

# A Robust Measure of Event Isotropy at Colliders

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(2004.06125) w/ J. Thaler, MIT

FCC-ee Webinar  
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# Motivation

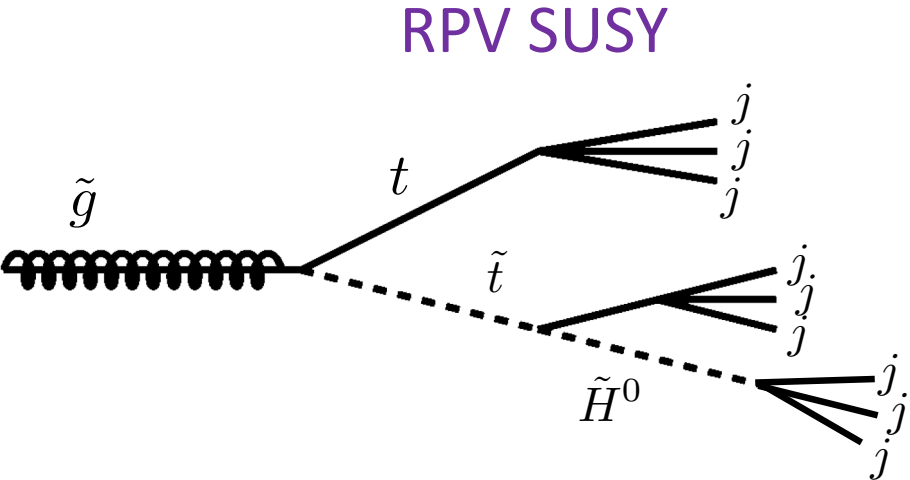
There is enormous capacity for precision SM measurements & discovery potential at colliders

- Could be new physics at electroweak scale hiding with rare kinematic signatures
- Strategy for new physics searches: identify signatures *fundamentally* different from QCD backgrounds

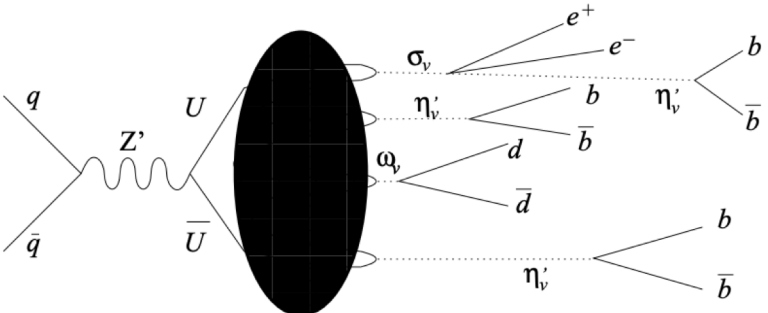
# Motivation

QCD at TeV scale is characterized by soft, collinear splittings, and therefore looks very *jetty*

But many new physics signatures look quasi-isotropic:



Hidden Valleys/Dark Showers



Strassler, Zurek 2006

- Also:
- Black holes
  - Soft bomb (SUEPs)
  - Many more...

# Motivation

There are lots of new physics scenarios with quasi-isotropic radiation patterns

When trying to quantify event shape

- Event shape observables designed to measure distance from *dijet*
  - *Thrust, C/D-parameter, sphericity, spherocity, supersphero...*
- Want distance from *isotropy*

## Event Isotropy

(CC, J. Thaler, 2004.06125)



Part 1: Defining Event Isotropy

Part 2: Applications of Event Isotropy  
at FCC-ee

# Energy Mover's Distance

We propose a new event shape observable: **event isotropy**

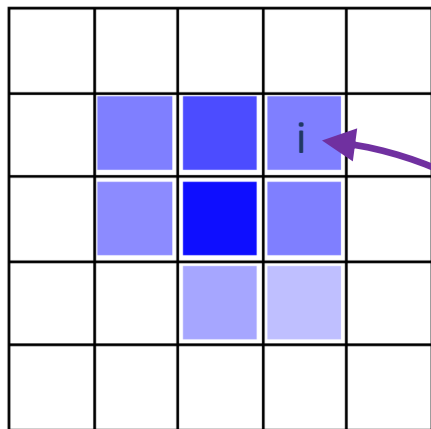
CC, J. Thaler 2004.06125

*Energy mover's distance* (EMD):

What is the minimum work to rearrange the energy distribution in event  $P$  to look like event  $Q$ ?

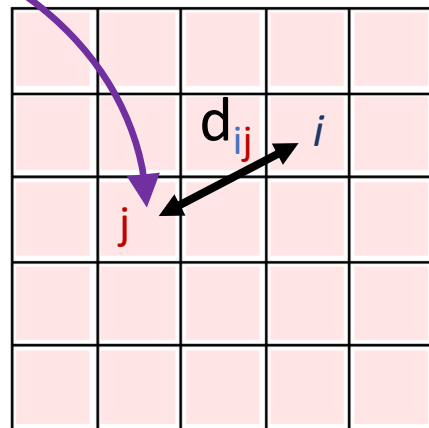
P. Komiske, E. Metodiev, J. Thaler 2019

$P$



$f_{ij}$

$Q$



$$\text{EMD}(P, Q) = \min_{\{f_{ij}\}} \sum_{ij} f_{ij} d_{ij}$$

$f_{ij}$  : energy transported

$d_{ij}$  : distance measure

$$f_{ij} \geq 0$$

$$\sum_{ij} f_{ij} = E_P^{\text{tot}} = E_Q^{\text{tot}} = 1$$

# Energy Mover's Distance

We propose a new event shape observable: **event isotropy**

CC, J. Thaler 2004.06125

*Energy mover's distance* (EMD):

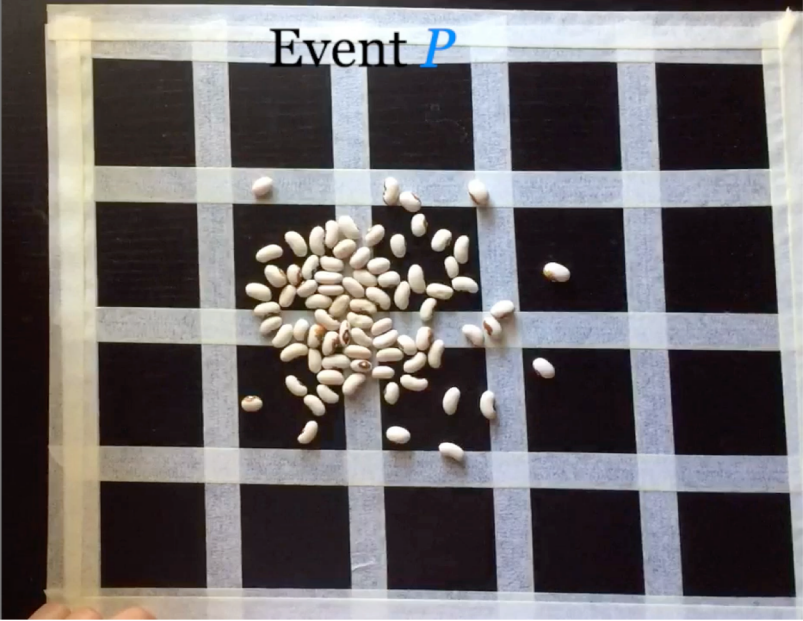
What is the minimum work to rearrange the energy distribution in event  $P$  to look like event  $Q$ ?

