

# prediction for LHC $J/\Psi$ Enhancement from RHIC extrapolation (and a bit of physics too)

## Rete Quarkonii 2010 (Nantes)

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SUBATECH, UMR 6457

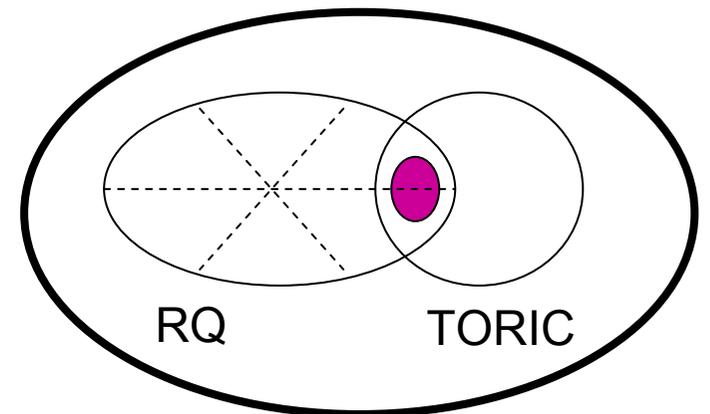
Université de Nantes, Ecole des Mines de Nantes, IN2P3/CNRS

With J. Aichelin H. Berrehrah & Th. Gousset,

I. Motivation

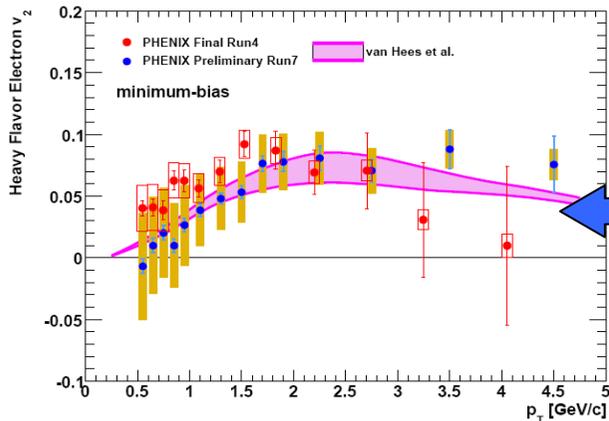
II. Understanding (partly) the present RHIC data on HQ E-loss

III. Quarkonia formation: probing the QGP ?



# Why ♥ heavy flavors in A-A (open and hidden)?

**Prejudice:** Open heavy flavors are mandatory to understand Q-Qbar evolution in QGP & quarkonia production



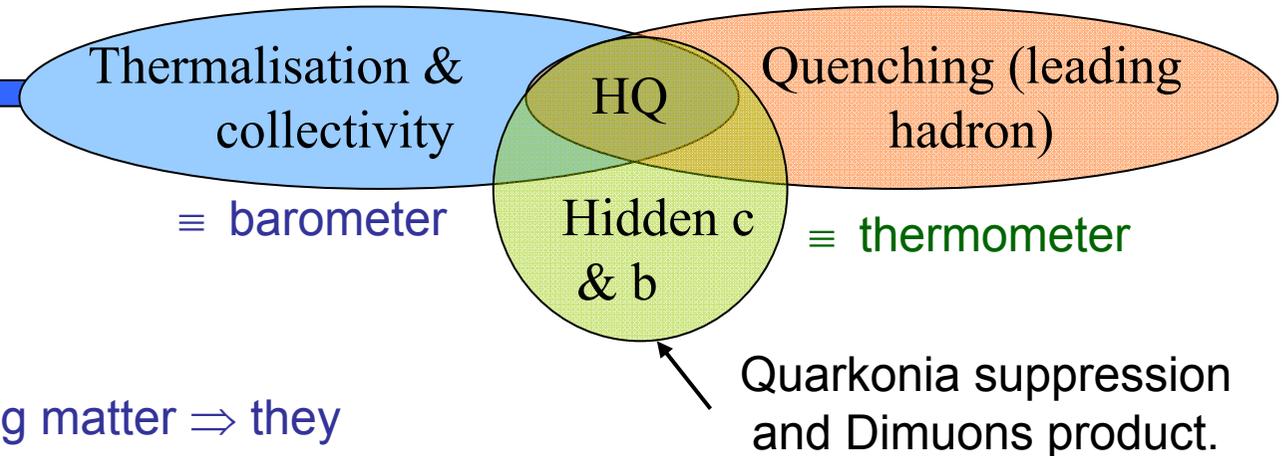
RHIC

HQ are imbedded in expanding matter  $\Rightarrow$  they participate to collective motion and gain elliptic flow ( $v_2$ : azimuthal asymmetry) at finite b

## Challenges:

- Description of HQ E-loss / equilibration from fundamental theory
- Joint  $v_2$ - $R_{AA}$  explanation ... will help to **better understand the theory**

## The Trilogy:



# Quarkonia in Stationary QGP

How can we prove (at best) that we have achieved is really *deconfined* state of matter ?

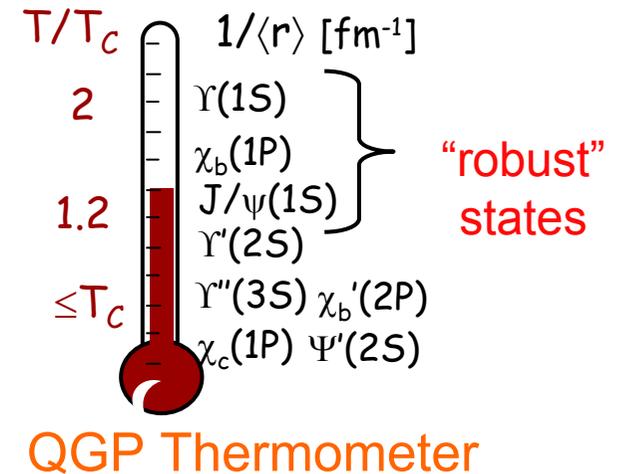
**Challenge**

“deconfinometer”  $\equiv$  {

- Color fluctuations
- Propagation of quarks over large distances

Best candidate:

Quarkonia (Q-Qbar bound state) sequential “suppression”, i.e. melting and/or dissociation (Matsui & Satz 86)



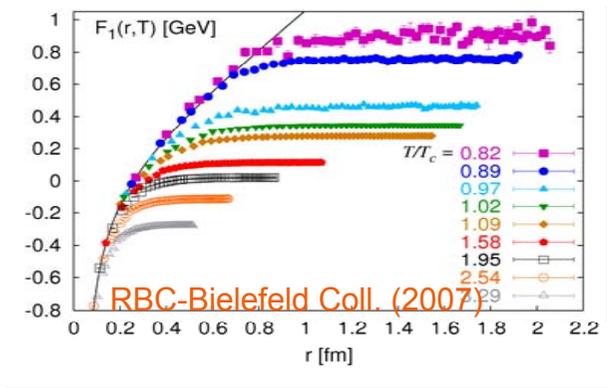
Indeed observed at SPS (CERN) and RHIC (BNL) experiments. However:

- alternative explanations, lots of unknown (also from theory side)
- no additional suppression at RHIC w.r.t. SPS !

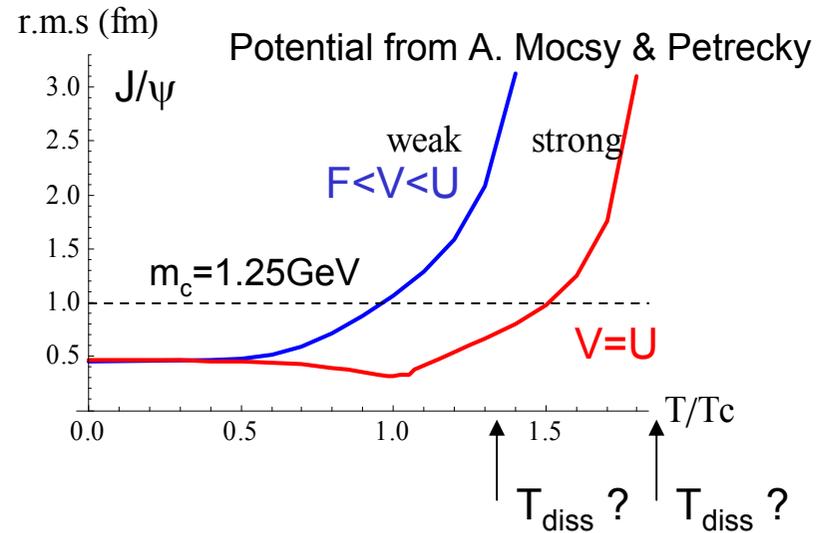
Nevertheless: Still best candidate and dedicated (di- $\mu$ ) program at LHC

# Caviats & Uncertainties (why ?)

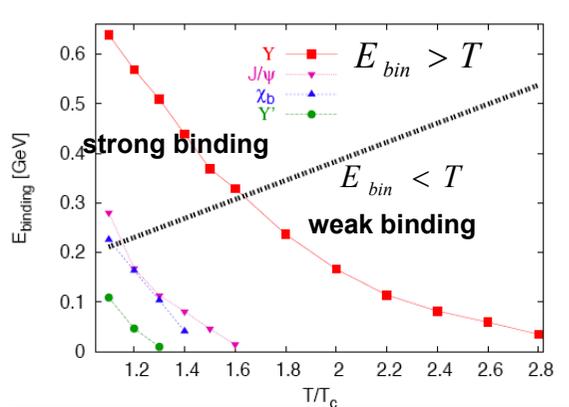
I. Quarkonia in *stationnary* medium are not understood from the fundamental LQCD theory



$\Rightarrow V(r,T) ?$



II. Criteria for quarkonia “existence” (as an effective degree of freedom) in *stationnary* medium is even less understood



III. What does this stationary picture has to do with reality anyhow ?

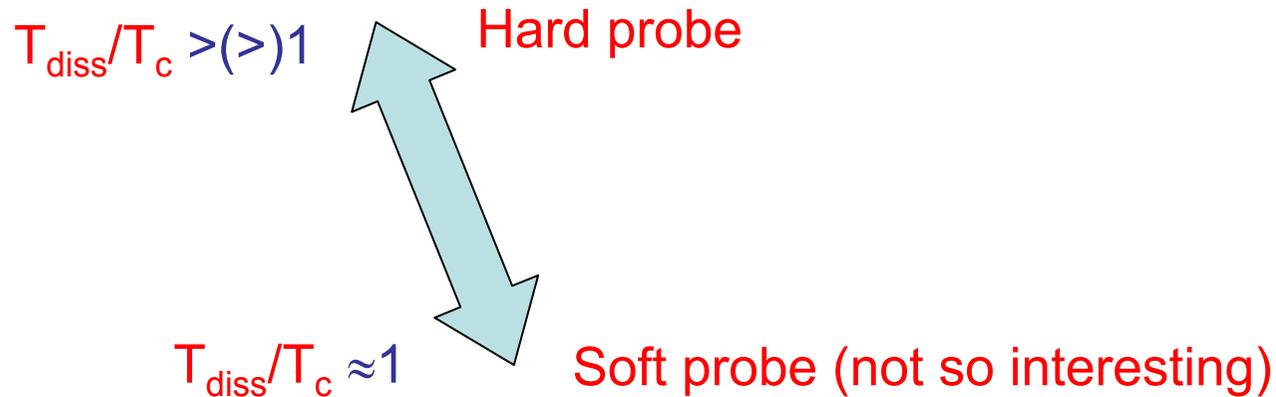
Quarkonia in URHIC... Can they teach us something about QGP (properties)?

Nothing quantitative ?

Nothing at all ?

# Semi-Qualitative questions

1. Are the data compatible with the picture of a strongly bound  $J/\psi$  (sequential suppression) ?



2. Can we challenge the picture of statistical recombination (A. Andronic, PBM, J. Stachel) ?

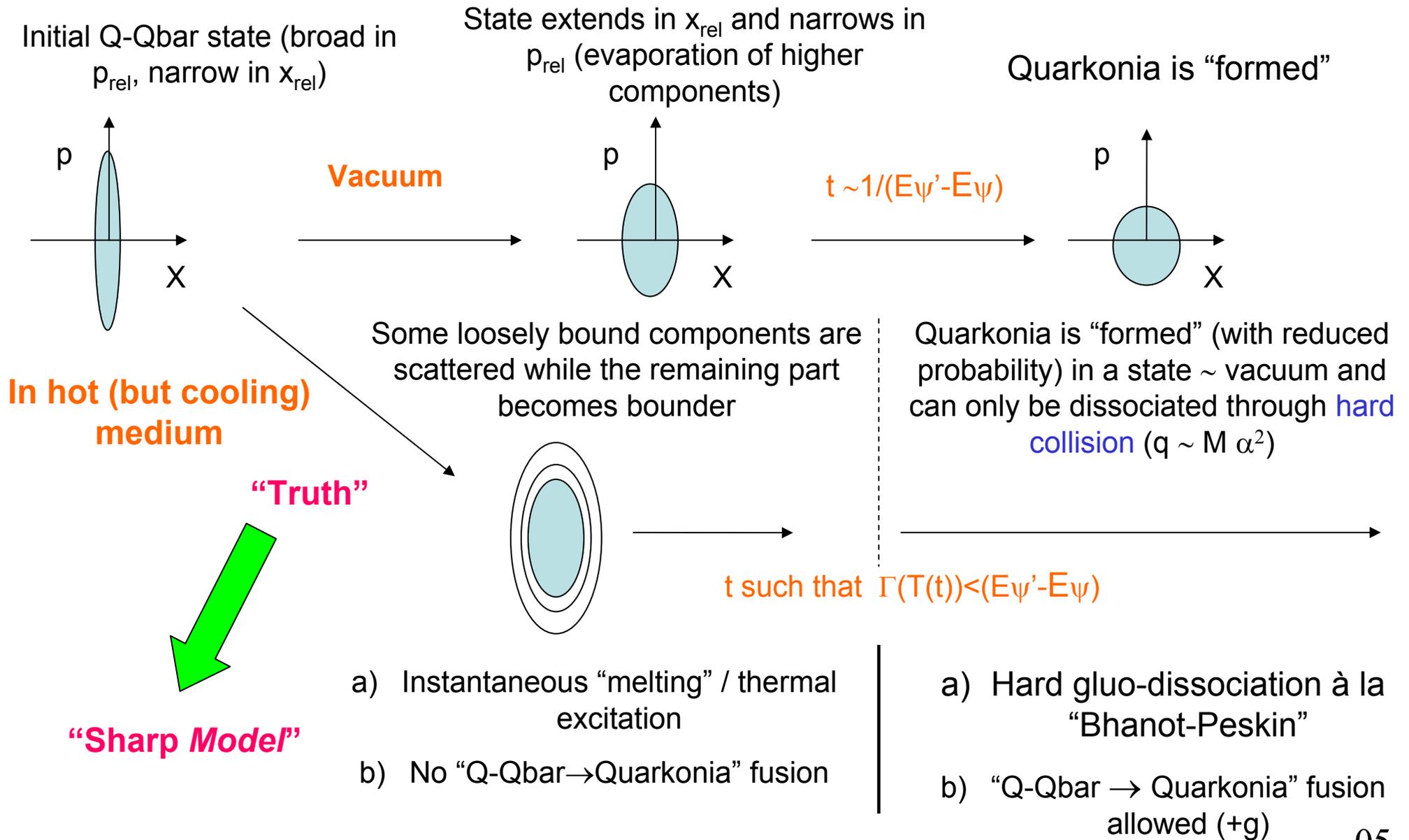
3. Can we try to *extract* the dissociation temperature from the data ?

The *main* object of interest here:  $T_{\text{diss}}$  (thermometer aspect): one of the fundamental quantities of statistical QCD.

