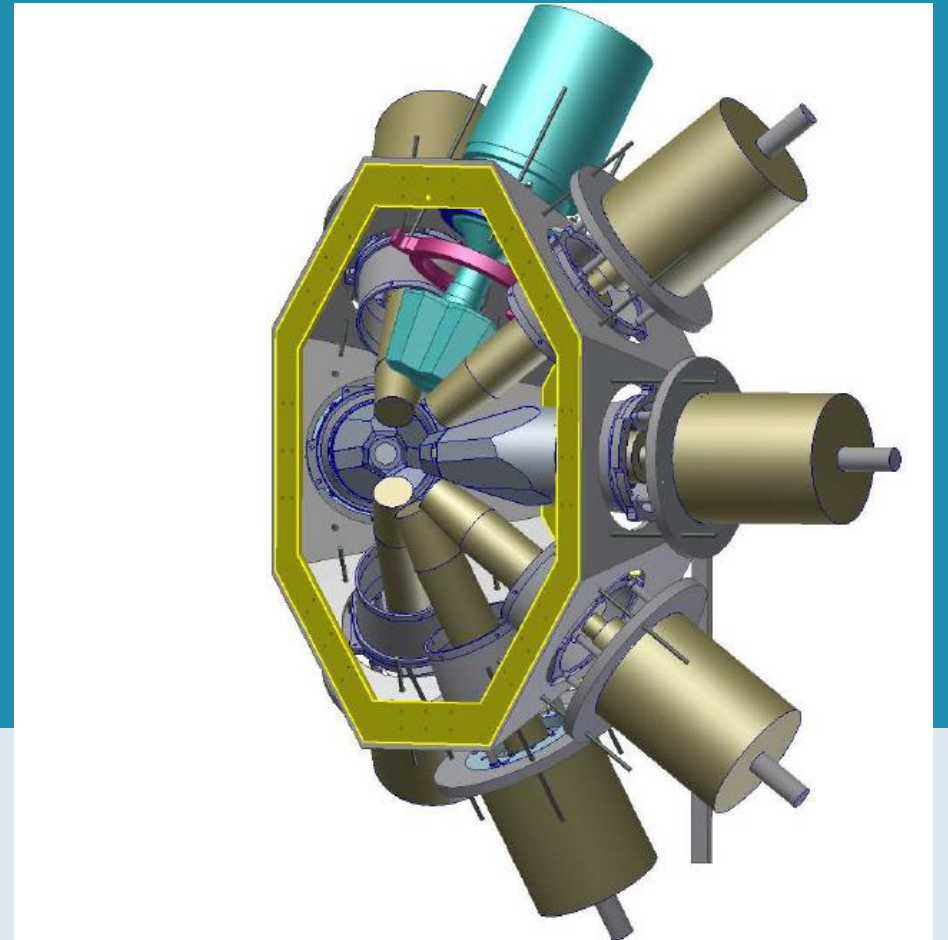


Absolute charge radii of radioactive isotopes measured by muonic x-ray spectroscopy at PSI

Proposal INTC-P-552 – 24 June 2020

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Atomic isotope shifts as measured in ISOLDE

ν , A and ν are experimental observables,
while $\delta\langle r^2 \rangle$ is the nuclear parameter of interest.

$$\delta\nu^{AA'} = \frac{A' - A}{AA'} \left(m_e \nu + M_{SMS} \right) + F \delta\langle r^2 \rangle^{AA'}$$

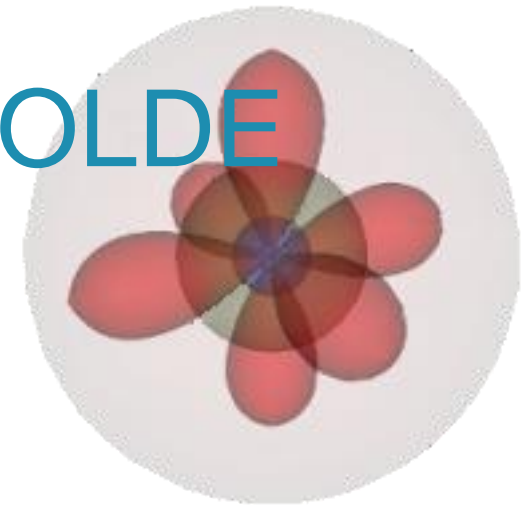
Mass shift

From one isotope to the next, the reduced mass of the nucleus + electron system varies, giving rise to a mass shift, scaling with A^{-2}

M & F are empirical parameters dependent on the transition. Their exact determination from first principles is only possible for systems up to 3 electrons.

Field shift

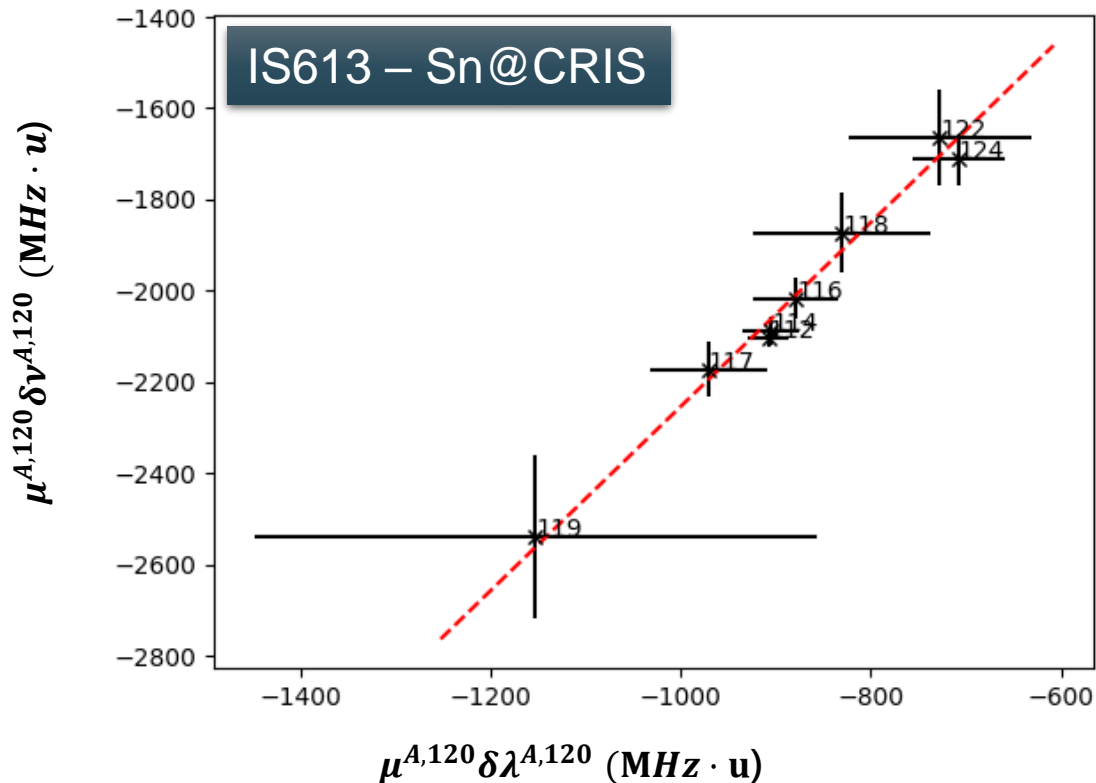
From one nuclear state to the next, the charge distribution within the nucleus may vary, perturbing electron orbitals with a non-vanishing overlap with the nucleus



