



# $Z\gamma$ VBS measurements with ATLAS full Run2

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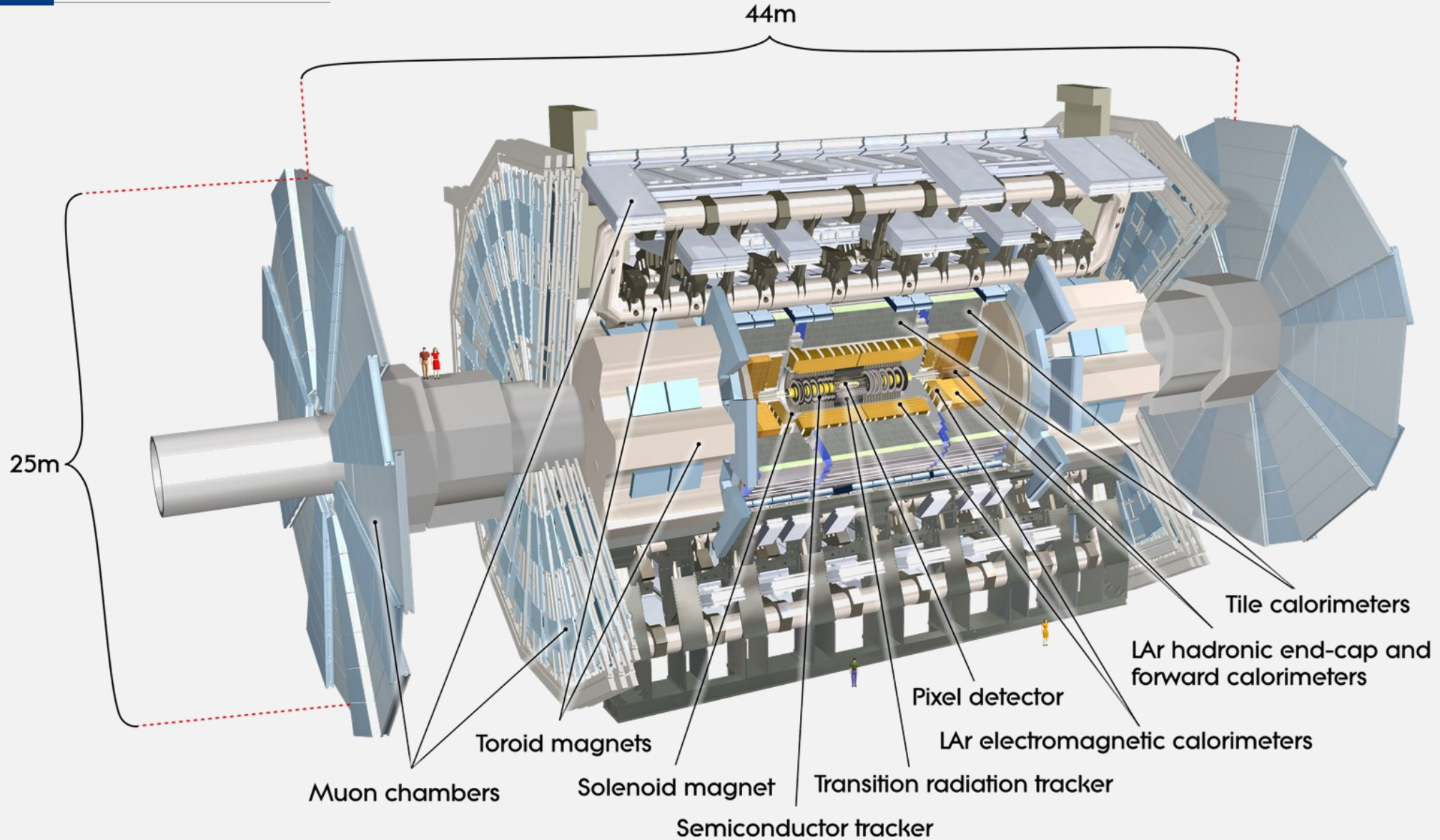
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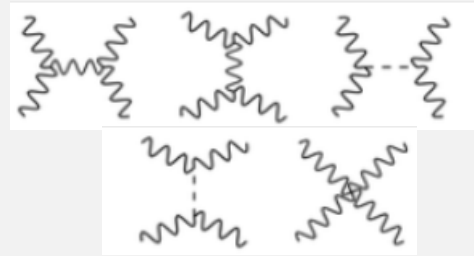
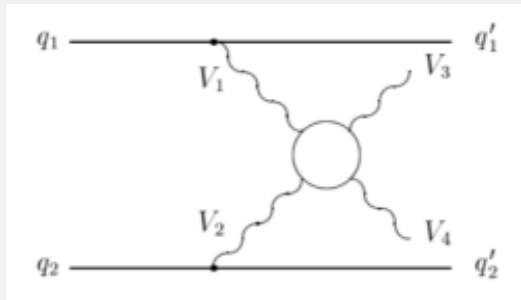
# ● ATLAS detector



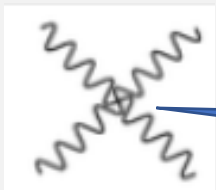
# Vector Boson Scattering

- Rare but vital in both SM and BSM

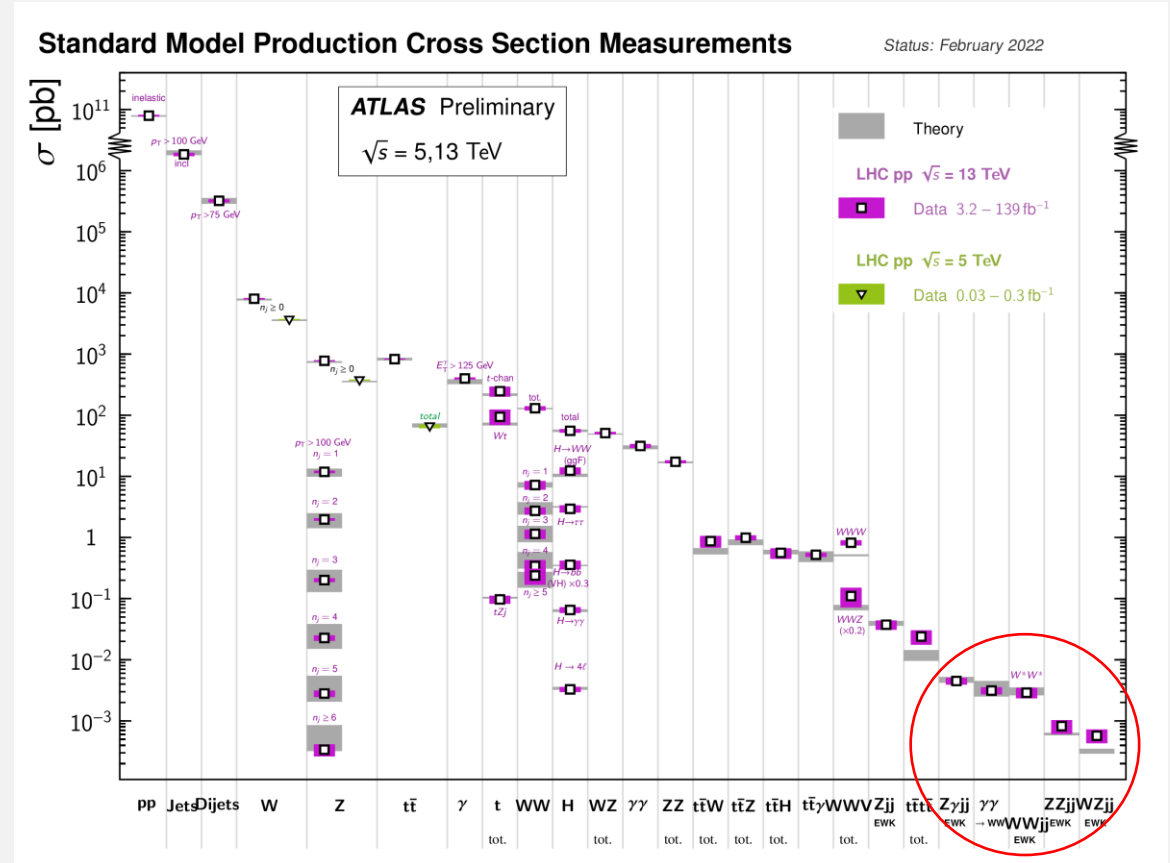
- Cross-section  $\sim \text{fb}$  : Challenging for analysis
- Rich physics contents



- Key process to probe the mechanism of electroweak symmetry breaking
- Sensitive to many new physics scenarios
- Crucial inputs for EFT study like aQGC



(anomalous) Quartic Gauge Coupling  
Higgs can also be involved



# ● ATLAS VBS Z $\gamma$ jj analysis with full Run2

- **Pure VBS and quartic coupling is not accessible (due to gauge invariance)**
  - Typical study of the EWK production of VVjj process
  - 2 energetic jets with large angle ( $\Delta\eta$ ), high invariant mass ( $m_{jj}$ )
  - Little hadronic activity in the rapidity gap  $\rightarrow$  distinctive feature of VBS VVjj
- **EWK Z $\gamma$  process observed and measured with ATLAS full Run2 data**
  - Leptonic decay of Z:
    - EWK Z( $\rightarrow ll$ ) $\gamma$ jj : observed at  $10\sigma$
  - Invisible decay of Z:
    - EWK Z( $\rightarrow \nu\nu$ ) $\gamma$ jj w/ photon  $p_T \in [15, 110]$  GeV: observed at  $5.2\sigma$
    - EWK Z( $\rightarrow \nu\nu$ ) $\gamma$ jj w/ photon  $p_T > 150$  GeV : to be public
- **BSM topics discussed : aQGC, dark photon, invisible decay of Higgs and so on**

	Obs (Exp) sign.	Fid. XS of EW-Z $\gamma$ jj / fb	Ref
Z( $\rightarrow ll$ ) $\gamma$ jj VBS analysis	$10\sigma$ ( $11\sigma$ )	$4.49 \pm 0.40$ (stat.) $\pm 0.42$ (syst.)	<a href="#">ATLAS-CONF-2021-038</a>
VBF+MET+Photon (EW-Z $\nu\nu$ ) $\gamma$ jj w/ $p_T^\gamma \in [15, 110]$ GeV	$5.2\sigma$ ( $5.1\sigma$ )	$1.31 \pm 0.20$ (stat.) $\pm 0.20$ (syst.)	<a href="#">Eur. Phys. J. C 82 (2022) 105</a>
Z( $\rightarrow \nu\nu$ ) $\gamma$ jj VBS analysis ( $p_T^\gamma > 150$ GeV)		(To be public)	



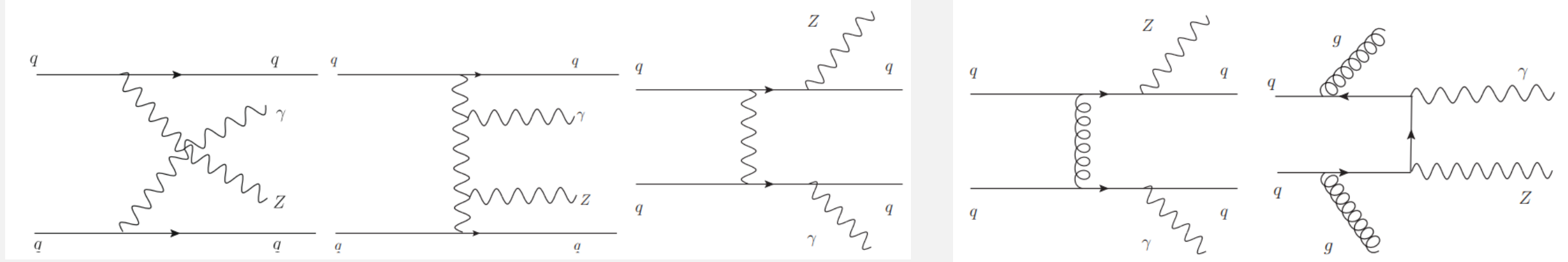
# $Z(\rightarrow ll)\gamma jj$ VBS

ATLAS-CONF-2021-038

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# ● $Z(\rightarrow ll)\gamma jj$ VBS analysis : Introduction