4. Can we transpose our “understanding” of RHIC to make some predictions for LHC ?

**Need for a time-dependent scenario**

# Quarkonia fate along decreasing $T(t)$

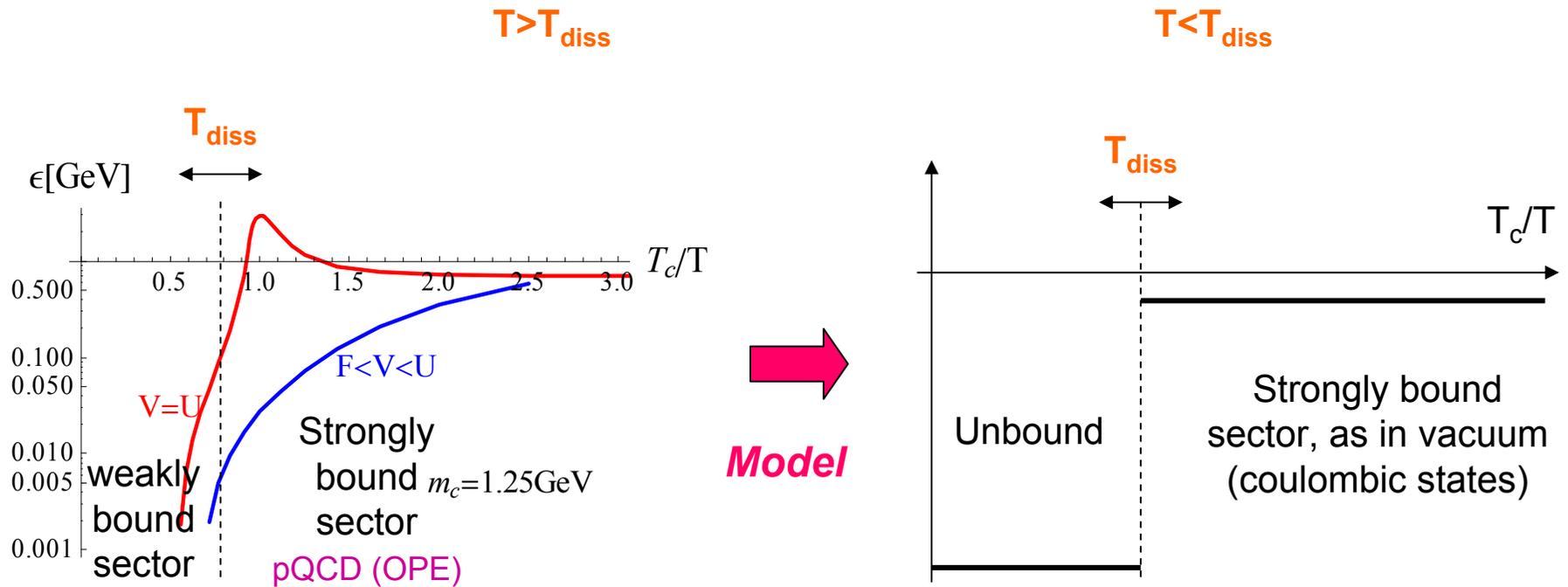


# Quarkonia fate along decreasing $T(t)$

**“Sharp Model”**

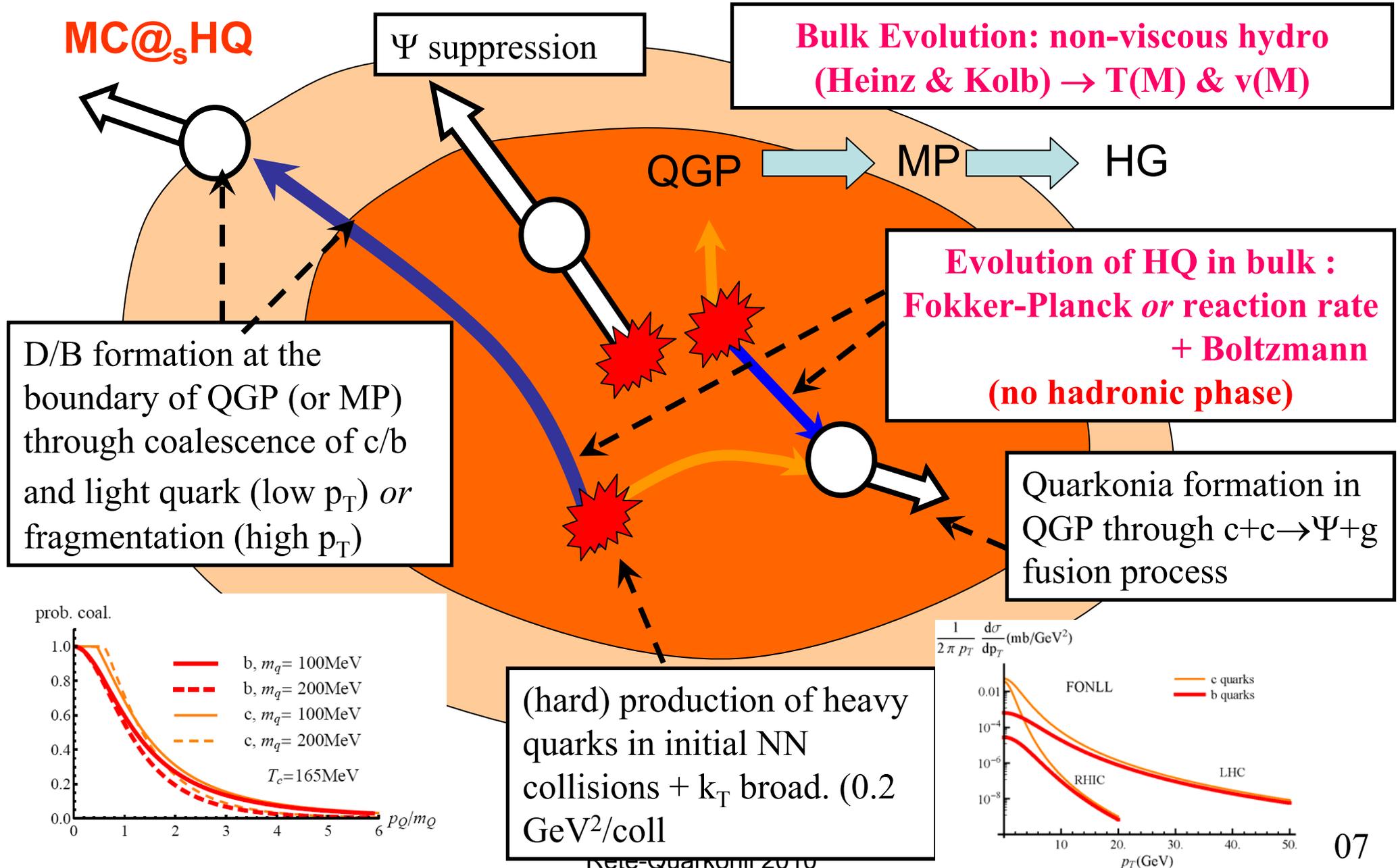
- a) Instantaneous melting / thermal excitation
- b) No “Q-Qbar → Quarkonia” fusion

- a) Hard gluo-dissociation à la “Bhanot-Peskin”
- b) “Q-Qbar → Quarkonia” fusion allowed



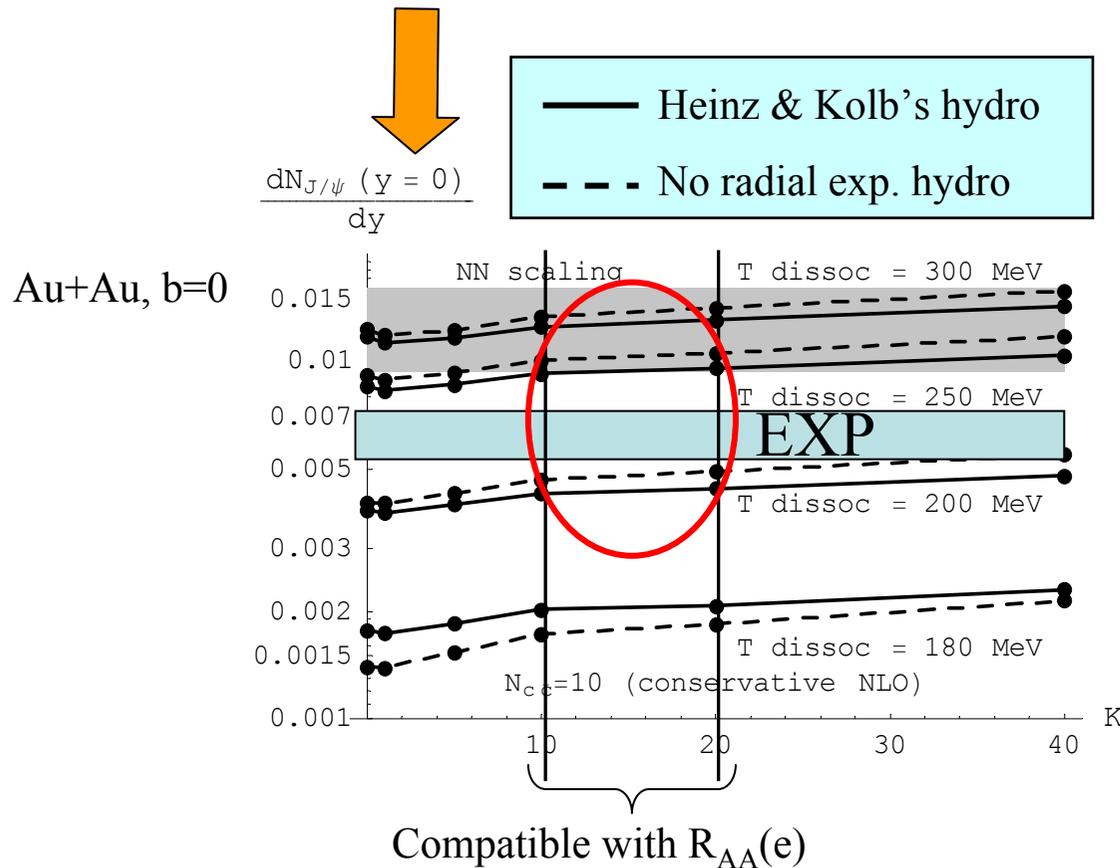
The idea: AS THE LATTICE and POTENTIAL MODELS are inconclusive, let  $T_{diss}$  as a free parameter and see if this can be constrained by the data (hence the title)

# Schematic view of the global framework



# The Landscape

Degree of thermalization of heavy quarks will not affect “too much” the integrated production rates;  $T_{\text{diss}}$  is the driving parameter for "recombined"  $J/\psi$  :



From SQM 2004, with additional Au+Au data.

Hope that the quarkonia production would be dominated by recombination

Multiple of pQCD stopping force ( $\alpha_s=0.3$ )

# I. “Understanding” the RHIC HQ-data

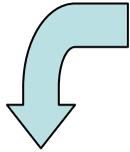
What is the dominant E loss mechanism @ RHIC ?  
And does its detailed origin influence the fate of  
quarkonia's ?

# Based on

- *Heavy quarks thermalization in ultra relativistic heavy ion collisions: Elastic versus Radiative*, P.B. Gossiaux, V. Guiho & J. Aichelin, Journal of Physics G **32** (2006) S359
- *Towards an understanding of the single electron data measured at the BNL Relativistic Heavy Ion Collider (RHIC)*, P.B. Gossiaux & J. Aichelin, Phys. Rev. C **78**, 014904 (2008); [arXiv:0802.2525 ]
- *Tomography of quark gluon plasma at energies available at the BNL Relativistic Heavy Ion Collider (RHIC) and the CERN Large Hadron Collider (LHC)*, P.B. Gossiaux, R. Bierkandt & J. Aichelin, Physical Review C **79** (2009) 044906; [arXiv:0901.0946]
- *Tomography of the Quark Gluon Plasma by Heavy Quarks*, P.-B. Gossiaux & J. Aichelin, J. Phys. G **36** (2009) 064028; [arXiv:0901.2462]
- *Energy Loss of Heavy Quarks in a QGP with a Running Coupling Constant Approach*, P.B. Gossiaux & J. Aichelin, Nucl. Phys. A **830** (2009), 203; [arXiv:0907.4329]
- *Competition of Heavy Quark Radiative and Collisional Energy Loss in Deconfined Matter*, P.B. Gossiaux, J. Aichelin, T. Gousset & V. Guiho, J. Phys. G: Nucl. Part. Phys. **37** (2010) 094019; [arXiv:1001.4166]
- *Gluon Radiation at small  $kT$  and Radiative Energy Loss of Heavy Quarks; I. The Bethe-Heitler Regime*, J. Aichelin, P.B. Gossiaux & Th Gousset (**In preparation**)

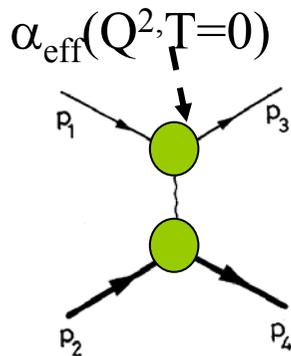
# Collisional E loss : The Peshier – Gossiaux – Aichelin approach (2008)

Motivation: Even a fast parton with the largest momentum  $P$  will undergo collisions with moderate  $q$  exchange and large  $\alpha_s(Q^2)$ . The running aspect of the coupling constant has been “forgotten/neglected” in most of approaches

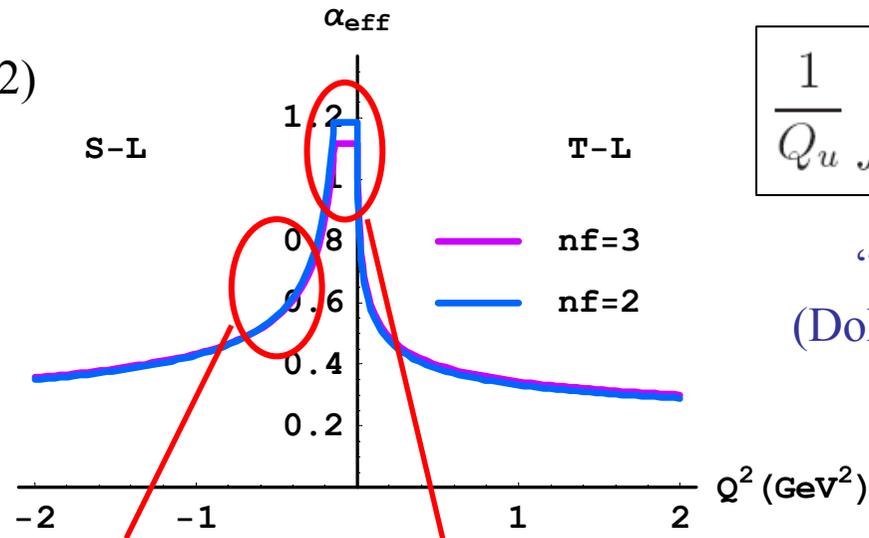


Effective  $\alpha_s(Q^2)$

(Dokshitzer 95, Brodsky 02)



Large values for intermediate momentum-transfer => larger cross section



IR safe. The detailed form very close to  $Q^2 = 0$  is not important does not contribute to the energy loss

$$\frac{1}{Q_u} \int_{|Q^2| \leq Q_u^2} dQ \alpha_s(Q^2) \approx 0.5$$

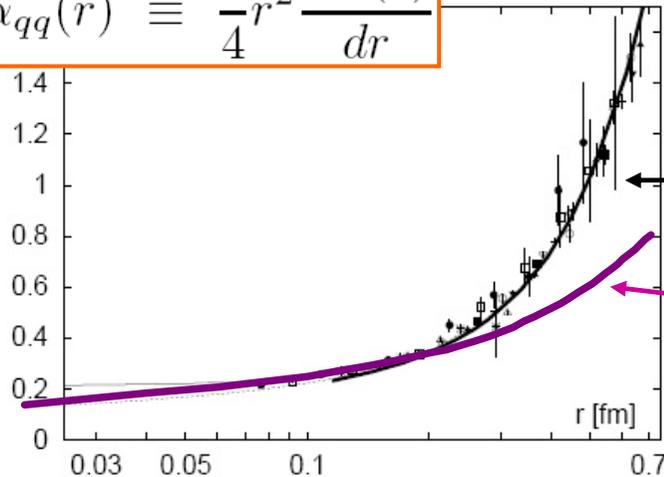
“Universality constrain” (Dokshitzer 02) helps reducing uncertainties:

**A model; not a renormalizable theory**

# $\mu$ -local-model: Eff. Running $\alpha_s$ vs lQCD

**T=0**

$$\alpha_{qq}(r) \equiv \frac{3}{4} r^2 \frac{dV(r)}{dr}$$



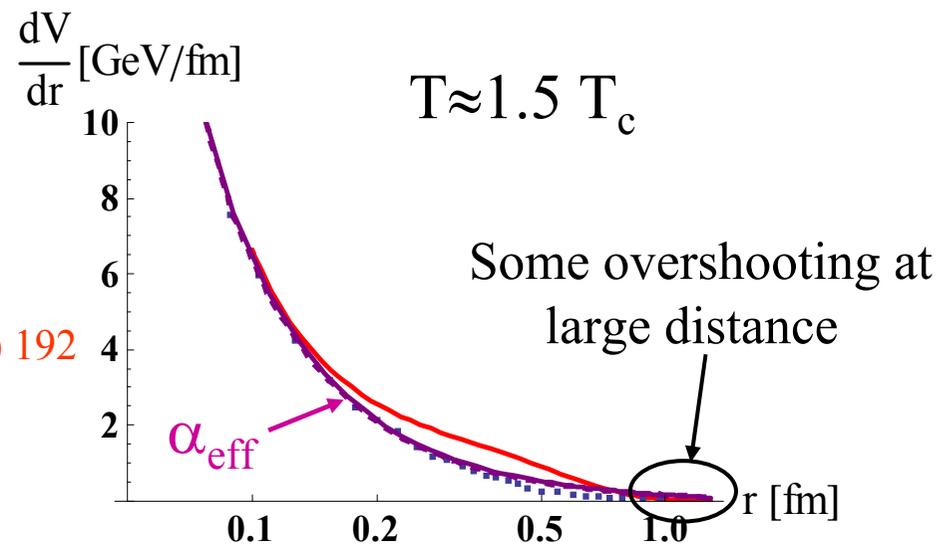
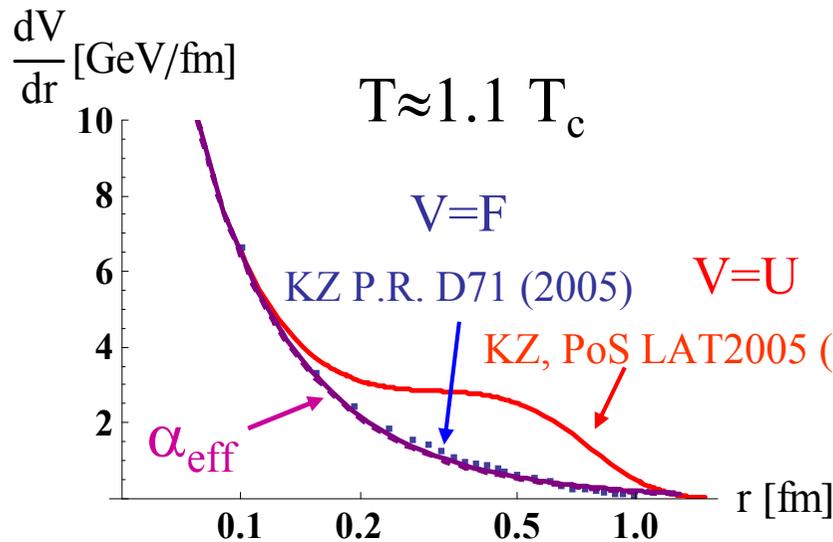
O. Kaczmarek & F. Zantow (KZ) ( $n_f=2$  QCD), P.R.D71 (2005) 114510

