

# Design of the FCC-ee Beam Polarimeter

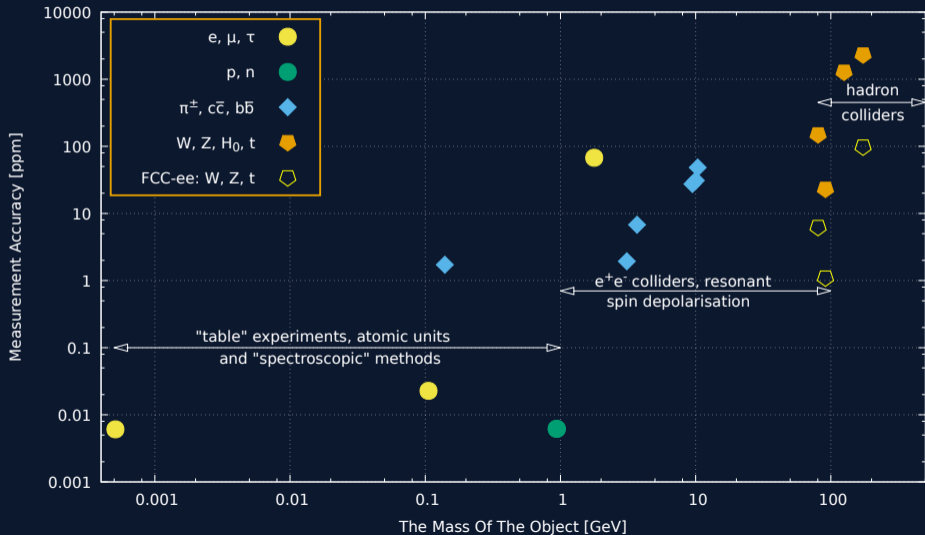
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## 4th FCC Physics and Experiments workshop

The Future Circular Collider Innovation Study (FCCIS) project has received funding from the European Union's Horizon 2020 research and innovation programme under grant No 951754.

# Who Weighs How Much

<http://pdglive.lbl.gov>



# $e^-e^+$ colliders

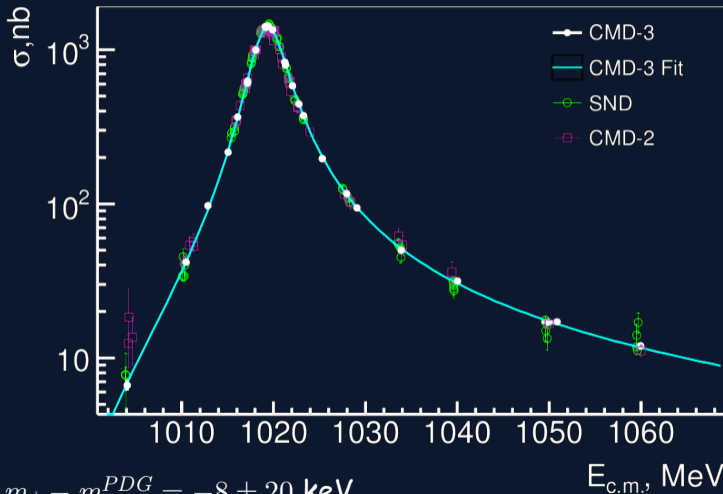
The center-of-masses energy in collision of electron with energy  $E_{e^-}$  and positron with energy  $E_{e^+}$  at crossing angle  $\theta$ :

$$E_{\text{cm}} = \sqrt{2E_{e^+}E_{e^-} + 2m^2c^4 - 2\cos\theta\sqrt{E_{e^+}^2 - m^2c^4}\sqrt{E_{e^-}^2 - m^2c^4}}$$

Roughly, for a collider with  $\theta = \pi$  the average collision energy is:

$$\langle E_{\text{cm}} \rangle \simeq 2\sqrt{\langle E_{e^+} \rangle \langle E_{e^-} \rangle}$$

