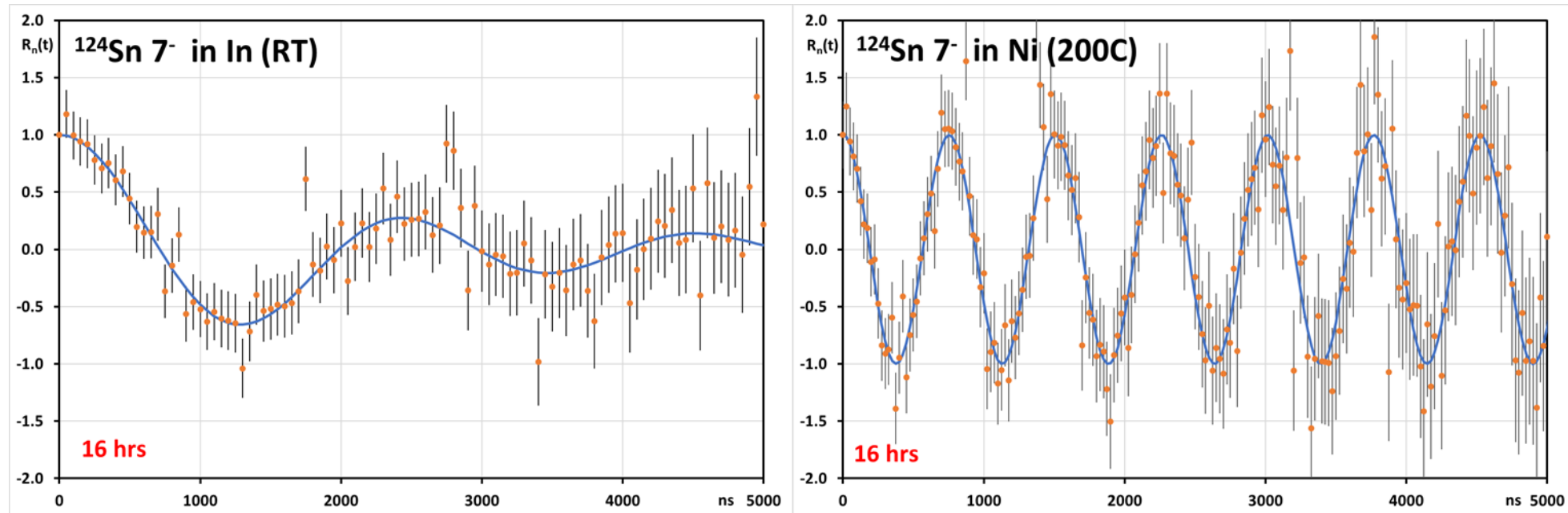
Quadrupole moments as coupling of
 $Q(11/2^-)$ and $Q(3/2^+)$ in $A^{+1}\text{Sn}$

Magnetic moments as coupling of
 $\mu(11/2^-)$ and $\mu(3/2^+)$ in $A^{+1}\text{Sn}$



Simulated spectra for long-lived 7^- state in ^{124}Sn

A fortunate case: Due to small Q expected and favorable decay characteristics PAC feasible in spite of long $t_{1/2}$ ($3.1 \mu\text{s}$)