Genuine non-pert (string)

optimal  $\mu$ , running  $\alpha_{\text{eff}}$

V: $\omega=0$  sector; dE/dx: finite  $\omega$

## Finite T



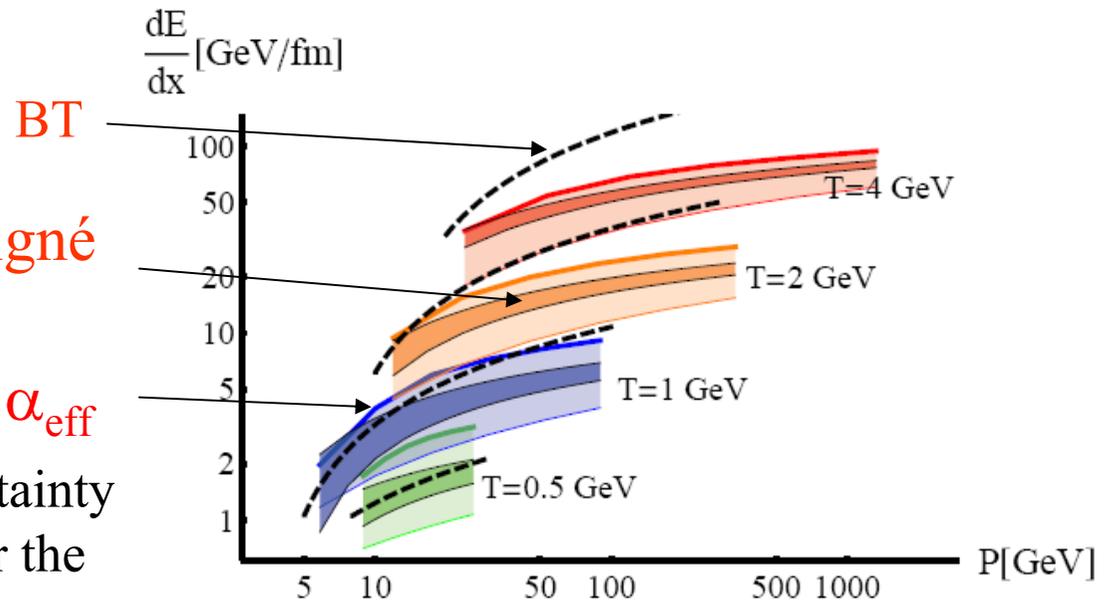
**Merging at  $\approx 2 T_c$**   
Rete-Quarkonii 2010

# $\mu$ -local-model: Eff. Running vs fixed $\alpha_s$

Dark bands: Peshier & Peigné  
(2008)

E: optimal  $\mu$ , running  $\alpha_{\text{eff}}$

Light bands: theoretical uncertainty  
related to the prescription for the  
HTL-hard transition



## Conclusions:

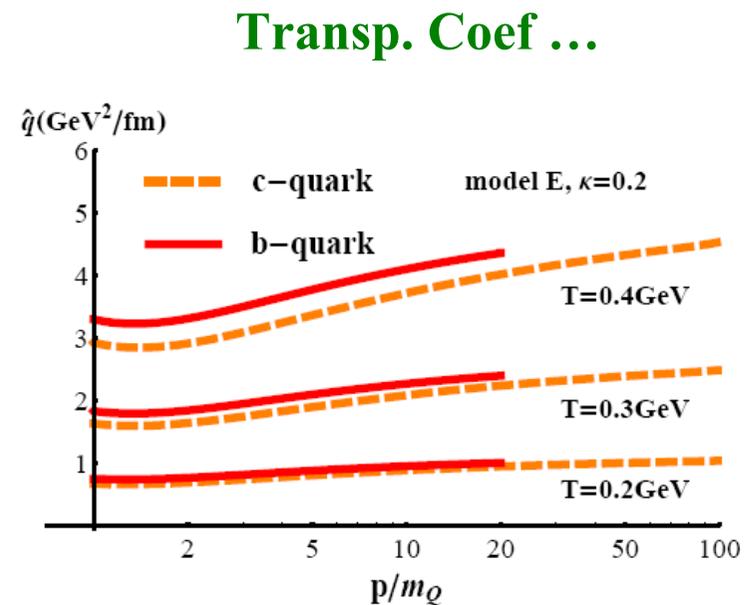
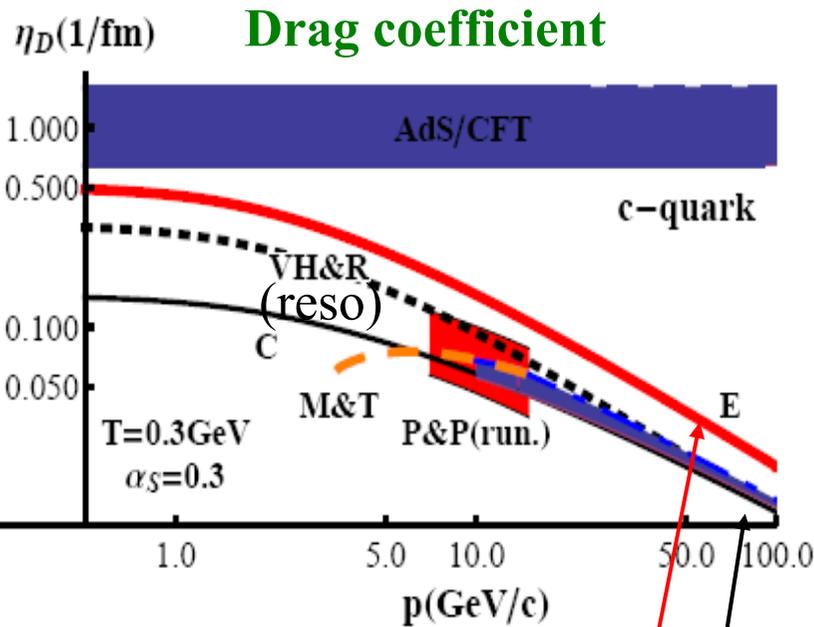
- Good agreement with PP for large T and large P
- Running  $\alpha_s$  is more than a cranking of BT (different shapes and T-dependences)

# Running $\alpha_s$ : some Energy-Loss values for purely collisional processes

$$\frac{dE_{coll}(c/b)}{dx}$$

T(MeV) \ p(GeV/c)	10	20
200	1 / 0.65	1.2 / 0.9
400	2.1 / 1.4	2.4 / 2

**≈ 10 % of HQ energy**

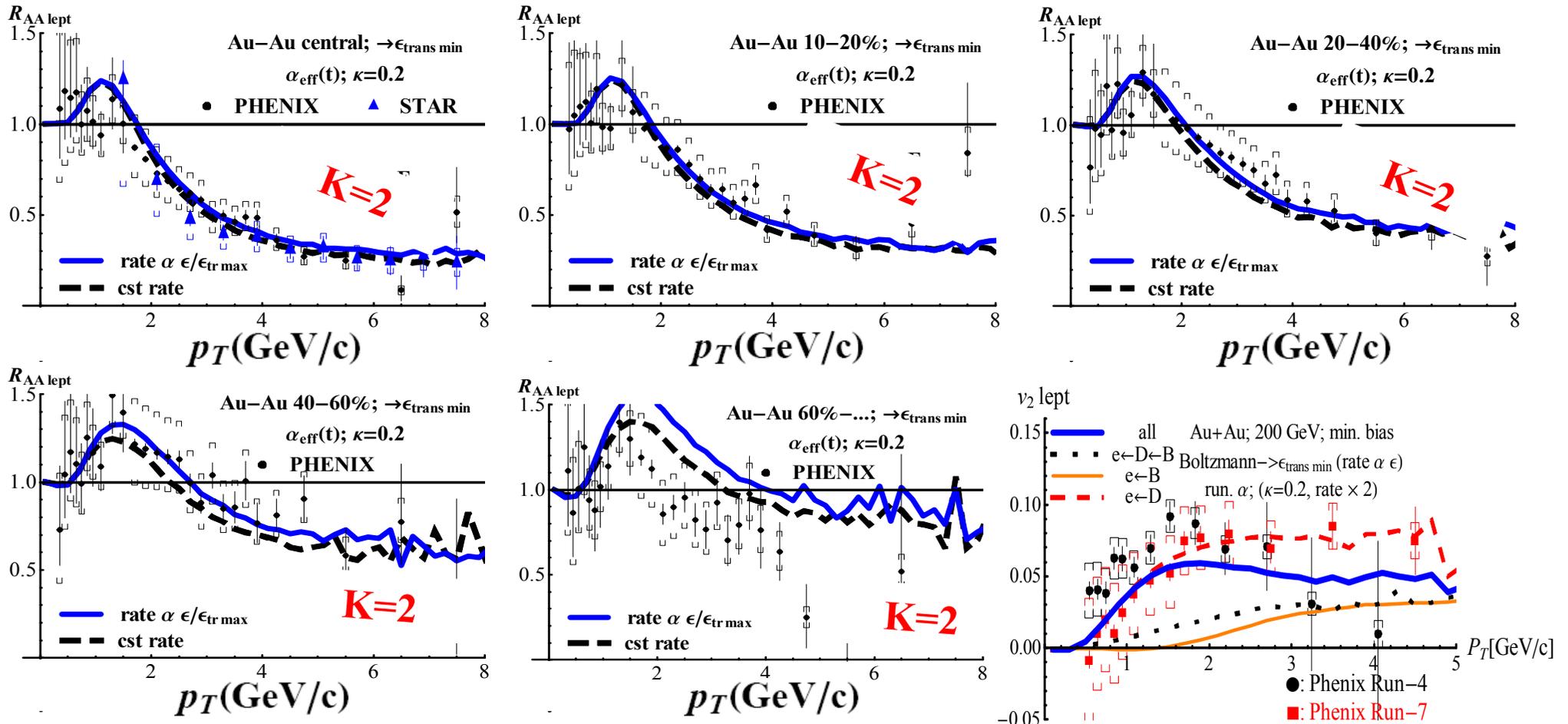


**E: optimal  $\mu$ , running  $\alpha_{eff}$**   
**C: optimal  $\mu$ ,  $\alpha_s(2\pi T)$**

**... of expected magnitude to reproduce the data (we “explain” the transport coeff. in a rather parameter free approach).**

# Observables (Au-Au) vs (rescaled) Model

Best observable so far:  $R_{AA}$  for single non-photonic electrons

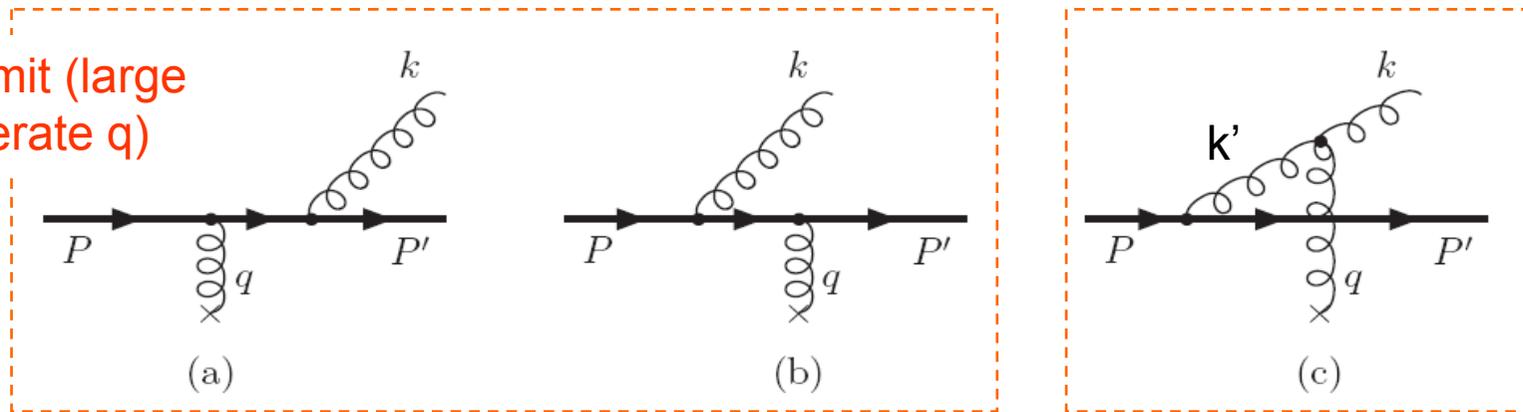


One reproduces  $R_{AA}$  on all  $p_T$  range with cranking K-factor  $\approx 2$  which permits to accommodate the “unknowns”

# Basic (massive) Gunion-Bertsch

Radiation  $\propto$  deflection of current (semi-classical picture)

Eikonal limit (large E, moderate q)



$$\omega \frac{d^3 \sigma_{\text{rad}}^{x \ll 1}}{d\omega d^2 k_{\perp} dq_{\perp}^2} = \frac{N_c \alpha_s}{\pi^2} (1-x) \times \frac{J_{\text{QCD}}^2}{\omega^2} \times \frac{d\sigma_{\text{el}}^{Qq}}{dq_{\perp}^2}$$

Dominates as small x as one "just" has to scatter off the virtual gluon k'

with

$$\frac{J_{\text{QCD}}^2}{\omega^2} = \left( \frac{\vec{k}_{\perp}}{k_{\perp}^2 + x^2 M^2 + (1-x) \underbrace{m_g^2}_{\text{Gluon thermal mass } \sim 2T}} - \frac{\vec{k}_{\perp} - \vec{q}_{\perp}}{(\vec{k}_{\perp} - \vec{q}_{\perp})^2 + x^2 \underbrace{M^2}_{\text{Quark mass}} + (1-x) m_g^2} \right)^2$$

(phenomenological; not in BDMPS)

Both cures the collinear divergences and influence the radiation spectra

# Radiation spectra

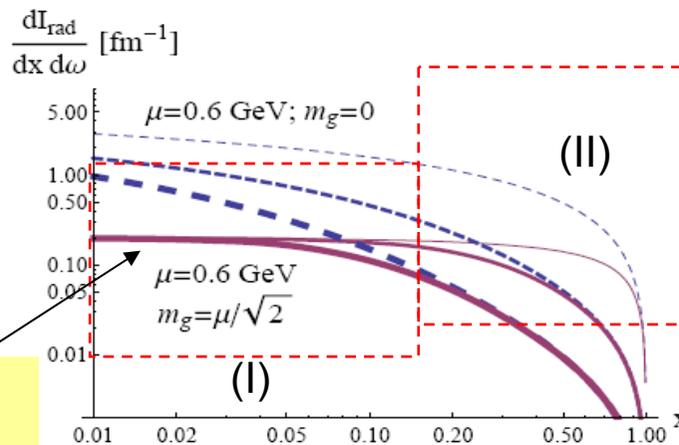
$$\omega \frac{d^2 \sigma_{\text{rad}}^{x \ll 1} \text{''QCD''}}{d\omega dq_{\perp}^2} \approx \frac{2N_c \alpha_s}{\pi} \ln \left( 1 + \frac{q_{\perp}^2}{3\tilde{m}_g^2} \right) \times \frac{d\sigma_{\text{el}}^{Qq}}{dq_{\perp}^2}$$

... to convolute with your favorite elastic cross section

$$\tilde{m}_g^2 = (1-x)m_g^2 + x^2 M^2$$

For coulomb scattering:

- Light quark
- c-quark
- b-quark



Little mass dependence  
(especially from  $q \rightarrow c$ )

