Dual-readout calorimetry with segmented crystals

4th FCC Physics and Experiments Workshop

12/11/20

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To optimize integration with a dual-readout hadron calorimeter and maintain excellent hadron resolution

To enhance particle identification capabilities and provide more handles for particle flow algorithms

Long history of pushing the frontier on high-resolution electromagnetic calorimetry for photons and electrons (and more recently also on time resolution!)

N

Overview of the talk

Motivation

- Precision measurements and search for new physics at e⁺e⁻ colliders would benefit from a detector with the highest energy resolution, segmentation and particle ID capabilities
- Typical EM resolution target for e⁺e⁻ detectors rather modest [~20%/√E] may not allow to fully exploit the potential of precise photon measurements (π^0 clustering, Brem recovery, B physics, ...) → see also "Use cases for an extreme electromagnetic resolution" by R. Aleksen

Detector concept

- Optimization of a hybrid segmented calorimeter concept achieving the highest resolution for both photons [\sim 3%/ \sqrt{E}] and neutral hadrons [<30%/√E]
- Include potential for detection of MIPs and EM showers with time resolution better than 20 ps

Approach

- Exploit technological developments to implement dual readout **capabilities** and achieve a working solution for the problem of crystals destroying hadronic calorimeter resolution
- Overall cost-performance optimization of the calorimeter design

Many more details about this talk in: https://doi.org/10.1088/1748-0221/15/11/P11005



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New perspectives on segmented crystal calorimeters for future colliders

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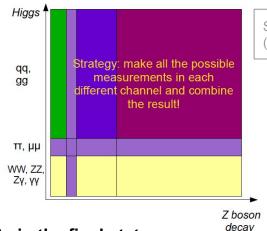
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ABSTRACT: Crystal calorimeters have a long history of pushing the frontier on high-resolution electromagnetic (EM) calorimetry for photons and electrons. We explore in this paper major innovations in collider detector performance that can be achieved with crystal calorimetry when longitudinal segmentation and dual-readout capabilities are combined with a new high EM resolution approach to Particle Flow in multi-jet events, such as $e^+e^+ \to HZ$ events in all-hadronic final-states at Higgs factories. We demonstrate a new technique for pre-processing π^0 momenta through combinatoric di-photon pairing in advance of applying jet algorithms. This procedure significantly reduces π^0 photon splitting across jets in multi-jet events. The correct photon-to-jet assignment efficiency improves by a factor of about 3 when the EM resolution is improved from 15 to $3\%/\sqrt{E}$. In addition, the technique of bremsstrahlung photon recovery significantly improves electron momentum measurements. A high EM resolution calorimeter increases the Z boson recoil mass resolution in Higgstrahlung events for decays into electron pairs to 80% of that for muon pairs. We present the design and optimization of a highly segmented crystal detector concept that achieves the required energy resolution of $3\%/\sqrt{E}$, and a time resolution better than 30 ps providing exceptional particle identification capabilities. We demonstrate that, contrary to previous detector designs that suffered from large neutral hadron resolution degradation from one interaction length of crystals in front of a sampling hadron calorimeter, the implementation of dual-readout on crystals permits to achieve a resolution better than $30\%/\sqrt{E} \oplus 2\%$ for neutral hadrons. Our studies find that the integration of crystal calorimetry into future Higgs factory collider detectors can open new perspectives by yielding the highest level of combined EM and neutral hadron resolution in the PFA paradigm.

Final States of e⁺e⁻ Higgs Physics @~246 GeV

- SM Higgs
 - **0 jets: 3%:** Z→II, νν (30%); H→0 jets (~10%, ττ, μμ, γγ, γZ/WW/ZZ→leptonic)
 - 2 jets: 32%
 - $Z \rightarrow qq$, $H \rightarrow 0$ jets. 70%*10% = 7%
 - $Z \rightarrow II$, vv; $H \rightarrow 2$ jets. 30%*70% = 21%
 - Z→II, vv; H→WW/ZZ→semi-leptonic. 3.6%
 - 4 jets: 55%
 - $Z \rightarrow qq$, $H \rightarrow 2$ jets. 70%*70% = 49%
 - $Z \rightarrow II$, vv: $H \rightarrow WW/ZZ \rightarrow 4$ jets. 30%*15% = 4.5%
 - 6 jets: 11%
 - Z→qq, H→WW/ZZ→4 jets. 70%*15% = 11%



Final state

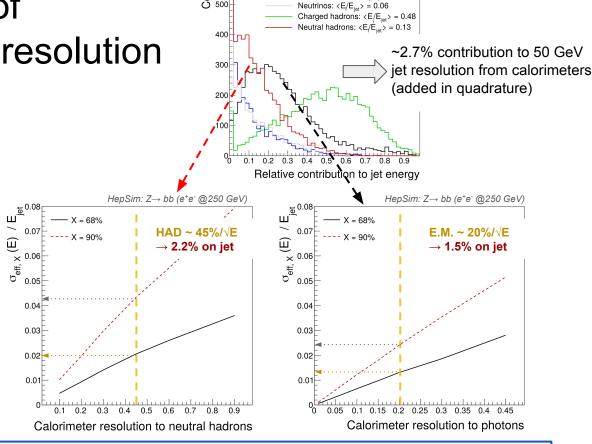
Slide borrowed from Manqi Ruan (LCWS 2019, Sendai, Japan)

- 97% of the SM Higgsstrahlung signal has jets in the final state
 - 1/3 has only 2 jets
 - 2/3 need color-single identification (grouping the hadronic final state particles into color-singlets)

Jet resolution is a key benchmark for e⁺e⁻ detectors performance

Traditional impact of calorimeters on jet resolution

- Baseline jet performance depends on particle composition and the relevant sub-detector resolutions
- Calorimeter resolution on neutral particles required to achieve target jet resolution of ~3%
 - Photons
 better than 20%/√E
 - Neutral hadrons
 (mostly K^{0,L} of <E>~5 GeV) better
 than 45%/√E



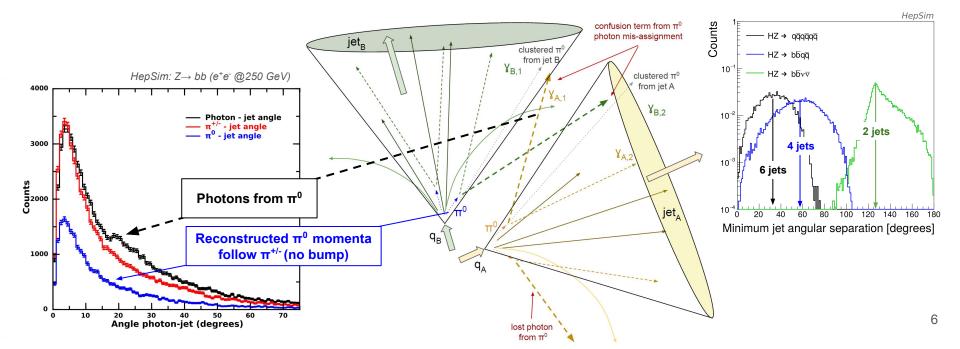
HepSim

Photons: $\langle E/E_{jet} \rangle = 0.27$ Charged leptons: $\langle E/E_{int} \rangle = 0.06$

But the role of calorimeters in jet reconstruction spans beyond the direct impact on energy resolution...

