

# Solar neutrinos and $\theta_{13}$

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The physics of the Sun and the solar neutrinos: II  
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**I. Solar neutrino data and  $\theta_{13}$**

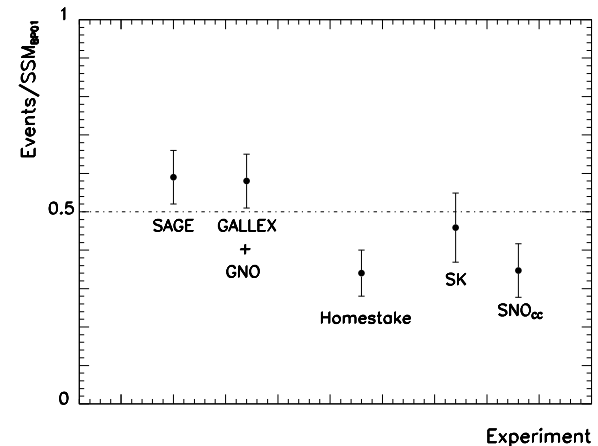
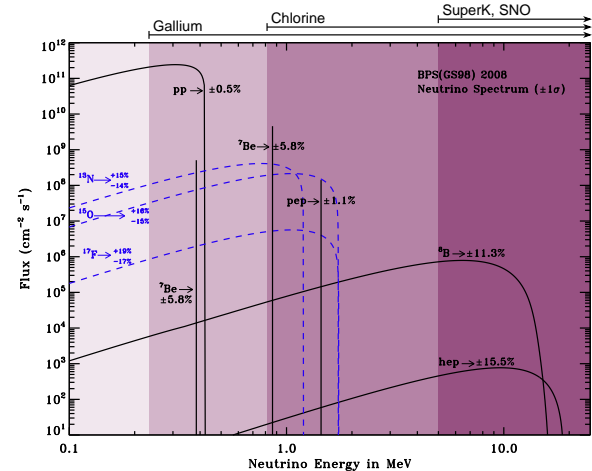
**II. Oscillation parameters and the SSM**

**III. Other hints of non-zero  $\theta_{13}$**

**Summary**

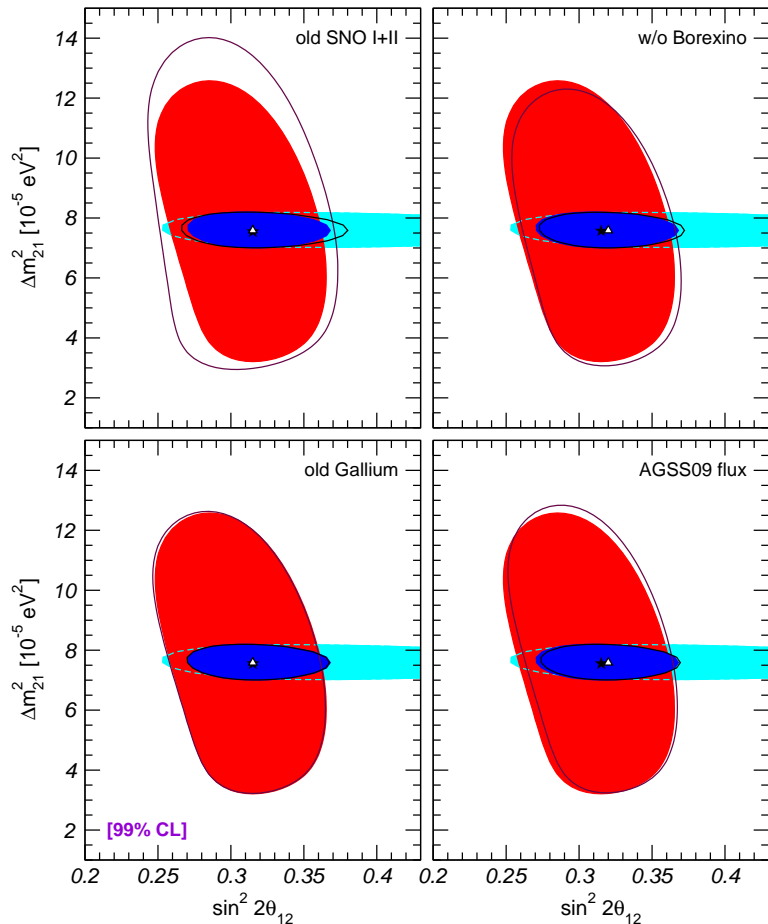
## The solar neutrino problem

- Nuclear reactions in the core of the Sun produce *electron neutrinos*;
- during the last 40 years, a number of underground experiments has measured their flux in different energy windows;
- it is found that ALL the experiments observe a deficit of about **30 – 60%**;
- the deficit is NOT the same for all the experiments, hence the effect is **energy dependent**.
- it is **not possible** to reconcile the data with the Standard Solar Model (SSM) by simply readjusting the parameters of the model;
- solution: neutrino  $\nu_e \rightarrow \nu_{\text{active}}$  oscillations;
- Effect well understood  $\Rightarrow$  **PROBLEM SOLVED.**



## The $\theta_{13} = 0$ limit: recent data

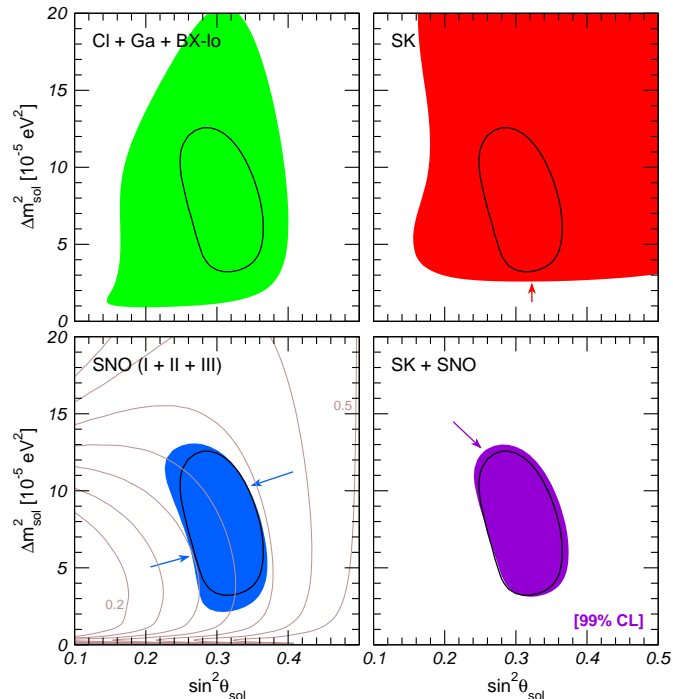
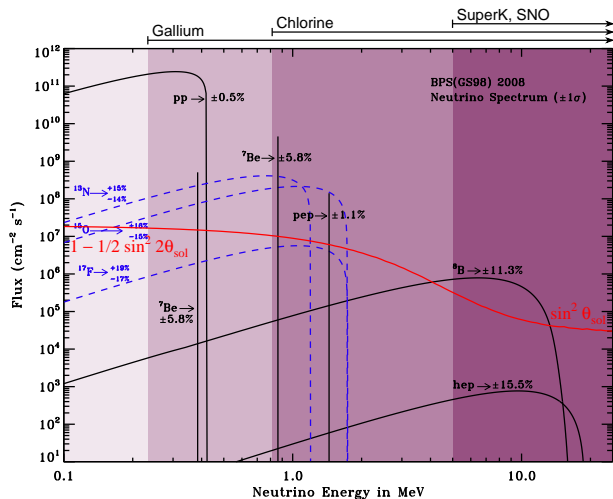
- Most relevant changes since last year:
  - new SNO-leta (low energy threshold analysis) replaces separated SNO-I and SNO-II data sets  $\Rightarrow$  bounds on  $\theta_{12}$  enhanced;
  - inclusion of Borexino results (both  ${}^7\text{Be}$  and  ${}^8\text{B}$  data)  $\Rightarrow$   $\theta_{12}$  decreases;
  - new results from SAGE with reduced systematics  $\Rightarrow$  negligible effects;
  - new AGSS09 solar model  $\Rightarrow$   $\theta_{12}$  increases;
- $\Delta m_{21}^2$  determined by KamLAND  $\Rightarrow$  insensitive to details of solar data.