Start: Event  $P$

$$\text{EMD}(P, Q) = \min_{\{f_{ij}\}} \sum_{ij} f_{ij} d_{ij}$$

$f_{ij}$  Energy transported  
 $d_{ij}$  Distance measure  
 $f_{ij} \geq 0$   
 $\sum_{ij} f_{ij} = E_P^{\text{tot}} = E_Q^{\text{tot}}$

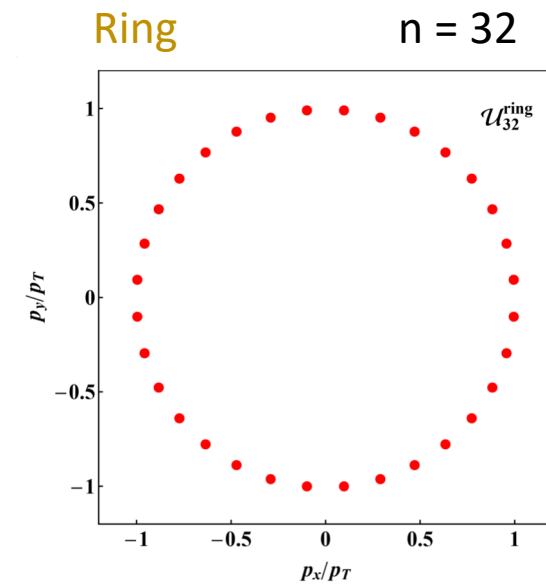
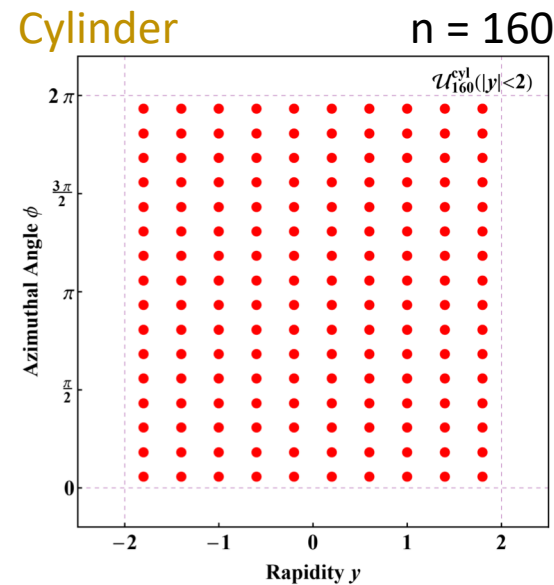
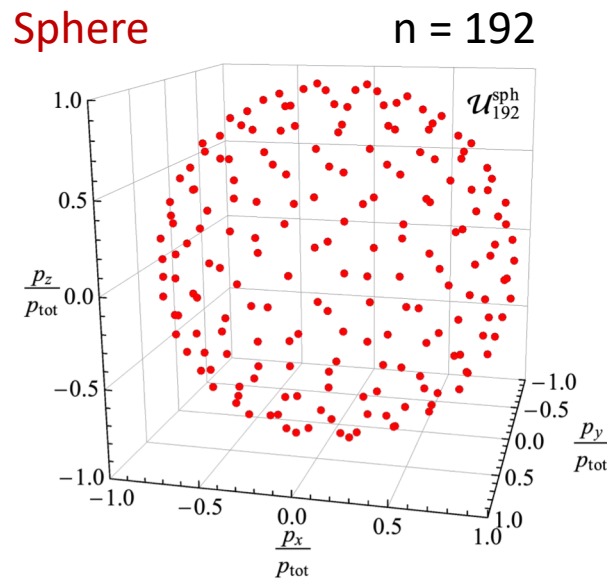
End: Event  $Q$



# Event Isotropy: EMD of an event to uniform radiation pattern

$$\mathcal{I}_n^{\text{geo}}(\mathcal{E}) = \text{EMD}_{\text{geo}}(\mathcal{U}_n^{\text{geo}}, \mathcal{E})$$

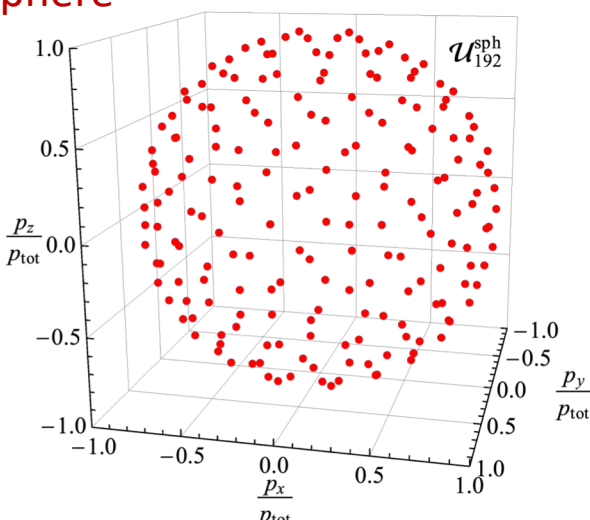
- *Geo*: Geometry of isotropic radiation pattern (sphere, cylinder, ring)
  - Associated energy weight  $w_i$  (moved with  $f_{ij}$ ) and distance measure  $d_{ij}$
- $n$ : Number of particles in quasi-uniform sample



# Event Isotropy

$$\mathcal{I}_n^{\text{geo}}(\mathcal{E}) = \text{EMD}_{\text{geo}}(\mathcal{U}_n^{\text{geo}}, \mathcal{E})$$

**Sphere**

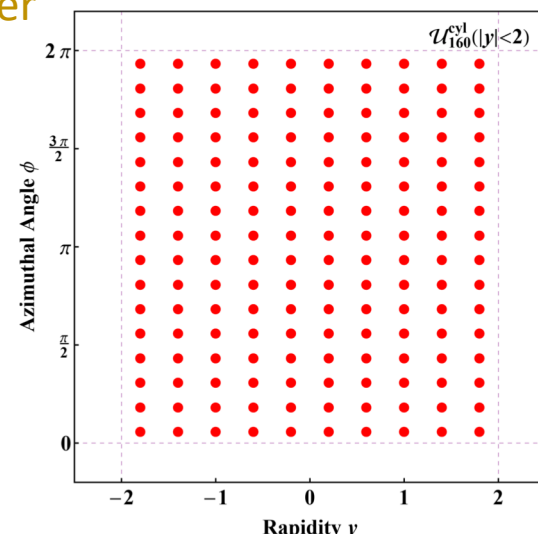


$e^+e^-$

$$w_i = E_i/E_{\text{tot}}$$

$$d_{ij} = 2(1 - \cos \theta_{ij})$$

**Cylinder**

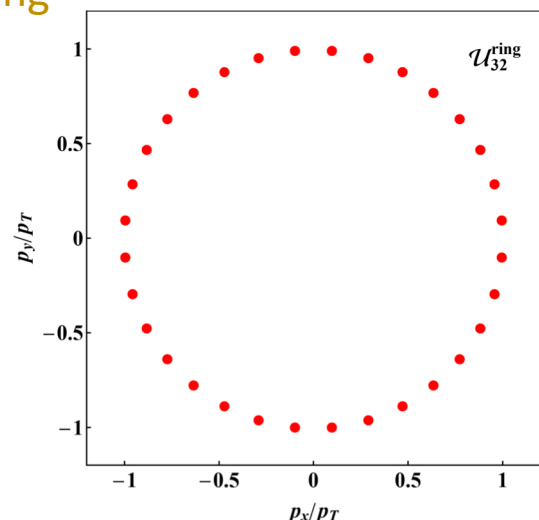


$pp$

$$w_i = p_{T,i}/p_{T,\text{tot}}$$

$$d_{ij} = \frac{12}{\pi^2 + 16y_{\text{max}}^2} (y_{ij}^2 + \phi_{ij}^2)$$

**Ring**



$pp$

$$w_i = p_{T,i}/p_{T,\text{tot}}$$

$$d_{ij} = \frac{\pi}{\pi - 2} (1 - \cos \phi_{ij})$$

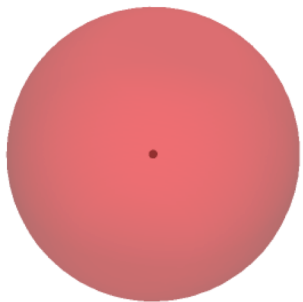
# Event Isotropy

- IRC safe
- Dimensionless
- Defined on sets with zero net momentum
- $\mathcal{I} \in [0, 1]$ , where 0 is isotropic and 1 is dijet