# $e^+e^- \rightarrow K_S K_L$ at VEPP-2000 (2013)



# Electron charge and Lorentz force

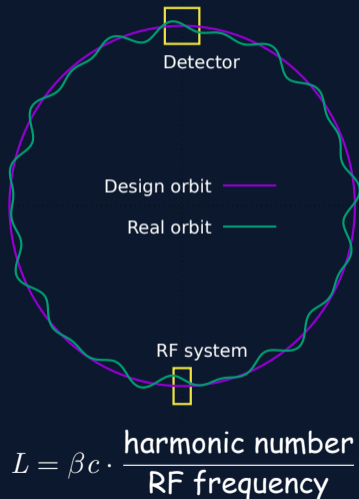
Consider electron with energy  $E$  and velocity  $v = \beta/c$ . In a field  $B_{\perp}$  instant bent angle  $d\alpha$  per arc length  $dl$  is

$$d\alpha = \frac{ec}{\beta} \frac{B_{\perp}}{E} dl$$

The closed orbit condition:

$$\int_0^{2\pi} d\alpha = 2\pi = \frac{ec}{\beta E} \int_0^L B_{\perp}(l) dl$$

The beam energy:  $\beta E = \frac{ec}{2\pi} \int_0^L B_{\perp}(l) dl$



$\int B_{\perp}(l) dl$  along the close orbit is known with accuracy  $\gtrsim 0.1\%$ .

# Bargmann-Michel-Telegdi equation

Besides Lorentz force  $B_{\perp}$  exerts a torque on the electron magnetic dipole moment and turns it in lab frame to the angle:

$$d\varphi = \frac{ec}{\beta} \frac{B_{\perp}}{E} \left(1 + \gamma \frac{\mu'}{\mu_0}\right) dl = \left(1 + \gamma \frac{\mu'}{\mu_0}\right) d\alpha, \quad \text{where } \gamma = \frac{E}{mc^2}.$$

The ratio of the anomalous and normal parts of electron magnetic moment:

$$\frac{\mu'}{\mu_0} = \frac{g-2}{2} = 0.00115965218091 \pm 0.000000000000026 \quad (\text{PDG 2020})$$

Electron spin rotation is  $\left(1 + \gamma \frac{\mu'}{\mu_0}\right)$  times faster than its own rotation.

$B_{\perp}(l)$  does not affect  $\frac{d\varphi}{d\alpha}$ : this ratio only depends on electron  $\gamma$ -factor

# Resonant Depolarization (RD)

- ▶  $\Omega$  - spin precession frequency
- ▶  $\omega$  - beam revolution frequency

$$\frac{d\varphi}{d\alpha} = \frac{\Omega}{\omega} = 1 + \gamma \frac{\mu'}{\mu_0}$$

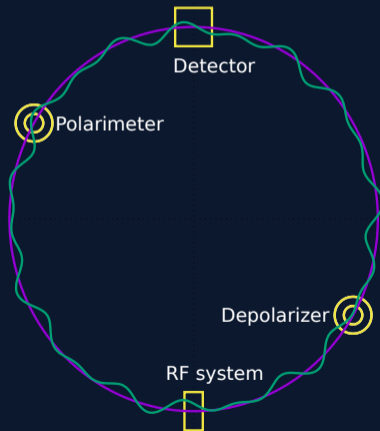
The  $\Omega/\omega$  ratio could be measured with accuracy better than 0.01 ppm.

RD approach requires:

- ▶ polarized beam,
- ▶ polarimeter & depolarizer.

Accuracy limitations ( $\Delta E_{cm}/E_{cm} \simeq 1$  ppm):

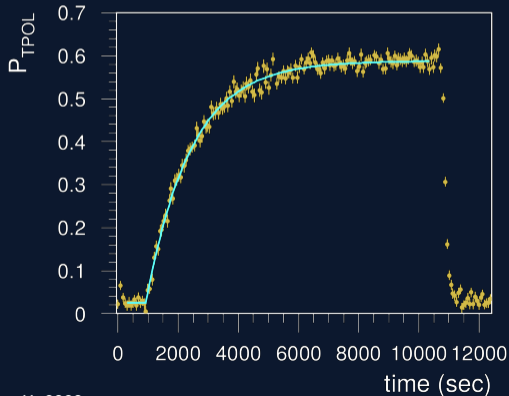
- ▶ rare measurements - interpolation,
- ▶ non-flat orbit -  $B_{\parallel}$  affects  $\Omega$ ,
- ▶  $E_{\text{beam}}(\text{i.p.}) \neq \langle E_{\text{beam}} \rangle$ ,
- ▶ collision angle uncertainty, etc.