- EW production  $Z\gamma jj$  studied in the  $e\bar{e}\gamma jj$  and  $\mu\bar{\mu}\gamma jj$  channels using 139/fb data
- Dominant background from QCD production  $Z\gamma jj$



Quartic gauge coupling  
VBS signal

Triple gauge coupling

EWK non-VBS signal

Gluon exchange  
QCD background

Gluon radiation  
QCD background



EWK production  $Z\gamma jj$   
(Signal)



QCD production  $Z\gamma jj$   
(Dominant Background)

Madgraph LO

Madgraph NLO  
(Alt. Sherpa2.2.4/2.2.10)

# ● $Z(\rightarrow ll)\gamma jj$ VBS analysis : Selection

Single and di-lepton trigger used in analysis

25GeV photon  $E_T$  requirement

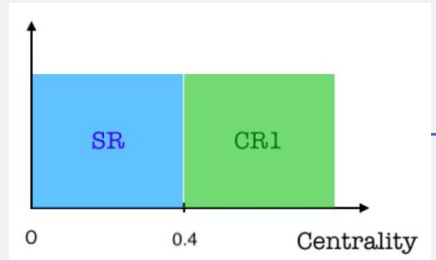
→ reduce significantly Z+jets and pile-up background

Remove low-mass resonance by requiring large  $m_{ll}$

Remove the FSR photon by requiring large  $m_{ll} + m_{ll\gamma}$

$Z\gamma$  centrality cut to separate EWK and QCD  $Z\gamma jj$  process

$$\zeta(Z\gamma) = \left| \frac{y_{Z\gamma} - (y_{j1} + y_{j2})/2}{(y_{j1} - y_{j2})} \right|$$



No jet in rapidity gap of two jets → increase S/B

Lepton	$p_T^\ell > 20, 30(\text{leading}) \text{ GeV}, \quad  \eta_\ell  < 2.47$ $N_\ell \geq 2$
Photon	$E_T^\gamma > 25 \text{ GeV}, \quad  \eta_\gamma  < 2.37$ $E_T^{\text{cone}20} < 0.07 E_T^\gamma$ $\Delta R(\ell, \gamma) > 0.4$
Jet	$p_T^{\text{jet}} > 50 \text{ GeV}, \quad  y_{\text{jet}}  < 4.4$ $ \Delta y  > 1.0$ $m_{jj} > 150 \text{ GeV}$ remove jets if $\Delta R(\gamma, j) < 0.4$ or if $\Delta R(\ell, j) < 0.3$
Event	$m_{ll} > 40 \text{ GeV}$ $m_{ll} + m_{ll\gamma} > 182 \text{ GeV}$ $\zeta(ll\gamma) < 0.4$ $N_{\text{jets}}^{\text{gap}} = 0$



# ● $Z(\rightarrow ll)\gamma jj$ VBS analysis : Background

## ➤ QCD $Z\gamma jj$ : Estimated from MC

- Norm. fitted in SR and CR1 ( $\zeta_{Z\gamma}$  cut inverted)

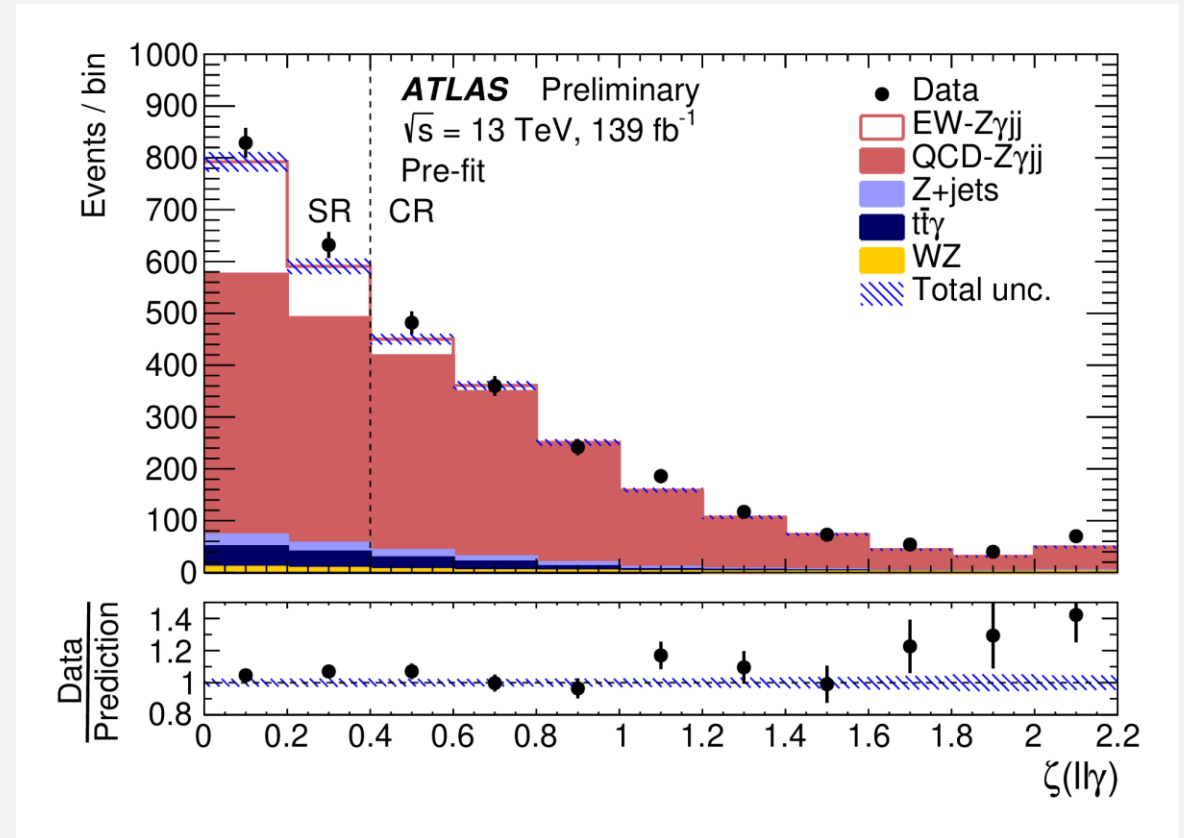
## ➤ Z+jets : Data-driven

- Normalization and shape extracted from data
- 2D Sideband method : photon ID and isolation

## ➤ $t\bar{t}\gamma$ : Estimated from MC (Madgraph LO)

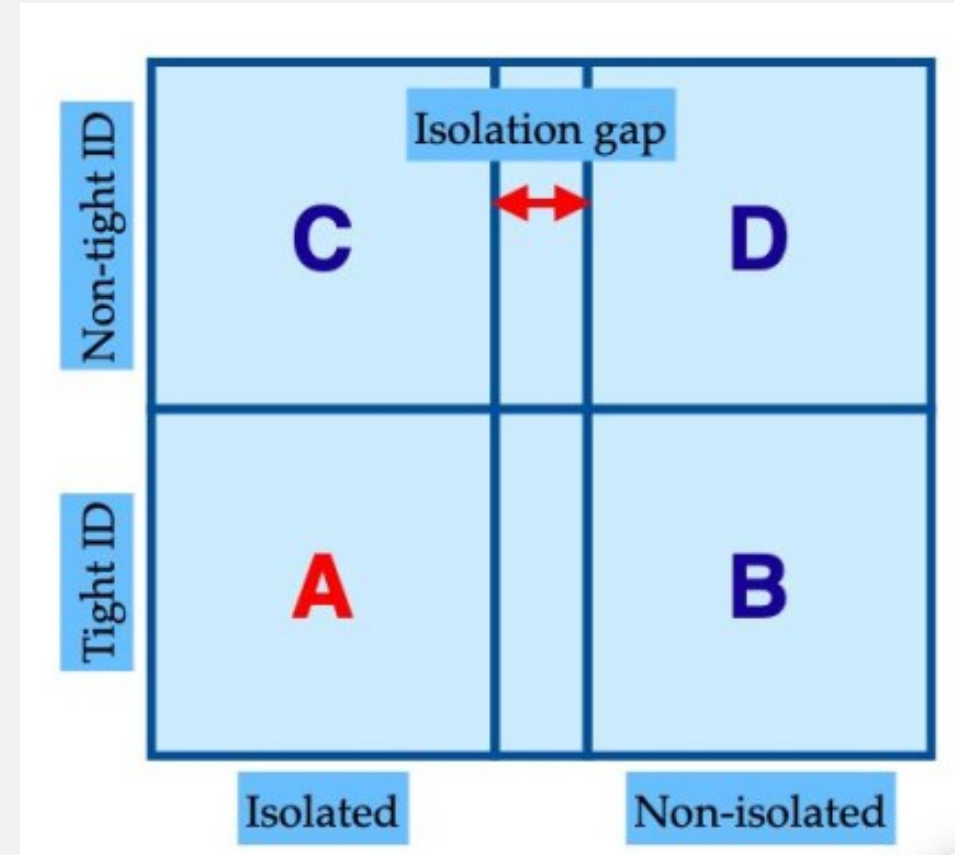
- Scale factor of 1.44 and in agreement with [1]
- Validated with data in standalone  $e\mu\gamma$  CR

## ➤ WZjj: Estimated from MC (Sherpa/Madgraph)



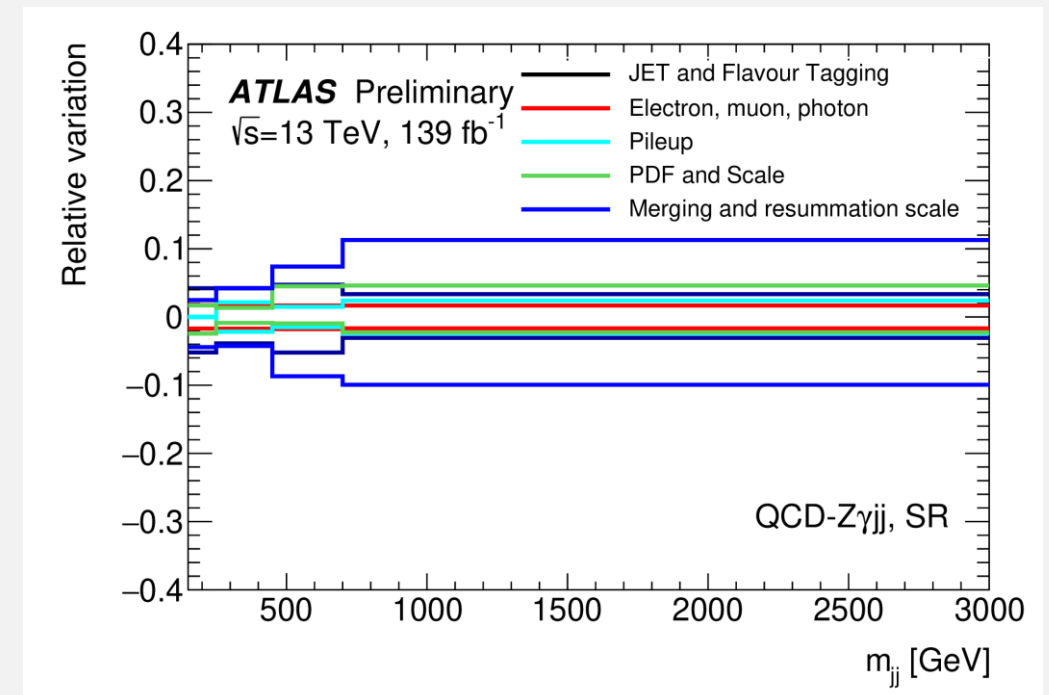
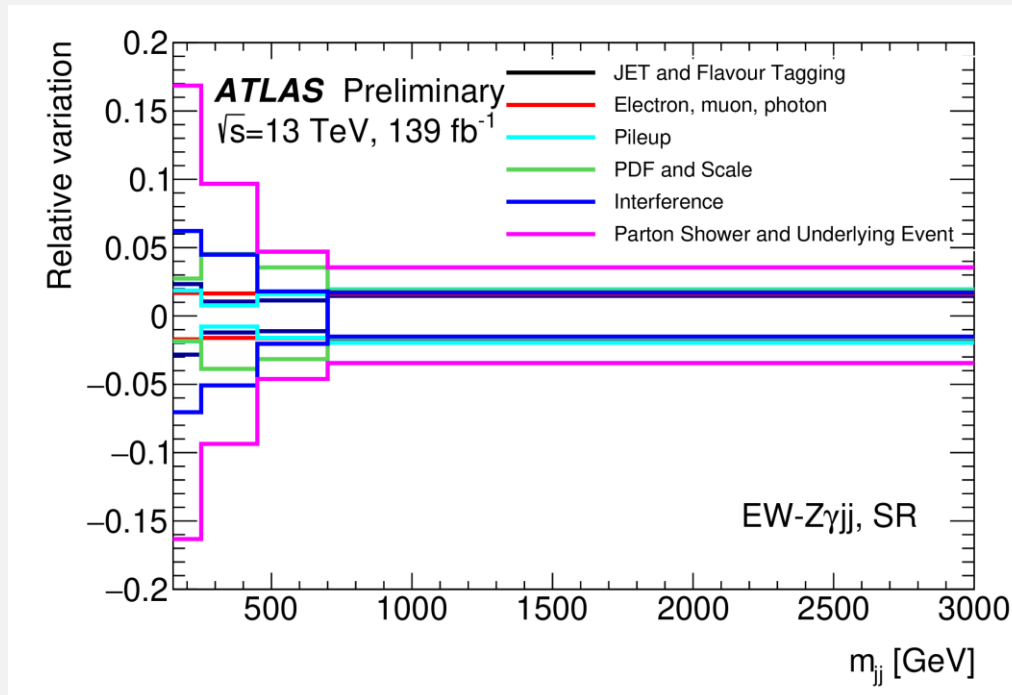
# ● $Z(\rightarrow ll)\gamma jj$ VBS analysis : Background