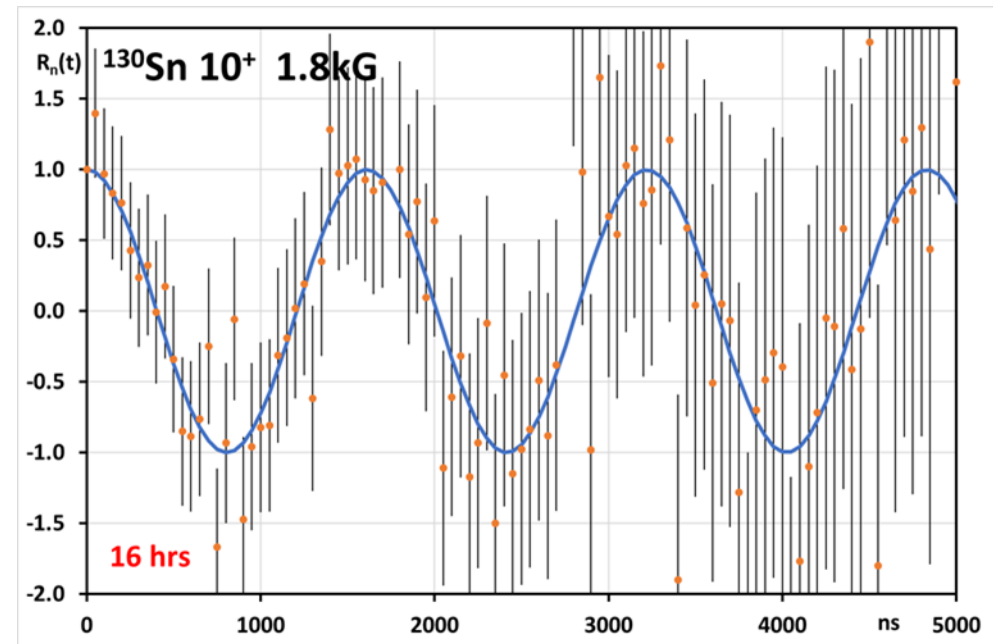
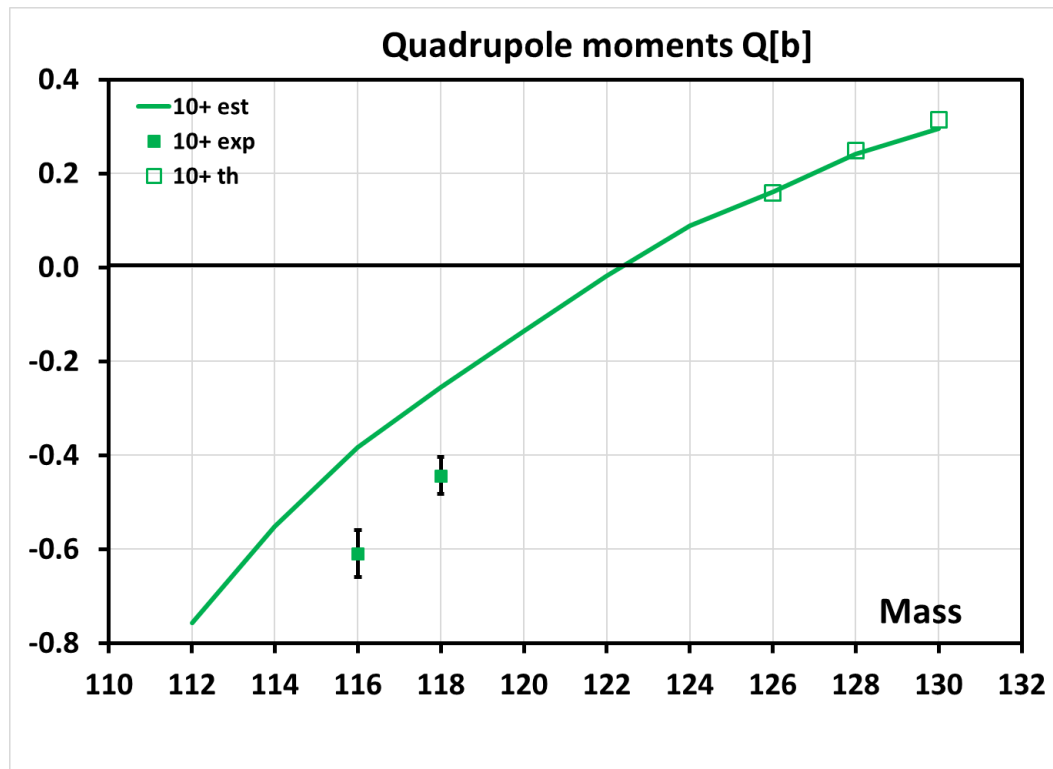


10^+ state in ^{130}Sn

- Should have a very pure $h_{11/2}^2$ configuration
 - Also 8^+ state will be virtually pure $h_{11/2}^2$
- B(E2) will give the most precise value for Q
- Thus: Measuring QI (in In) for **new reference!**
- However: Difficult to estimate run time
- Therefore: Postpone until after MI experiment!

**Check of preliminary
RIKEN results for μ :**

**Simulated spectrum for
measurement in magnet**



Acceptable accuracy reachable!

Required beamtimes

On-line

ISOLDE beam, UC/RILIS					State of interest			Experiment		
	lp	t1/2 [s]	Approx. int. [at/ μ C]	Required int. [at/sec]		lp	t1/2 [ns]	measure	host	shifts
^{119}In	9/2 ⁺	144	4x10 ⁷	2x10 ⁶	^{119}Sn	3/2 ⁺	18	Q, μ	Zn,C,S,Fe	3
$^{118\text{m}}\text{In}$	8 ⁻	8.1	5x10 ⁷	1x10 ⁶	^{118}Sn	5 ⁻	22	Q	C	1
$^{120\text{m}}\text{In}$	8 ⁻	47.3	5x10 ⁷	1x10 ⁶	^{120}Sn	5 ⁻	5.5	Q	C	1
$^{122\text{m}}\text{In}$	8 ⁻	11	2x10 ⁸	1x10 ⁶	^{122}Sn	5 ⁻	7.9	Q	C	1
$^{124\text{m}}\text{In}$	8 ⁻	3.7	4x10 ⁷	1x10 ⁶	^{124}Sn	5 ⁻	270	Q, μ	Zn,Fe	2
$^{126\text{m}}\text{In}$	8 ⁻	1.6	7x10 ⁶	1x10 ⁶	^{126}Sn	5 ⁻	11	Q	C	1
$^{128\text{m}}\text{In}$	8 ⁻	0.72	3x10 ⁶	1x10 ⁶	^{128}Sn	5 ⁻	8.6	Q	C	1
$^{130\text{m}}\text{In}$	5 ⁺	0.54	1x10 ⁵	2x10 ⁵	^{130}Sn	5 ⁻	52	Q, μ	Zn,Fe	4
^{132}In	7 ⁻	0.2	1x10 ⁴	4x10 ⁴	^{132}Sn	6 ⁺	21.3	μ	Fe	2
$^{124\text{m}}\text{In}$	8 ⁻	3.7	4x10 ⁷	5x10 ⁵	^{124}Sn	7 ⁻	3100	Q, μ	In,Ni	4
$^{130\text{m}}\text{In}$	10 ⁻	0.55	1x10 ⁵	2x10 ⁵	^{130}Sn	10 ⁺	1610	μ	Cu	3