# RD Examples

HERA electron beam ( $E=27.6$  GeV)  
polarization build-up by the  
Sokolov-Ternov effect

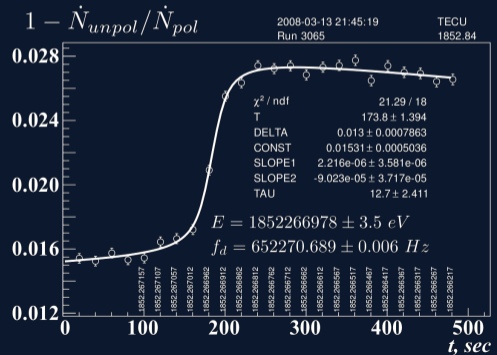
26 June 2007



November 11, 2020

Slow  $e^-$  beam resonant depolarization  
at the VEPP-4M collider,  $E=1.852$  GeV

13 March 2008





# Excerpts from FCC-ee CDR

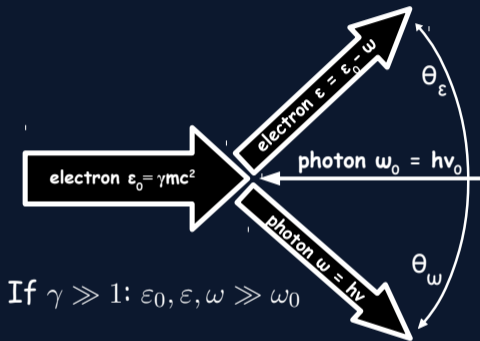
- ▶ Beam energy calibration by Resonant Depolarization is the basis for the precise measurements of the  $Z$  and  $W$  masses with a precision of  $\sim 100$  keV and  $\sim 500$  keV correspondingly.
- ▶ About 200 polarized pilot bunches/ring will not collide - just used for frequent beam energy measurements by RD.
- ▶ It is impossible to use RD at higher beam energies since the increased energy spread make the spin resonances too strong, reducing the asymptotic polarization to an unacceptably small value.
- ▶  $E_{\text{cm}}$  near the  $e^+e^- \rightarrow t\bar{t}$  threshold will be measured by the final state reconstruction of  $e^+e^- \rightarrow W^+W^-, ZZ, Z\gamma$  events and from the knowledge of the  $W$  and  $Z$  masses.

# Polarimeters on the Compton Effect

- ▶ Fast measurement of beam polarization is required for precise beam energy determination by RD.
- ▶ Positive experience at high beam energies - LEP, HERA, SLD.
- ▶ Known recipes: analyze scattered photons for transverse beam polarization, for longitudinal - use scattered electrons.

Inverse Compton scattering is used for direct beam energy calibration at low-energy  $e^\pm$  colliders: VEPP-4M, BEPC-II, VEPP-2000.

# Inverse Compton Scattering



If  $\gamma \gg 1$ :  $\epsilon_0, \epsilon, \omega \gg \omega_0$

Scattering parameter

$$u = \frac{\omega}{\epsilon} = \frac{\theta_\epsilon}{\theta_\omega} = \frac{\omega}{\epsilon_0 - \omega} = \frac{\epsilon_0 - \epsilon}{\epsilon}$$

is in the range

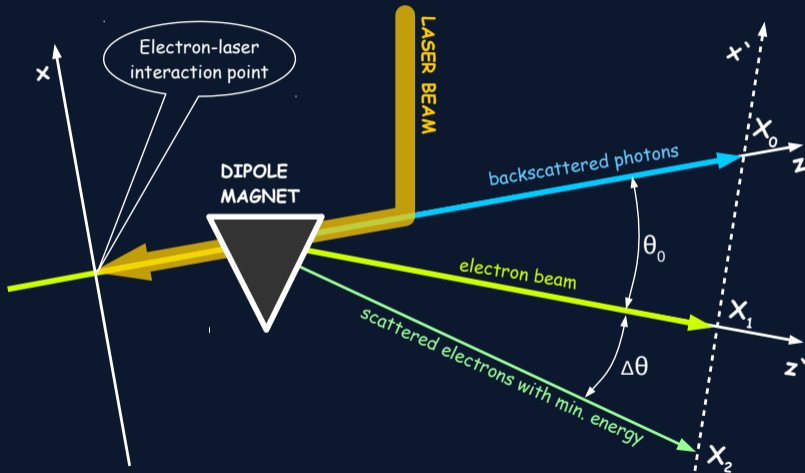
$$u \in [0, \kappa], \text{ where } \kappa = \frac{4\omega_0\epsilon_0}{(mc^2)^2}$$