- QCD  $Z\gamma jj$ : Estimated from MC
  - Norm. fitted in SR and CR1 ( $\zeta_{Z\gamma}$  cut inverted)
- **Z+jets : Data-driven**
  - **Normalization and shape extracted from data**
  - **2D Sideband method : photon ID and isolation**
- $t\bar{t}\gamma$ : Estimated from MC (Madgraph LO)
  - Scale factor of 1.44 and in agreement with [1]
  - Validated with data in standalone  $e\mu\gamma$  CR
- $WZjj$ : Estimated from MC (Sherpa/Madgraph)



# ● $Z(\rightarrow ll)\gamma jj$ VBS analysis : Systematics

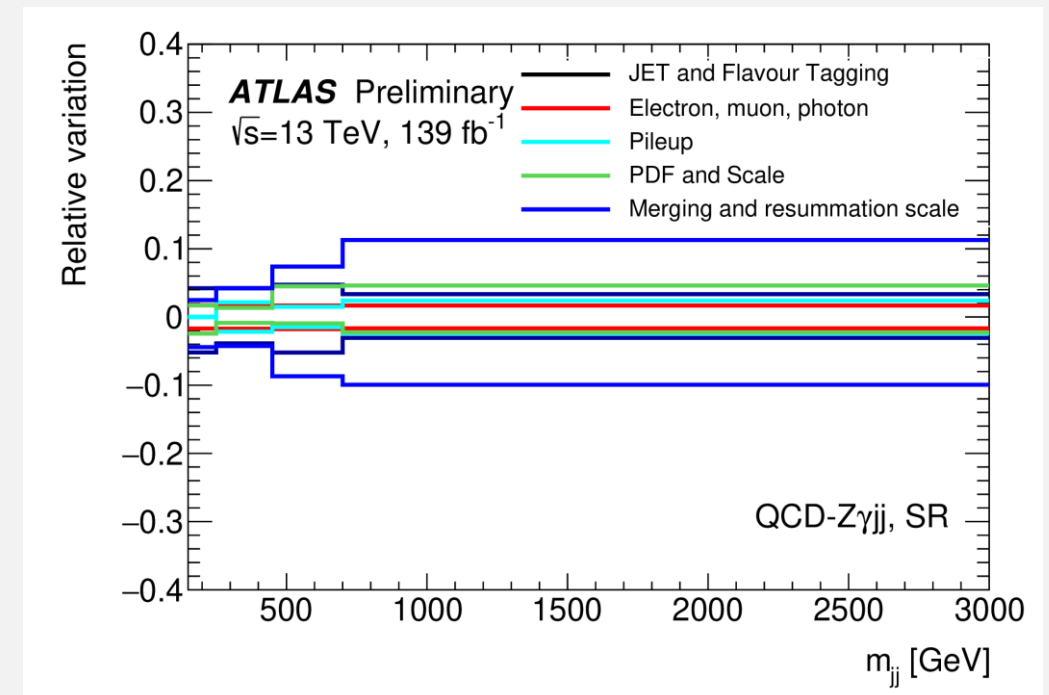
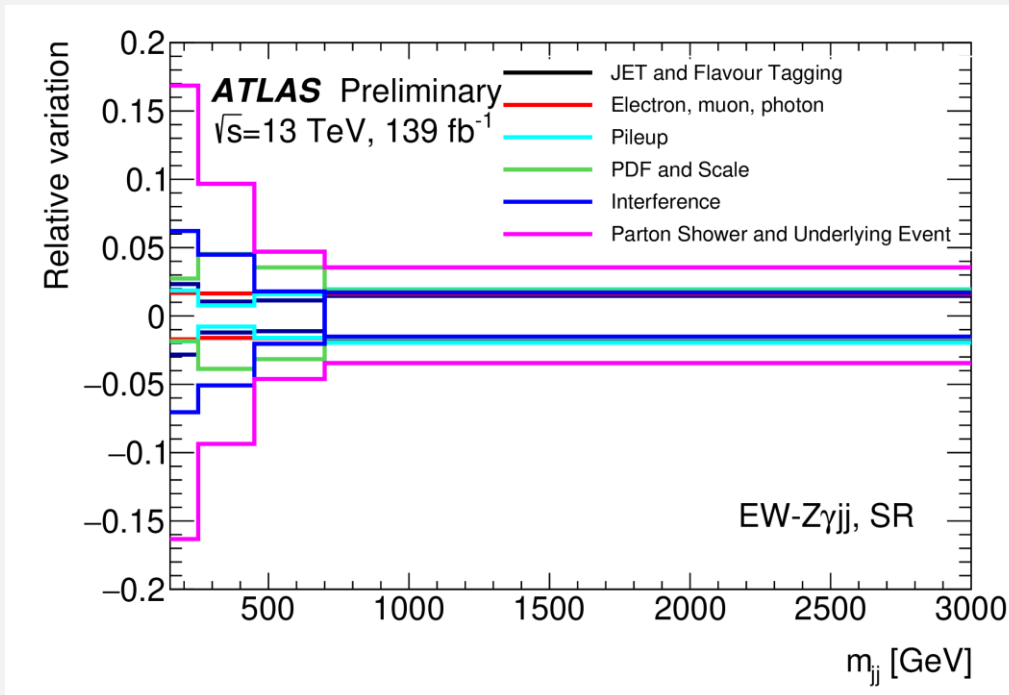
- **Experimental Systematics:**
  - Lepton, Photon, Jet and PRW
  - Typically <2% and largest from jet energy calibration and response
  - Correlated among all the regions and processes
- **Background Normalization:**
  - 35% uncertainty for Z+jets from Data-driven
  - 15% (20%) uncertainty for  $t\bar{t}\gamma$  (WZ) estimated from QCD scale and PDF



# $Z(\rightarrow ll)\gamma jj$ VBS analysis : Systematics

## Theoretical Systematics:

- Scale and PDF variation for both EW- and QCD-  $Z\gamma jj$
- Parton showering and underlying event model variation of EW- $Z\gamma jj$ 
  - Only shape difference considered
- Merging (CKKW) and resummation (QSF) scale variation of QCD- $Z\gamma jj$ 
  - Estimated based on Sherpa2.2.10 LO samples
- Interference between EW- and QCD- $Z\gamma jj$  considered as an extra uncertainty



# ● $Z(\rightarrow ll)\gamma jj$ VBS analysis : Signal Extraction

- Maximum likelihood fit of  $m_{jj}$  on SR and CR simultaneously to extract

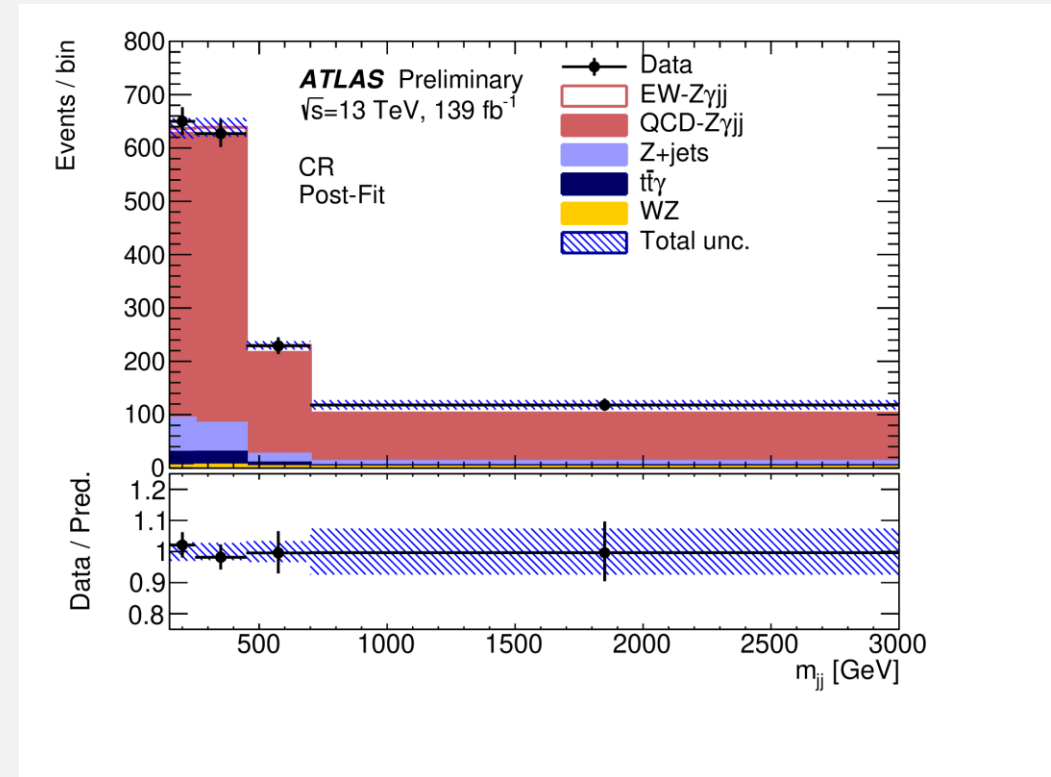
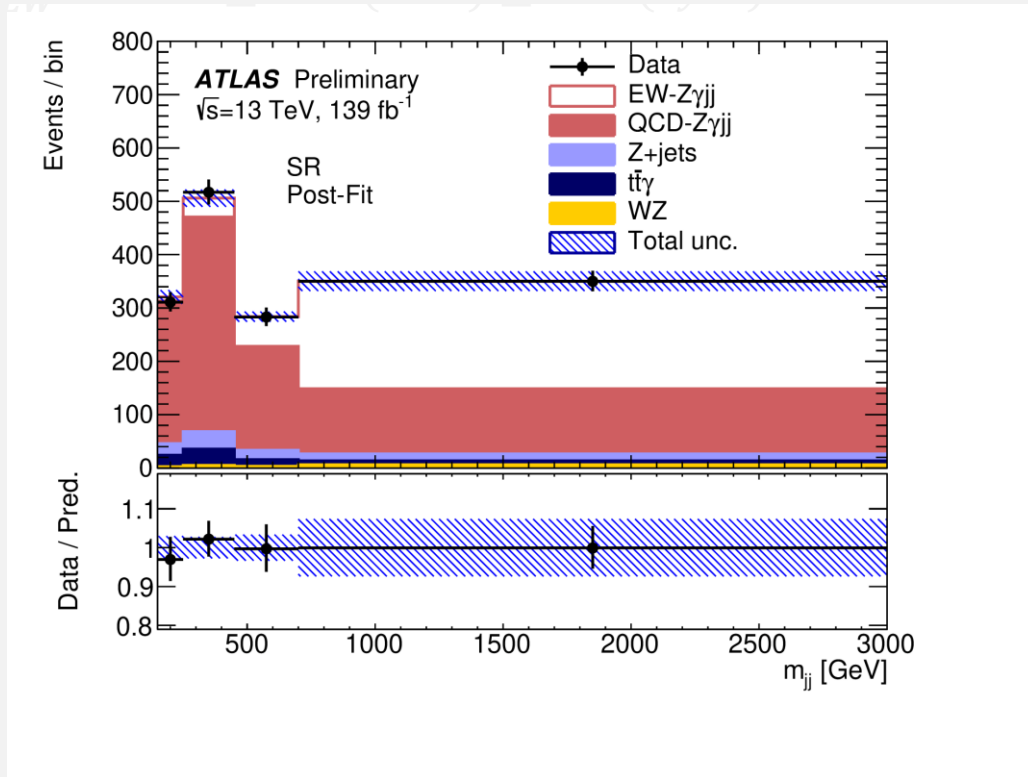
- Signal strength for EW- $Z\gamma jj$  :  $\mu_{EW} \equiv \frac{\sigma_{EW}^{meas.}}{\sigma_{EW}^{exp.}}$  correlated between SR and CR
- Two norm. factors for QCD- $Z\gamma jj$  : decorrelated between SR and CR  
→ CR only used to validate the shape and constrain the systematics