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Off-line

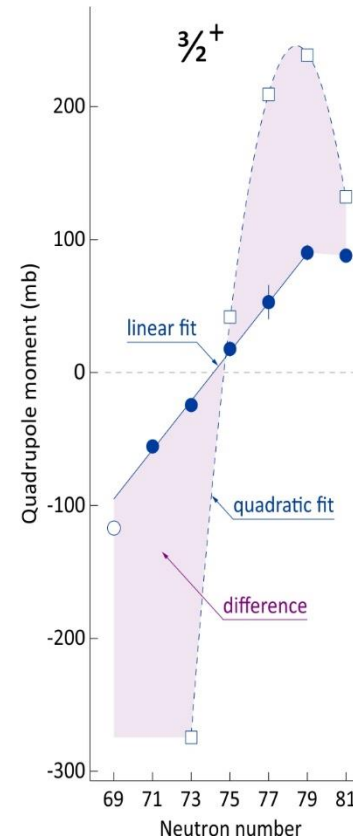
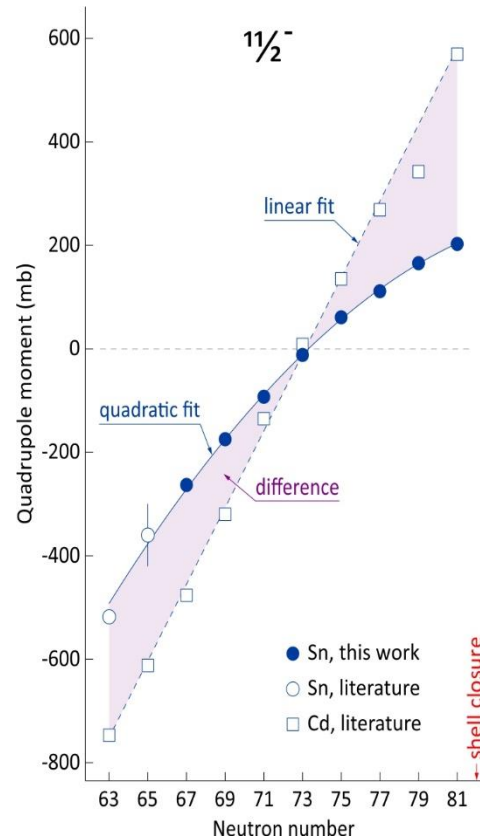
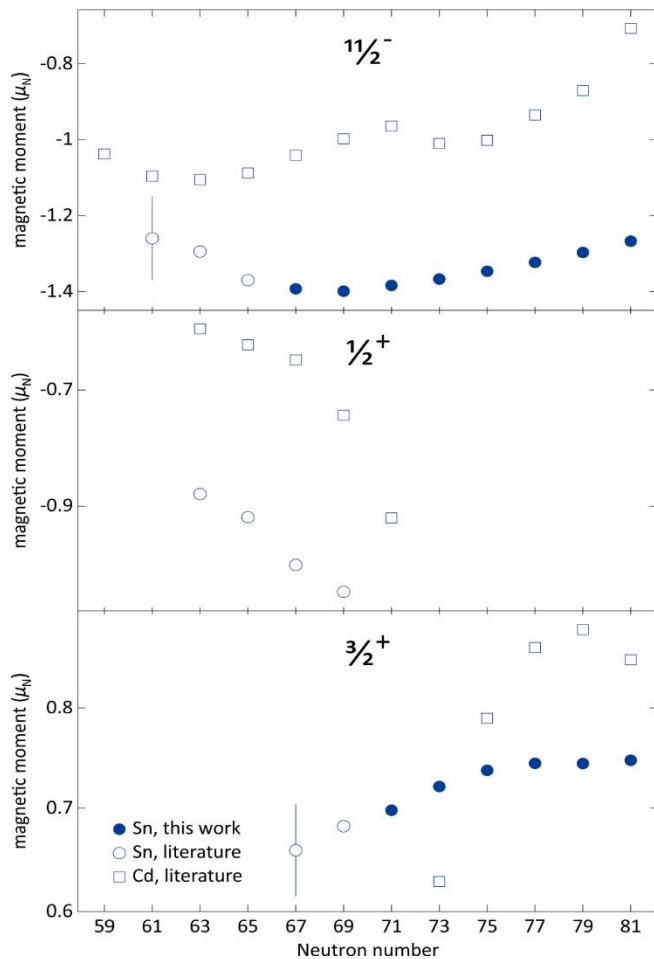
$^{116\text{m}}\text{Sb}$	8 ⁻	1h	5x10 ⁷	2x10 ^{10a)}	^{116}Sn	5 ⁻	320	Q, μ	Zn,In,Fe,Ni	2
$^{118\text{m}}\text{Sb}$	8 ⁻	5.1h	1x10 ⁸	4x10 ^{10a)}	^{118}Sn	5 ⁻	22	Q, μ	Zn,C,Fe,Gd	1
^{120}Sb	8 ⁻	5.8d	2x10 ⁸	2x10 ^{11a)}	^{120}Sn	5 ⁻	8	Q	C,Gd	1