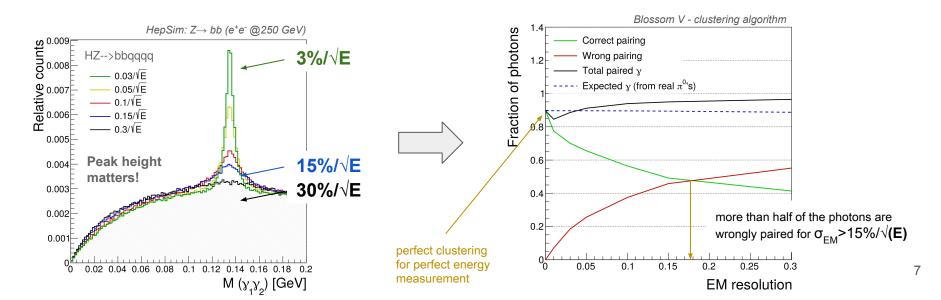
High photon resolution potential for PFA

- Many photons from π^0 decay are emitted at a ~20-35° angle wrt to the jet momentum and can get scrambled across neighboring jets
- Effect particularly pronounced in 4 and 6 jets topologies



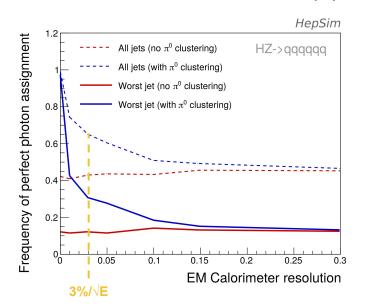
A graph-based algorithm for π⁰ clustering

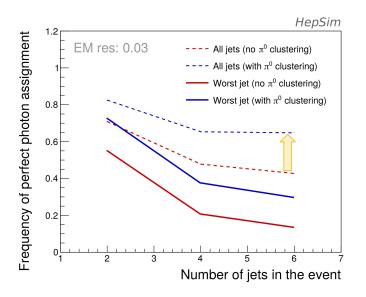
- A high EM resolution enables efficient clustering of photons from π^0 's
 - \circ Large fraction of π^0 photons correctly clustered with good σ_{FM}
 - \rightarrow ~90% for ~3%/ $\sqrt{(E)}$ vs 50% for ~30%/ $\sqrt{(E)}$
 - \sim Large fraction of "**fake \pi^0's**"reconstructed with poor σ_{FM}
 - \rightarrow ~50% for ~30%/ $\sqrt{(E)}$ vs 10% with ~3%/ $\sqrt{(E)}$



Improvements in photon-to-jet correct assignment

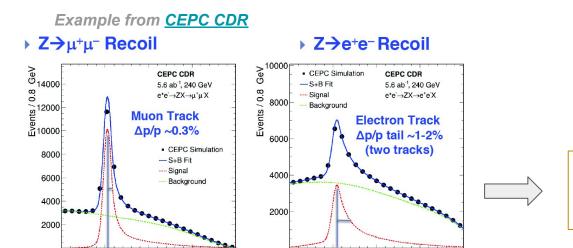
- **High e.m. resolution enables** photons **clustering into \pi^0's** by reducing their angular spread with respect to the corresponding jet momentum
- Improvements in the fraction of photons correctly clustered to a jet sizable only for e.m. resolutions of $\sim 3\%/\sqrt{(E)}$





Recovery of Bremsstrahlung photons

- Reconstruction of the Higgs boson mass and width from the recoil mass of the Z boson is a key tool at e⁺e⁻ colliders
- Potential to improve the resolution of the recoil mass signal from Z→ee decays to about 80% of that from Z→ µµ decays [with Brem photon recovery at EM resolution of 3%/√E]



120

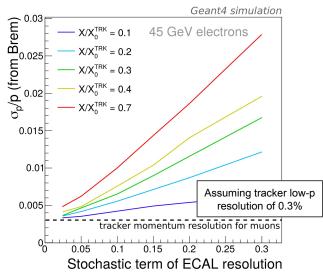
125

130

135 14 MRecoil [GeV]

125

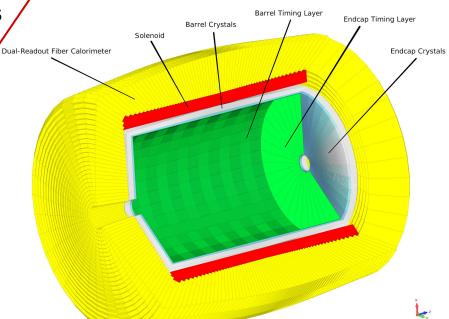
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~80% of resolution recovery with $3\%/\sqrt{(E)}$

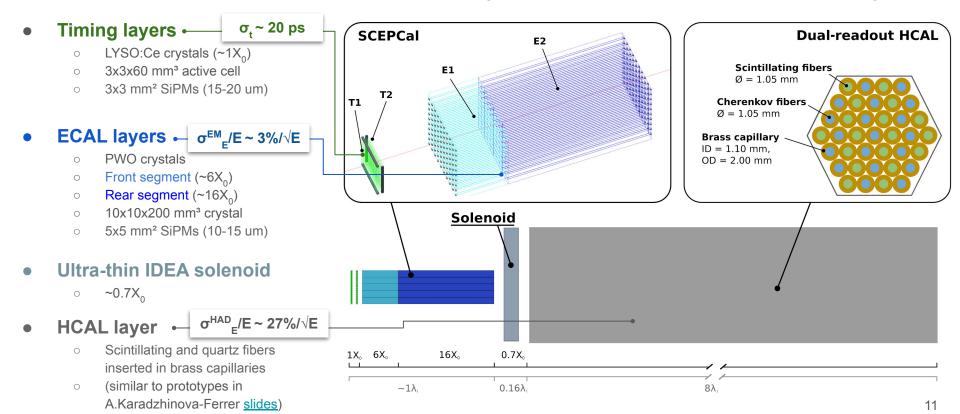
The combination of a **segmented crystal high precision EM calorimeter** (*SCEPCal*) **with a dual-readout hadron calorimeter**would be *IDEAL* to take up the challenge
of precision physics at future e⁺e⁻ colliders

- Design optimization of a segmented crystal ECAL
- Effective integration with a dual-readout HCAL
- Global cost-performance optimization



Layout overview

- Transverse and longitudinal segmentations optimized for particle identification and particle flow algorithms
- Exploiting SiPM readout for contained cost and power budget



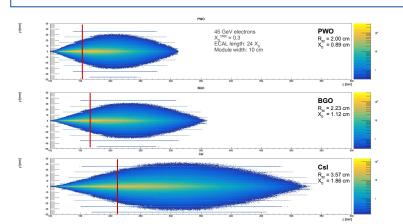
Some crystal options

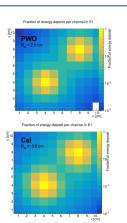
- PWO: the most compact, the fastest, the cheapest
- BGO/BSO: in between (potential for dual-readout)
- Csl: the less compact, the slowest, the brightest

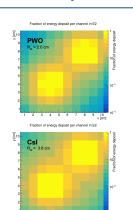


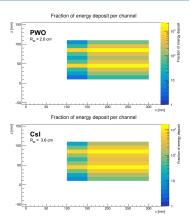
Crystal	Density g/cm³	λ _i cm	X ₀ cm	R _M cm	Relative LY @ RT	Decay time ns	Photon density (LY / $\tau_{\rm D}$) ph/ns	dLY/dT (% / °C)	Cost (10 m³) Est. \$/cm³	Cost*X ₀ Est. \$/cm ²
PWO	8.3	20.9	0.89	2.00	1	10	0.10	-2.5	8	7.1
BGO	7.1	22.7	1.12	2.23	70	300	0.23	-0.9	7	7.8
BSO	6.8	23.4	1.15	2.33	14	100	0.14		6.8	7.8
Csl	4.5	39.3	1.86	3.57	550	1220	0.45	+0.4	4.3	8.0