	SR	CR1
$\mu_{EWK}$	✓	✓
$\mu_{QCD}^{SR}$	✓	
$\mu_{QCD}^{CR1}$		✓

# ● $Z(\rightarrow ll)\gamma jj$ VBS analysis : Signal Extraction

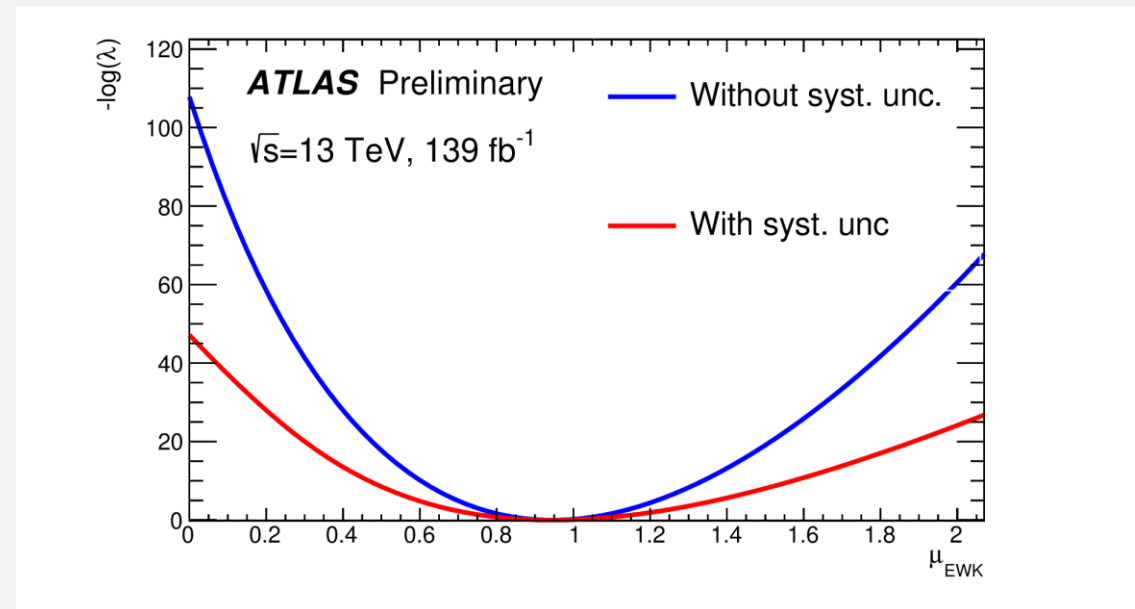
- Maximum likelihood fit of  $m_{jj}$  on SR and CR simultaneously to extract
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  - Two norm. factors for QCD- $Z\gamma jj$  : decorrelated between SR and CR  
→ CR only used to validate the shape and constrain the systematics
- The post-fit distribution shows good data/MC agreement

Sample	SR	CR
$N_{EW-Z\gamma jj}$	$300 \pm 36$	$55 \pm 7$
$N_{QCD-Z\gamma jj}$	$987 \pm 55$	$1352 \pm 60$
$N_{t\bar{t}\gamma}$	$72 \pm 11$	$59 \pm 9$
$N_{WZ}$	$17 \pm 3$	$14 \pm 3$
$N_{Z+jets}$	$85 \pm 30$	$143 \pm 43$
Total	$1461 \pm 38$	$1624 \pm 40$
$N_{obs}$	1461	1624



## ● $Z(\rightarrow ll)\gamma jj$ VBS analysis : Signal Extraction

- Maximum likelihood fit of  $m_{jj}$  on SR and CR simultaneously to extract
  - Signal strength for EW- $Z\gamma jj$  :  $\mu_{EW} \equiv \frac{\sigma_{EW}^{meas.}}{\sigma_{EW}^{exp.}}$  correlated between SR and CR
  - Two norm. factors for QCD- $Z\gamma jj$  : decorrelated between SR and CR  
→ CR only used to validate the shape and constrain the systematics
- The post-fit distribution shows good data/MC agreement
- $\mu_{EW} = 0.95 \pm 0.08 (stat) \pm 0.11 (syst)$



EW-  $Z(\rightarrow ll)\gamma jj$  observed with more than  $10\sigma$  ( $11\sigma$  expected)

# ● $Z(\rightarrow ll)\gamma jj$ VBS analysis : Measurement of Cross-section

## • Fiducial cross-section of EW- $Z\gamma jj$ measured from $\mu_{EW}$ :

- $\sigma_{EW} = 4.49 \pm 0.40 (stat) \pm 0.42 (syst) fb$
- $\sigma_{EW}^{pred} = 4.73 \pm 0.01 (stat) \pm 0.15 (PDF)_{-0.22}^{+0.23} (scale) fb$

	Data stat.	MC stat.	Background	Reco	EW mod.	QCD mod.	Total
$\Delta\sigma_{EW}/\sigma_{EW} [\%]$	$\pm 9$	$\pm 1$	$\pm 1$	$\pm 5$	$_{-5}^{+6}$	$_{-4}^{+5}$	$\pm 13$

## • Fid. cross-section of EW+QCD $Z\gamma jj$ measured in SR-only:

- $\sigma_{EW+QCD} = 20.6 \pm 0.6 (stat)_{-1.0}^{+1.2} (syst) fb$
- $\sigma_{EW+QCD}^{pred} = 20.4 \pm 0.1 (stat) \pm 0.2 (PDF)_{-2.0}^{+2.6} (scale) fb$

Source	Size [%]
Electron/photon calibration	$\pm 0.3$
Photon	$\pm 0.3$
Backgrounds	$\pm 1.0$
Electron	$\pm 1.1$
Flavour tagging	$\pm 1.1$
Muon	$\pm 1.1$
MC stat.	$\pm 1.4$
Pileup	$\pm 2.6$
Jets	$\pm 4.7$
QCD- $Z\gamma jj$ modelling	$_{-4.3}^{+4.8}$
EW- $Z\gamma jj$ modelling	$_{-4.6}^{+5.7}$
Data stat.	$\pm 8.8$
Total	$_{-12.6}^{+13.4}$



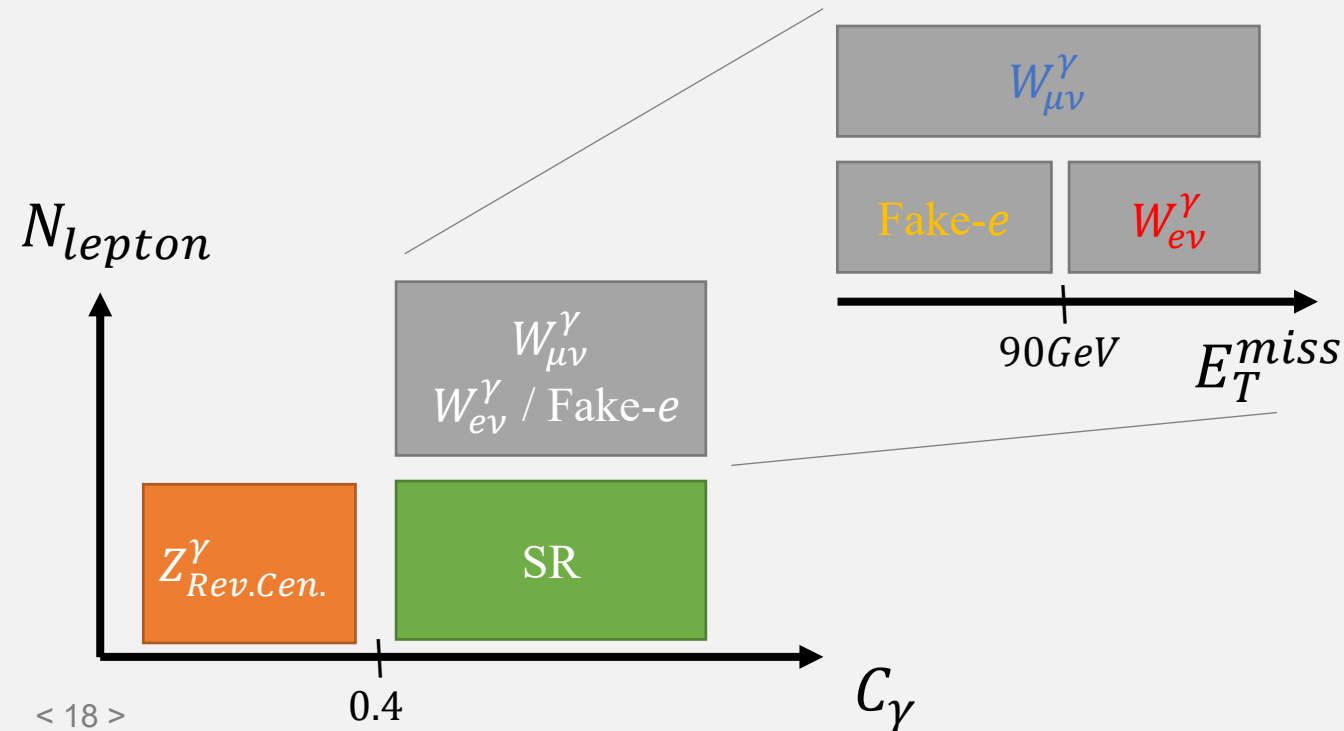
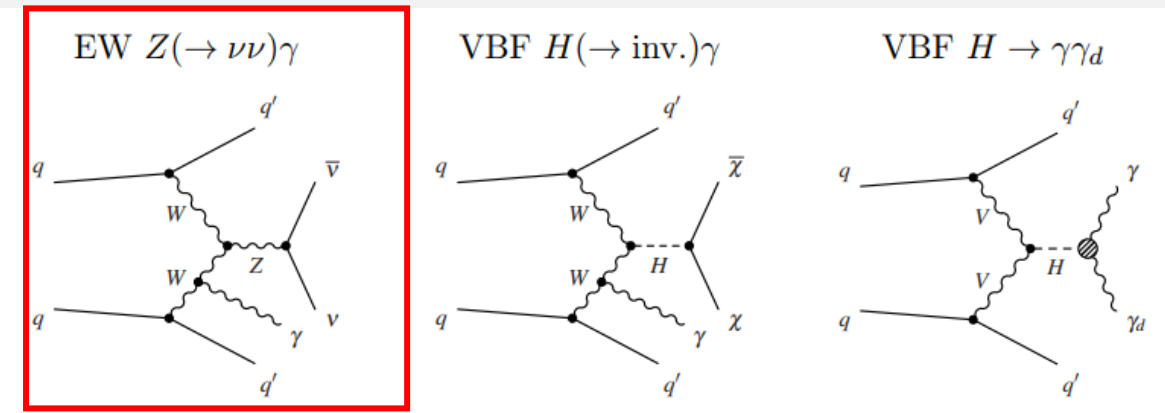