$$\mathcal{I}_n^{\text{geo}}(\mathcal{E}) = \text{EMD}_{\text{geo}}(\mathcal{U}_n^{\text{geo}}, \mathcal{E})$$

$$\mathcal{I}^{\text{sph}} = 0$$

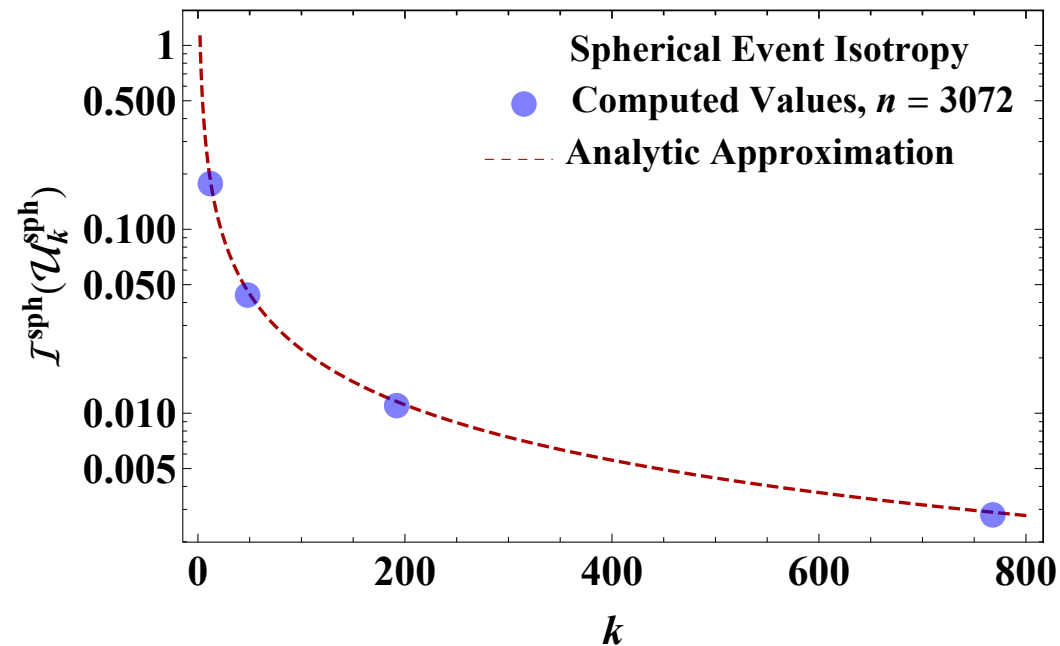
$$\mathcal{I}^{\text{sph}} = 1$$



# Event Isotropy

Any finite-multiplicity event has a **theoretical bound** on isotropy which is saturated when the event is symmetrized on the geometry

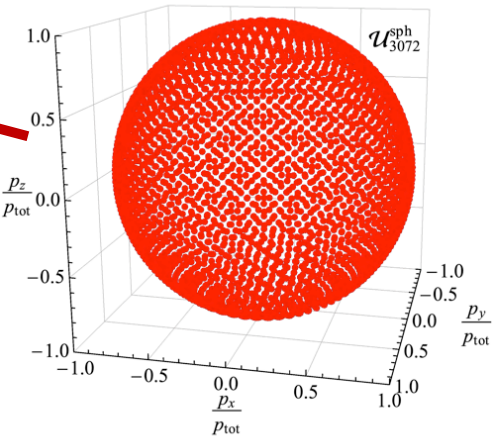
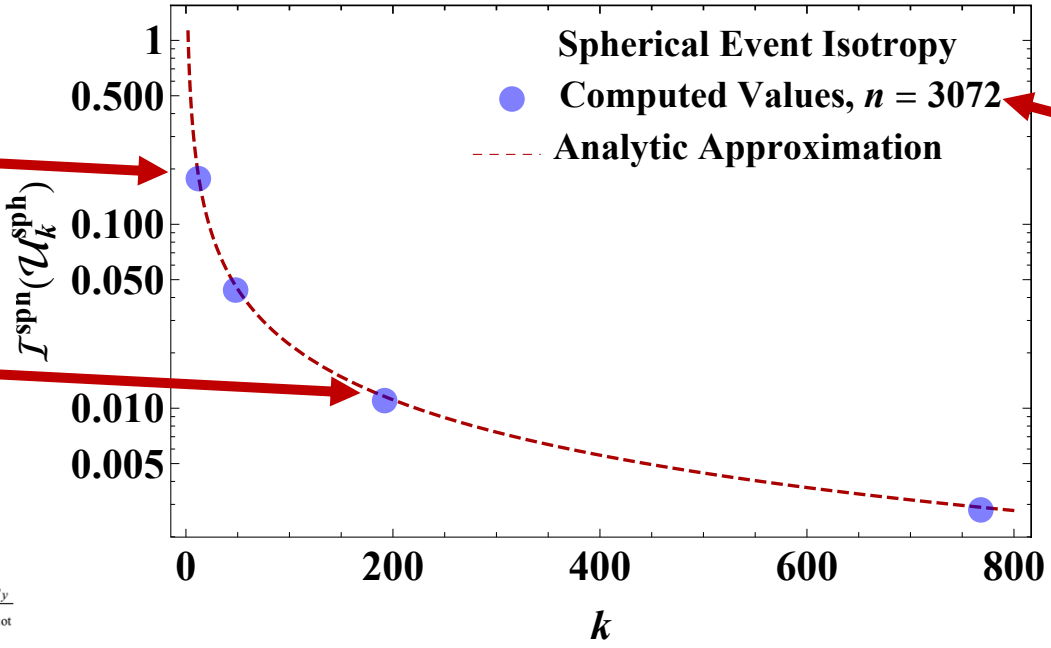
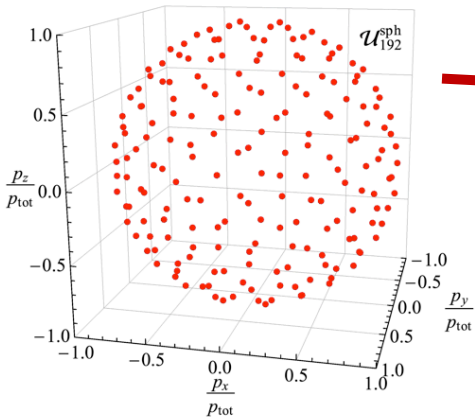
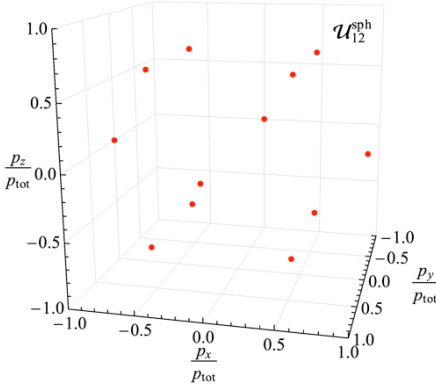
*Analytic approximations match computation well*