Working with the Crystal Clear Collaboration at CERN to evaluate crystal candidates for DRO





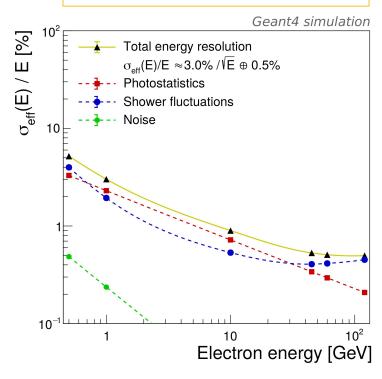




Energy resolution for **EM particles**

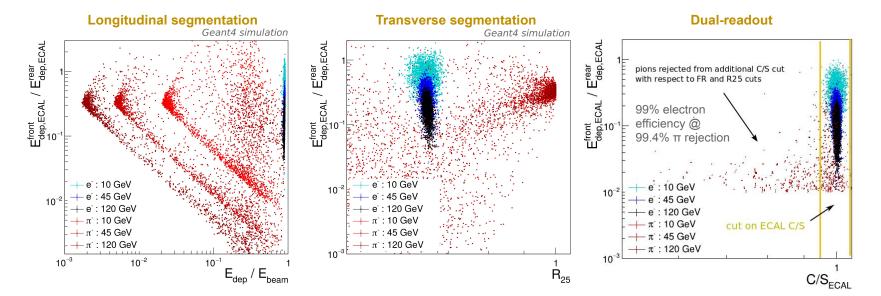
- Contributions to energy resolution:
 - Shower fluctuations
 - Longitudinal leakage
 - Tracker material budget
 - Services for front layers readout
 - Photostatistics
 - Tunable parameter depending on:
 - SiPM choice
 - Crystal choice
 - Noise
 - Negligible with SiPMs
 - High gain devices (~10⁵)
 - Small dark count rate within signal integration time window





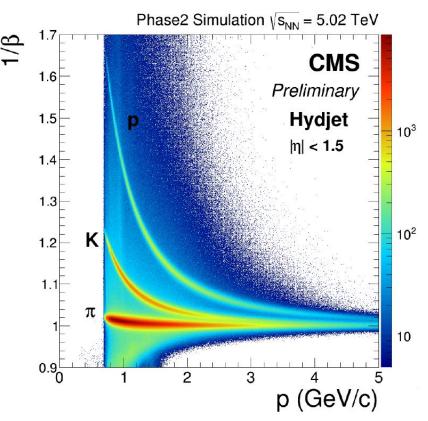
Particle ID with crystal segmentation

- Topology of longitudinal/transverse energy deposits in crystals provides a clear e^{+/-}/π^{+/-} discrimination→better than 99% electron efficiency at 99% pion rejection (with simple cuts)
- Large potential for improvement with the addition of dual-readout information and use of more sophisticated pattern recognition algorithm



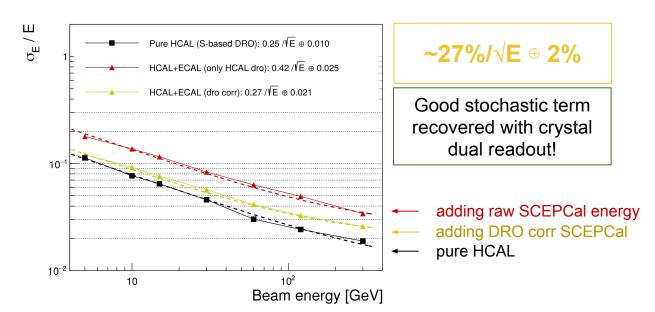
Particle ID with time-of-flight

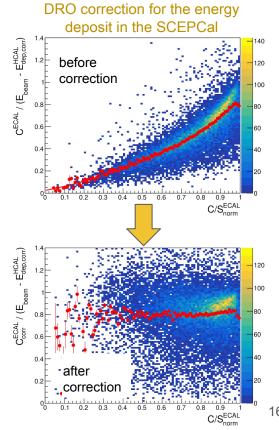
- Crystals can provide excellent time-of-flight capabilities for particle identification:
 - Time tagging of MIPs with ~30 ps
 time resolution with single layer
 - See <u>MTD in CMS Phase 2 upgrade</u>
 - Time resolution of 30 ps to e.m.
 showers with E >20 GeV
 with the ECAL (rear) segment(s)
 - See <u>Phase 2 CMS ECAL Upgrade</u>



Energy resolution for neutral hadrons

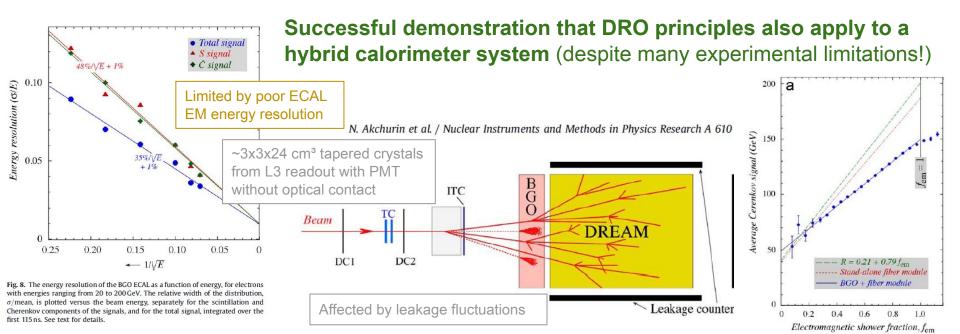
- 1. Correct the energy deposit in the HCAL with DRO
- 2. Correct the energy deposit in the SCEPCal with DRO
- Calibrated sum of SCEPCal+HCAL





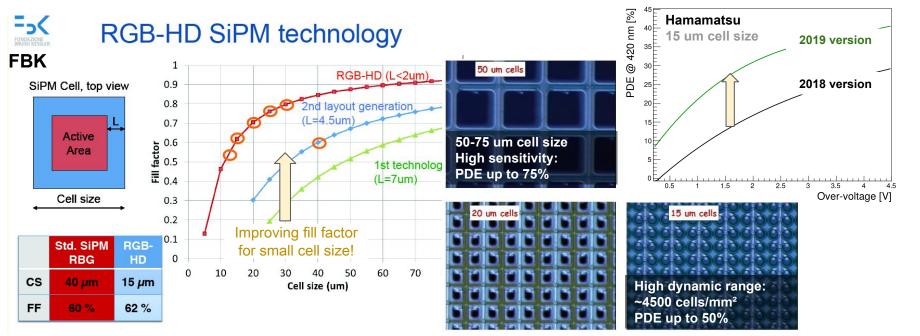
Implementing dual readout in crystals

 First test of combination of a DRO crystal ECAL with DREAM HCAL back in 2009 with BGO modules (N.Ackurin et al., NIM A 610 (2009) 488-501)



Technological advancements (SiPMs)

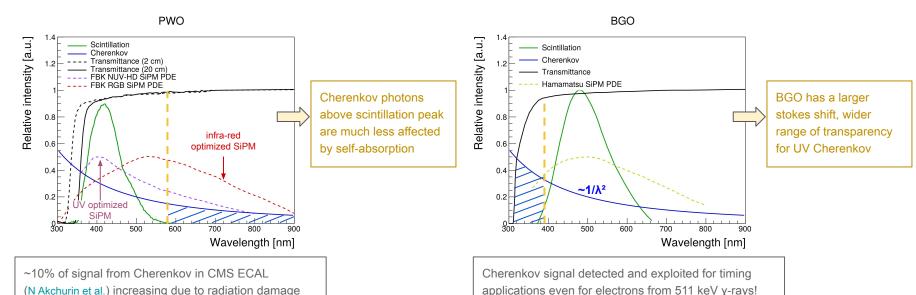
- Many technological advancements in the field of photodetectors
- Compact and robust SiPMs with small cell size and fast recharge time (~4 ns)
 extending the dynamic range and enhancing sensitivity in a wide range of wavelengths



Cherenkov detection in PWO and BGO

that filters out the UV scintillation component!