$\kappa \simeq 1.53$  if  $\epsilon_0 = 100 \text{ GeV}$  &  $\omega_0 = 1 \text{ eV}$

$$\text{Scattering angles: } \theta_\omega = \frac{1}{\gamma} \sqrt{\frac{\kappa}{u} - 1}; \quad \theta_\epsilon = \frac{u}{\gamma} \sqrt{\frac{\kappa}{u} - 1}.$$

**Note:**  $\max(\theta_\epsilon) = 2\omega_0/mc^2$  (when  $u = \kappa/2$ ). It is  $\simeq 10 \mu\text{rad}$  for green light.

# Generic configuration: x-z plane



# Scattered electrons

The energy  $\varepsilon$  of scattered electron is:

$$\varepsilon = \frac{\varepsilon_0}{1+u} \rightarrow \min(\varepsilon) = \frac{\varepsilon_0}{1+\kappa}$$

Electron bending angle is defined by  $B = ec \int B_{\perp}(l) dl$ :

$$\theta_{\max} \equiv \frac{B}{\min(\varepsilon)} = \frac{B}{\varepsilon_0} + \kappa \frac{B}{\varepsilon_0} = \frac{B}{\varepsilon_0} + \frac{4\omega_0 B}{(mc^2)^2} = \theta_0 + \Delta\theta$$

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Maximum angles of scattered electrons:

scattering:  $\max(\theta_{\varepsilon}) = \frac{2\omega_0}{mc^2}$

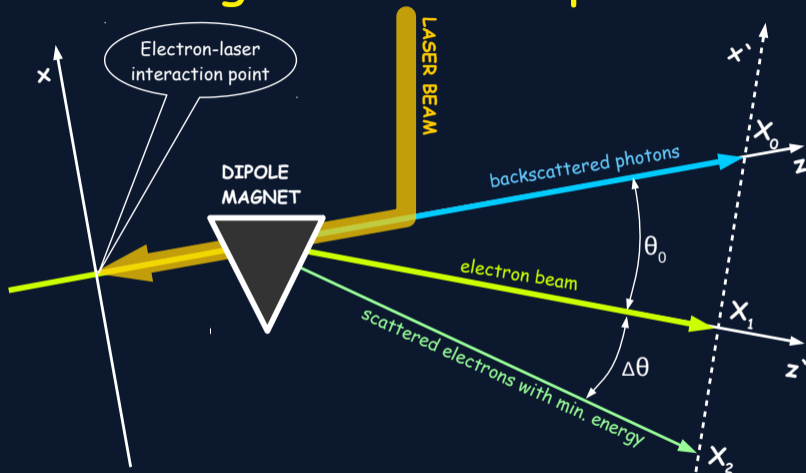
bending:  $\Delta\theta = \frac{2\omega_0}{mc^2} \cdot \frac{2B}{mc^2}$

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Hence  $\gamma = \frac{mc^2}{4\omega_0} \cdot \frac{\Delta\theta}{\theta_0}$

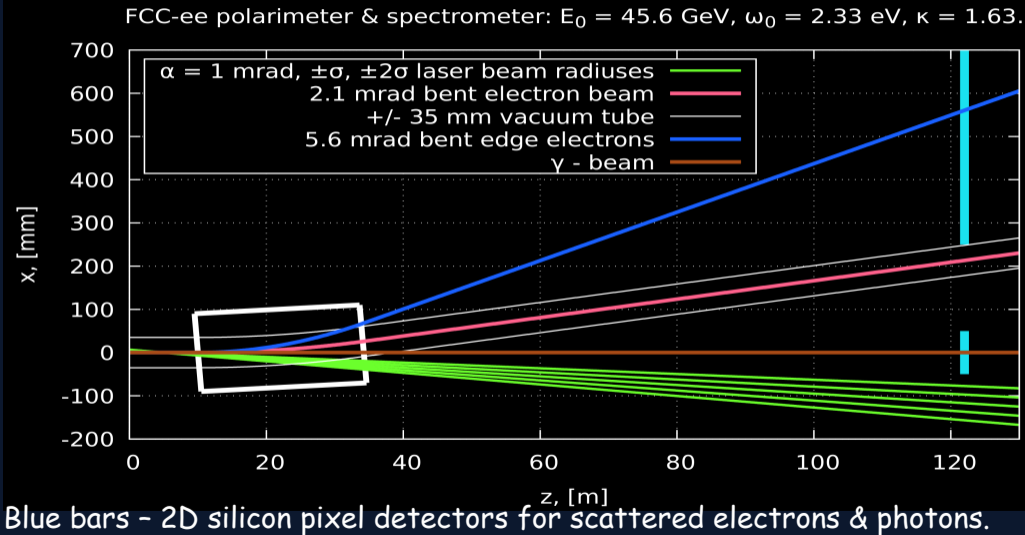
$\int B_{\perp}(l) dl$  does not affect  $\frac{\Delta\theta}{\theta_0}$