# Event Isotropy

Any finite-multiplicity event has a **theoretical bound** on isotropy which is saturated when the event is symmetrized on the geometry

*Analytic approximations match computation well*





Part 1: Defining Event Isotropy

Part 2: **Applications** of Event Isotropy  
at FCC-ee

# Standard Model Benchmark

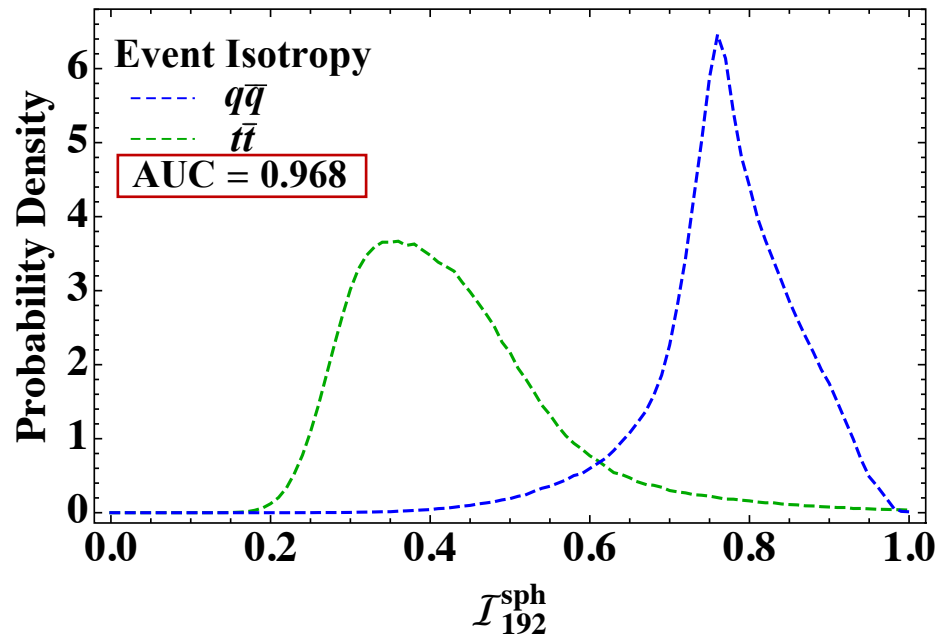
QCD dijet vs. top pair production

$e^+e^-$  Collisions at  $\sqrt{s} = 350$  GeV

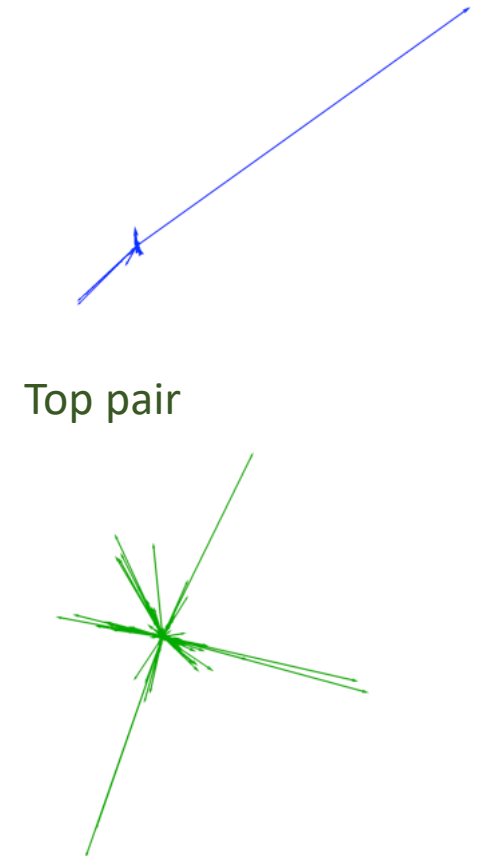
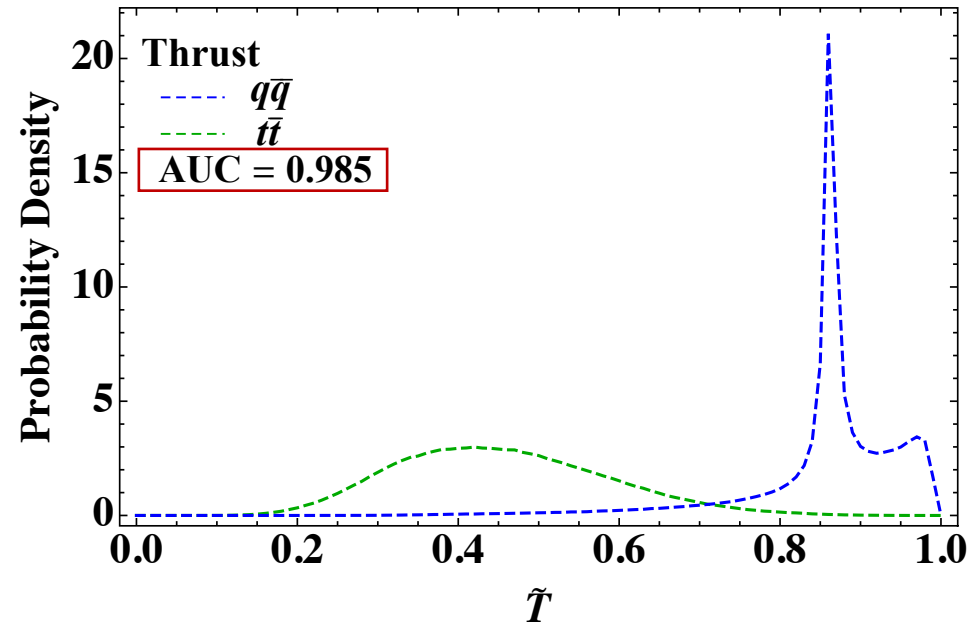
*Sphere Geometry*

QCD Dijet

Event isotropy



Scaled thrust



CC, J. Thaler (2004.06125)