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Slides for discussion

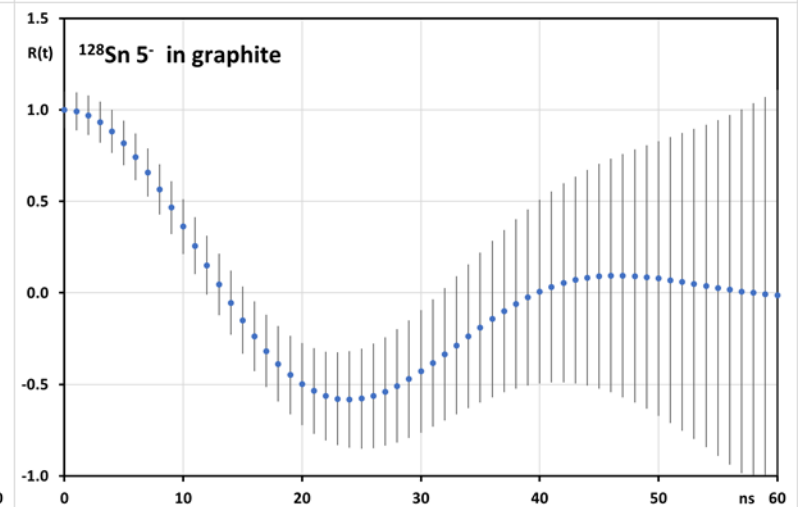
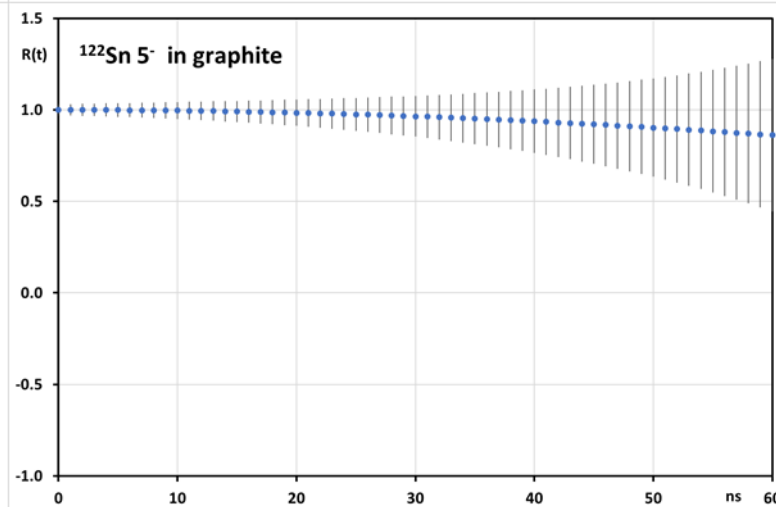
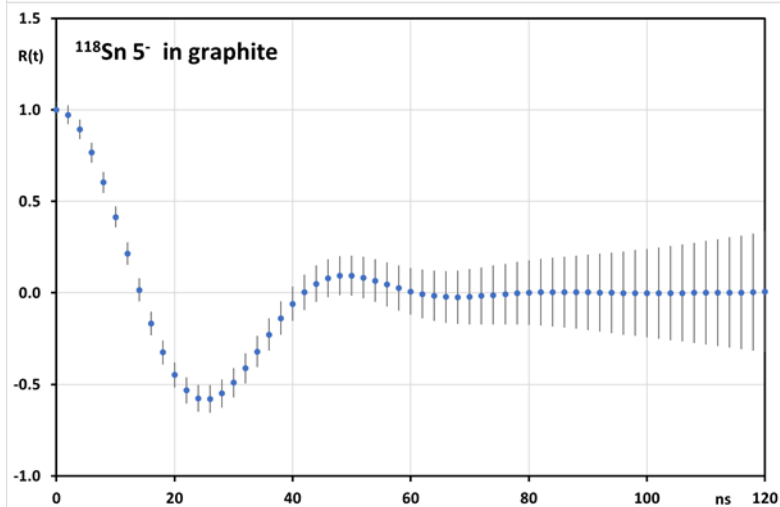
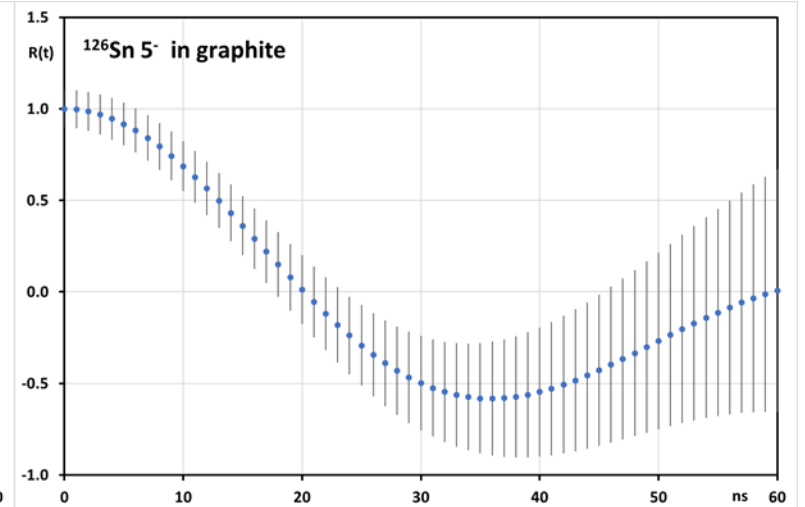
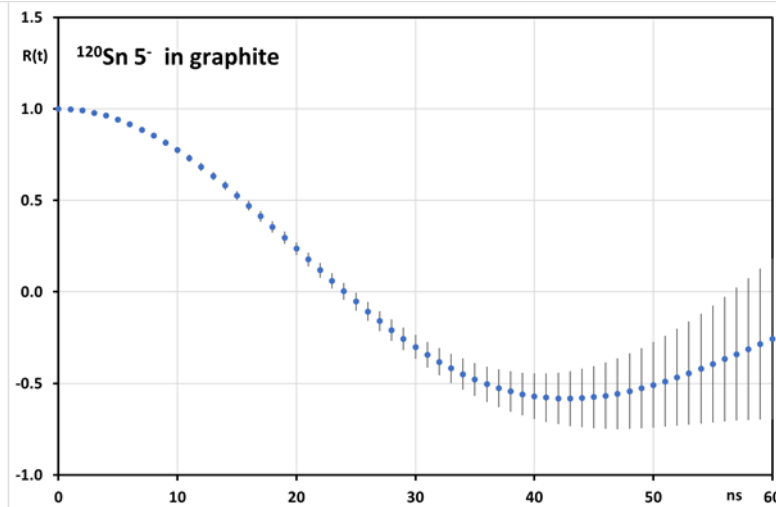