Strong dead cone  
effect for  $x > m_g / M_Q$   
(mass hierarchy)

If typical  $q_{\perp} \approx T$  :

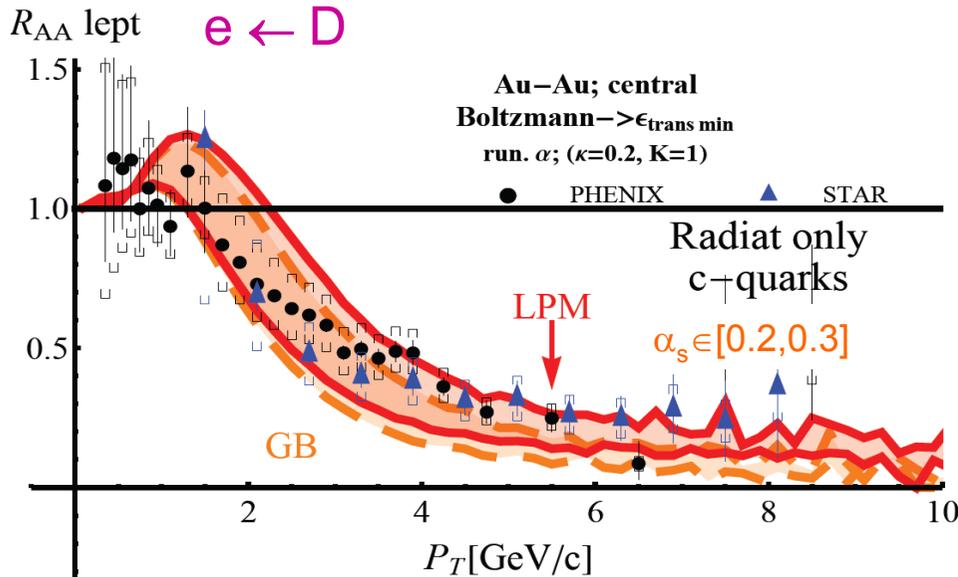
$$\frac{d^2 I_{\text{GB}}^{x \ll 1}}{dz d\omega} \sim \frac{2N_c \alpha_s}{3\pi} \times \frac{1}{m_g^2 + x^2 M^2} \times \underbrace{\frac{\langle q_{\perp}^2 \rangle}{\lambda}}_{\hat{q}}$$

$$\frac{dE_{\text{GB}}(Q)}{dz} \approx \frac{4N_c \alpha_s}{\pi} \times \frac{0.8\mu}{M + \mu} \times \frac{E}{\lambda_Q}$$

Strong mass effect in the average Eloss  
(mostly dominated by region II), similar to  
AdS/CFT

Interesting *per se*, but not much connected to the quenching or  $R_{\text{AA}}$ .

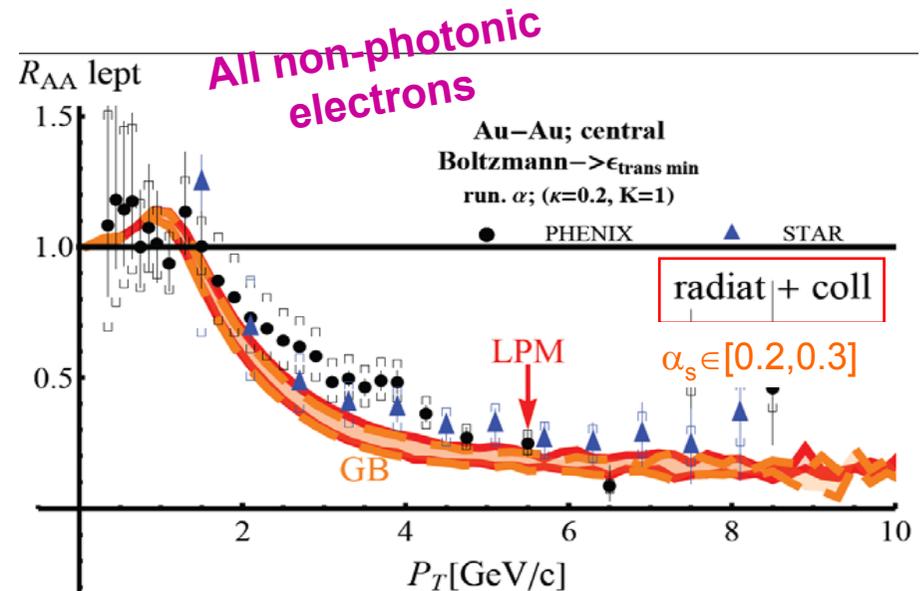
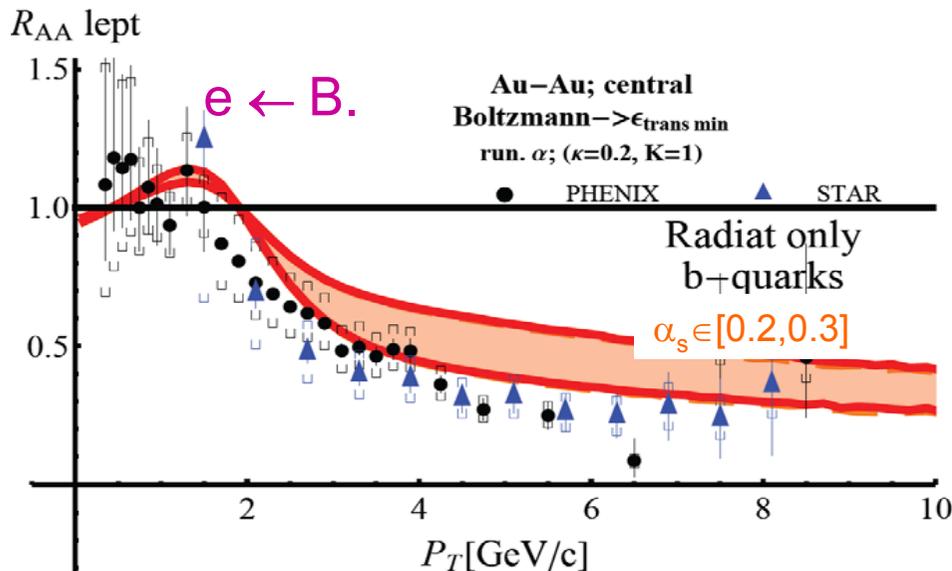
# Results with (Coherent) Radiation Included



1. Coherence: Some moderate increase of  $R_{AA}$  for D at large  $p_T$ .
2. No effect seen for B

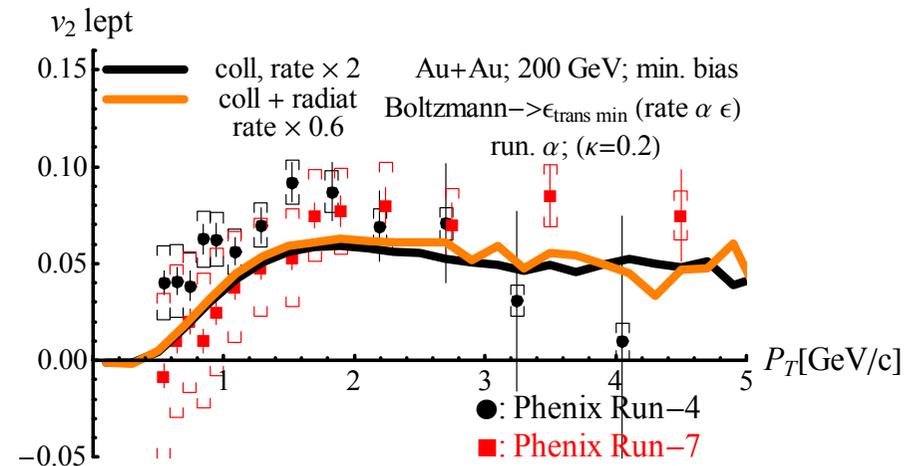
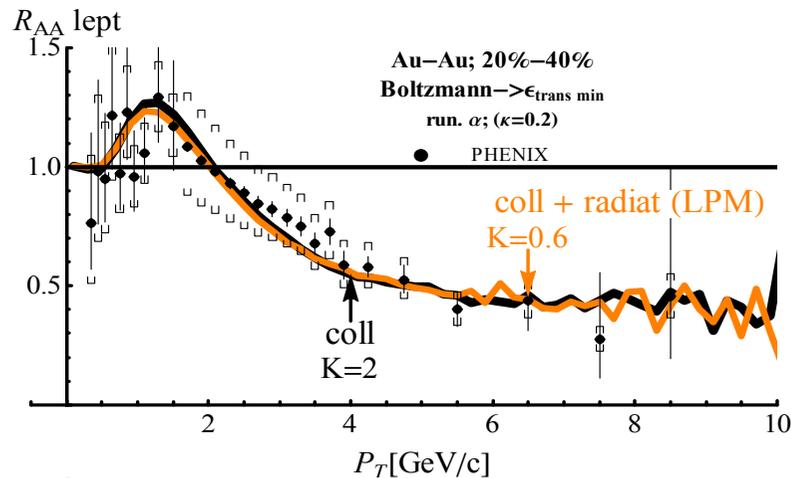
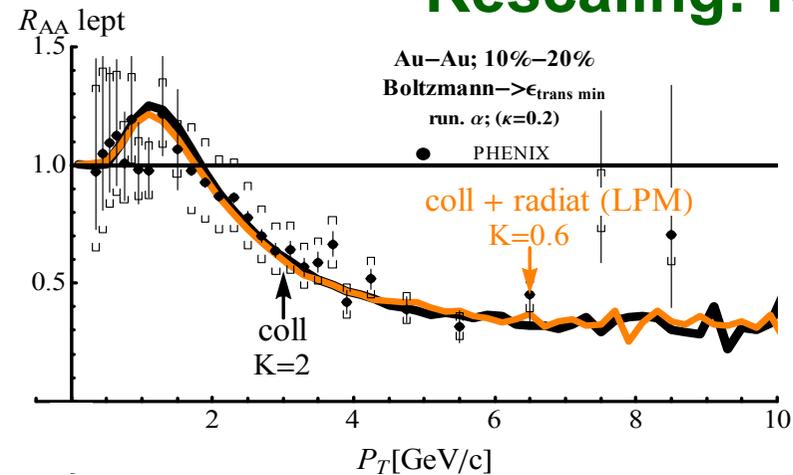
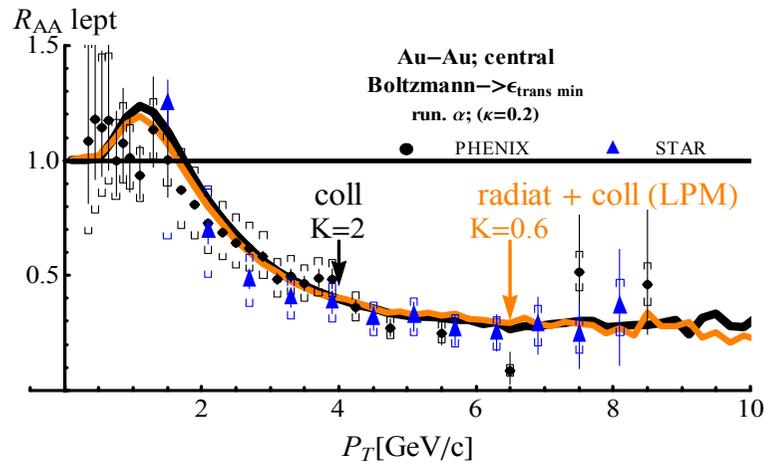
Conclusions can vary a bit depending on the value of the transport coefficient

Indication that  $R_{AA}$  at RHIC is mostly the physics of rather numerous but small E losses, not very sensitive to coherence.



# Collisional vs {Radiative + Coll}

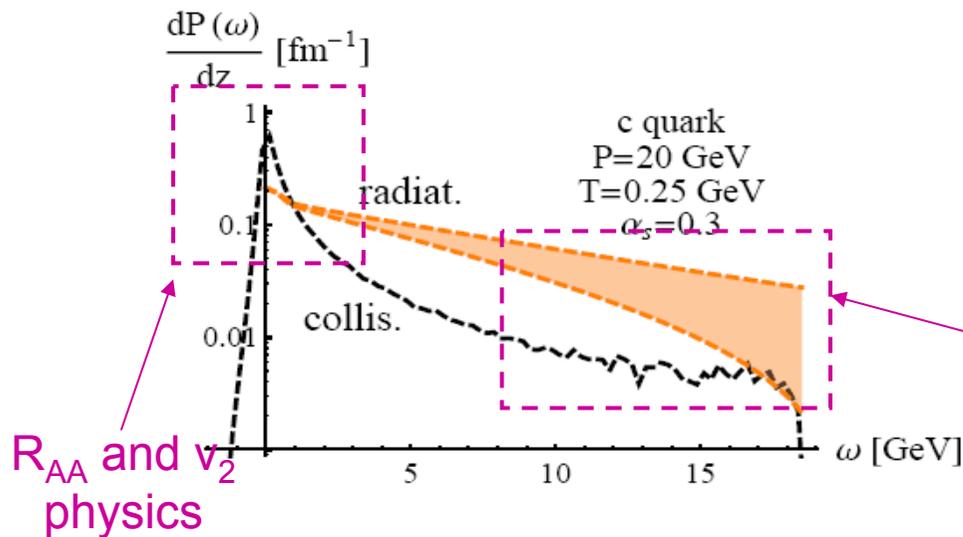
**Rescaling:  $K=0.6$**



The present data cannot decipher between the 2 local microscopic E-loss scenarios

# Interpretation

The heavy-quark physics at play for RHIC measured up to now ( $R_{AA}$  and  $v_2$ ) is the one of small (relative) E-loss (and thus of the Fokker-Planck equation)... even at the largest  $p_T$



Explains why purely collisional models “work” so well

What we need

- D and B separately (in any case)
- tagged HQ jets and  $I_{AA}$  (and other correlations)

Bad control on the theory

In our view, it is nevertheless more plausible to describe the physics in terms of a rather strong collisional energy loss supplied with an even stronger radiative energy loss (at least for  $\gamma \gg 1$ ).

# QGP properties: low momentum

As we reproduce experimental data with rescaled model:

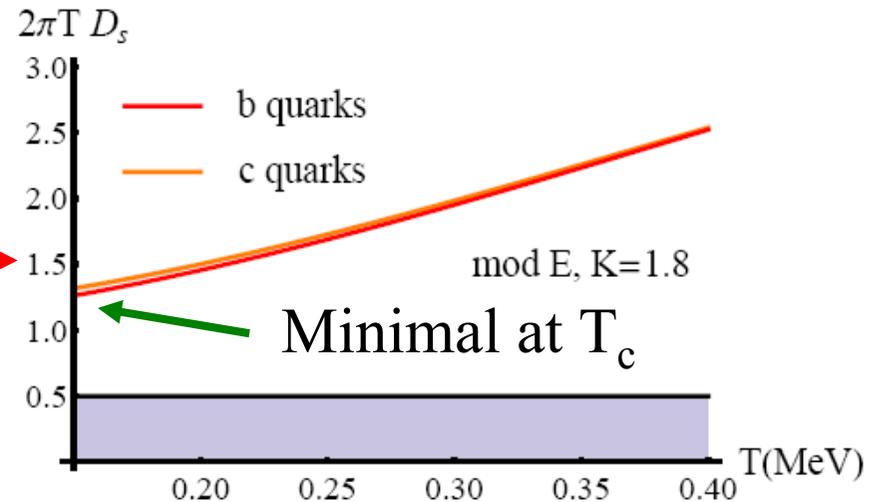
Moore-Teaney:

$$\frac{D}{\eta/(e+p)} \approx 6 \Rightarrow \eta/s \approx DT/6$$

“robust”pQCD

$$\approx \frac{2\pi T D}{3 \times 4\pi}$$

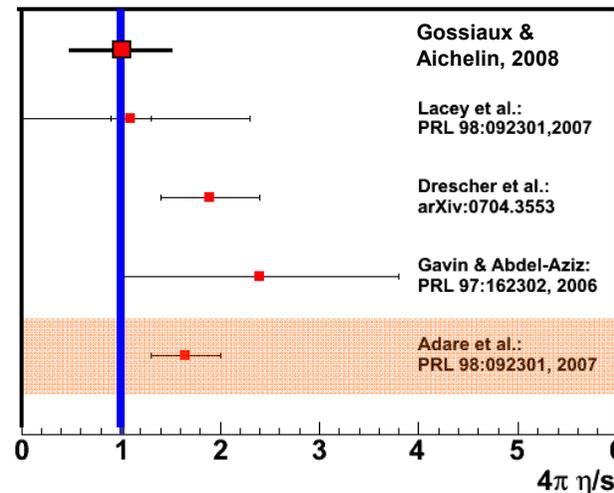
$$\Rightarrow \eta/s \approx \frac{0.5}{4\pi} \text{ at } T_c$$



Strong coupling; AdS/CFT:

$$\eta/s \approx DT/2 \approx \frac{2\pi T D}{4\pi}$$

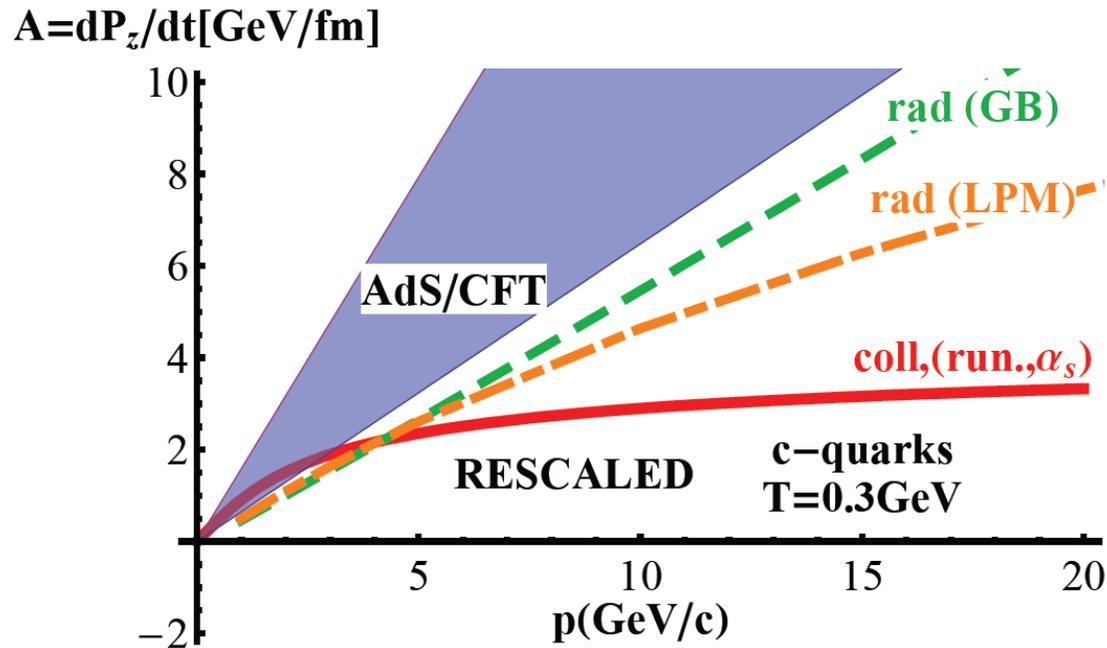
$$\Rightarrow \eta/s \approx \frac{1.5}{4\pi} \text{ at } T_c$$



But diffusion constant of heavy quark is already an interesting quantity in itself and could be evaluated on the lattice !!!