## Solar neutrinos: anatomy of the oscillation solution

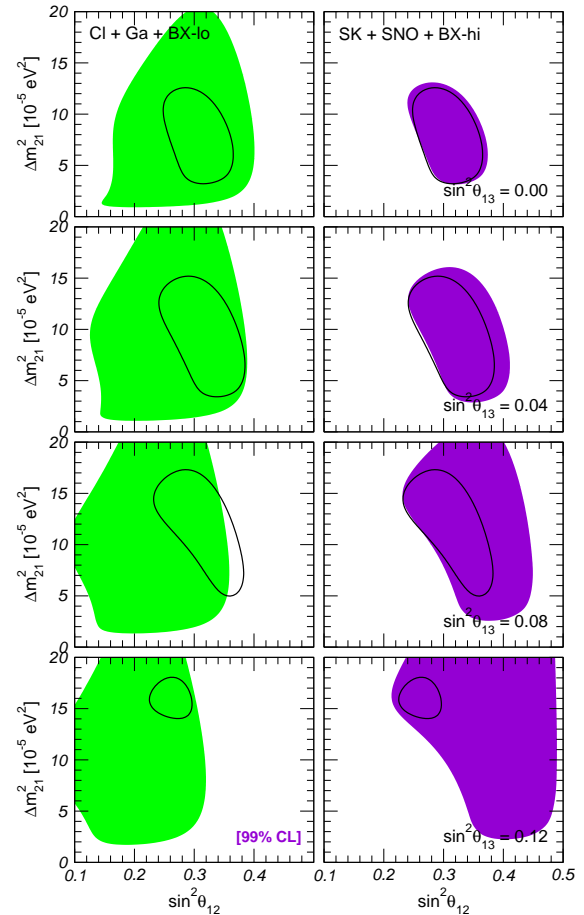
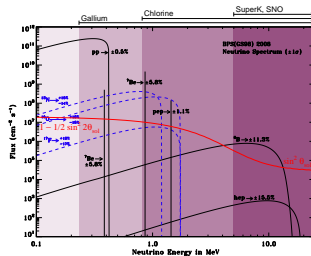
$$i \frac{d\vec{\nu}}{dt} = \left[ \frac{\Delta m_{\text{sol}}^2}{4E\nu} \begin{pmatrix} -\cos 2\theta_{\text{sol}} & \sin 2\theta_{\text{sol}} \\ \sin 2\theta_{\text{sol}} & \cos 2\theta_{\text{sol}} \end{pmatrix} \pm \sqrt{2} G_F \begin{pmatrix} N_e & 0 \\ 0 & 0 \end{pmatrix} \right] \vec{\nu}, \quad \text{with } \vec{\nu} = \begin{pmatrix} \nu_e \\ \nu_a \end{pmatrix};$$

- Data:  $\begin{cases} \text{low-E (Cl, Ga): } P_{ee} \approx 1 - \frac{1}{2} \sin^2 2\theta_{\text{sol}}, \\ \text{high-E (SK, SNO): } P_{ee} \approx \sin^2 \theta_{\text{sol}}; \end{cases}$
- fit presently dominated by high-E.



## Bound on $\theta_{13}$ from solar data

- $\nu_\mu \equiv \nu_\tau \Rightarrow$  no sensitivity to  $\theta_{23}$  and  $\delta_{CP}$ ;
  - $\Delta m_{31}^2 \approx \infty \Rightarrow$  specific value of  $\Delta m_{31}^2$  irrelevant;
- $\Rightarrow$  solar data only depend on  $\Delta m_{21}^2$ ,  $\theta_{12}$  and  $\theta_{13}$ ;
- probability:  $\begin{cases} \text{low-E: } P_{ee} \approx \cos^4 \theta_{13} \left(1 - \frac{1}{2} \sin^2 2\theta_{12}\right), \\ \text{high-E: } P_{ee} \approx \cos^4 \theta_{13} \sin^2 \theta_{12}; \end{cases}$
  - as  $\theta_{13}$  increases,  $\cos^4 \theta_{13}$  decreases and:
    - low-E data favor **smaller**  $\theta_{12}$ ;
    - high-E data favor **larger**  $\theta_{12}$  and  $\Delta m_{21}^2$ .