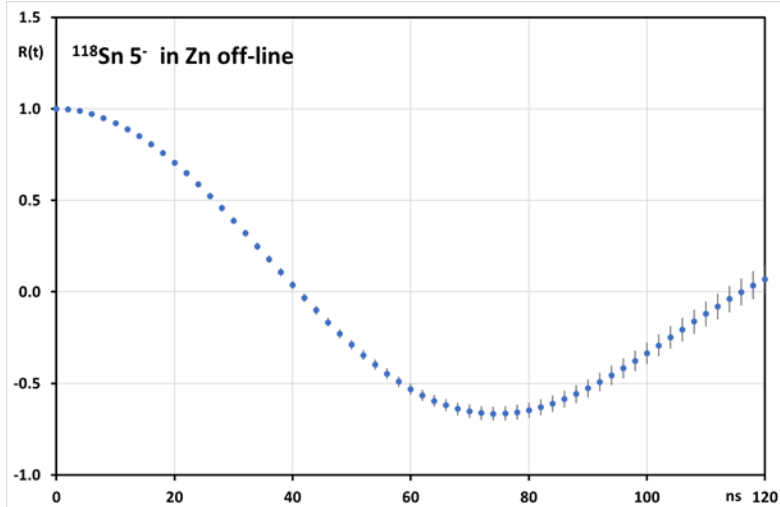
Sn results from COLLAPS

- Recent results from laser spectroscopy of odd-mass Sn isotopes from COLLAPS: ***D.T. Yordanov et al., Comm. Phys. 3, 107 (2020)*** – magnetic and quadrupole moments and r.m.s. radii for odd-mass Sn isotopes