# QGP properties: stopping power

Gathering all *rescaled* models (*coll. and radiative*):

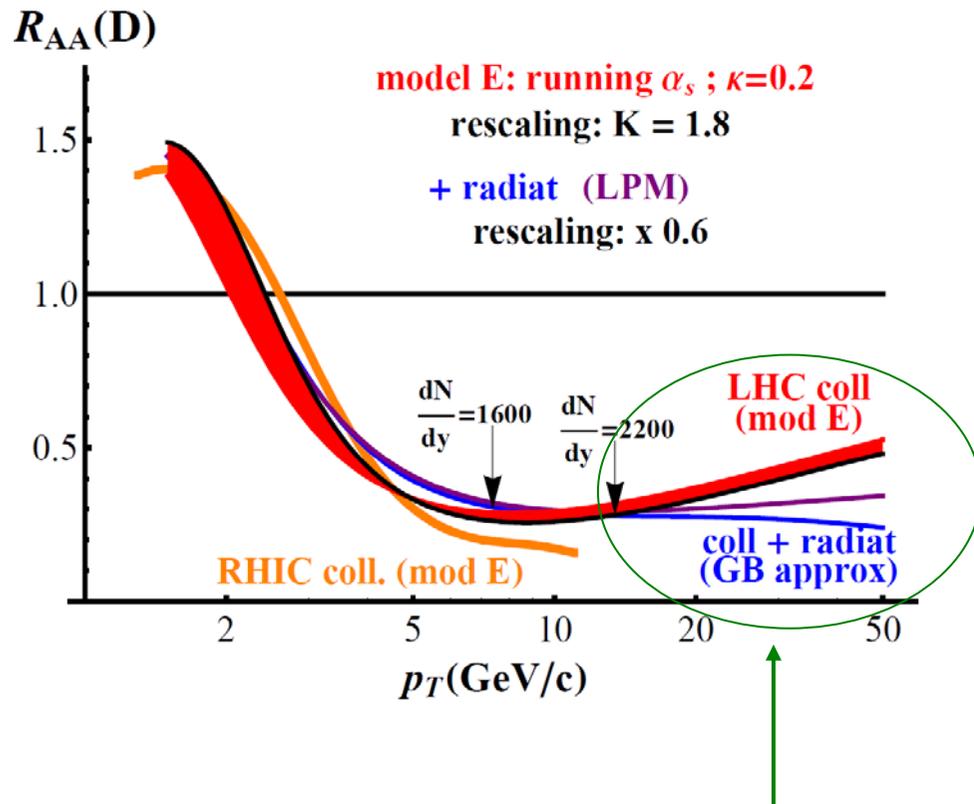


Exp. cannot resolve  
between those  
various trends

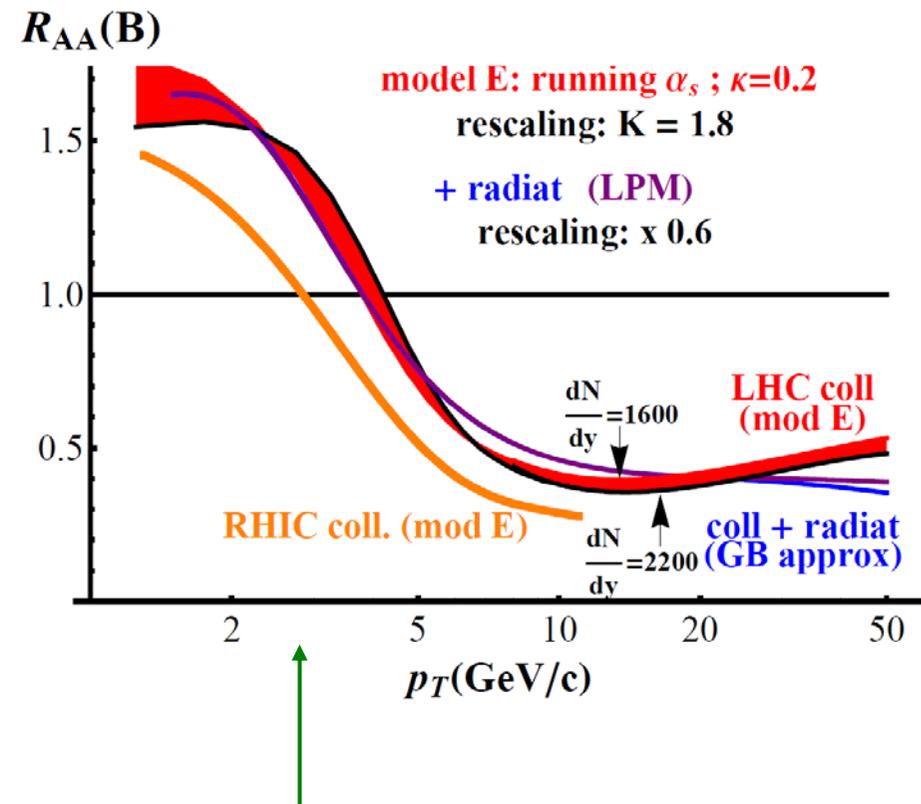
quite consistent as the  
drag coefficient reflects  
the average momentum  
loss (per unit time) =>  
large weight on  $x \sim 1$

Noticeably enough, AdS/CFT lower bound is quite close to the  
incoherent radiation limit

# Perspectives :D & B meson: LHC (radiat + collisional)

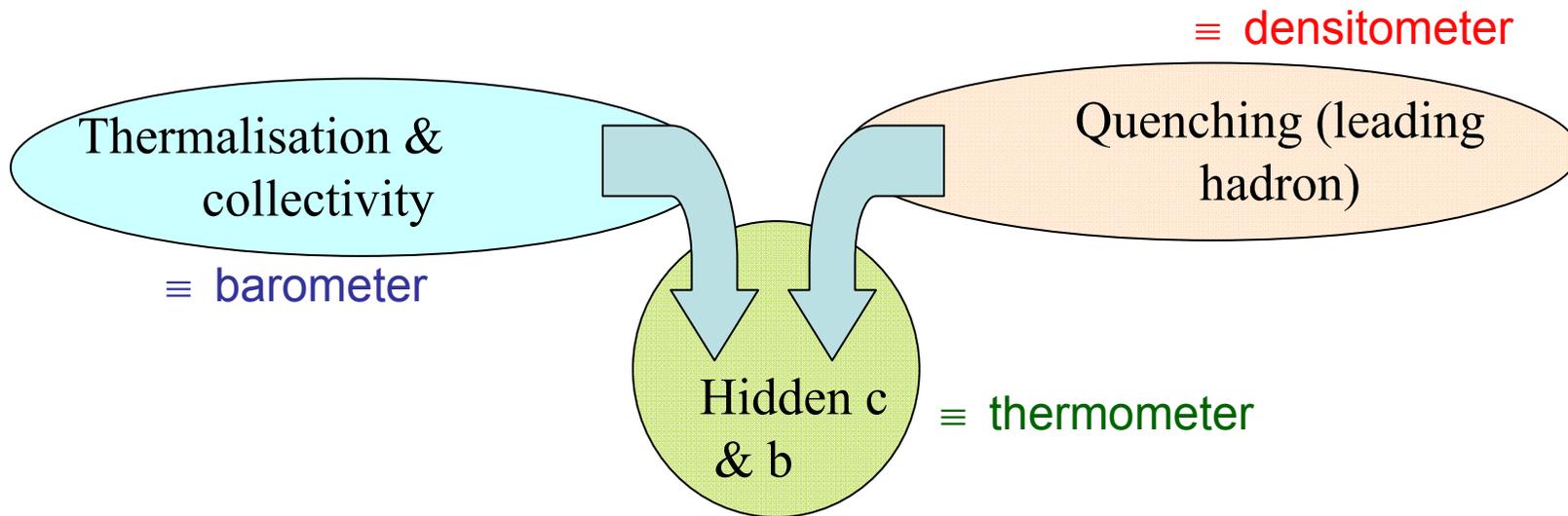


D spectra in Pb-Pb (5.5 TeV):  
 Some window to decipher  
 between the various Energy-  
 loss models, for  $p_T > 20 \text{ GeV}/c$



B spectra in Pb-Pb (5.5 TeV):  
 Pretty independent of E-loss  
 model (properly calibrated  
 w.r.t. RHIC data)

➤ physics of HQ at low momentum w.r.t. fluid cell seems “under control”

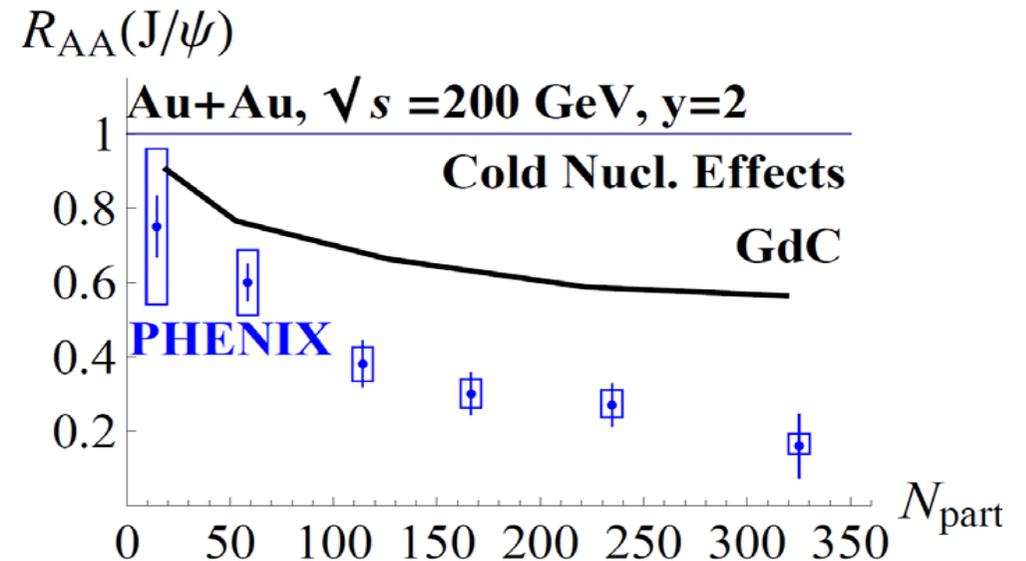
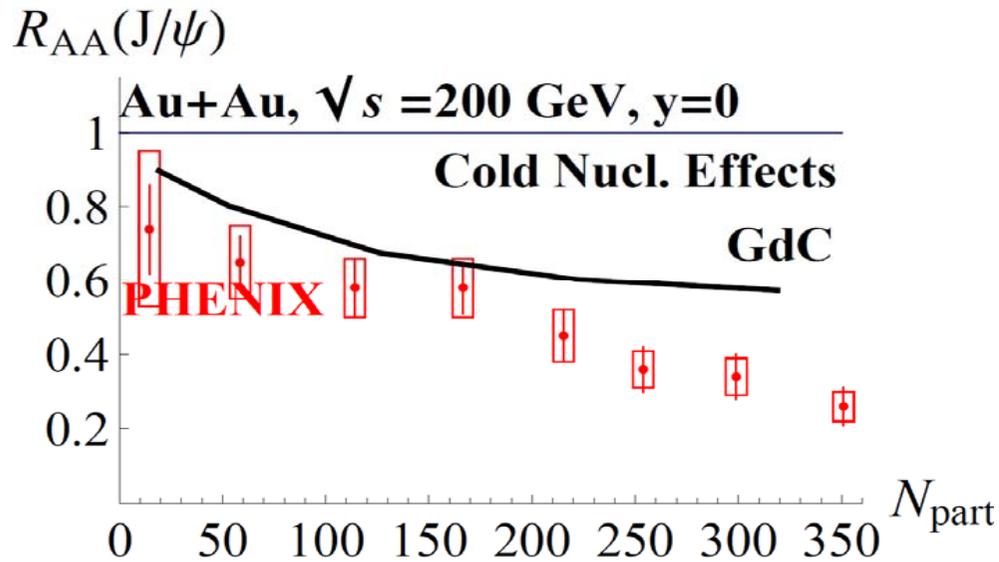


## II. Quarkonia in QGP

*Work in progress*

# Integrated $J/\psi$ numbers @ RHIC

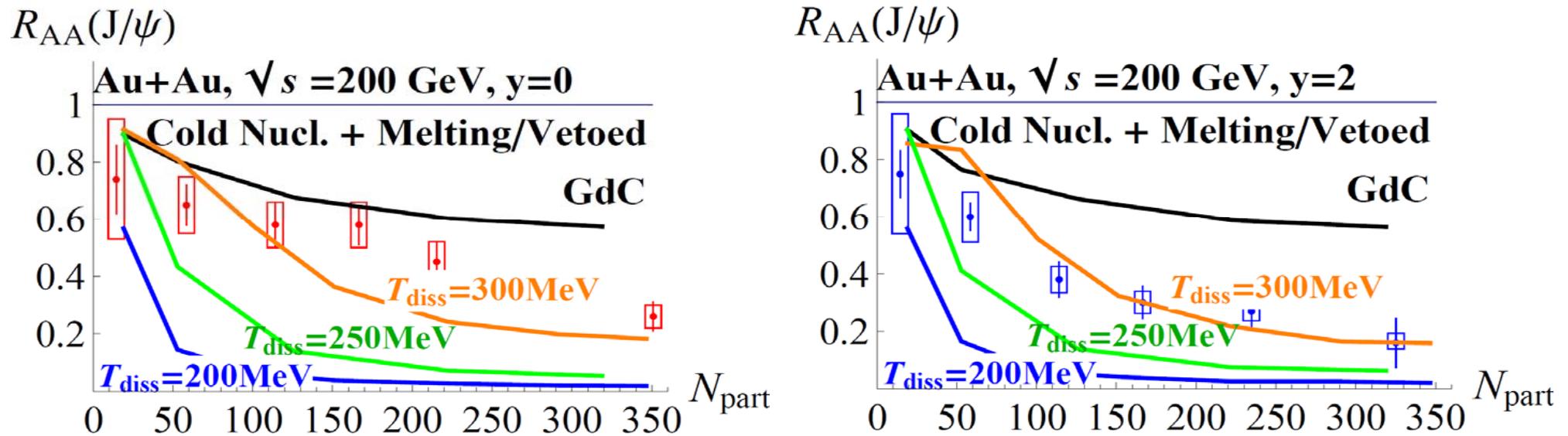
First, we need a baseline taking into account the cold nuclear matter effects (Shadowing, Cronin,...); we take the picture of R. Granier de Cassagnac (2007)



Progress to be made here

# Integrated J/Ψ numbers @ RHIC

Next, the (*instantaneous*) vetoing of quarkonia formation due to melting:



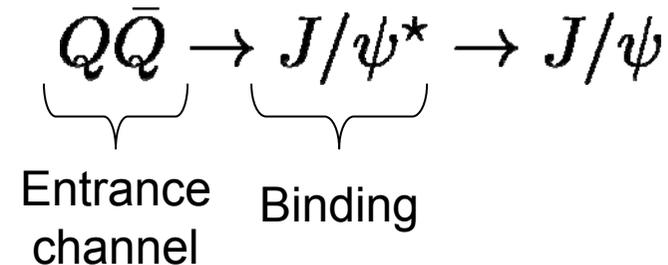
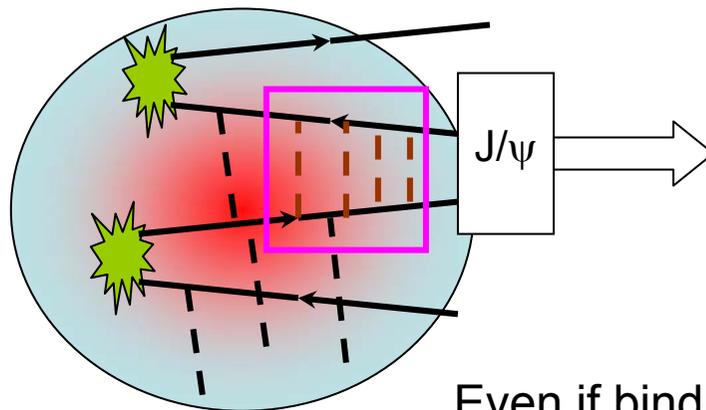
Good agreement obtained with a rather large value of  $T_{diss} \approx 2 T_c$ .