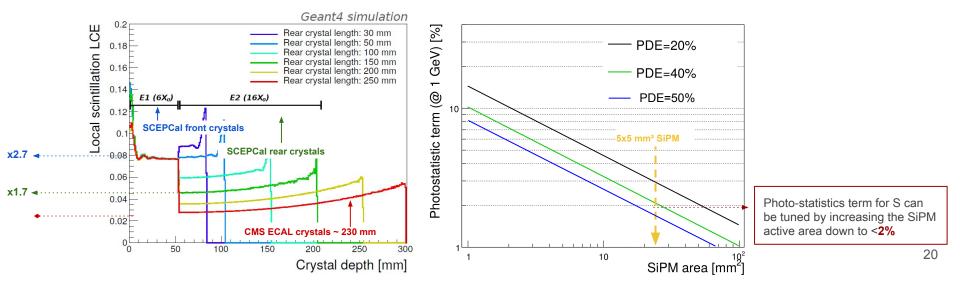
- Sensitivity in both the UV and infrared region with Silicon Photomultipliers
- At least two crystal candidates for a compact, cost-contained ECAL with DRO capabilities:
 - Detect Cherenkov photons in either the UV (BGO) or infrared region (PWO)
 - Ongoing laboratory measurement at CERN Lab27 to validate simulation (Crystal Clear RD18)



Stefan Gundacker et al., 2020 Phys. Med. Biol.65 025001

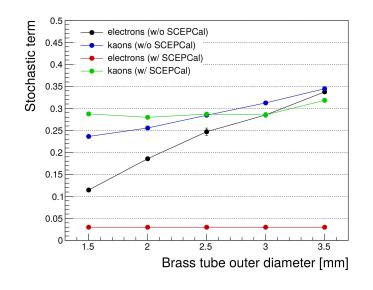
SCEPCal key features for **DRO optimization**

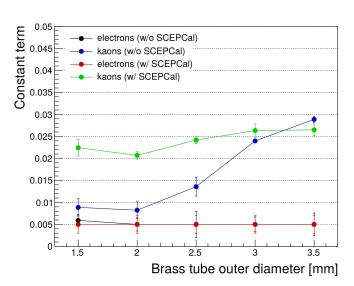
- **High granularity increases light collection efficiency** (both C and S)
 - 1 cm² cross section compared to ~ 3 cm² in L3/CMS and crystal length reduced by ~2x
- SiPM active area can be tuned to achieve target resolution (stoch. term)
 - Light collection efficiency increasing linearly with SiPM area
- SiPM with smaller dynamic range but high PDE can be selected for C-detection



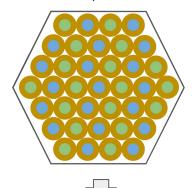
Cost/performance optimization of HCAL segment

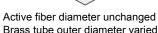
- Brass tube outer diameter (OD) can be increased to 3/3.5 mm with marginal impact on the hadron resolution
- Relative channel reduction and cost decrease approximately with $\sim 1/\Omega D^2$





Brass capillaries "Nominal" dimension OD=2 mm, ID=1.1 mm









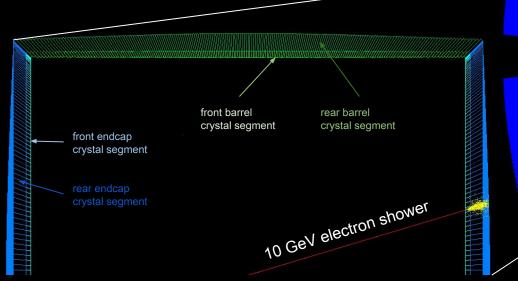
1.5 mm

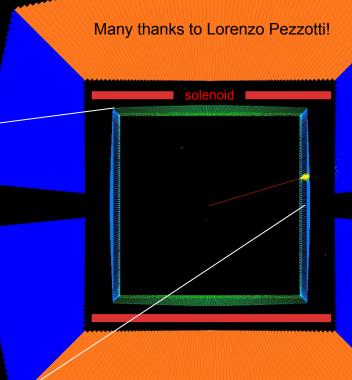


3.5 mm

Ongoing integration in 4π Geant4 IDEA simulation

- Preliminary pointing geometry
- About 1M channels in total (~1 cm² crystals)
- Use of replicas and parameterised volumes to optimize computational time