Experimental approach: King plot

$$\mu_{AA'} = \frac{AA'}{A'-A}$$

$$\mu_{AA'}\delta\nu^{AA'} = M + F\mu_{AA'}\delta\langle r^2\rangle^{AA'}$$



- The modified isotope shifts are linearly proportional to the modified changes in the charge radii.
- The y-intercept and the slope give direct access to the atomic parameters.
- You need 2 points to draw a line, and a reference to determine a 'change' → 3 absolute radii

Measuring 3 absolute charge radii

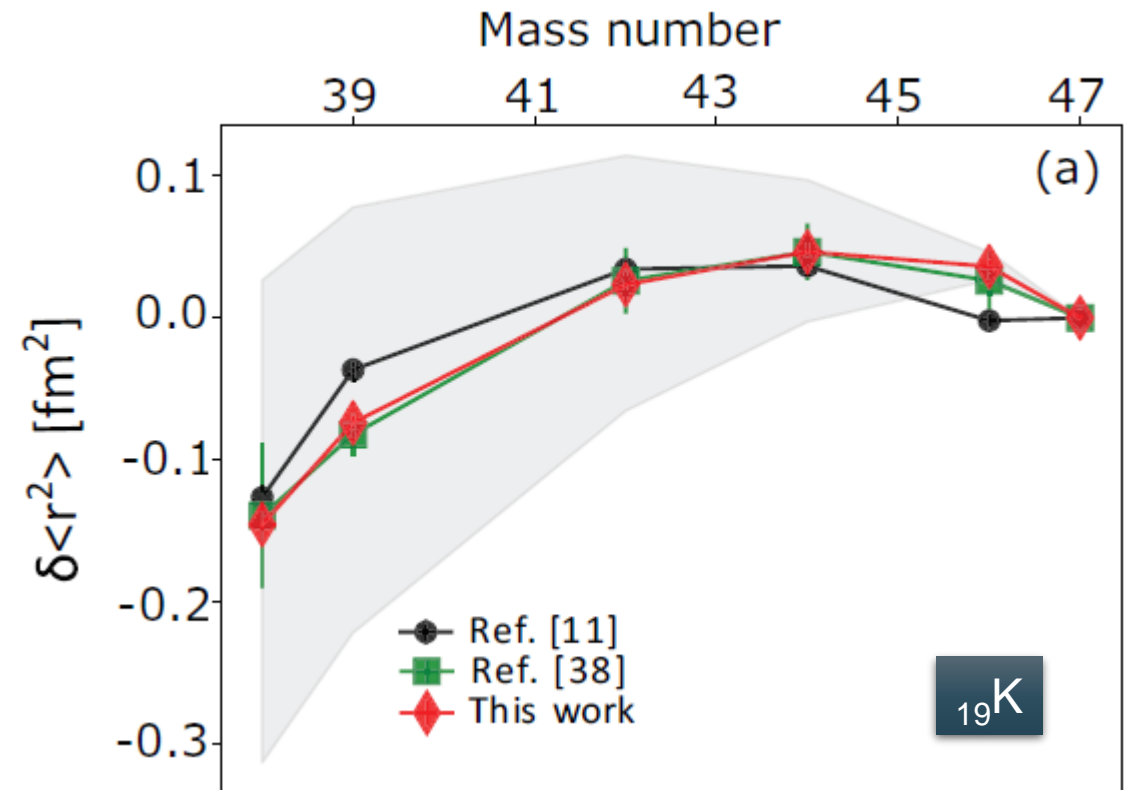
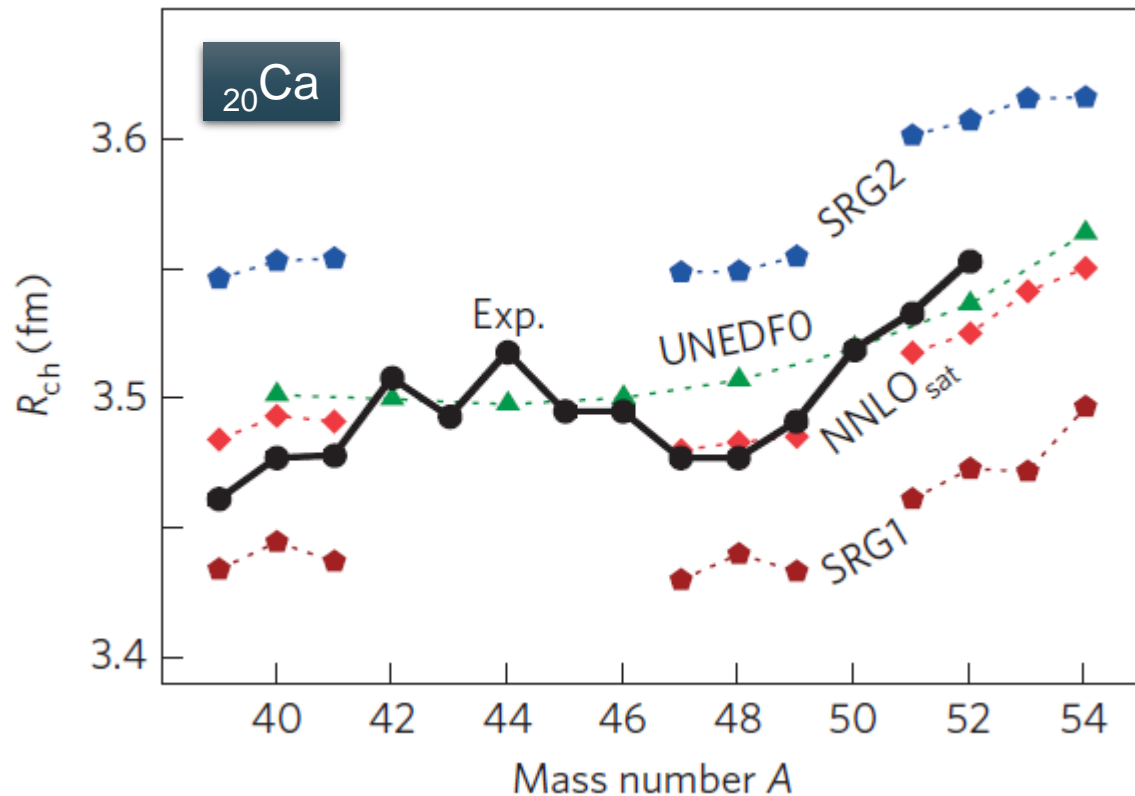
H	alkali &																		He
Li	Be	alkali-earth										B	C	N	O	F	Ne		
Na	Mg											Al	Si	P	S	Cl	Ar		
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr		
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe		
Cs	Ba	Lu	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn		
Fr	Ra	Lr	Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg	Cp								
		La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb				
		Ac	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No				

- There are **no odd-Z element with 3 stable isotopes** for the standard techniques (e.g. muonic x rays, electron scattering)
- Applying those techniques to **radioactive isotopes** is currently extremely limited:
 - ❑ **SCRIT@RIKEN**: electron scattering from photo-fission products;
 - ✓ **muX@PSI**: muonic x-ray spectroscopy of long-lived radioisotopes;
 - ❑ Absolute radii are best extracted from the combined analysis of both techniques.