# Standard Model Benchmark

QCD dijet vs. top pair production

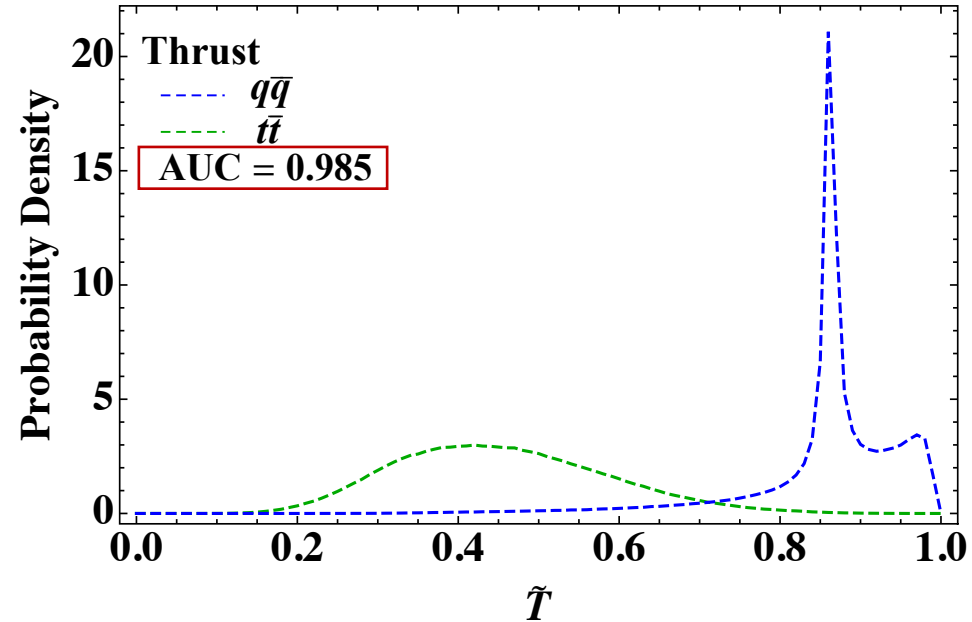
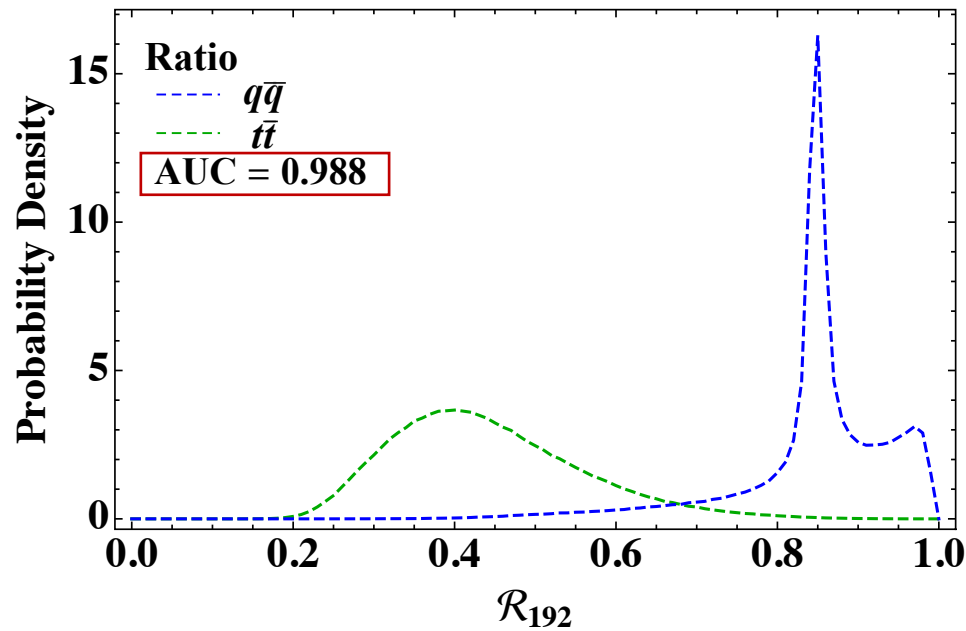
$e^+e^-$  Collisions at  $\sqrt{s} = 350$  GeV

*Sphere Geometry*

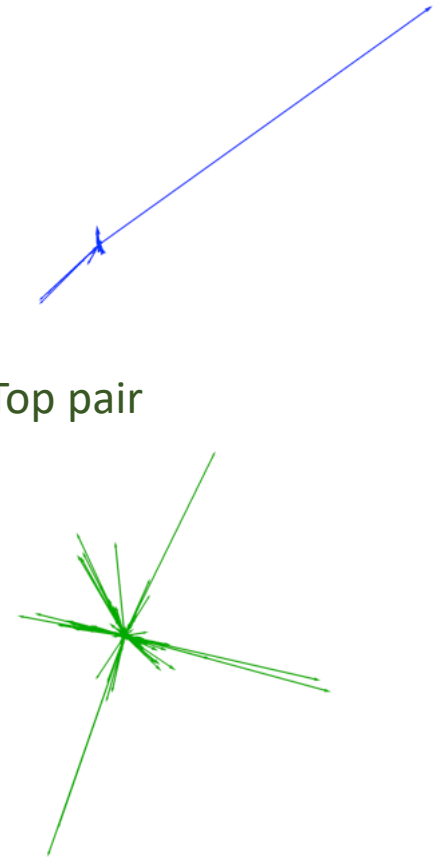
QCD Dijet

$$\mathcal{R}_{192} = \frac{\mathcal{I}_{192}^{\text{sph}}}{\mathcal{I}_{192}^{\text{sph}} + (1 - \tilde{T})}$$

Scaled thrust



Top pair



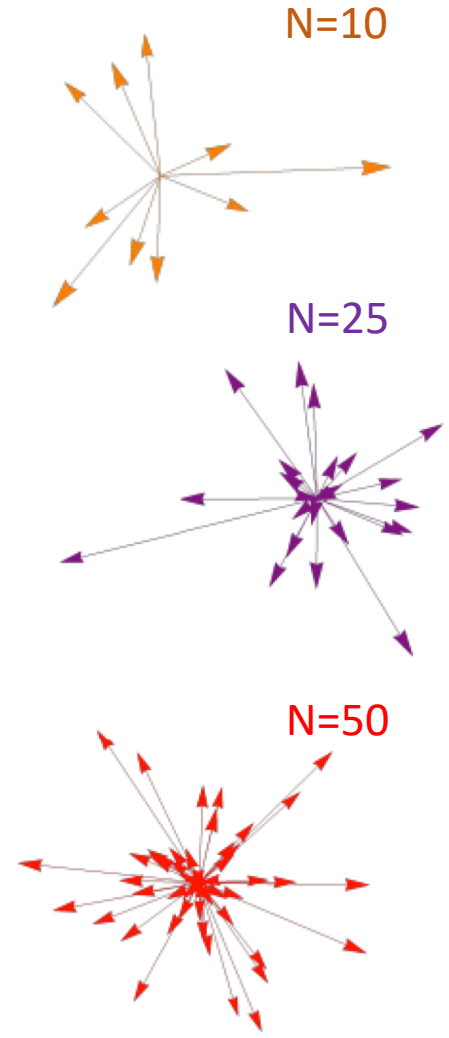
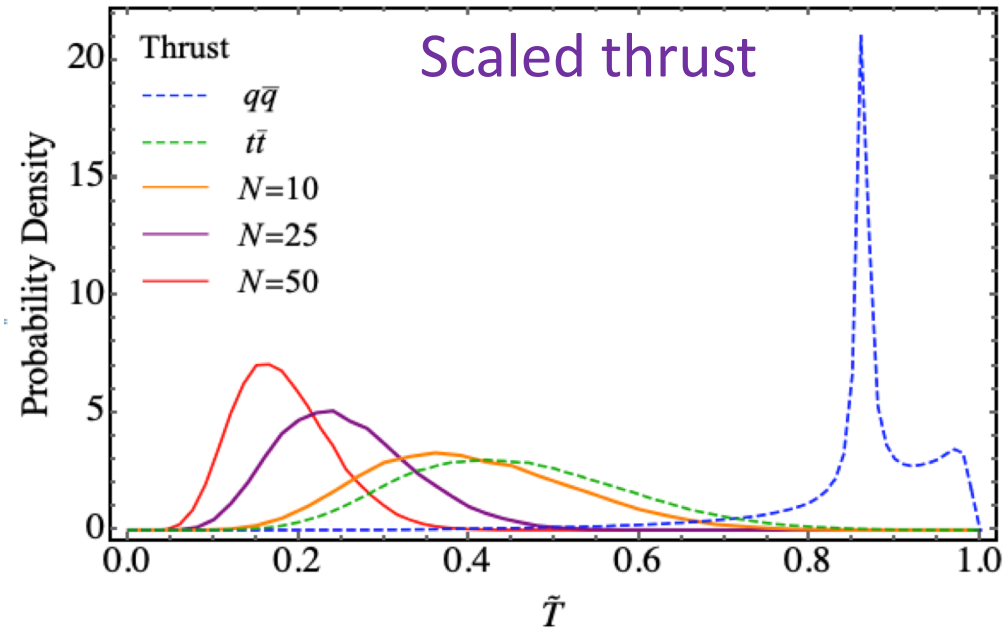
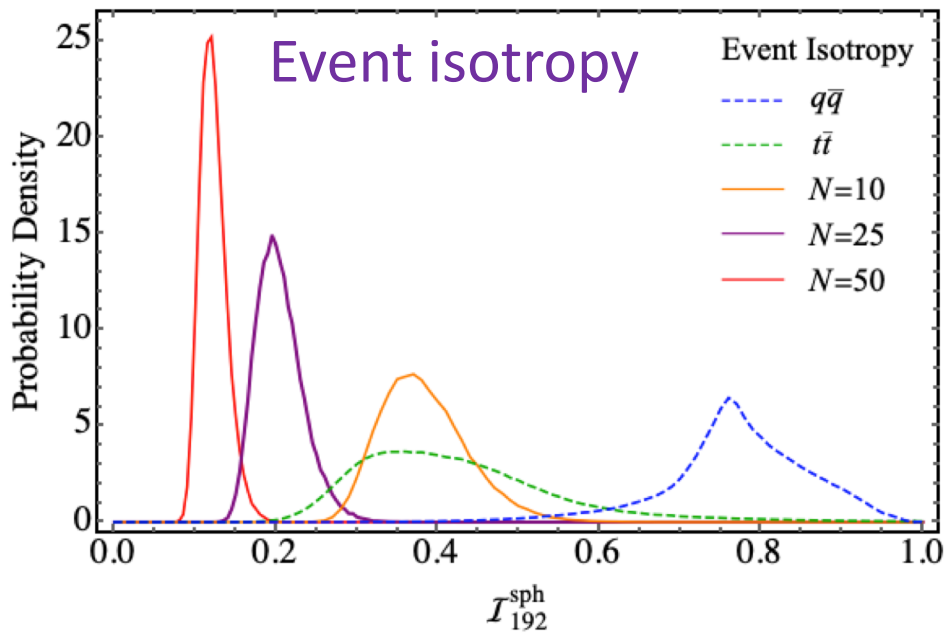
CC, J. Thaler (2004.06125)

