

How to measure  
Virtual particles?

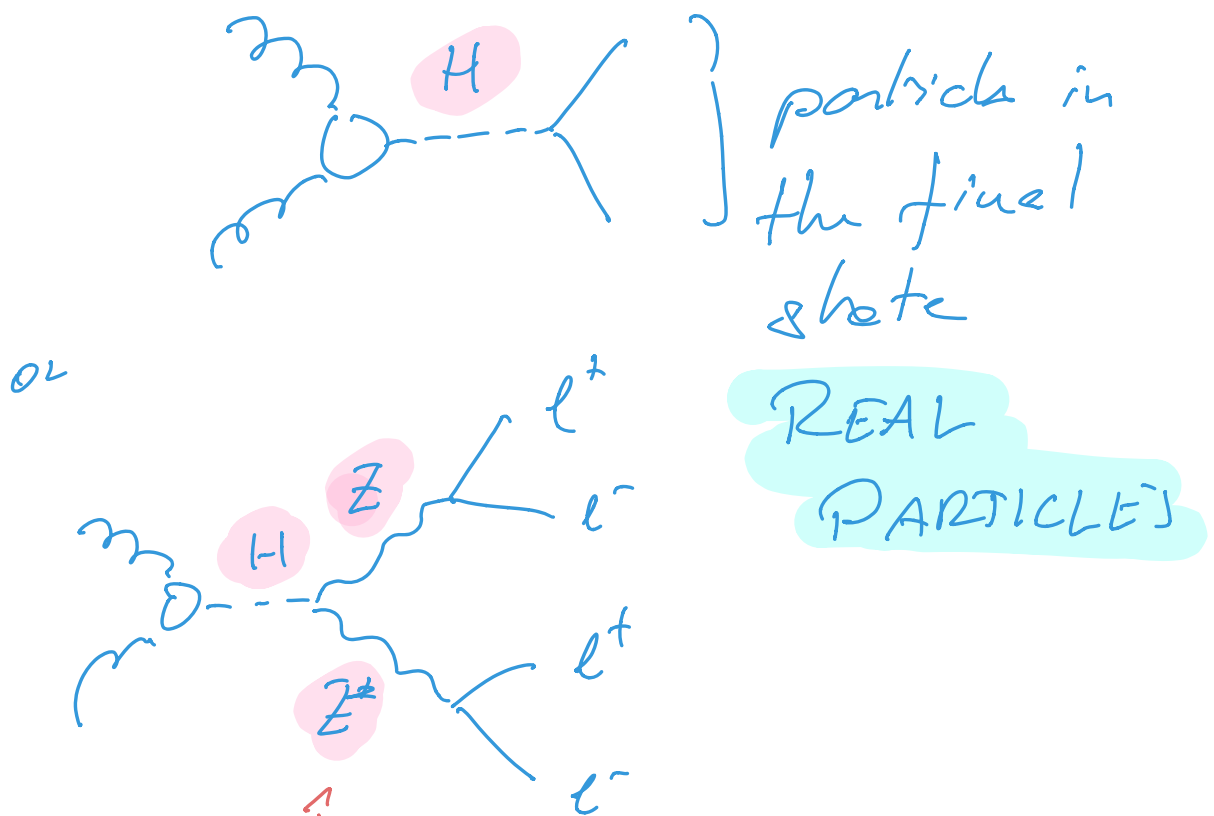
Intrinsically Quantum Mechanical  
question.

Quantum Mechanical Particle:

$$\Psi(\vec{r}, t) = \Psi(\vec{r}) e^{\frac{iEt}{\hbar}}$$

This is for a free particle

How about particles  
appearing in interactions?



particles in  
the final  
state

REAL  
PARTICLES

↑ Particles that are  
intermediates in the interaction.

CAN BE CALLED VIRTUAL

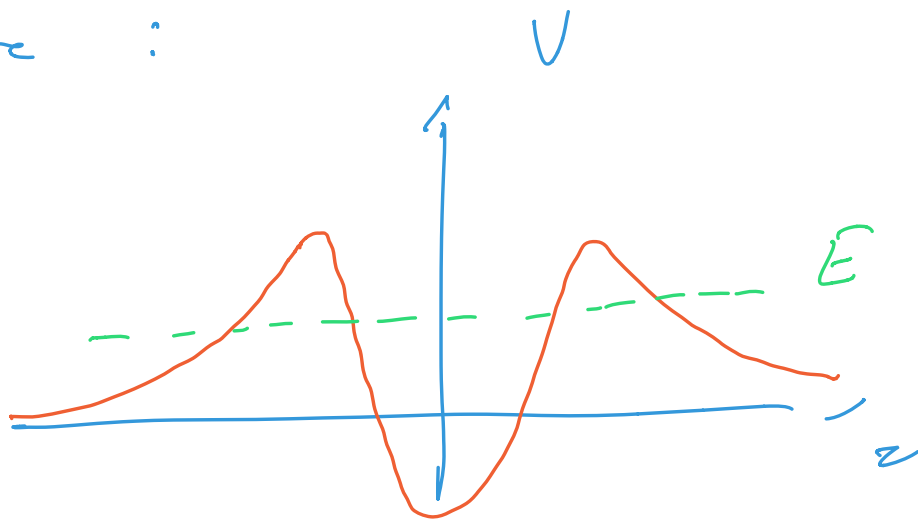
Taking a closer look  
at virtual particles, i.e.  
particles that appear  
as intermediate - can  
be viewed as solutions  
of a damped oscillator,  
which can also produce  
resonance when excited  
with the right energy -