# Generic configuration: x-z plane

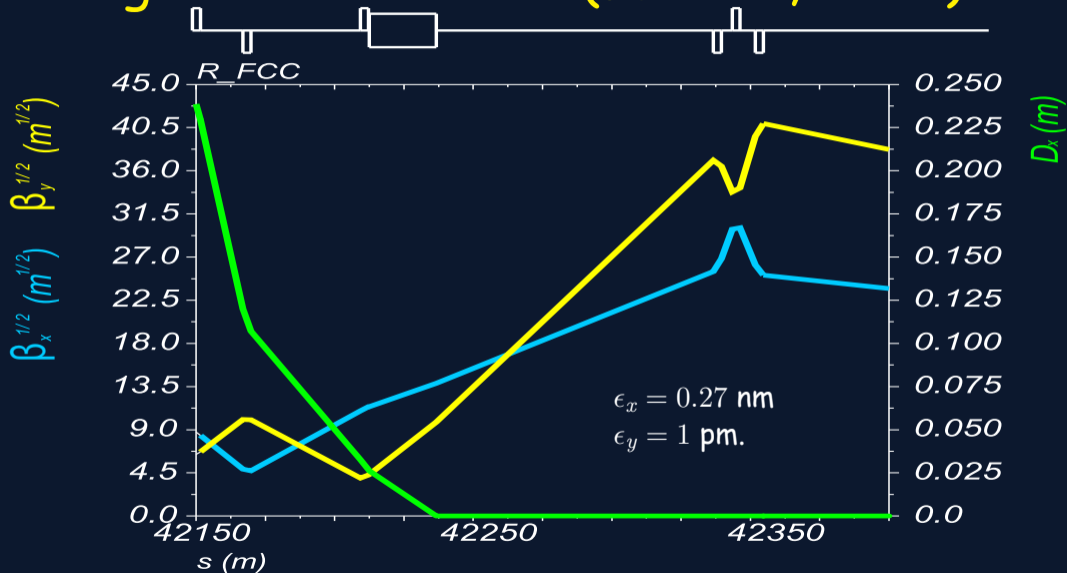


Since  $\Delta\theta = \kappa\theta_0$  direct beam energy calibration is possible:  $E = \frac{(mc^2)^2}{4\omega_0} \cdot \frac{\Delta\theta}{\theta_0}$

# FCC-ee polarimeter: x-z plane

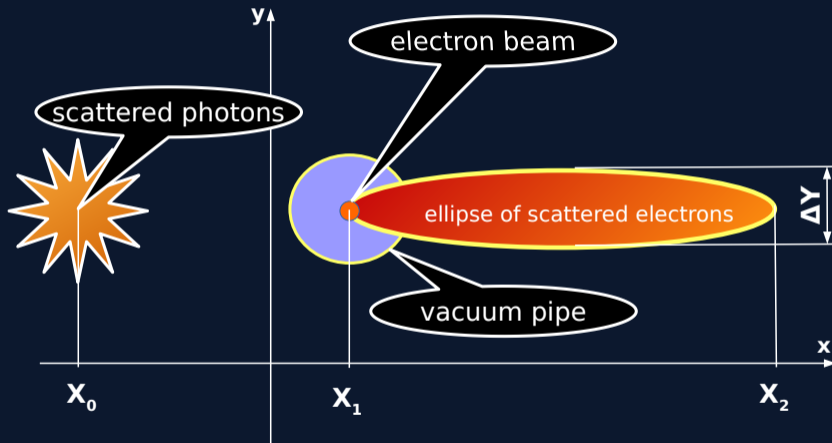


# Integration to lattice (K. Oide, 2018)





# The Polarimeter: $x'$ - $y'$ plane



Direct beam energy measurement is: 
$$E = \frac{(mc^2)^2}{4\omega_0} \cdot \frac{X_2 - X_1}{X_1 - X_0}$$