# Toy Model: Uniform $N$ -body Phase space

Discriminating  $N = \{10, 25, 50\}$ -body samples

$e^+e^-$  Collisions at  $\sqrt{s} = 350$  GeV

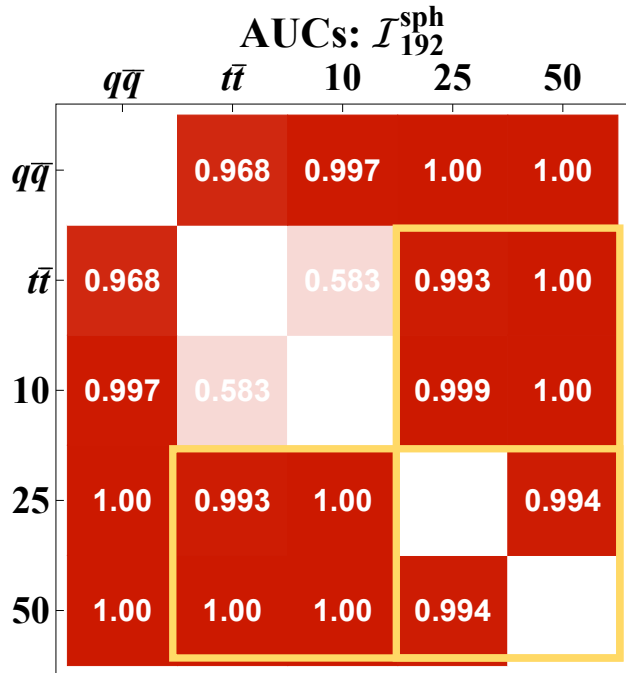
*Spherical Geometry*



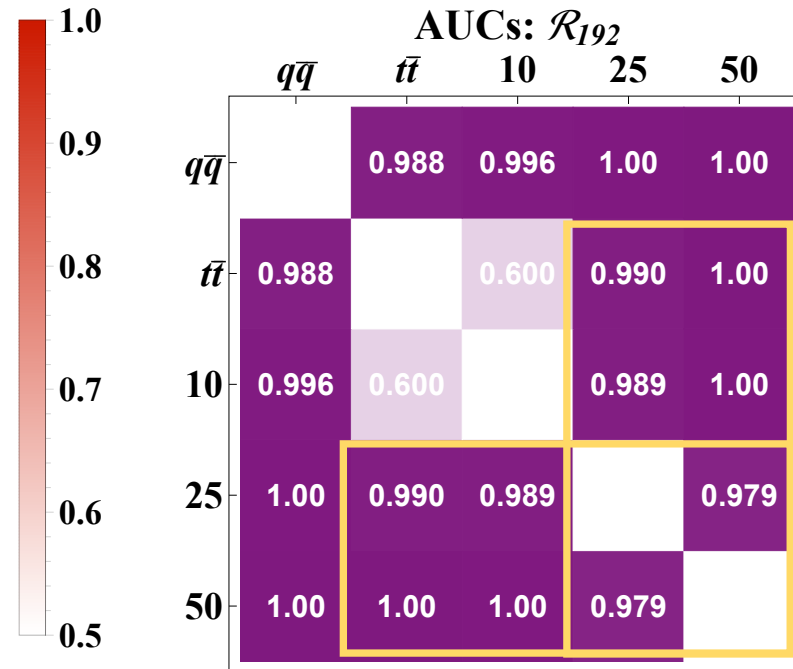
CJC, J. Thaler (2004.06125)

# Benchmark Summary

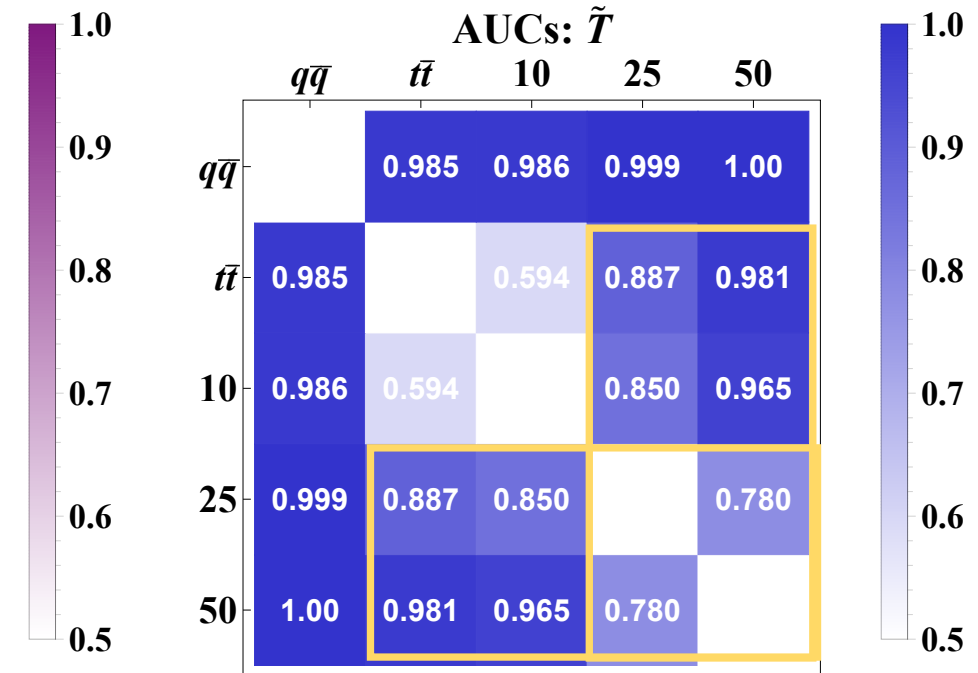
Event isotropy



Ratio



Scaled thrust



Event isotropy excels at differentiating quasi-isotropic event topologies from each other