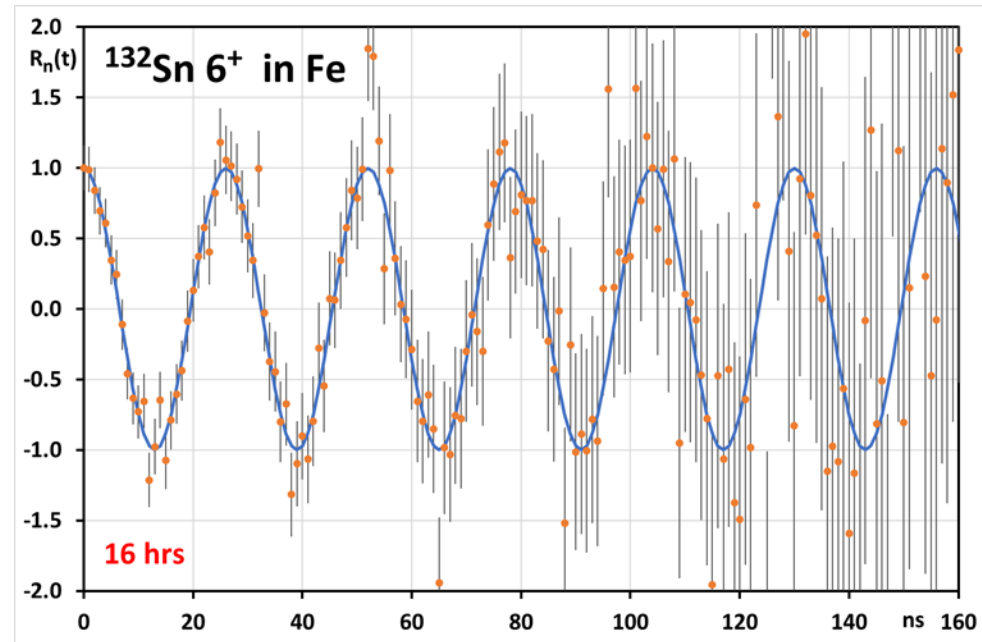


- The magnetic and the quadrupole **moments of the s.p. states** have been determined!
- Our aim – **test the additivity rule for a chain of semi-magic (Sn) nuclei** → does the **simple SM picture** work or what could it teach us?

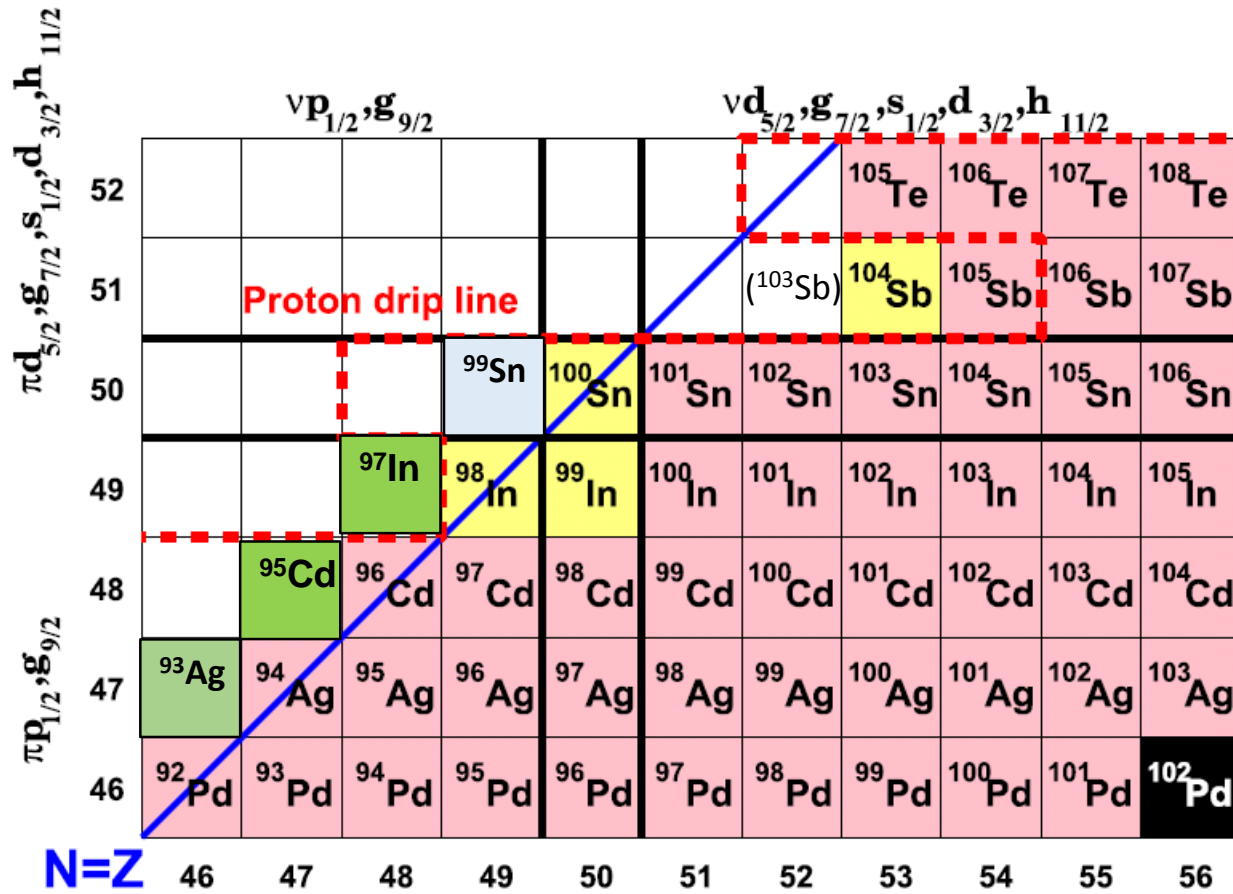
Expected spectra for short-lived 5⁻ states