Some claims of “sequential suppression” with a very bound J/ψ were indeed made by several physicists

“.....We do not need recombination !”.....  
 except that Q and Qbar may be close in phase space

# Turning on (re)combination + hard dissoc

(Re)combination (could become dominant at LHC):



Even if binding process is fast and medium-independent (quarkonia are small bound states), the distributions of  $Q$  and  $\bar{Q}$  in the entrance channel depend on the past history

(transport theory)

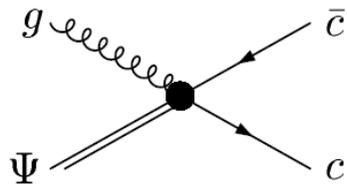
## Discussion

- The majority of quarkonium suppression models ignore open heavy flavor suppression due to induced gluon radiation and collisional energy loss (charm quenching)
  - Is this omission justified? **No**
  - Does charm suppression affect recombination? **Yes**
  - Do medium effects in AA affect the formation time of quarkonia? **If formation time taken as the Heisenberg time, Yes**

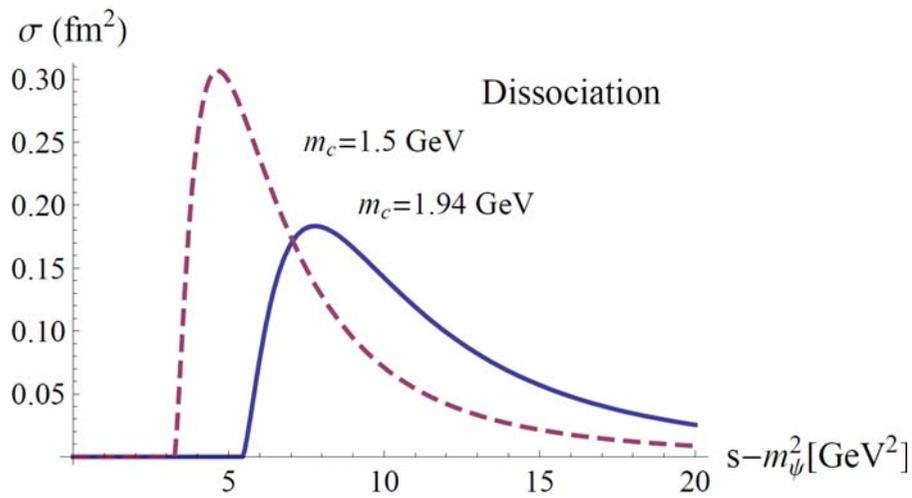
# Basic Ingredients

## Dissociation

hard dissociation taken according to Bhanot and Peskin + recoil correction (Arleo et al 2001)



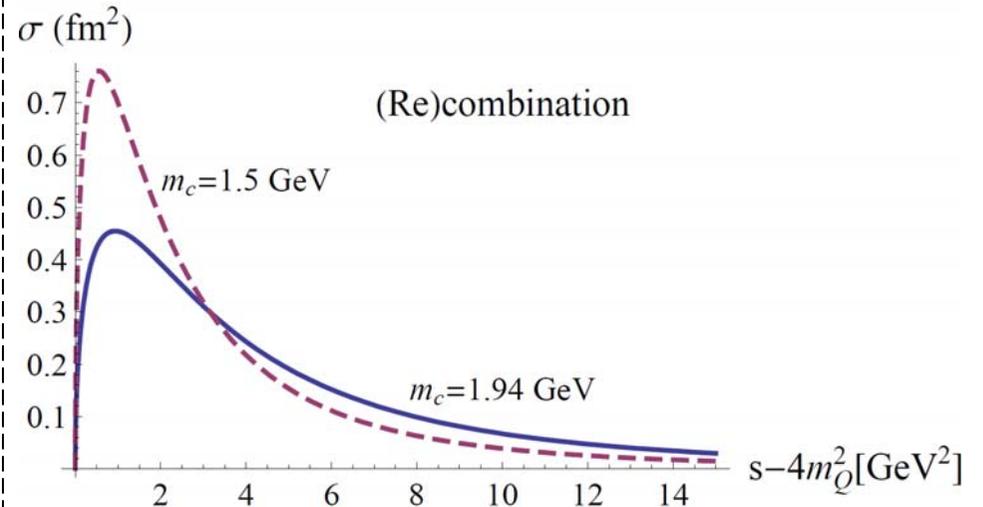
$$\sigma_{(Q\bar{Q})g}(\omega) = \frac{2^{11}}{3^4} \alpha_s \pi a_0^2 \frac{(\omega/\varepsilon(0) - 1)^{3/2}}{(\omega/\varepsilon(0))^5} \Theta(\omega - \varepsilon(0))$$



Max  $\approx 2 \text{ fm}^2$  at  $\omega \approx 500 \text{ MeV}$

## Recombination

Cross section obtained from  $\sigma_{\text{diss}}$  via detailed balance



# Recombination: hierarchy of approaches...

Complexity

Statistical weights (at transition). no detailed dynamics. ☹ assumes all time scales are small vs. transition time. ☺ simple to deal with. PBM, Stachel & Andronic; Gorenstein, Kostyuk;...

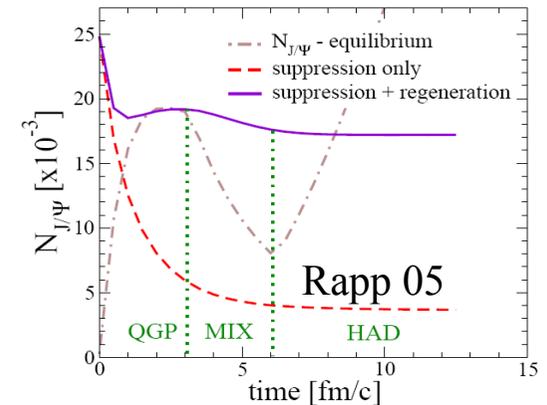
Rate equations: 
$$\frac{dN_{\Psi}}{dt} = -\Gamma_{\Psi} (N_{\Psi} - N_{\Psi}^{eq})$$

- ☺ Might contain the essential physics at a global level.
- ☹ Model of  $f_c(x,p)$  needed. ☹ no possibility of studying diff. spectra. Grandchamp, rapp and Brown; (early) Thews

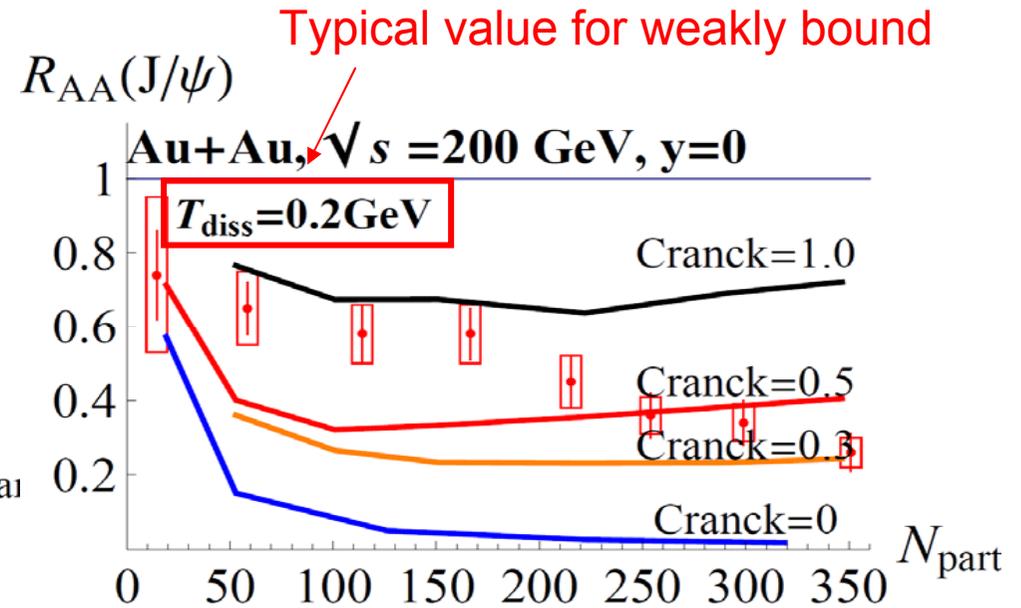
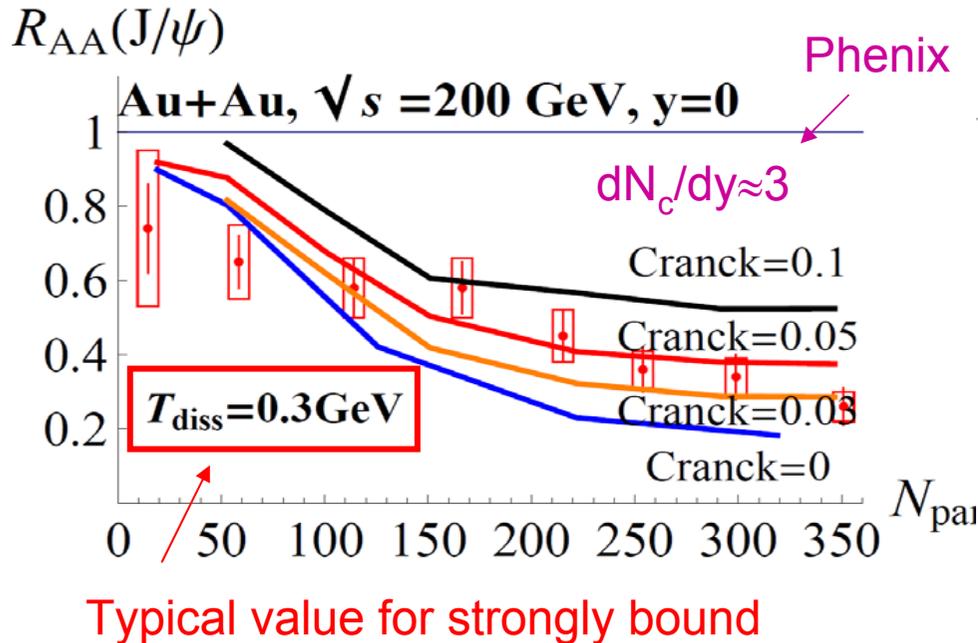
Transport theory assuming spatial homogeneous  $f_i(p)$ . ☺ diff spectra. ☹ misses surface effects, x-p correl, Q are not uniformly distributed. Thews and Mangano

Transport theory. ☺ solves the caviats of other approaches. ☹ may obscure the physics. Zhang (AMPT); Bratkovskaya & Cassing (HSD); Gossiaux;...

... does not mean a hierarchy of answers (hopefully)!



# Turning on (re)combination + hard dissoc

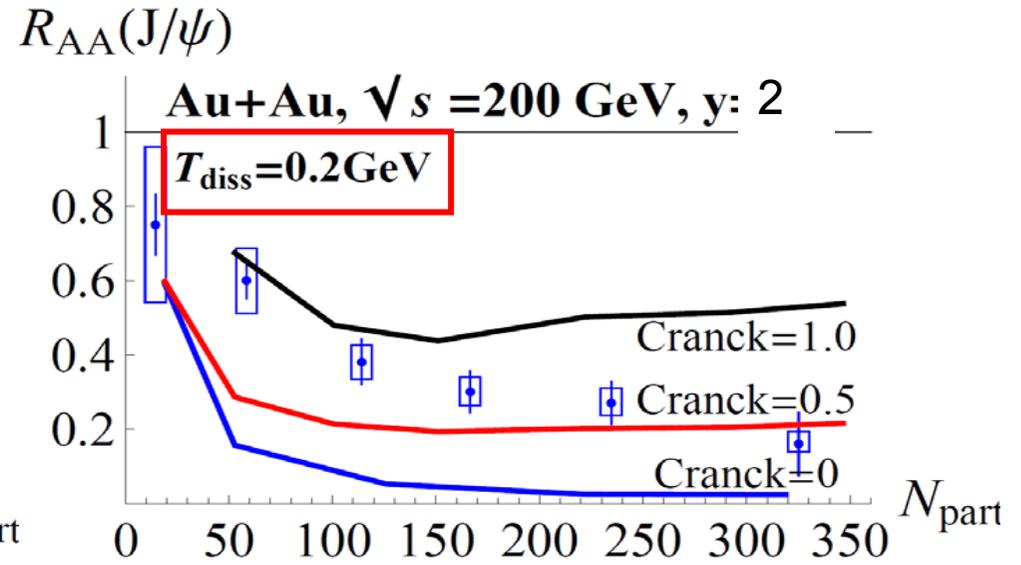
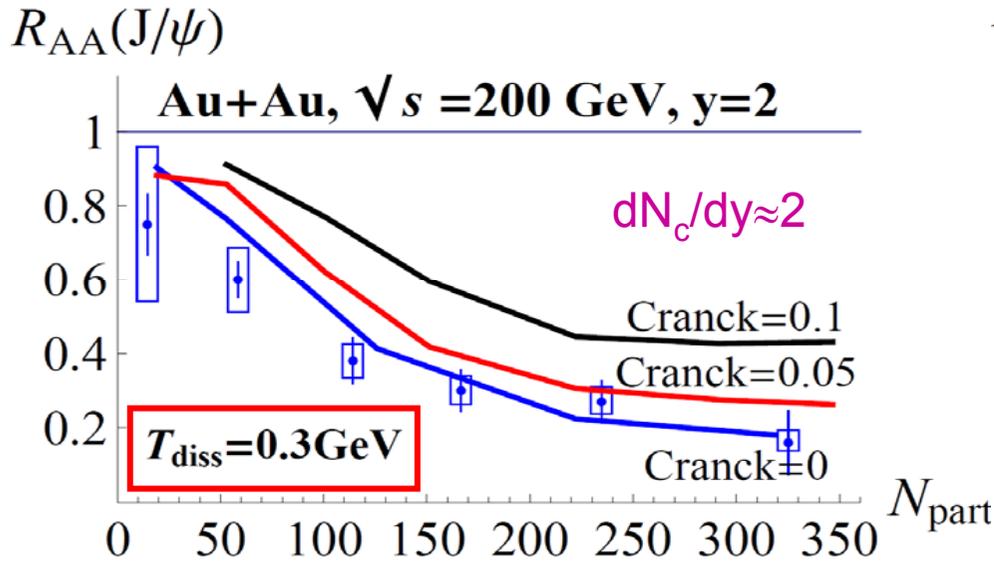


**Problem:** One has to reduce the fusion probability by a factor  $\sim 10$  to reproduce the data (if recomb. cross section taken at face value, one arrives at  $R_{AA}$  (most central  $> 2$  !).