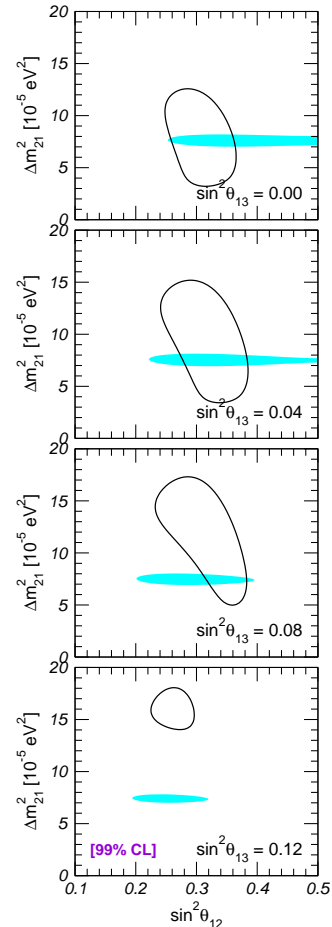


## Bound on $\theta_{13}$ from KamLAND data

- Only  $P_{ee}$  measured  $\Rightarrow$  no sensitivity to  $\theta_{23}$  and  $\delta_{CP}$ ;
  - $\Delta m_{31}^2 \approx \infty \Rightarrow$  specific  $\Delta m_{31}^2$  value irrelevant;
- $\Rightarrow$  KamLAND data only depend on  $\Delta m_{21}^2$ ,  $\theta_{12}$  and  $\theta_{13}$ ;
- probability:  $P_{ee} \approx \cos^4 \theta_{13} \left( 1 - \sin^2 2\theta_{12} \sin^2 \frac{\Delta m_{21}^2 L}{4E} \right)$ ,
  - $\Delta m_{21}^2$  is determined by  $\langle L \rangle$  and by the energy spectrum, hence it does not change with  $\theta_{13}$ ;
  - as  $\theta_{13}$  increases, data favor **smaller**  $\theta_{12}$ ;
  - for large  $\theta_{13}$  oscillation signal is suppressed  $\Rightarrow$  fit gets worse.

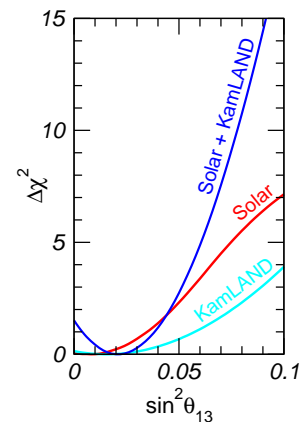
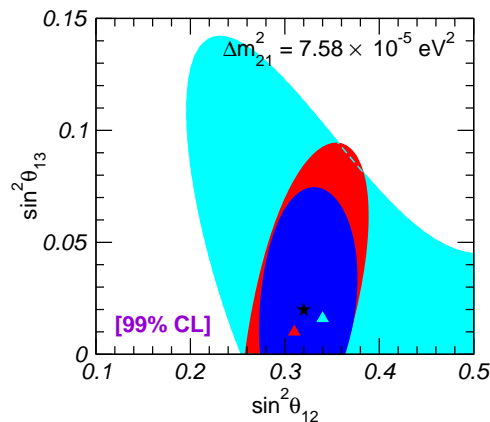
## Synergy with solar data

- As  $\theta_{13}$  increases, solar region moves to larger  $\Delta m_{21}^2$ , while KamLAND region does not;
- also, for large  $\theta_{13}$  KamLAND adds to **low-E** solar data in favoring small  $\theta_{12}$ , increasing the tension with **high-E** solar data.



## Hint for non-zero $\theta_{13}$ in solar and KamLAND data

- For  $\theta_{13} = 0$ , we have  $\sin^2 \theta_{12} = \begin{cases} 0.30 & \text{from solar data;} \\ 0.36 & \text{from KamLAND data;} \end{cases}$  [Fogli et al, arXiv:0806.2649]  
[Schwetz et al, arXiv:0808.2016]
- hence there is a tension between solar and KamLAND;
- as we have just seen, when  $\theta_{13}$  increases:
  - solar region slightly moves to larger  $\theta_{12}$  (high-E data dominate over low-E ones);
  - KamLAND region definitely shifts to smaller  $\theta_{12}$ ;
- therefore, a non-zero value of  $\theta_{13}$  reduces the tension between solar and KamLAND data;
- new SNO-III data favor smaller  $\phi_{CC}/\phi_{NC} \Rightarrow$  smaller  $\theta_{12}$  from solar  $\Rightarrow$  tension with KamLAND is increased  $\Rightarrow$  larger  $\theta_{13}$  favored.



### Reconstructing the neutrino fluxes

- Strategy: perform a solar model independent analysis of both solar and terrestrial neutrino data in the framework of  $3\nu$  mixing;
- aim: to determine both the **flavor parameters** and all the **solar neutrino fluxes** with a minimum set of theoretical priors;
- 11 parameters:  $\theta_{12}$ ,  $\theta_{13}$ ,  $\Delta m_{21}^2$  and 8 reduced fluxes  $f_i = \Phi_i/\Phi_i^{\text{ref}}$ ;

Flux	$\Phi_i^{\text{ref}} [\text{cm}^{-2} \text{s}^{-1}]$
pp	$5.97 \times 10^{10}$
${}^7\text{Be}$	$5.07 \times 10^9$
pep	$1.41 \times 10^8$
${}^{13}\text{N}$	$2.88 \times 10^8$
${}^{15}\text{O}$	$2.15 \times 10^8$
${}^{17}\text{F}$	$5.82 \times 10^6$
${}^8\text{B}$	$5.94 \times 10^6$
hep	$7.90 \times 10^3$

- imposed physical conditions:

– fluxes must be positive:

$$\Phi_i \geq 0$$

– the number of nuclear reactions terminating the pp-chain should not exceed the number of nuclear reactions which initiate it:

$$\Phi_{7\text{Be}} + \Phi_{8\text{B}} \leq \Phi_{\text{pp}} + \Phi_{\text{pep}}$$

– the  ${}^{14}\text{N}(p, \gamma){}^{15}\text{O}$  reaction must be the slowest process in the main branch of the CNO-cycle:

$$\Phi_{15\text{O}} \leq \Phi_{13\text{N}}$$

– the CNO-II branch must be subdominant:

$$\Phi_{17\text{F}} \leq \Phi_{15\text{O}}$$

– pep & pp have the same nuclear matrix element:

$$f_{\text{pep}}/f_{\text{pp}} = 1.008 \pm 0.010$$



## Results with the luminosity constraint

- Best-fit fluxes:

$$f_{pp} = 0.990^{+0.010}_{-0.009} [^{+0.023}_{-0.030}],$$

$$f_{Be} = 1.00^{+0.10}_{-0.09} [^{+0.25}_{-0.21}],$$

$$f_{pep} = 0.998 \pm 0.014 [^{\pm 0.04}],$$

$$f_{^{13}N} = 2.7^{+1.7}_{-1.2} [^{+5.6}_{-2.4}],$$

$$f_{^{15}O} = 1.8 \pm 0.9 [^{+2.2}_{-1.8}],$$

$$f_{^{17}F} \leq 32 [72],$$

$$f_{^8B} = 0.85 \pm 0.03 [^{\pm 0.08}],$$

$$f_{hep} = 1.7^{+1.3}_{-1.4} [^{+3.8}_{-1.7}],$$

- oscillation parameters:

$$\Delta m_{21}^2 = 7.6 \pm 0.2 [^{\pm 0.5}] \times 10^{-5} \text{ eV}^2,$$

$$\sin^2 \theta_{12} = 0.33 \pm 0.02 [^{\pm 0.05}],$$

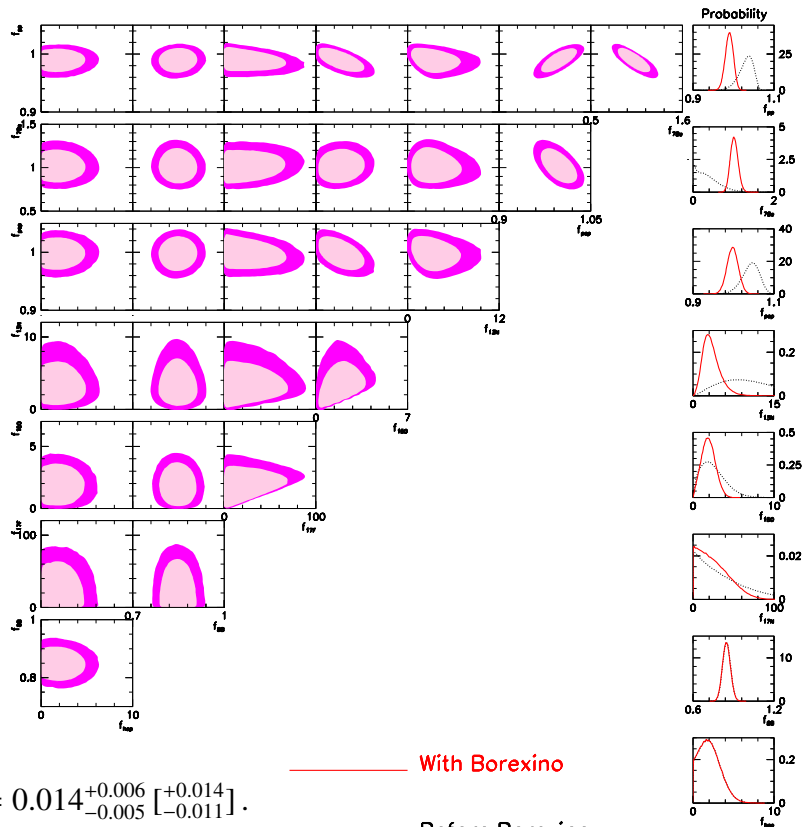
$$\sin^2 \theta_{13} = 0.02 \pm 0.012 [^{+0.03}_{-0.02}],$$

- solar luminosity:

$$\frac{L_{pp\text{-chain}}}{L_{\odot}} = 0.986^{+0.005}_{-0.006} [^{+0.011}_{-0.014}] \iff \frac{L_{CNO}}{L_{\odot}} = 0.014^{+0.006}_{-0.005} [^{+0.014}_{-0.011}].$$

————— With Borexino

..... Before Borexino



## Results without the luminosity constraint

- Best-fit fluxes:

$$f_{pp} = 0.98_{-0.15}^{+0.16} [_{-0.40}^{+0.47}],$$

$$f_{Be} = 1.01_{-0.09}^{+0.10} [_{-0.22}^{+0.27}],$$

$$f_{pep} = 0.98_{-0.15}^{+0.16} [_{-0.40}^{+0.47}],$$

$$f_{^{13}N} = 2.7_{-1.3}^{+1.8} [_{-2.5}^{+5.7}],$$

$$f_{^{15}O} = 1.9 \pm 1.0 [_{-1.9}^{+2.3}],$$

$$f_{^{17}F} \leq 34 [79],$$

$$f_{^8B} = 0.85 \pm 0.03 [_{\pm 0.08}],$$

$$f_{hep} = 1.7_{-1.4}^{+1.3} [_{-1.7}^{+3.8}],$$

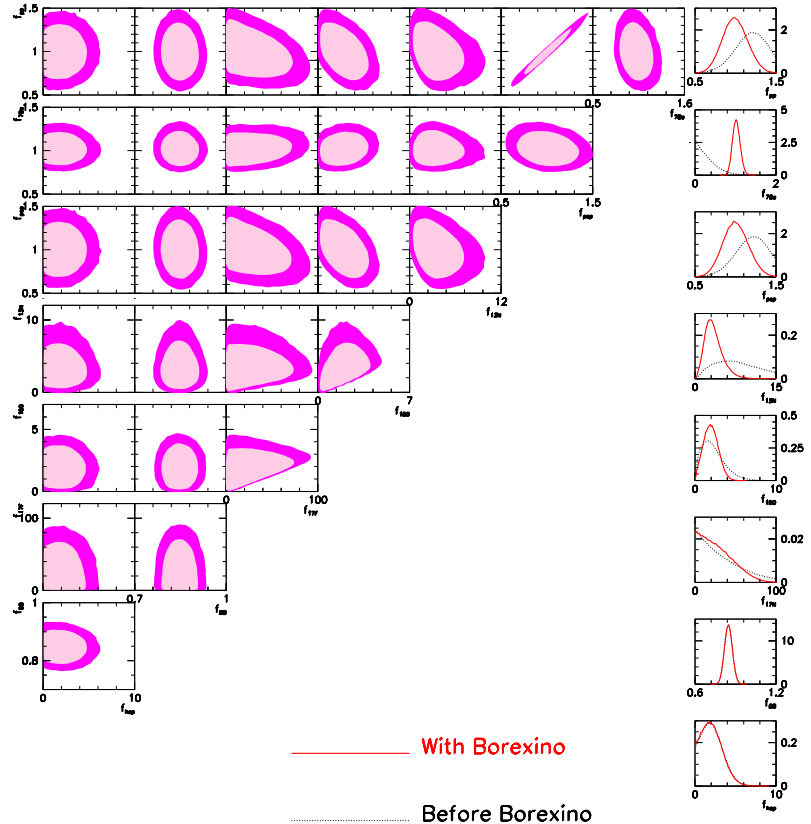
- solar luminosity:

$$\frac{L_{pp-chain}}{L_{\odot}} = 0.98_{-0.14}^{+0.15} [_{\pm 0.40}],$$

$$\frac{L_{CNO}}{L_{\odot}} = 0.015_{-0.007}^{+0.005} [_{-0.014}^{+0.013}],$$

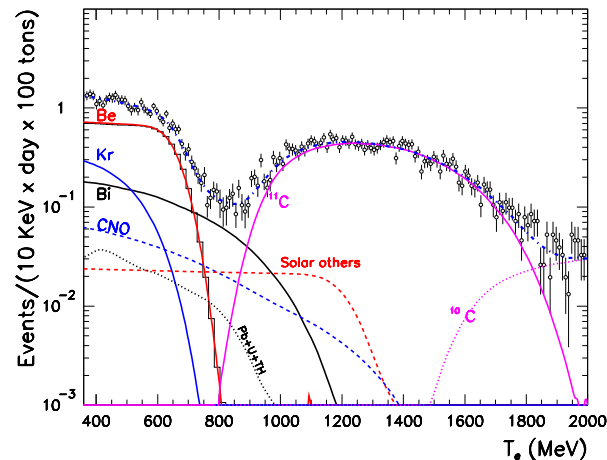
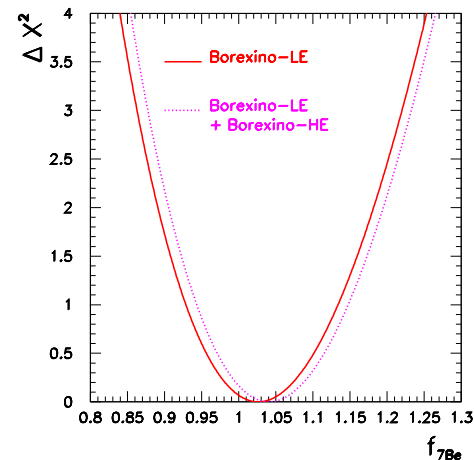
- from which we derive:

$$\frac{L_{\odot}(\text{neutrino-inferred})}{L_{\odot}} = 1.00 \pm 0.14 [_{-0.34}^{+0.37}].$$



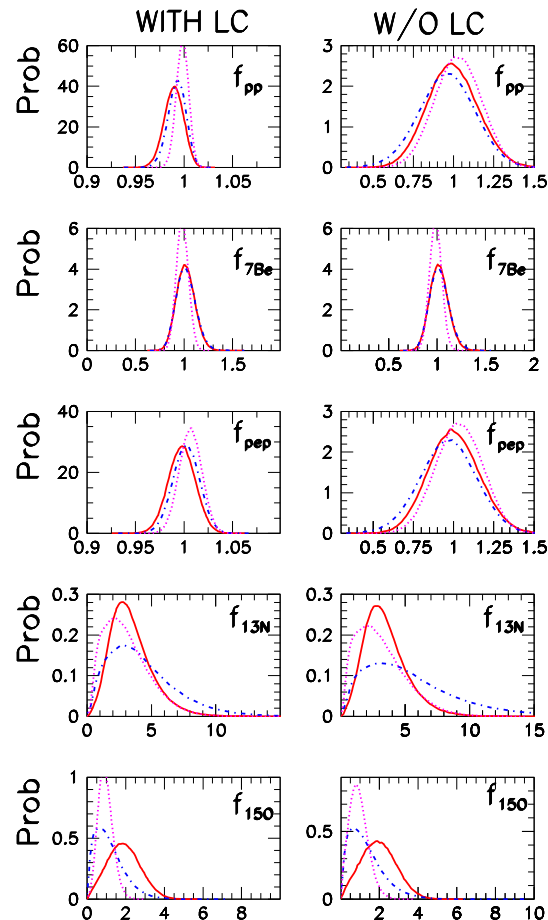
### The Borexino experiment

- Borexino has provided a unique measurement of solar neutrinos at low energy [[arXiv:0805.3843](https://arxiv.org/abs/0805.3843)];
- however, the official analysis only focuses on the extraction of  ${}^7\text{Be}$ , and treats CNO neutrinos as “background”;
- this is inconsistent with our approach, which aims at a joint determination of **all** the fluxes on the same footing;
- hence, we have performed our own analysis of the Borexino spectrum;
- backgrounds:
  - ${}^{14}\text{C}$  is removed by a cut  $T_e \geq 365$  keV;
  - ${}^{238}\text{U}$ ,  ${}^{214}\text{Pb}$  are assumed to be known;
  - ${}^{85}\text{Kr}$ ,  ${}^{210}\text{Bi}$ ,  ${}^{11}\text{C}$ ,  ${}^{10}\text{C}$  are left free and fitted;
- our fit is in excellent agreement with the results of the Borexino collaboration.