As a damped oscillator

$$E \rightarrow E - i \frac{\Gamma}{2}$$

Just add a complex  
term to the energy-

How this can be  
achieved in QM is  
to consider a scattering  
with a metastable  
state :



(for details see  
scattering theory) ~

$$\text{Over } E - i\frac{\Gamma}{2}$$

Then the probability  
to find the particle

will be:

$$|\Psi(\vec{x}, t)|^2 = |\Psi(\vec{x})|^2 e^{-\frac{\Gamma t}{\hbar}}$$

Now if we compare  
this to a statistical

decay law when the probability for a decay is constant:

$$N(t) = N_0 e^{-\frac{t}{\tau}}$$

↑  
mean lifetime.

Then  $\frac{P}{h} = \frac{1}{\tau}$

i.e.  $\boxed{P \cdot \tau = h}$

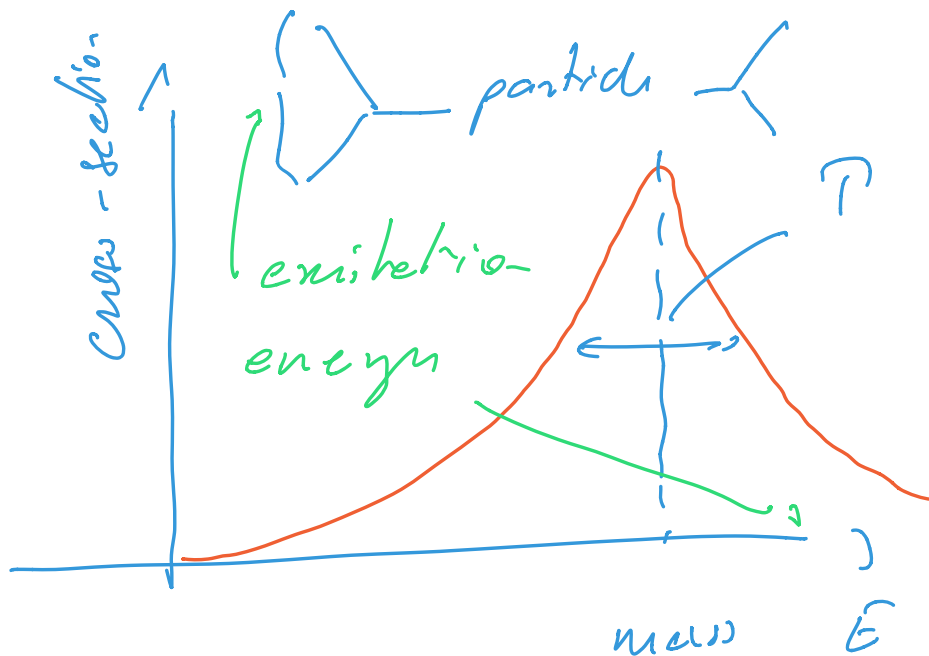
$\Delta E$   
Variation  
in energy

$\Delta t$   
Variation  
in time -

$\Gamma \rightarrow$  is the total width

$\tau \rightarrow$  Particle lifetime

$\Gamma$  corresponds to the width of a resonance



Exchange of virtual particles far from their mass has a cost on the rate but is very possible.

That is what happens in the case when the Higgs boson decays rapidly ( $1.6 \times 10^{-22}$  s)



In which case we study the decay products and infer the properties -

or when the  $Z^*$  is off-mass shell -

In both cases the particle only appears

as a VIRTUAL PARTICLE

There is a more  
shadowy domain where  
the decay width is  
extremely small, and therefore  
the decay lifetime is  
very long e.g. muons,  
or protons (many more) -

These particles can be  
interpreted as  $n$  real particles  
decaying -

A word about energy  
conservation - Indeed  
in the case of a  $\Delta E$   
there is no energy conserved.  
This is the basis of the  
Heisenberg Principle - <sup>(more</sup>  
<sub>(next page)</sub>

However for the modification  
of the wavefunction. This  
is done in QM Scattering  
theory just with the potential  
defined above!

The concept is splendid  
as it allows to interpret  
forces not as resulting  
from an "ACTION AT A  
DISTANCE" but by the  
exchange of a particle!

This overall does not  
violate energy conservation,  
but it is rather borrowed  
for a short interval -