**Problem never comes alone:** Strongly bound quarkonia are the ones for which the Bhanot-Peskin approach should be legitimate.  $\Phi$  states exist early  $\Rightarrow$  lot of HQ pairs present in phase space

Absolute numbers are better reproduced (if one believes in mostly canonical – cranck=0.5-1 – recombination), although the  $R_{AA}$  dependence on  $N_{part}$  is not as satisfying

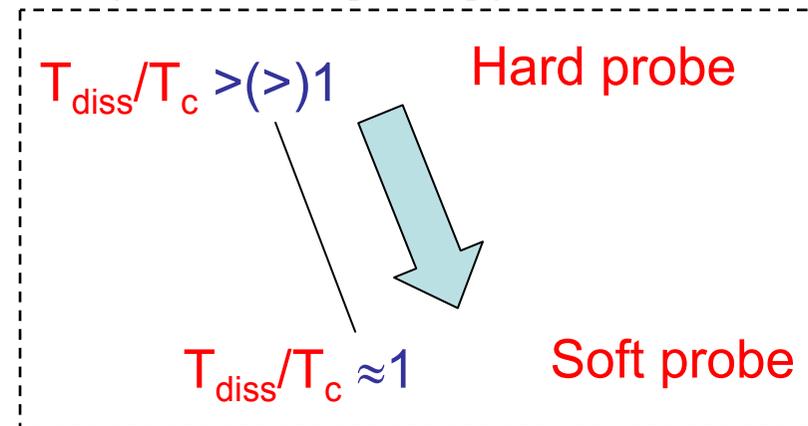
# Turning on (re)combination at $y=2$



No room left for coalescence at  $y=2$ . **What are the physical mechanisms for taming the fusion ?**

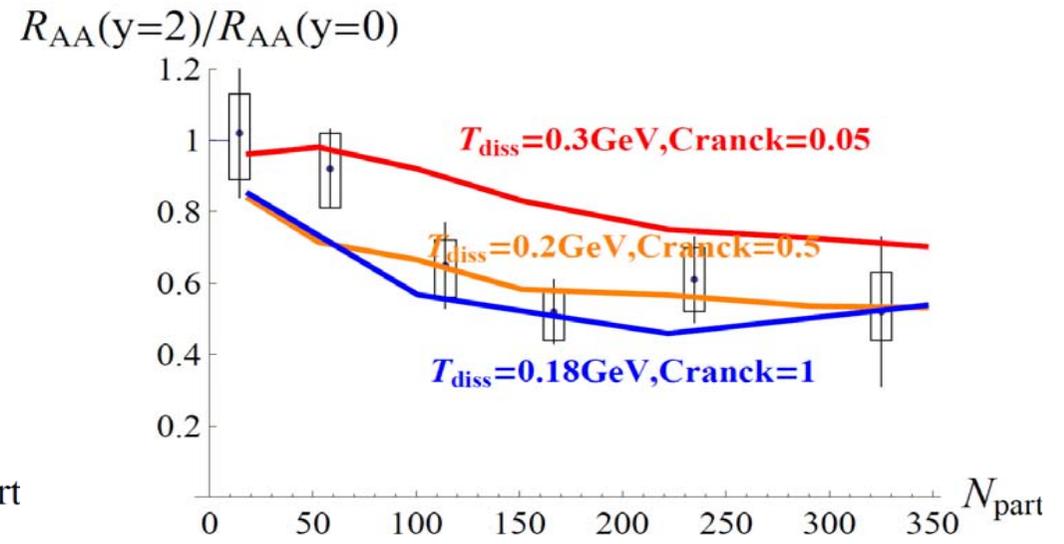
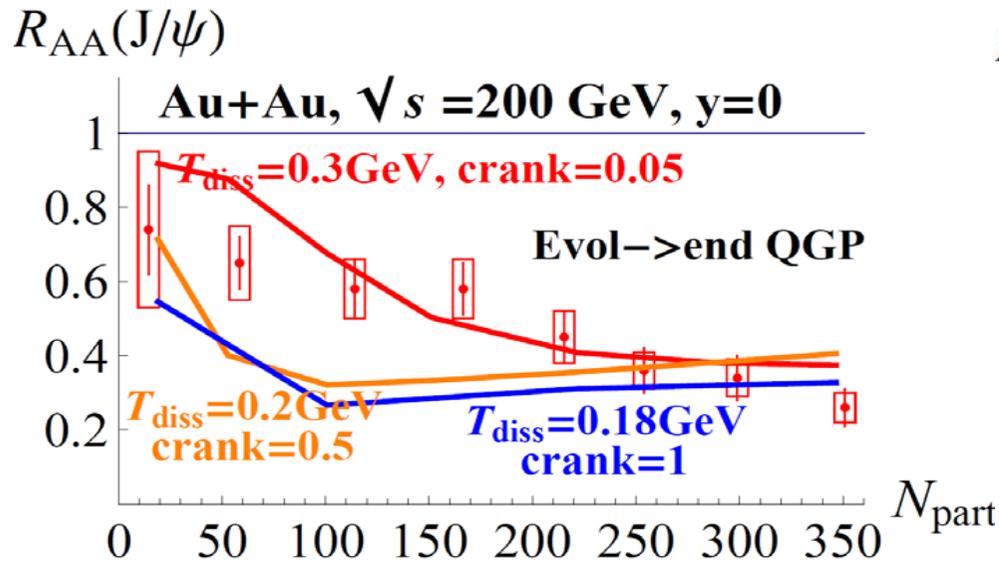
**Moreover:** The pQCD Bhanot and Peskin result is usually considered to be small w.r.t. other effective approaches at small  $s-M^2$

Good agreement with the same  $\sigma_{fus}$  band (Cranck.  $\in [0.5, 1]$ )



# Best parameters from $R_{AA}$

“Optimal” choices in the  $(T_{\text{diss}}, \sigma_{\text{fus}})$  parameter plane

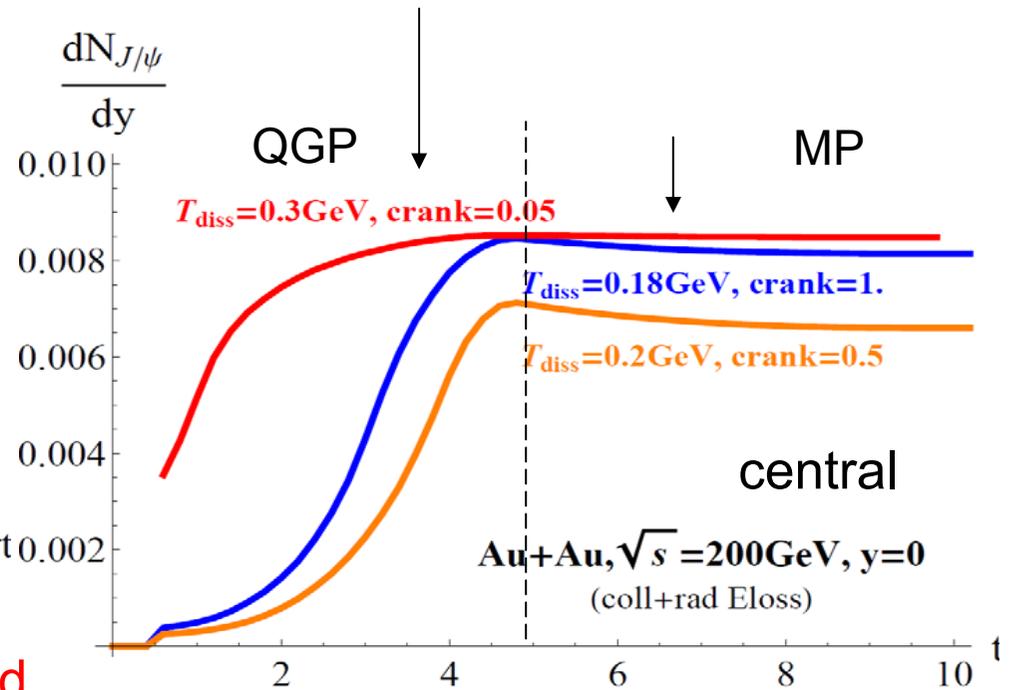
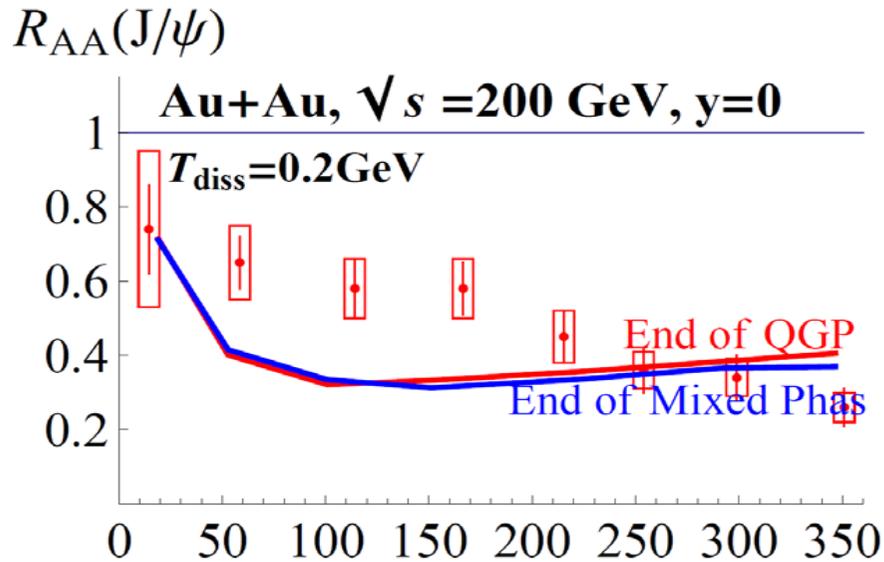


Conclusion:  $T_{\text{diss}} \in [0.2, 0.3]$ ... but difficult to go beyond

# Finer analysis: Thermometer of what ?

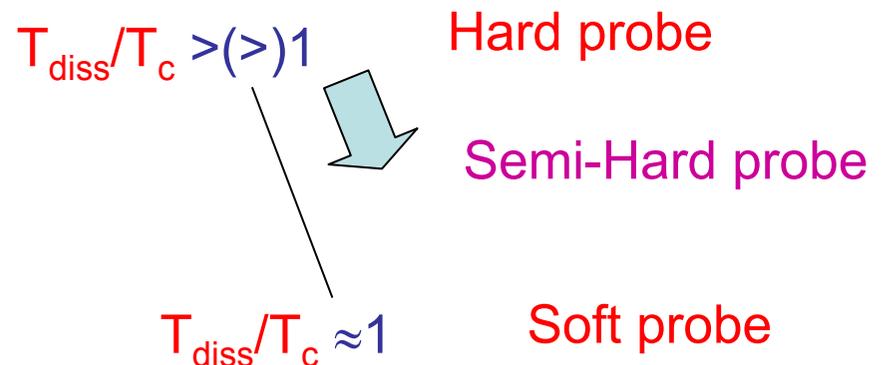
Other parameters...  $E_{\text{loss}}$ , detailed  
Medium evolution...

Dominant production at various time depending  
on  $T_{\text{diss}}$ ... saturates *before* the end of the QGP

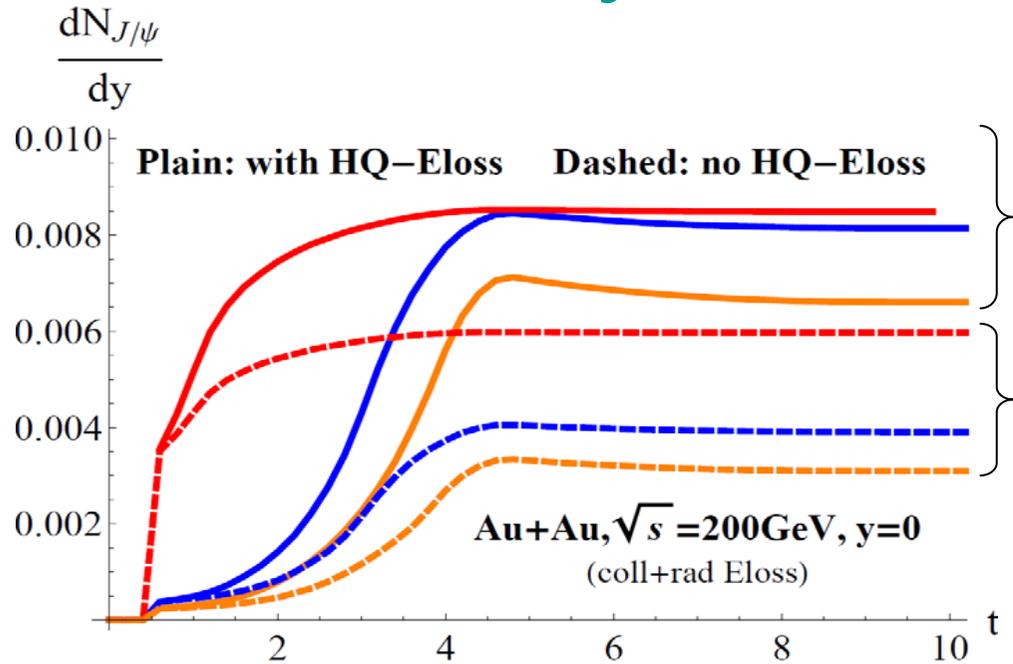


If quarkonia are a thermometer, it should  
be first agreed upon the phase it probes

Dynamical evolution does not confirm  
the idea of statistical recombination in  
the mixed phase



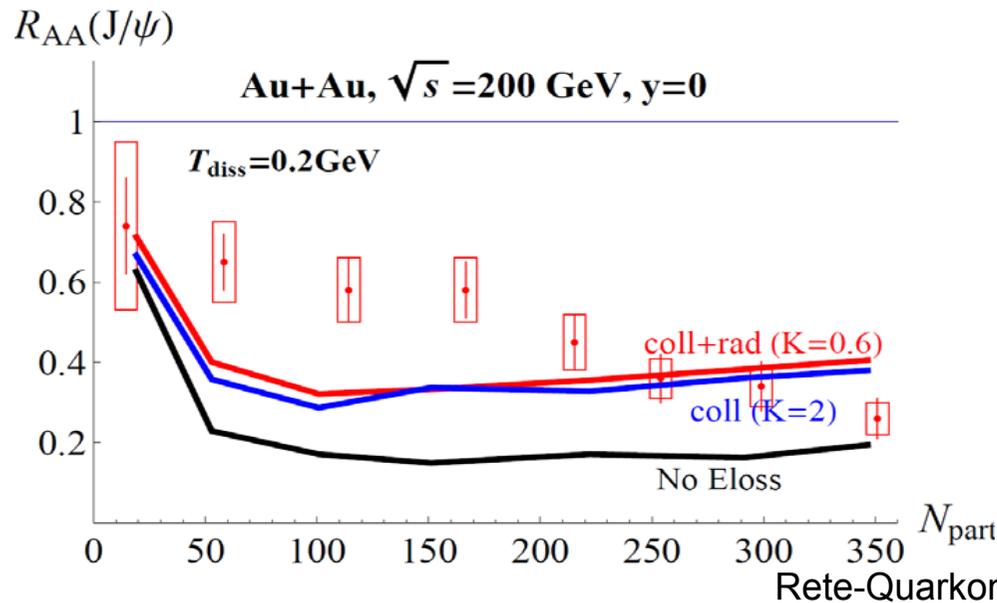
# Finer analysis: role of HQ energy loss



Eloss

Energy loss favors the coalescence of  $J/\psi$  (brings the c quarks together in phase space)

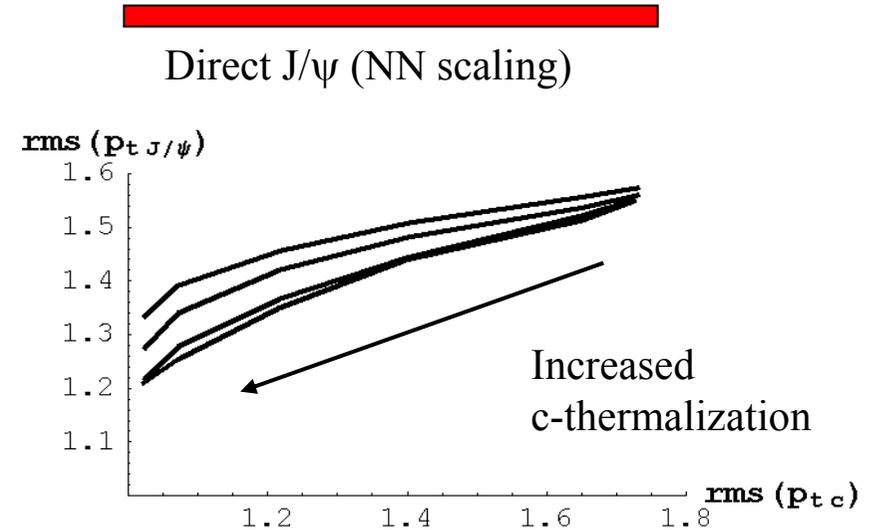
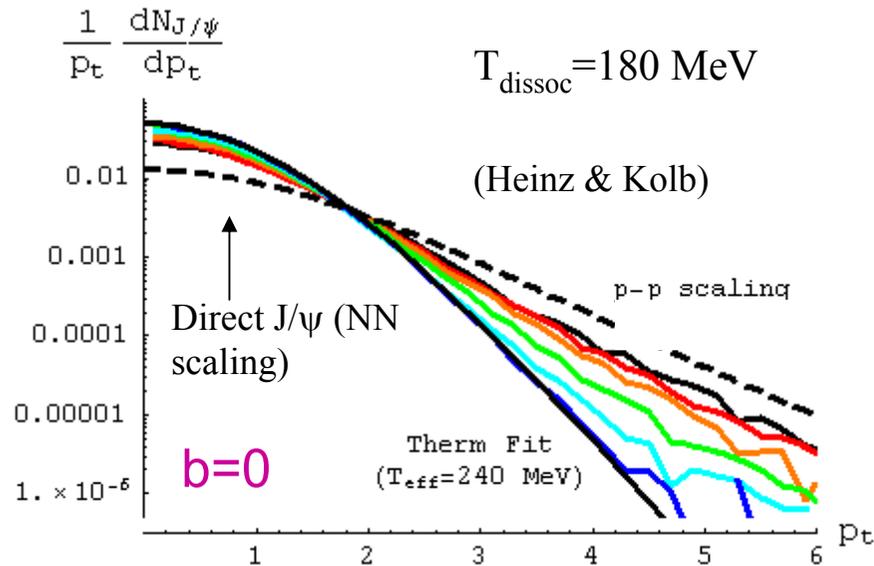
No Eloss