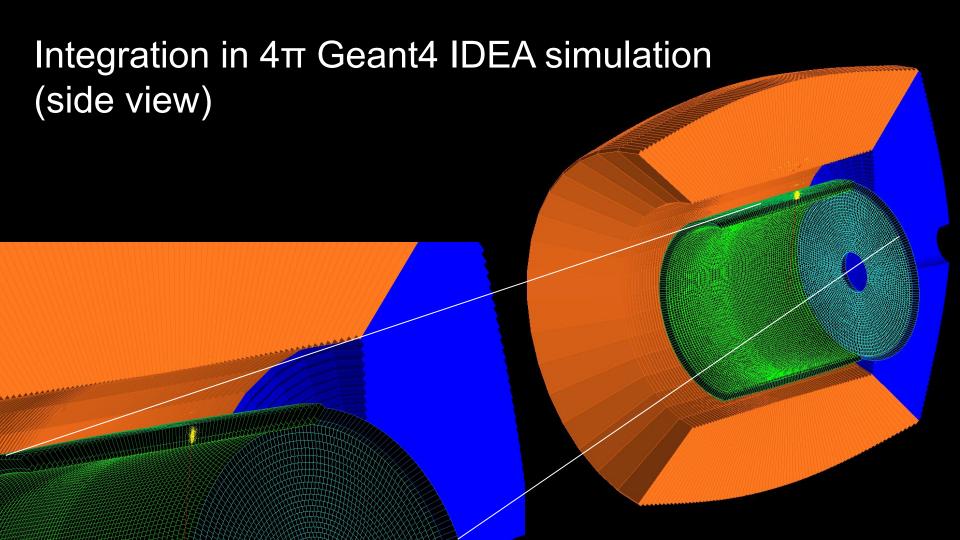


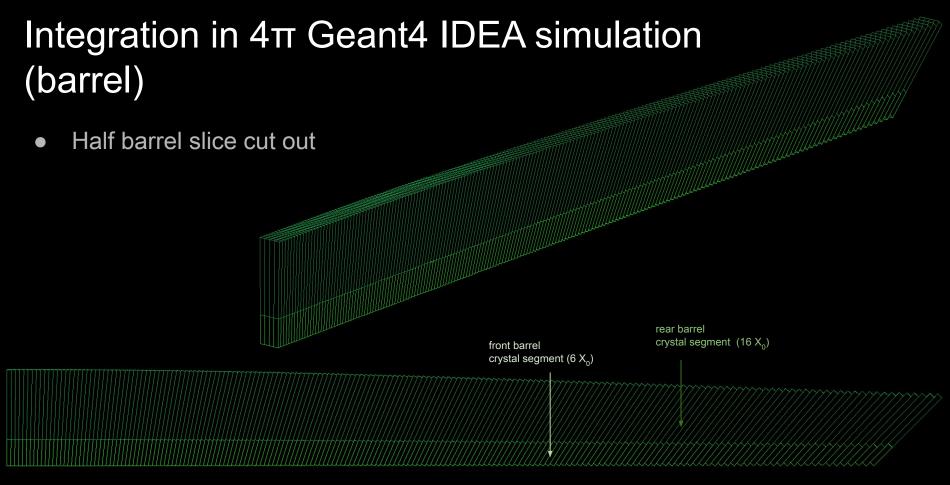
Summary

- Highlights of a segmented crystal option for the IDEA detector:
 - Excellent DRO hadron calorimetry better than ~30%/√E is maintained with a segmented crystal EM calorimeter in front of the thin solenoid in the IDEA detector
 - Addition of ~3%/ \sqrt{E} EM resolution for photons and brem recovery for electrons ($Z\rightarrow ee$ recoil)
 - **Efficient pre-clustering of pizero photons**, improves the correct photon-to-jet assignment especially in 4 and 6 jets event topologies
- Optimization of DRO capabilities:
 - Rapid technological advancements in SiPMs and the use of a segmented crystal geometry ease a cost effective implementation of dual-readout in crystals
- Combination of a DRO ECAL with a DRO HCAL allows for a global optimization of each calorimeter compartment in terms of channel count, readout and cost

Additional slides

More on 4π geometry integration

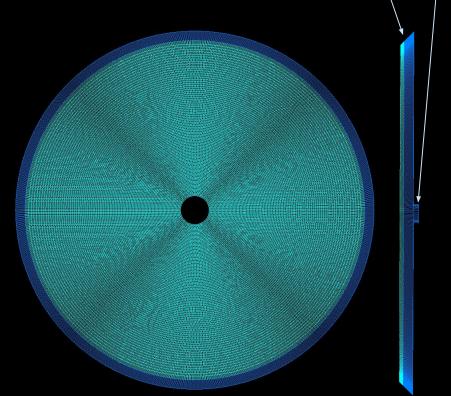




Integration in 4π Geant4 IDEA simulation (endcap)

Concentric pointing rings

 Each ring divided in replicas to yield similar crystal dimensions



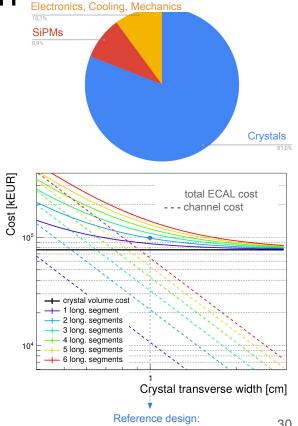
inner ring

outer ring

More on cost/performance optimization

Cost-power drivers and optimization

- Channel count in SCEPCal is limited to ~2.5M
 - 625k channels/layer (2 "timing layers" + "ECAL layers")
- Cost drivers in **ECAL** layers (tot ~95M€):
 - ~81% crystals, 9% SiPMs, 10% (electronics+cooling+mechanics)
 - ~19% of cost scales with channel count
- Power budget driven by electronics: ~74 kW
 - 18.5 kW/layer
- Room for fine tuning of the segmentation and of the detector performance/cost optimization (see backup)



1 cm², 2 segments cost ~ 95M€

Detector **cost** drivers

Crystal options

- LYSO:Ce for timing layer (optimal choice for the CMS MTD)
- PWO (very compact CMS and PANDA ECALs preferred choice)
- Many other crystals on the market may allow further optimization

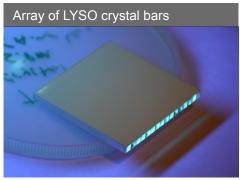
Crystal costs used as reference

- Quotes from crystal vendors
 - **PWO:** ~7€ /cc (for 10 m³, cut and polished)
 - LYSO: ~30€ /cc (for cut, polished and wrapped elements)

SiPMs

- Recent estimates from CMS Upgrade experience:
 - ~6€/SiPM (9x9 mm² active area)
 - can embed a LED for monitoring: additional ~1€/channel
- Cost constantly dropping and technology improving in the last decade
 - can aim at a factor ~2-4 reduction in the next decade





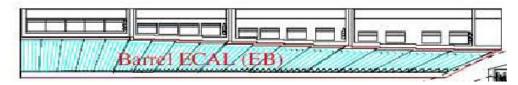
Cost and power breakdowns for SCEPCal

	T1+T2 (TIMING)	E1+E2 (ECAL)		
Area barrel	53	53		
Area endcap	19	19		
Total area (barrel+endcaps)	72 m²	72 m²		
# Channels barrel	977k	859k		
# Channels endcaps	344k	374k		
Total # of channels (barrel + endcaps)	1.3 M	1.2 M		
Crystal cost	10 M€	78 M€		
SiPM cost (+monitoring for ECAL only)	8 M€	8.5 M€		
Electronics cost	5 M€	4.5 M€		
Cooling+power+mechanics cost	5 M€	5 M€		
Sub-total cost (barrel+endcaps)	28 M€	96 M€		
Total cost (barrel+endcaps)	~124 M€			

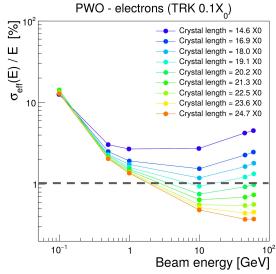
	T1+T2 (TIMING)	E1+E2 (ECAL)		
# of readout channels	~1.3M	~1.2M		
SiPMs (kW)	2.7	2.5		
Electronics (kW)	34.3	33.5		
Sub-total (kW)	38	36		
Total (kW)	~74 kW			

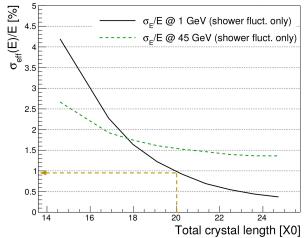
Optimization of crystal volume

- Crystal pointing geometry
 - →reduce by ~20% crystal volume and channel count



- Optimizing crystal length vs energy resolution
 - with 20 X₀ contribution to constant term from shower
 leakage comparable to intercalibration precision: O(1%)
 - no substantial impact on stochastic component (negligible wrt photo-statistics term of ~4-5%)



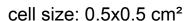


Transverse segmentation (visual impact) cell size: 2x2 cm²

Fraction of energy deposit per channel in E2

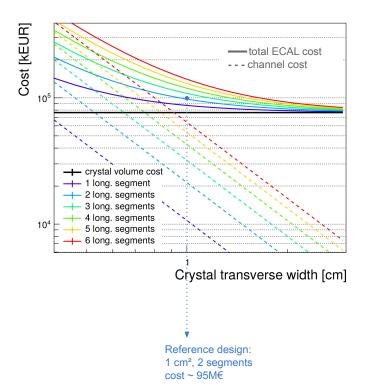
Fraction of energy deposit per channel in E1

cell size: 1x1 cm²



Optimization of segmentation

- Segmentation optimized for performance/cost:
 - Transverse segmentation:
 - \rightarrow 1 cm ~ R_M / 2 (half Molière radius)
 - Longitudinal segmentation: 2 segments
 - →particle ID with no dead material at shower max
 - →simple for readout and services (front and rear)
- Impact of ch. count on overall detector cost <20% for baseline segmentation choice
- Total cost ~ 95 M€