# $EW Z(\rightarrow \nu\nu)\gamma jj$

Eur. Phys. J. C 82 (2022) 105

# ● Observation of EW $Z(\rightarrow \nu\nu)\gamma jj$ : Overview

- Analysis originally designed to search for  $H(\rightarrow \text{inv})\gamma$  with VBF+**MET**+Photon signature
- EW-production of  $Z(\rightarrow \nu\nu)\gamma jj$  studied for  $p_T^\gamma \in [15, 110]$  GeV with dedicated regions
- Dominant background from QCD- $Z\gamma jj$  and  $W(l\nu)\gamma$ +jets and controlled with CRs
  - $W_{\mu\nu}^\gamma$ ,  $W_{ev}^\gamma$  and Fake- $e$  region: allowing one lepton (or jet fake electron)
  - $Z_{Rev.Cen.}^\gamma$  CR: low photon centrality (reversed) where QCD- $Z\gamma jj$  enriched
- Signal extracted from simultaneous fitting across all the regions



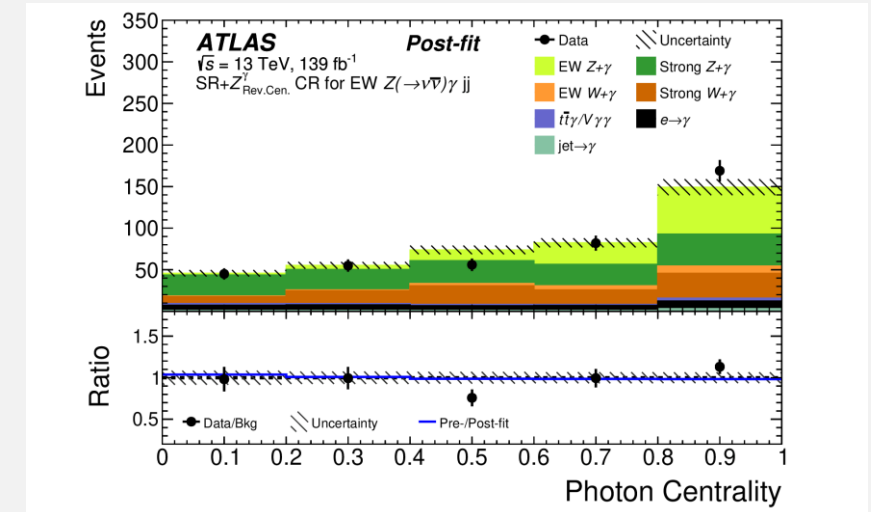
# ● Observation of EW $Z(\rightarrow \nu\nu)\gamma jj$ : Selection

- **Centrality Cut**
  - Photon centrality:  $C_\gamma$
  - 3<sup>rd</sup> jet centrality:  $C_3$

Observable	Requirements
$N_{\text{jet}}$ with $p_T > 25$ GeV	$\geq 2$
$ \eta(j_{1,2}) $	$< 4.5$
$p_T(j_1)$ [GeV]	$> 60$
$p_T(j_2)$ [GeV]	$> 50$
$\Delta R(j, \ell)$	$> 0.4$
$ \Delta\eta_{ij} $	$> 3.0$
$C_3$	$< 0.7$
$m_{jj}$ [TeV]	$> 0.5$
truth- $E_T^{\text{miss}}$ [GeV]	$> 150$
$\Delta\phi(\text{truth-}\vec{E}_T^{\text{miss}}, j_i)$	$> 1.0$
$p_T(\gamma)$ [GeV]	$> 15, < 110$
$ \eta(\gamma) $	$< 2.37$
$E_T^{\text{cone20}}/E_T^\gamma$	$< 0.07$
$\Delta R(\gamma, \text{jet-or-}\ell)$	$> 0.4$
$C_\gamma$	$> 0.4$
$\Delta\phi(\text{truth-}\vec{E}_T^{\text{miss}}, \gamma)$	$> 1.8$
$N_\ell$ with $p_T > 4$ GeV and $ \eta  < 2.47$	0

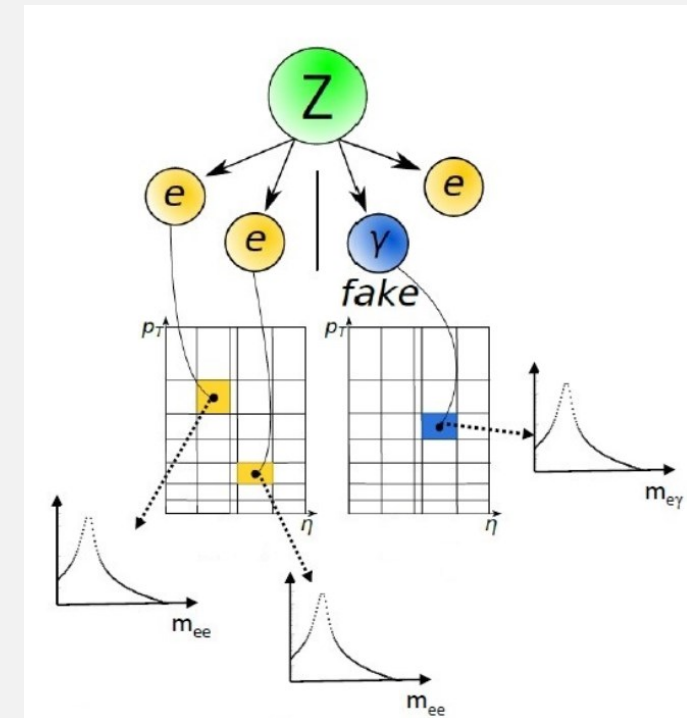
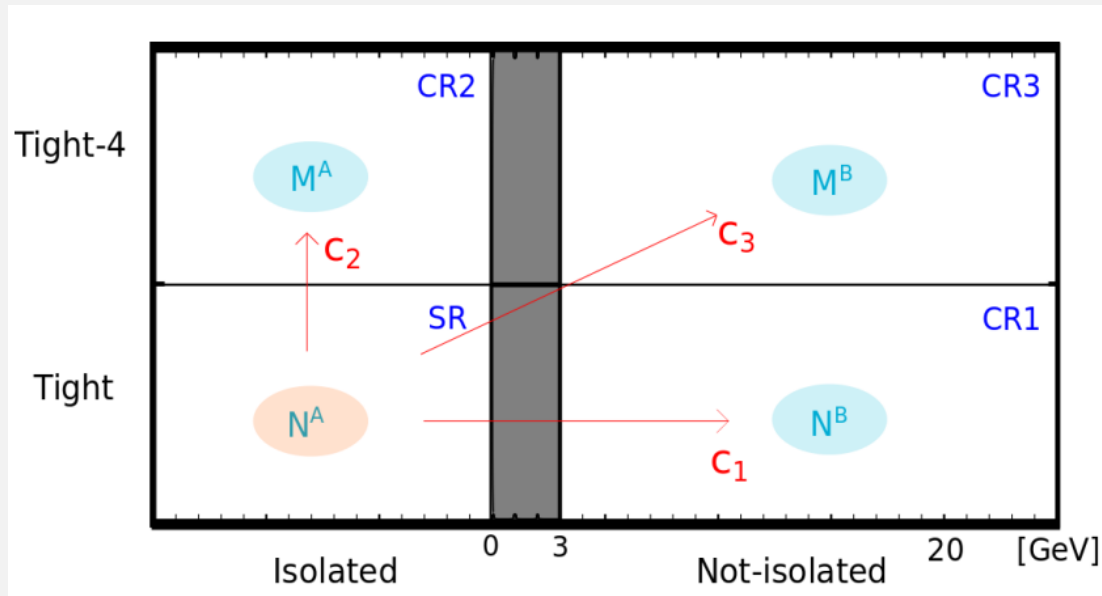
$$C_\gamma = \exp\left[-\frac{4}{(\eta_1 - \eta_2)^2}\left(\eta_\gamma - \frac{\eta_1 + \eta_2}{2}\right)^2\right]$$

$$C_3 = \exp\left[-\frac{4}{(\eta_1 - \eta_2)^2}\left(\eta_3 - \frac{\eta_1 + \eta_2}{2}\right)^2\right]$$



# ● Observation of EW $Z(\rightarrow \nu\nu)\gamma jj$ : Fake Photon Background

- Jet fakes photon enter SR e.g. from  $Z(\nu\nu)+jets$ 
  - Estimated using data-driven method based on isolation and tight ID
  - $\sim 1\%$  of SR and 50% uncertainty assigned mainly due to MC statistics
- Electron fakes photon from e.g.  $W(e\nu)+jets$ :
  - measured by comparing  $ee$  and  $e\gamma$  rates in Z peak
  - $\sim 6\%$  in EW  $Z(\rightarrow \nu\nu)\gamma$  signal region and uncertainty ranging from 15-30%



# ● Observation of EW $Z(\rightarrow \nu\nu)\gamma jj$ : Uncertainties

- **Dominated by statistical unc. in all channels**
- **Large systematic variation from modelling:**
  - Scale var. 25%~56% (3%~11%) for QCD (EW)- $V\gamma jj$
  - Madgraph v.s. Sherpa up to 20% for QCD- $V\gamma jj$
  - Parton showering model: 4-15% for EW- $V\gamma jj$
  - Interference between EW- and QCD- $V\gamma jj$  up to -22%
- **Post-fit impact of each systematics term →**
  - Largest exp. systematic impact from jet related

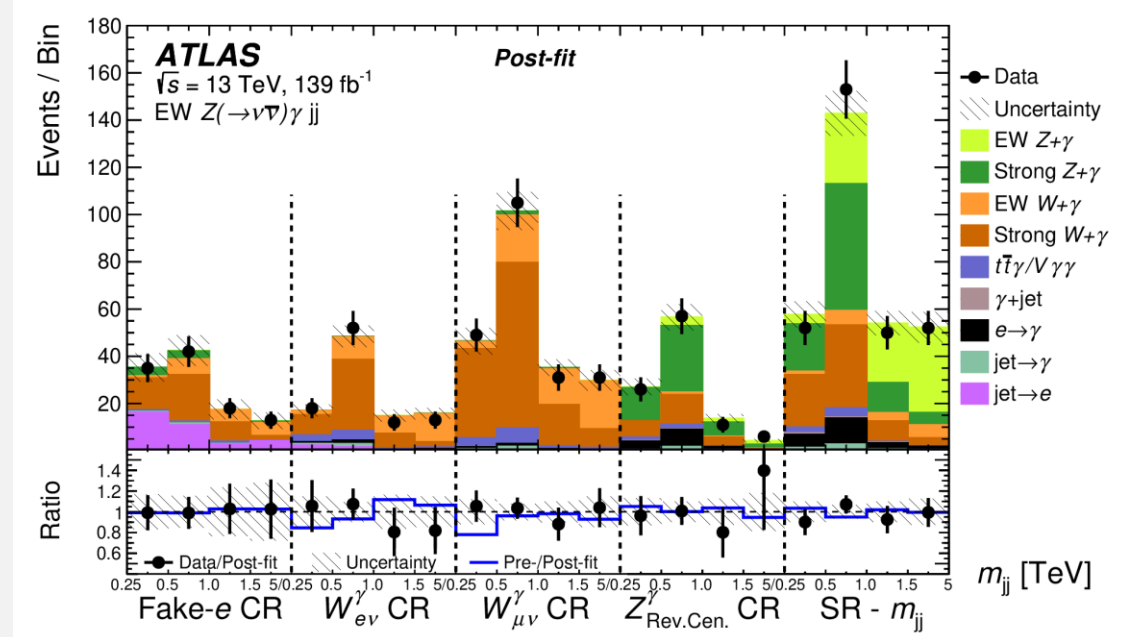
Source	$1\sigma$ Uncertainty on $\mu_{Z\gamma EW}$
Jet scale and resolution	0.076
$V\gamma$ + jets theory	0.067
pile-up	0.040
Photon	0.035
$e \rightarrow \gamma$ , jet $\rightarrow e, \gamma$ Bkg.	0.035
Lepton	0.027
$E_T^{\text{miss}}$	0.023
Signal theory shape	0.020
Signal theory acceptance	0.12
Data stats.	0.16
$W\gamma$ + jets/ $Z\gamma$ + jets Norm.	0.073
MC stats.	0.063
<b>Total</b>	<b>0.25</b>