Simulated spectrum for 6^+ state in ^{132}Sn



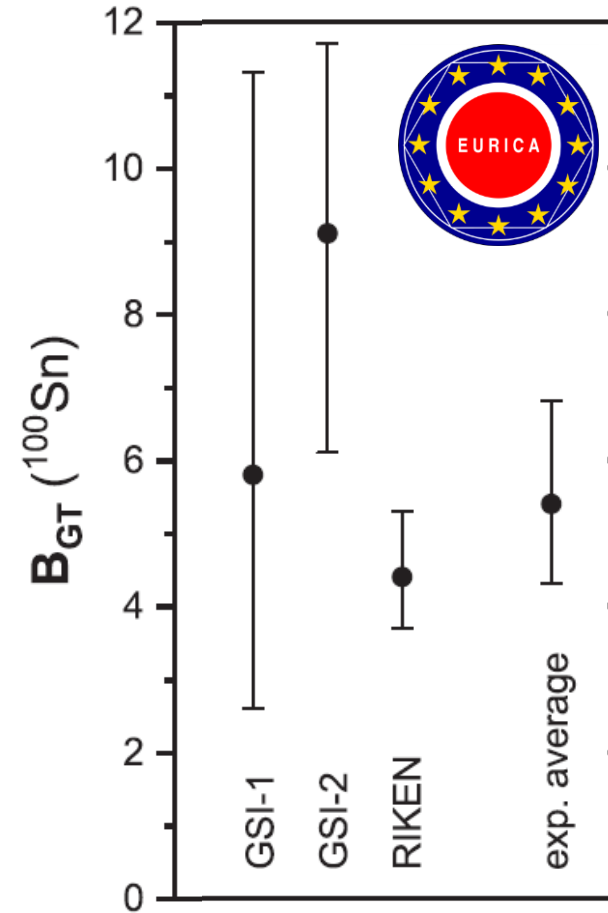
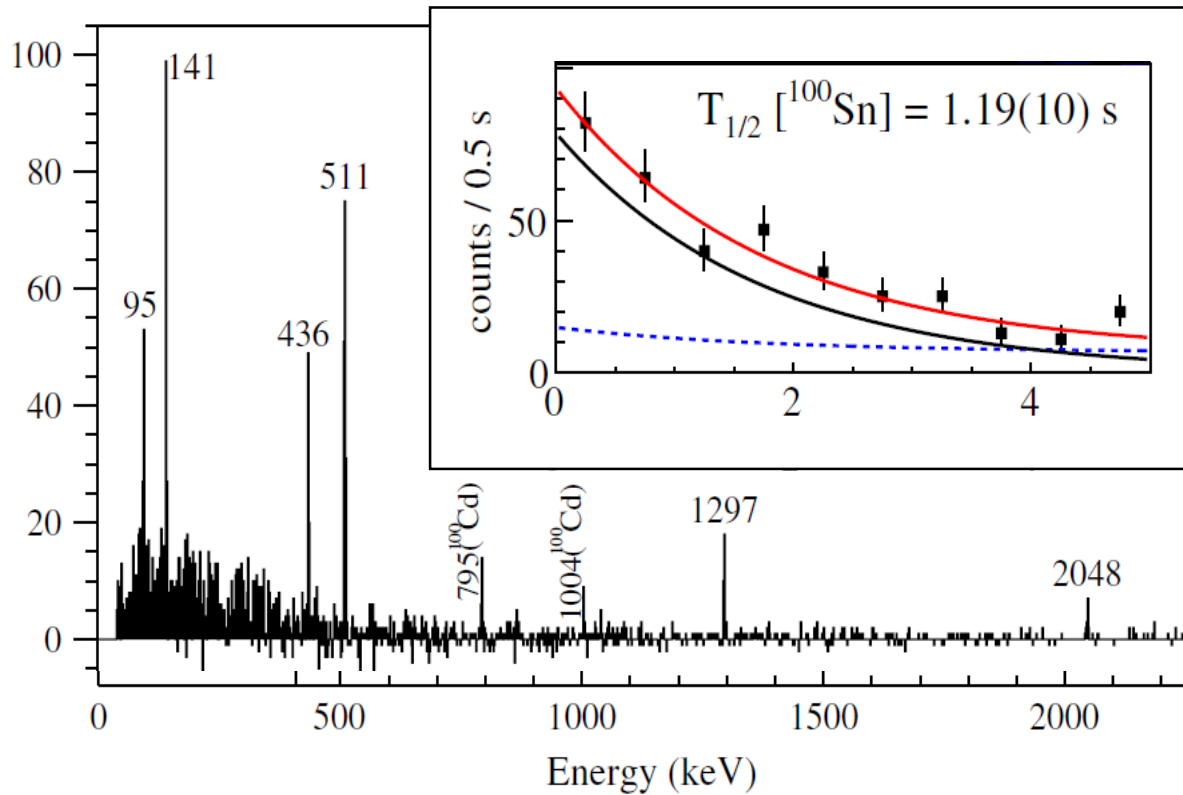
Gamow-Teller β decay of ^{100}Sn ($Z, N=50$)