More on dual-readout implementation

DRO in the rear SCEPCal segment only

- Majority of the energy deposit from hadron is in the rear ECAL section
- Dual readout can be implemented in the rear section only
 - No degradation in performance wrt a full (front+rear) DRO ECAL
 - +50% in channel count wrt to non-DRO ECAL can be mitigated by decreasing granularity in the rear compartment where shower radius is larger

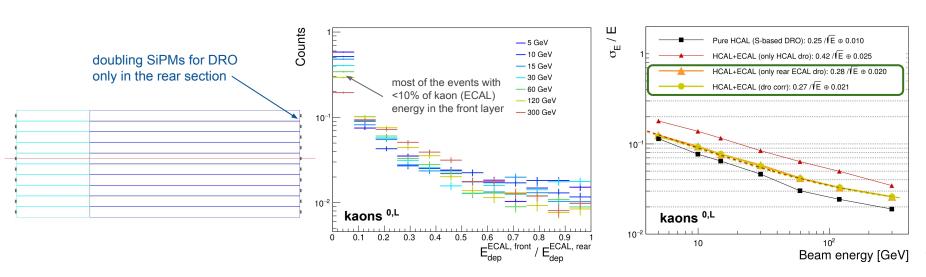
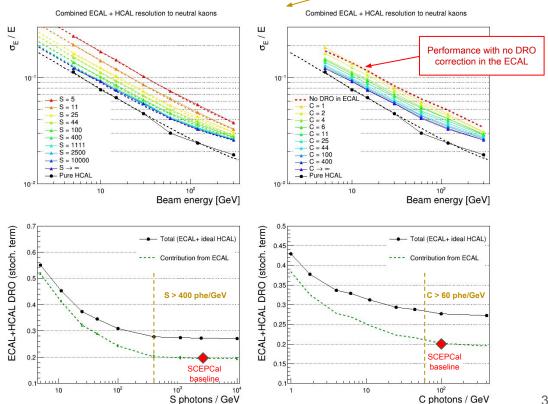


Photo-statistic requirements for S and C

Smearing according to Poisson statistics

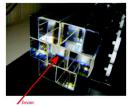
- Poor S directly impact the ECAL resolution stochastic term (even without DRO):
 - S > 400 phe/GeV to limit the contribution to HCAL stoch. term below 20%
- A limited resolution to C
 (photostatistics) impacts the C/S
 and thus the precision of the
 event-by-event DRO correction
 - C > 60 phe/GeV to limit the contribution to HCAL stoch. term below 20%



Validation of Geant4 ray-tracing simulation

- Geant4 simulation for ray-tracing of Cherenkov photons validated
- Reproducing experimental results from test beam

(thanks to G.Gaudio for help in retrieving details of the setup!)

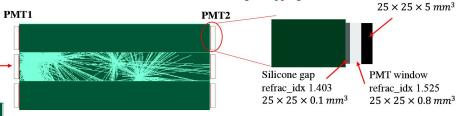


g. 2. The PWO matrix consisted of seven crystals with dimensions of c 3 × 20 cm³. These were arranged as shown in the figure and the beam entered e matrix in the central crystal. All crystals were individually wrapped in minized mylar. Both the unstream and downstream end facts were covered.

F. Bedeschi, G. Gaudio, et al. https://www.sciencedirect.com/science/article/pii/S0168900212014520

Geometry and material description in the paper

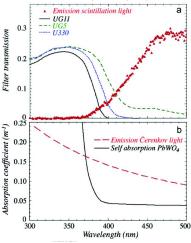
- > 7 crystals with dimensions of $30 \times 30 \times 200 \ mm^3$
- All crystals were individually wrapped in aluminized mylar.
- Hamamatsu R8900-100 tubes
- Both the upstream and downstream end faces of the matrix were covered with a large optical transmission filter (U330 or UG5)
- Silicone cookies were used to reduce the light trapping effect



PMT

- Crystal wrapped with aluminum sheet of 0.985 reflectivity
- > 0.1 mm silicone gap between crystal and PMT Borosilicate glass window
- Interface between gap and PMT window is set as the filter
- PMT surface is set as sensitive

Simulation of optical filters and PWO optical properties

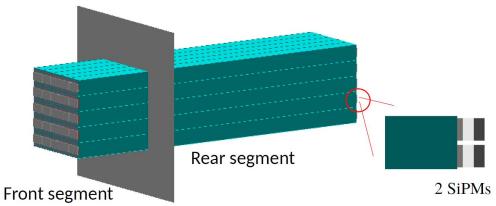


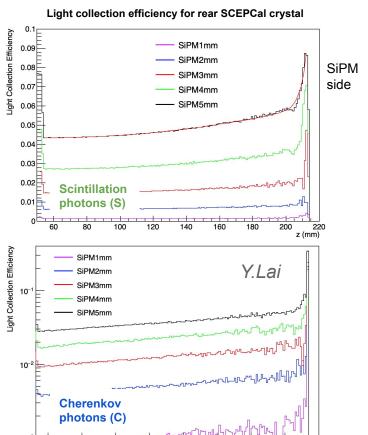
MC to data comparison: simulation predicting ~40% more Cherenkov photons (fine tuning ongoing)

3 3 3,						
	Detected photons (50 GeV e-)		Number in paper (50 GeV e-)			
Filters	Upstream	downstream				
No filter /No filter	9950	14860				
No filter/U330	9146	781				
No filter/UG5	9199	1278				
U330/U330	517	774	650			
U330/UG5	513	1246	1250			

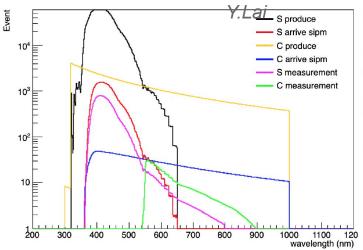
Ray-tracing in the SCEPCal

- Study impact of various parameters on light collection efficiency for both S and C:
 - LCE grows linearly with SiPM active area
 - LCE grows with shorter crystals





Fraction of S and C photons detected with dual SiPM



- RGB and UV SiPM are used to detect Cherenkov and scintillation photons
- All the photons detected by UV SiPM are considered as S
- The 550nm filter is added to RGB SiPM, so only photons with wavelength > 550nm could be detected. In this region, C is dominant
- The left plot shows spectrum of S and C when they are produced, arrived at the end and collected by SiPM
- The number of photons at different stages are shown in the table below, but it is a rough estimate, as the scintillation spectrum we are using is clearly rough up when wavelengths > 550nm.

Table 2. Photon yield for both Cherenkov and scintillation light in response to a 45 GeV electron shower in the rear SCEPCal segment assuming a $PbWO_4$ crystal and the SiPM spectral sensitivity shown in Figure 24 (left).

	Scintillation	f_S	Cherenkov	f_C
	[photons/GeV]	[%]	[photons/GeV]	[%]
Generated	200000	100	56000	100
Collected	10000	5.0	2130	3.8
Detected by NUV SiPM #1 (λ < 550 nm)	2000	1.0	140	0.25
Detected by RGB SiPM #2 ($\lambda > 550 \text{ nm}$)	< 20	< 0.01	160	0.3

Increase of C/S ratio in irradiated PWO crystals

An example of high wavelength Cherenkov detection

- Radiation damage in PWO crystals filtering out the scintillation and enhancing the relative contribution of C photon (with lambda>500 nm) to the signal
- Pulse shapes also get faster

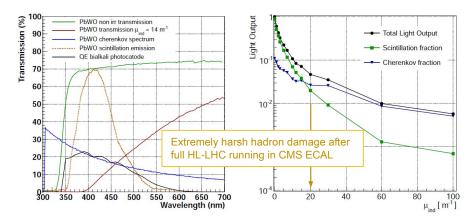
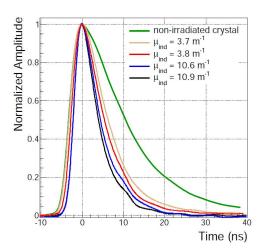


Figure 4.5: Left: wavelength dependence of Cherenkov and scintillation light compared with the transmission of hadron damaged crystals and the quantum efficiency (QE) of the photodetector. Right: contribution of scintillation and Cherenkov signal to the total light output at different μ_{ind} .