# Si pixel detector for scattered electrons

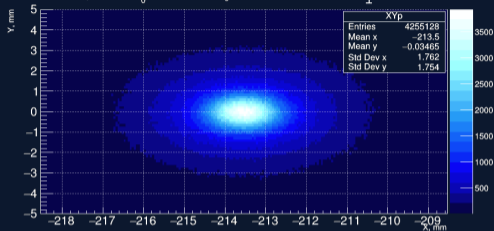
- ▶ Detector size:  $L_x = 400 \text{ mm}, L_y = 4 \text{ mm}$
- ▶ Number of pixels:  $N_x = 400, N_y = 80$
- ▶ Pixel size:  $S_x = 1 \text{ mm}, S_y = 50 \mu\text{m}$

The similar setup have been studied in ILC note LC-M-2012-001:

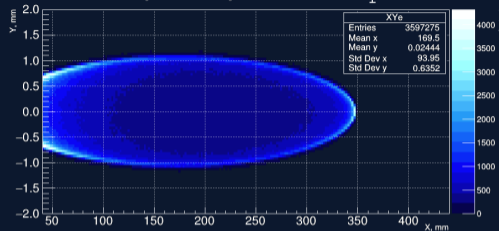
"A Transverse Polarimeter for a Linear Collider of 250 GeV e Beam Energy"

# Scattered $\gamma$ & $e$ : $\xi_{\parallel}\zeta_{\perp} = +0.25$

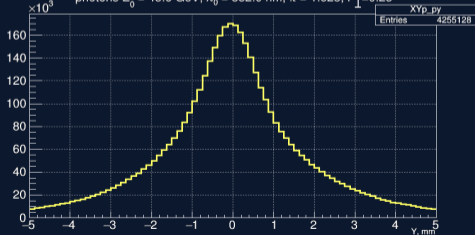
photons  $E_0 = 45.6$  GeV,  $\lambda_0 = 532.0$  nm,  $\kappa = 1.628$ ,  $P_{\perp} = 0.25$



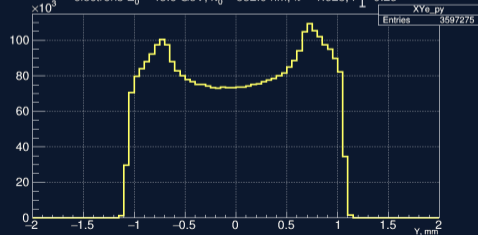
electrons  $E_0 = 45.6$  GeV,  $\lambda_0 = 532.0$  nm,  $\kappa = 1.628$ ,  $P_{\perp} = 0.25$