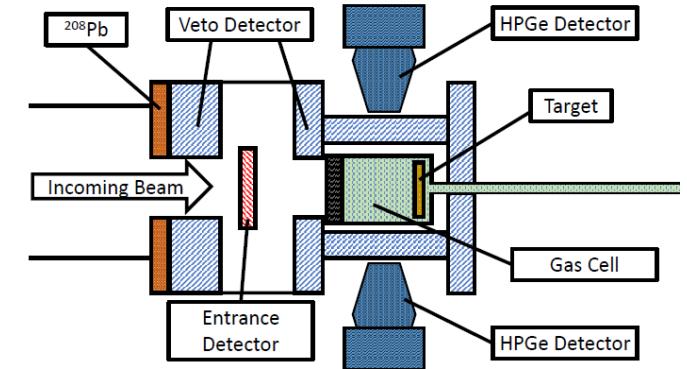
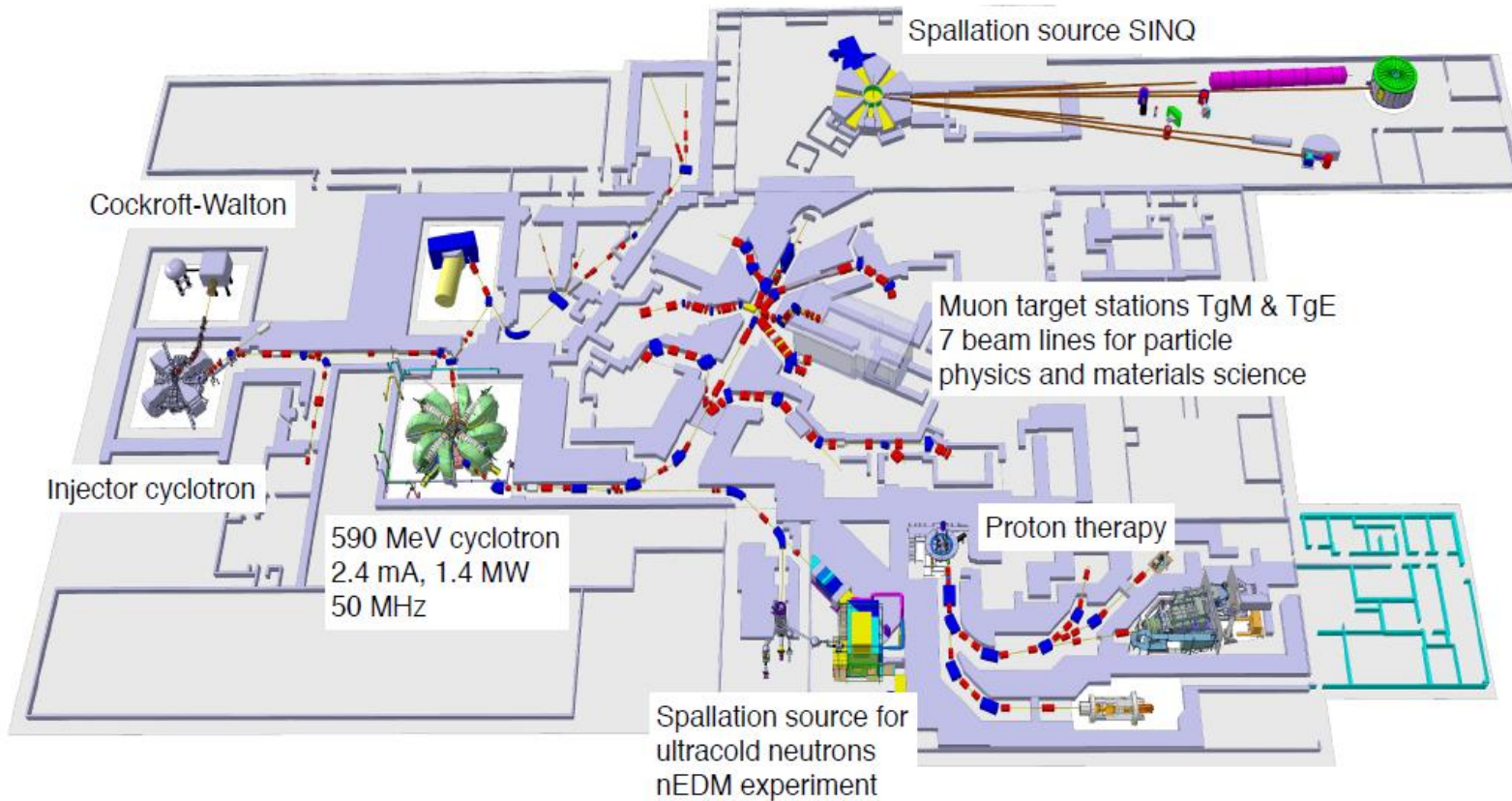
Combining the available ISOLDE isotopes with electron scattering would open many new possibilities

5 K. Tsukada et al, First elastic electron scattering from ^{187}Re , PRL 118 (2017) 262501.
 E. Rapisarda et al, Measurement of the quadrupole moment of ^{187}Re from the hyperfine structure of muonic X rays, Physical Review C 101 (2020) 054313.