# Conclusions

Event isotropy is useful for discriminating and characterizing events in the quasi-isotropic regime

## Part 1:

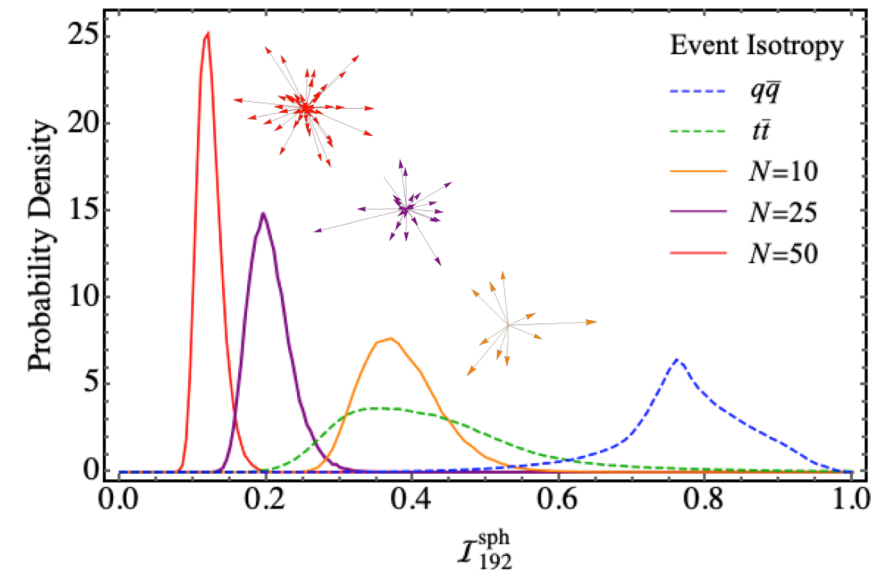
- Application of Energy Mover's Distance
- Calculated with Wasserstein Distance

## Part 2:

- Discriminates between quasi-uniform samples
- Characterizes event shape of new physics and high multiplicity SM events

## Future Studies

*!Jet isotropy:* To consider isotropic signatures boosted against a jet, remove jet and boost remaining event backwards by jet momentum



Thank you!

Back ups:

# Dark Showers & Event Isotropy

# Dark Showers from 5d Simplified Models

Using 5d simplified models, we can model many particles and interactions with **few parameters**

Consider slice of (4+1)d AdS (RS1) with scalars that propagate in the bulk

- Each scalar has infinite Kaluza-Klein tower scalars
- Gauge / gravity duality: Interpret KK modes as 4d hadrons

$$\underbrace{\Phi(x^\mu, z)}_{\text{5d Scalar}} = \sum_{n=1}^{\infty} \underbrace{\phi_n(x^\mu)}_{\text{4d Hadrons}} \underbrace{\psi_n(z)}_{\substack{\text{Wave function in } z \\ \text{Warped Finite Extra Dim.}}}$$



# Dark Showers from 5d Simplified Models

Including a cubic coupling between 5d field  $\leftrightarrow$  infinite cubic couplings between KK modes in 4d

$$\int \sqrt{g} d^4x dz \mathcal{L}_{\text{int}} = - \int \sqrt{g} d^4x dz c \Phi_1 \Phi_2 \Phi_3 \quad \leftarrow \text{plug in expansion} \quad \left[ \Phi(x^\mu, z) = \sum_{n=1}^{\infty} \phi_n(x^\mu) \psi_n(z) \right]$$

$$= - \int d^4x c \sum_{i,j,k} \left( \int \sqrt{g} dz \psi_{1,i}(z) \psi_{2,j}(z) \psi_{3,k}(z) \right) \phi_{1,i}(x) \phi_{2,j}(x) \phi_{3,k}(x)$$

Wavefunctions control 4d coupling:  $\mathcal{L}_{4d} \supset \sum_{i,j,k} c_{ijk} \phi_{1,i}(x) \phi_{2,j}(x) \phi_{3,k}(x);$

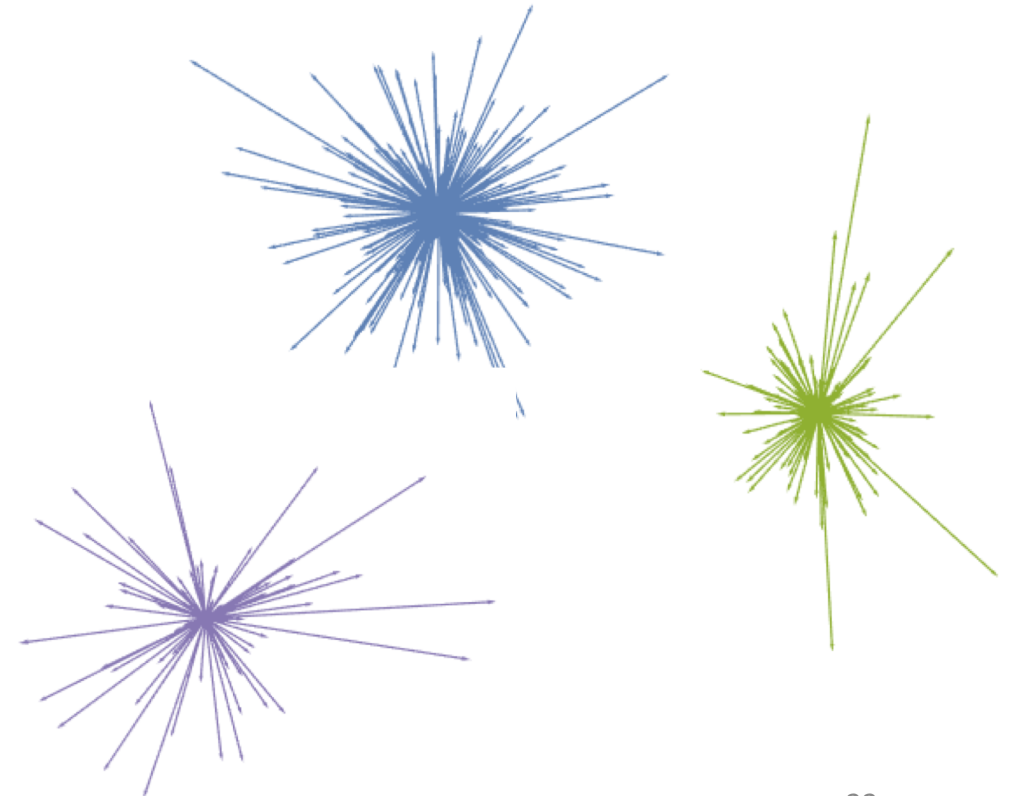
# Dark Showers from 5d Simplified Models