However: Once the Energy loss has been “properly” calibrated on non-photonic single-e  $R_{AA}$ , then the production rates do not depend too much on the detailed phenomena

# The $P_T$ world

Differential production might reveal more physics



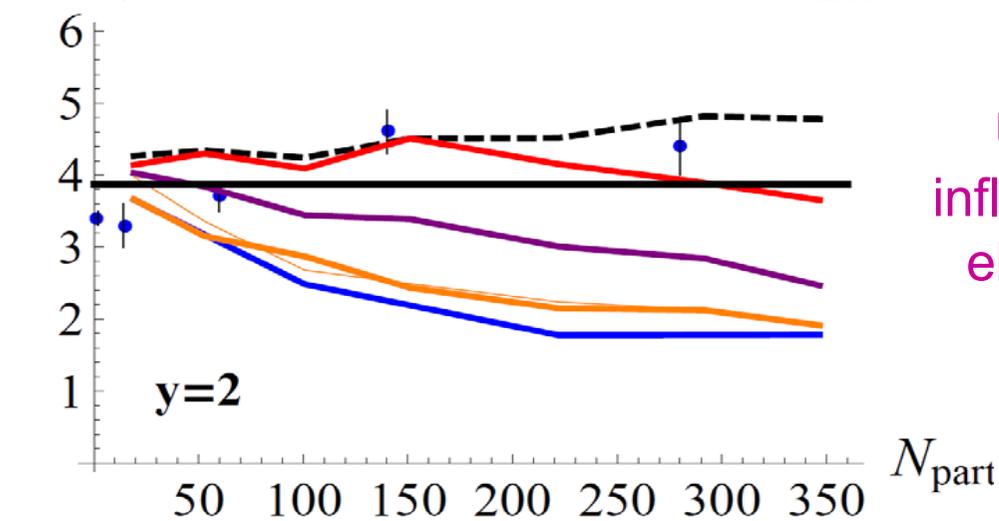
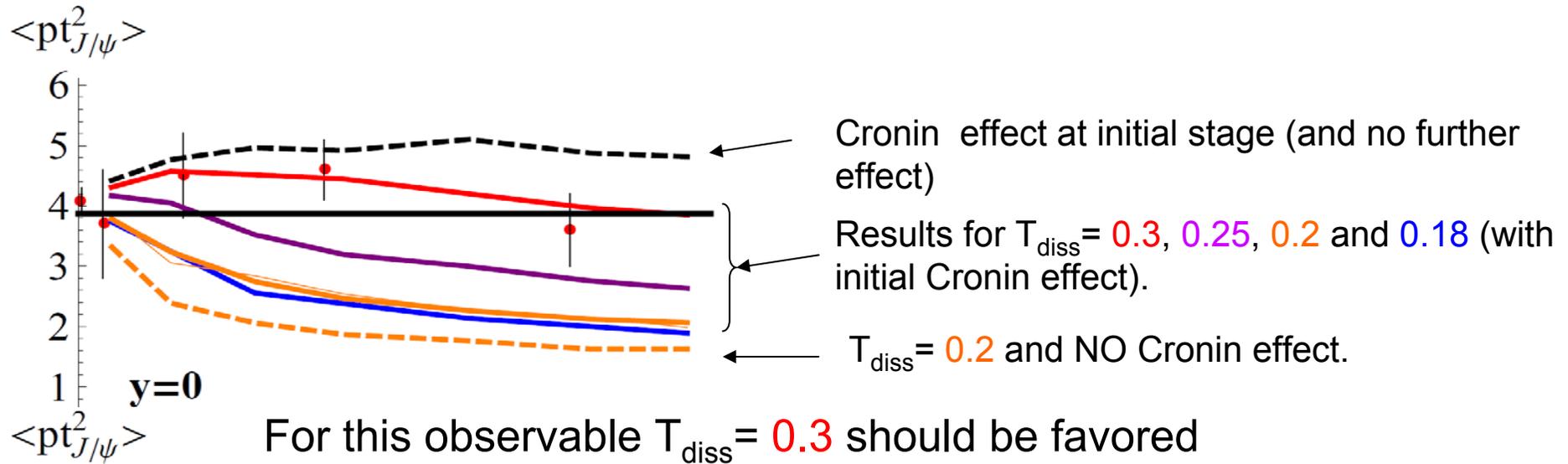
Prediction for  $b=0$  and just recombination (2004)

QGP “cools” the charms, even with the radial flow

Softer  $p_T$  spectrum as for direct production. Possible “ $p_T$  shrinking” in A-A. But first, understand the  $k_t$  broadening in d+Au (none seen around  $y=0$  !?)

# The $P_T$ world

... and now compared with the data:



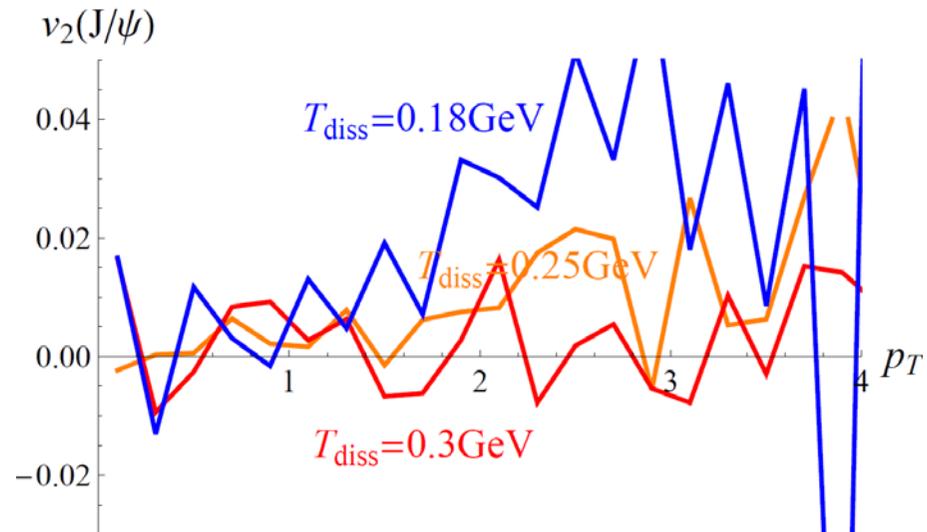
Unknown:  
influence of the  
elastic cross  
section

TABLE I: The mass shift  $\Delta M_{J/\psi}$  and elastic  $J/\psi+N$  cross section predicted by different models.

Ref.	$-\Delta M_{J/\psi}$ (MeV)	$\sigma_{J/\psi N}$ (mb)
[12]	3	0.3
[15]		1.5
[19]	10÷5	
[20]	7÷4	
[21]	4	
[32]	11÷8	
[33]		5
[34]		8
[35]	5	
this	$\gtrsim 21$	$\gtrsim 17$

Voloshin (2005)

# The keystone (?): $v_2$

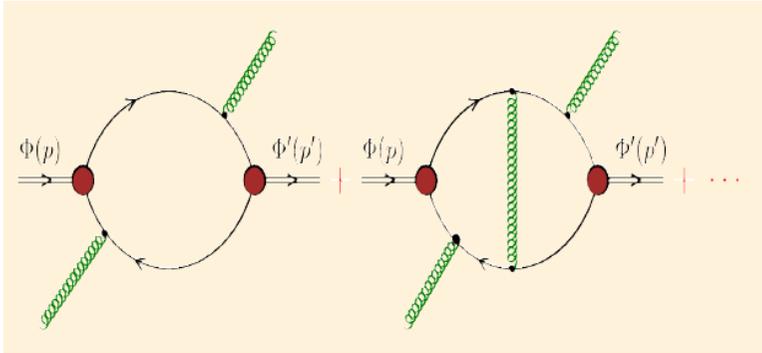


In fact, due to possible elastic cross section of  $J/\psi$ ,  $v_2$  is only conclusive *per se* if one observes NO  $v_2$

# Investigating the role of elastic processes

Dominant process:

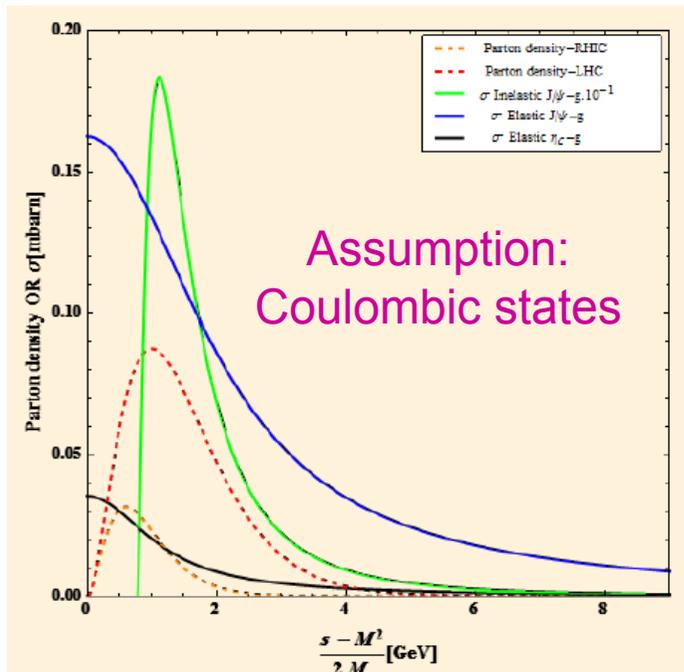
Work of H. Berrehrah (see QGP France 2009 & Hot quarks 2010)



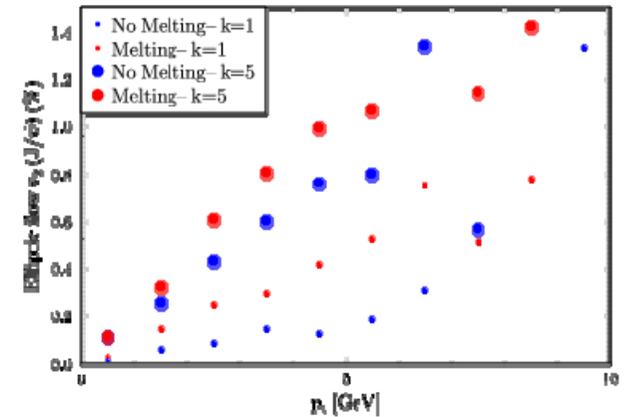
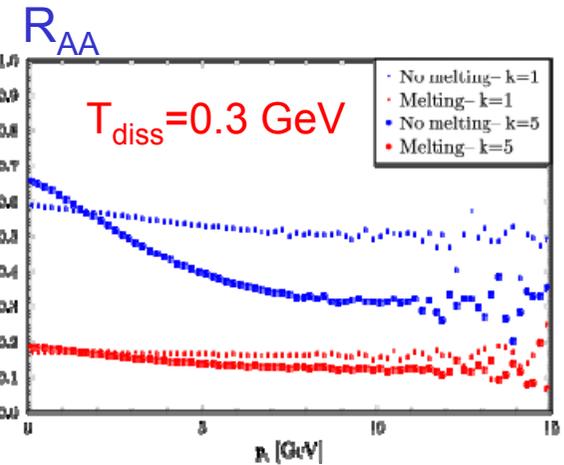
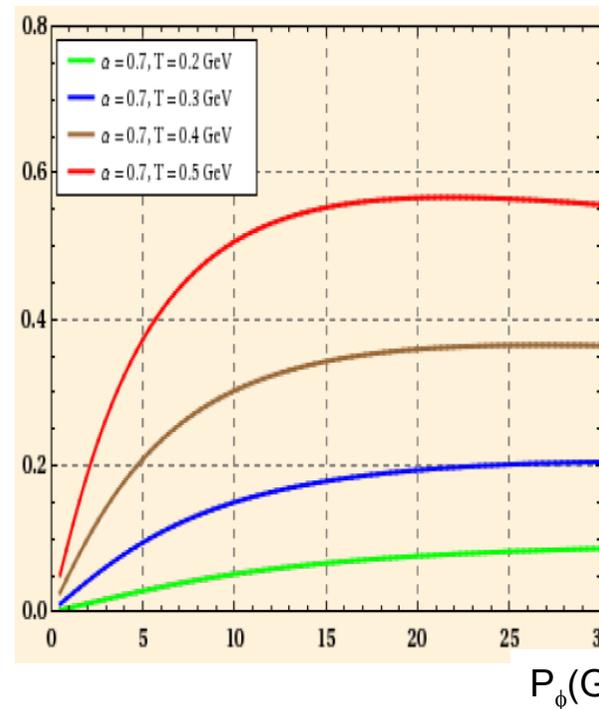
Penalized by higher power of the coupling constant w.r.t. inelastic scattering... but no threshold

Inclusion in MC@sHQ

Total cross section



Drag force



Elliptic flow

# Preliminary conclusion

1. Are the data compatible with the picture of a strongly bound  $J/\psi$  (sequential suppression) ?

3. Can we try to *extract* the dissociation temperature from the data ?

A rather large effective dissociation temperature ( $T_{\text{diss}} \approx 0.25-0.3$  GeV) seems to be favored by the data, **provided** one has a good quantitative argument to explain why the recombination of HQ should be reduced by a factor 10 w.r.t. the naive Bhanot - Peskin cross section (gluon mass ?)

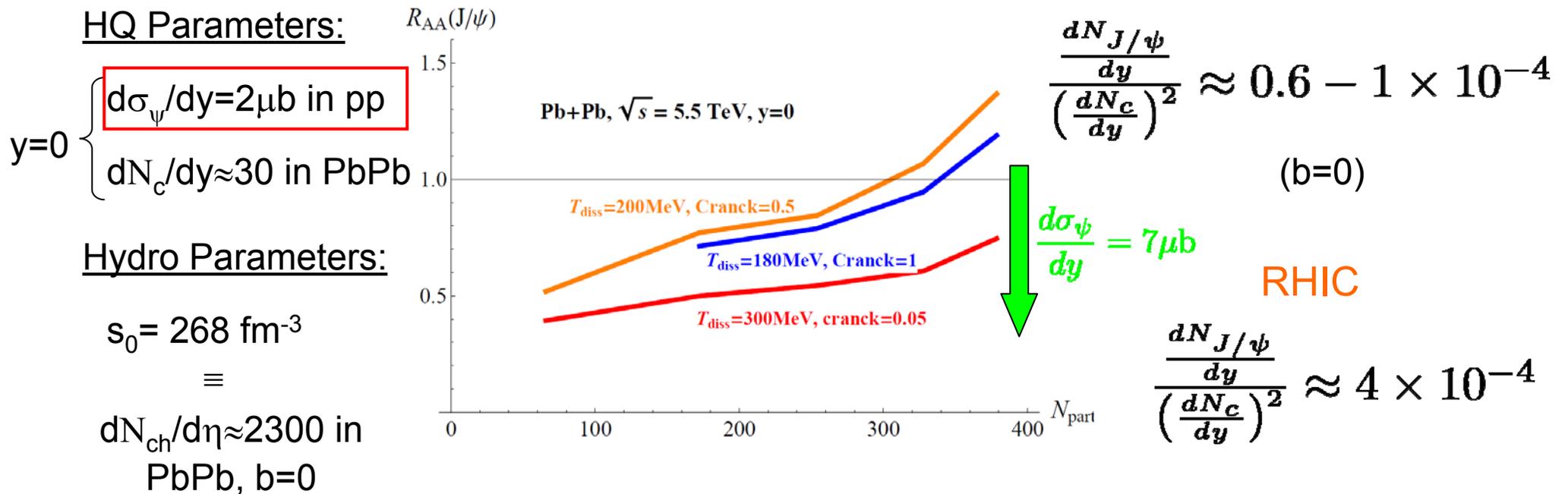
Otherwise, low dissociation ( $T_{\text{diss}} \approx 0.2$  GeV) are unavoidable

2. Can we challenge the picture of statistical recombination (A. Andronic, PBM, J. Stachel) ?

Statistical recombination picture could not be recovered from the transport theory

# Prediction for LHC:

Work to be continued during the LHC ERA:



Fusion of c-quarks at LHC: 15-25 x more probable than at RHIC, but strong increase of the prompt J/ψ as well....