Impact on the nuclear physics interpretation

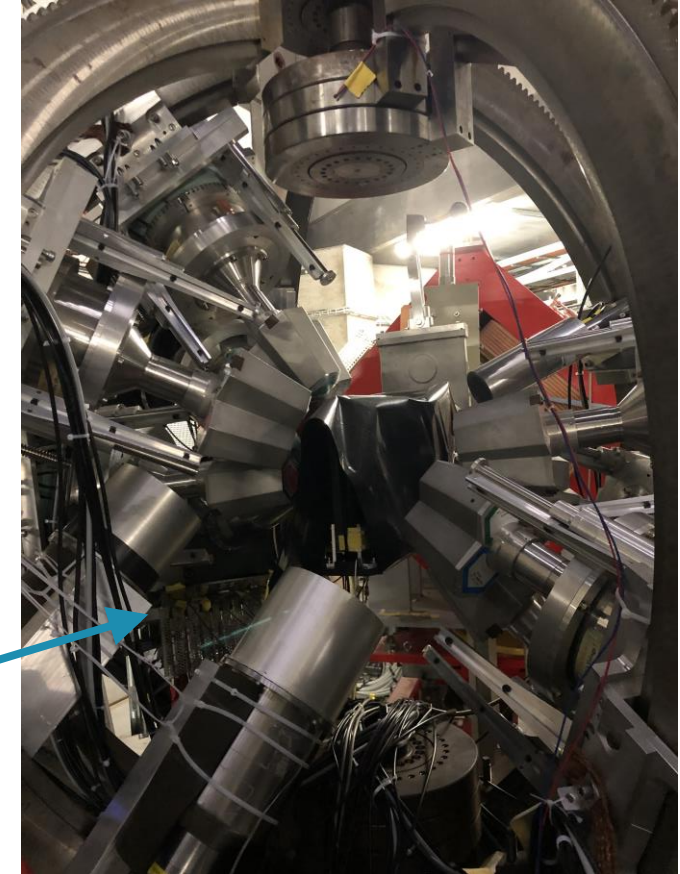
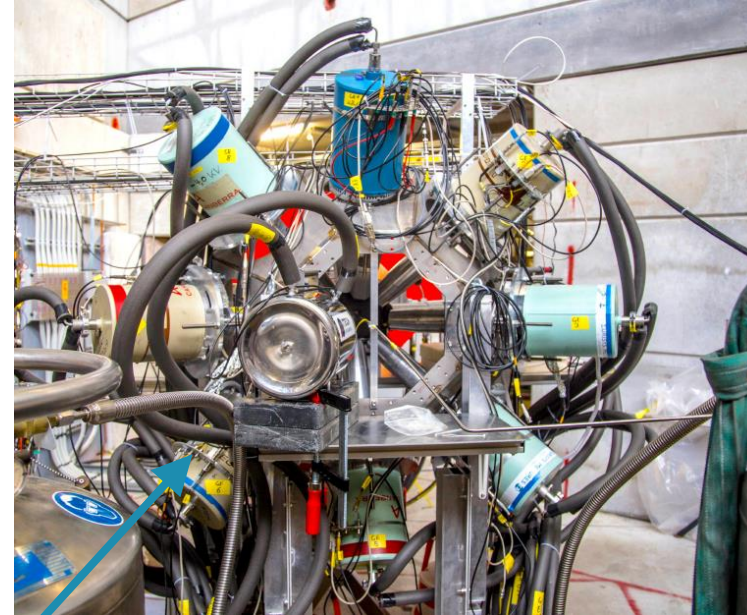
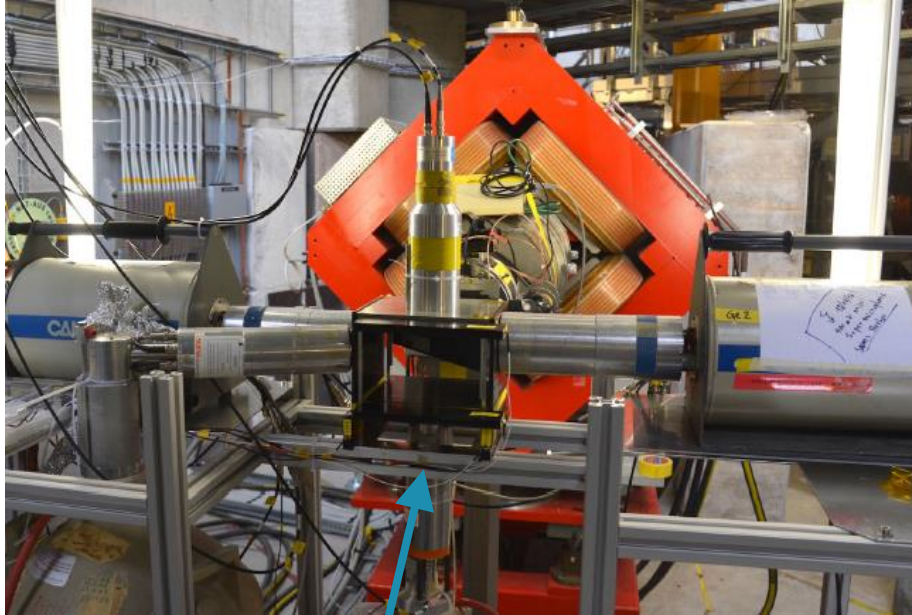


μ -atomic spectroscopy with muX@PSI



- A muon beam is delivered from the HIPA facility at PSI to the $\pi\text{E}1$ experimental area.
- The muon enters the experimental setup and is captured in a hydrogen gas cell, transferred to deuterium and eventually to the isotope of interest.
- The captured muon cascades down towards the ground state and the emitted x-rays are monitored with the Ge detector array

μ -atomic spectroscopy with muX@PSI



- 2016: 2 HPGe (Leuven & PSI)
- 2017/18: the Death Star Array: 1 MiniBall Cluster (Leuven)
- + detectors from PSI and the gamma loan pool (Orsay)
- 2019: MiniBall@PSI campaign
- 2021 and beyond: back to the Death Star Array but seeking better detectors

First measurement: $^{185,187}\text{Re}$

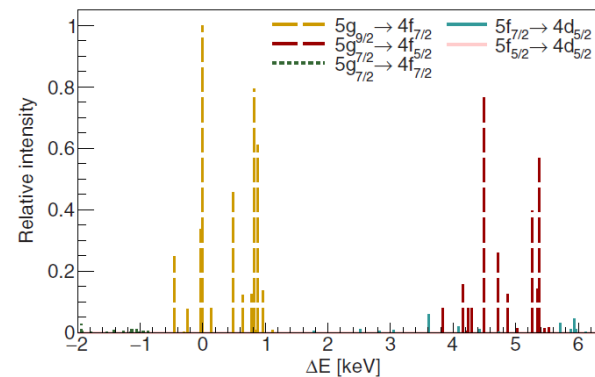
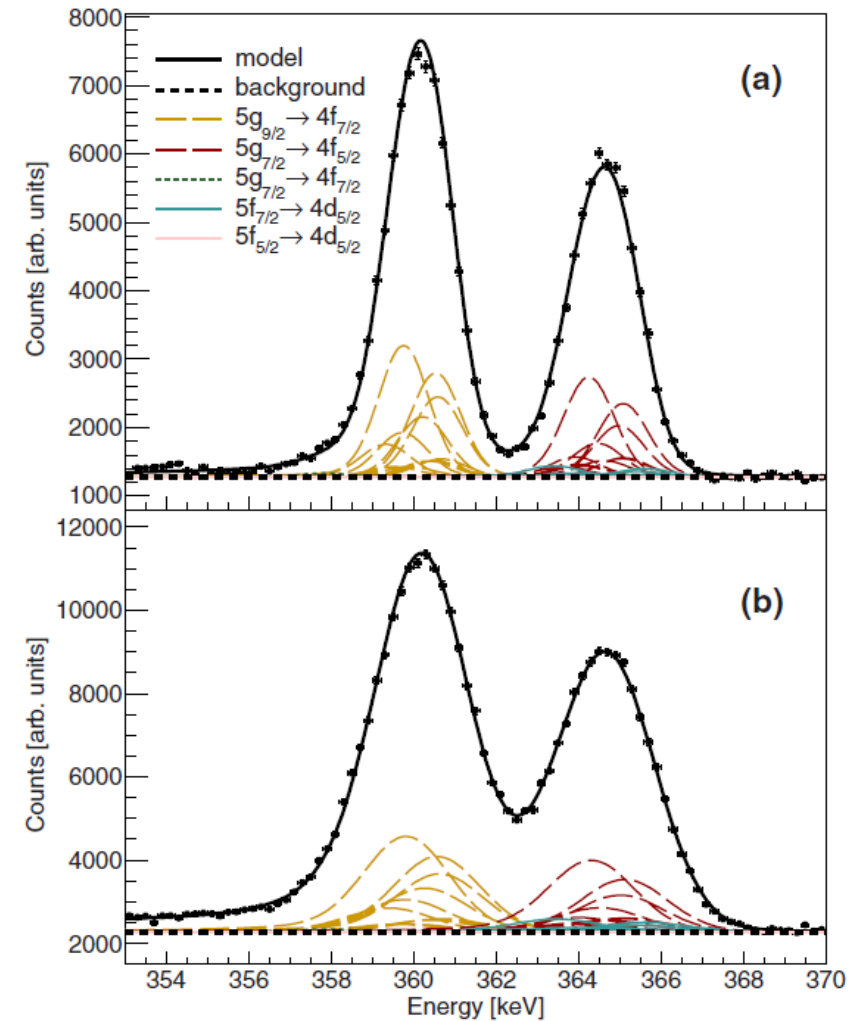
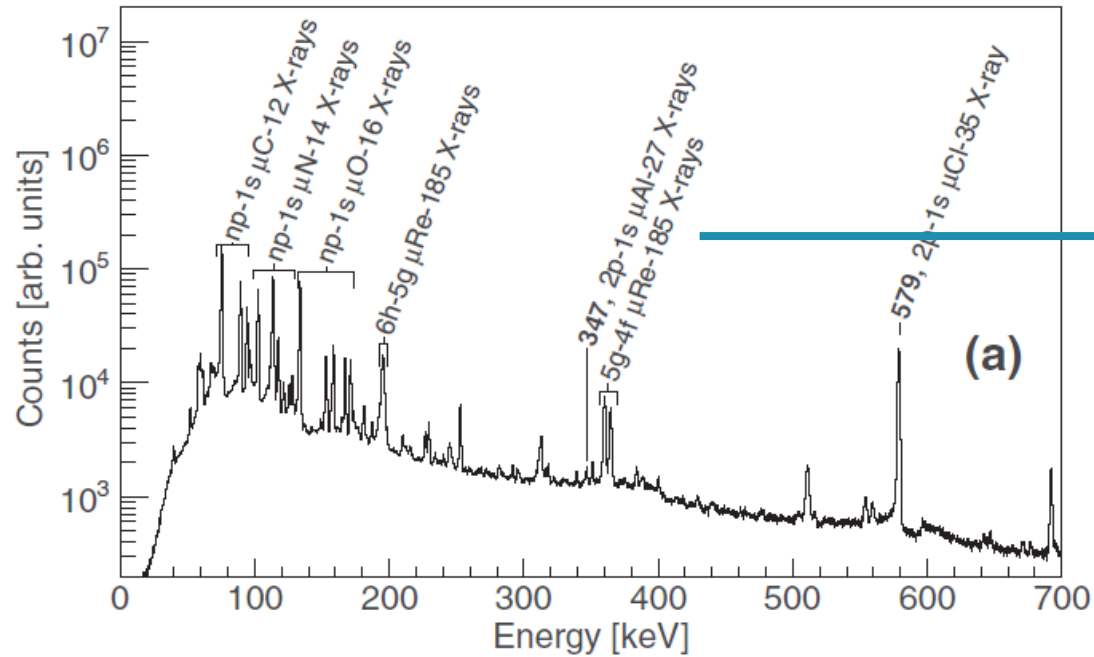