5d scalar mass corresponds to different phenomenology in dark shower

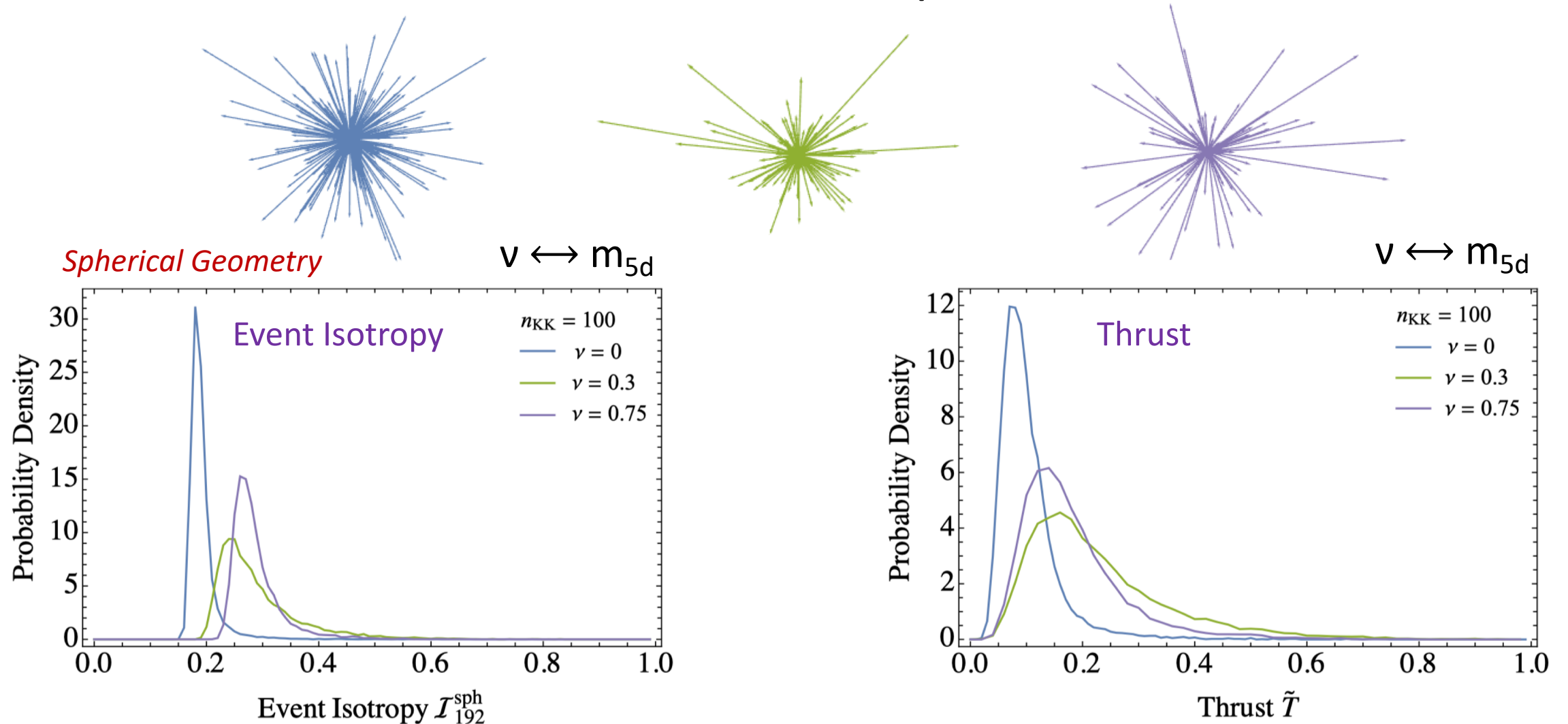
**Goal of model:** interpolate between *jetty* and *spherical* signatures

Model dark shower as

1. Starting at  $n_{\text{KK}} = 100$
2. Two-body decays between modes:  
$$\phi_n \rightarrow \phi_m \phi_l$$
3. Cascade develops to stable 4d hadrons
4. Split hadrons into 2 massless particles



# Dark Showers from 5d Simplified Models

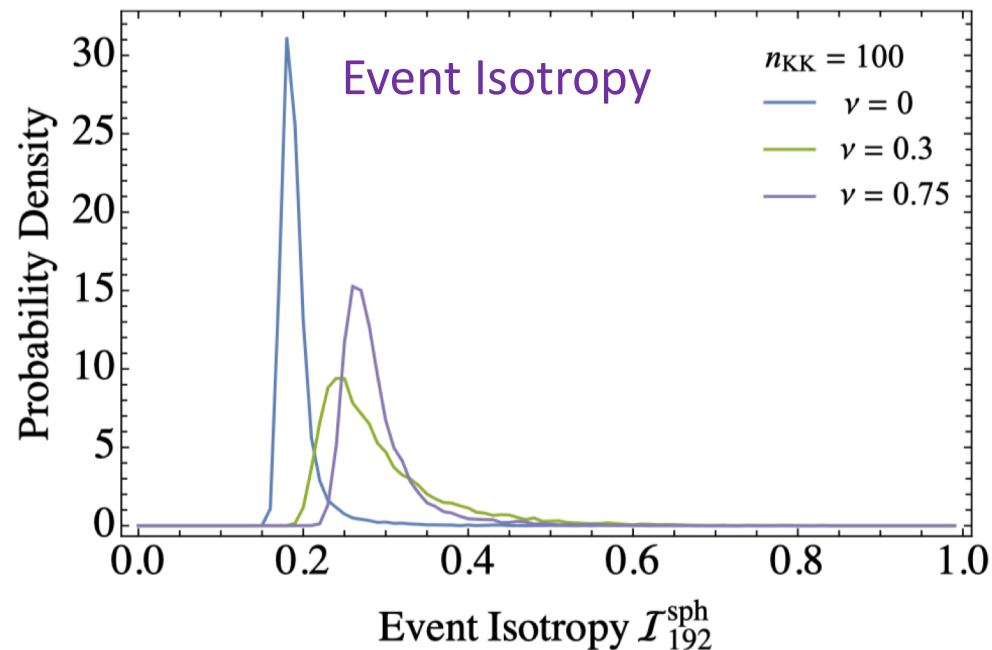


# Dark Showers from 5d Simplified Models

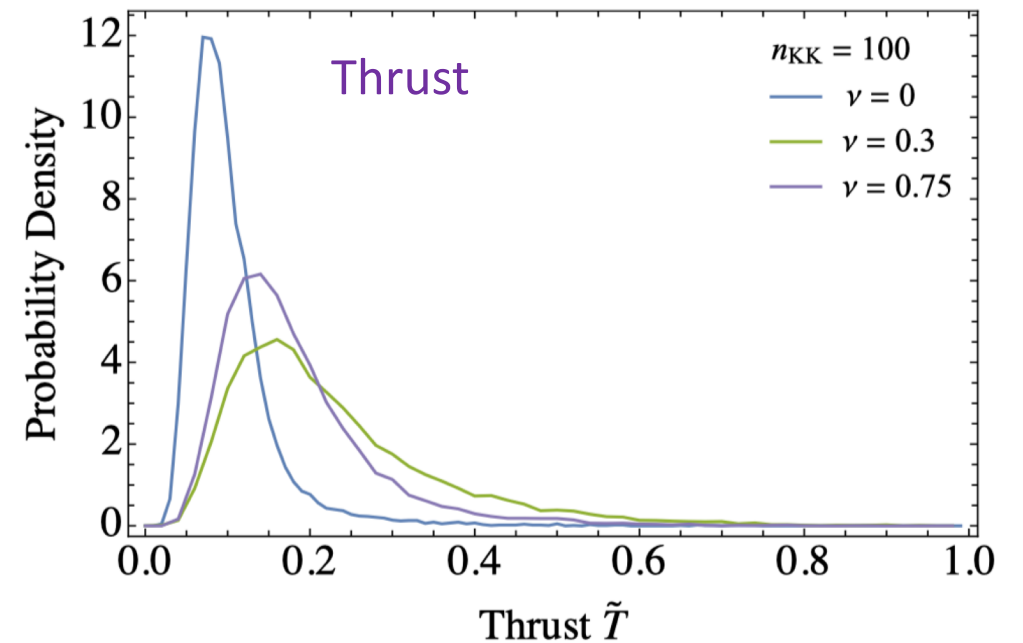
Clearly, thrust & event isotropy probe different structure!

Spherical Geometry

$v \leftrightarrow m_{5d}$



$v \leftrightarrow m_{5d}$



# Dark Showers from 5d Simplified Models