# ● Observation of EW $Z(\rightarrow \nu\nu)\gamma jj$ : Signal Extraction & Meas.

- **Maximum likelihood fit performed :**  
signal strength and normalization of dominant background determined simultaneously
- **4  $m_{jj}$  bins for each region and totally 4+16 bins**
- **5.2 $\sigma$  (5.1 $\sigma$  expected) observed of EW- $Z\gamma jj$  process**
- $\sigma_{EW} = 1.31 \pm 0.20$  (stat)  $\pm 0.20$  (syst) fb
- **In agreement with prediction:**  
 $\sigma_{EW}^{pred} = 1.27 \pm 0.01$  (stat)  
 $\pm 0.17$  (LO QCD scale)  
 $\pm 0.03$  (PDF) fb  
(0.3% NLO QCD k-factor correction from VBFNLO applied)

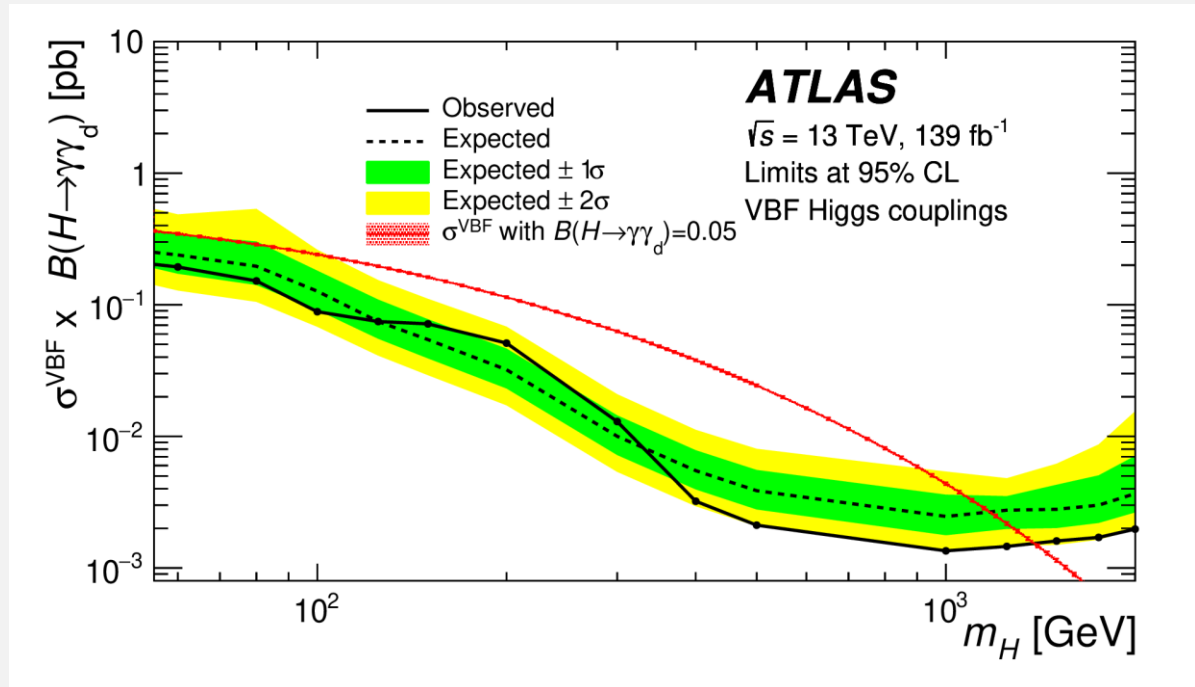
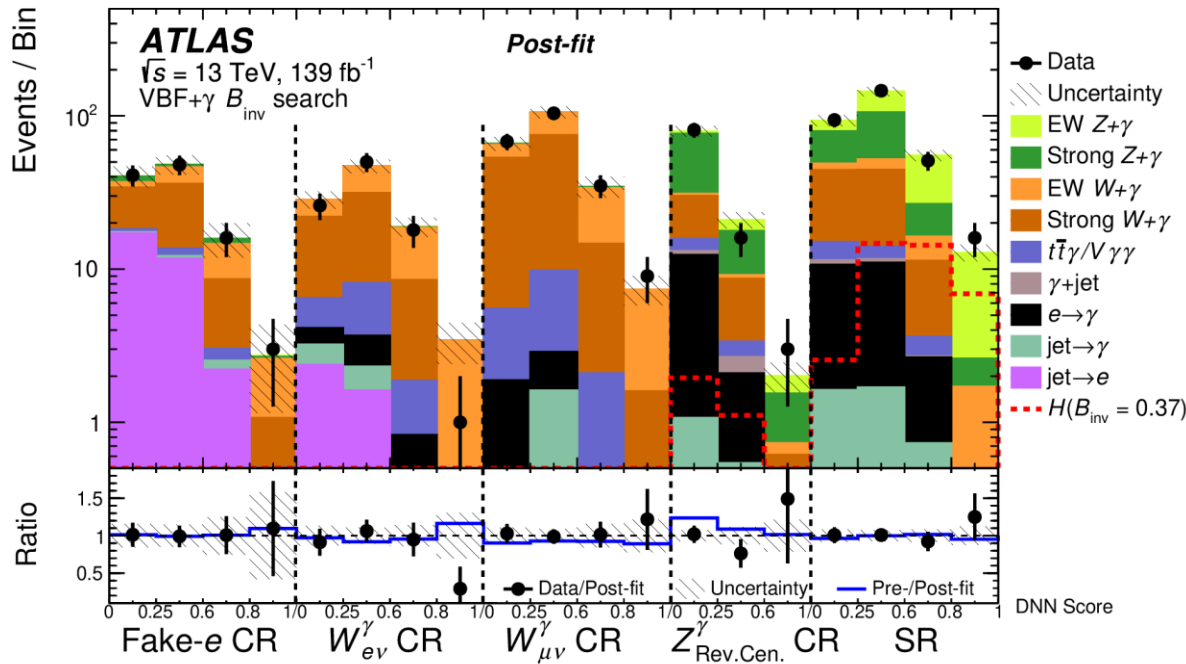
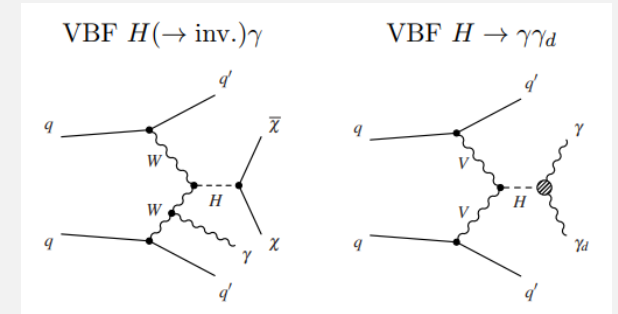
	SR	$Z_{Rev.Cen.}^\gamma$ CR	$W_{\ell\nu}^\gamma$ CRs
$\mu_{Z\gamma EWK}$	✓	✓	
$\mu_{Z\gamma QCD}$	✓	✓	
$\mu_{W\gamma}$	✓	✓	✓

$\mu_{Z\gamma EW}$	$\beta_{Z\gamma strong}$	$\beta_{W\gamma}$
$1.03 \pm 0.25$	$1.02 \pm 0.41$	$1.01 \pm 0.20$



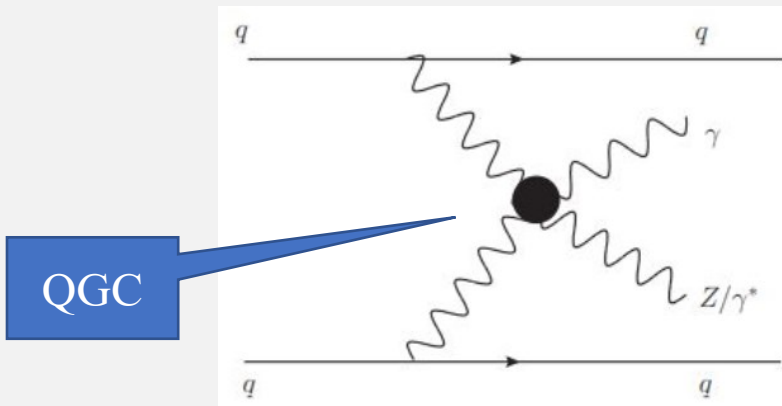
# ● Observation of EW $Z(\rightarrow \nu\nu)\gamma jj$ : BSM interpretation

- Same VBF+MET+Photon signature also used to search for  $H \rightarrow inv.$  and  $H \rightarrow \gamma\gamma_d$
  - Dense Neural Network (DNN) used as fitting discriminant
  - Highly suppress the QCD production  $Z\gamma jj$  events
  - No significant excess observed
- 95% CL upper limit of  $0.37$  ( $0.34^{+0.15}_{-0.10}$  exp.) set on observed branching ratio



# ● $Z(\rightarrow \nu\nu)\gamma jj$ VBS analysis : Overview

- Dedicated measurement of SM EWK  $Z(\rightarrow \nu\nu)\gamma jj$  process with full Run2 data
- High  $p_T^\gamma > 150\text{GeV}$  and combined with orthogonal low  $p_T^\gamma$  (15 – 110GeV) observation from VBF+MET+Photon analysis
- Dominant background from QCD  $Z(\rightarrow \nu\nu)\gamma$  [36%] and  $W(l\nu)\gamma/tt\gamma$  [32%/6%] controlled by:
  - QCD- $Z\gamma jj$  enriched regions : low  $m_{jj}$  and reversed centrality requirement
  - $W\gamma$  region :  $\geq 1$  lepton
  - Normalization simultaneously extracted together with signal strength in fit
- Fake photon and MET background estimated with data-driven and  $\sim 13\%$  in total
- Boosted decision tree developed to increase S/B and used as fitting discriminant in SR, fit together with  $m_{jj}$  in CRs
- Sensitive final states to SM/anomalous QGC and limit set using EFT formalism

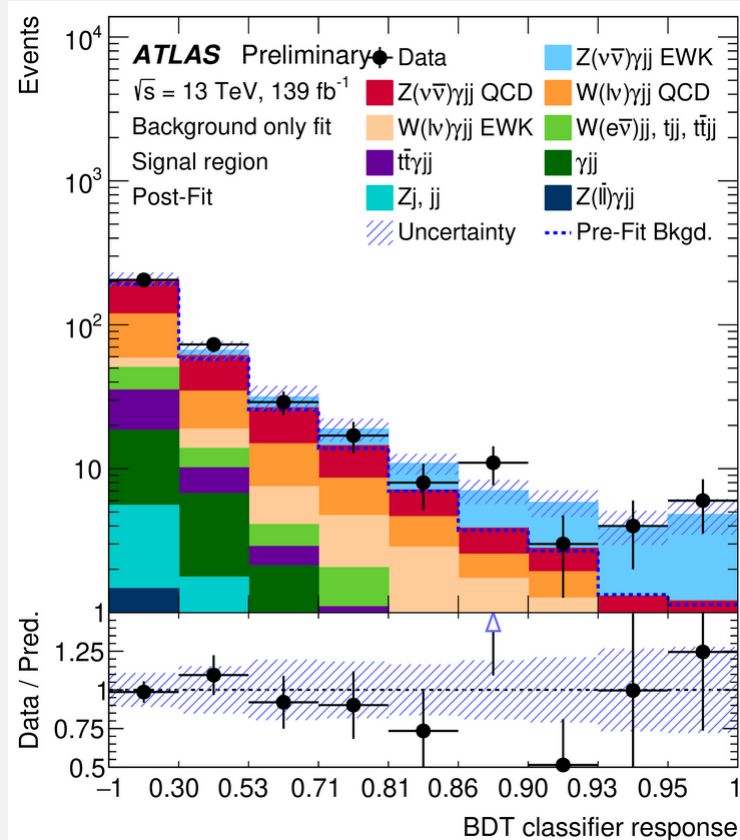


Dimension 8 operators	SM			Beyond SM					
	WWWW	WWZZ	ZZZZ	WWAZ	WWAA	ZZZA	ZZAA	ZAAA	AAAA
$\mathcal{O}_{S,0/1}$	✓	✓	✓						
$\mathcal{O}_{M,0/1/6/7}$	✓	✓	✓	✓	✓	✓	✓		
$\mathcal{O}_{M,2/3/4/5}$		✓	✓	✓	✓	✓	✓		
$\mathcal{O}_{T,0/1/2}$	✓	✓	✓	✓	✓	✓	✓	✓	✓
$\mathcal{O}_{T,5/6/7}$		✓	✓	✓	✓	✓	✓	✓	✓
$\mathcal{O}_{T,8/9}$			✓			✓	✓	✓	✓