FIG. 7. Prompt γ -ray spectrum of ^{185}Re obtained by GeR (a) and GeL (b) showing the $5g \rightarrow 4f$ hf complex. The full black line shows the best fit to the data. The lines predicted by the hfs formalism are shown below the spectra.

Where to with muX?

- Research in support of laser spectroscopy activities across the nuclear landscape: hoping to reach from $_{19}\text{K}$ to $_{89}\text{Ac}$ and beyond...
- Producing and isolating a pure target is one of the challenges that we face.
- Choosing where to begin is another!

• $_{47}\text{Ag}$

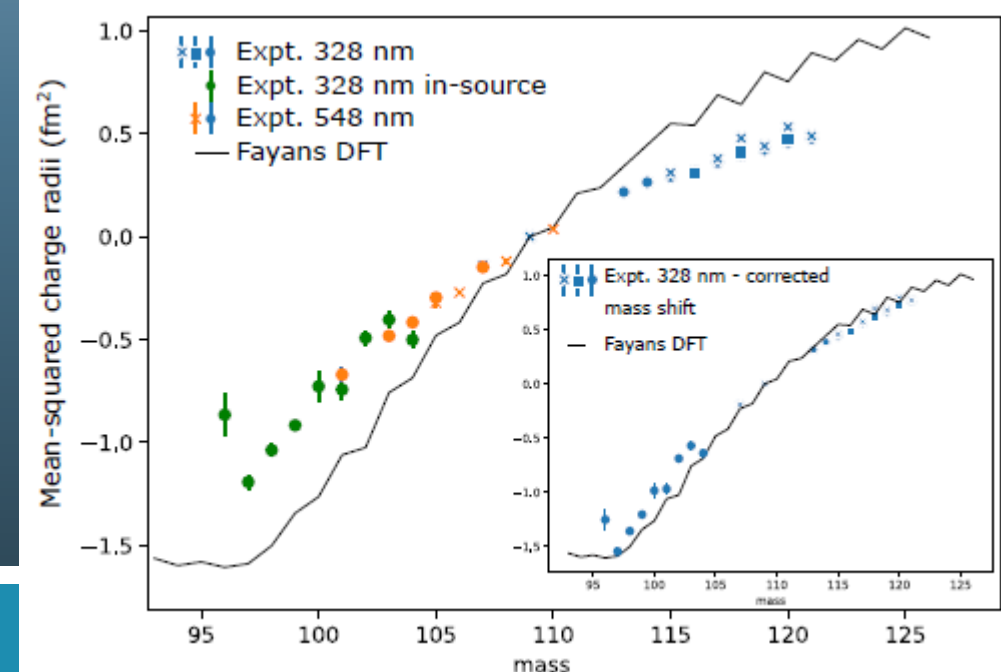
• $_{57}\text{La}$

• $_{65}\text{Tb}$

- TAC: purity of the collected sample?
 - 90% elemental purity
 - 99% isotopic purity

$_{47}\text{Ag}$

- In the vicinity of $Z=50$ and spanning from $N=50$ to $N=82$;
- Previous investigations already reached down to $N=50$ (LISOL);
- New work under analysis from Jyvaskyla from $N=49$ to $N=74$;
- New proposal at ISOLDE to push to $N=82$;
- At term, many groups aim to study the elusive case of the high-spin isomers in the self-conjugate ^{94}Ag .