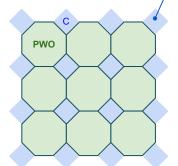


Dedicated **C-sensitive elements** (option)

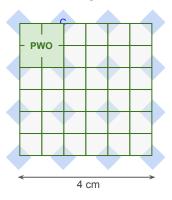
- A 'honeycomb' structure for the rear crystal section
 - Pure Cherenkov radiators nested with scintillating crystals
 - C and S elements individually readout with SiPMs
 - Size of C-element can be optimized to achieve good C "sampling"
- Front SCEPCal segment unchanged:
 - Pure S-crystal with 1 cm² → no projective cracks
- Reduce transverse segmentation in the rear segment by using octagonal (~1 cm side) crystals
 - Shower radius is larger in the rear section (less segmentation needed)
 - Total SCEPCal channel count reduced by ~25%



rear segment

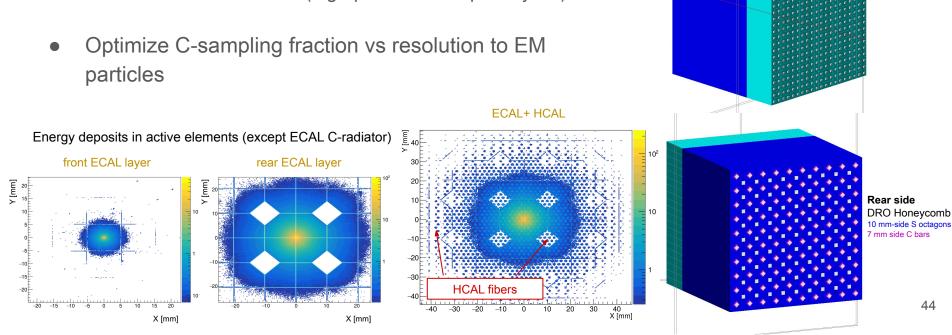


front segment



C-only DRO optimization (work in progress)

- Design under optimization
 - Tuning granularity and dimensions of C sensitive material
 - Choice of C-radiator (e.g. quartz vs undoped crystal)



Front side Pure S

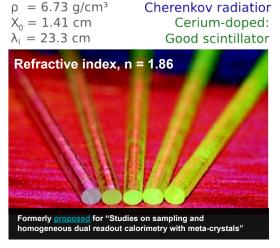
1 cm² granularity

Crystal based Spaghetti Calorimeters

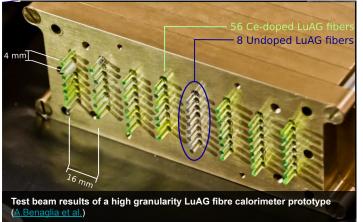
- Technology wise, a lot of progress in high granularity crystal calorimeters
 - New materials and new production processes

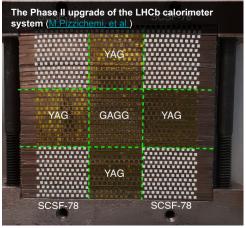
Undoped:

- Undoped LuAG crystals as excellent cherenkov radiators
- Crystal based SPACAL being studied for LHCb HL-LHC upgrade



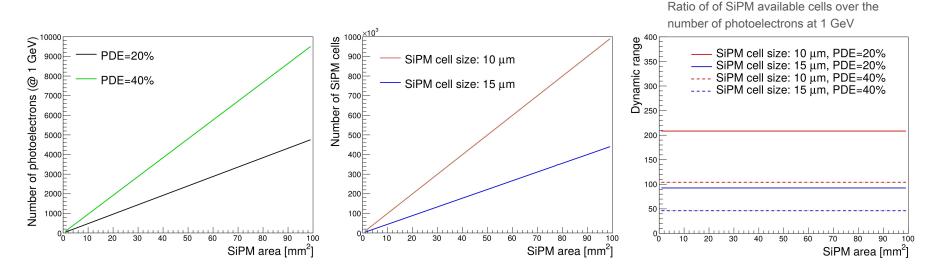
Lu₃Al₅O₁₂





Dynamic range with SiPMs

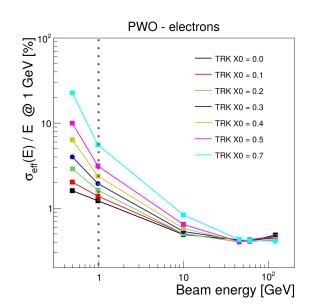
- 15 um cell pitch has high PDE (up to 50%) → optimal for T1 and T2 (timing)
- 10 um cell pitch has larger dynamic range → possibly better for E1, E2 (ECAL)

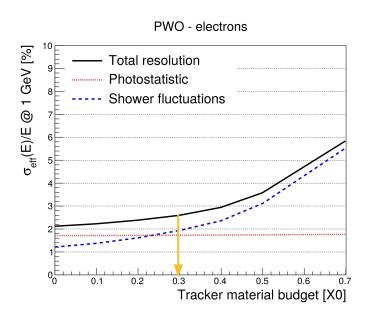


More on ECAL and HCAL performance simulation

Impact of tracker and dead material budget

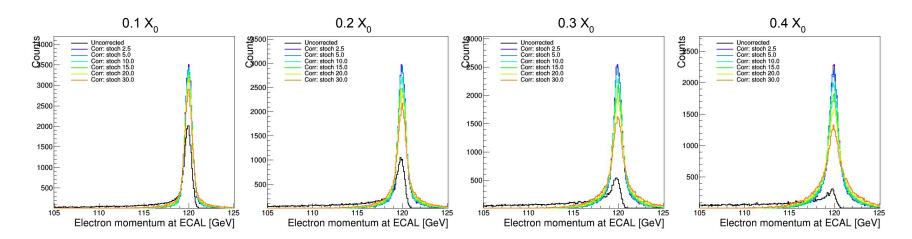
- Tracker material budget <0.3X₀ for <2% impact on stoch. term
 - Well within the target of the CEPC and IDEA reference tracker designs
- Dead material for services <0.3X₀ for impact on stoch. term < 2%
 - Compatible with estimated material budget from cooling (5 mm Al plate)
 and readout electronics





Recovery of Bremsstrahlung photons (1)

- Electron momentum at the entrance of ECAL smeared by 0.3 %
- 120 GeV electrons
- Adding back brem photons with ECAL resolution



Recovery of Bremsstrahlung photons (2)

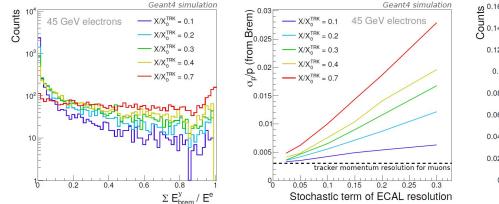


Figure 3. Left: fraction of the total energy lost by 45 GeV electrons through bremsstrahlung radiation within the tracker volume (before reaching the calorimeter) for different scenarios of tracker material budget. Right: contribution to the resolution of the electron momentum at vertex due to bremsstrahlung assuming the energy of photons emitted within the tracker volume are measured by calorimeter with a certain stochastic term of energy resolution.