# ● $Z(\rightarrow \nu\nu)\gamma jj$ VBS analysis : Results

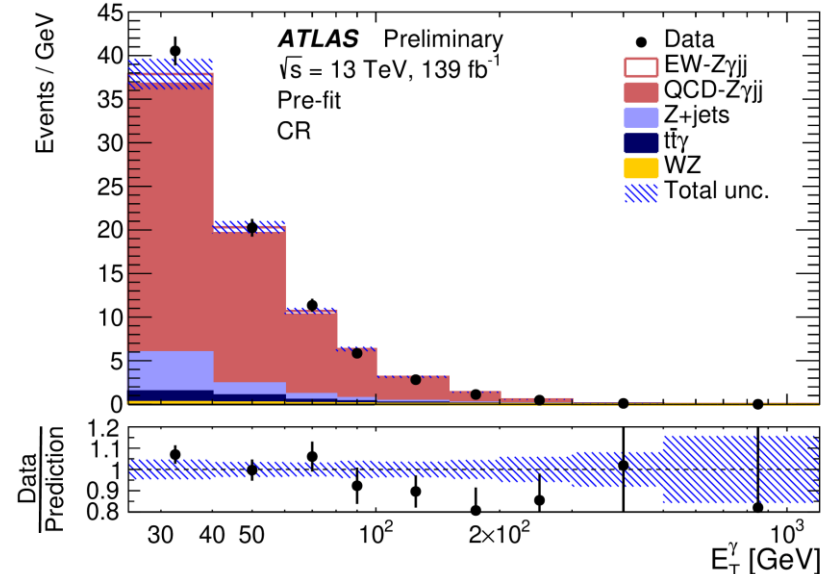
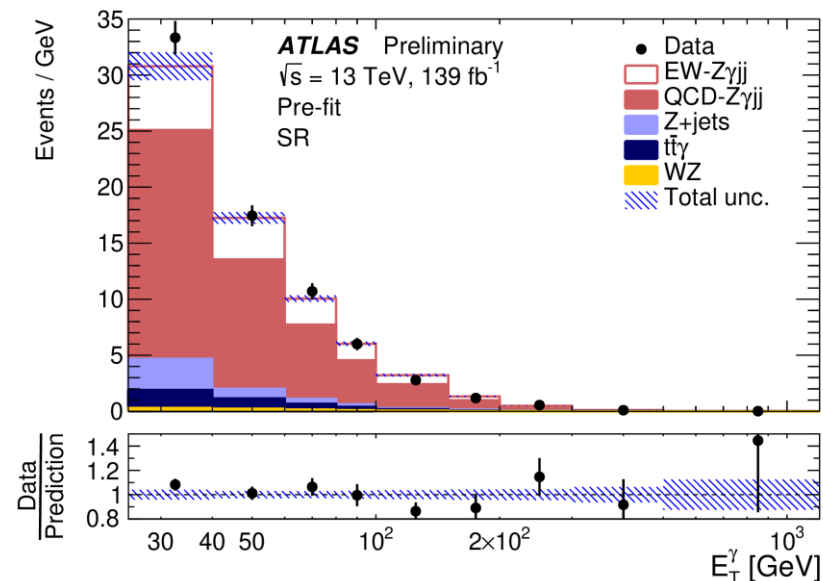
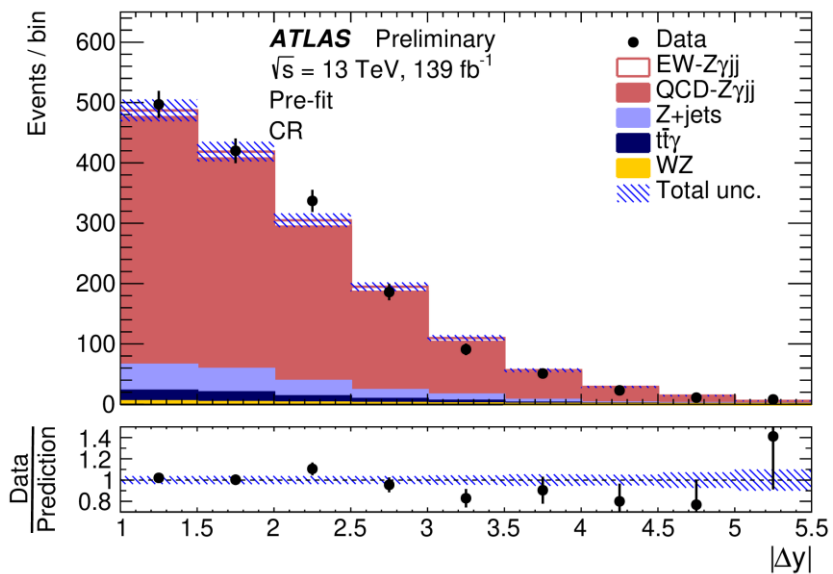
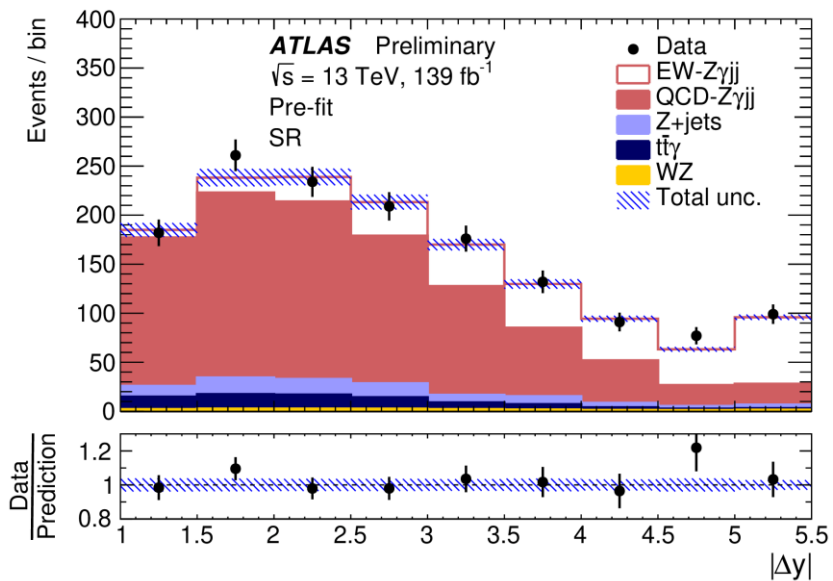
- Evidence of EW  $Z(\rightarrow \nu\nu)\gamma jj$  with high  $p_T^\gamma > 150\text{GeV}$
- Combination with observation of EW  $Z(\rightarrow \nu\nu)\gamma jj$  at low  $p_T^\gamma$  from VBF+MET+ $\gamma$  analysis : better significance
- No significant deviation from SM prediction and limit set on EFT dim-8 operator, competitive with or better than previous analyses, in particular  $f_{T5}/\Lambda^4$ ,  $f_{T8}/\Lambda^4$  and  $f_{T9}/\Lambda^4$  (best up to now)



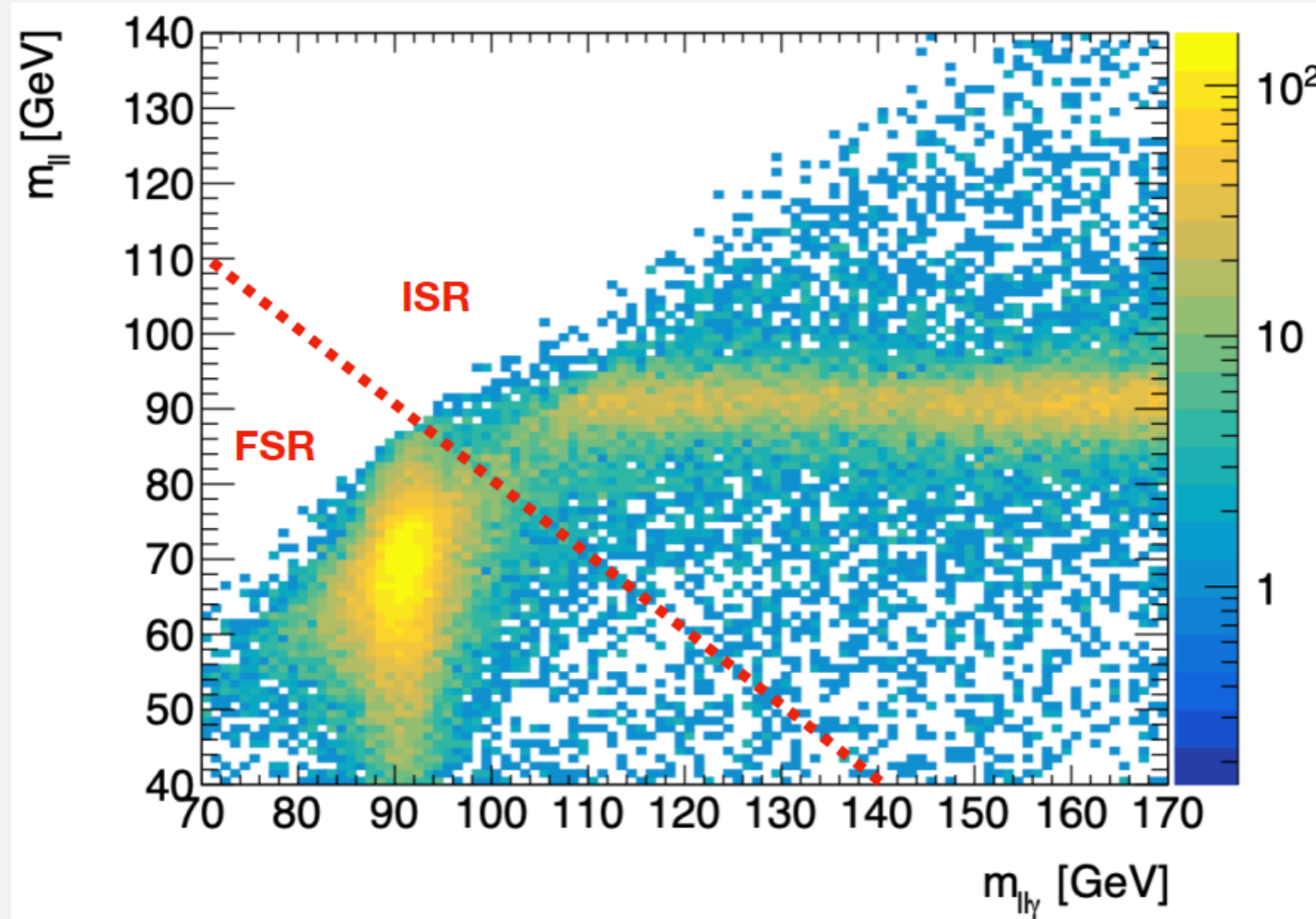
Coefficient	Observed limit, $\text{TeV}^{-4}$	Expected limit, $\text{TeV}^{-4}$
$f_{T0}/\Lambda^4$	$[-9.4, 8.4] \times 10^{-2}$	$[-1.3, 1.2] \times 10^{-1}$
● $f_{T5}/\Lambda^4$	$[-8.8, 9.9] \times 10^{-2}$	$[-1.2, 1.3] \times 10^{-1}$
● $f_{T8}/\Lambda^4$	$[-5.9, 5.9] \times 10^{-2}$	$[-8.1, 8.0] \times 10^{-2}$
● $f_{T9}/\Lambda^4$	$[-1.3, 1.3] \times 10^{-1}$	$[-1.7, 1.7] \times 10^{-1}$
$f_{M0}/\Lambda^4$	$[-4.6, 4.6]$	$[-6.2, 6.2]$
$f_{M1}/\Lambda^4$	$[-7.7, 7.7]$	$[-1.0, 1.0] \times 10^1$
$f_{M2}/\Lambda^4$	$[-1.9, 1.9]$	$[-2.6, 2.6]$