D. Lubos *et al.*, Phys Rev. Lett. 122, 222502 (2019)

P. Gysbers *et al.*, Nature Physics 15, 428 (2019)

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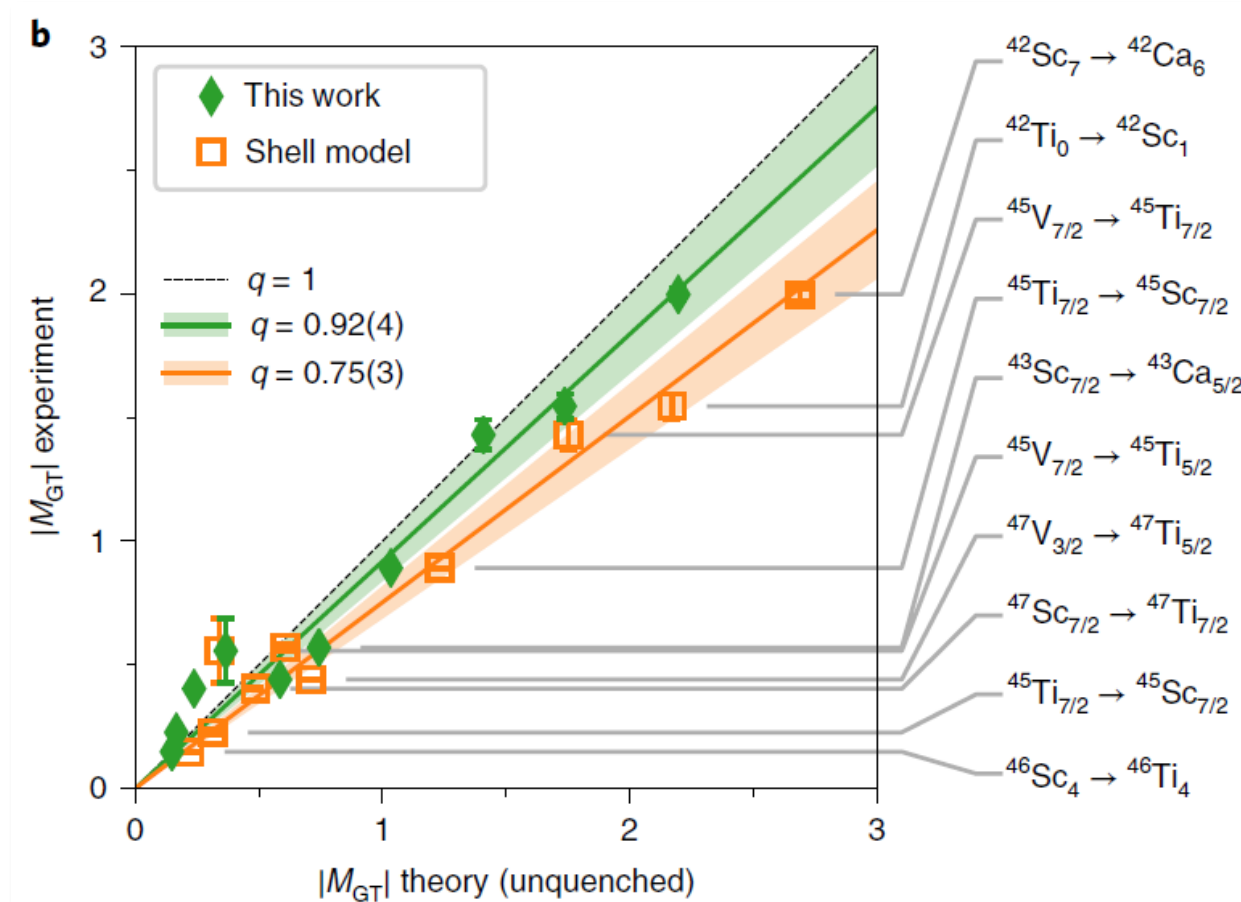


D. Lubos *et al.*, Phys Rev. Lett. 122, 222502 (2019)

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Gamow-Teller β decay of ^{100}Sn ($Z, N=50$)

- Discrepancy between exp. and theoretical β decay rates, $g_A(1,27)$ quenched ~ 0.75 (e.g. Towner “Quenching of spin matrix elements in nuclei” Phys. Rep. 155 (1987)), *is without first-principle explanation*
- Combining EFT of the strong and the weak forces with quantum many-body techniques explains the discrepancy



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