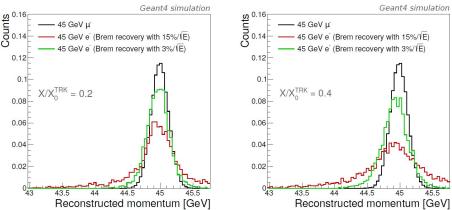
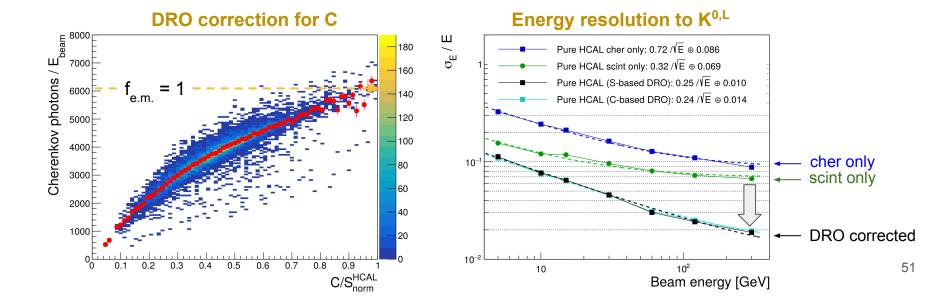


Figure 4. Distributions of the reconstructed momentum for muons (assuming a tracker momentum resolution of 0.3%) and for electrons assuming recovery of bremsstrahlung photons with an energy resolution of $15\%/\sqrt{E}$ and $3\%/\sqrt{E}$. Two scenarios are shown: assuming a tracker material budget equivalent to 0.2 X_0 (left) and $0.4 X_0$ (right).

Geant4 simulation

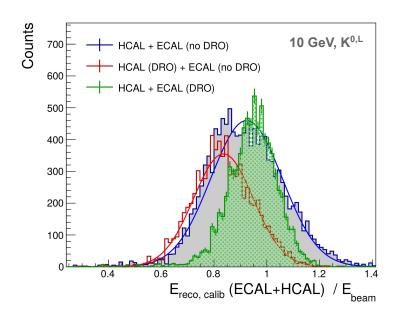
Performance of the dual readout HCAL only

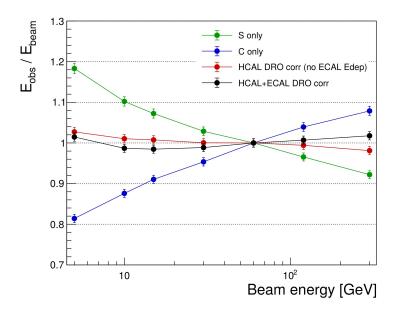
- Performance studied by selecting events with hadrons that do not interact in the crystal
- Dual readout correction works as expected
 - Energy resolution of ~25%/√E ⊕ 1% to hadrons
 - Linearity and gaussian distributions restored



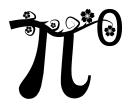
Linearity (SCEPCal + DRO HCAL)

Gaussian distributions and response linearity restored





Maximum weight matching via Blossom V algorithm for π^0 reconstruction in multi-jet events



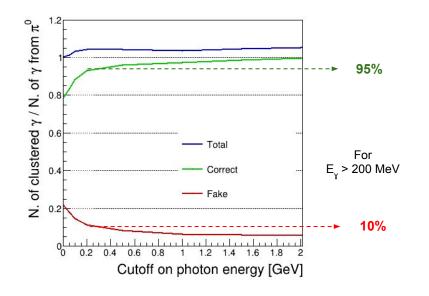
Algorithm

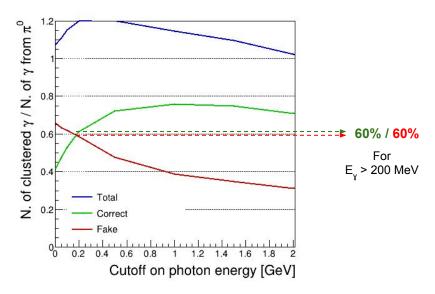


- <u>max_weight_matching</u> (G, maxcardinality=False, weight='weight')
- Compute a maximum-weighted matching of G.
 - o A matching is a subset of edges in which no node occurs more than once.
 - The weight of a matching is the sum of the weights of its edges.
 - A maximal matching cannot add more edges and still be a matching.
 - The cardinality of a matching is the number of matched edges.
- If G has edges with weight attributes the edge data are used as weight values else the weights are assumed to be 1.
- This function takes time O(number_of_nodes ** 3).
- This method is based on the "blossom" method for finding augmenting paths and the "primal-dual" method for finding a matching of maximum weight, both methods invented by Jack Edmonds [1].

Algo performance vs photon energy cut (results)

• Close to 100% of π^0 's with both photons with energy >200 MeV correctly reconstructed with 3%/ $\sqrt(E)$ resolution

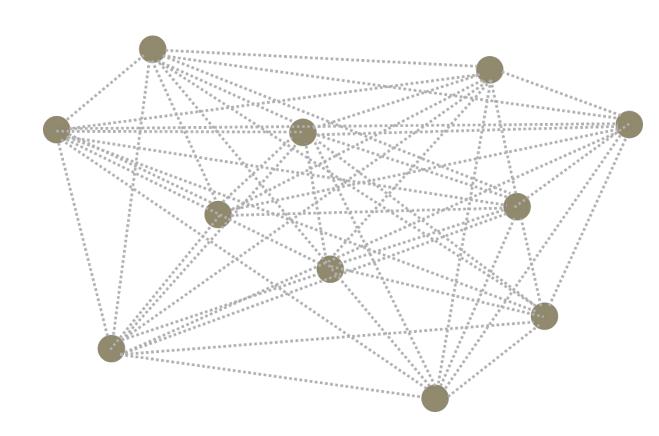




Building graph

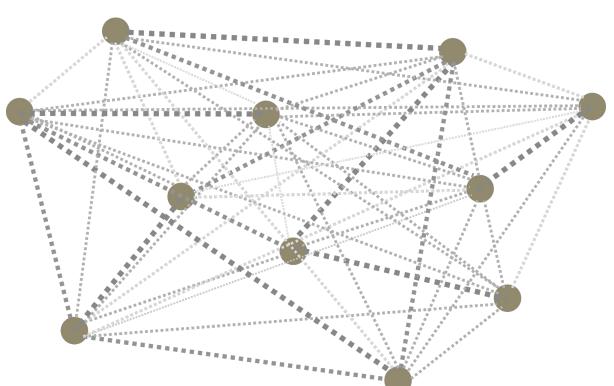
- **node** = photon
- edge = pair of photons

- node properties
 - o px, py, pz, E
- edge properties
 - invariant mass
 - boost
 - o angle



Assigning weights

- Assign a weight, w_{ij}, to each edge
- $\bullet \quad \chi^2_{ij} = (M_{\gamma,i \gamma,j} M_{\pi})^2 / M_{\pi}$
- $W_{ij} = 1 \chi^2_{ij} / \chi^2_{max}$
- $\chi^2_{\text{max}} = \text{max}(\chi^2_{ij})$
- w_{ij} ∈ [0,1]



Comments on solution

- black dots = photons that do not originate from a π⁰ decay
- Hard cut on 'structure'
 may reduce to
 substantially the fraction
 of wrong photon pairing
 from photons not from
 π⁰ decays ("spare
 photons")