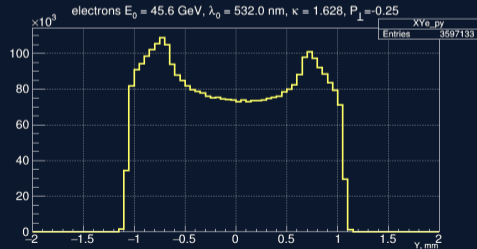
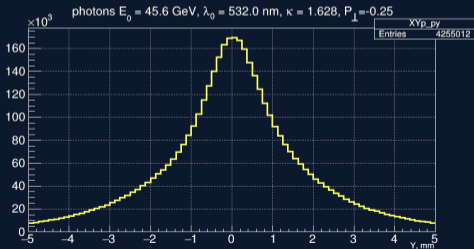
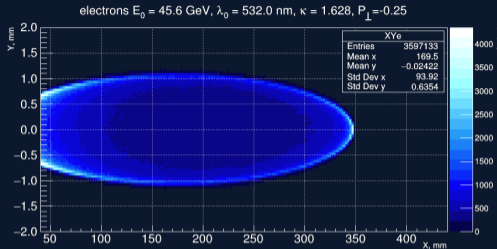
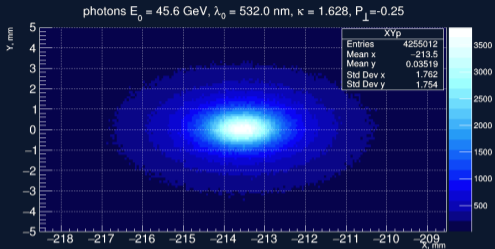
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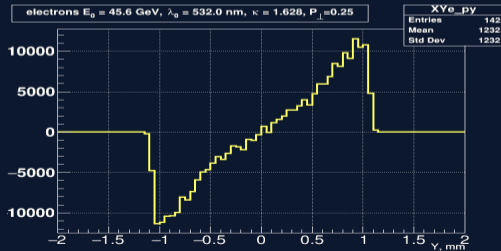
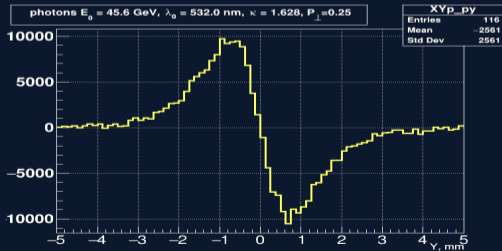
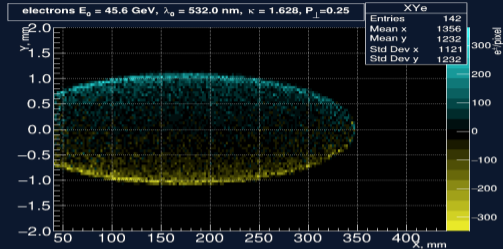
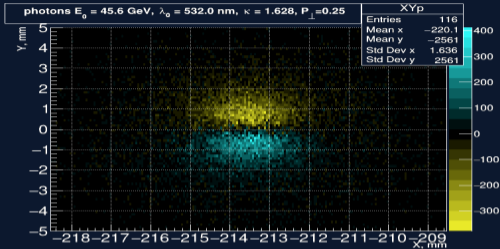
electrons  $E_0 = 45.6$  GeV,  $\lambda_0 = 532.0$  nm,  $\kappa = 1.628$ ,  $P_{\perp} = 0.25$



# Scattered $\gamma$ & $e$ : $\xi_{\parallel} \zeta_{\perp} = -0.25$



# Scattered $\gamma$ & $e$ : The Difference



# Polarimetry with electrons

- ▶ Maximum polarization asymmetry  $d\sigma_{\perp}$  is observed at the angles

$$\theta_y^{\gamma} = \pm mc^2 / E_{\text{beam}} \text{ for photons - doesn't depend on } \omega_0;$$

$$\theta_y^e = \pm 2\omega_0 / mc^2 \text{ for electrons - doesn't depend on } E_{\text{beam}}.$$

- ▶ Scattered electrons propagate to the inner side of the beam orbit: there is no direct background from high energy SR photons.
- ▶ Electrons are ready to be detected by their ionization losses while  $\gamma$ 's need to be converted to  $e^+e^-$  pairs: this leads either to low detection efficiency either to low spatial resolution.
- ▶ The flux density of electrons is much lower due to bending and corresponding spatial separation by energies. Simultaneous detection of multiple scattered electrons is thus much easier.
- ▶ Analysis of the scattered electrons distribution allows to measure the longitudinal beam polarization as well as the transverse one.

# Compton Scattering cross section

for circular polarization of light  $\xi_{\circ} = \pm 1$  depends on both longitudinal  $\zeta_{\circ}$  and transverse  $\zeta_{\perp}$  polarizations of the electron:

$$d\sigma_0 = \frac{r_e^2}{\kappa^2(1+u)^3} \left( \kappa(1+(1+u)^2) - 4\frac{u}{\kappa}(1+u)(\kappa-u) \right) du d\varphi,$$