- **VBS process has rich physics interest and widely studied in ATLAS**
  - Important test of SM like EWSB and Higgs mechanism
  - Sensitive to new physics including invisible Higgs decay and dark matter
  - Crucial input for EFT study like aQGC
- **Z $\gamma$  VBS process observed and measured with ATLAS full Run2 data**
  - EWK production of  $Z(\rightarrow ll)\gamma jj$  observed with  $10\sigma$
  - EWK production of  $Z(\rightarrow \nu\nu)\gamma jj$  observed with  $5.2\sigma$
- Measurement of SM  $Z(\rightarrow \nu\nu)\gamma jj$  VBS analysis with high photon  $p_T$  :
  - Combination with low photon  $p_T$  observation from VBF+MET+Photon analysis
  - Sensitive limit set on EFT dimension-8 operator and best result of  $f_{T5}/\Lambda^4$ ,  $f_{T8}/\Lambda^4$  and  $f_{T9}/\Lambda^4$

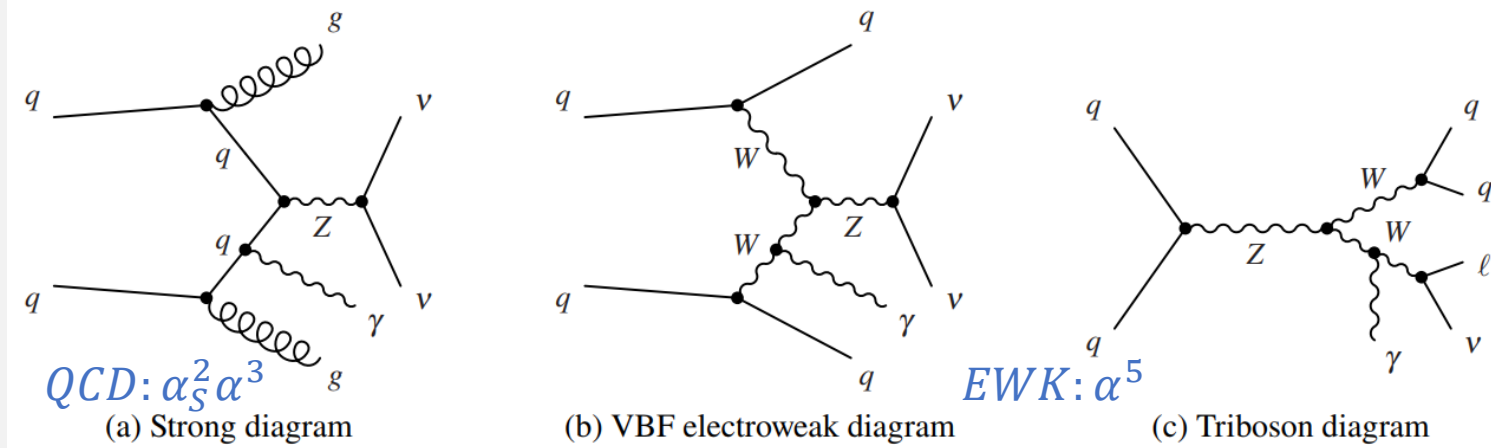
# Backups: $Z(\rightarrow ll)\gamma jj$ VBS



# ● Backups: $Z(\rightarrow ll)\gamma jj$ VBS



# Backups: EW $Z(\rightarrow \nu\nu)\gamma jj$



Process	Fake- $e$ CR	$W_{ev}^\gamma$ CR	$W_{\mu\nu}^\gamma$ CR	$Z_{Rev.Cen.}^\gamma$ CR	SR - $m_{jj}$ [TeV]			
					0.25-0.5	0.5-1.0	1.0-1.5	$\geq 1.5$
Strong $Z\gamma$ + jets	$8 \pm 8$	$0 \pm 1$	$3 \pm 2$	$50 \pm 12$	$20 \pm 6$	$54 \pm 12$	$13 \pm 5$	$5 \pm 2$
EW $Z\gamma$ + jets	$0.6 \pm 0.2$	$0.3 \pm 0.2$	$0.4 \pm 0.2$	$7 \pm 2$	$4 \pm 1$	$30 \pm 7$	$25 \pm 5$	$36 \pm 7$
Strong $W\gamma$ + jets	$43 \pm 9$	$47 \pm 9$	$133 \pm 21$	$24 \pm 6$	$22 \pm 6$	$35 \pm 10$	$9 \pm 3$	$3 \pm 1$
EW $W\gamma$ + jets	$19 \pm 6$	$31 \pm 7$	$59 \pm 13$	$1.4 \pm 0.5$	$2 \pm 1$	$6 \pm 1$	$4 \pm 1$	$5 \pm 1$
jet $\rightarrow \gamma$	$1 \pm 1$	$2 \pm 2$	$3 \pm 2$	$2 \pm 2$	$1 \pm 1$	$2 \pm 2$	$1 \pm 1$	$0.4 \pm 0.3$
jet $\rightarrow e$	$34 \pm 17$	$5 \pm 3$	–	–	–	–	–	–
$e \rightarrow \gamma$	–	$2.7 \pm 0.4$	$2.9 \pm 0.4$	$13 \pm 1$	$6 \pm 1$	$11 \pm 1$	$2.6 \pm 0.4$	$1.4 \pm 0.3$
$\gamma$ + jet	–	–	–	$0.7 \pm 0.5$	$0.7 \pm 0.5$	$0.4 \pm 0.3$	$0.1 \pm 0.1$	$0.1 \pm 0.1$
$t\bar{t}\gamma/V\gamma\gamma$	$3 \pm 1$	$9 \pm 2$	$13 \pm 2$	$3 \pm 1$	$2 \pm 1$	$4 \pm 1$	$0.4 \pm 0.2$	$0.1 \pm 0.1$
Fitted Yields	$108 \pm 10$	$96 \pm 8$	$213 \pm 14$	$102 \pm 9$	$58 \pm 6$	$143 \pm 12$	$54 \pm 5$	$52 \pm 6$
Data	108	95	216	100	52	153	50	52
Data/Fit	$1.00 \pm 0.14$	$0.99 \pm 0.12$	$1.01 \pm 0.09$	$0.98 \pm 0.13$	$0.90 \pm 0.15$	$1.07 \pm 0.11$	$0.93 \pm 0.16$	$0.99 \pm 0.18$

# Backups: EW $Z(\rightarrow \nu\nu)\gamma jj$

Process	Generator	ME Order	PDF	Parton Shower	Tune
SM process samples					
Strong $V\gamma$ + jets	SHERPA 2.2.8	NLO (up to 1-jet), LO (up to 3-jets)	NNPDF3.0NNLO	SHERPA MEPS@NLO	SHERPA
EW $V\gamma$ + jets	MADGRAPH5_AMC@NLO 2.6.5	LO	NNPDF3.1LO	PYTHIA 8.240	A14
EW $VV$ + jets	SHERPA 2.2.1 or SHERPA v2.2.2	LO	NNPDF3.0NNLO	SHERPA MEPS@NLO	SHERPA
$VV$ + jets	SHERPA 2.2.1 or SHERPA 2.2.2	NLO (up to 1-jet), LO (up to 3-jets)	NNPDF3.0NNLO	SHERPA MEPS@NLO	SHERPA
EW $V$ + jets	HERWIG 7.1.3 or HERWIG 7.2.0	NLO	MMHT2014NLO68CL	HERWIG 7.1.3	HERWIG 7
Strong $W(\rightarrow \mu\nu)$ + jets/ $W(\rightarrow \tau\nu)$ + jets	SHERPA 2.2.7	NLO (up to 2-jets), LO (up to 4-jets)	NNPDF3.0NNLO	SHERPA MEPS@NLO	SHERPA
$t\bar{t}\gamma$	MADGRAPH5_AMC@NLO 2.2.3	NLO	NNPDF2.3LO	PYTHIA 8.186	A14
$t\bar{t}/Wt$	POWHEG BOX v2	NLO	NNPDF3.0NLO	PYTHIA 8.230	A14
$V\gamma\gamma$	SHERPA 2.2.2 (at 0-jet), LO (up to 2-jets)	NLO	NNPDF3.0NNLO	SHERPA MEPS@NLO	SHERPA
$\gamma$ + jet	SHERPA 2.2.2	NLO (up to 2-jets), LO (up to 4-jets)	NNPDF3.0NNLO	SHERPA MEPS@NLO	SHERPA
Higgs-related samples					
ggF Higgs	POWHEG v2 NNLOPS	NNLO	PDF4LHC15	PYTHIA 8.230	AZNLO
Higgs + $\gamma$	MADGRAPH5_AMC@NLO 2.6.2	NLO	PDF4LHC15	HERWIG 7.1.3p1	A14
ggF Higgs $\rightarrow \gamma\gamma_d$	POWHEG v2 NNLOPS	NNLO	PDF4LHC15	PYTHIA 8.244p3	AZNLO
VBF Higgs $\rightarrow \gamma\gamma_d$	POWHEG v2	NLO	CTEQ6L1	PYTHIA 8.244p3	AZNLO
Systematic variation samples					
$V\gamma$ + jets $\alpha^4$ interference	MADGRAPH5_AMC@NLO 2.6.2	LO	NNPDF3.1LO	PYTHIA 8.240	AZNLO

# EFT results for $Z(\rightarrow \nu\nu)\gamma jj$ VBS

Unitarity is not preserved

Clipping at  $E_c$   
Unitarity is preserved

Coefficient	Observed limit, $\text{TeV}^{-4}$	Expected limit, $\text{TeV}^{-4}$
$f_{T0}/\Lambda^4$	$[-9.4, 8.4] \times 10^{-2}$	$[-1.3, 1.2] \times 10^{-1}$
● $f_{T5}/\Lambda^4$	$[-8.8, 9.9] \times 10^{-2}$	$[-1.2, 1.3] \times 10^{-1}$
● $f_{T8}/\Lambda^4$	$[-5.9, 5.9] \times 10^{-2}$	$[-8.1, 8.0] \times 10^{-2}$
● $f_{T9}/\Lambda^4$	$[-1.3, 1.3] \times 10^{-1}$	$[-1.7, 1.7] \times 10^{-1}$
$f_{M0}/\Lambda^4$	$[-4.6, 4.6]$	$[-6.2, 6.2]$
$f_{M1}/\Lambda^4$	$[-7.7, 7.7]$	$[-1.0, 1.0] \times 10^1$
$f_{M2}/\Lambda^4$	$[-1.9, 1.9]$	$[-2.6, 2.6]$

Coefficient	$E_c$ , TeV	Observed limit, $\text{TeV}^{-4}$	Expected limit, $\text{TeV}^{-4}$
$f_{T0}/\Lambda^4$	1.7	$[-8.7, 7.1] \times 10^{-1}$	$[-8.9, 7.3] \times 10^{-1}$
● $f_{T5}/\Lambda^4$	2.4	$[-3.4, 4.2] \times 10^{-1}$	$[-3.5, 4.3] \times 10^{-1}$
● $f_{T8}/\Lambda^4$	1.7	$[-5.2, 5.2] \times 10^{-1}$	$[-5.3, 5.3] \times 10^{-1}$
● $f_{T9}/\Lambda^4$	1.9	$[-7.9, 7.9] \times 10^{-1}$	$[-8.1, 8.1] \times 10^{-1}$
$f_{M0}/\Lambda^4$	0.7	$[-1.6, 1.6] \times 10^2$	$[-1.5, 1.5] \times 10^2$
$f_{M1}/\Lambda^4$	1.0	$[-1.6, 1.5] \times 10^2$	$[-1.4, 1.4] \times 10^2$
$f_{M2}/\Lambda^4$	1.0	$[-3.3, 3.2] \times 10^1$	$[-3.0, 3.0] \times 10^1$

$E_T^Y > 600\text{GeV}$  for  $E_c < 4\text{TeV}$ ;  $E_T^Y > 900\text{GeV}$  for  $E_c > 4\text{TeV}$