R. Ferrer et al, ... radii of $N=50-54\text{Ag}$, *PLB* **728** (2014) 191-197.

13 R.P. de Groot et al, [CRIS] of silver..., *INTC-P-551*.

I. Mukha et al, ... two-proton radioactivity of ^{94}Ag , *Nature* **439** (2006) 298-302.

$_{47}\text{Ag}$

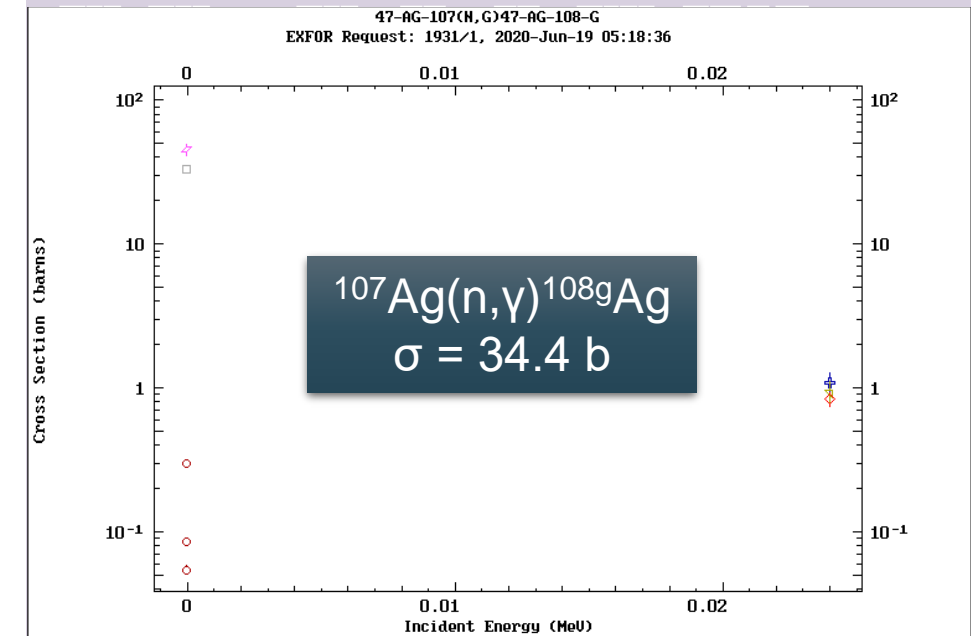
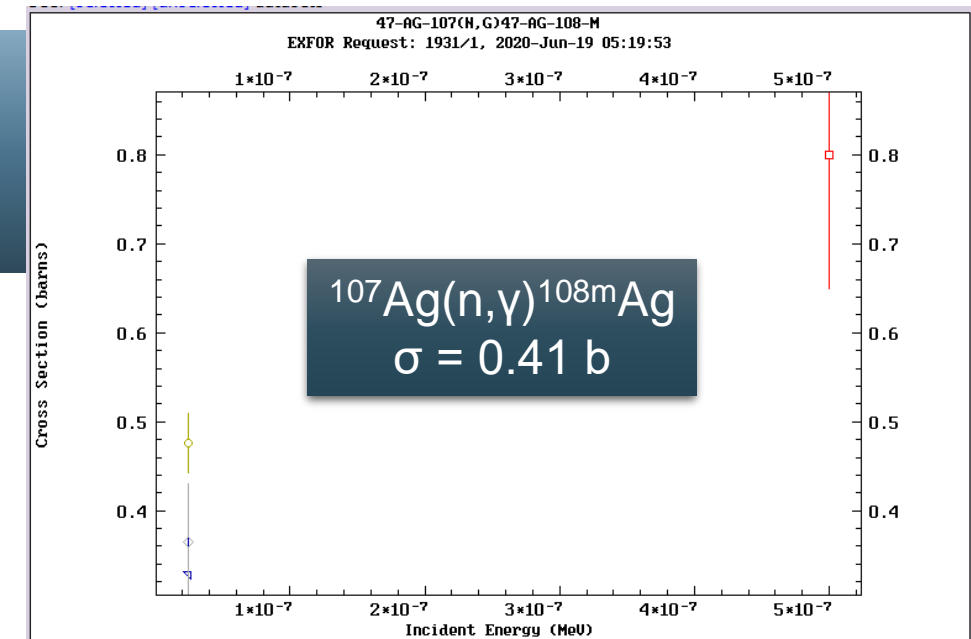
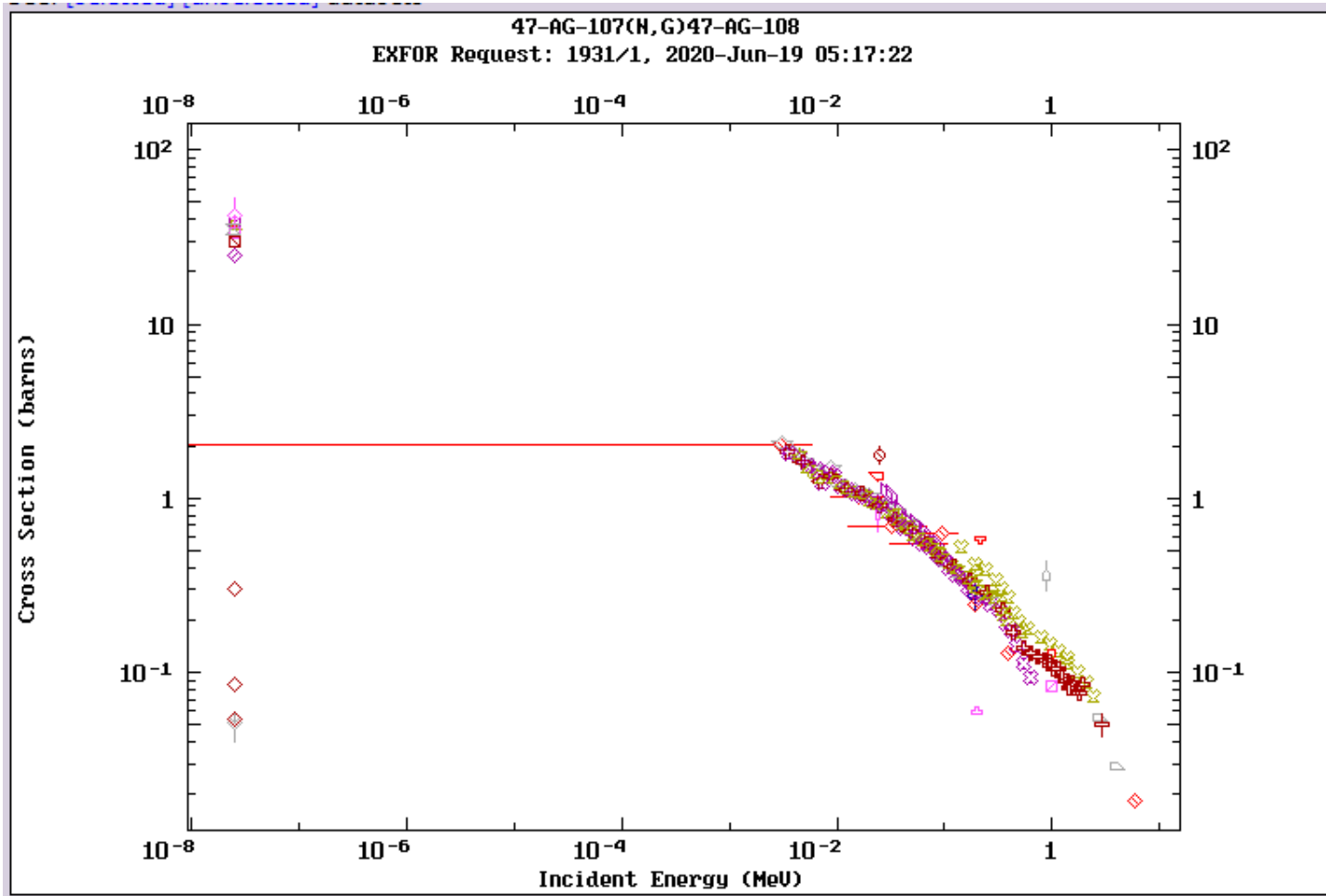
- $_{47}\text{Ag}$ features 2 stable isotopes: $^{107,109}\text{Ag}$ with spin $\frac{1}{2}$
- It also has a long-lived isotope: $^{108\text{m}}\text{Ag}$ with spin 6 and $T_{1/2}=438$ years
- Production: $^{107}\text{Ag}(n,\gamma)$ followed by mass separation
- ISOLDE has experience in the production of $_{47}\text{Ag}$

	^{107}Cd β^+	^{108}Cd Stable	^{109}Cd e- capture	^{110}Cd Stable	^{111}Cd Stable
	^{106}Ag β^+	^{107}Ag Stable	^{108}Ag β^-	^{109}Ag Stable	^{110}Ag β^-
	^{105}Pd Stable	^{106}Pd Stable	^{107}Pd β^-	^{108}Pd Stable	^{109}Pd β^-

- TAC: Is the isomer produced?
- TAC: Ratio of ^{107}Ag to $^{108\text{m}}\text{Ag}$?