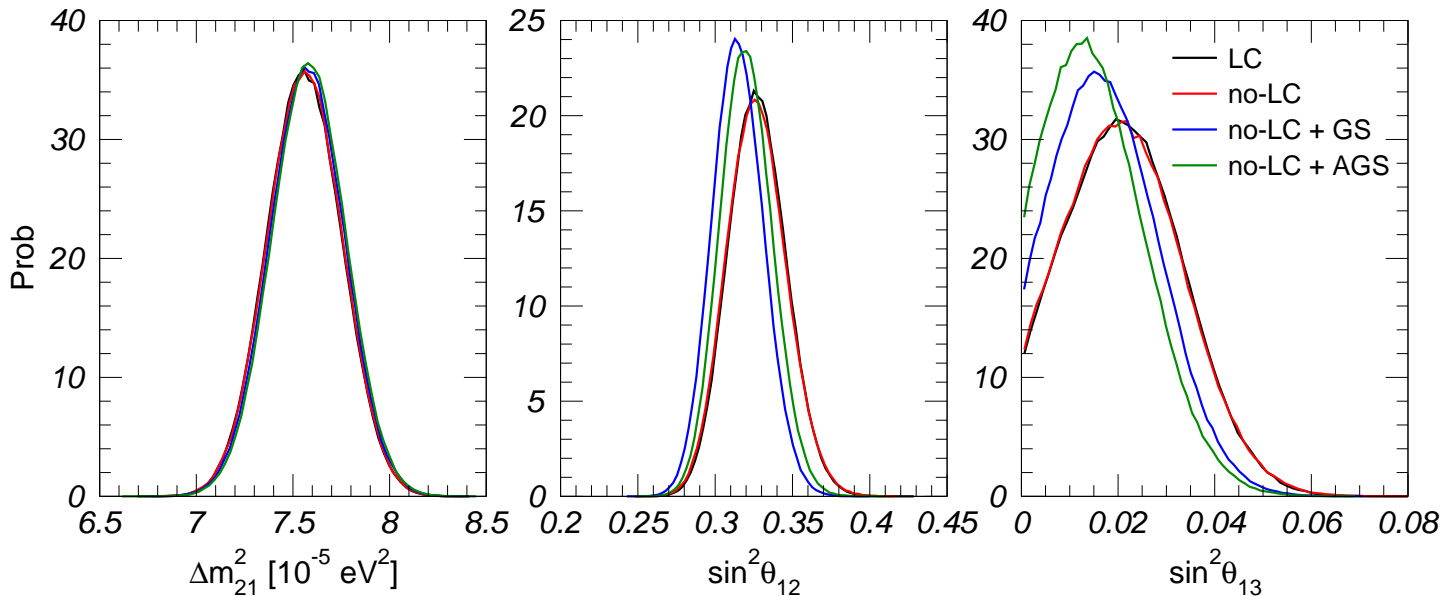
### The role and potential of Borexino

- Three types of fit:
  - **solid**: present, full-spectrum;
  - **dash-dotted**: present,  ${}^7\text{Be}$  line only;
  - **dotted**: future (no  ${}^{11}\text{C}$ ,  $\text{stat} \times 2$ ,  $\text{sys} / 3$ );
- use of spectral info irrelevant for  ${}^7\text{Be}$ ;
- CNO improves  $\Rightarrow$  Borexino can see them, even with unknown  ${}^{210}\text{Bi}$  background;
- CNO also important for Chlorine and Gallium:
  - Gallium mainly sensitive to  ${}^{13}\text{N}$  (lower  $E_\nu$ );
  - Chlorine mainly sensitive to  ${}^{15}\text{O}$  (higher  $E_\nu$ );
- Gallium excess  $\Rightarrow$   ${}^{13}\text{N}$  always larger than 1;
- Chlorine deficit  $\Rightarrow$   ${}^{15}\text{O}$  senses tension with Borexino;
- future data will improve fluxes, but not dramatically.



### Impact of the SSM on the oscillation parameters

- Imposing the luminosity constraint has no effect on the oscillation parameters;
- $\Delta m_{21}^2$  completely dominated by KamLAND  $\Rightarrow$  insensitive to the SSM's details;
- conversely, the preferred range of  $\theta_{12}$  and  $\theta_{13}$  depends on the SSM.



## Atmospheric neutrinos

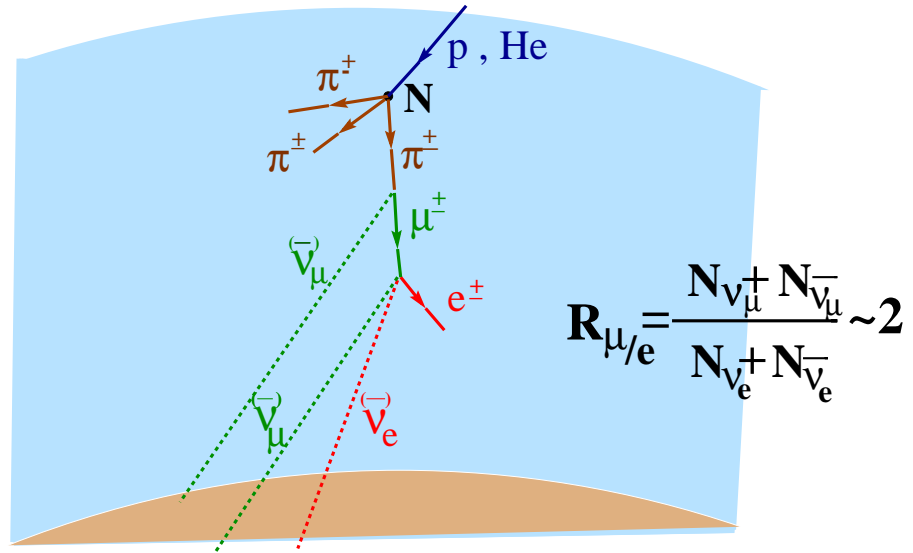
- Atmospheric neutrinos are produced by the interaction of *cosmic rays* ( $p$ , He, ...) with the Earth's atmosphere:

- 1  $A_{\text{cr}} + A_{\text{air}} \rightarrow \pi^{\pm}, K^{\pm}, K^0, \dots$

- 2  $\pi^{\pm} \rightarrow \mu^{\pm} + \nu_{\mu}$ ,

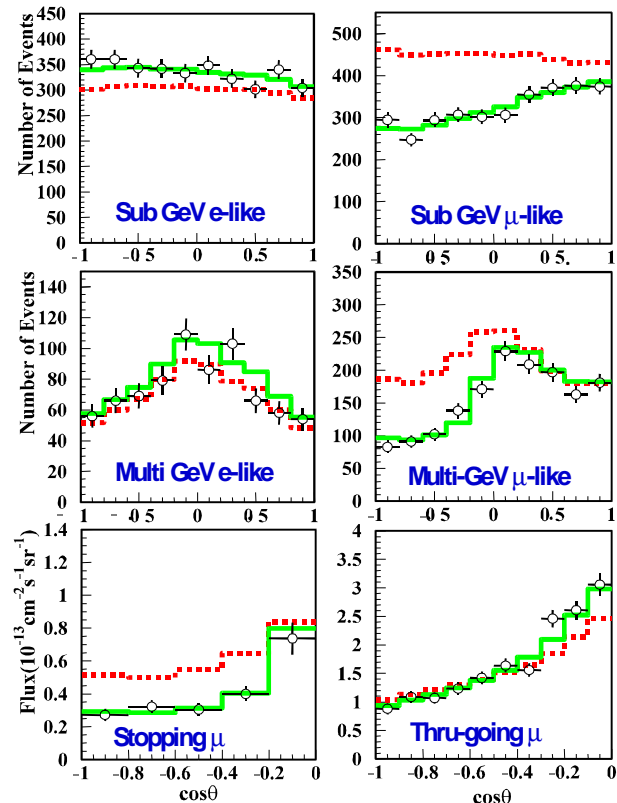
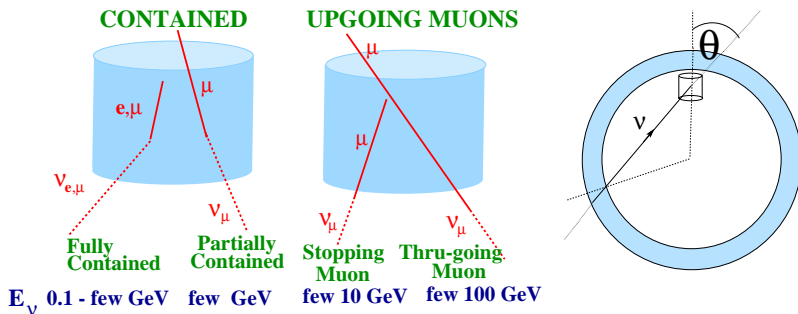
- 3  $\mu^{\pm} \rightarrow e^{\pm} + \nu_e + \nu_{\mu}$ ;

- at the detector, some  $\nu$  interacts and produces a **charged lepton**, which is observed;
- $\nu_{\mu}$  and  $\nu_e$  fluxes have large ( $\approx 20\%$ ) uncertainties;
- however, the  $\nu_{\mu}/\nu_e$  ratio is predicted with quite good accuracy ( $\approx 5\%$ ).