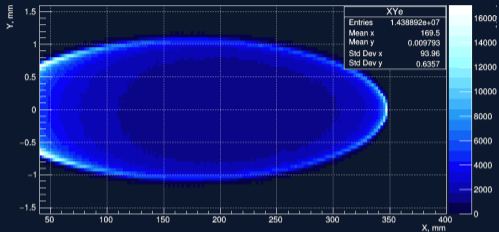
$$d\sigma_{\parallel} = \frac{\xi_{\circ}\zeta_{\circ}r_e^2}{\kappa^2(1+u)^3} u(u+2)(\kappa-2u) du d\varphi,$$

$$d\sigma_{\perp} = -\frac{\xi_{\circ}\zeta_{\perp}r_e^2}{\kappa^2(1+u)^3} 2u\sqrt{u(\kappa-u)} \cos(\varphi - \phi_{\perp}) du d\varphi.$$

For vertical electron (beam) polarization  $\phi_{\perp} = \pi/2$

# Fit: cross section & emittance

electrons  $E_0 = 45.6$  GeV,  $\lambda_0 = 532.0$  nm,  $\kappa = 1.628$ ,  $P_{\perp} = 0.10$



$\chi^2/\text{NDF} = 6356.7/6129$  | Prob = 0.0208

$X_0 = -213.538 \pm 0.000$  mm

$X_1 = -000.008 \pm 0.010$  mm

$X_2 = 0347.631 \pm 0.003$  mm

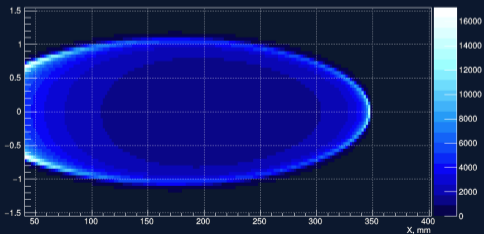
$\sigma_x = 194.8 \pm 4.4$   $\mu\text{m}$

$\sigma_y = 23.69 \pm 0.02$   $\mu\text{m}$

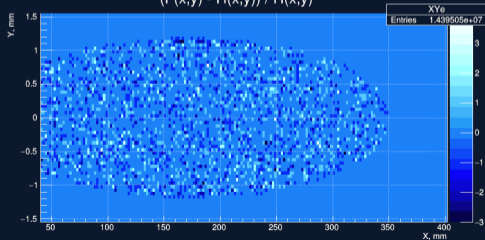
$E_{\text{beam}} = 45.6032 \pm 0.0035$  GeV.

$P_{\perp} = 0.0997 \pm 0.0016$

$F(x,y)$



$(F(x,y) - H(x,y)) / H(x,y)^{1/2}$





# Laser parameters

- ▶  $\lambda_0 = 532 \text{ nm}$ , waist  $\sigma_0 = 0.25 \text{ mm}$ ,  $z_R = 148 \text{ cm}$ , divergence  $\theta = 0.169 \text{ mrad}$ .
- ▶ Interaction angle  $\alpha = 1.0 \text{ mrad}$  (horizontal crossing).
- ▶ Laser pulse:  $E_L = 1 \text{ mJ}$ ,  $\tau_L = 5 \text{ ns}$ ,  $f = 3 \text{ kHz}$ ,  $P_L = 80 \text{ kW}$ ,  $\langle P_L \rangle = 3 \text{ W}$ .
- ▶ Beam electron energy  $E_{beam} = 45.6 \text{ GeV}$ , cross section  $R_\times \simeq 50\%$ .
- ▶ Scattering probability  $W = P_L/P_c \cdot R_\times \cdot \eta(R_L, R_A) \simeq 7 \cdot 10^{-8}$ .
- ▶  $N_e = 10^{10} \text{ e}^\pm/\text{bunch}$ :  $\dot{N}_\gamma = f \cdot N_e \cdot W \simeq 2 \cdot 10^6 \text{ s}^{-1}$ .

# Summary

- ▶ Detecting both scattered photons & electrons increases the reliability of beam polarization measurement.
- ▶ FCC-ee polarimeter provides  $\simeq 1\%$  / s accuracy for  $\zeta_{\perp}$ .
- ▶ The beam energy spectrometer option:
  - ▶ statistical accuracy  $\Delta E/E \simeq 100$  ppm / 10 sec;
  - ▶ systematic effects estimation requires further studies & simulations: yet no limitations;
  - ▶ possesses high accuracy in beam sizes & positions determination.
- ▶ The test of the approach is possible and highly desirable.  
The only mandatory requirement for a test electron beam is:

$$\sqrt{\frac{\varepsilon_y}{\beta_y}} < \sqrt{\frac{2\omega_0}{mc^2}} \simeq 10 \text{ urad}$$