^{47}Ag

- TAC: Is the isomer produced?
✓ Yes



$_{47}\text{Ag}$

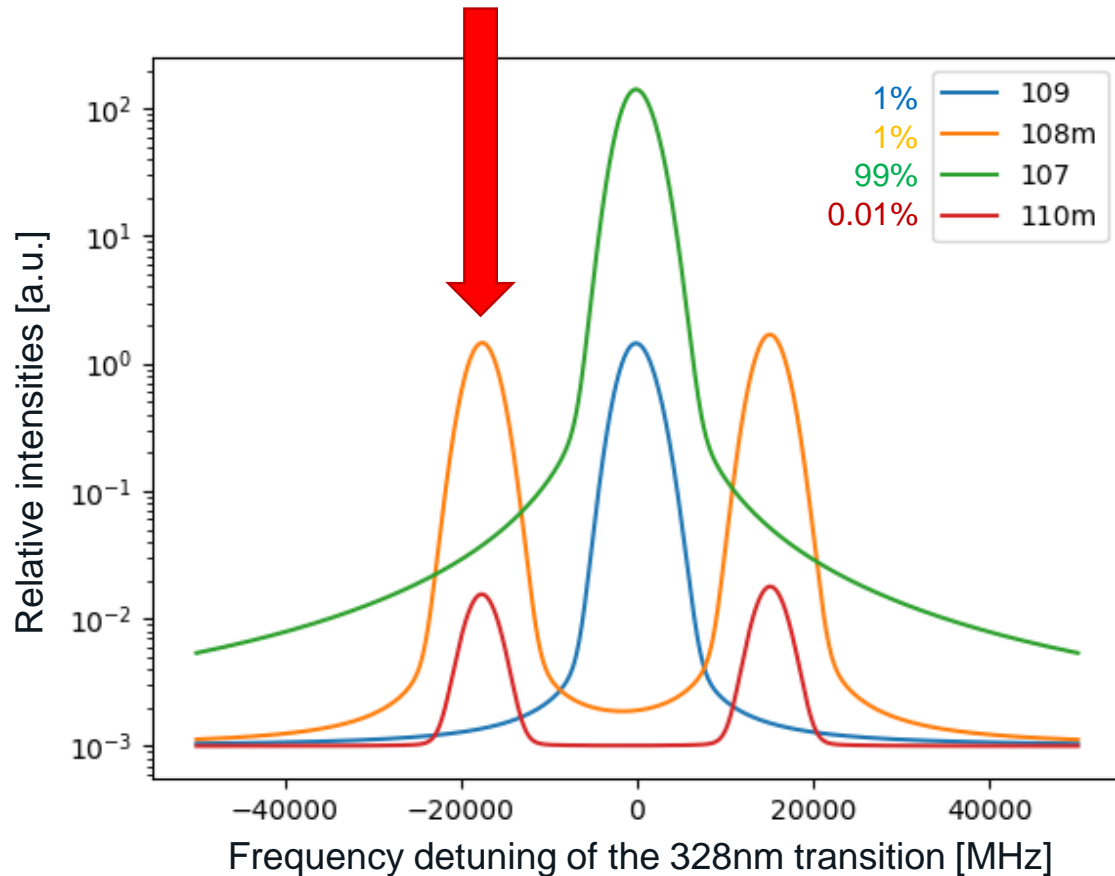
- TAC: Ratio of ^{107}Ag to $^{108\text{m}}\text{Ag}$?
- TAC: Can the ion source handle the throughput?

- Situation similar to the $^{168}\text{Er}(n,\gamma)^{169}\text{Er}$ case at MEDICIS
 - Same order of magnitude cross section
 - Enriched material as starting point
 - 2% radioisotope content at the end of irradiation
 - Demonstrated a collection of 17 MBq = 2×10^{13} atoms without RILIS ($\epsilon_{\text{ion}} \sim 0.2\%$)

- ✓ 1 mg of ^{107}Ag can yield 12 MBq of $^{108\text{m}}\text{Ag}$, i.e. 2.3×10^{17} atoms, after 50 days irradiation + 10 days cooling
- ✓ This represents $\sim 4\%$ fraction of the total sample size
- ✓ RILIS reports a 14% ionization efficiency, resulting in 3×10^{16} collected atoms.

^{47}Ag

- ✓ TAC: Ratio of ^{107}Ag to $^{108\text{m}}\text{Ag}$?
- ✓ TAC: Can the ion source handle the throughput?



- ✓ RILIS reports a 14% ionization efficiency, resulting in 3×10^{16} collected atoms.
- RILIS in normal mode can already separate Ag isotopes with widely different spin/nuclear structure:
 - If tuned on $^{108\text{m}}\text{Ag}$, both $^{107,109}\text{Ag}$ are naturally suppressed from the source
- ✓ No throughput difficulty

^{57}La

- Neutron-deficient lanthanides are gaining interest with new facilities such as MARA in Jyvaskyla and S3 at GANIL
- Limited laser spectroscopy work so far to $^{131,135,137-139}\text{La}$, suggesting triaxiality in the neutron-deficient isotopes
- Most-neutron-deficient isotope exhibits proton emission and could reveal new features in charge radii

H. Iimura et al, ... isotope shifts of ^{135}La , ^{137}La , and ^{138}La ..., PRC 68 (2003) 054328.

¹⁸ *T.E. Cocolios, Master Thesis, McGill University 2005.*

H.A. Schuessler et al, Nuclear moments of ... ^{131}La ..., Proceedings to LAP2006, p95-96 (2006).

^{57}La

- TAC: La scheme?
- TAC: What can Mainz do?