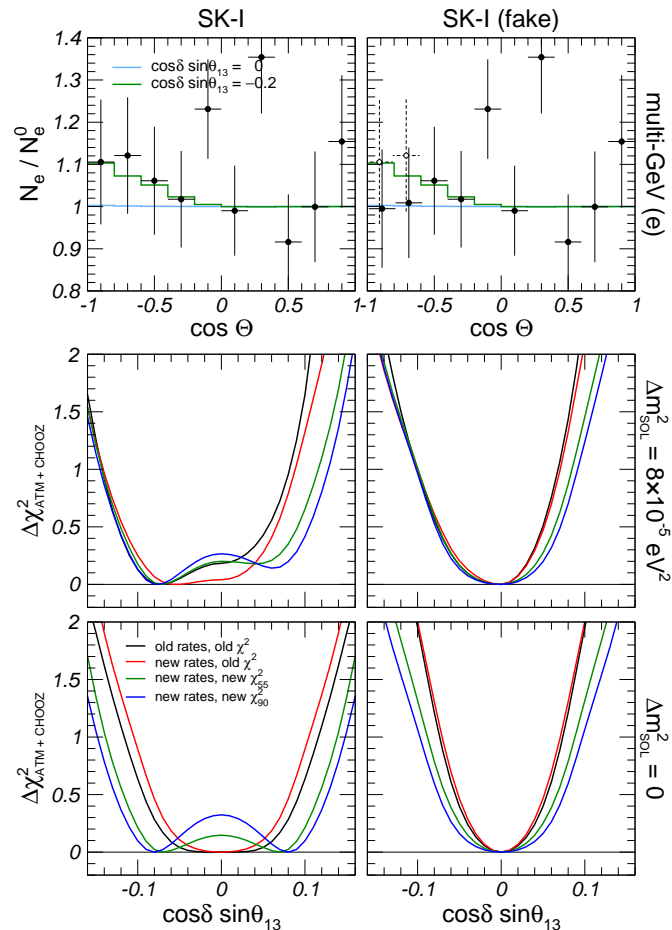
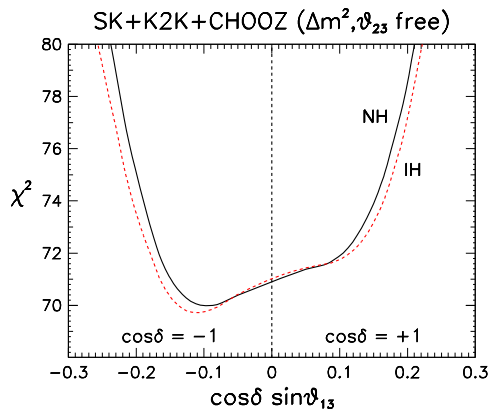
## Atmospheric neutrino oscillations

- Data (dots) vs. Monte-Carlo (red dashed line):
  - *small excess* in sub-GeV  $\nu_e$ ;
  - *no problem* in multi-GeV  $\nu_e$ ;
  - *zenith-dependent deficit* in all  $\nu_\mu$  samples;
- deficit in  $\nu_\mu$ :
  - grows with  $L$ ;
  - decreases with  $E_\nu$ ;
- deficit cannot be explained by flux uncertainties;
- solution:  $\nu_\mu \rightarrow \nu_\tau$  oscillations (green solid line).



## $\theta_{13}$ from atmospheric SK-I data

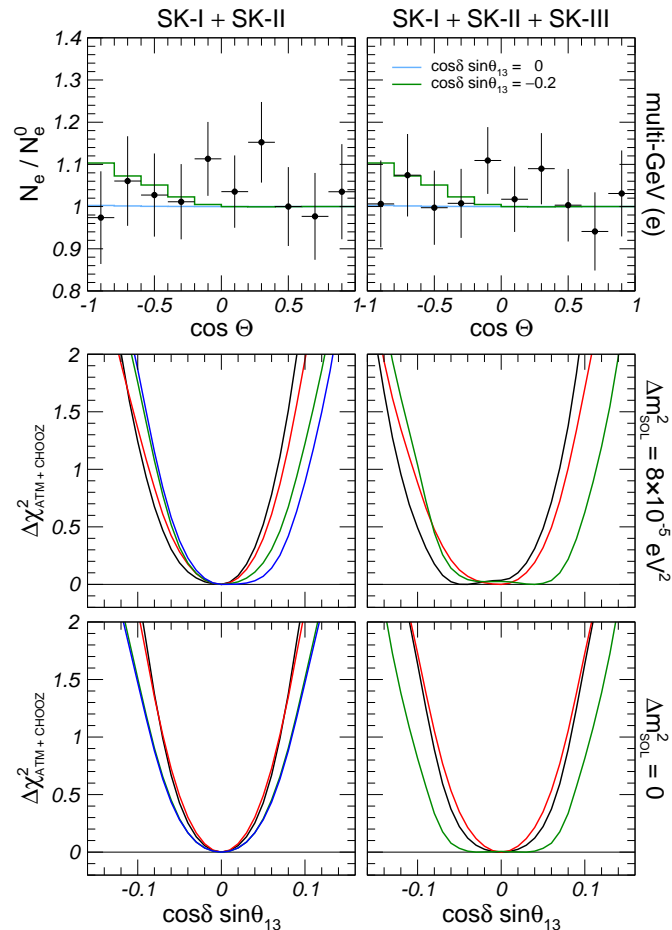
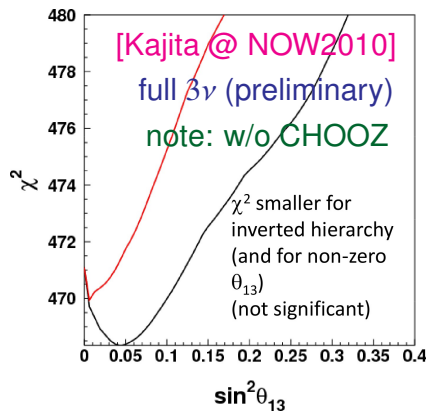
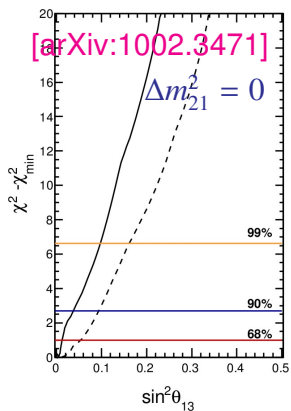
- Hint of non-zero  $\theta_{13}$  in atm SK-I (+ LBL) data; [Fogli et al, hep-ph/0506083 & arXiv:0806.2649];
- characteristics affected by  $\delta_{CP} \Rightarrow$  inclusion of subleading  $\Delta m_{21}^2$  effects important;
- hint triggered by a peculiar signature of multi-GeV  $e$ -like events in SK-I data;
- details of the simulation very important.





## $\theta_{13}$ after atmospheric SK-III data

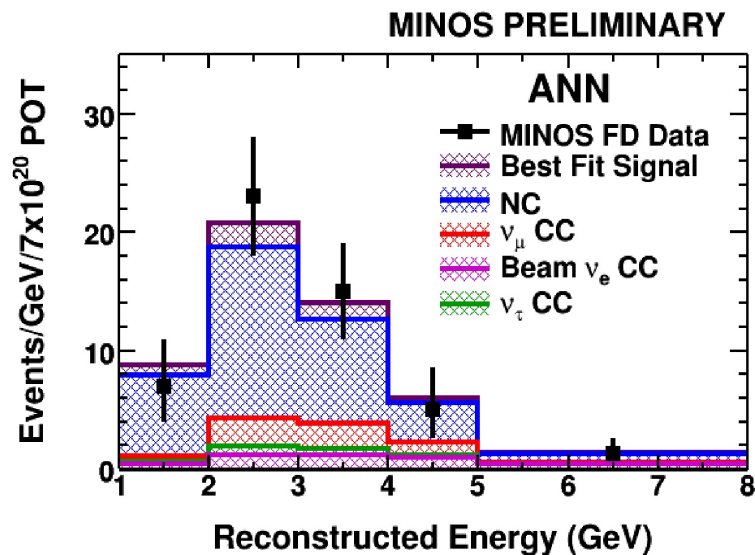
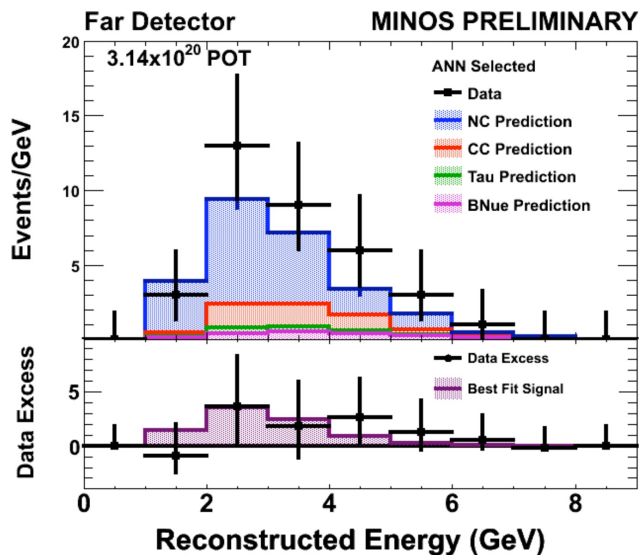
- Peculiar signature of multi-GeV  $e$ -like SK-I data not present in SK(I+II) data;
- however, a weak excess reappear after the inclusion of SK-III data;
- SK analysis for  $\Delta m_{31}^2 = 0$  confirms  $\theta_{13} = 0$ ;
- preliminary results from a full  $3\nu$  fit suggest weak deviations may be present for IH.



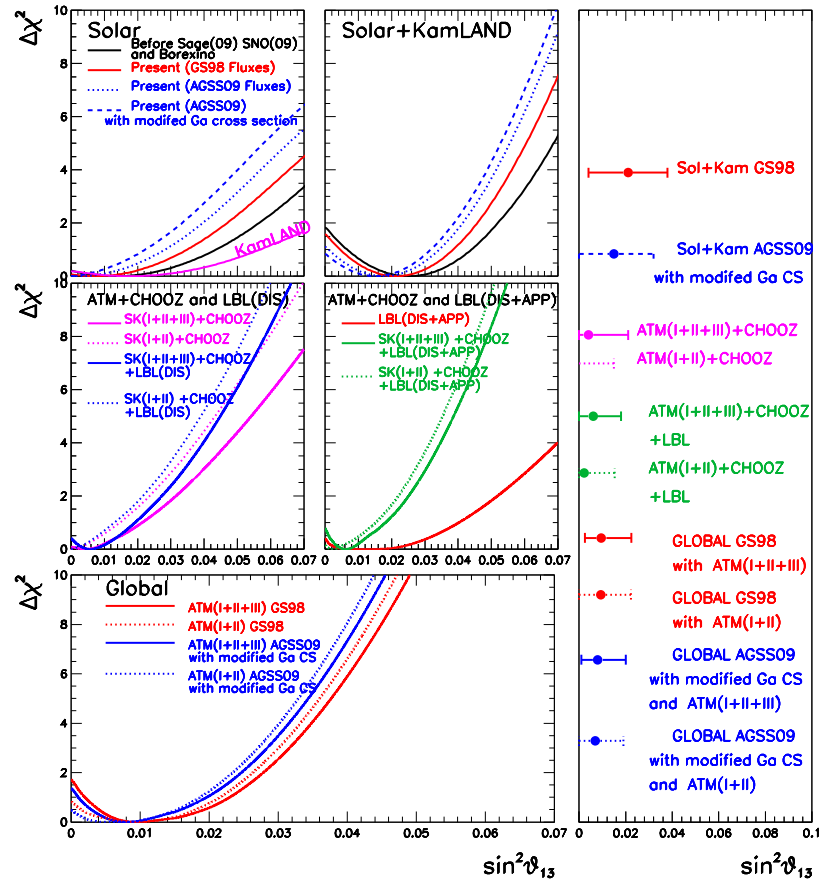
#### $\nu_e$ appearance at the Minos experiment

- $\nu_\mu$ 's are produced at accelerator through  $\pi$  decay, with mean energy  $\sim 3$  GeV;
- flux measured at 735 km  $\Rightarrow$  deficit of  $\nu_\mu$ 's observed  $\Rightarrow$  atm  $\nu_\mu \rightarrow \nu_\tau$  conversion confirmed;
- $\nu_e$  appearance:
 

$\left\{ \begin{array}{l} 3.1 \times 10^{20} \text{ pot: } 35 \text{ observed, } 27.0 \pm 5.2 \pm 2.0 \text{ expected} \Rightarrow 1.5\sigma \text{ excess;} \\ 7.0 \times 10^{20} \text{ pot: } 54 \text{ observed, } 49.1 \pm 7.0 \pm 2.7 \text{ expected} \Rightarrow 0.7\sigma \text{ excess.} \end{array} \right.$
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- **Solar** neutrino data alone can impose an upper bound on  $\theta_{13}$ ;
- in combination with KamLAND this bound becomes stronger;
- a small non-zero  $\theta_{13}$  improves the agreement between solar and KamLAND data;
- these results are qualitatively robust with respect to the details of the SSM (GS, AGSS, free);
- weak preference for non-zero  $\theta_{13}$  in atmospheric data still to be properly quantified;
- hint of non-zero  $\theta_{13}$  in **Minos**  $\nu_e$  appearance sample strongly reduced by the new data.



[Gonzalez-Garcia, MM & Salvado, JHEP 04 (2010) 056]