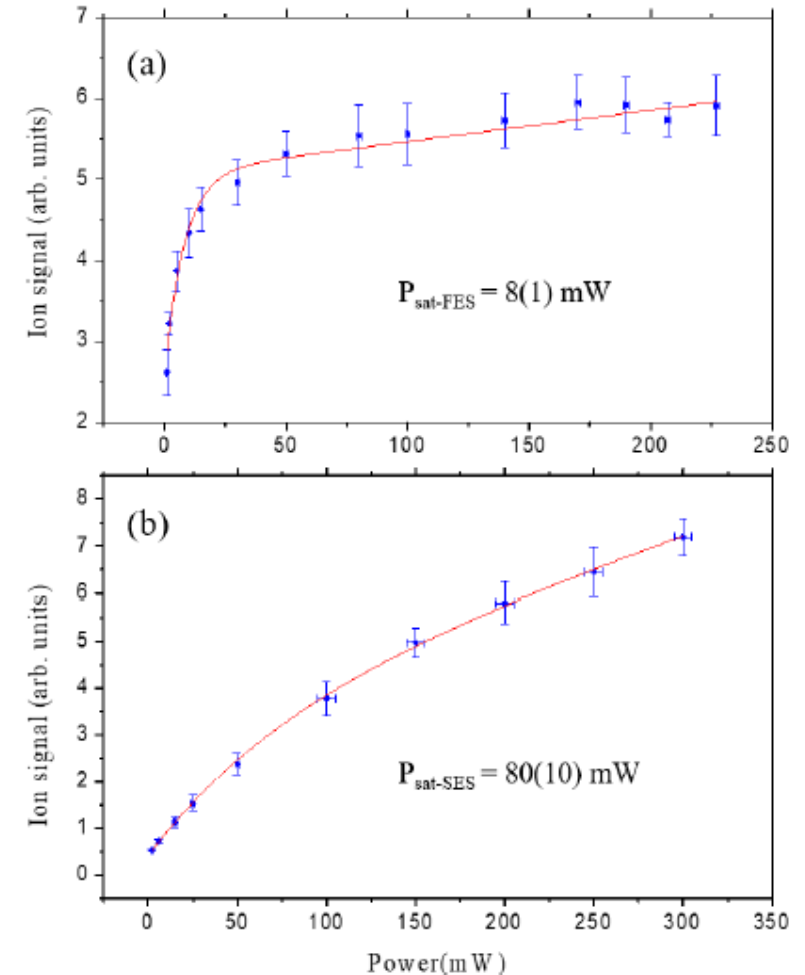
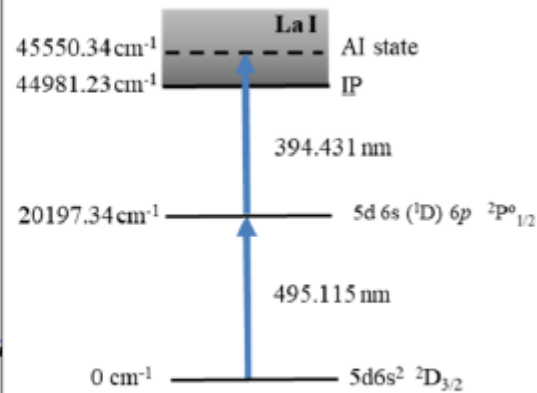
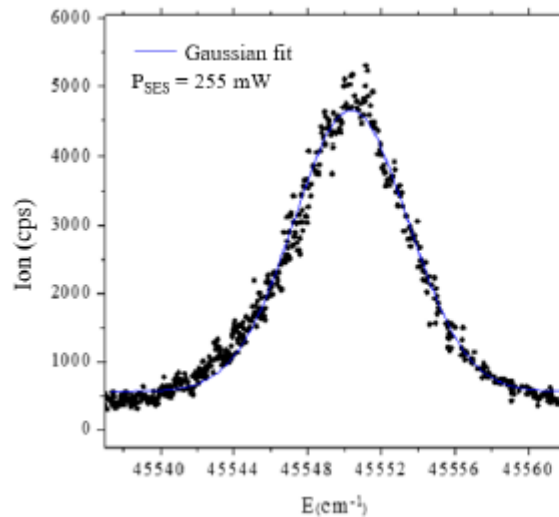
- ^{57}La contains 2 stable isotopes: ^{138}La and ^{139}La
 - ❖ Natural abundance of ^{138}La : 0.00088
 - Has not been studied with μx rays or e^- scattering
 - ❑ Commercially available with enrichment to 5%
 - Requires further enrichment to be suitable at μx
- An additional long-lived isotopes is available: ^{137}La with $T_{1/2}=60,000$ years
 - Can be produced in $^{136}\text{Ce}(n,\gamma)^{137}\text{Ce}(\beta^+/\text{EC})^{137}\text{La}$ with the intermediate isotope having $T_{1/2}=9\text{h}$, followed with radiochemistry to isolate La from Ce
 - ❑ Risks to produce isotopic contamination from $^{138}\text{Ce}(n,\gamma)^{139}\text{Ce}(\text{EC})^{139}\text{La}$ where the intermediate isotope has $T_{1/2}=137.6\text{d}$
 - Sample purity requires mass measurement for quality control (no γ /stable)

^{136}Ce Stable	^{137}Ce β^+	^{138}Ce Stable	^{139}Ce e- capture	^{140}Ce Stable
^{135}La β^+	^{136}La β^+	^{137}La e- capture	^{138}La Stable	^{139}La Stable
^{134}Ba Stable	^{135}Ba Stable	^{136}Ba Stable	^{137}Ba Stable	^{138}Ba Stable

^{57}La

- ✓ TAC: La scheme?
- ✓ TAC: What can Mainz do?

- ✓ ^{57}La has been successfully laser ionized at TRIUMF and the scheme is available.
- ✓ Mainz can perform the characterization of the isotope ratio in the case of ^{137}La .



${}^{65}\text{Tb}$

- ${}^{65}\text{Tb}$ is in the middle of the lanthanide series
- It is gaining interest beyond its medical applications
- Neutron-rich isotopes are mid-shell in both protons and neutrons, where many correlations are possible and leading to a rich nuclear structure
- Most-neutron-deficient isotope exhibits proton emission and could reveal new features in charge radii

${}_{65}\text{Tb}$

✓ TAC: What can Mainz do?

- ${}_{65}\text{Tb}$ has only 1 stable isotope: ${}^{159}\text{Tb}$
 - It however also has 2 long-lived isotopes:
 - ${}^{158}\text{Tb}$, $T_{1/2}=180$ years
 - ✓ Production via ${}^{158}\text{Gd}(d,2n){}^{158}\text{Tb}$
 - ❖ Risks of isotopic contamination with $\text{natGd}(d,xn){}^{157,159}\text{Tb}$
 - ${}^{157}\text{Tb}$, $T_{1/2}=99$ years
 - ✓ Production via ${}^{156}\text{Dy}(n,\gamma){}^{157}\text{Dy}(\text{EC}){}^{157}\text{Tb}$
 - ❖ Risks of isotopic contamination with ${}^{158}\text{Dy}(n,\gamma){}^{159}\text{Dy}(\text{EC}){}^{159}\text{Tb}$
- ✓ Requires characterization in Mainz

${}^{156}\text{Dy}$ Stable	${}^{157}\text{Dy}$ β^+	${}^{158}\text{Dy}$ Stable	${}^{159}\text{Dy}$ e- capture	${}^{160}\text{Dy}$ Stable
${}^{155}\text{Tb}$ e- capture	${}^{156}\text{Tb}$ β^+	${}^{157}\text{Tb}$ e- capture	${}^{158}\text{Tb}$ β^+	${}^{159}\text{Tb}$ Stable
${}^{154}\text{Gd}$ Stable	${}^{155}\text{Gd}$ Stable	${}^{156}\text{Gd}$ Stable	${}^{157}\text{Gd}$ Stable	${}^{158}\text{Gd}$ Stable
${}^{153}\text{Eu}$ Stable	${}^{154}\text{Eu}$ β^-	${}^{155}\text{Eu}$ β^-	${}^{156}\text{Eu}$ β^-	${}^{157}\text{Eu}$ β^-

Updated request and remaining questions

Separation of ^{108m}Ag

- Can be produced at ILL
- Should contain 1-5% ^{108m}Ag
- Should take 1 to 2 weeks of operation
- Ampoule handling should be done by CERN
 - ✓ Ampoule preparation by Charlotte Duchemin (KU Leuven/CERN EN-STI-RBS)
 - ✓ New protocol by EN-STI-RBS to reduce time & exposure after irradiation; demonstrated & approved by RP

Separation of ^{138}La

- Enriched material with 5% abundance commercially available
- Laser ionization scheme developed at TRIUMF and compatible with RILIS operation
- Other activities are moved to Mainz: quality control of ^{137}La , $^{157,158}\text{Tb}$
- No need for new target units, provided that they do not contain isobaric impurities at $A=108,138$

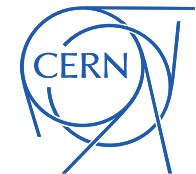
Collaboration



... for the muX collaboration



... for the interest in absolute radii for laser spectroscopy



... for the production & purification